

$$p_0^{\pi}(s) = v_0(s)$$

$$v^{\pi}(s) = (1-\gamma) \sum_{t=0}^{\infty} \gamma^t p_t^{\pi}(s) \quad \leftarrow \text{状态访问分布}$$

state visitation dist.

$$S = \{s_1, s_2, \dots, s_n\}$$

$$\begin{aligned} \sum_{i=1}^n v^{\pi}(s_i) &= (1-\gamma) \sum_{i=1}^n \sum_{t=0}^{\infty} \gamma^t p_t^{\pi}(s_i) \\ &= (1-\gamma) \sum_{t=0}^{\infty} \gamma^t \boxed{\sum_{i=1}^n p_t^{\pi}(s_i)} = 1 \\ &= (1-\gamma) \sum_{t=0}^{\infty} \gamma^t \\ &= (1-\gamma) \cdot \frac{1}{1-\gamma} = 1 \end{aligned}$$

$$\sum_{s \in S} v^{\pi}(s) = 1$$

$$\rho^{\pi}(s, a) = (1-\gamma) \sum_{t=0}^{\infty} \gamma^t p_t^{\pi}(s) r(a|s) \quad \leftarrow \text{占用度量}$$

$$\text{对比 } v^{\pi}(s) = (1-\gamma) \sum_{t=0}^{\infty} \gamma^t p_t^{\pi}(s) \quad \text{occupancy measure}$$

存在关系

$$\rho^{\pi}(s, a) = v^{\pi}(s) r(a|s)$$