

Idiosyncrasies

Vladimir Feinberg

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1 Notation

Landau notation is used in the standard sense for single variables: $f = O(g)$ if there exists a c such that $f(x) \leq cg(x)$ for all x sufficiently large, with x perhaps restricted to the support of g as required by the context. We use the analogous sense for $\Omega, \Theta, o, \omega$.

In multiple variables, big- O and friends require $f(\mathbf{x}) \leq cg(\mathbf{x})$ and similar inequalities, respectively, for all \mathbf{x} in the support for the current context with $\|\mathbf{x}\|_\infty$ sufficiently large. To capture the essence of asymptotics, a tilde will crudely absorb behavior up to logarithmic factors: $f = \tilde{O}(g)$ if $f = O(g \log^k g)$ for some $k \in \mathbb{N}$ and possibly multivariate function g .

When some iterative process is clear, such as \mathbf{x}_t arising from iterative optimization of an objective f , then the gradient will be abbreviated $\nabla_t = \nabla f(\mathbf{x}_t)$. Similarly we use $H_t = \nabla^2 f(\mathbf{x}_t)$.

2 Abbreviations

- iid: independent and identically distributed
- rv: random variable
- wp: with probability
- wrt: with respect to
- wlog: without loss of generality