# W271 Section 3 Lab 1

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```
knitr::opts_chunk$set(cache=TRUE)
library(knitr)
opts_chunk$set(tidy.opts=list(width.cutoff=60),tidy=TRUE)
```

# Problem statement

In this lab, we are going to model the relationship between age and voters' preference for Bernie Sanders over Hillary Clinton.

#### **Dataset**

## dt ##

The dataset comes from the 2016 American National Election Survey.

```
library(dplyr)
library(ggplot2)
library(Hmisc)
library(GGally)
library(data.table)
library(stargazer)
if (dir.exists("/Users/daghanaltas/Hacking/Berkeley/W271/Labs/w271_lab1/")) {
    setwd("/Users/daghan/Hacking/Berkeley/W271/Labs/w271_lab1/")
} else if (dir.exists("/Users/daghan/Hacking/Berkeley/W271/Labs/w271_lab1/")) {
    setwd("/Users/daghan/Hacking/Berkeley/W271/Labs/w271_lab1/")
} else {
    setwd("~/Desktop/w271/Lab1")
}
df <- read.csv("./public_opinion.csv")</pre>
dt <- data.table(df)</pre>
head(dt)
##
      sanders_preference party race_white gender birthyr
## 1:
                              1
                                         1
                        0
                                         1
                                                 2
                                                      1957
## 2:
                              3
## 3:
                        1
                                         1
                                                1
                                                      1963
## 4:
                       1
                              1
                                         1
                                                 1
                                                      1980
## 5:
                       1
                              2
                                         1
                                                 1
                                                      1974
## 6:
                                         1
                                                      1958
describe(dt)
```

```
1200 Observations
   5 Variables
##
##
  sanders_preference
##
         n missing distinct
                                        Sum
                               Info
                                                 Mean
                                                          Gmd
##
                 9
                               0.733
                                         686
                                                0.576
                                                       0.4889
##
##
         n missing distinct
##
                              Info
                                        Mean
                                                  Gmd
            0 3
                               0.875
##
      1200
                                       1.851
                                               0.8309
##
                      2
                          3
## Value
                1
               459
## Frequency
                    461
                          280
## Proportion 0.382 0.384 0.233
  race_white
##
                               Info
                                         Sum
         n missing distinct
                                                 Mean
                                                          Gmd
##
                 0 2
                               0.592
                                         875
                                               0.7292
                                                        0.3953
##
##
## gender
         n missing distinct
##
                              Info
                                        Mean
                                                  Gmd
                0
                               0.748
                                       1.525
##
      1200
                                               0.4992
##
## Value
                1
## Frequency
               570
                    630
## Proportion 0.475 0.525
## birthyr
##
         n missing distinct Info Mean
                                                \operatorname{\mathsf{Gmd}}
                                                         .05
                                                                  .10
                                1
##
      1200
               0
                        73
                                        1968
                                                19.53
                                                         1940
                                                                  1946
       .25
##
                .50
                        .75
                                 .90
                                        .95
##
      1955
               1968
                      1982
                                1991
                                        1994
##
## lowest : 1921 1924 1925 1926 1927, highest: 1993 1994 1995 1996 1997
```

# Description of the data

The dataset contains 5 variables with 1200 samples:

- sanders\_preference: A categorical variable with 2 levels, denoting whether the voter prefers Bernie Sanders (=1) or Hillary Clinton (=0).
- party: A categorical variable with 3 levels, denoting whether the voter prefers is affiliated with the Democratic Party (=1), Independent (=2), or Republican Party (=3).
- race\_white: A categorical variable with 2 levels, denoting wheter the voter is White (=1), or not (=0).
- gender: A categorical variable with 2 levels, denoting whether the voter is male (=1), or female (=2).
- birthyr: A numerical variable, denoting the birthyear of the voter.

#### **Observations:**

• There are 9 missing values (NAs) for the **sanders\_preference** variable.

- There is no direct age variable. We'll derive it from the birthyr variable.
- None of the other variables have missing values.

## Clean-up

dim(dt)

##

## 1:

## 2:

MeanAge 49.89

47.04

dtage <- 2015 - dt\$birthyr

• We are going to create a new variable, age based on the birthyr variable through the following formula:

$$age = 2015 - birthyr$$

We will use 2015, as the data was collected in 2016, since we are interested in the age of the voters **when** the data was collected. (All people born in 2015 will be counted as age=1, but this is only true if the survey was taken on 12/31/2016; suppose the survey was taken on 01/01/2016, then none of the people born in 2015 actually reached age 1, they are all actually age 0 when being surveyed, in this case "age = 2015 - birthyr" is the correct formula. We don't know when the survey was taken, but by changing the calculation to "age = 2015 - birthyr", the minimum age is 18 now)

• We'll convert all categorical variables to R factor variables.

• We are going to remove the 9 observations without the **sanders\_preference** value. A possible way to impute these **NA** values could be to use a logistic regression but for this work, we'll simply opt to remove these observations (9 out of 1200 observations is less than 1% of the data), especially given that the other values for each observation are close to the mean of their respective columns. A table of the NA observations are detailed below:

```
dt missing = dt[is.na(sanders preference)]
dt notmissing = dt[!is.na(sanders preference)]
table = data.table(Data = c("NA's", "Remaining Data"), PartyDem = c(round(nrow(dt_missing[party ==
    "D"])/nrow(dt_missing), 2), round(nrow(dt_notmissing[party ==
    "D"])/nrow(dt_notmissing), 2)), PartyInd = c(round(nrow(dt_missing[party ==
    "I"])/nrow(dt_missing), 2), round(nrow(dt_notmissing[party ==
    "I"])/nrow(dt notmissing), 2)), PartyRep = c(round(nrow(dt missing[party ==
    "R"])/nrow(dt_missing), 2), round(nrow(dt_notmissing[party ==
    "R"])/nrow(dt_notmissing), 2)), Race_white = c(round(nrow(dt_missing[race_white ==
    1])/nrow(dt_missing), 2), round(nrow(dt_notmissing[race_white ==
    1])/nrow(dt_notmissing), 2)), GenderFemale = c(round(nrow(dt_missing[gender ==
    "F"])/nrow(dt_missing), 2), round(nrow(dt_notmissing[gender ==
    "F"])/nrow(dt_notmissing), 2)), MeanAge = c(round(dt_missing[,
   mean(age)], 2), round(dt_notmissing[, mean(age)], 2)))
table
##
                Data PartyDem PartyInd PartyRep Race_white GenderFemale
                         0.44
                                  0.33
                                           0.22
                                                      0.67
## 1:
                NA's
                                                                    0.89
## 2: Remaining Data
                         0.38
                                  0.38
                                           0.23
                                                       0.73
                                                                    0.52
```

```
dt <- dt[!is.na(dt$sanders_preference), ]</pre>
```

We observe that 8 out of 9 NAs are female and this could be problematic. However, i) given that gender is not a meaningful explonatory variable for preference\_bernie (see relevant section below in univariate analysis) and ii) the relatively low number of data points with missing values (9 out of 1200), and iii) that all other variables deviate very little between the NAs subset and the rest of the data, we can justify our decision to remove NA subset from the original dataset.

# **Explotary Data Analysis**

## Univariate analysis

Sanders vs. Hillary Preference

## Count Bernie Hillary Total ## Voter Count 686.00 505.00 1191 ## pi.hat 0.58 0.42 1

In this survey, 58% of voters prefer Hillary over Bernie. While there is a larger than expected Bernie preference (since Hillary Clinton won the Democratic nomiation, one would expect to see a higher ratio for Clinton than Bernie), there isn't a substantial tilt in one direction or the other. One possible explanation is that Bernie is more popular among the Independents and Republicans. So we are going to assume that this sample does not exhibit a meaningful selection bias (sample set is random).

#### Party affiliations

## Count

```
c.table <- array(data = c(sum(dt$party == "D"), sum(dt$party ==
    "D")/length(dt$party), sum(dt$party == "I"), sum(dt$party ==
    "I")/length(dt$party), sum(dt$party == "R"), sum(dt$party ==
    "R")/length(dt$party), sum((dt$party == "D") | (dt$party ==
    "I") | (dt$party == "R")), sum((dt$party == "D") | (dt$party ==
    "I") | (dt$party == "R"))/length(dt$party)), dim = c(2, 4),
    dimnames = list(Count = c("Voter Count", "pi.hat"), Party_affiliation = c("Democrat",
        "Independent", "Republican", "Total")))

round(c.table, 2)</pre>
## Party affiliation
```

Democrat Independent Republican Total

```
## Voter Count 455.00 458.00 278.00 1191 ## pi.hat 0.38 0.38 0.23 1
```

We observe that 38% of the voters in the dataset are affiliated with the Democratic Party, whereas only 23% are affiliated with the Republican Party. The 0.6 Democratic to Republican ratio is noteworthy. The data appears to be skewed towards Democratic voters (perhaps a specific region of the country). Our model may not be applicable to the entire country. A further analysis of how the dataset was sampled from the entire population would be very useful.

#### Race

```
c.table <- array(data = c(sum(dt$race_white == 1), sum(dt$race_white ==
    1)/length(dt$race_white), sum(dt$race_white == 0), sum(dt$race_white ==
    0)/length(dt$race_white), sum((dt$race_white == 1) | (dt$race_white ==
    0)), sum((dt$race_white == 1) | (dt$race_white == 0))/length(dt$race_white)),
    dim = c(2, 3), dimnames = list(Count = c("Voter Count", "pi.hat"),
        Race = c("White", "Non White", "Total")))

round(c.table, 2)</pre>
```

```
## Race
## Count White Non White Total
## Voter Count 869.00 322.00 1191
## pi.hat 0.73 0.27 1
```

The 73% white / non-white ratio is inline with the overall US population (according to the 2016 US Census, whites made up 72.4% of the population). The dataset does not appear to have a selection bias with respect to the voter race

#### Gender

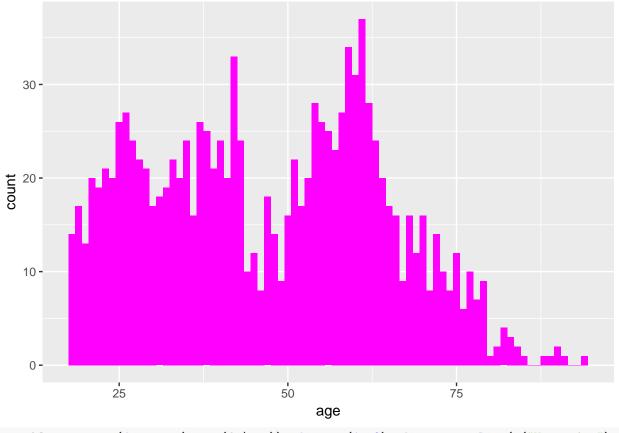
```
c.table <- array(data = c(sum(dt$gender == "M"), sum(dt$gender ==
    "M")/length(dt$gender), sum(dt$gender == "F"), sum(dt$gender ==
    "F")/length(dt$gender), sum((dt$gender == "M") | (dt$gender ==
    "F")), sum((dt$gender == "M") | (dt$gender == "F"))/length(dt$gender)),
    dim = c(2, 3), dimnames = list(Count = c("Voter Count", "pi.hat"),
        Gender = c("Male", "Female", "Total")))</pre>
round(c.table, 2)
```

```
## Gender
## Count Male Female Total
## Voter Count 569.00 622.00 1191
## pi.hat 0.48 0.52 1
```

The female / male ration is 1.10 on the dataset and the population ratio (according to Wikipedia) is 1.05. So the sample data doesn't appear to have a meaningful skew.

#### Age

```
ggplot(dt, aes(age)) + geom_histogram(binwidth = 1, fill = "magenta")
```



```
## Youngest Oldest
## Voter Age 18 94
```

We observe that age data for the voters in the survey is within the norms (i.e, there is no one below 18) an as expected, as the age variable moves beyond 70, there is a rapid decline. However the data appears to be tri-model. There is not an obvious explanation for that either. This may point to a selection bias (i.e, the sample isn't trully random). We'll note the shortcoming in our final analysis as a caution.

# Multivariate analysis

At this section, we are going to focus on the relationship between the outcome (sanders\_preference) and possible explanatory variables including:

- preference vs. party
- preference vs. race
- preference vs. gender

## preference vs. party

```
c.tabs <- xtabs(~sanders_preference + party, data = dt)
c.tabs <- rbind(c.tabs, colSums(c.tabs))</pre>
```

```
c.tabs <- cbind(c.tabs, rowSums(c.tabs))</pre>
c.table <- array(data = as.array(c.tabs), dim = c(3, 4), dimnames = list(Preference = c("Hillary",</pre>
    "Bernie", "Total"), Party = c("Democratic", "Independent",
    "Republican", "Total")))
round(c.table, 2)
##
             Party
## Preference Democratic Independent Republican Total
##
                      249
                                   156
                                              100
                                                     505
      Hillary
      Bernie
                      206
                                              178
                                                     686
##
                                   302
##
      Total
                      455
                                   458
                                              278
                                                   1191
round(c.table/dim(dt)[1], 2)
##
             Party
##
  Preference Democratic Independent Republican Total
                                 0.13
##
      Hillary
                     0.21
                                             0.08 0.42
                                 0.25
##
      Bernie
                     0.17
                                             0.15 0.58
##
      Total
                     0.38
                                 0.38
                                             0.23 1.00
chisq.test(c.tabs)
##
   Pearson's Chi-squared test
##
##
## data: c.tabs
## X-squared = 46.046, df = 6, p-value = 2.898e-08
```

We have further proof that Bernie is popular with the wrong group (i.e, Independents and Republicans), which is a point we touched on the univariate analysis section for the preference variable. While he enjoys roughly 2x the popularity of Hillary Clinton among the Independents and Republicans, he is less popular among the Democrats. Our intution to include party affiliation as an explanatory variable is backed by the Chi-Square independence test. Witht the p-value close to 0, we can accept the alternative hypothesis that party and preference\_bernie are dependent and therefore **party variable should be added to the model.** 

#### preference vs. race white

```
c.tabs <- xtabs(~sanders_preference + race_white, data = dt)</pre>
c.tabs <- rbind(c.tabs, colSums(c.tabs))</pre>
c.tabs <- cbind(c.tabs, rowSums(c.tabs))</pre>
c.table <- array(data = as.array(c.tabs), dim = c(3, 3), dimnames = list(Preference = c("Hillary",</pre>
    "Bernie", "Total"), Race = c("Non whites", "Whites", "Total")))
round(c.table, 2)
##
              Race
## Preference Non whites Whites Total
##
      Hillary
                       190
                              315
                                     505
##
                              554
                                     686
      Bernie
                       132
##
      Total
                       322
                              869
                                   1191
```

```
round(c.table/dim(dt)[1], 2)
##
             Race
## Preference Non whites Whites Total
##
      Hillary
                    0.16
                           0.26 0.42
                    0.11
##
      Bernie
                           0.47 0.58
##
      Total
                    0.27
                           0.73 1.00
chisq.test(c.tabs)
##
##
   Pearson's Chi-squared test
##
## data: c.tabs
## X-squared = 49.823, df = 4, p-value = 3.932e-10
```

Bernie enjoys 4 times more support from White voters than Non-White voters. This is definitely a strong signal for our model, not to mention the very very low p-value for the Chi-square independence test, so there is strong empirical evidence to accept the alternative hypothesis that race and bernie\_preference are not independent. We will add race as a dependent variable to our model.

#### preference vs. gender

```
t <- table(dt[, .(Gender = ifelse(gender == "F", "Female", "Male"),
    Preference = ifelse(sanders_preference == 1, "Sanders", "Hillary"))])
##
           Preference
## Gender
            Hillary Sanders
                263
##
    Female
                        359
    Male
                242
                         327
##
round(t/sum(t), 2)
##
           Preference
            Hillary Sanders
## Gender
     Female
               0.22
##
                       0.30
               0.20
                        0.27
##
     Male
chisq.test(t)
##
##
   Pearson's Chi-squared test with Yates' continuity correction
##
## X-squared = 0.00076975, df = 1, p-value = 0.9779
```

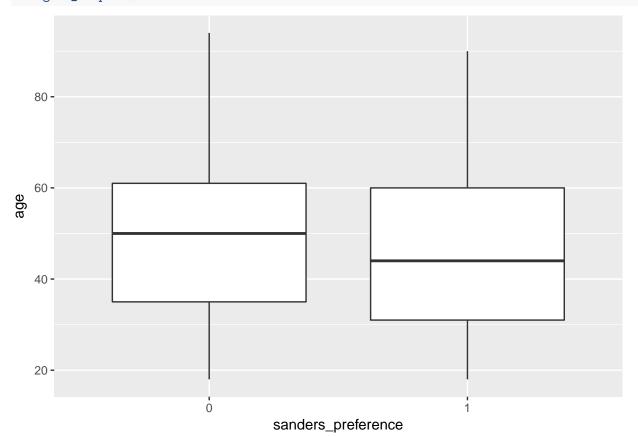
Both males and females are more likely to prefer Sanders. But the ratio is nearly identical:  $P(prefers\_sanders|female) = \frac{0.27}{0.47} = 0.58$  and  $P(prefers\_sanders|male) = \frac{0.30}{0.52} = 0.58$ . Our intuition is further backed by the very high p-value for indepence test. We can't reject the null hypothesis that the gender and preference\\_sanders are independent. So we will not include gender in our model.

# Preference vs. age

```
dt[, .(age, Preference = ifelse(sanders_preference == 1, "Sanders",
    "Hillary"))][, .(`Mean Age` = mean(age)), by = Preference] # Average age of those who prefer Sande

## Preference Mean Age
## 1: Sanders 46.11953
## 2: Hillary 48.29307

ggplot(dt, aes(x = sanders_preference, y = age, group = sanders_preference)) +
    geom boxplot()
```

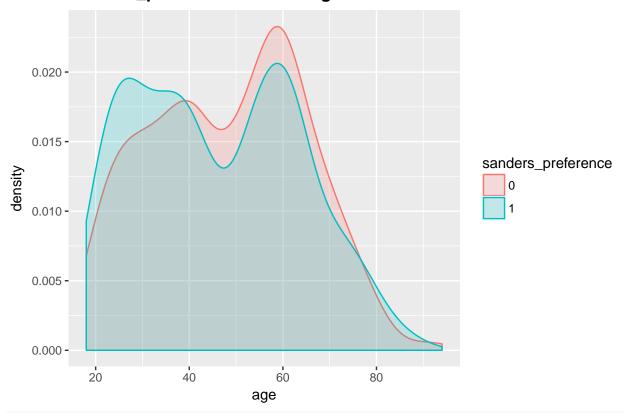


Looking at the boxplot, it is clear that mean age for people who prefer Bernie Sanders is younger, but not that much. Also the 1st quartile is lower, but also not that much. So the boxplot doesn't provide a strong visual evidence for either adding or excluding the age as an explanatory variable.

We are going to plot a frequency polygon for age conditioned on sanders\_preference to have a closer look.

```
ggplot(dt, aes(age, fill = sanders_preference, color = sanders_preference)) +
    geom_density(alpha = 0.2) + ggtitle("Sanders_preference for each age") +
    theme(plot.title = element_text(lineheight = 1, face = "bold"))
```

# Sanders\_preference for each age



#### t.test(dt\$age ~ dt\$sanders\_preference)

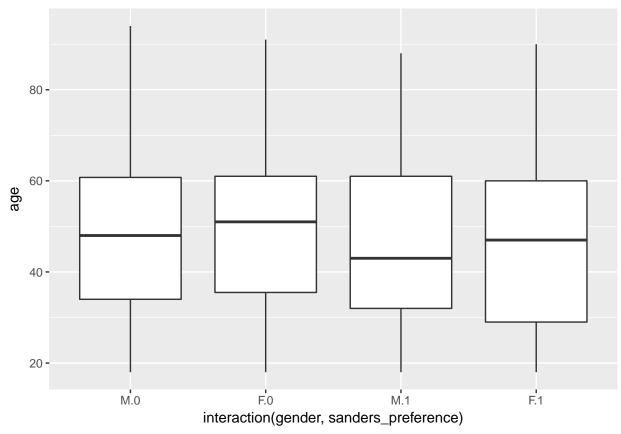
```
##
## Welch Two Sample t-test
##
## data: dt$age by dt$sanders_preference
## t = 2.1991, df = 1116.5, p-value = 0.02808
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.2342468 4.1128247
## sample estimates:
## mean in group 0 mean in group 1
## 48.29307 46.11953
```

The frequency polygon indicates that there is a clear difference in favor of Bernie Sanders for voters below the age of 40 and somewhat of a reverse effect for the voters above the age of 40. Also the t-test shows that there is reasonable evidence to reject to null hypothesis and accept that the mean age of voters who prefer Bernie Sanders is younger than those who prefer Hillary Clinton. We will include age in our model.

## Interactions

preference ~ age & gender

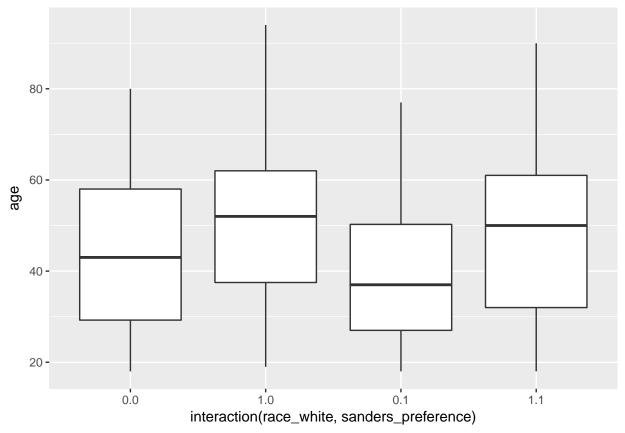
```
ggplot(dt, aes(x = interaction(gender, sanders_preference), y = age)) +
    geom_boxplot()
```



There is a mild interaction between age, gender and sanders\_preference (males who prefer Sanders have the lowest mean age). We remain skeptical that there is evidence of an interaction between age and gender variables as an explanatory variable for the model. However, we'll conduct a model test in the next section.

# preference ~ age & race\_white

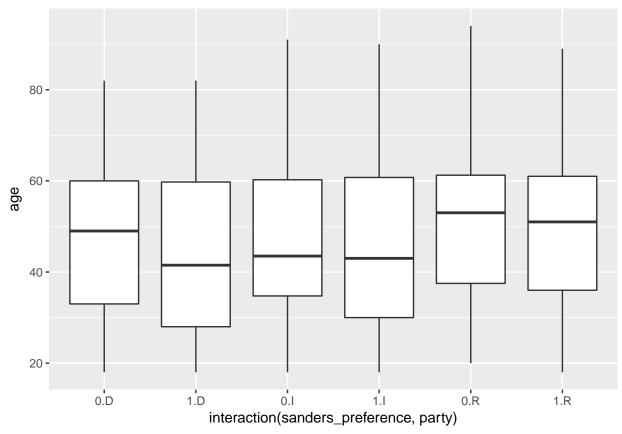
```
ggplot(dt, aes(x = interaction(race_white, sanders_preference),
    y = age)) + geom_boxplot()
```



Non-white voters who prefer Bernie arex the youngest group (based on their 1st, 3rd quartile and mean age). We'll explore the interaction between age and race during our model exploration.

# preference $\sim$ age & party

```
ggplot(dt, aes(x = interaction(sanders_preference, party), y = age)) +
    geom_boxplot()
```



For Republicans and Independents, the mean and 3rd quartiles for age don't change that much based on sanders\_preference. But 1st quartile for Independents as well as the mean age for Democrats changes noticeably based on sanders\_preference. We are going to explore the interaction between the age and party variables.

## Models

Based on the exploratory data analysis, our model exploration strategy is as follows:

- Investigate whether gender is a significant explanatory variable or not.
- Investigge that both party and race\_white are meaningful explanatory variables.
- Investigate additional interactions:
  - Interaction between age and race
  - Interaction between age and party
  - Interaction between party and race
  - Interaction between age and gender

# Is gender important?

Our exploratory analysis has indicated that there is no empirical evidence to include gender as an explanatory variable. For the sake of thoroughness, we'll conduct one final analysis.

#### **Null Hypothesis**

In our null hypothesis we are going to assume that  $\beta_{gender}=0$ 

```
model1.H0 = glm(sanders_preference ~ age, dt, family = binomial(link = "logit"))
summary(model1.H0)
##
## Call:
## glm(formula = sanders_preference ~ age, family = binomial(link = "logit"),
##
       data = dt)
##
## Deviance Residuals:
##
      Min
                10
                     Median
                                   3Q
                                           Max
## -1.4074 -1.2842 0.9841
                              1.0620
                                        1.1840
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
                           0.173958
                                    3.802 0.000144 ***
## (Intercept) 0.661384
              -0.007522
                           0.003457 -2.176 0.029566 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 1623.5 on 1190 degrees of freedom
## Residual deviance: 1618.7 on 1189 degrees of freedom
## AIC: 1622.7
##
## Number of Fisher Scoring iterations: 4
Alternative hypothesis
In the alternative hypothesis, we are going to assume that \beta_{gender} \neq 0
model1.Ha = glm(sanders_preference ~ age + gender, dt, family = binomial(link = "logit"))
summary(model1.Ha)
##
## Call:
## glm(formula = sanders_preference ~ age + gender, family = binomial(link = "logit"),
      data = dt)
##
##
## Deviance Residuals:
                    Median
      Min
                1Q
                                   3Q
                                           Max
## -1.4111 -1.2869 0.9838
                             1.0625
                                        1.1816
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 0.653207
                           0.183064
                                    3.568 0.000359 ***
               -0.007535
                           0.003458 -2.179 0.029346 *
## age
                                    0.143 0.886079
## genderF
               0.016857
                           0.117657
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 1623.5 on 1190 degrees of freedom
```

```
## Residual deviance: 1618.7 on 1188 degrees of freedom
## AIC: 1624.7
##
## Number of Fisher Scoring iterations: 4
```

#### Comparing H0 to Ha

```
anova(model1.H0, model1.Ha, test = "Chisq")

## Analysis of Deviance Table

## Model 1: sanders_preference ~ age

## Model 2: sanders_preference ~ age + gender

## Resid. Df Resid. Dev Df Deviance Pr(>Chi)

## 1 1189 1618.7

## 2 1188 1618.7 1 0.020525 0.8861
```

We've confirmed once again that there is no evidence supporting the alternative hypothesis that **gender** is an explanatory variable given that **age** is in the model. We fail to reject the null hypothesis that  $\beta_{qender} = 0$ .

# Adding race and party affiliation

We are now going to include race and party. To recap:

0.713501

0.594231

## race\_white1 0.872782

## partyI
## partyR

## ---

##

0.140368

0.162972

0.141872

## (Dispersion parameter for binomial family taken to be 1)

## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1

```
• Null hypothesis H_0:
       - logit(\pi_{preference\_sanders}) = \beta_0 + \beta_1 age
   • Alternative hypothesis H_a:
        - logit(\pi_{preference\_sanders}) = \beta_0 + \beta_1 age + \beta_2 partyI + \beta_3 partyR + \beta_4 race\_white
model3.H0 = glm(sanders_preference ~ age, dt, family = binomial(link = "logit"))
model3.Ha = glm(sanders_preference ~ age + party + race_white,
    dt, family = binomial(link = "logit"))
summary(model3.Ha)
##
## Call:
## glm(formula = sanders_preference ~ age + party + race_white,
##
       family = binomial(link = "logit"), data = dt)
##
  Deviance Residuals:
       Min
##
                   1Q
                        Median
                                       3Q
                                                Max
##
  -1.7036 -1.1792
                        0.7907
                                   0.9881
                                             1.6662
##
## Coefficients:
##
                  Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.139978
                              0.199715 -0.701 0.483374
                              0.003666 -3.404 0.000664 ***
## age
                -0.012480
```

5.083 3.71e-07 \*\*\*

3.646 0.000266 \*\*\*

6.152 7.66e-10 \*\*\*

```
##
##
      Null deviance: 1623.5 on 1190 degrees of freedom
## Residual deviance: 1533.2 on 1186 degrees of freedom
## AIC: 1543.2
## Number of Fisher Scoring iterations: 4
# Comparing HO and Ha
anova(model3.H0, model3.Ha, test = "Chisq")
## Analysis of Deviance Table
##
## Model 1: sanders_preference ~ age
## Model 2: sanders_preference ~ age + party + race_white
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
         1189
                  1618.7
## 2
         1186
                  1533.2 3
                              85.511 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The p-values for the party(I|R) and  $race\_white1$  explanatory variales are very low. In addition, the p-value for Ha (model3.Ha) is also very low. We conclude that there is strong empirical evidence for including race and party affilition in our model.

#### Exploring models with interactions

We are going to contruct 4 additional models to explore the interactions:

- Between race and age
- Between party and age
- Between party and race
- Between gender and age

```
model4.H0 = glm(sanders_preference ~ age + party + race_white,
    dt, family = binomial(link = "logit")) # also = H3.HA
model4.Ha1 = glm(sanders_preference ~ age + party + race_white +
    age:race_white, dt, family = binomial(link = "logit"))
model4.Ha2 = glm(sanders_preference ~ age + party + race_white +
    age:party, dt, family = binomial(link = "logit"))
model4.Ha3 = glm(sanders_preference ~ age + party + race_white +
    party:race_white, dt, family = binomial(link = "logit"))
model4.Ha4 = glm(sanders_preference ~ age + party + race_white +
    age:gender, dt, family = binomial(link = "logit"))
stargazer(model4.H0, model4.Ha1, model4.Ha2, model4.Ha3, model4.Ha4,
    type = "text", report = ("vc*p"))
```

```
##
                   0.714***
                               0.709***
                                           0.360
                                                   0.749***
## partyI
                                                              0.721***
##
                   p = 0.00000 p = 0.00000 p = 0.377 p = 0.004 p = 0.00000
##
##
  partyR
                    0.594***
                               0.587***
                                           0.151
                                                     0.574
##
                   p = 0.0003 p = 0.0004 p = 0.757 p = 0.121 p = 0.0003
                    0.873***
## race white1
                                 0.419
                                         0.874*** 0.888***
                                                              0.874***
##
                    p = 0.000
                               p = 0.297 p = 0.000 p = 0.00001 p = 0.000
##
## age:race_white1
                                 0.010
                               p = 0.229
##
##
                                           0.008
##
  age:partyI
##
                                         p = 0.354
##
                                           0.009
## age:partyR
##
                                         p = 0.329
##
## partyI:race white1
                                                    -0.051
##
                                                   p = 0.869
                                                     0.019
## partyR:race white1
                                                   p = 0.964
##
##
##
  age:genderF
                                                                0.001
##
                                                              p = 0.643
                               0.195
                                                    -0.150
## Constant
                     -0.140
                                         0.088
                                                              -0.141
                    p = 0.484 p = 0.569 p = 0.759 p = 0.497 p = 0.480
##
##
## Observations
                     1,191
                                1,191
                                           1,191
                                                     1,191
## Log Likelihood
                    -766.601
                               -765.868 -765.960
                                                              -766.493
                                                   -766.582
## Akaike Inf. Crit. 1,543.201 1,543.736 1,545.920 1,547.163
## Note:
                                               *p<0.1; **p<0.05; ***p<0.01
```

We observe that none of the alternative models have any new explanatory variable with a low p-value. We'll confirm our findings with a pairwise anova table  $H_0 vs. H_{a1}, H_0 vs. H_{a2}, H_0 vs. H_{a3}$ , and  $H_0 vs. H_{a4}$ 

```
model4.1.anova <- anova(model4.H0, model4.Ha1, test = "Chisq")
model4.2.anova <- anova(model4.H0, model4.Ha2, test = "Chisq")
model4.3.anova <- anova(model4.H0, model4.Ha3, test = "Chisq")
model4.4.anova <- anova(model4.H0, model4.Ha4, test = "Chisq")

model4.anova.results <- data.frame(c(model4.1.anova$`Pr(>Chi)`[2],
    model4.2.anova$`Pr(>Chi)`[2], model4.3.anova$`Pr(>Chi)`[2],
    model4.4.anova$`Pr(>Chi)`[2]))

colnames(model4.anova.results) <- "Pr(>Chi)"
rownames(model4.anova.results) <- c("model4.Ha1", "model4.Ha2",
    "model4.Ha3", "model4.Ha4")
model4.anova.results</pre>
```

```
## Pr(>Chi)
## model4.Ha1 0.2260354
## model4.Ha2 0.5269330
## model4.Ha3 0.9810663
## model4.Ha4 0.6423527
```

None of the 4 interaction models yields a test statistic satisfactory to reject the null hypothesis. There is no emprical evidence of any interaction between age and race, age and party, party and race, and age and gender.

#### Model selection conclusion

Based on our model study, we conclude that the most appropriate model for the specific question we want to answer (whether it is a good idea to focus on younger voters) given the dataset is:

```
\mathbf{logit}(\pi_{\mathbf{preference\_sanders}}) = \beta_0 + \beta_1 \mathbf{age} + \beta_2 \mathbf{partyI} + \beta_3 \mathbf{partyR} + \beta_4 \mathbf{race\_white}
```

## **Odds Ratios**

Based on our model, the estimated logit probability is

```
\mathbf{logit}(\hat{\pi}_{\mathbf{preference-sanders}}) = -0.1340 - 0.0125 age + 0.7135 party I + 0.5942 party R + 0.8728 race\_white
```

#### Odds Ratio for age

The estimated odds ratio for age is

$$\hat{OR}_{age} = exp(c\hat{\beta}_1)$$

With c = -10, we calculate the odds ratio and 95% intervals.

Odds ratio:

```
## 97.5 % 2.5 %
## 1.055 1.218
```

The Wald and LR intervals are similar.

With 95% confidence, the odds of preference for Sanders increases by an amount between 1.05 and 1.22 times for every 10-year decrease in the voter's age, holding other variables constant.

#### Odds Ratio for party

#### Odds Ratio for partyI

The estimated odds ratio for partyI is

$$\hat{OR}_{partyI} = exp(\hat{\beta}_2)$$

Odds ratio:

```
# Odds ratio for partyI
round(exp(1 * model4.H0$coefficients[3]), 3)
## partyI
## 2.041
95% Wald interval:
# Wald interval for the partyI odds ratio
beta.ci <- confint.default(object = model4.H0, parm = "partyI",</pre>
    level = 0.95)
round(exp(1 * beta.ci), 3)
##
          2.5 % 97.5 %
## partyI 1.55 2.688
95% LR interval:
# LR interval for the partyI odds ratio
beta.ci <- confint(object = model4.HO, parm = "partyI", level = 0.95)
## Waiting for profiling to be done...
round(exp(1 * beta.ci), 3)
   2.5 % 97.5 %
   1.551 2.690
```

The Wald and LR intervals are similar.

With 95% confidence, the odds of a voter preferring Sanders are between 1.55 to 2.69 times as large when the voter is an Independent than when the voter is a Democrat, holding other variables constant.

#### Odds Ratio for partyR

The estimated odds ratio for partyR is

$$\hat{OR}_{partyR} = exp(\hat{\beta}_3)$$

Odds ratio:

```
# Odds ratio for partyR
round(exp(1 * model4.H0$coefficients[4]), 3)
```

```
## partyR
## 1.812
95% Wald interval:
# Wald interval for the partyI odds ratio
beta.ci <- confint.default(object = model4.HO, parm = "partyR",
    level = 0.95)
round(exp(1 * beta.ci), 3)
          2.5 % 97.5 %
## partyR 1.316 2.493
95% LR interval:
# LR interval for the partyI odds ratio
beta.ci <- confint(object = model4.HO, parm = "partyR", level = 0.95)
## Waiting for profiling to be done...
round(exp(1 * beta.ci), 3)
## 2.5 % 97.5 %
## 1.318 2.498
The Wald and LR intervals are similar.
With 95% confidence, the odds of a voter preferring Sanders are between 1.32 to 2.49 times as large when the
voter is a Republican than when the voter is a Democrat, holding other variables constant.
Odds Ratio comparing Independent to Republican
The estimated odds ratio comparing partyI to partyR is
                                  \hat{OR}_{nartuIvspartuR} = exp(\hat{\beta}_2 - \hat{\beta}_3)
Odds ratio:
beta.hat <- model4.H0$coefficients[-1] # matches up beta indices with [i] to help avoid mistakes
```

 $K \leftarrow matrix(data = c(0, 0, 1, -1, 0), nrow = 1, ncol = 5, byrow = TRUE)$ 

```
linear.combo <- mcprofile(object = model4.HO, CM = K)
ci.log.OR <- confint(object = linear.combo, level = 0.95, adjust = "none")
round(exp(ci.log.OR$confint), 3)</pre>
```

```
## lower upper
## 1 0.818 1.549
```

The Wald and LR intervals are similar.

With 95% confidence, the odds of a voter preferring Sanders are between 0.82 to 1.55 times as large when the voter is an Independent than when the voter is a Republican, holding other variables constant. Because 1 is inside the interval, there is insufficient evidence to indicate the preference for Sanders is different for Independent voters compared to Republicant voters.

#### Odds Ratio for race\_white

The estimated odds ratio for race white is

$$\hat{OR}_{race\ white} = exp(\hat{\beta}_4)$$

Odds ratio:

```
# Odds ratio for race_white
round(exp(1 * model4.H0$coefficients[5]), 3)
## race white1
         2.394
##
95% Wald interval:
# Wald interval for the race_white odds ratio
beta.ci <- confint.default(object = model4.H0, parm = "race_white1",</pre>
    level = 0.95)
round(exp(1 * beta.ci), 3)
               2.5 % 97.5 %
## race white1 1.813 3.161
95% LR interval:
# LR interval for the race white odds ratio
beta.ci <- confint(object = model4.H0, parm = "race white1",
    level = 0.95)
## Waiting for profiling to be done...
round(exp(1 * beta.ci), 3)
## 2.5 % 97.5 %
## 1.814 3.165
```

The Wald and LR intervals are similar.

With 95% confidence, the odds of a voter preferring Sanders are between 1.81 to 3.16 times as large when the voter is white than when the voter is non-white, holding other variables constant.

# **Probability Plots**

```
#### the base model (for plotting all observations)
logit.mod.base <- glm(formula = sanders_preference ~ age, family = binomial(link = logit),</pre>
    data = dt
#### the full model (for plotting subgroups)
logit.mod.full <- glm(formula = sanders_preference ~ age + party +</pre>
    race_white, family = binomial(link = logit), data = dt)
#### function for calculating C.I.
# Wald confidence interval
wald.ci.pi <- function(newdata, mod.fit.obj, alpha) {</pre>
    linear.pred <- predict(object = mod.fit.obj, newdata = newdata,</pre>
        type = "link", se = TRUE)
    CI.lin.pred.lower <- linear.pred$fit - qnorm(p = 1 - alpha/2) *</pre>
        linear.pred$se # Wald interval
    CI.lin.pred.upper <- linear.pred$fit + qnorm(p = 1 - alpha/2) *</pre>
        linear.pred$se # Wald interval
    CI.pi.lower <- exp(CI.lin.pred.lower)/(1 + exp(CI.lin.pred.lower))</pre>
    CI.pi.upper <- exp(CI.lin.pred.upper)/(1 + exp(CI.lin.pred.upper))</pre>
    list(lower = CI.pi.lower, upper = CI.pi.upper)
```

#### Bubble plot of the base model for all observations

In this case, the data include all observations.

```
### aggregate the data by age for plotting observations
w <- aggregate(formula = as.numeric(dt$sanders_preference) -
        1 ~ dt$age, FUN = sum) # sanders supporters at each age
n <- aggregate(formula = as.numeric(dt$sanders_preference) ~
        dt$age, FUN = length) # total voters at each age

names(w)[1] <- "age"
names(w)[2] <- "preference"
names(n)[1] <- "age"
names(n)[2] <- "preference"

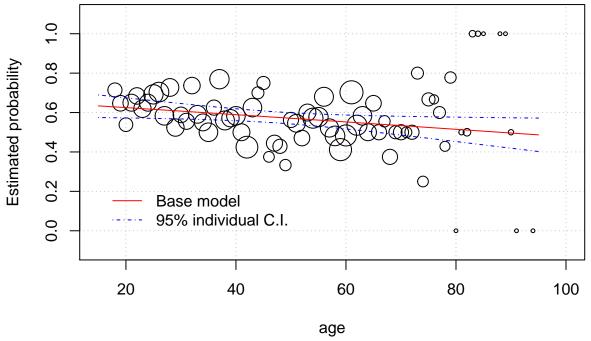
w.n <- data.frame(age = w$age, n = n$preference, w = w$preference,
        ratio = round(w$preference/n$preference, 4))
# head(w.n) # ratio = (sanders_supporters/total number of
# voters)</pre>
```

The estimated logistic model with the 95% Wald confidence intervals for the base model

$$logit(\pi_{preference\_sanders}) = \beta_0 + \beta_1 age$$

the bubble plot also shows the observed ratio of voters who prefer Sanders at each age, with the plotting size being proportional to the number of observations at that age.

```
# Plot data points
symbols(x = w$age, y = w$preference/n$preference, circles = sqrt(n$preference),
   inches = 0.12, xlab = "age", ylab = "Estimated probability",
   xlim = c(15, 100), panel.first = grid(col = "gray", lty = "dotted"))
# Plot model fit
curve(expr = predict(object = logit.mod.base, newdata = data.frame(age = x),
   type = "response"), col = "red", add = TRUE, xlim = c(15,
   95))
# Plot C.I. bands
curve(expr = wald.ci.pi(newdata = data.frame(age = x), mod.fit.obj = logit.mod.base,
   alpha = 0.05) $lower, col = "blue", lty = "dotdash", add = TRUE,
   xlim = c(15, 95)
curve(expr = wald.ci.pi(newdata = data.frame(age = x), mod.fit.obj = logit.mod.base,
   alpha = 0.05) *upper, col = "blue", lty = "dotdash", add = TRUE,
   xlim = c(15, 95)
# Legend
legend(x = 15, y = 0.25, legend = c("Base model", "95% individual C.I."),
   lty = c("solid", "dotdash"), col = c("red", "blue"), bty = "n")
```



The base model shows the preference for Sanders declines as the voter age increases.

## Comparing different voter groups using the full model

For comparing different groups of voters using the full model, we will plot the observed data points for the subgroup of voters each model represents with the estimated probability and 95% confidence intervals.

```
\mathbf{logit}(\pi_{\mathbf{preference\_sanders}}) = \beta_{\mathbf{0}} + \beta_{\mathbf{1}}\mathbf{age} + \beta_{\mathbf{2}}\mathbf{partyI} + \beta_{\mathbf{3}}\mathbf{partyR} + \beta_{\mathbf{4}}\mathbf{race\_white}
```

the *gender* factor has been excluded in our model, we will only include *party* and *race\_white* in the subgroup plotting function.

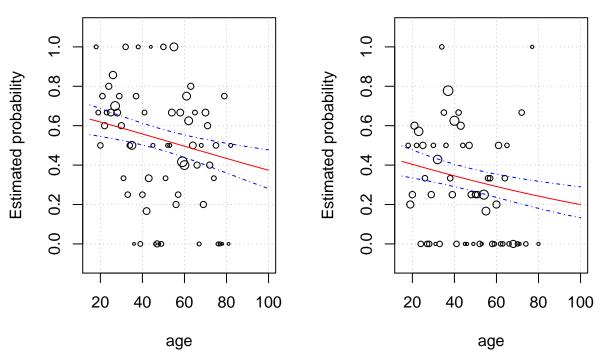
```
#### Define function plotsubgroup.pi.ci() for subgroup
#### probability plot
plotsubgroup.pi.ci <- function(newdata, mod.fit.obj, Party, Race) {</pre>
   party.G = Party
   race_white.G = Race
    # Strings for plot title
   if (Race == "1") {
       raceStr = "white"
   } else if (Race == "0") {
       raceStr = "non-white"
   } else {
       raceStr = " "
   }
   if (Party == "D") {
       partyStr = "Democratic"
   } else if (Party == "I") {
       partyStr = "Independent"
   } else if (Party == "R") {
       partyStr = "Republican"
   } else {
       partyStr = " "
   }
    # Creating subgroup data frame for the specified party and
   dt.G <- newdata[newdata$race_white == race_white.G & newdata$party ==</pre>
       party.G, ]
    # Creating aggregated data for plotting observations
    w.G <- aggregate(formula = as.numeric(dt.G$sanders preference) -
        1 ~ dt.G$age, FUN = sum) # sanders supporters for each age
   n.G <- aggregate(formula = as.numeric(dt.G$sanders_preference) ~</pre>
       dt.G$age, FUN = length) # total voters for each age
    # change to easy to understand column names
   names(w.G)[1] <- "age"</pre>
   names(w.G)[2] <- "preference"</pre>
   names(n.G)[1] <- "age"</pre>
   names(n.G)[2] <- "preference"</pre>
   w.n.G <- data.frame(age = w.G$age, n = n.G$preference, w = w.G$preference,
       ratio = round(w.G$preference/n.G$preference, 4))
```

```
# PLOT
# Plot data points
symbols(x = w.G$age, y = w.G$preference/n.G$preference, circles = sqrt(n.G$preference),
   inches = 0.05, xlab = "age", ylab = "Estimated probability",
   xlim = c(15, 100), panel.first = grid(col = "gray", lty = "dotted"),
   main = paste(partyStr, ":", raceStr))
# Plot model fit
curve(expr = predict(object = logit.mod.full, newdata = data.frame(age = x,
   party = party.G, race_white = race_white.G), type = "response"),
   col = "red", add = TRUE, xlim = c(15, 100), ylim = c(0, 100)
       1), xlab = "age", ylab = expression(hat(pi)))
# Plot C.I. bands
curve(expr = wald.ci.pi(newdata = data.frame(age = x, party = party.G,
   race_white = race_white.G), mod.fit.obj = logit.mod.full,
   alpha = 0.05) $lower, col = "blue", lty = "dotdash", add = TRUE,
   xlim = c(15, 100)
curve(expr = wald.ci.pi(newdata = data.frame(age = x, party = party.G,
   race_white = race_white.G), mod.fit.obj = logit.mod.full,
   alpha = 0.05) *upper, col = "blue", lty = "dotdash", add = TRUE,
   xlim = c(15, 100)
# legend(x=55, y=1.0, legend = c('model', '95\% C.I.'), lty =
\# c('solid', 'dotdash'), col = c('red', 'blue'), bty = 'n')
```

# Estimated probability of preferring sanders vs observations for different voter groups

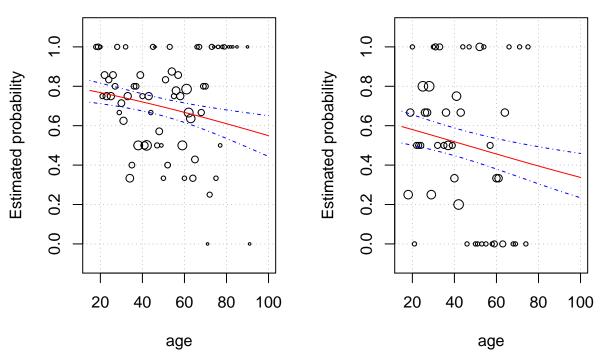
# **Democratic: white**

# Democratic: non-white



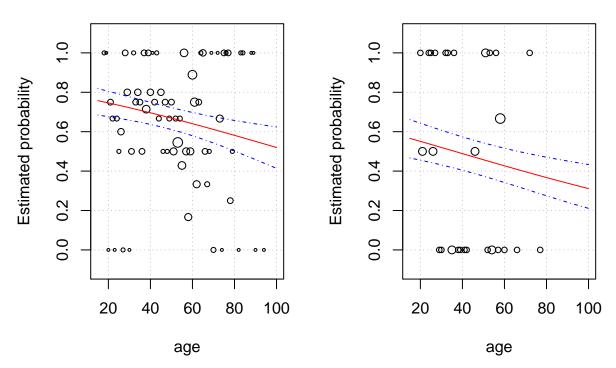
# Independent: white

# Independent : non-white



# Republican: white

# Republican: non-white



The estimated probability plots (the model prediction is shown in red, the 95% confidence intervals are shown by the dashed blue lines) based on our model show that the preference for Bernie Sanders was higher among the white voters than the non-white voters within each political party. In addition, Sanders enjoyed a similar level of support among the Independent and Republican voters, however, the preference for Sanders was lower among the Democratic voters compared to the Independent and Republican voters.

# Conclusion

Through our analysis, we have found that age is a statistically significant variable in predicting a preference for Sanders. Based on the sample, we find that 63% of voters under the age of 40 prefer Sanders, compared to 55% of voters 40 or older. In the broadest approach, this segmentation can be used for marketing purposes if the goal is to target the largest number of people.

Given we are lookig to market to a specific demographic, however, it would make sense to narrow the segment of voters in order to get the most return for our investment. In addition to age, we have found that race, and party preference are also statistically significant. The odds of a voter preferring Sanders are between 1.81 and 3.16 times (95% confidence) as large when the voter is white, 1.55 to 2.69 times as large when the voter identifies as a Republican. We note that it is unlikely that a Republican voter would purchase a Democratic candidate's T-shirt, and that the preference in the data is between two Democratic candidates, thus not validating the preference for Sanders over a Republican candidate.

With this additional information, we can refine our strategy to focus on younger (<40) white voters. Since we are trying to sell a product, we would recommend still targeting Democratic voters since they will likely have the highest chance of purchasing Democratic merchandise. We would also include Independents as they are between parties. In the same vein, we would recommend being cautious in targeting Republicans as they will be less likely to purchase Democratic merchandise.