

W271 Section 3 Lab 4

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```
knitr::opts_chunk$set(cache=TRUE)

library(easypackages)
packages("knitr","xts","forecast","ggfortify","ggplot2", "dplyr","plotly", "Hmisc",
         "tseries","stats","fpp", "forcats")
opts_chunk$set(tidy.opts=list(width.cutoff=60),tidy=TRUE)
rm(list=ls())
```

I. Introduction

II. Loading and cleaning up the data

We'll load the data and inspect the structure. We will also check to see if there are any missing values.

```
setwd("/Users/daghanaltas/Hacking/Berkeley/W271/Labs/w271_lab4")
df <- read.csv("./Lab4-series2.csv")
str(df)
```

```
## 'data.frame': 311 obs. of 2 variables:
## $ X: int 1 2 3 4 5 6 7 8 9 10 ...
## $ x: num 5.54 5.55 5.17 4.88 4.85 ...
```

```
cbind(head(df), tail(df))
```

```
##   X      x   X      x
## 1 1 5.544 306 5.240
## 2 2 5.555 307 5.546
## 3 3 5.172 308 5.078
## 4 4 4.878 309 4.907
## 5 5 4.851 310 4.599
## 6 6 4.686 311 4.681
```

```
sum(is.na(df)) # check if there is any NA
```

```
## [1] 0
```

There are no missing variables and the first column is the index column, which can be discarded. We are going to convert the data to a (xts) based time series

```
ms <- as.xts(ts(df$x, start = c(1990, 1), frequency = 12))
ms.training <- ms["/2014"]
ms.test <- ms["2015/"]
rbind(head(ms.training, 3), tail(ms.training, 3))
```

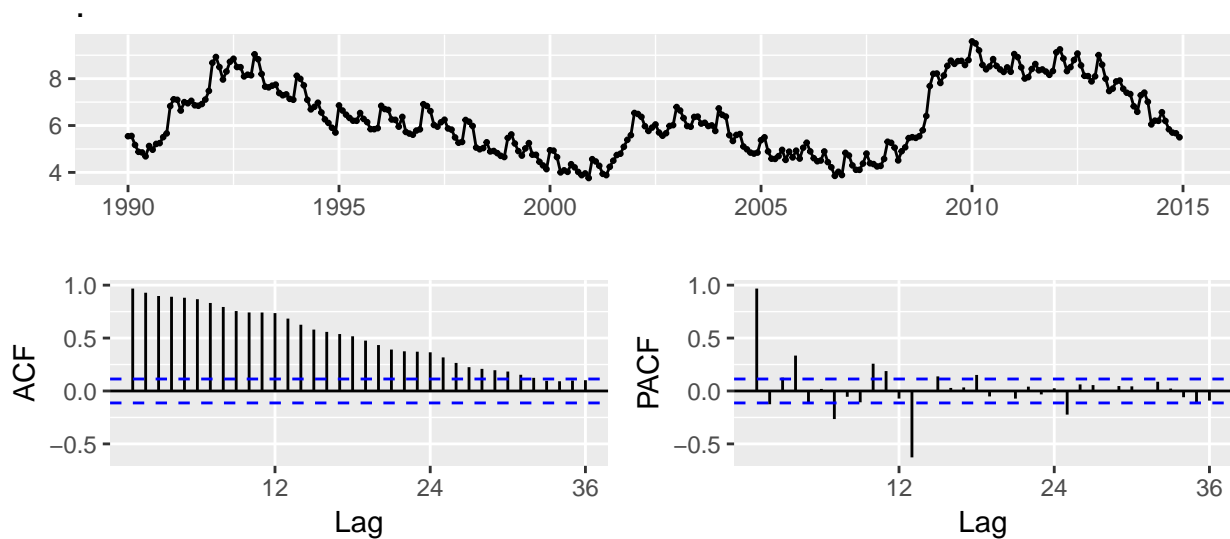
```
##           [,1]
## Jan 1990 5.544
## Feb 1990 5.555
## Mar 1990 5.172
```

```
## Oct 2014 5.698
## Nov 2014 5.668
## Dec 2014 5.498
```

III. EDA

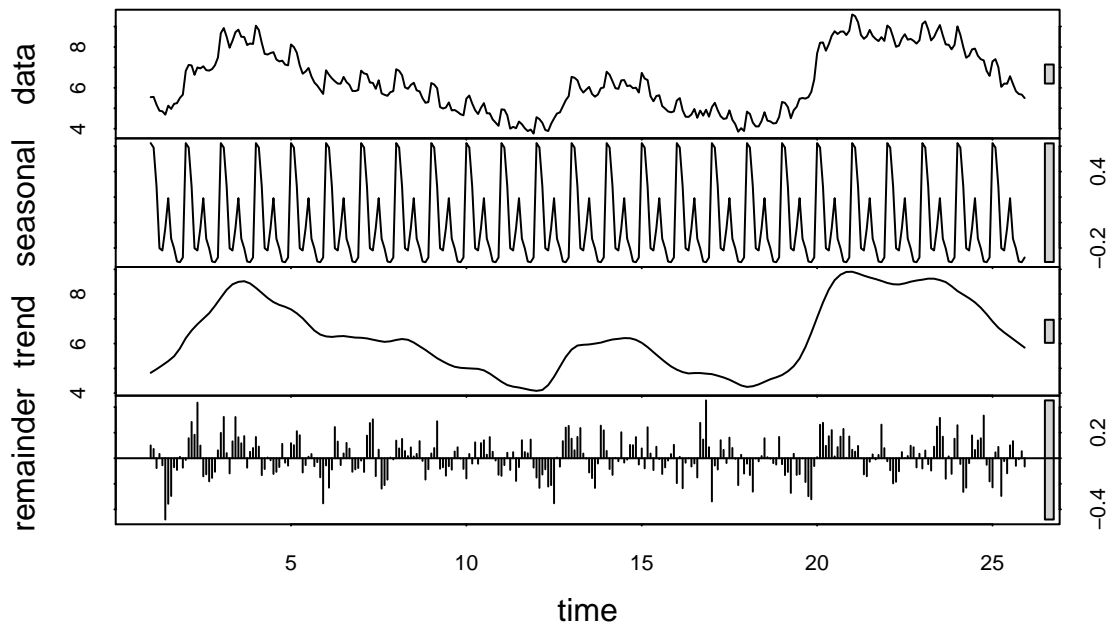
We first plot the time series together with its ACF and PACF.

```
# there is an issue with X axis when plotting xts objects,
# converting to ts for plotting
as.ts(ms.training, start = head(index(ms.training), 1), end = tail(index(ms.training),
1)) %>% ggtsdisplay
```



We also use STL decomposition (HA ch6.5) to decompose the series into seasonal and trend components.

```
fit.stl <- stl(ms.training, t.window = 15, s.window = "periodic",
robust = TRUE)
plot(fit.stl)
```

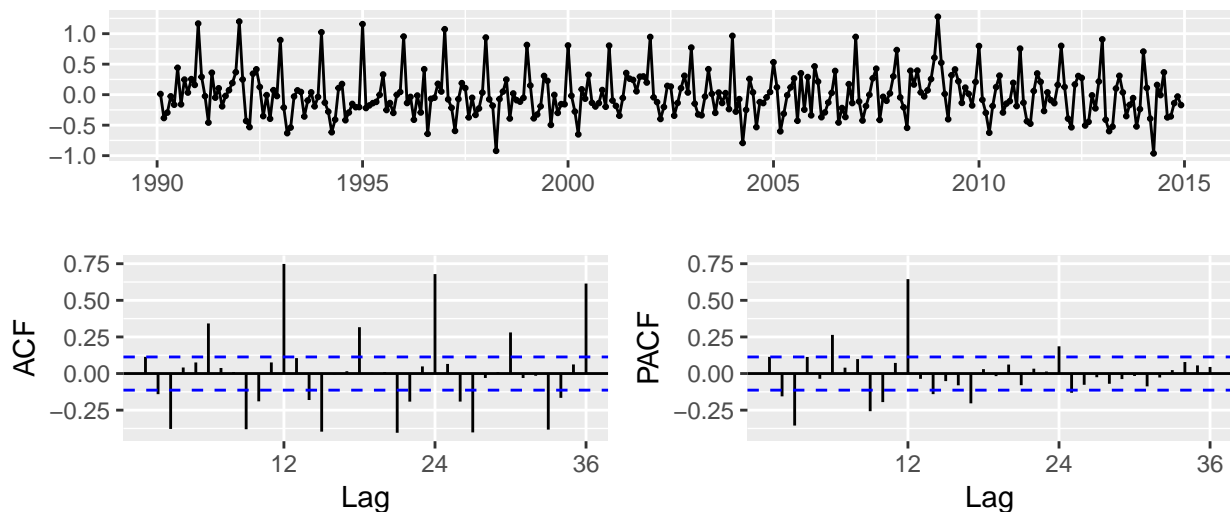


The series both show a trend and a seasonal component. It is not stationary in the mean. This indicates the need for differencing to stabilize the mean.

Transformations

We have trend so we start with taking a first difference of the time series.

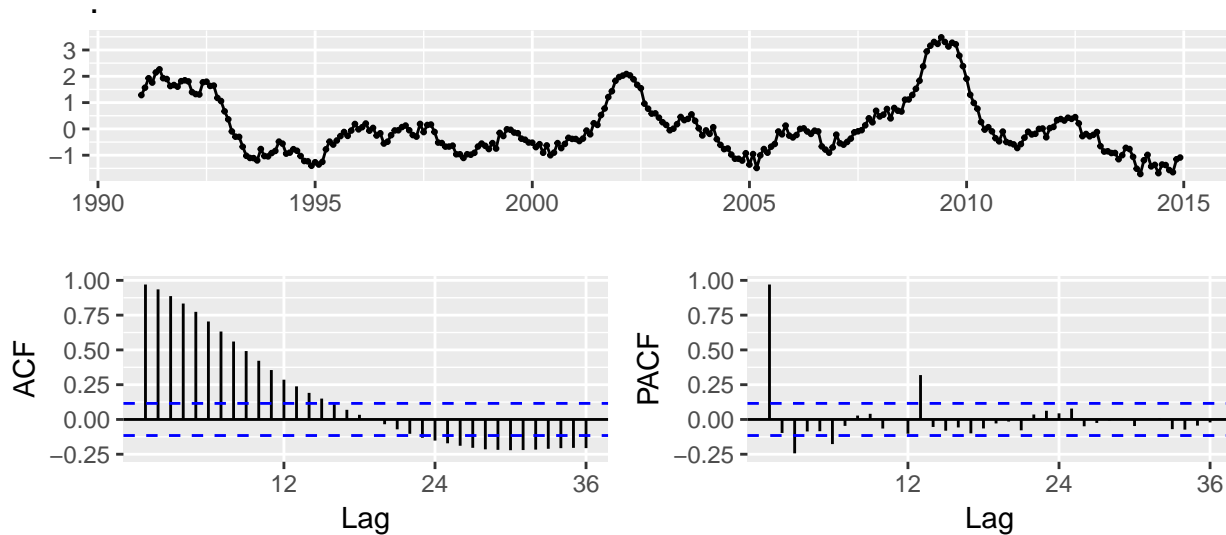
```
# First differencing only
ms.training.1d <- diff(ms.training, lag = 1)
# We'll filter out the first value (since we have a 1 lag
# differencing)
ms.training.1d <- ms.training.1d[!is.na(ms.training.1d)]
as.ts(ms.training.1d, start = head(index(ms.training.1d), 1),
      end = tail(index(ms.training.1d), 1)) %>% ggtsdisplay
```



With only the first-differencing, the series appear to be somewhat stationary. But looking at the time domain as well as the PACF graph, it is clear that there is a strong yearly (at lag 12) component that needs to be

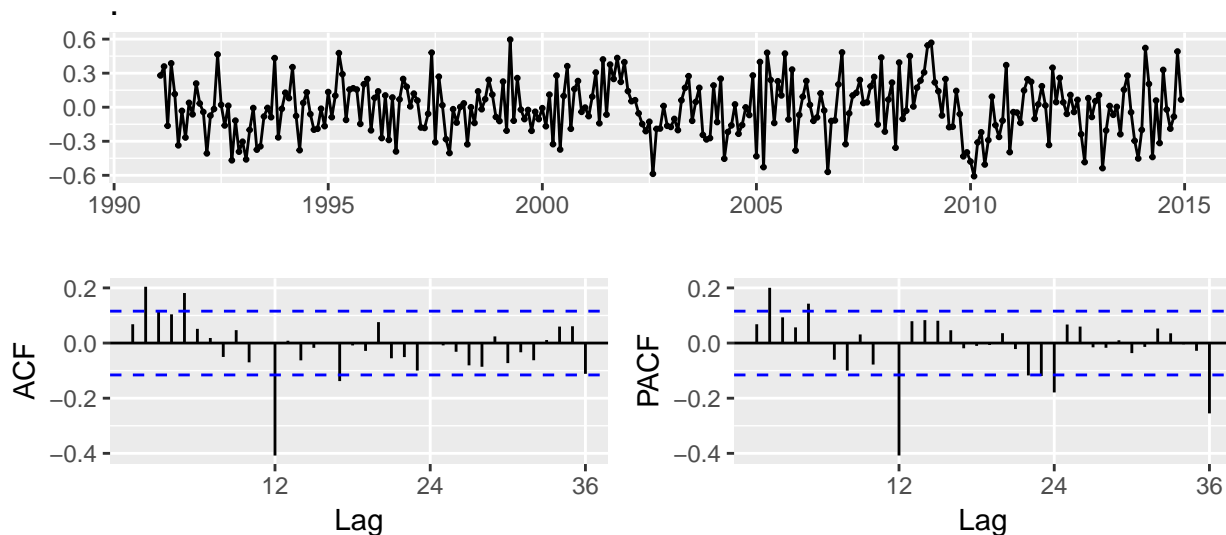
addressed. Next we are going to explore the seasonal effects.

```
# Seasonal differencing only
ms.training.12d <- diff(ms.training, lag = 12)
# We'll filter out the first 12 values (since we have a
# 12-lag differencing)
ms.training.12d <- ms.training.12d[!is.na(ms.training.12d)]
as.ts(ms.training.12d, start = head(index(ms.training.12d), 1),
      end = tail(index(ms.training.12d), 1)) %>% ggtsdisplay
```



We observe that the seasonal differencing has significantly smoothed the time domain graph and we further observe that effect on the ACF / PACF graphs. However, the trend is obvious and the series are not stationary. We will combine the seasonal and non-seasonal components for our next exploratory graph

```
# Both the first and the seasonal differencing
ms.training.1d.12d <- diff(diff(ms.training, lag = 1), lag = 12)
# We'll filter out the first 12 values (since we have a
# 12-lag differencing)
ms.training.1d.12d <- ms.training.1d.12d[!is.na(ms.training.1d.12d)]
as.ts(ms.training.1d.12d, start = head(index(ms.training.1d.12d),
      1), end = tail(index(ms.training.1d.12d), 1)) %>% ggtsdisplay
```



We note that our first-difference / lag-12 seasonal differenced model appear much more stationary and allow us to start conducting ACF / PACF analysis to find the *auto-regressive* and *moving-average* components. We will further strengthen our argument with an augmented Dickey Fuller test between the 2 potential series (first-difference vs. first-difference/seasonal-difference).

```
adf.test(ms.training.1d.12d)
```

```
## Warning in adf.test(ms.training.1d.12d): p-value smaller than printed p-
## value

##
## Augmented Dickey-Fuller Test
##
## data: ms.training.1d.12d
## Dickey-Fuller = -4.8865, Lag order = 6, p-value = 0.01
## alternative hypothesis: stationary
```

We observe that there is empirical evidence to consider our first-difference / 12-lag seasonal difference model to be stationary. In addition, we see a PACF strong component at lag 12, which suggests a seasonal MA(1) component. There are statistically significant ACF/PACF components at lag 2 and 5 without a clear pattern pointing in either MA or AR direction. ACF graph suggests an MA(2) model, whereas PACF graph suggests an AR(2) model. Both graphs hint at a lag(5) component, in addition to the seasonal MA(1) component.

EDA Summary

- Our analysis points to an $ARIMA(p, 1, q)(P, 1, Q)_{12}$ model
- Our non-seasonal AR/MA search for p/q should go up to lag(5)
- Our expectation is to find an appropriate model with $p \in (1, 2)$ and $q \in (1, 2)$

IV. Model search

In the plots of the differenced data, there are spikes in the PACF at lags 12, 24, 36 .. and a spike in ACF at lag 12, suggesting a seasonal MA(1) component.

There are significant spikes at lags 2, 5 in both the ACF and PACF, suggesting a possible MA(2) or AR(2) term, however, the choice is not obvious.

We decide to start with an $ARIMA(0,1,2)(0,1,1)_{12}$ and manually fit some variations on it to identify the models with the lowest AIC and AICc values. In addition, we also consider the out-of-sample performance (MAPE) on the testing data.

Define a function for model testing

Since the procedure is repetitive, we define a function for model testing:

```
# Define a function for testing models
model.test <- function(ORDER, SEASONAL) {

  fit.test <- Arima(ms.training, order = ORDER, seasonal = SEASONAL)
  fit.test$residuals %>% ggtsdisplay # residual plot

  # find MAPE
  f1 <- ms.training %>% Arima(order = ORDER, seasonal = list(order = SEASONAL,
    period = 12)) %>% forecast(h = 11)
```

```

# return AIC, AICc, BIC, MAPE.train, MAPE.test
temp <- cbind(fit.test[6], fit.test[15], fit.test[16], accuracy(f1,
  ms.test)[1, 5], accuracy(f1, ms.test)[2, 5])
colnames(temp) = c("AIC", "AICc", "BIC", "MAPE.train", "MAPE.test")
rownames(temp) = NULL
temp
}

```

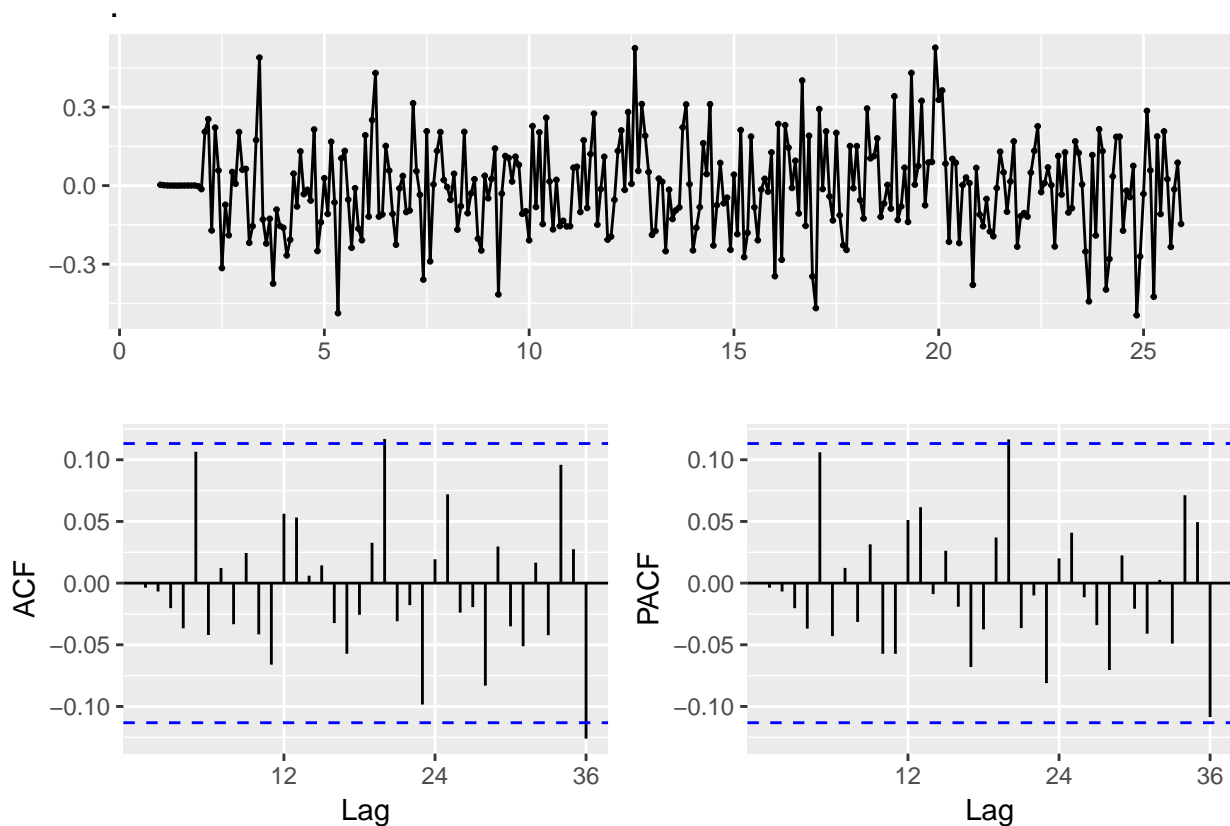
Model testing

```

# Define the model to be tested
Order = c(2, 1, 2) # order
Seasonal = c(0, 1, 1) # seasonal component

model.test(Order, Seasonal)

```



```

##      AIC      AICc      BIC      MAPE.train MAPE.test
## [1,] -123.8599 -123.5599 -101.903  2.364426   3.78801

```

Summary of Models

Candidate Models

ARIMA AIC AICc BIC MAPE.train MAPE.test

(0,1,5)(0,1,1)[12] -120.65 -120.25 -95.03 2.36 5.88

```

(0,1,6)(0,1,1)[12] -120.24 -119.72 -90.96 2.35 5.66
(1,1,1)(0,1,1)[12] -122.71 -122.57 -108.08 2.39 3.32
(1,1,2)(0,1,1)[12] -125.81 -125.60 -107.52 2.36 3.85
(1,1,3)(0,1,1)[12] -123.83 -123.53 -101.87 2.36 3.81
(1,1,1)(0,1,2)[12] -122.23 -122.01 -103.93 2.38 3.67
(2,1,1)(0,1,1)[12] -125.86 -125.64 -107.56 2.36 3.77
(3,1,1)(0,1,1)[12] -123.86 -123.56 -101.9 2.36 3.78
(2,1,1)(1,1,1)[12] -125.55 -125.25 -103.59 2.35 4.11
(1,1,1)(1,1,1)[12] -122.40 -122.19 -104.10 2.38 3.69
(2,1,1)(0,1,2)[12] -125.38 -125.08 -103.42 2.35 4.11
(2,1,2)(0,1,1)[12] -123.86 -123.56 -101.90 2.36 3.79

```

Grid Search

We'll now conduct a grid search to see if any other model provide an enhancement over these models.

```

results <- data.frame(p = 1:25, q = 1:25, AIC = 0, AICc = 0,
  BIC = 0)
for (p in 1:5) {
  for (q in 1:5) {
    m <- ms.training %>% Arima(order = c(p, 1, q), seasonal = list(order = c(0,
      1, 1), period = 12))
    index <- (p - 1) * 5 + q
    results[index, ] = c(p, q, m$aic, m$aicc, m$bic)
  }
}
rbind(results[which.min(results$AIC), ], results[which.min(results$AICc),
  ], results[which.min(results$BIC), ])

```

```

##    p q      AIC      AICc      BIC
## 6  2 1 -125.8566 -125.6430 -107.5591
## 61 2 1 -125.8566 -125.6430 -107.5591
## 1  1 1 -122.7133 -122.5715 -108.0754

```

Candidate models

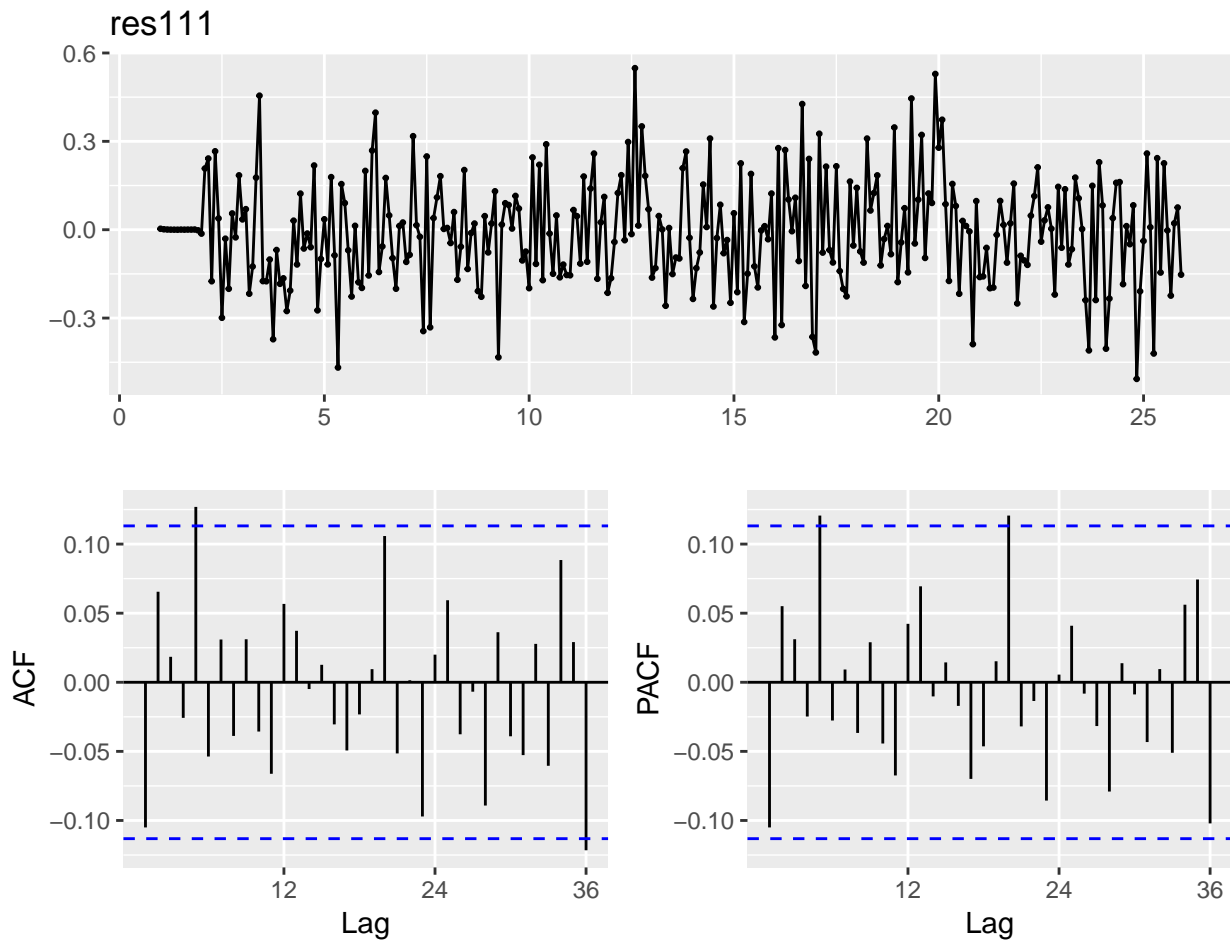
The grid search corroborates our exploratory analysis. We have looked for an optimal p, q combination within the $p \in 1, 5$ and $q \in 1, 5$. Based on the information criteria optimization, we are going to focus on the following models:

- ARIMA(1,1,1)(0,1,1)[12] (minimizes BIC)
- ARIMA(2,1,1)(0,1,1)[12] (minimizes AIC / AICc)

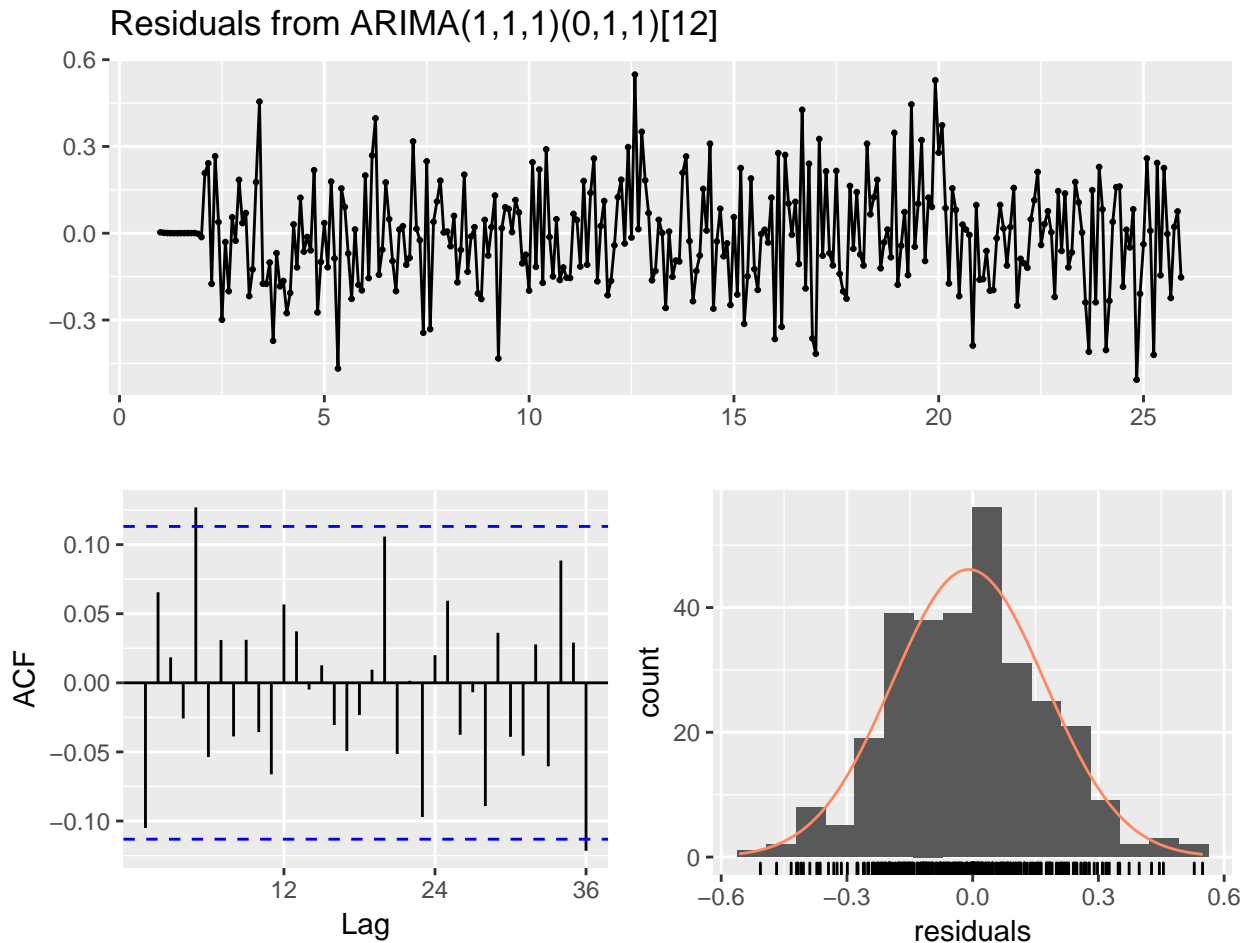
VI. Model validation

ARIMA(1,1,1)(0,1,1)[12]: lowest BIC

```
fit111 <- ms.training %>% Arima(order = c(1, 1, 1), seasonal = list(order = c(0,  
  1, 1), period = 12))  
res111 <- residuals(fit111)  
ggttsdisplay(res111)
```



```
checkresiduals(fit111)
```

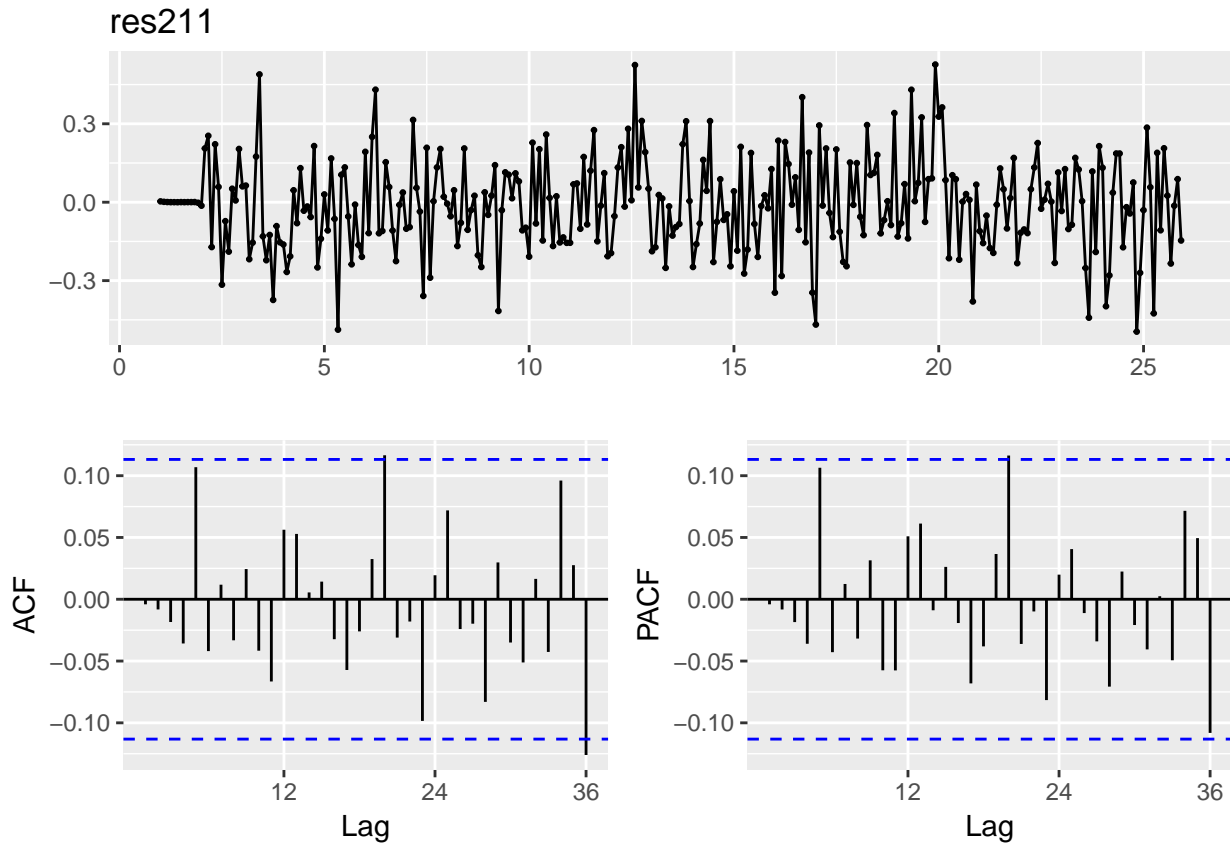
```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(1,1,1)(0,1,1)[12]
## Q* = 24.11, df = 21, p-value = 0.2878
##
## Model df: 3.   Total lags used: 24
Box.test(res111, lag = 16, fitdf = 4, type = "Ljung") # p-value = 0.2188

##
##  Box-Ljung test
##
## data:  res111
## X-squared = 15.428, df = 12, p-value = 0.2188
# Box.test(res, lag=36, fitdf=6, type='Ljung') # p-value =
# 0.1085

# QUESTION: what parameters to use for the Box.test???
```

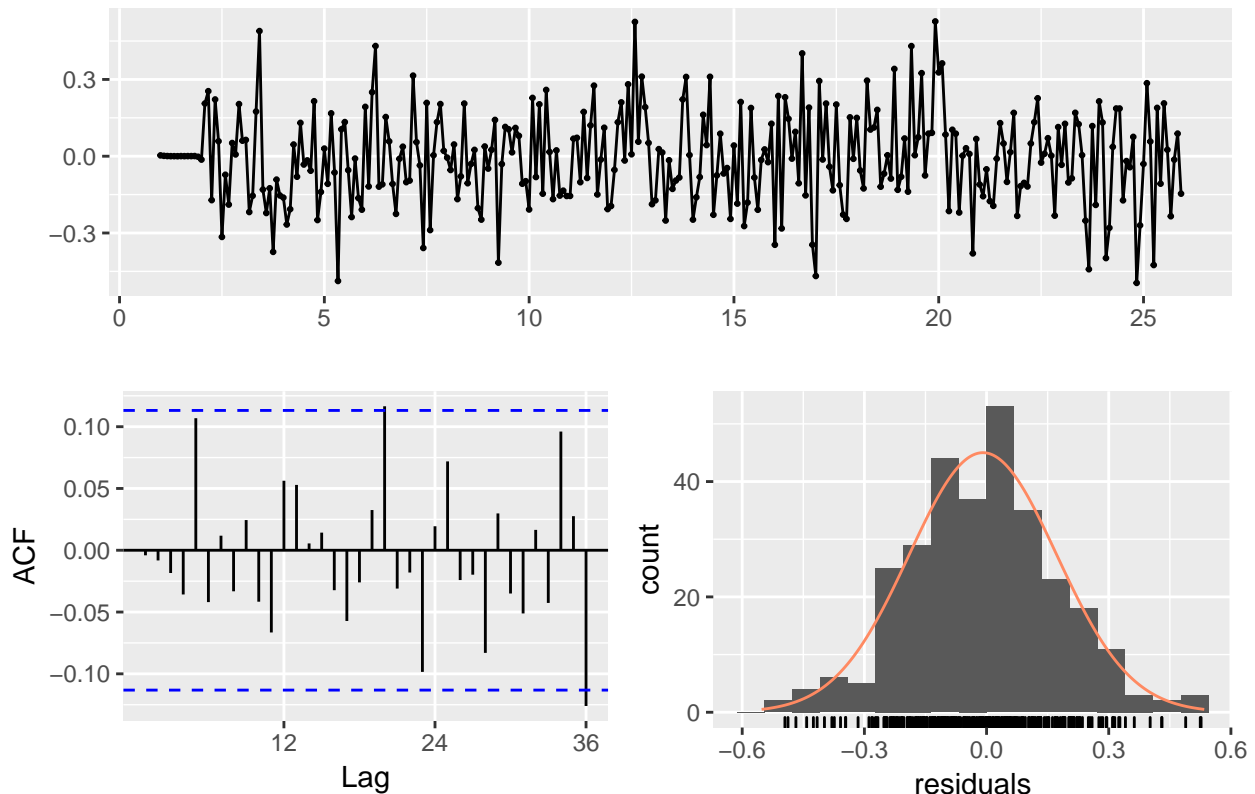
ARIMA(2,1,1)(0,1,1)[12]: lowest AIC, AICc

```
fit211 <- ms.training %>% Arima(order = c(2, 1, 1), seasonal = list(order = c(0,  
  1, 1), period = 12))  
res211 <- residuals(fit211)  
ggtsdisplay(res211)
```



```
checkresiduals(fit211)
```

Residuals from ARIMA(2,1,1)(0,1,1)[12]



```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(2,1,1)(0,1,1)[12]
## Q* = 19.069, df = 20, p-value = 0.5174
##
## Model df: 4.   Total lags used: 24
Box.test(res211, lag = 16, fitdf = 4, type = "Ljung") # p-value = 0.6722

##
##  Box-Ljung test
##
## data:  res211
## X-squared = 9.3568, df = 12, p-value = 0.6722
# Box.test(res, lag=36, fitdf=6, type='Ljung') # p-value =
# 0.2596

# QUESTION: what parameters to use for the Box.test????
```

The results for both models are similar: - We can ignore the 2 spikes outside the 95% significant limits, the residuals appear to be white noise. - A Ljung-Box test also shows that the residuals have no remaining auto-correlations.

VII. Forecast

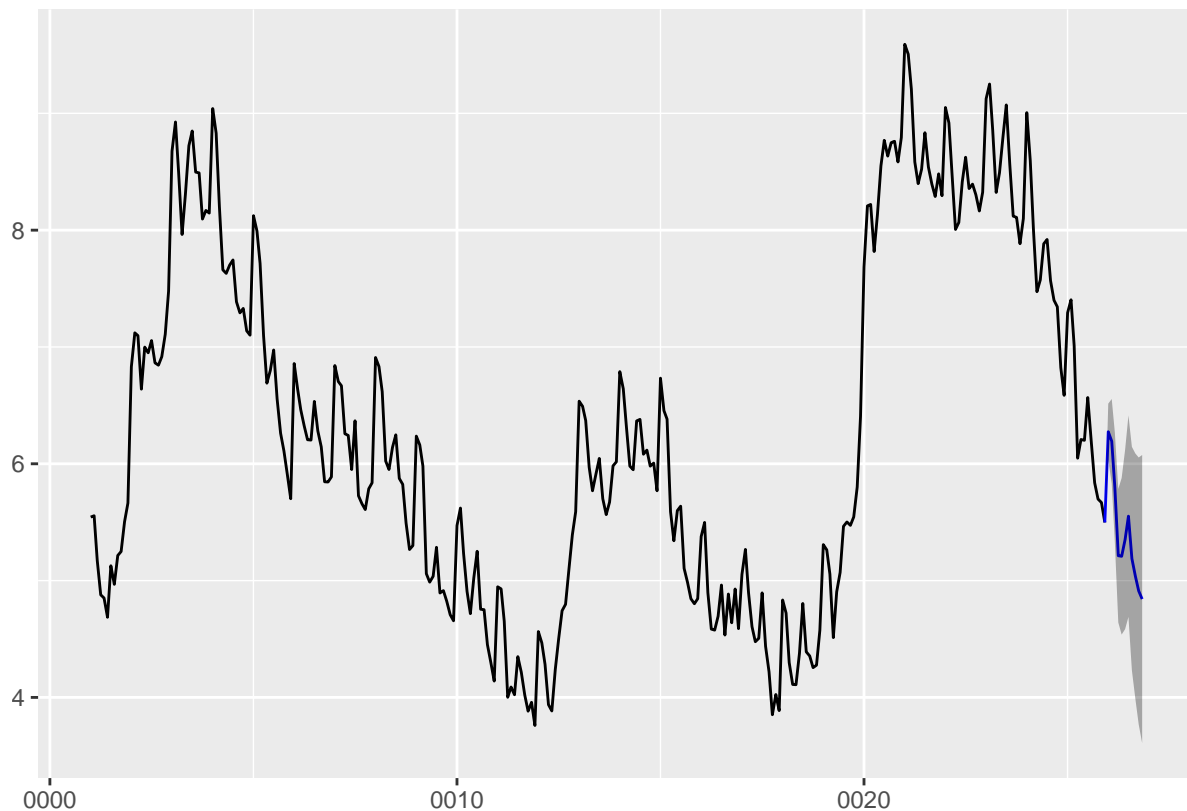
We do a 11-month ahead forecast of the series in 2015 using both models.

```
forecast111 <- fit111 %>% forecast(h = 11)
forecast211 <- fit211 %>% forecast(h = 11)
(results <- rbind(accuracy(forecast111, ms.test), accuracy(forecast211,
  ms.test)))[, 1:5])
```

##		ME	RMSE	MAE	MPE	MAPE
##	Training set	-0.009339336	0.1825311	0.1427566	-0.1059365	2.389875
##	Test set	0.026623361	0.2002727	0.1779535	0.1710571	3.319050
##	Training set	-0.008926836	0.1810804	0.1416233	-0.1017597	2.364688
##	Test set	-0.012986097	0.2163455	0.1986888	-0.6007220	3.770132

We note that the $ARIMA(1,1,1)(0,1,1)_{12}$ has the lowest MAPE score for the test set (2015). Therefore we are going to conduct our final forecast with that model

```
forecast111 %>% autoplot()
```



WE NEED HIST to show residuals are normal

VIII. Conclusions