

$$\frac{\partial^2 T}{\partial x^2} \approx \frac{T(x_{j+1}, y_i) - 2T(x_j, y_i) + T(x_{j-1}, y_i))}{h^2}$$

$$\frac{\partial^2 T}{\partial y^2} \approx \frac{T(x_j, y_{i+1}) - 2T(x_j, y_i) + T(x_j, y_{i-1}))}{h^2}$$

For  $\frac{\partial T}{\partial x}(0, y) = 0 \Rightarrow \frac{\partial T}{\partial x}(x_j, y_i) \approx \frac{-3T(x_j, y_i) + 4T(x_{j+1}, y_i) - T(x_{j+2}, y_i))}{2h}$

$$\Rightarrow \frac{-3T(x_0, y_i) + 4T(x_1, y_i) - T(x_2, y_i))}{2h} = 0 \Leftrightarrow -3T(x_0, y_i) + 4T(x_1, y_i) - T(x_2, y_i) = 0$$

$$\Rightarrow T(x_0, y_i) = \frac{4T(x_1, y_i) - T(x_2, y_i))}{3}$$

insert in  
equation system

$$T(x_2, y_i) - 2T(x_1, y_i) + \left( \frac{4T(x_1, y_i) - T(x_2, y_i))}{3} \right) = f$$

$$= - \frac{3T(x_2, y_i) - 6T(x_1, y_i) + 4T(x_1, y_i) - T(x_2, y_i))}{3h^2} = f$$

$$= - \frac{2T(x_2, y_i) - 2T(x_1, y_i))}{3h^2} = f$$

For  $\frac{\partial T}{\partial x}(L, y) = 0 \Rightarrow \frac{\partial T}{\partial x}(x_j, y_i) \approx \frac{3T(x_j, y_i) - 4T(x_{j-1}, y_i) + T(x_{j-2}, y_i))}{2h}$

$$\Rightarrow 3T(x_N, y_i) - 4T(x_{N-1}, y_i) + T(x_{N-2}, y_i) = 0 \Rightarrow T(x_N, y_i) = \frac{4T(x_{N-1}, y_i) - T(x_{N-2}, y_i))}{3}$$

insert in  
equation sys.

$$\left( \frac{4T(x_{N-1}, y_i) - T(x_{N-2}, y_i))}{3} \right) - 2T(x_{N-1}, y_i) - T(x_{N-2}, y_i) = f$$

$$= \frac{4T(x_{N-1}, y_i) - T(x_{N-2}, y_i) - 6T(x_{N-1}, y_i) - 3T(x_{N-2}, y_i))}{3h^2} = \frac{2T(x_{N-1}, y_i) + 4T(x_{N-2}, y_i))}{3h^2} = f$$

Same principle for  $\frac{\partial T}{\partial y}(x, L_y) = 0$