Binary Index Tree

```
static class BIT {
    long[] tree;
    int[] data;
    public BIT(int[] in) {
        data=in;
        tree=new long[data.length+1];
        for (int i=1;i<tree.length;i++) {</pre>
            int index=i;
            int val=data[i-1];
            while(index<tree.length) {</pre>
                 tree[index]+=val;
                 index+=Integer.lowestOneBit(index);
    //sum from 0 to endIndex inclusive
    public long rangeSum(int endIndex) {
        endIndex++;
        long sum=0;
        while (endIndex>0) {
            sum+=tree[endIndex];
            endIndex-=Integer.lowestOneBit(endIndex);
        return sum;
    //sum from 1 to r inclusive
    public long rangeSum(int 1, int r) {
        return rangeSum(r)-rangeSum(1-1);
    public void updateDelta(int index, int delta) {
        int fenIndex=index+1;
        int val=delta;
        data[index]+=delta;
        while (fenIndex<tree.length) {</pre>
            tree[fenIndex]+=val;
            fenIndex+=Integer.lowestOneBit(fenIndex);
    public void updateVal(int index, int newVal) {
        int fenIndex=index+1;
        int val=newVal-data[index];
        data[index]=newVal;
        while (fenIndex<tree.length) {</pre>
            tree[fenIndex]+=val;
            fenIndex+=Integer.lowestOneBit(fenIndex);
    public String toString(){
        return "Tree: " + Arrays.toString(tree) + "\n" + "Data:" + Arrays.toString(data);
}
```

Disjoint Set

```
class DisjointSet {
    int[] parent;
    int[] rank;
    public DisjointSet(int size) {
        parent=new int[size];
        rank=new int[size];
        for(int i=0;i<size;i++)</pre>
            parent[i]=i;
    public int find(int x) {
        if (parent[x] ==x)
             return x;
        else
             return parent[x]=find(parent[x]);
    }
    public void union(int x, int y) {
        int xRoot=find(x);
        int yRoot=find(y);
        if (rank[xRoot] < rank[yRoot])</pre>
            parent[xRoot] = yRoot;
        else if(rank[yRoot] < rank[xRoot])</pre>
            parent[yRoot] = xRoot;
            parent[yRoot] = xRoot;
            rank[xRoot]++;
        }
    }
}
```

Sparse Table

```
class SparseTable {
    int[][] table;
    ArrayList<Integer> pows=new ArrayList<>(25);
    public SparseTable(int[] in) {
        int power=1;
        int exp=0;
        pows.add(power);
        while (power<in.length) {</pre>
            power<<=1;</pre>
            exp++;
            pows.add(power);
        table=new int[in.length][exp];
        for(int i=0;i<in.length;i++)</pre>
             table[i][0]=in[i];
        for(int j=1;j<exp;j++)</pre>
             for (int i=0;i<in.length;i++) {</pre>
                 if (i+pows.get(j-1)>=in.length)
                     table[i][j]=table[i][j-1];
                 else
                     table[i][j]=Math.min(table[i][j-1], table[i+pows.get(j-1)][j-1]);
             }
    //minimum from 1 to r inclusive
    public int rmq(int left, int right) {
        if (left==right)
             return table[left][0];
        if (left==right-1)
            return table[left][1];
        int diff=right-left+1;
        int exp=0;
        while (pows.get (exp) < diff)</pre>
            exp++;
        exp--;
        return Math.min(table[left][exp], table[right-pows.get(exp)+1][exp]);
    }
}
```

TopSort

```
static class topSort{
    HashMap<Integer, Integer> indegree=new HashMap<>();
    ArrayList<Integer> ordering=new ArrayList<>();
    //Assumes all vertices in the edges keyset
   public topSort(HashMap<Integer, HashSet<Integer>> edges) {
        for(int key:edges.keySet())
            indegree.put(key, 0);
        for(int key:edges.keySet())
            for(int out:edges.get(key))
                indegree.put(out,indegree.remove(out)+1);
        ArrayDeque<Integer> deque=new ArrayDeque<>();
        for(int key:edges.keySet())
            if (indegree.get (key) ==0)
                deque.add(key);
        while(!deque.isEmpty()){
            int cur=deque.pollFirst();
            ordering.add(cur);
            for(int out:edges.get(cur)) {
                int val=indegree.get(out);
                indegree.put(out, val-1);
                if (val-1==0)
                    deque.add(out);
        }
    }
}
```

KnapSack

```
class KnapSack {
    static int[][] dp;
    static int[] weight={};
    static int[] vals={};
    static int maxWeight=11;
    public static int knapSack(int index, int curWeight) {
        if (index>=vals.length)
            return 0;
        if (dp[index] [curWeight]!=0)
            return dp[index][curWeight];
        if (curWeight+weight[index]>maxWeight)
            return dp[index][curWeight]=knapSack(index+1,curWeight);
            return
dp[index][curWeight] = Math.max(knapSack(index+1, curWeight), vals[index] + knapSack(index+1)
,curWeight+weight[index]));
    public static void main(String args[]){
        dp=new int[weight.length] [maxWeight+1];
        System.out.println(knapSack(0,0));
```

Inversions

```
class Inversions{
    int[] list;
    int count;
    public Inversions(int[] in){
        list=in.clone();
        Arrays.sort(in);
        HashMap<Integer, Integer> compressMap=new HashMap<>();
        for(int i=0;i<in.length;i++) {</pre>
            compressMap.put(in[i],i);
        for(int i=0;i<list.length;i++)</pre>
            list[i]=compressMap.get(list[i]);
        int[] empty=new int[in.length];
        BIT fenwick=new BIT(empty);
        for(int i=0;i<list.length;i++) {</pre>
            count+=fenwick.rangeSum(list[i],list.length-1);
            fenwick.updateDelta(list[i],1);
    }
}
```

Strongly Connected Components

```
class connectedComponents {
    ArrayList<ArrayList<Integer>> groups=new ArrayList<>();
    ArrayList<Integer> curGroup=new ArrayList<>();
    ArrayDeque<Integer> stack=new ArrayDeque<>();
    HashSet<Integer> visited=new HashSet<>();
HashMap<Integer, HashSet<Integer>> edges;
    HashMap<Integer, HashSet<Integer>> reverse;
    public connectedComponents(HashMap<Integer, HashSet<Integer>>
edges,HashMap<Integer, HashSet<Integer>> reverse) {
        this.edges=edges;
        this.reverse=reverse;
        for(int start: edges.keySet())
            DFSorder(start);
        visited=new HashSet<>();
              System.out.println(stack);
        while(!stack.isEmpty()){
            DFSgroup(stack.pollFirst());
            if(curGroup.size()!=0) {
                 groups.add(curGroup);
                curGroup=new ArrayList<>();
        }
    public void DFSorder(int start) {
        if(visited.contains(start))
            return;
        visited.add(start);
        for(int e:edges.get(start))
            DFSorder(e);
        stack.addFirst(start);
    public void DFSgroup(int start) {
        if (visited.contains(start))
            return:
        visited.add(start);
        curGroup.add(start);
        for(int e:reverse.get(start))
            DFSgroup(e);
    }
```

Totient Sieve

Letter Ordering

```
class letterOrdering {
    public static void main(String[] args) throws IOException {
        BufferedReader br=new BufferedReader(new InputStreamReader(System.in));
        int len=Integer.parseInt(br.readLine());
        ArrayList<String> list=new ArrayList<>(len);
        for(int i=0;i<len;i++)</pre>
            list.add(br.readLine());
        HashMap<Integer, HashSet<Integer>> edges=new HashMap<>();
        int start=(int)'a';
        for(int i=start;i<start+26;i++) {</pre>
            edges.put(i, new HashSet<>());
        for (int i=0; i<len-1; i++) {</pre>
            String cur=list.get(i);
            String next=list.get(i+1);
            int index=0;
            while (cur.charAt (index) ==next.charAt (index) ) {
                 if(index==cur.length()||index==next.length()) {
                     if (next.length() < cur.length()) {</pre>
                         System.out.println("Impossible");
                         return;
                     break;
                 }
            if (index<Math.min(cur.length(), next.length())) {</pre>
                 edges.get((int)cur.charAt(index)).add((int)next.charAt(index));
          System.out.println(edges);
        topSort sort=new topSort(edges);
        String out="";
        for(int e:sort.ordering)
            out+=((char)e);
        System.out.println(out.length() == 26?out: "Impossible");
    }
```