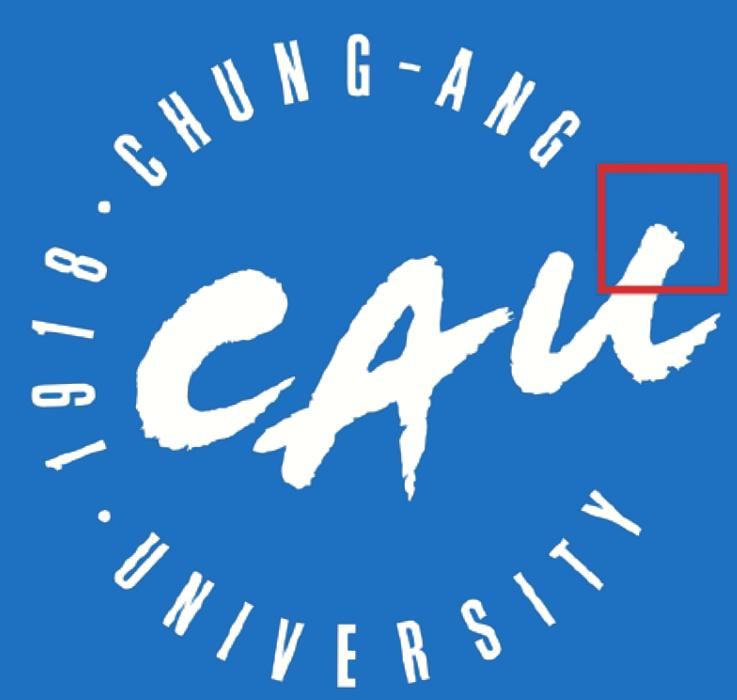


# Unsupervised Segmentation incorporating Shape Prior via Generative Adversarial Networks

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## I. Motivation



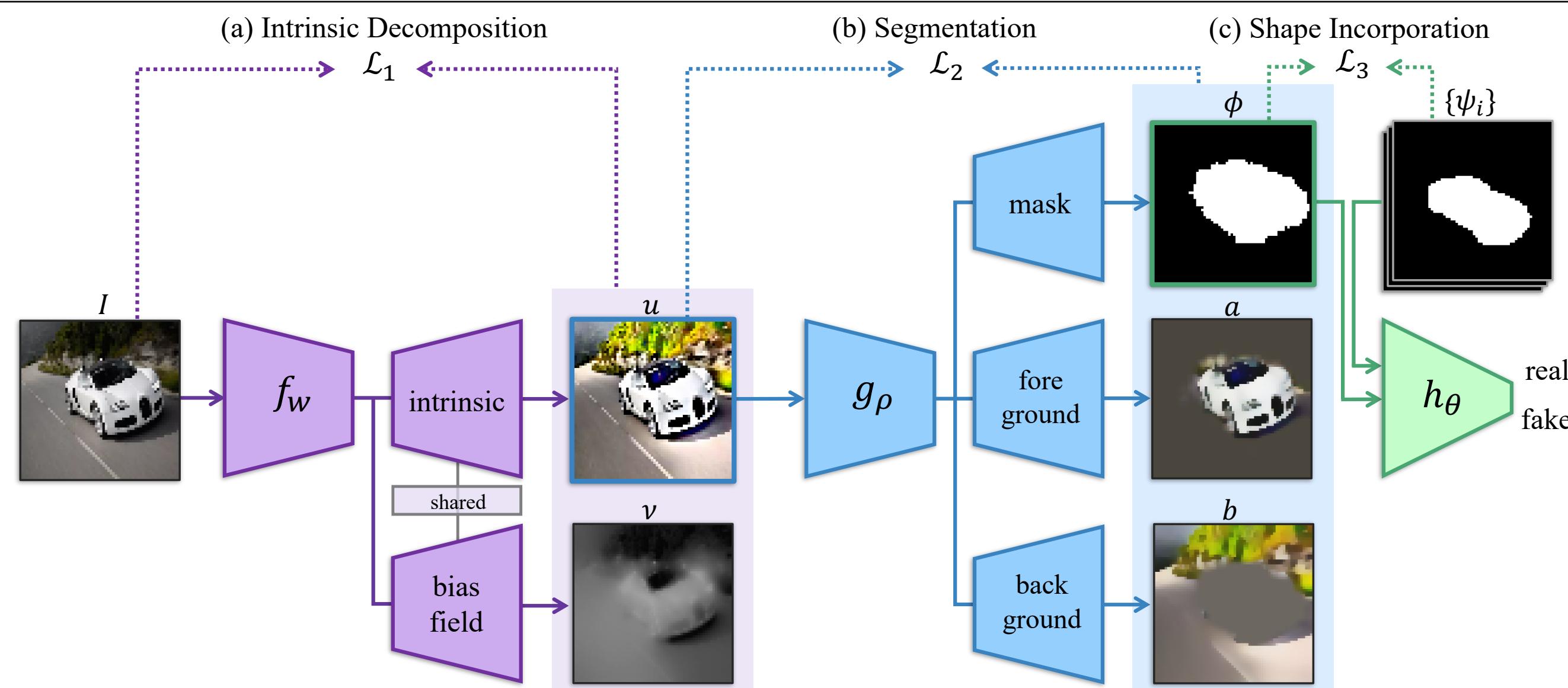
Bi-partitioning

### Challenges in object segmentation:

- Interruption by bias fields and occlusions.
- Poor generalization and expensive annotations problems of supervised learning.
- GAN-based unsupervised approaches struggle to learn distributions of enormous dimensions.

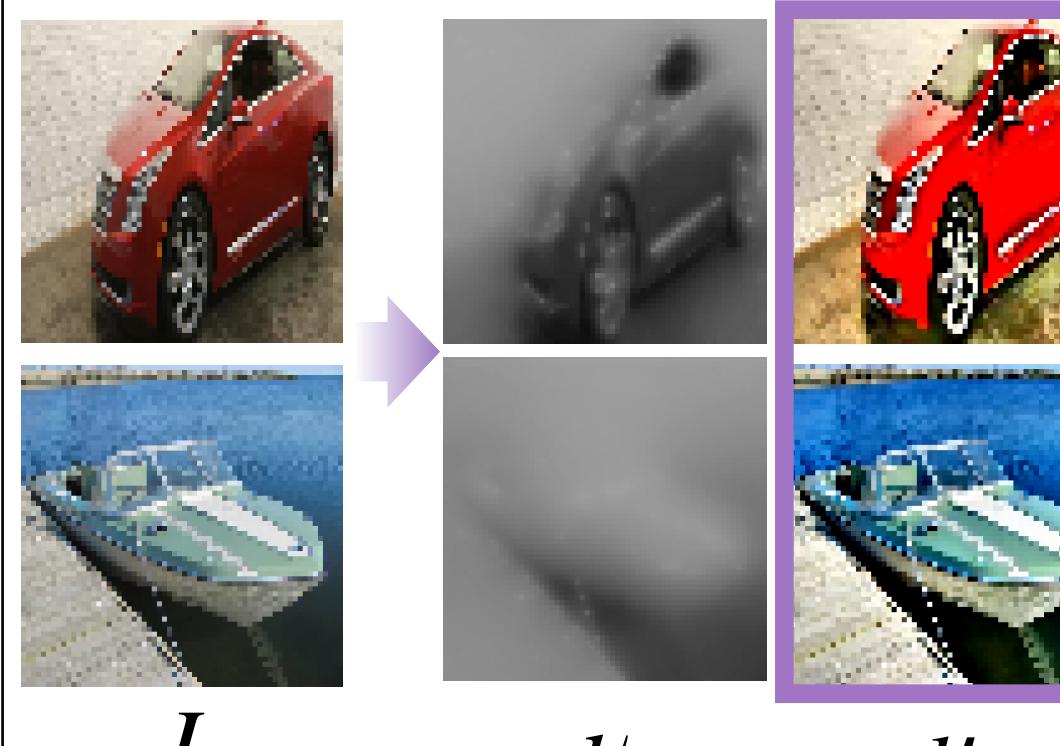
**Our solution:** retrieve intrinsic representations to remove bias fields, train segmentation network based on an unsupervised energy and impose shape constraints by applying GAN framework that learns only geometric distributions.

## II. Method Overview



- (a)  $f$  obtains an intrinsic representation  $u$  that is robust to a bias field  $\nu$ .  
(b)  $g$  derives a segmenting function  $\phi$  from  $u$  in an unsupervised way.  
(c)  $h$  imposes a geometric constraint to  $\phi$  using a set of prior shapes  $\{\psi_i\}$ .

## III. Intrinsic Decomposition

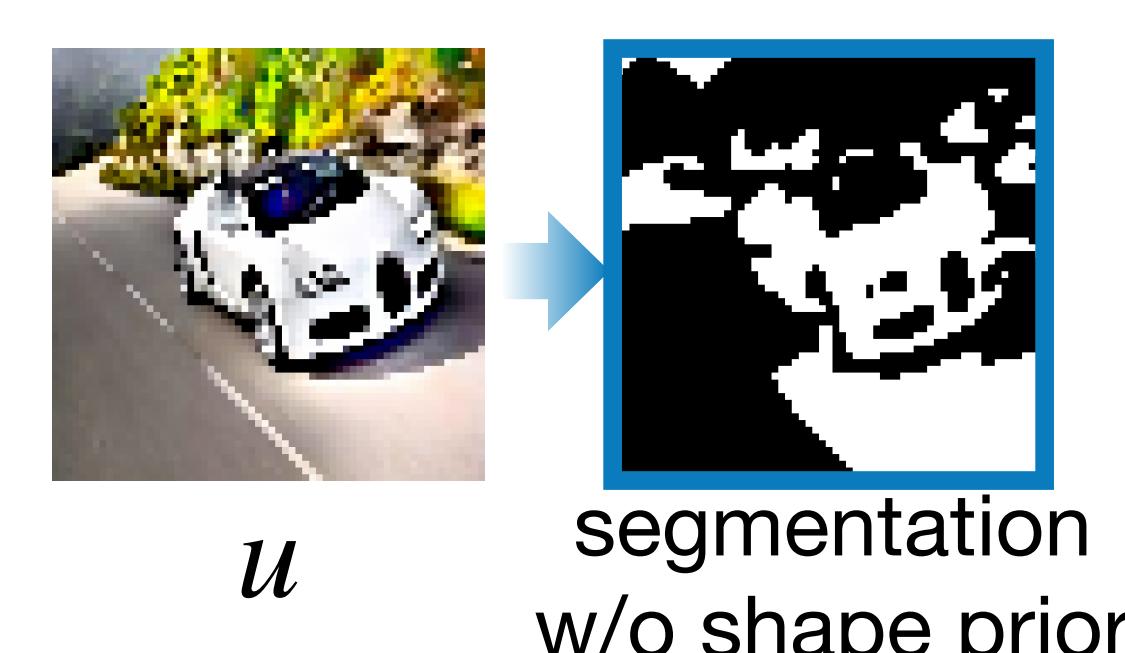


$$I = \nu(u + \eta)$$

$$\mathcal{L}_1(u, \nu; I) = \frac{\|I - u\|^2}{\nu} + \lambda \|\nabla u\| + \alpha \|\nabla \nu\|^2 + \beta \|\nu - 1\|^2$$

- An image  $I$  is decomposed into a bias field  $\nu$  and an intrinsic representation  $u$  using the objective function  $\mathcal{L}_1$  derived from an image formation model using an additive noise with a multiplicative bias field.
- The model parameter  $w$  of  $f$  is optimized based on  $\mathcal{L}_1$ .

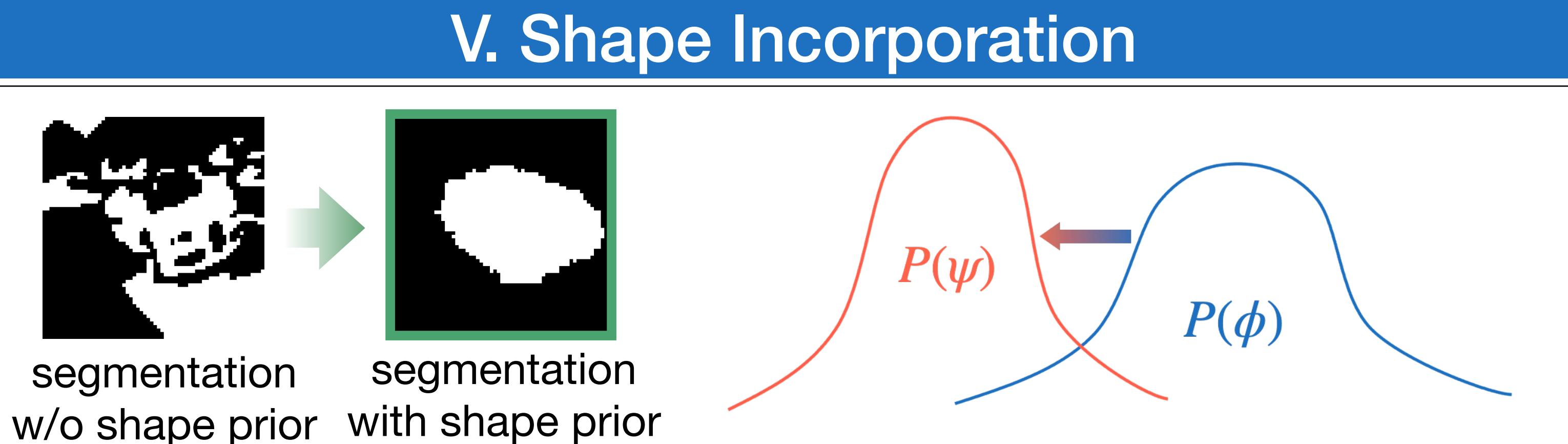
## IV. Unsupervised Segmentation



$$\begin{aligned} \mathcal{L}_2(\phi, a, b; u) = \int_{\Omega} |u(x) - a(x)|^2 \phi(x) dx + \int_{\Omega} |u(x) - b(x)|^2 (1 - \phi(x)) dx \\ + \gamma_1 \|\nabla \phi(x)\| + \gamma_2 \|\nabla a(x)\| + \gamma_3 \|\nabla b(x)\| \end{aligned}$$

- A piecewise smooth Mumford-Shah<sup>1</sup> model is applied for the objective function  $\mathcal{L}_2$  for unsupervised segmentation.
- The segmenting function  $\phi$  and its associated estimates  $a$  and  $b$  are directly achieved by the deep neural network  $g$ .
- The obtained  $u$  is used as input for  $g$ .

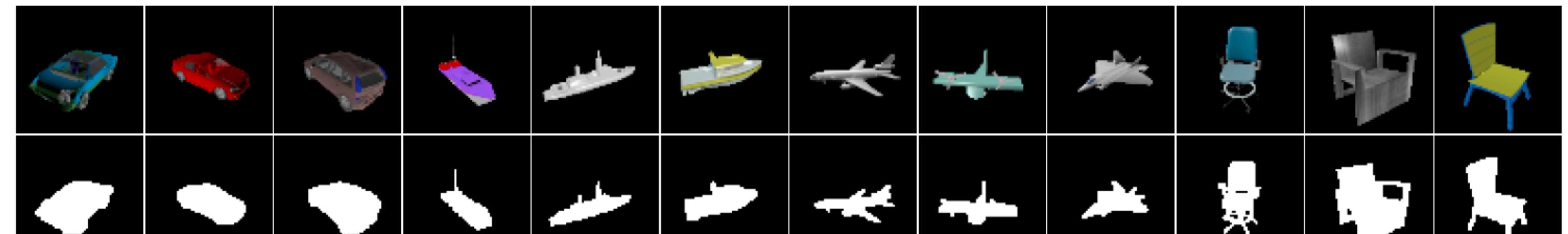
$$\begin{aligned} \mathcal{L}_2(\phi, a, b; u) = \int_{\Omega} |u(x) - a(x)|^2 \phi(x) dx + \int_{\Omega} |u(x) - b(x)|^2 (1 - \phi(x)) dx \\ + \gamma_1 \|\nabla \phi(x)\| + \gamma_2 \|\nabla a(x)\| + \gamma_3 \|\nabla b(x)\| \end{aligned}$$



$$\mathcal{L}_3(\rho, \theta; \mathcal{S}, \mathcal{R}) = \mathbb{E}_{\psi \sim P(\psi)}[\log(h(\psi))] - \mathbb{E}_{\phi \sim Q(\phi)}[\log(h(\phi))] - \frac{\kappa}{2} \mathbb{E}_{\psi \sim P(\psi)}[\|\nabla h(\psi)\|_2^2]$$

- Shape constraints are imposed by minimizing the discrepancy between probability distributions of partitioning function  $Q(\phi)$  and prior shape  $P(\psi)$  using the GAN loss function  $\mathcal{L}_3$ .
- $\mathcal{L}_3$  is used to optimize the model parameters of both the segmentation network  $g$  and the discriminator  $h$ .

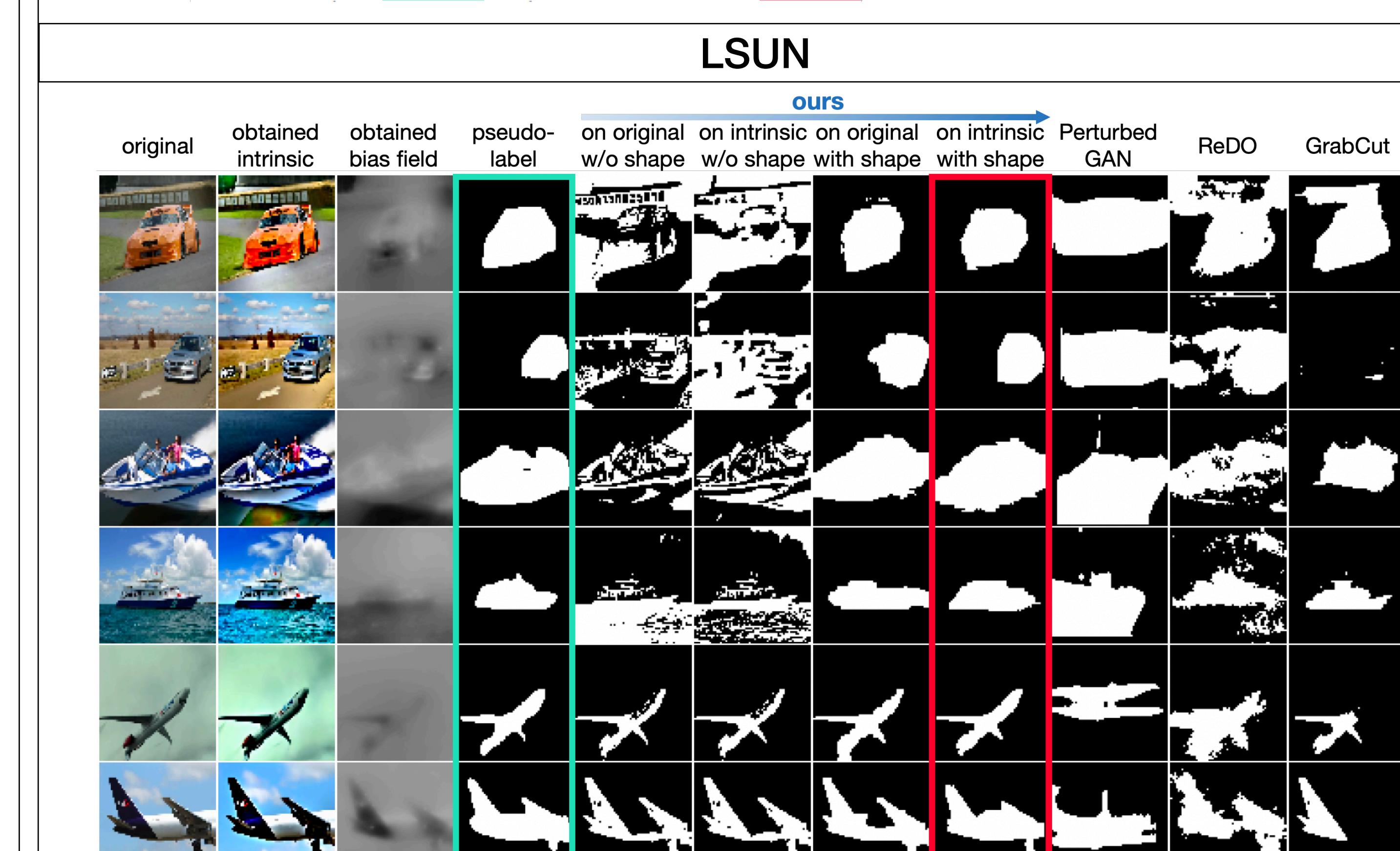
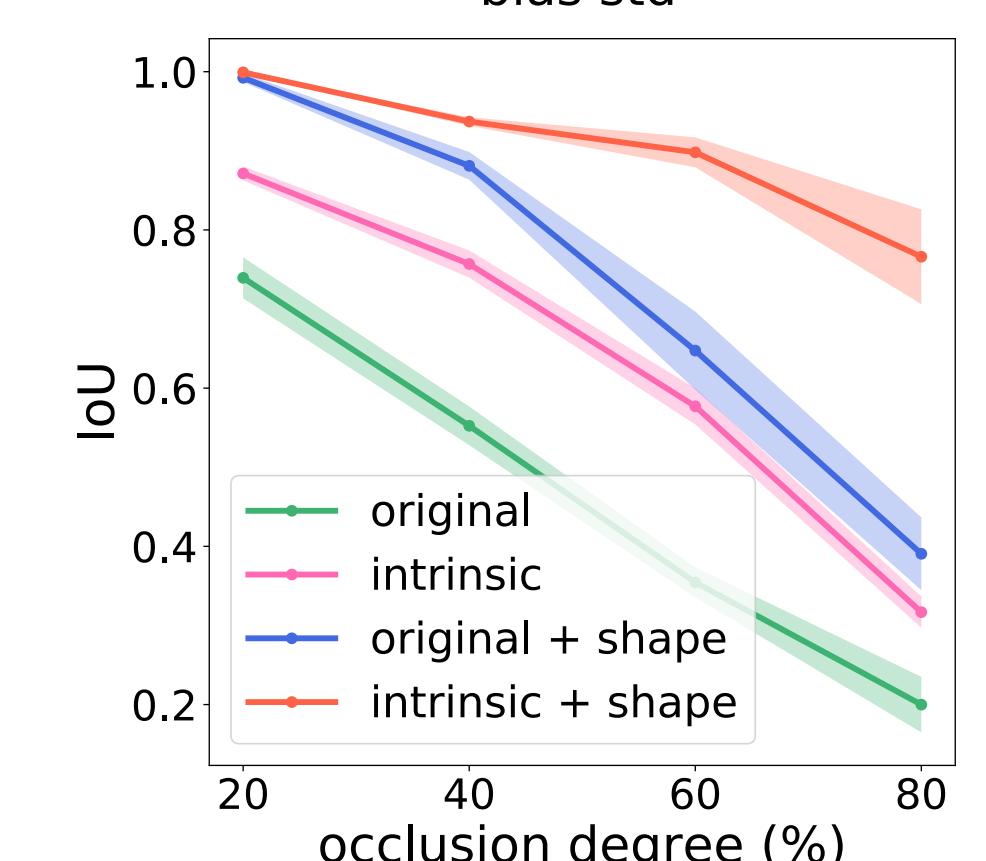
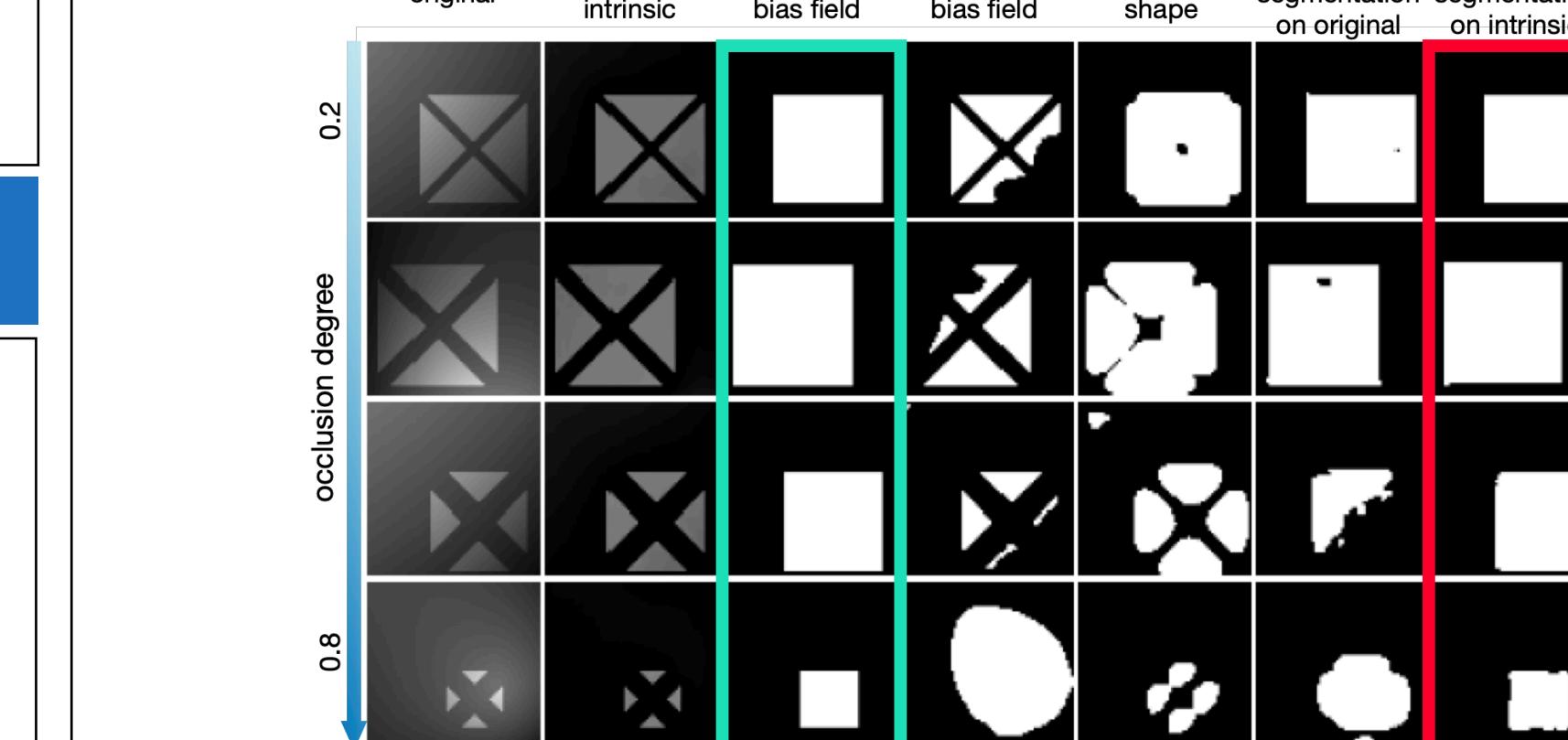
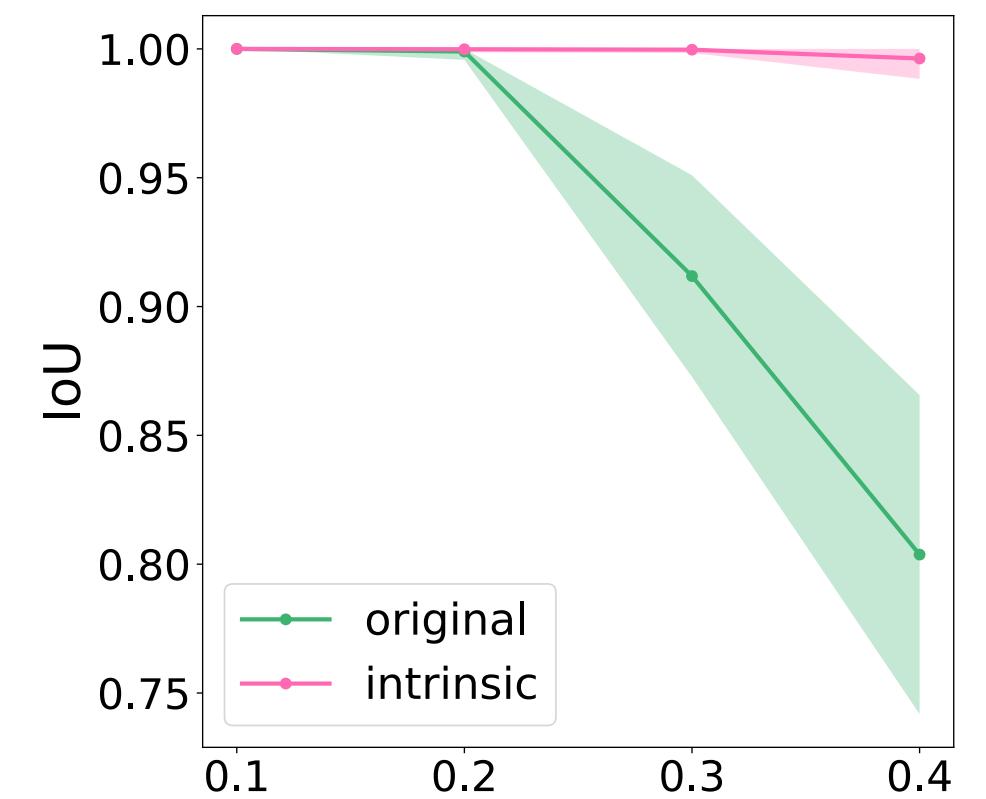
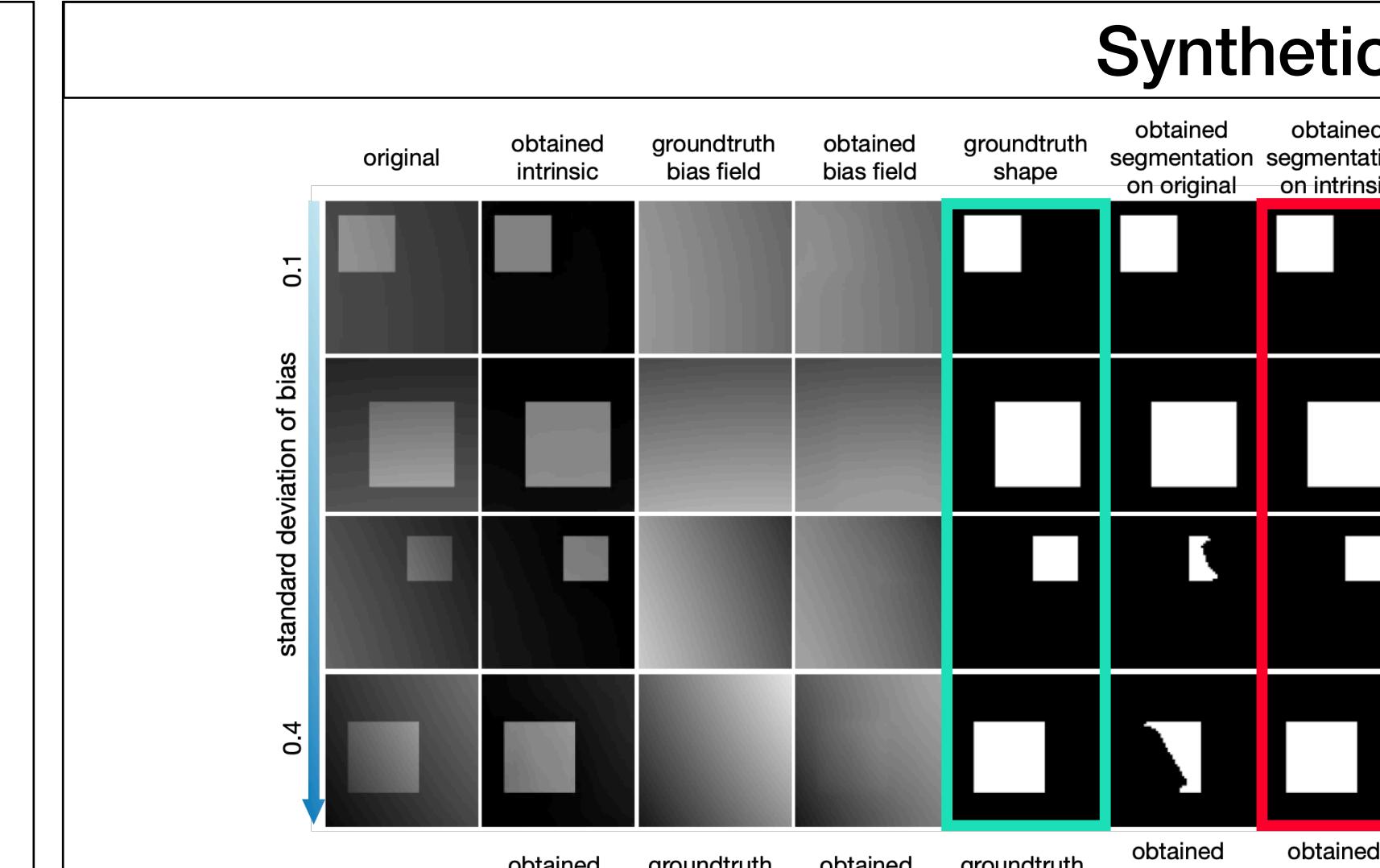
Shape prior construction with a set of deformed shapes  $\psi_i(x) = \chi_S \circ t_i(x)$ :



Examples of shape prior data

- $P(\psi)$  is constructed by the equivalence class  $\mathcal{S} = \{\psi_i = \chi_S \circ t_i \mid t_i \in \mathcal{T}\}$  of shape  $\mathcal{S}$  under the action of the transformation group  $\mathcal{T}$ .

## VI. Results



## Reference

- Mumford, D.B. and Shah, J., 1989. Optimal approximations by piecewise smooth functions and associated variational problems. Communications on pure and applied mathematics.