False Discovery Rates, A New Deal

Matthew Stephens

2014/2/24

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- Thought: I should get organized; I should help others get organized.

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- While doing research, record what you did and what the outcome was.
- Use version control git and internet repositories (bitbucket, github) to organize notes, code, etc.
- Use knitr to help make your research reproducible.

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- An amateur example: http://github.com/stephens999/ash

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- This talk was written with knitr (with RStudio)!

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- "publishing figures or results without the complete software environment could be compared to a mathematician publishing an announcement of a mathematical theorem without giving the proof" (Buckheit and Donohoe)
- "an article about a computational result is advertising, not scholarship. The actual scholarship is the full software environment, code and data, that produced the result." [Claerbout]

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- Reproducing work is also the first step to extending it.
- ullet Helps communications among researchers (eg student + advisor).
- If you do not publish code implementing your methods, your methods will likely go unused.

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- Google "donohoe buckheit" for "Wavelab and reproducible research"

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FDR, local fdr, and q values

Although precise definitions vary depending on whether one takes a Bayesian or Frequentist approach to the problem, roughly

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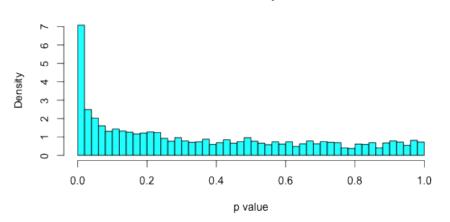
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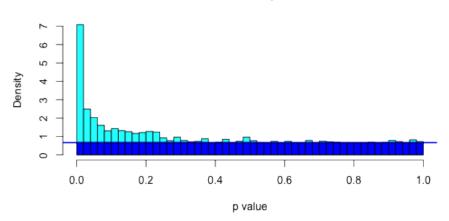
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• The fdr is more relevant, but slightly harder to estimate than FDR because it involves density estimation rather than tail-area estimation.

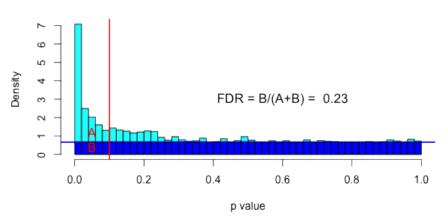
Example: FDR estimation



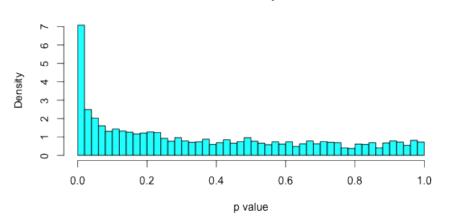
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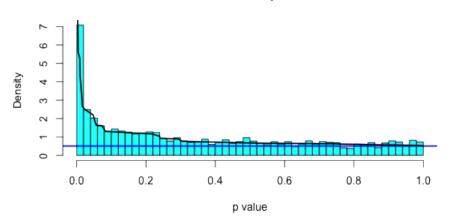
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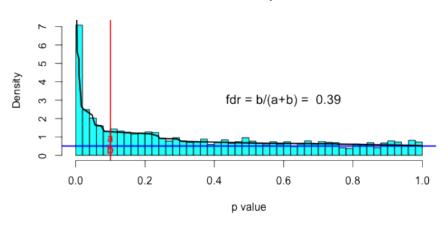
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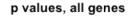
- If some effects are measured very imprecisely, those tests "lack power" and simply add noise
- In particular, such tests increase the estimated number of nulls, and increase the FDR for other tests
- It would seem preferable to simply ignore the tests with very low precision. Summarizing each test by a *p* value (or *Z* score) loses the information about precision.

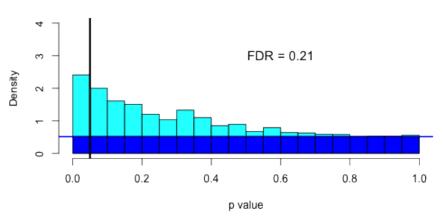
Example: Mouse Heart Data

```
##
        gene
              lv1 lv2 rv1
                                rv2 genelength
## 1
       Itm2a 2236 2174
                         9484 10883
                                           1626
##
      Sergef
               97
                     90
                          341
                                 408
                                           1449
    Fam109a 383
                   314
                         1864
                               2384
                                           2331
        Dhx9 2688 2631 18501
                                           4585
## 4
                              20879
              762
                    674
## 5
       Ssu72
                         2806
                               3435
                                           1446
## 8
      Eif2b2
              736
                    762
                         3081
                               3601
                                           1565
```

 Data on 150 mouse hearts, dissected into left and right ventricle (courtesy Scott Schmemo, Marcelo Nobrega)

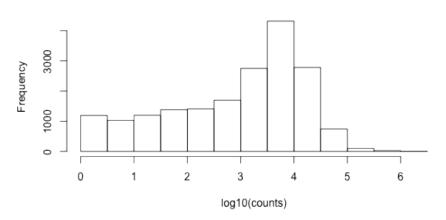
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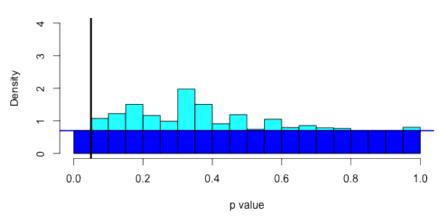
Mouse Data: Counts vary considerably across genes

Distribution of total counts



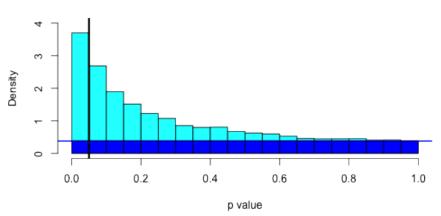
Lower count genes, less power

p values, low count genes



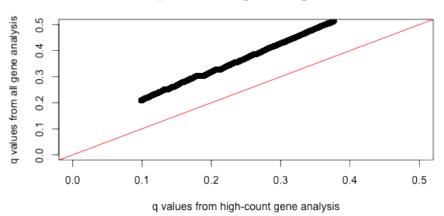
Higher count genes, more power

p values, high count genes



FDR problem 1: low count genes add noise, increase q values

q values for high count genes



FDR problem 1: Summary

 Analyzing p values or Z scores doesn't fully account for measurement precision.

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- The standard qvalue approach assumes that all the p values near 1 are null.
- Analogously, one can assume that all Z scores near 0 are null. Efron refers to this as the "Zero Assumption".
- The ZA allows us to estimate the null proportion, π_0 , using the density of p values near 1 (or Z scores near 0).

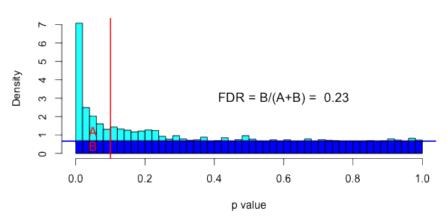
Problem 2: The ZA

• The ZA seems initially natural.

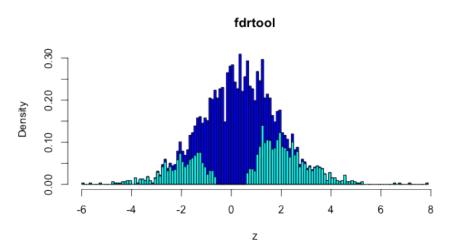
Problem 2: The ZA

- The ZA seems initially natural.
- However, it turns out to imply unrealistic assumptions about the distribution of non-zero effects.

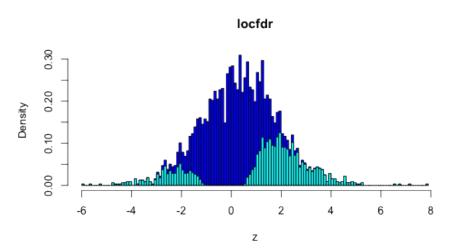
Implied distribution of p values under H_1



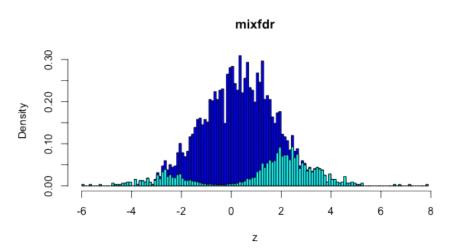
Implied distribution of Z scores under alternative (fdrtool)



Implied distribution of Z scores under alternative (locfdr)



Implied distribution of Z scores under alternative (mixfdr)



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- By summarizing each observation by a Z score or p value, standard fdr tools ignore precision of different measurements
- Standard tools make the ZA, which implies actual effects have a (probably unrealistic) bimodal distribution. [and tends to overestimate π_0 , losing power]
- Also standard tools focus only on zero vs non-zero effects. (eg what if we would like to identify genes that have at least a 2-fold change?)

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- $fdr(Z) \approx \pi_0 N(Z; 0, 1) / f_Z(Z)$



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[From $\hat{\beta}_j \sim N(\beta_j, s_j)$]

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fdr given by

$$p(\beta_j = 0|\hat{\beta}_j) = \pi_0 p(\hat{\beta}_j | \beta_j = 0) / p(\hat{\beta}_j)$$



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- By allowing K large, and σ_k to span a dense grid of values, we get a fairly flexible unimodal symmetric distribution.
- Can approximate, arbitrarily closely, any scale mixture of normals. Includes almost all priors used for sparse regression problems (spike-and-slab, double exponential/Laplace/Bayesian Lasso, horseshoe).

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- If allow a very large number of uniforms this provides the non-parametric mle for g; cf Grenander 1953; Campy + Thomas.

Illustration: g a mixture of 0-centered normals

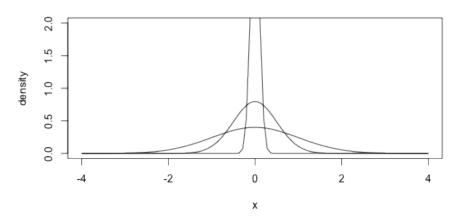


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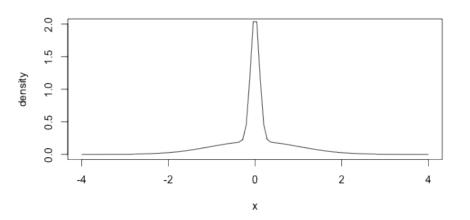


Illustration: g a mixture of 0-anchored uniforms

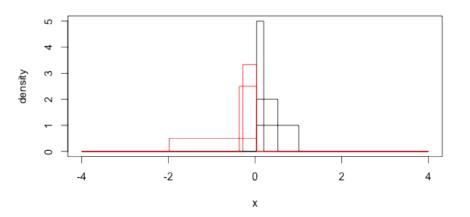
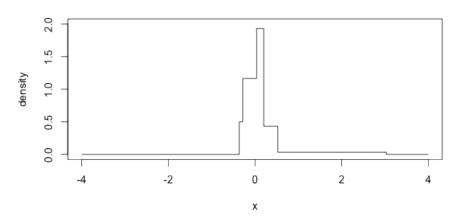


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- However, the data cannot distinguish between $\beta_j=0$ and β_j "very small"
- As a result π_0 is formally unidentifiable. Eg data can never rule out $\pi_0 = 0$.

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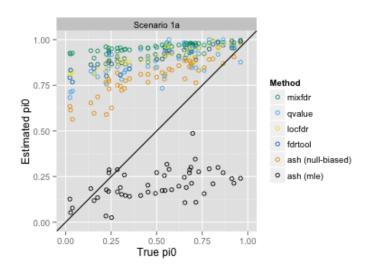
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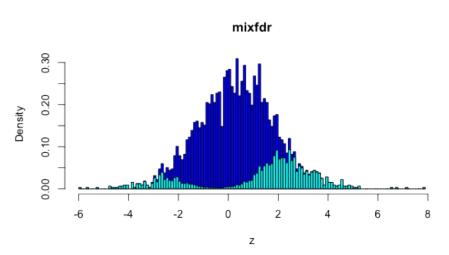
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- In practice, implement upper bound by using penalized likelihood that encourages π_0 to be as big as possible.

Illustration: Simulated Example

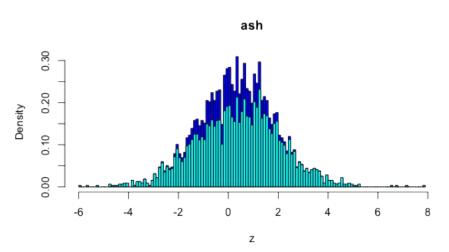


Example: BRCA data

Recall Problem: distribution of alternative Z values multimodal



Problem Fixed: distribution of alternative Z values unimodal



BRCA1: Compare π_0 estimates

```
round(c(hh.fdrtool$param[3], hh.locfdr$fp0[1, 3], hh.mixfdr$p;
2)
```

```
## [1] 0.64 0.74 0.80 0.21
```

BRCA1: Compare number significant at fdr<0.05

```
c(sum(hh.fdrtool$lfdr < 0.05), sum(hh.locfdr$fdr < 0.05), sum (0.05), sum(hh.ashz$ZeroProb < 0.05))
```

```
## [1] 154 171 162 341
```

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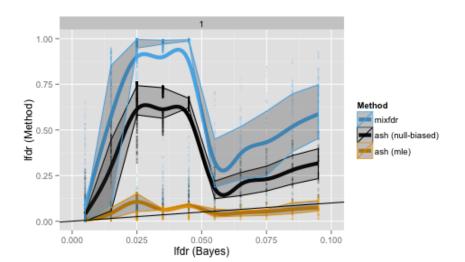
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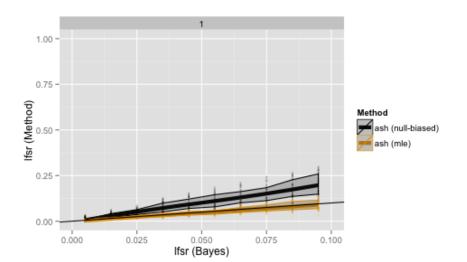
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- That is we replace fdr with False Sign Rate (fsr), the probability that
 if we say an effect is positive (negative), it is not.
- Example: suppose we estimate that $\Pr(\beta_j < 0) = 0.975$ and $\Pr(\beta_j > 0) = 0.025$. Then we report β_j as a "(negative) discovery", and estimate its fsr as 0.025.

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- So for example we can easily compute fdrs for discoveries other than "non-zero" (eg compute $\Pr(\beta_j > 2|\hat{\beta}_j)$).
- And use it to obtain point estimates and credible intervals for each β_j , taking account of information from all the other β_j .

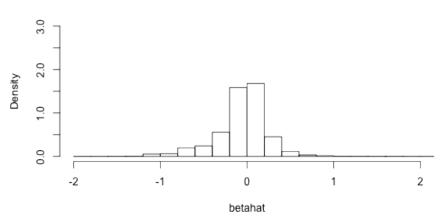
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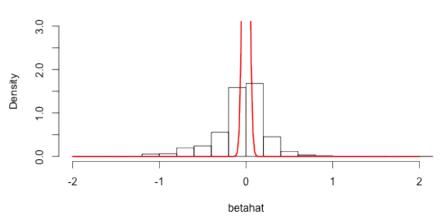
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- So we call the approach "Adaptive Shrinkage" (ASH).



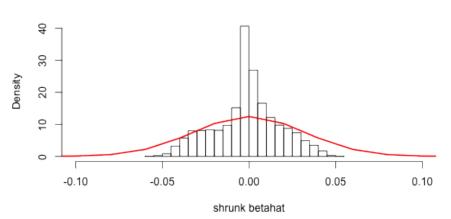
Raw effect size estimates



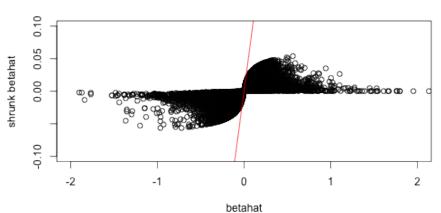
Raw effect size estimates



Shrunken estimates



Estimates vs Shrunken estimates



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- But by using two numbers $(\hat{\beta}, s)$ instead of one (p values or z scores) precision of different measurementscan be better accounted for.
- Unimodal assumption for effects reduces conservatism
- False Sign Rate is more robust to assumptions, and perhaps therefore preferable, than False Discovery Rate.

Other Applications

• Widely applicable: requiring only an estimated effect size and standard error for each object.

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- Currently applying it to wavelet shrinkage applications.

Guarantees?

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- Theory anyone?

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- Including Scott Powers, Mengyin Lu, Tian Sen, Wei Wang, Zhengrong Xing.

Reproducible research

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- Website: http://stephenslab.uchicago.edu

Pandoc Command used

```
pandoc -s -S -i --template=my.beamer -t beamer -V
theme: CambridgeUS -V colortheme: beaver slides.md -o
slides.pdf
(alternative to produce html slides; but figures would need reworking)
pandoc -s -S -i -t dzslides --mathjax slides.md -o
slides.html
Here is my session info:
print(sessionInfo(), locale = FALSE)
## R version 3.0.2 (2013-09-25)
## Platform: x86_64-apple-darwin10.8.0 (64-bit)
##
## attached base packages:
## [1] splines parallel stats
                                       graphics grDevices utils
  [8] methods base
                                         4日 → 4周 → 4 重 → 4 重 → 9 9 ○
```

Some odd things in the data

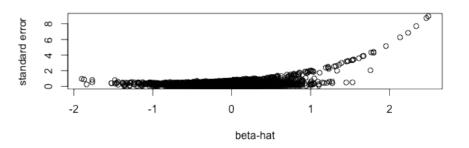


Figure: plot of chunk unnamed-chunk-40

Error: incorrect number of dimensions

A technicality

• Suppose you estimate $\Pr(\beta_j < 0) = 0.98$, $\Pr(\beta_j > 0) = 0.01$, $\Pr(\beta_j = 0) = 0.01$.

A technicality

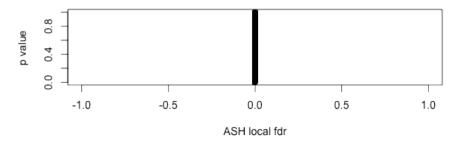
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A technicality

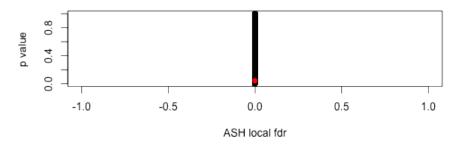
- Suppose you estimate $\Pr(\beta_j < 0) = 0.98$, $\Pr(\beta_j > 0) = 0.01$, $\Pr(\beta_j = 0) = 0.01$.
- Should you declare an fdr of 0.01 or 0.02?
- Maybe fsr makes more sense anyway?

Shrinkage is adaptive to information

Need to fix counts.associate to use fdr method in ash



Shrinkage is adaptive to information

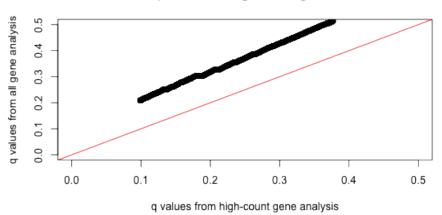


Shrinkage is adaptive to information

```
## gene lv1 lv2 rv1 rv2 pval zdat.ash$lfdr
## 19422 Mgat5b 7 10 320 452 0.03795 0
## 20432 Sec63 1042 1034 5496 6649 0.04908 0
```

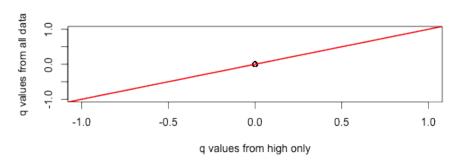
Recall FDR problem 1: q values increased by low count genes

q values for high count genes



2014/2/24

ASH q values more robust to inclusion of low count genes



Compare fitted $f(\beta)$, both estimating π_0 and fixing $\pi_0 = 0$.