

TEMPLATES

SHANGHAI JIAOTONG UNIVERSITY

Metis

Member:

SISHAN LONG
YUTONG XIE
JINGYI CAI

Coach:

YUNQI LI
XUEYUAN ZHAO

Contents

1	数学	3
1.1	FFT	3
1.2	NTT	5
1.3	高斯消元	6
1.4	中国剩余定理	8
1.5	Polya 寻找等价类	10
1.6	拉格朗日插值	11
1.7	欧拉公式	11
1.8	求行列式的值	11
1.9	莫比乌斯	11
1.10	Cayley 公式与森林计数	12
2	数据结构	13
2.1	KD Tree	13
2.2	Splay by xyt	15
2.3	主席树 by cjl	18
2.4	主席树 by xyt	20
2.5	树分治 by xyt	21
2.6	树链剖分 by cjl	23
2.7	树链剖分 by xyt	24
2.8	点分治 by xyt	26
2.9	LCT by xyt	28
3	计算几何	31
3.1	向量旋转	31
3.2	至少被 i 个圆覆盖的面积	31
3.3	计算几何杂	34
3.4	三维变换	35
4	字符串	37
4.1	Manacher	37
4.2	AC-Automachine by cjl	37
4.3	AC-Automachine by xyt	39
4.4	后缀数组	40
4.5	扩展 KMP	41
4.6	回文树	42
4.7	SAM by lss	43
4.8	SAM by xyt	44
5	图论	46
5.1	图论相关	46
5.2	SteinerTree by cjl	46
5.3	LCA by xyt	48
5.4	KM	48
5.5	KM 三次方	50
5.6	Dinic by cjl	51
5.7	网络流 by xyt	52

5.8	最大密度子图	54
5.9	强联通分量	56
5.10	边双联通分量	56
5.11	点双联通分量加构造森林块	57
5.12	K 短路	58
6	其他	60
6.1	Dancing Links(精确覆盖及重复覆盖)	60
6.2	序列莫队	64
6.3	模拟退火	65
6.4	Java	67
6.5	博弈论相关	69
7	Tips	70

1 数学

1.1 FFT

```
const int maxn = 1e6 + 5;
typedef complex<long double> cpb;
int N; cpb a[maxn], aa[maxn], b[maxn], bb[maxn], c[maxn], cc[maxn];
void fft(cpb x[], cpb xx[], int n, int step, int type){
    if(n == 1){
        xx[0] = x[0];
        return;
    }
    int m = n >> 1;
    fft(x, xx, m, step << 1, type);
    fft(x + step, xx + m, m, step << 1, type);
    cpb w = exp(cpb(0., PI * type / m));
    cpb t = 1.;
    for(int i = 0; i < m; ++i){
        cpb t0 = xx[i];
        cpb t1 = xx[i+m];
        xx[i] = t0 + t * t1;
        xx[i+m] = t0 - t * t1;
        t *= w;
    }
}

int main(){
    int n, x;
    scanf("%d", &n);
    for(int i = 0; i < n; ++i) scanf("%d", &x), a[i] = cpb(x, 0.);
    for(int i = 0; i < n; ++i) scanf("%d", &x), b[i] = cpb(x, 0.);
    for(N = 1; N < n + n; N <= 1);
    fft(a, aa, N, 1, 1);
    fft(b, bb, N, 1, 1);
    for(int i = 0; i < N; ++i) cc[i] = aa[i] * bb[i];
    fft(cc, c, N, 1, -1);
    for(int i = 0; i < N; ++i) c[i] = c[i].real() / N;
}

// 复数 递归
typedef complex<double> cpb;
void fft(cpb x[], cpb xx[], int n, int step, int type){ // step 表示步长 代
    码后面举个例子说明一下好了
    if(n == 1){xx[0] = x[0]; return;}
    int m = n >> 1;
    fft(x, xx, m, step << 1, type); // A[0]
    fft(x + step, xx + m, m, step << 1, type); // A[1]
    cpb w = exp(cpb(0, type * pi / m)); // 求原根  $pi / m$  其实就是  $2 * pi / n$ 
    cpb t = 1;
    for(int i = 0; i < m; ++i){
```

```

        cpb t0 = xx[i]; // 这个里面是A[0]的内容
        cpb t1 = xx[i+m]; // 这个里面是A[1]的内容
        xx[i] = t0 + t * t1;
        xx[i+m] = t0 - t * t1;
        t *= w;
    }
}

int main(){
    // main函数我就乱写了 >w<
    a[].get();
    b[].get();
    A = a.length();
    B = b.length();
    for(N = 1; N < A + B; N <= 1);
    fft(a, aa, N, 1, 1);
    fft(b, bb, N, 1, 1);
    for(int i = 0; i < N; ++i) cc[i] = aa[i] * bb[i];
    fft(cc, c, N, 1, -1);
    for(int i = 0; i < N; ++i) c[i] /= N;
    c[].print();
    return 0;
}

// 原根 蝶型
const int p = 7340033;
const int g = 3;
void fft(int xx[], int n, int type){
    // 这里在对二进制位对称的位置进行交换
    for(int i = 0; i < n; ++i){ // i枚举每一个下标
        int j = 0; // j为n位二进制下i的对称
        for(int k = i, m = n - 1; m != 0; j = (j << 1) | (k & 1), k >>= 1, m >>= 1);
        if(i < j) swap(xx[i], xx[j]); // 为了防止换了之后又换回来于是只在 i < j 时交换
    }
    // for代替递归
    for(int m = 1; m < n; m <= 1){ // m为当前讨论区间长度的一半
        int w = powmod(g, (1LL * type * (p - 1) / (m << 1) + p - 1) % (p - 1));
        for(int j = 0; j < n; j += (m << 1)){ // j为当前讨论区间起始位
            // 啊这些都和递归一样了
            int t = 1;
            for(int i = 0; i < m; ++i){
                int t0 = xx[i+j];
                int t1 = 1LL * xx[i+j+m] * t % p;
                xx[i+j] = (t0 + t1) % p;
                xx[i+j+m] = (t0 - t1 + p) % p;
                t = 1LL * t * w % p;
            }
        }
    }
}

```

```

    }
}
int main(){
    // 继续乱写 >w<
    a[].get();
    b[].get();
    A = a.length();
    B = b.length();
    for(N = 1; N < A + B; N <= 1);
    fft(a, N, 1);
    fft(b, N, 1);
    for(int i = 0; i < N; ++i) c[i] = 1LL * a[i] * b[i] % p;
    fft(c, N, -1);
    int inv_N = powmod(N, p - 2);
    for(int i = 0; i < N; ++i) c[i] = 1LL * c[i] * inv_N % p;
    c[].print();
    return 0;
}

```

1.2 NTT

```

void solve(long long number[], int length, int type) {
    for (int i = 1, j = 0; i < length - 1; ++i) {
        for (int k = length; j ^= k >>= 1, ~j & k; );
        if (i < j) {
            std::swap(number[i], number[j]);
        }
    }
    long long unit_p0;
    for (int turn = 0; (1 << turn) < length; ++turn) {
        int step = 1 << turn, step2 = step << 1;
        if (type == 1) {
            unit_p0 = power_mod(MAGIC, (MOD - 1) / step2, MOD);
        } else {
            unit_p0 = power_mod(MAGIC, MOD - 1 - (MOD - 1) / step2, MOD);
        }
        for (int i = 0; i < length; i += step2) {
            long long unit = 1;
            for (int j = 0; j < step; ++j) {
                long long &number1 = number[i + j + step];
                long long &number2 = number[i + j];
                long long delta = unit * number1 % MOD;
                number1 = (number2 - delta + MOD) % MOD;
                number2 = (number2 + delta) % MOD;
                unit = unit * unit_p0 % MOD;
            }
        }
    }
}

```

```

    }
}

void multiply() {
    for (; lowbit(length) != length; ++length);
    solve(number1, length, 1);
    solve(number2, length, 1);
    for (int i = 0; i < length; ++i) {
        number[i] = number1[i] * number2[i] % MOD;
    }
    solve(number, length, -1);
    for (int i = 0; i < length; ++i) {
        answer[i] = number[i] * power_mod(length, MOD - 2, MOD) % MOD;
    }
}

```

1.3 高斯消元

```

int n, r, t;
const int pp=10007;
int e[333][333];
int fa[333];
struct Point{
    int x, y;
    int num;
    Point() {}
    Point(int x, int y, int num = -1) : x(x), y(y), num(num) {}
};
Point p[333];
int dist2(const Point &p) {
    return p.x * p.x + p.y * p.y;
}
Point operator + (const Point &a, const Point &b) {
    return Point(a.x + b.x, a.y + b.y);
}

Point operator - (const Point &a, const Point &b) {
    return Point(a.x - b.x, a.y - b.y);
}

int dot(Point a, Point b) {
    return a.x * b.x + a.y * b.y;
}

int cross(Point a, Point b) {
    return a.x * b.y - a.y * b.x;
}

int find(int x) {

```

```

    if (fa[x] == x) return x;
    else {
        fa[x] = find(fa[x]);
        return fa[x];
    }
}

void addedge(int x, int y) {
    e[x][x]++;
    e[x][y] = -1;
    int fax=find(fa[x]);
    int fay=find(fa[y]);
    if (fax != fay) fa[fax] = fay;
}

int P(int x, int k) {
    if (k == 0) return 0;
    if (k == 1) return x;
    int ret = P(x, k / 2);
    ret = ret *ret % pp;
    if (k & 1) ret = ret * x % pp;
    return ret;
}

void Guass() {
    --n;
    int ans = 1;
    for (int i = 1; i <= n; i++) {
        int pos = i; int mx = 0;
        for (int j = i; j <= n; j++)
            if (abs(e[j][i])>mx) {
                mx = abs(e[j][i]);
                pos = j;
            }
        if (pos != i) {
            for (int j = 1; j <= n; j++) {
                swap(e[i][j], e[pos][j]);
            }
            ans *= -1;
        }
        int inv = P(e[i][i], pp - 2);
        for (int j = i+1; j <= n; j++) {
            int t = inv * e[j][i] % pp;
            for (int k = i; k <= n; k++)
                e[j][k] = (e[j][k] - t*e[i][k]) % pp;
        }
    }
    for (int i = 1; i <= n; i++)
        ans = ans * e[i][i] % pp;
    if (ans < 0) ans += pp;
}

```



```

        cout << ans << endl;
    }
    void doit(int k) {
        Point a[333];
        int m = 0;
        for (int i = 1; i <= n; i++)
            if (i != k && dist2(p[i] - p[k]) <= r*r) {
                bool flag = 1;
                for (int j = 1; j <= n ; j++)
                    if (j != k && j != i) {
                        if (cross(p[j] - p[k], p[i] - p[k]) == 0 && dot(p[j] - p[k], p[i] - p[k]) > 0 && dist2(p[j] - p[k]) < dist2(p[i] - p[k])) {
                            flag = 0;
                            break;
                        }
                    }
                if (flag) addedge(k, i);
            }
    }
}

void solve() {
    cin >> n >> r;
    for (int i = 1; i <= n; i++) {
        scanf("%d%d", &p[i].x, &p[i].y);
    }
    for (int i = 1; i <= n; i++) fa[i] = i;
    memset(e, 0, sizeof(e));
    for (int i = 1; i <= n; i++)
        doit(i);
    for (int i = 2; i <= n; i++)
        if (find(i) != find(i-1)) {
            puts("-1");
            return;
        }
    Guass();
}

int main() {
    cin >> t;
    for (int i = 1; i <= t; i++) solve();
    return 0;
}

```

1.4 中国剩余定理

```

long long extended_Euclid(long long a, long long b, long long &x, long long
&y) { //return gcd(a, b)
    if (b == 0) {

```

```

        x = 1;
        y = 0;
        return a;
    }
    else {
        long long tmp = extended_Euclid(b, a % b, x, y);
        long long t = x;
        x = y;
        y = t - a / b * y;
        return tmp;
    }
}

long long China_Remainder(long long a[], long long b[], int n, long long &
    cir) { //a[]存放两两互质的除数 b[]存放余数
    long long x, y, ans;
    ans = 0; cir = 1;
    for (int i = 1; i <= n; i++) cir *= a[i];
    for (int i = 1; i <= n; i++) {
        long long tmp = cir / a[i];
        extended_Euclid(a[i], tmp, x, y);
        ans = (ans + y * tmp * b[i]) % cir; //可能会爆long long 用
        快速乘法
    }
    return (cir + ans % cir) % cir;
}

bool merge(long long &a1, long long &b1, long long a2, long long b2) { //num
    = b1(mod a1), num = b2(mod a2)
    long long x, y;
    long long d = extended_Euclid(a1, a2, x, y);
    long long c = b2 - b1;
    if (c % d) return false;
    long long p = a2 / d;
    x = (c / d * x % p + p) % p;
    b1 += a1 * x;
    a1 *= a2 / d;
    return true;
}

long long China_Remainder2(long long a[], long long b[], int n) { //a[]存放
    除数(不一定两两互质) b[]存放余数
    long long x, y, ans, cir;
    cir = a[1]; ans = b[1];
    for (int i = 2; i <= n; i++) {
        if (!merge(cir, ans, a[i], b[i])) return -1;
    }
    return (cir + ans % cir) % cir;
}

```

1.5 Polya 寻找等价类

/*

Polya 定理:

设 $G=\{1, 2, 3, \dots, n\}$ 是 $X=\{a_1, a_2, a_3, \dots, a_n\}$ 上一个置换群, 用 m 中颜色对 X 中的元素进行涂色,

那么不同的涂色方案数为: $1/|G|*(m^{C(1)}+m^{C(2)}+m^{C(3)}+\dots+m^{C(k)})$. 其中 $C(k)$ 为置换 k 的循环节的个数。

*/

```
int f[101];
long long mul[101];
bool vis[101];
int pos[101];
int n, m, k;
long long ans = 0, K;
int a[301], b[301];
int getfa(int x) { return !f[x] ? x : (f[x] = getfa(f[x])); }
int g[301][301];
long long check()
{
    int cnt = 0;
    for (int i = 1; i <= n; i++) vis[i] = false;
    for (int i = 1; i <= n; i++)
        if (!vis[i])
        {
            for (int j = i; vis[j] == false; j = pos[j])
                vis[j] = true;
            ++ cnt;
        }
    for (int i = 1; i <= n; i++)
        for (int j = 1; j <= n; j++)
            if (g[i][j] != g[pos[i]][pos[j]]) return 0;
    return mul[cnt];
}
void dfs(int x)
{
    if (x == n + 1)
    {
        long long tmp = check();
        if (tmp) ++ K;
        ans += tmp;
        return ;
    }
    for (int i = 1; i <= n; i++)
        if (!vis[i])
        {
            vis[i] = true;
            pos[x] = i;
```

```

        dfs(x + 1);
        vis[i] = false;
    }
}
int main( )
{
    scanf("%d %d %d", &n, &m, &k);
    mul[0] = 1;
    for (int i = 1; i <= n; i++) mul[i] = mul[i - 1] * k;
    for (int i = 1; i <= m; i++)
        scanf("%d %d", &a[i], &b[i]), g[a[i]][b[i]] ++, g[b[i]][a[i]] ++;
    dfs(1);
    cout << ans / K << endl;
    return 0;
}

```

1.6 拉格朗日插值

$$p_j(x) = \prod_{i \in I_j} \frac{x - x_i}{x_j - x_i}$$

$$L_n(x) = \sum_{j=1}^n y_j p_j(x)$$

1.7 欧拉公式

$V - E + F = C + 1$ C 为联通块数量

$V - E + F = 2 - 2G$ G is the number of genus of surface

1.8 求行列式的值

行列式有很多性质，第 a 行 $*k$ 加到第 b 行上去，行列式的值不变。

三角行列式的值等于对角线元素之积。

第 a 行与第 b 行互换，行列式的值取反。

常数 $*$ 行列式，可以把常数乘到某一行里去。

注意：全是整数并取模的话当然需要逆元

1.9 莫比乌斯

$$\sum_{d|n} \mu(d) = [n == 1]$$

$$\mu(m) = \begin{cases} (-1)^r & m = p_1 p_2 \dots p_r \\ 0 & p^2 | n \end{cases}$$

某个 Mobius 推倒:

$$\begin{aligned}
& \sum_{i=1}^n \sum_{j=1}^m lcm(i, j) \\
&= \sum_{d=1}^n \sum_{i=1}^n \sum_{j=1}^m [gcd(i, j) == d] \frac{ij}{d} \\
&= \sum_{d=1}^n \sum_{i=1}^{n/d} \sum_{j=1}^{m/d} [gcd(i, j) == 1] ijd \\
&= \sum_{d=1}^n d \sum_{i=1}^{n/d} \sum_{j=1}^{m/d} i * j \sum_{d' | i, d' | j} \mu(d') \\
&= \sum_{d=1}^n \sum_{d'=1}^{n/d} \sum_{i=1}^{n/dd'} \sum_{j=1}^{m/dd'} dijd'^2 \mu(d') \\
&\text{令 } D = dd' \quad s(x, y) = \frac{xy(x+1)(y+1)}{4} \\
&= \sum_{D=1}^n s(\frac{n}{D}, \frac{m}{D}) D \sum_{d' | D} d' \mu(d')
\end{aligned}$$

$$\mu(n) = \begin{cases} 1 & \text{若 } n = 1 \\ (-1)^k & \text{若 } n \text{ 无平方数因子, 且 } n = p_1 p_2 \dots p_k \\ 0 & \text{若 } n \text{ 有大于 1 的平方数因数} \end{cases}$$

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & \text{若 } n = 1 \\ 0 & \text{其他情况} \end{cases}$$

$$g(n) = \sum_{d|n} f(d) \Leftrightarrow f(n) = \sum_{d|n} \mu(d) g(\frac{n}{d}), g(x) = \sum_{n=1}^{[x]} f(\frac{x}{n}) \Leftrightarrow f(x) = \sum_{n=1}^{[x]} \mu(n) g(\frac{x}{n})$$

1.10 Cayley 公式与森林计数

Cayley 公式是说, 一个完全图 K_n 有 n^{n-2} 棵生成树, 换句话说 n 个节点的带标号的无根树有 n^{n-2} 个。

令 $g[i]$ 表示点数为 i 的森林个数, $f[i]$ 表示点数为 i 的生成树计数 ($f[i] = i^{i-2}$) 那么便有

$$g[i] = \sum (g[i-j] \times cnr[i-1][j-1] \times f[j])$$

$$g[i] = \sum \frac{g[i-j] \times fac[i-1] \times f[j]}{fac[j-1] \times fac[i-j]} = fac[i-1] \times \sum (\frac{f[j]}{fac[j-1]} \times \frac{g[i-j]}{fac[i-j]})$$

2 数据结构

2.1 KD Tree

```
long long norm(const long long &x) {
    // For manhattan distance
    return std::abs(x);
    // For euclid distance
    return x * x;
}

struct Point {
    int x, y, id;
    const int& operator [] (int index) const {
        if (index == 0) {
            return x;
        } else {
            return y;
        }
    }
}

friend long long dist(const Point &a, const Point &b) {
    long long result = 0;
    for (int i = 0; i < 2; ++i) {
        result += norm(a[i] - b[i]);
    }
    return result;
}

} point[N];

struct Rectangle {
    int min[2], max[2];
    Rectangle() {
        min[0] = min[1] = INT_MAX;
        max[0] = max[1] = INT_MIN;
    }
    void add(const Point &p) {
        for (int i = 0; i < 2; ++i) {
            min[i] = std::min(min[i], p[i]);
            max[i] = std::max(max[i], p[i]);
        }
    }
}

long long dist(const Point &p) {
    long long result = 0;
    for (int i = 0; i < 2; ++i) {
        // For minimum distance
        result += norm(std::min(std::max(p[i], min[i]), max[i]) - p[i]);
        // For maximum distance
        result += std::max(norm(max[i] - p[i]), norm(min[i] - p[i]));
    }
    return result;
}
```

```

    }
};
struct Node {
    Point seperator;
    Rectangle rectangle;
    int child[2];
    void reset(const Point &p) {
        seperator = p;
        rectangle = Rectangle();
        rectangle.add(p);
        child[0] = child[1] = 0;
    }
} tree[N << 1];
int size, pivot;
bool compare(const Point &a, const Point &b) {
    if (a[pivot] != b[pivot]) {
        return a[pivot] < b[pivot];
    }
    return a.id < b.id;
}
int build(int l, int r, int type = 1) {
    pivot = type;
    if (l >= r) {
        return 0;
    }
    int x = ++size;
    int mid = l + r >> 1;
    std::nth_element(point + l, point + mid, point + r, compare);
    tree[x].reset(point[mid]);
    for (int i = l; i < r; ++i) {
        tree[x].rectangle.add(point[i]);
    }
    tree[x].child[0] = build(l, mid, type ^ 1);
    tree[x].child[1] = build(mid + 1, r, type ^ 1);
    return x;
}
int insert(int x, const Point &p, int type = 1) {
    pivot = type;
    if (x == 0) {
        tree[++size].reset(p);
        return size;
    }
    tree[x].rectangle.add(p);
    if (compare(p, tree[x].seperator)) {
        tree[x].child[0] = insert(tree[x].child[0], p, type ^ 1);
    } else {
        tree[x].child[1] = insert(tree[x].child[1], p, type ^ 1);
    }
}

```

```

    return x;
}
// For minimum distance
void query(int x, const Point &p, std::pair<long long, int> &answer, int
type = 1) {
    pivot = type;
    if (x == 0 || tree[x].rectangle.dist(p) > answer.first) {
        return;
    }
    answer = std::min(answer,
        std::make_pair(dist(tree[x].seperator, p), tree[x].seperator.id
        ));
    if (compare(p, tree[x].seperator)) {
        query(tree[x].child[0], p, answer, type ^ 1);
        query(tree[x].child[1], p, answer, type ^ 1);
    } else {
        query(tree[x].child[1], p, answer, type ^ 1);
        query(tree[x].child[0], p, answer, type ^ 1);
    }
}
std::priority_queue<std::pair<long long, int> > answer;
void query(int x, const Point &p, int k, int type = 1) {
    pivot = type;
    if (x == 0 ||
        ((int)answer.size() == k && tree[x].rectangle.dist(p) > answer.top().
        first) {
        return;
    }
    answer.push(std::make_pair(dist(tree[x].seperator, p), tree[x].seperator
        .id));
    if ((int)answer.size() > k) {
        answer.pop();
    }
    if (compare(p, tree[x].seperator)) {
        query(tree[x].child[0], p, k, type ^ 1);
        query(tree[x].child[1], p, k, type ^ 1);
    } else {
        query(tree[x].child[1], p, k, type ^ 1);
        query(tree[x].child[0], p, k, type ^ 1);
    }
}
}

```

2.2 Splay by xyt

```

struct Splay{
    int tot, rt;
    struct Node{

```



```

        int lson, rson, fath, sz;
        int data;
        bool lazy;
};
Node nd[MAXN];
void reverse(int i){
    if(!i) return;
    swap(nd[i].lson, nd[i].rson);
    nd[i].lazy = true;
}
void push_down(int i){
    if(!i || !nd[i].lazy) return;
    reverse(nd[i].lson);
    reverse(nd[i].rson);
    nd[i].lazy = false;
}
void zig(int i){
    int j = nd[i].fath;
    int k = nd[j].fath;
    if(k && j == nd[k].lson) nd[k].lson = i;
    else if(k) nd[k].rson = i;
    nd[i].fath = k;
    nd[j].fath = i;
    nd[nd[i].rson].fath = j;
    nd[j].lson = nd[i].rson;
    nd[i].rson = j;
    nd[i].sz = nd[j].sz;
    nd[j].sz = nd[nd[j].lson].sz + nd[nd[j].rson].sz + 1;
}
void zag(int i){
    int j = nd[i].fath;
    int k = nd[j].fath;
    if(k && j == nd[k].lson) nd[k].lson = i;
    else if(k) nd[k].rson = i;
    nd[i].fath = k;
    nd[j].fath = i;
    nd[nd[i].lson].fath = j;
    nd[j].rson = nd[i].lson;
    nd[i].lson = j;
    nd[i].sz = nd[j].sz;
    nd[j].sz = nd[nd[j].lson].sz + nd[nd[j].rson].sz + 1;
}
void down_path(int i){
    if(nd[i].fath) down_path(nd[i].fath);
    push_down(i);
}
void splay(int i){
    down_path(i);

```

```

        while(nd[i].fath){
            int j = nd[i].fath;
            if(nd[j].fath == 0){
                if(i == nd[j].lson) zig(i);
                else zag(i);
            }else{
int k = nd[j].fath;
if(j == nd[k].lson){
    if(i == nd[j].lson) zig(j), zig(i);
    else zag(i), zig(i);
}else{
    if(i == nd[j].rson) zag(j), zag(i);
    else zig(i), zag(i);
}
            }
        }
        rt = i;
    }
int insert(int stat){ // 插入信息
    int i = rt;
    ++tot;
    nd[tot].data = stat;
    nd[tot].sz = 1;
    if(!nd[i].sz){
        nd[tot].fath = 0;
        rt = tot;
        return tot;
    }
    while(i){
        ++nd[i].sz;
        if(stat < nd[i].data){
if(nd[i].lson) i = nd[i].lson;
else{
    nd[i].lson = tot;
    break;
}
        }else{
if(nd[i].rson) i = nd[i].rson;
else{
    nd[i].rson = tot;
    break;
}
        }
    }
    nd[tot].fath = i;
    splay(tot);
    return tot;
}
}

```

```

void delet(int i){ // 删除信息
    if(!i) return;
    splay(i);
    int ls = nd[i].lson;
    int rs = nd[i].rson;
    nd[ls].fath = nd[rs].fath = 0;
    nd[i].lson = nd[i].rson = 0;
    if(ls == 0){
        rt = rs;
        nd[rs].fath = 0;
    }else{
        rt = ls;
        while(nd[ls].rson) ls = nd[ls].rson;
        splay(ls);
        nd[ls].fath = 0;
        nd[rs].fath = ls;
        nd[ls].rson = rs;
    }
    nd[rt].sz += nd[nd[rt].rson].sz;
}

int get_rank(int i){ // 查询节点编号为 i 的 rank
    splay(i);
    return nd[nd[i].rson].sz + 1;
}

int find(int stat){ // 查询信息为 stat 的节点编号
    int i = rt;
    while(i){
        if(stat < nd[i].data) i = nd[i].lson;
        else if(stat > nd[i].data) i = nd[i].rson;
        else return i;
    }
    return i;
}

int get_kth_max(int k){ // 查询第 k 大 返回其节点编号
    int i = rt;
    while(i){
        if(k <= nd[nd[i].rson].sz) i = nd[i].rson;
        else if(k > nd[nd[i].rson].sz + 1) k -= nd[nd[i].rson].sz + 1, i = nd[i].lson;
        else return i;
    }
    return i;
}

}sp;

```

2.3 主席树 by cjy

```

const int N = 100005;
struct Tree {
    int l, r, L, R, x;
} h[(int)3e6];
int n, m, q, a[N], b[N];
int root[N], tot;
void Build(int x, int l, int r) {
    h[x].l = l; h[x].r = r; h[x].x = 0;
    if (l < r) {
        int m = (l + r) / 2;
        h[x].L = ++tot; Build(tot, l, m);
        h[x].R = ++tot; Build(tot, m + 1, r);
    }
}
void build(int x, int y, int num) {
    int l = h[y].l, r = h[y].r;
    h[x].l = l; h[x].r = r;
    h[x].x = h[y].x + 1; //-----
    if (l < r) {
        int m = (l + r) / 2;
        if (num <= m) {
            h[x].L = ++tot; build(tot, h[y].L, num);
            h[x].R = h[y].R;
        }
        else {
            h[x].L = h[y].L;
            h[x].R = ++tot; build(tot, h[y].R, num);
        }
        h[x].x = h[h[x].L].x + h[h[x].R].x;
    }
}
int find(int x, int y, int k) {
    if (h[x].l == h[x].r) return h[x].l;
    int t = h[h[y].L].x - h[h[x].L].x;
    if (t >= k) return find(h[x].L, h[y].L, k);
    else return find(h[x].R, h[y].R, k - t);
}
int main() {
    scanf("%d%d", &n, &q);
    for (int i = 1; i <= n; i++) {
        scanf("%d", &a[i]);
        b[i] = a[i];
    }
    sort(b + 1, b + n + 1);
    m = unique(b + 1, b + n + 1) - (b + 1);
    for (int i = 1; i <= n; i++)
        a[i] = lower_bound(b + 1, b + m + 1, a[i]) - (b + 1) + 1;
    root[0] = tot = 1;
}

```

```

Build(1, 1, m); //-----
for (int i = 1; i <= n; i++) {
    root[i] = ++tot;
    build(tot, root[i - 1], a[i]);
}
for(int i = 1; i <= q; i++) {
    int l, r, k;
    scanf("%d%d%d", &l, &r, &k);
    printf("%d\n", b[find(root[l - 1], root[r], k)]);
}
return 0;
}

```

2.4 主席树 by xyt

```

const int maxn = 1e5 + 5;
const int inf = 1e9 + 1;
struct segtree{
    int tot, rt[maxn];
    struct node{
        int lson, rson, size;
    }nd[maxn*40];
    void insert(int &i, int left, int right, int x){
        int j = ++tot;
        int mid = (left + right) >> 1;
        nd[j] = nd[i];
        nd[j].size++;
        i = j;
        if(left == right) return;
        if(x <= mid) insert(nd[j].lson, left, mid, x);
        else insert(nd[j].rson, mid + 1, right, x);
    }

    int query(int i, int j, int left, int right, int k){
        if(left == right) return left;
        int mid = (left + right) >> 1;
        if(nd[nd[j].lson].size - nd[nd[i].lson].size >= k) return
            query(nd[i].lson, nd[j].lson, left, mid, k);
        else return query(nd[i].rson, nd[j].rson, mid + 1, right, k -
            (nd[nd[j].lson].size - nd[nd[i].lson].size));
    }
}st;
int n, m;
int a[maxn], b[maxn], rnk[maxn], mp[maxn];
bool cmp(int i, int j){return a[i] < a[j];}
int main(){
    scanf("%d%d", &n, &m);
    for(int i = 1; i <= n; ++i) scanf("%d", &a[i]);

```

```

    for(int i = 1; i <= n; ++i) rnk[i] = i;
    sort(rnk + 1, rnk + 1 + n, cmp);
    a[0] = inf;
    for(int i = 1, j = 0; i <= n; ++i){
        int k = rnk[i], kk = rnk[i-1];
        if(a[k] != a[kk]) b[k] = ++j;
        else b[k] = j;
        mp[b[k]] = a[k];
    }
    for(int i = 1; i <= n; ++i) st.insert(st.rt[i] = st.rt[i-1], 1, n, b[i]);
    for(int i = 1; i <= m; ++i){
        int x, y, k;
        scanf("%d%d%d", &x, &y, &k);
        printf("%d\n", mp[st.query(st.rt[x-1], st.rt[y], 1, n, k)]);
    }
    return 0;
}

```

2.5 树分治 by xyt

```

/*询问树上有多少对pair距离不超过k
  每次找重心 经过一些容斥
  求经过重心与不经过重心pair数*/
const int maxn = 1e4 + 5;
vector<pii> mp[maxn];
void add_edge(int u, int v, int d){
    mp[u].push_back(make_pair(v, d));
    mp[v].push_back(make_pair(u, d));
}
int n, ans, limit, gra, min_maxx;
int sz[maxn];
bool flag[maxn];
vector<int> vec;
void get_gra(int u, int fa, int nowsize){
    sz[u] = 1;
    int maxx = 0;
    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l].first;
        if(v == fa || flag[v]) continue;
        get_gra(v, u, nowsize);
        sz[u] += sz[v];
        maxx = max(maxx, sz[v]);
    }
    maxx = max(maxx, nowsize - sz[u]);
    if(maxx < min_maxx) min_maxx = maxx, gra = u;
}

```

```

void get_dist(int u, int fa, int d){
    vec.push_back(d);
    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l].first;
        if(v == fa || flag[v]) continue;
        get_dist(v, u, d + mp[u][l].second);
    }
}

int calc(int u, int delta){
    int rtn = 0;
    vec.clear();
    get_dist(u, 0, 0);
    sort(vec.begin(), vec.end());
    int m = vec.size();
    for(int i = 0, j = m - 1; i < j; ++i){
        while(i < j && vec[i] + vec[j] + delta > limit) --j;
        rtn += j - i;
    }
    return rtn;
}

void devide(int u, int nowsize){
    min_maxx = maxx;
    get_gra(u, 0, nowsize);
    flag[u=gra] = true;
    ans += calc(u, 0);
    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l].first;
        if(flag[v]) continue;
        ans -= calc(v, mp[u][l].second * 2);
        devide(v, sz[v] > sz[u] ? nowsize - sz[u] : sz[v]);
    }
}

void init(){
    ans = 0;
    for(int i = 1; i <= n; ++i) mp[i].clear();
    memset(flag, 0, sizeof flag);
}

void work(){
    init();
    for(int i = 1; i < n; ++i){
        int u, v, d;
        scanf("%d%d%d", &u, &v, &d);
        add_edge(u, v, d);
    }
    devide(1, n);
    printf("%d\n", ans);
}

```

```

int main(){
    while(true){
        scanf("%d%d", &n, &limit);
        if(n == 0) break;
        work();
    }
    return 0;
}

```

2.6 树链剖分 by cjy

```

const int N = 800005;
int n, m, Max, b[N], edge_pos[N], path[N];
int tot, id[N * 2], nxt[N * 2], lst[N], val[N * 2];
int fa[N], siz[N], dep[N], hvy[N], top[N], pos[N];
struct Tree {
    int l, r;
    int mn, mx, sgn;
} h[N * 4];
void Add(int x, int y, int z) {
    id[++tot] = y; nxt[tot] = lst[x]; lst[x] = tot; val[tot] = z;
}
void dfs1(int x, int Fa) {
    fa[x] = Fa;
    siz[x] = 1;
    dep[x] = dep[Fa] + 1;
    int max_size = 0;
    for (int i = lst[x]; i; i = nxt[i]) {
        int y = id[i];
        if (y != Fa) {
            path[y] = i; //-----
            dfs1(y, x);
            if (siz[y] > max_size) {
                max_size = siz[y];
                hvy[x] = y;
            }
            siz[x] += siz[y];
        }
    }
}
void dfs2(int x, int Top) {
    top[x] = Top;
    pos[x] = ++m;
    b[m] = val[path[x]]; //b[m] = val[x];
    edge_pos[path[x] / 2] = m; //when change only one edge's value
    if (hvy[x]) dfs2(hvy[x], Top); //heavy son need to be visited first
    for (int i = lst[x]; i; i = nxt[i]) {

```



```

        int y = id[i];
        if (y == fa[x] || y == hvy[x]) continue;
        dfs2(y, y);
    }
}

void work(int x, int y) {
    int X = top[x], Y = top[y];
    if (X == Y) {
        if (dep[x] < dep[y]) Negate(1, pos[x] + 1, pos[y]);
        else if (dep[x] > dep[y]) Negate(1, pos[y] + 1, pos[x]);
        //if (dep[x] <= dep[y]) Negate(1, pos[x], pos[y]);
        //else Negate(1, pos[y], pos[x]);
        return ;
    }
    if (dep[X] >= dep[Y]) {
        Negate(1, pos[X], pos[x]);
        work(fa[X], y);
    }
    else {
        Negate(1, pos[Y], pos[y]);
        work(x, fa[Y]);
    }
}

int main() {
    tot = 1; memset(lst, 0, sizeof(lst));
    memset(hvy, 0, sizeof(hvy));
    (Add_edge)
    dep[0] = 0; dfs1(1, 0); //the root is 1
    m = 0; dfs2(1, 1);
    build(1, 1, n);
    Change(1, edge_pos[x], y); //change one edge's value directly in
    Tree
    work(x, y); //change value of a chain
    return 0;
}

```

2.7 树链剖分 by xyt

```

struct qtree{
    int tot;
    struct node{
        int hson, top, size, dpth, papa, newid;
    }nd[maxn];

    void find(int u, int fa, int d){
        nd[u].hson = 0;
        nd[u].size = 1;
    }
}

```

```

        nd[u].papa = fa;
        nd[u].dpth = d;
        int max_size = 0;
        for(int l = 0; l < mp[u].size(); ++l){
            int v = mp[u][l].first;
            if(v == fa) continue;
            f[mp[u][l].second.second] = v;
            find(v, u, d + 1);
            nd[u].size += nd[v].size;
            if(max_size < nd[v].size){
                max_size = nd[v].size;
                nd[u].hson = v;
            }
        }
    }

    void connect(int u, int t){
        nd[u].top = t;
        nd[u].newid = ++tot;
        if(nd[u].hson != 0) connect(nd[u].hson, t);
        for(int l = 0; l < mp[u].size(); ++l){
            int v = mp[u][l].first;
            if(v == nd[u].papa || v == nd[u].hson) continue;
            connect(v, v);
        }
    }

    int query(int u, int v){
        int rtn = -inf;
        while(nd[u].top != nd[v].top){
            if(nd[nd[u].top].dpth < nd[nd[v].top].dpth) swap(u, v);
            rtn = max(rtn, st.query(1, 1, n, nd[nd[u].top].newid, nd[u].newid));
            u = nd[nd[u].top].papa;
        }
        if(nd[u].dpth > nd[v].dpth) swap(u, v);
        rtn = max(rtn, st.query(1, 1, n, nd[u].newid, nd[v].newid));
        return rtn;
    }

    void modify(int u, int v){
        while(nd[u].top != nd[v].top){
            if(nd[nd[u].top].dpth < nd[nd[v].top].dpth) swap(u, v);
            st.modify(1, 1, n, nd[nd[u].top].newid, nd[u].newid);
            u = nd[nd[u].top].papa;
        }
        if(nd[u].dpth > nd[v].dpth) swap(u, v);
    }

```

```

        st.modify(1, 1, n, nd[u].newid + 1, nd[v].newid);
    }
    void clear(){
        tot = 0;
        nd[0].hson = nd[0].top = nd[0].size = nd[0].dpth = nd[0].
            papa = nd[0].newid = 0;
        for(int i = 1; i <= n; ++i) nd[i] = nd[0];
    }
}qt;

```

2.8 点分治 by xyt

```

// POJ 1741
// 询问一棵树中有多少对点距离不超过 k
typedef pair<int, int> pii;
const int maxn = 1e4 + 5;
vector<pii> mp[maxn];
void add_edge(int u, int v, int d){
    mp[u].push_back(make_pair(v, d));
    mp[v].push_back(make_pair(u, d));
}
int n, ans, limit, gra, min_maxx;
int sz[maxn];
bool flag[maxn];
vector<int> vec;
void get_gra(int u, int fa, int nowsize){
    sz[u] = 1;
    int maxx = 0;
    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l].first;
        if(v == fa || flag[v]) continue;
        get_gra(v, u, nowsize);
        sz[u] += sz[v];
        maxx = max(maxx, sz[v]);
    }
    maxx = max(maxx, nowsize - sz[u]);
    if(maxx < min_maxx) min_maxx = maxx, gra = u;
}
void get_dist(int u, int fa, int d){
    vec.push_back(d);
    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l].first;
        if(v == fa || flag[v]) continue;
        get_dist(v, u, d + mp[u][l].second);
    }
}
int calc(int u, int delta){

```

```

    int rtn = 0;
    vec.clear();
    get_dist(u, 0, 0);
    sort(vec.begin(), vec.end());
    int m = vec.size();
    for(int i = 0, j = m - 1; i < j; ++i){
        while(i < j && vec[i] + vec[j] + delta > limit) --j;
        rtn += j - i;
    }
    return rtn;
}

void devide(int u, int nowsize){
    min_maxx = maxx;
    get_gra(u, 0, nowsize);
    flag[u=gra] = true;
    ans += calc(u, 0); // 加上经过重心的答案
    for(int l = 0; l < mp[u].size(); ++l){ // 容斥掉同一棵子树中经过重心的答案
        int v = mp[u][l].first;
        if(flag[v]) continue;
        ans -= calc(v, mp[u][l].second * 2);
        devide(v, sz[v] > sz[u] ? nowsize - sz[u] : sz[v]);
    }
}

void init(){
    ans = 0;
    for(int i = 1; i <= n; ++i) mp[i].clear();
    memset(flag, 0, sizeof flag);
}

void work(){
    init();
    for(int i = 1; i < n; ++i){
        int u, v, d;
        scanf("%d%d%d", &u, &v, &d);
        add_edge(u, v, d);
    }
    devide(1, n);
    printf("%d\n", ans);
}

int main(){
    while(true){
        scanf("%d%d", &n, &limit);
        if(n == 0) break;
        work();
    }
    return 0;
}

```

2.9 LCT by xyt

// 这个有些地方有点问题... // 标注部分

```
const int MAXN = 2e5 + 5;
int n, m;
struct Lct{
    struct Node{
        int sum;
        int lson, rson, fath, ance;
        bool lazy;
    };
    Node nd[MAXN];
    void push_up(int i){
        nd[i].sum = nd[nd[i].lson].sum + nd[nd[i].rson].sum + 1;
    }
    void reverse(int i){ //
        if(!i) return;
        swap(nd[i].lson, nd[i].rson);
        nd[i].lazy = true;
    }
    void push_down(int i){ //
        if(!i || !nd[i].lazy) return;
        reverse(nd[i].lson);
        reverse(nd[i].rson);
        nd[i].lazy = false;
    }
    void zig(int i){
        int j = nd[i].fath;
        int k = nd[j].fath;
        if(k && j == nd[k].lson) nd[k].lson = i;
        else if(k) nd[k].rson = i;
        nd[i].fath = k;
        nd[j].fath = i;
        nd[nd[i].rson].fath = j;
        nd[j].lson = nd[i].rson;
        nd[i].rson = j;
        nd[i].ance = nd[j].ance;
        push_up(j);
        push_up(i);
    }
    void zag(int i){
        int j = nd[i].fath;
        int k = nd[j].fath;
        if(k && j == nd[k].lson) nd[k].lson = i;
        else if(k) nd[k].rson = i;
        nd[i].fath = k;
        nd[j].fath = i;
        nd[nd[i].lson].fath = j;
```

```

        nd[j].rson = nd[i].lson;
        nd[i].lson = j;
        nd[i].ance = nd[j].ance;
        push_up(j);
        push_up(i);
    }
    void down_path(int i){ //
        if(nd[i].fath) down_path(nd[i].fath);
        push_down(i);
    }
    void splay(int i){
        down_path(i);
        while(nd[i].fath){
            int j = nd[i].fath;
            if(nd[j].fath == 0){
                if(i == nd[j].lson) zig(i);
                else zag(i);
            }else{
                int k = nd[j].fath;
                if(j == nd[k].lson){
                    if(i == nd[j].lson) zig(j), zig(i);
                    else zag(i), zig(i);
                }else{
                    if(i == nd[j].rson) zag(j), zag(i);
                    else zig(i), zag(i);
                }
            }
        }
    }
}

void access(int i){
    int j = 0;
    while(i){
        splay(i);
        if(nd[i].rson){
            nd[nd[i].rson].ance = i;
            nd[nd[i].rson].fath = 0;
        }
        nd[i].rson = j;
        nd[j].fath = i;
        push_up(i);
        j = i;
        i = nd[i].ance;
    }
}

void set_root(int i){ //
    access(i);
    splay(i);
}

```

```

        reverse(i);
    }
    int find_root(int i){ //
        access(i);
        splay(i);
        while(nd[i].lson) i = nd[i].lson;
        splay(i);
        return i;
    }
    void link(int i, int j){ //
        set_root(i);
        nd[i].ance = j;
        access(i);
    }
    void cut(int i){ //
        access(i);
        splay(i);
        nd[nd[i].lson].ance = nd[i].ance;
        nd[nd[i].lson].fath = 0;
        nd[i].lson = 0;
        nd[i].ance = 0;
    }
};
Lct lct;
void query(){
    int pos;
    scanf("%d", &pos);
    ++pos;
    lct.access(pos);
    lct.splay(pos);
    printf("%d\n", lct.nd[pos].sum - 1);
}
void modify(){
    int pos, fath;
    scanf("%d%d", &pos, &fath);
    ++pos, fath += pos;
    if(fath > n) fath = n + 1;
    lct.splay(pos);
    if(lct.nd[pos].lson){
        lct.nd[lct.nd[pos].lson].ance = lct.nd[pos].ance;
        lct.nd[lct.nd[pos].lson].fath = 0;
        lct.nd[pos].lson = 0;
    }
    lct.nd[pos].ance = fath;
}
int main(){
    scanf("%d", &n);
    for(int i = 1; i <= n; ++i){

```

```

        int k;
        scanf("%d", &k);
        k += i;
        if(k > n) k = n + 1;
        lct.nd[i].ance = k;
    }
    for(int i = 1; i <= n + 1; ++i) lct.nd[i].sum = 1;
    scanf("%d", &m);
    for(int i = 1; i <= m; ++i){
        int k;
        scanf("%d", &k);
        if(k == 1) query();
        else modify();
    }
    return 0;
}

```

3 计算几何

3.1 向量旋转

```

void rotate(double theta){
    double coss = cos(theta), sinn = sin(theta);
    double tx = x * coss - y * sinn;
    double ty = x * sinn + y * coss;
    x = tx, y = ty;
}

```

3.2 至少被 i 个圆覆盖的面积

时间复杂度: $n^2 \log n$

```

const double pi=acos(-1);
const double eps=1e-12;
double sqr(double x){
    return x*x;
}
double sign(double x){
    return (x>eps)-(x<-eps);
}
double ans[2333];
int n;
struct P{
    double x,y;
    P(){}
    P(double x,double y):x(x),y(y){}
    void scan(){scanf("%lf%lf",&x,&y);}
    double sqrlen(){return (sqr(x)+sqr(y));}
}

```



```

    double len(){return sqrt(sqr(x)+sqr(y));}
    P zoom(double d){
        double l=d/len();
        return P(l*x,l*y);
    }
    P rev(){
        return P(y,-x);
    }
}dvd,a[233];
P centre[233];
double atan2(P x){
    return atan2(x.y,x.x);
}
P operator+(P a,P b){
    return P(a.x+b.x,a.y+b.y);
}
P operator-(P a,P b){
    return P(a.x-b.x,a.y-b.y);
}
double operator*(P a,P b){
    return a.x*b.y-a.y*b.x;
}
P operator*(double a,P b){
    return P(a*b.x,a*b.y);
}
P operator/(P a,double b){
    return P(a.x/b,a.y/b);
}
struct circle{
    double r;P o;
    circle(){}
    void scan(){
        o.scan();
        //scanf("%lf",&r);
    }
}cir[2333];
struct arc{
    double theta;
    int delta;
    P p;
    arc(){}
    arc(double theta,P p,int d):theta(theta),p(p),delta(d){}
}vec[4444];
int nV;
bool operator<(arc a,arc b){
    return a.theta+eps<b.theta;
}
int cnt;

```

```

void psh(double t1,P p1,double t2,P p2){
    if(t2+eps<t1)
        cnt++;
    vec[nV++]=arc(t1,p1,1);
    vec[nV++]=arc(t2,p2,-1);
}
void combine(int d,double area,P o){
    if(sign(area)==0) return;
    centre[d]=1/(ans[d]+area)*(ans[d]*centre[d]+area*o);
    ans[d]+=area;
}
bool equal(double x,double y){
    return x+eps>y and y+eps>x;
}
bool equal(P a,P b){
    return equal(a.x,b.x) and equal(a.y,b.y);
}
bool equal(circle a,circle b){
    return equal(a.o,b.o) and equal(a.r,b.r);
}
P p[4];
double cub(double x){return x*x*x;}

int main(){
    n = 0;
    cin>>n;
    for(int i = 0; i < n; ++i) cir[i].o.scan(), cin>>cir[i].r;
    for(int i = 0; i <= n; ++i) ans[i] = 0.0;
    for(int i = 0; i <= n; ++i) centre[i] = P(0, 0);
    for(int i=0;i<n;i++){
        dvd=cir[i].o-P(cir[i].r,0);
        nV=0;
        vec[nV++]=arc(-pi,dvd,1);
        cnt=0;
        for(int j=0;j<n;j++) if(i!=j){
            double d=(cir[j].o-cir[i].o).sqrln();
            if(d<sqr(cir[j].r-cir[i].r)+eps){
                if(cir[i].r+i*eps<cir[j].r+j*eps)
                    psh(-pi,dvd,pi,dvd);
            }else if(d+eps<sqr(cir[j].r+cir[i].r)){
                double lambda=0.5*(1+(sqr(cir[i].r)-sqr(cir[j].r))/d);
                P cp=cir[i].o+lambda*(cir[j].o-cir[i].o);
                P nor((cir[j].o-cir[i].o).rev().zoom(sqrt(sqr(cir[i].r)-(cp-
                    cir[i].o).sqrln())));
                P frm(cp+nor);
                P to(cp-nor);
                psh(atan2(frm-cir[i].o),frm,atan2(to-cir[i].o),to);
            }
        }
    }
}

```

```

    }
    sort(vec+1,vec+nV);
    vec[nV++]=arc(pi,dvd,-1);
    for(int j=0;j+1<nV;j++){
        cnt+=vec[j].delta;
        double theta=vec[j+1].theta-vec[j].theta;
        double area=sqr(cir[i].r)*theta*0.5;
        combine(cnt,area,cir[i].o+1.0/area/3*cub(cir[i].r)*P(sin(vec[j]
            +1).theta)-sin(vec[j].theta),cos(vec[j].theta)-cos(vec[j+1].
            theta));
        combine(cnt,-sqr(cir[i].r)*sin(theta)*0.5,1./3*(cir[i].o+vec[j].
            p+vec[j+1].p));
        combine(cnt,vec[j].p*vec[j+1].p*0.5,1.0/3*(vec[j].p+vec[j+1].p))
        ;
    }
}
printf("Case %d: ", Case);
printf("%.3f\n\n",ans[1] );//ans[i]: 至少被i个圆覆盖的面积
return 0;
}

```

3.3 计算几何杂

```

bool pit_on_seg(pit a, pit b, pit c){ // 点在线段上
    if(dcmp(det(b - a, c - a)) != 0) return false;
    if(dcmp(dot(a - b, a - c)) > 0) return false;
    return true;
}

bool pit_in_polygon(pit q){ // 点在多边形内
    int cnt = 0;
    for(int i = 1; i <= n; ++i){
        pit p1 = p[i];
        pit p2 = p[suc[i]];
        if(pit_on_seg(q, p1, p2)) return true;
        int k = dcmp(det(p2 - p1, q - p1));
        int d1 = dcmp(p1.y - q.y);
        int d2 = dcmp(p2.y - q.y);
        if(k > 0 && d1 <= 0 && d2 > 0) ++cnt;
        if(k < 0 && d2 <= 0 && d1 > 0) --cnt;
    }
    if(cnt != 0) return true;
    else return false;
}

bool seg_in_polygon(pit a, pit b){ // 线段在多边形内 撒点
    vec v = b - a;
    for(int t = 1; t <= 1000; ++t){
        pit c = a + v * (1.00 * (rand() % 10000) / 10000);
    }
}

```

```

        if(pit_in_polygon(c)) continue;
        else return false;
    }
    return true;
}

```

3.4 三维变换

```

struct Matrix{
    double a[4][4];
    int n,m;
    Matrix(int n = 4):n(n),m(n){
        for(int i = 0; i < n; ++i)
            a[i][i] = 1;
    }
    Matrix(int n, int m):n(n),m(m){}
    Matrix(Point A){
        n = 4;
        m = 1;
        a[0][0] = A.x;
        a[1][0] = A.y;
        a[2][0] = A.z;
        a[3][0] = 1;
    }
    //+-略
    Matrix operator *(const Matrix &b)const{
        Matrix ans(n,b.m);
        for (int i = 0; i < n; ++i)
            for (int j = 0; j < b.m; ++j)
            {
                ans.a[i][j] = 0;
                for (int k = 0; k < m; ++k)
                    ans.a[i][j] += a[i][k] * b.a[k][j];
            }
        return ans;
    }
    Matrix operator * (double k)const{
        Matrix ans(n,m);
        for (int i = 0; i < n; ++i)
            for (int j = 0; j < m; ++j)
                ans.a[i][j] = a[i][j] * k;
        return ans;
    }
};

Matrix cur(4), I(4);

Point get(int i){//以下三个是变换矩阵，get是使用方法

```

```

    Matrix ori(p[i]);
    ori = cur * ori;
    return Point(ori.a[0][0],ori.a[1][0],ori.a[2][0]);
}

void trans(){//平移
    int l,r;
    Point vec;
    vec.read();
    cur = I;
    cur.a[0][3] = vec.x;
    cur.a[1][3] = vec.y;
    cur.a[2][3] = vec.z;
}

void scale(){//以base为原点放大k倍
    Point base;
    base.read();
    scanf("%lf",&k);
    cur = I;
    cur.a[0][0] = cur.a[1][1] = cur.a[2][2] = k;
    cur.a[0][3] = (1.0 - k) * base.x;
    cur.a[1][3] = (1.0 - k) * base.y;
    cur.a[2][3] = (1.0 - k) * base.z;
}

void rotate(){//绕以base为起点vec为方向向量的轴逆时针旋转theta
    Point base,vec;
    base.read();
    vec.read();
    double theta;
    scanf("%lf",&theta);
    if (dcmp(vec.x)==0&&dcmp(vec.y)==0&&dcmp(vec.z)==0) return;
    double C = cos(theta), S = sin(theta);
    vec = vec / len(vec);
    Matrix T1,T2;
    T1 = T2 = I;
    T1.a[0][3] = base.x;
    T1.a[1][3] = base.y;
    T1.a[2][3] = base.z;
    T2.a[0][3] = -base.x;
    T2.a[1][3] = -base.y;
    T2.a[2][3] = -base.z;
    cur = I;
    cur.a[0][0] = sqr(vec.x) * (1 - C) + C;
    cur.a[0][1] = vec.x * vec.y * (1-C) - vec.z * S;
    cur.a[0][2] = vec.x * vec.z * (1-C) + vec.y * S;
    cur.a[1][0] = vec.x * vec.y * (1-C) + vec.z * S;
    cur.a[1][1] = sqr(vec.y) * (1-C) + C;
    cur.a[1][2] = vec.y * vec.z * (1-C) - vec.x * S;

```

```

    cur.a[2][0] = vec.x * vec.z * (1-C) - vec.y * S;
    cur.a[2][1] = vec.y * vec.z * (1-C) + vec.x * S;
    cur.a[2][2] = vec.z * vec.z * (1-C) + C;
    cur = T1 * cur * T2;
}

```

4 字符串

4.1 Manacher

```

// manacher
// 0-base
// odd s[i] len[i*2]
// even s[i],s[i+1] len[i*2+1]
void manacher(char *s) {
    int l = strlen(s);
    len[0] = 1;
    for (int i = 1, j = 0; i < n * 2 - 1; ++i) {
        int p = i / 2, q = i - p;
        int mx = (j + 1) / 2 + len[j] - 1;
        len[i] = mx < q ? 0 : min(mx - q + 1, len[j * 2 - i]);
        while (p - len[i] >= 0 && q + len[i] < l && s[p - len[i]] ==
            s[q + len[i]]) len[i]++;
        if (q + len[i] - 1 > mx) mx = q + len[i] - 1;
    }
}

// 1-base
// only even s[i],s[i+1] len[i]
void manacher(char *s) {
    int l = strlen(s + 1);
    int mx = 0, id;
    for (int i = 1; i <= l; ++i) {
        if (mx >= i) len[i] = min(mx - i, len[id * 2 - i]); else len[i] = 0;
        for (; s[i - len[i]] == s[i + len[i] + 1]; len[i]++);
        if (i + len[i] > mx) mx = len[i] + i, id = i;
    }
}

```

4.2 AC-Automachine by cjy

```

#define N 1500
int next[N][10], flag[N], fail[N], a[N];
int m, ans, root;
int newnode(){
    m++;
    for (int i = 1; i <= 4; i++)

```

```

        next[m][i] = -1;
    flag[m] = 1;
    return m;
}
void init(){
    m = -1;
    root = newnode();
}
void insert(char s[]){
    int len = strlen(s+1);
    int now = root;
    for (int i = 1; i <= len; i++){
        int t = id(s[i]);
        if (next[now][t] == -1)
            next[now][t] = newnode();
        now = next[now][t];
    }
    flag[now] = 0;
}
void build(){
    queue<int> Q;
    fail[root] = root;
    for (int i = 1; i <= 4; i++)
        if (next[root][i] == -1)
            next[root][i] = root;
        else{
            fail[next[root][i]] = root;
            flag[next[root][i]] &= flag[root];
            Q.push(next[root][i]);
        }
    while (!Q.empty()){
        int now = Q.front();
        Q.pop();
        for (int i = 1; i <= 4; i++)
            if (next[now][i] == -1)
                next[now][i] = next[fail[now]][i];
            else{
                fail[next[now][i]] = next[fail[now]][i];
                flag[next[now][i]] &= flag[next[fail[now]][i]];
                Q.push(next[now][i]);
            }
    }
}
char s[1005];
int main(){
    int n;
    int cases = 0;

```

```

    while(scanf("%d", &n), n){
        init();
        for (int i = 1; i <= n; i++){
            scanf("%s", s+1);
            insert(s);
        }
        build();
    }
    return 0;
}

```

4.3 AC-Automachine by xyt

```

struct trie{
    int size, indx[maxs][26], word[maxs], fail[maxs];
    bool jump[maxs];
    int idx(char ff){return ff - 'a';}
    void insert(char s[]){
        int u = 0;
        for(int i = 0; s[i]; ++i){
            int k = idx(s[i]);
            if(!indx[u][k]) indx[u][k] = ++size;
            u = indx[u][k];
        }
        word[u] = 1;
        jump[u] = true;
    }
    void get_fail(){
        queue<int> que;
        int head = 0, tail = 0;
        que.push(0);
        while(!que.empty()){
            int u = que.front();
            que.pop();
            for(int k = 0; k < 26; ++k){
                if(!indx[u][k]) continue;
                int v = indx[u][k];
                int p = fail[u];
                while(p && !indx[p][k]) p = fail[p];
                if(indx[p][k] && indx[p][k] != v) p = indx[p][k];
                fail[v] = p;
                jump[v] |= jump[p];
                que.push(v);
            }
        }
    }
    int query(char s[]){

```



```

    int rtn = 0, p = 0;
    int flag[maxs];
    memcpy(flag, word, sizeof flag);
    for(int i = 0; s[i]; ++i){
        int k = idx(s[i]);
        while(p && !indx[p][k]) p = fail[p];
        p = indx[p][k];
        int v = p;
        while(jump[v]){
            rtn += flag[v];
            flag[v] = 0;
            v = fail[v];
        }
    }
    return rtn;
}

} dict;

```

4.4 后缀数组

//sa[i] 表示排第 i 位的后缀是谁 rk[i] 表示后缀 i 排第几位
//h[i] 为 suffix(sa[i-1]) 和 suffix(sa[i]) 的最长公共前缀
*//开数组要*2*

```

inline void getsa(int j){
    memset(sum,0,sizeof(sum));
    for(int i=1;i<=n;++i) ++sum[rk[i+j]];
    for(int i=1;i<=n;++i) sum[i]+=sum[i-1];
    for(int i=n;i>0;--i) tsa[sum[rk[i+j]]--]=i;
    memset(sum,0,sizeof(sum));
    for(int i=1;i<=n;++i) ++sum[rk[i]];
    for(int i=1;i<=n;++i) sum[i]+=sum[i-1];
    for(int i=n;i>0;--i) sa[sum[rk[tsa[i]]]--]=tsa[i];
}

int main(){
    scanf("%s",s+1); n=strlen(s+1);
    for(int i=1;i<=n;++i) ++sum[s[i]];
    for(int i=1;i<=MC;++i) sum[i]+=sum[i-1];
    for(int i=n;i>0;--i) sa[sum[s[i]]--]=i;
    rk[sa[1]]=1;
    for(int i=2,p=1;i<=n;++i){
        if(s[sa[i]]!=s[sa[i-1]]) ++p;
        rk[sa[i]]=p;
    }
    for(int j=1;j<=n;j<=1){
        getsa(j);
        trk[sa[1]]=1;
    }
}

```

```

    for(int i=2,p=1;i<=n;++i){
        if(rk[sa[i]]!=rk[sa[i-1]] || rk[sa[i]+j]!=rk[sa[i-1]+j]) ++p;
        trk[sa[i]]=p;
    }
    for(int i=1;i<=n;++i) rk[i]=trk[i];
}
    for(int i=1;i<=n;++i) printf("%d ",sa[i]); printf("\n");
for(int i=1,j=0;i<=n;++i){
    if(rk[i]==1) continue;
    while(i+j<=n && sa[rk[i]-1]+j<=n && s[i+j]==s[sa[rk[i]-1]+j]) ++j;
    h[rk[i]]=j;
    if(j>0) --j;
}
    for(int i=1;i<=n;++i) printf("%d ",h[i]); printf("\n");
return 0;
}

```

4.5 扩展 KMP

```

// (1-base) next[i] = lcp(text[1..n], text[i..n]), text[1..next[i]] = text[i
    ..(i + next[i] - 1)]
void build(char *pattern) {
    int len = strlen(pattern + 1);
    int j = 1, k = 2;
    for (; j + 1 <= len && pattern[j] == pattern[j + 1]; j++);
    next[1] = len;
    next[2] = j - 1;
    for (int i = 3; i <= len; i++) {
        int far = k + next[k] - 1;
        if (next[i - k + 1] < far - i + 1) {
            next[i] = next[i - k + 1];
        }
        else {
            j = max(far - i + 1, 0);
            for (; i + j <= len && pattern[i + j] == pattern[j]; j++);
            next[i] = j;
            k = i;
        }
    }
}

void solve(char *text, char *pattern) {
    int len = strlen(text + 1);
    int lenp = strlen(pattern + 1);
    int j = 1, k = 1;
    for (; j <= len && j <= lenp && pattern[j] == text[j]; j++);
    extend[1] = j - 1;
}

```

```

    for (int i = 2; i <= len; i++) {
        int far = k + extend[k] - 1;
        if (next[i - k + 1] < far - i + 1) {
            extend[i] = next[i - k + 1];
        }
        else {
            j = max(far - i + 1, 0);
            for (; i + j <= len && 1 + j <= lenp && pattern[1 +
                j] == text[i + j]; j++);
            extend[i] = j;
            k = i;
        }
    }
}

```

4.6 回文树

```

const int N = 400010;
int ch[N][26], fail[N], len[N], tot, cnt1[N], cnt2[N];
char s[200010];

void ready(){
    len[0] = 0; len[1] = -1;
    fail[0] = 1; fail[1] = -1;
}

void Insert(char *s, int *cnt){
    int now = 1, l = strlen(s), x, y, tmp;
    for(int i = 0; i < l; i ++){
        x = s[i] - 'a';
        while(s[i] != s[i - len[now] - 1]) now = fail[now];
        if (!ch[now][x]){
            ch[now][x] = ++ tot;
            len[tot] = len[now] + 2;
        }
        y = ch[now][x];
        tmp = fail[now];
        if (tmp == -1) fail[y] = 0;
        else{
            while(s[i] != s[i - len[tmp] - 1]) tmp = fail[tmp];
            fail[y] = ch[tmp][x];
        }
        now = y;
        cnt[now] ++;
    }
}

int main(){
    int T, tests = 0;

```

```

scanf("%d", &T);
while(tests < T){
    for(int i = 0; i <= tot; i++){
        for(int j = 0; j < 26; j++) ch[i][j] = 0;
        len[i] = cnt1[i] = cnt2[i] = 0;
    }
    tot = 1;
    ready();
    scanf("%s", s);
    Insert(s, cnt1);
    scanf("%s", s);
    Insert(s, cnt2);
    for(int i = tot; i >= 2; i--){
        cnt1[fail[i]] += cnt1[i],
        cnt2[fail[i]] += cnt2[i];
    }
    LL ans = 0;
    for(int i = 2; i <= tot; i++) ans += 1LL * cnt1[i] * cnt2[i];
    printf("Case #%d: %lld\n", ++tests, ans);
}
return 0;
}

```

4.7 SAM by lss

```

const int L = 600005; // n * 2 开大一点, 只开 n 会挂
struct Node
{
    Node *nx[26], *fail;
    int l, num;
};
Node *root, *last, sam[L], *b[L];
int sum[L], f[L];
int cnt;
char s[L];
int l;
void add(int x)
{
    ++cnt;
    Node *p = &sam[cnt];
    Node *pp = last;
    p->l = pp->l + 1;
    last = p;
    for(; pp && !pp->nx[x]; pp = pp->fail) pp->nx[x] = p;
    if(!pp) p->fail = root;
    else{
        if(pp->l + 1 == pp->nx[x]->l) p->fail = pp->nx[x];
    }
}

```

```

        else{
            ++cnt;
            Node *r = &sam[cnt], *q = pp->nx[x];
            *r = *q;
            r->l = pp->l + 1;
            q->fail = p->fail = r;
            for(; pp && pp->nx[x] == q; pp = pp->fail) pp->nx[x]
                = r;
        }
    }
}

int main()
{
    scanf("%s", s);
    l = strlen(s);
    root = last = &sam[0];
    for(int i = 0; i < l; ++i) add(s[i] - 'a');
    for(int i = 0; i <= cnt; ++i) ++sum[sam[i].l];
    for(int i = 1; i <= l; ++i) sum[i] += sum[i - 1];
    for(int i = 0; i <= cnt; ++i) b[--sum[sam[i].l]] = &sam[i];
    Node *now = root;
    for(int i = 0; i < l; ++i){
        now = now->nx[s[i] - 'a'];
        ++now->num;
    }
    for(int i = cnt; i > 0; --i){
        int len = b[i]->l;
        //cerr<<"num="<<b[i]->num<<endl;
        f[len] = max(f[len], b[i]->num);
        //cerr<<b[i]->num<<" "<<b[i]->fail->num<<" ..."<<endl;
        b[i]->fail->num += b[i]->num;
        //cerr<<b[i]->num<<" "<<b[i]->fail->num<<" ..."<<endl;
    }
    for(int i = l - 1; i >= 1; --i) f[i] = max(f[i], f[i + 1]);
    for(int i = 1; i <= l; ++i) printf("%d\n", f[i]);
    return 0;
}

```

4.8 SAM by xyt

```

const int maxn = 351000;
struct sam{
    int tot, lst;
    struct node{
        int indx[26], fa, lnth, rts;
        void init(){
            fa = -1;

```

```

        lnth = rts = 0;
        memset(indx, -1, sizeof indx);
    }
}nd[maxn];
void init(){
    tot = lst = 0;
    nd[tot].init();
}
int newnode(){
    nd[++tot].init();
    return tot;
}
void insert(char ch){
    int c = ch - 'a';
    int newp = newnode(), p = lst;
    nd[newp].lnth = nd[p].lnth + 1;
    while(p != -1 && nd[p].indx[c] == -1){
        nd[p].indx[c] = newp;
        p = nd[p].fa;
    }
    if(p == -1) nd[newp].fa = 0;
    else{
        int q = nd[p].indx[c];
        if(nd[p].lnth + 1 == nd[q].lnth) nd[newp].fa = q;
        else{
            int newq = newnode();
            nd[newq] = nd[q];
            nd[newq].lnth = nd[p].lnth + 1;
            nd[q].fa = nd[newp].fa = newq;
            while(p != -1 && nd[p].indx[c] == q){
                nd[p].indx[c] = newq;
                p = nd[p].fa;
            }
        }
    }
    lst = newp;
}

}dict;
bool cmp(int i, int j){
    return dict.nd[i].lnth > dict.nd[j].lnth;
}
int n, ans[maxn], rk[maxn];
char str[maxn];
void work(){
    dict.init();
    n = strlen(str);
    for(int i = 0; i < n; ++i) dict.insert(str[i]);
}

```

```

    for(int i = 1; i <= dict.tot; ++i) rk[i] = i;
    sort(rk + 1, rk + 1 + dict.tot, cmp);
    for(int i = 0, p = 0; i < n; ++i)
        dict.nd[p=dict.nd[p].indx[str[i]-'a']].rts = 1;
    for(int i = 1; i <= dict.tot; ++i){
        int p = rk[i];
        ans[dict.nd[p].lnth] = max(ans[dict.nd[p].lnth], dict.nd[p].
            rts);
        dict.nd[dict.nd[p].fa].rts += dict.nd[p].rts;
    }
    for(int i = n; i >= 1; --i) ans[i-1] = max(ans[i-1], ans[i]);
    for(int i = 1; i <= n; ++i) printf("%d\n", ans[i]);
}

```

5 图论

5.1 图论相关

1. 差分约束系统

(1) 以 $x[i] - x[j] \leq c$ 为约束条件, $j \rightarrow i : c$, 求最短路得到的是 $x[i] \leq x[s]$ 的最大解, 存在负权回路无解

(2) 以 $x[i] - x[j] \geq c$ 为约束条件, $j \rightarrow i : c$, 求最长路得到的 $x[i] \geq x[s]$ 的最小解, 存在正权回路无解 // 若有 $x[i] = x[j]$ 则 $i < 0 \rightarrow j$

2. 最大闭合权子图

s 向正权点连边, 负权点向 t 连边, 边权为点权绝对值, 再按原图连边, 边权为 INF

3. 最大密度子图: $\max \frac{|E'|}{|V'|}$

(1) 猜测答案 g 若最大流大于 EPS 则 g 合法

(2) $s \rightarrow v : \text{INF}, u \rightarrow t : \text{INF} + g - \text{deg}[u], u \rightarrow v : 1.00$

4. 2-SAT

利用对称性建图, 若 u 与 u' 在同一强连通分量中, 则无解, 若有解输出方案, 拓扑排序后自底向上 (从 ind = 0 到 otd = 0) 选择删除

5. 最小割

(1) 二分图最小点权覆盖集: $s \rightarrow u : w[u], u \rightarrow v : \text{INF}, v \rightarrow t : w[v]$

5.2 SteinerTree by cjj

```

const int N = 100005;
const int M = 200005;
const int P = 8;
const int inf = 0x3f3f3f3f;
int n, m, p, status, idx[P], f[1 << P][N];
//int top, h[N];
priority_queue<pair<int, int>> q;
bool vis[N];
int tot, lst[N], nxt[M], id[M], len[M];
void Add(int x, int y, int z) {

```

```

        id[++tot] = y; nxt[tot] = lst[x]; lst[x] = tot; len[tot] = z;
    }
    void dijkstra(int dis[]) {
        while(!q.empty()) {
            int x = q.top().second; q.pop();
            if (vis[x]) continue;
            vis[x] = 1;
            for (int i = lst[x]; i; i = nxt[i]) {
                int y = id[i];
                if (dis[x] + len[i] < dis[y]) {
                    dis[y] = dis[x] + len[i];
                    if (!vis[y]) q.push(make_pair(-dis[y], y));
                }
            }
        }
    }
}

void Steiner_Tree() {
    for (int i = 1; i < status; i++) {
        //top = 0;
        while (!q.empty()) q.pop();
        memset(vis, 0, sizeof(vis));
        for (int j = 1; j <= n; j++) {
            for (int k = i & (i - 1); k; (--k) &= i)
                f[i][j] = min(f[i][j], f[k][j] + f[i ^ k][j]);
            if (f[i][j] != inf) {
                //h[++top] = j, vis[j] = 1;
                q.push(make_pair(-f[i][j], j));
            }
        }
        //SPFA(f[i]);
        dijkstra(f[i]);
    }
}

int main() {
    while (scanf("%d%d%d", &n, &m, &p) == 3) {
        status = 1 << p;
        tot = 0; memset(lst, 0, sizeof(lst));
        /*求最小生成森林
        每棵生成树中至少选择一个点，点权为代价
        新开一个空白关键点作为源
        for (int i = 1; i <= n; i++) {
            scanf("%d", &val[i]);
            Add(0, i, val[i]); Add(i, 0, val[i]);
        }*/
        for (int i = 1; i <= m; i++) {
            int x, y, z;
            scanf("%d%d%d", &x, &y, &z);

```



```

        Add(x, y, z); Add(y, x, z);
    }
    for (int i = 1; i <= p; i++) scanf("%d", &idx[i]);
    memset(f, 0x3f, sizeof(f));
    for (int i = 1; i <= n; i++) f[0][i] = 0;
    for (int i = 1; i <= p; i++)
        f[1 << (i - 1)][idx[i]] = 0;
    Steiner_Tree();
    int ans = inf;
    for (int i = 1; i <= n; i++) ans = min(ans, f[status - 1][i]);
    printf("%d\n", ans);
}
return 0;
}

```

5.3 LCA by xyt

```

int maxbit, dpth[maxn], ance[maxn][maxb];
void dfs(int u, int fath){
    dpth[u] = dpth[fath] + 1; ance[u][0] = fath;
    for(int i = 1; i <= maxbit; ++i) ance[u][i] = ance[ance[u][i-1]][i-1];
    for(int l = last[u]; l; l = next[l]){
        int v = dstn[l];
        if(v == fath) continue;
        dfs(v, u);
    }
}
int lca(int u, int v){
    if(dpth[u] < dpth[v]) swap(u, v);
    int p = dpth[u] - dpth[v];
    for(int i = 0; i <= maxbit; ++i)
        if(p & (1 << i)) u = ance[u][i];
    if(u == v) return u;
    for(int i = maxbit; i >= 0; --i){
        if(ance[u][i] == ance[v][i]) continue;
        u = ance[u][i]; v = ance[v][i];
    }
    return ance[u][0];
}

```

5.4 KM

```

int weight[M][M], lx[M], ly[M];
bool sx[M], sy[M];
int match[M];
bool search_path(int u){

```

```

    sx[u] = true;
    for (int v = 0; v < n; v++){
        if (!sy[v] && lx[u] + ly[v] == weight[u][v]){
            sy[v] = true;
            if (match[v] == -1 || search_path(match[v])){
                match[v] = u;
                return true;
            }
        }
    }
    return false;
}

int KM()
{
    for (int i = 0; i < n; i++){
        lx[i] = ly[i] = 0;
        for (int j = 0; j < n; j++)
            if (weight[i][j] > lx[i])
                lx[i] = weight[i][j];
    }
    memset(match, -1, sizeof(match));
    for (int u = 0; u < n; u++){
        while (1){
            memset(sx, 0, sizeof(sx));
            memset(sy, 0, sizeof(sy));
            if (search_path(u)) break;

            int inc = len * len;
            for (int i = 0; i < n; i++)
                if (sx[i])
                    for (int j = 0; j < n; j++)
                        if (!sy[j] && ((lx[i] + ly[j] - weight[i][j]) < inc))
                            inc = lx[i] + ly[j] - weight[i][j];
            for (int i = 0; i < n; i++){
                if (sx[i]) lx[i] -= inc;
                if (sy[i]) ly[i] += inc;
            }
        }
    }
    int sum = 0;
    for (int i = 0; i < n; i++)
        if (match[i] >= 0) sum += weight[match[i]][i];
    return sum;
}

int main()
{

```

```

        memset(weight, 0, sizeof(weight));
        for (int i = 1; i <= len; i++)
            weight[a[i]][b[i]]++;
        cout<<KM()<<endl;
        return 0;
}

```

5.5 KM 三次方

```

const int N=1010;
const int INF = 1e9;
int n;
struct KM{
int w[N][N];
int lx[N], ly[N], match[N], way[N], slack[N];
bool used[N];
void initialization(){
    for(int i = 1; i <= n; i++){
        match[i] = 0;
        lx[i] = 0;
        ly[i] = 0;
        way[i] = 0;
    }
}
void hungary(int x){//for i(1 -> n) : hungary(i);
    match[0] = x;
    int j0 = 0;
    for(int j = 0; j <= n; j++){
        slack[j] = INF;
        used[j] = false;
    }
    do{
        used[j0] = true;
        int i0 = match[j0], delta = INF, j1;
        for(int j = 1; j <= n; j++){
            if(used[j] == false){
                int cur = -w[i0][j] - lx[i0] - ly[j];
                if(cur < slack[j]){
                    slack[j] = cur;
                    way[j] = j0;
                }
                if(slack[j] < delta){
                    delta = slack[j];
                    j1 = j;
                }
            }
        }
    }
}
}

```

```

    for(int j = 0; j <= n; j++){
        if(used[j]){
            lx[match[j]] += delta;
            ly[j] -= delta;
        }
        else slack[j] -= delta;
    }
    j0 = j1;
}while (match[j0] != 0);

do{
    int j1 = way[j0];
    match[j0] = match[j1];
    j0 = j1;
}while(j0);
}

int get_ans(){//maximum ans
int sum = 0;
for(int i = 1; i<= n; i++)
    if(match[i] > 0) sum += -w[match[i]][i];
return sum;
}
}KM_solver;

```

5.6 Dinic by cjj

```

const int N = 20000;
const int inf = 100000;
int tot, id[N], nxt[N], lst[N], cap[N];
int d[N];
queue<int> Q;
void Add(int x, int y, int z) {
    id[++tot] = y; nxt[tot] = lst[x]; lst[x] = tot; cap[tot] = z;
    id[++tot] = x; nxt[tot] = lst[y]; lst[y] = tot; cap[tot] = 0;
}
bool bfs() {
    while (!Q.empty()) Q.pop();
    Q.push(S);
    memset(d, 0, sizeof(d)); d[S] = 1;
    while (!Q.empty()) {
        int x = Q.front(); Q.pop();
        for (int i = lst[x]; i; i = nxt[i]) {
            int y = id[i];
            if (cap[i] && !d[y]) {
                d[y] = d[x] + 1;
                if (y == T) return true;
                Q.push(y);
            }
        }
    }
}

```

```

        }
    }
    return false;
}
int find(int x, int flow) {
    if (x == T) return flow;
    int res = 0;
    for (int i = lst[x]; i; i = nxt[i]) {
        int y = id[i];
        if (cap[i] && d[y] == d[x] + 1) {
            int now = find(y, min(flow - res, cap[i]));
            res += now;
            cap[i] -= now, cap[i ^ 1] += now;
        }
    }
    if (!res) d[x] = -1;
    return res;
}
int dinic() {
    int ans = 0;
    while (bfs())
        ans += find(S, inf);
    return ans;
}
int main() {
    tot = 1; memset(lst, 0, sizeof(lst));

    printf("%d\n", dinic());
    return 0;
}

```

5.7 网络流 by xyt

```

// sap
struct edge{
    int v, r, flow;
    edge(int v, int flow, int r) : v(v), flow(flow), r(r) {}
};
vector<edge> mp[maxn];
void add_edge(int u, int v, int flow){
    mp[u].push_back(edge(v, flow, mp[v].size()));
    mp[v].push_back(edge(u, 0, mp[u].size() - 1));
}
int maxflow, disq[maxn], dist[maxn];
int sap(int u, int nowflow){
    if(nowflow == 0 || u == T) return nowflow;

```

```

    int tempflow, deltaflow = 0;
    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l].v;
        if(mp[u][l].flow > 0 && dist[u] == dist[v] + 1){
            tempflow = sap(v, min(nowflow - deltaflow, mp[u][l].flow));
            mp[u][l].flow -= tempflow;
            mp[v][mp[u][l].r].flow += tempflow;
            deltaflow += tempflow;
            if(deltaflow == nowflow || dist[S] >= T) return deltaflow;
        }
    }
    disq[dist[u]]--;
    if(disq[dist[u]] == 0) dist[S] = T;
    dist[u]++;
    disq[dist[u]]++;
    return deltaflow;
}

int main(){
    while(dist[S] < T) maxflow += sap(S, inf);
}

// 费用流
struct edge{
    int v, r, cost, flow;
    edge(int v, int flow, int cost, int r) : v(v), flow(flow), cost(cost), r
        (r) {}
};

vector<edge> mp[maxn];
void add_edge(int u, int v, int flow, int cost){
    mp[u].push_back(edge(v, flow, cost, mp[v].size()));
    mp[v].push_back(edge(u, 0, -cost, mp[u].size() - 1));
}

int S, T, maxflow, mincost;
int dist[maxn], pth[maxn], lnk[maxn];
bool inq[maxn];
queue<int> que;
bool find_path(){
    for(int i = 1; i <= T; ++i) dist[i] = inf;
    dist[S] = 0;
    que.push(S);
    while(!que.empty()){
        int u = que.front();
        que.pop();
        inq[u] = false;
        for(int l = 0; l < mp[u].size(); ++l){
            int v = mp[u][l].v;
            if(mp[u][l].flow > 0 && dist[v] > dist[u] + mp[u][l].cost){
                dist[v] = dist[u] + mp[u][l].cost;
                pth[v] = u;
            }
        }
    }
}

```

```

        lnk[v] = 1;
        if(!inq[v]){
            inq[v] = true;
            que.push(v);
        }
    }
}
if(dist[T] < inf) return true;
else return false;
}
void adjust(){
    int deltaflow = inf, deltacost = 0;
    for(int v = T; v != S; v = pth[v]){
        deltaflow = min(deltaflow, mp[pth[v]][lnk[v]].flow);
        deltacost += mp[pth[v]][lnk[v]].cost;
    }
    maxflow += deltaflow;
    mincost += deltaflow * deltacost;
    for(int v = T; v != S; v = pth[v]){
        mp[pth[v]][lnk[v]].flow -= deltaflow;
        mp[mp[pth[v]][lnk[v]].v][mp[pth[v]][lnk[v]].r].flow += deltaflow;
    }
}
int main(){while(find_path()) adjust();}

```

5.8 最大密度子图

```

const int maxn = 1e2 + 5;
const double eps = 1e-10;
const double d = 1e2;
const double inf = 1e9;
struct edge{
    int r, v;
    double flow;
    edge(int v, int r, double flow) : v(v), r(r), flow(flow) {}
};
vector<edge> mp[maxn];
void add_edge(int u, int v, double flow){
    mp[u].push_back(edge(v, mp[v].size(), flow));
    mp[v].push_back(edge(u, mp[u].size() - 1, 0.00));
}
int n, m, S, T, a[maxn], deg[maxn];
int dist[maxn], disq[maxn];
double sap(int u, double nowflow){
}
double value(){
}

```

```

    double maxflow = 0.00;
    while(dist[S] <= T) maxflow += sap(S, inf);
    return -0.50 * (maxflow - d * n);
}

void build(double g){
    g *= 2.00;
    for(int i = 1; i <= n; ++i) add_edge(S, i, d); // s -> v : INF
    for(int i = 1; i <= n; ++i) add_edge(i, T, d + g - deg[i]); // u ->
        t : INF + g - deg[u] 其中 deg[u] 为点 u 的度数 (双向边)
    for(int i = 1; i <= n; ++i)
        for(int j = 1; j < i; ++j){
            if(a[i] >= a[j]) continue;
            add_edge(i, j, 1.00); // u -> v : 1.00
            add_edge(j, i, 1.00);
        }
}

void clear(){
    memset(dist, 0, sizeof dist);
    memset(disq, 0, sizeof disq);
    for(int i = 1; i <= T; ++i) mp[i].clear();
}

double binary(double left, double right){ // 猜测答案 g [1 / n, m / 1]
    int step = 0;
    while(left + eps < right && step <= 50){
        ++step;
        double mid = (left + right) / 2;
        clear();
        build(mid);
        double h = value();
        if(h > eps) left = mid;
        else right = mid;
    }
    return left;
}

void work(){
    m = 0;
    scanf("%d", &n);
    S = n + 1, T = n + 2;
    for(int i = 1; i <= n; ++i) scanf("%d", &a[i]);
    for(int i = 1; i <= n; ++i) deg[i] = 0;
    for(int i = 1; i <= n; ++i)
        for(int j = 1; j < i; ++j){
            if(a[i] >= a[j]) continue;
            ++m;
            ++deg[i];
            ++deg[j];
        }
    printf("%.12f\n", binary(0.00, m));
}

```



```

}
int main(){
    int case_number;
    scanf("%d", &case_number);
    for(int cs = 1; cs <= case_number; ++cs){
        printf("Case #%d: ", cs);
        work();
    }
    return 0;
}

```

5.9 强联通分量

```

int cnt, top, scc;
int bel[maxn], dfn[maxn], low[maxn], stck[maxn];
bool inst[maxn];
void tarjan(int u){
    dfn[u] = low[u] = ++cnt;
    stck[++top] = u;
    inst[u] = true;
    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l];
        if(!dfn[v]){
            tarjan(v);
            low[u] = min(low[u], low[v]);
        } else if(inst[v]) low[u] = min(low[u], dfn[v]);
    }
    if(dfn[u] == low[u]){
        ++scc;
        int v;
        do{
            v = stck[top--];
            bel[v] = scc;
            inst[v] = false;
        } while(v != u);
    }
}

```

5.10 边双联通分量

```

int scc, top, cnt;
int dfn[maxn], low[maxn], stck[maxn], bel[maxn];
bool inst[maxn];
void tarjan(int u){

    dfn[u] = low[u] = ++cnt;
    stck[++top] = u;

```

```

    inst[u] = true;

    for(int l = 0; l < mp[u].size(); ++l){
        int v = mp[u][l].v;
        if(mp[u][l].flag) continue;
        mp[u][l].flag = mp[v][mp[u][l].r].flag = true;
        if(!dfn[v]){
            tarjan(v);
            low[u] = min(low[u], low[v]);
        } else if(inst[v]) low[u] = min(low[u], dfn[v]);
    }

    if(dfn[u] == low[u]){
        ++scc;
        int v;
        do{
            v = stck[top--];
            bel[v] = scc;
            inst[v] = false;
            ++sz[scc];
        } while(v != u);
    }
}

```

5.11 点双联通分量加构造森林块

```

//Point Biconnected Component
bool mark[M << 1];
int part;
int ind, dfn[N], low[N], st[M << 1], top, root[N];
void tarjan(int x, int cur)
{
    dfn[x] = low[x] = ++ind;
    for(int i = hd[x]; i; i = nx[i])
    {
        if(mark[i]) continue;
        mark[i] = mark[i ^ 1] = 1;
        st[++top] = i;

        int v = th[i];
        if(dfn[v])
        {
            low[x] = min(low[x], dfn[v]);
            continue;
        }
        tarjan(v, cur);
        low[x] = min(low[x], low[v]);
    }
}

```

```

    if(low[v] >= dfn[x])
    {
        ++part;
        int k;
        do
        {
            k = st[top--];
            root[th[k]] = cur; //联通块里点双联通分量标号最小值
            root[th[k ^ 1]] = cur;
            addtree(part, th[k]);
            addtree(th[k], part); //part为点双联通分量的标号
            addtree(part, th[k ^ 1]);
            addtree(th[k ^ 1], part);
        }while(th[k ^ 1] != x);
    }
}

bool vis[N << 1];
long long val[N << 1], son[N << 1];
void dfs(int x)
{
    vis[x] = 1;
    val[x] = (x <= n ? w[x] : 111);
    son[x] = 011;
    for(int i = thd[x]; i; i = tnx[i])
    if(!vis[tth[i]])
    {
        int v = tth[i];
        dfs(v);
        (val[x] *= val[v]) %= MOD;

        if(x <= n) (son[x] += val[v]) %= MOD;
    }
}

```

5.12 K 短路

// POJ 2449

/******

K短路 用 *dijkstra* + *A** 启发式搜索

当点 v 第 K 次出堆的时候, 这时候求得的路径是 k 短路。

*A** 算法有一个启发式函数 $f(p) = g(p) + h(p)$, 即评估函数 = 当前值 + 当前位置到终点的最短距离

$g(p)$: 当前从 s 到 p 点所走的路径长度, $h(p)$ 就是点 p 到目的点 t 的最短距离。

$f(p)$ 就是当前路径从 s 走到 p 再从 p 到 t 的所走距离。

步骤:

1>求出 $h(p)$ 。将有向边反向，求出目的点 t 到所有点的最短距离，用 $dijkstra$ 算法

2>将原点 s 加入优先队列中

3>优先队列取出 $f(p)$ 最小的一个点 p

如果 $p==t$ ，并且出来的次数恰好是 k 次，那么算法结束

否则，如果 p 出来的次数多余 k 次，就不用再进入队列中

否则遍历 p 相邻的边，加入优先队列中

注意：如果 $s==t$ ，那么求得 k 短路应该变成 $k++$ ；

*****/

```
#define MAXN 1005
#define MAXM 200100
struct Node{
    int v,c,nxt;
}Edge[MAXN];
int head[MAXN], tail[MAXN], h[MAXN];
struct Statement{
    int v,d,h;
    bool operator <( Statement a )const
    {    return a.d+a.h<d+h;    }
};
void addEdge( int u,int v,int c,int e ){
    Edge[e<<1].v=v; Edge[e<<1].c=c; Edge[e<<1].nxt=head[u]; head[u]=e<<1;
    Edge[e<<1|1].v=u; Edge[e<<1|1].c=c; Edge[e<<1|1].nxt=tail[v]; tail[v]=e
        <<1|1;
}

void Dijstra( int n,int s,int t ){
    bool vis[MAXN];
    memset( vis,0,sizeof(vis) );
    memset( h,0x7F,sizeof(h) );
    h[t]=0;
    for( int i=1;i<=n;i++ ){
        int min=0x7FFF;
        int k=-1;
        for( int j=1;j<=n;j++ ){
            if( vis[j]==false && min>h[j] )
                min=h[j],k=j;
        }
        if( k==-1 )break;
        vis[k]=true;
        for( int temp=tail[k];temp!=-1;temp=Edge[temp].nxt ){
            int v=Edge[temp].v;
            if( h[v]>h[k]+Edge[temp].c )
                h[v]=h[k]+Edge[temp].c;
        }
    }
}

int Astar_Kth( int n,int s,int t,int K ){
    Statement cur,nxt;
```

```

//priority_queue<Q>q;
priority_queue<Statement>FstQ;
int cnt[MAXN];
memset( cnt,0,sizeof(cnt) );
cur.v=s; cur.d=0; cur.h=h[s];
FstQ.push(cur);
while( !FstQ.empty() ){
    cur=FstQ.top();
    FstQ.pop();
    cnt[cur.v]++;
    if( cnt[cur.v]>K ) continue;
    if( cnt[t]==K )return cur.d;
    for( int temp=head[cur.v];temp!=-1;temp=Edge[temp].nxt ){
        int v=Edge[temp].v;
        nxt.d=cur.d+Edge[temp].c;
        nxt.v=v;
        nxt.h=h[v];
        FstQ.push(nxt);
    }
}
return -1;
}
int main()
{
    int n,m;
    while( scanf( "%d %d",&n,&m )!=EOF ){
        int u,v,c;
        memset( head,0xFF,sizeof(head) );
        memset( tail,0xFF,sizeof(tail) );
        for( int i=0;i<m;i++){
            scanf( "%d %d %d",&u,&v,&c );
            addEdge( u,v,c,i );
        }
        int s,t,k;
        scanf( "%d %d %d",&s,&t,&k );
        if( s==t ) k++;
        Dijkstra( n,s,t );
        printf( "%d\n",Astar_Kth( n,s,t,k ) );
    }
    return 0;
}

```

6 其他

6.1 Dancing Links(精确覆盖及重复覆盖)

// HUST 1017

// 给定一个 n 行 m 列的 $0/1$ 矩阵, 选择某些行使得每一列都恰有一个 1

```
const int MAXN = 1e3 + 5;
const int MAXM = MAXN * MAXN;
const int INF = 1e9;
int ans;
int chosen[MAXM];
struct DancingLinks{
    int row, col, tot;
    int up[MAXM], dn[MAXM], lf[MAXM], rg[MAXM];
    int hd[MAXM], sz[MAXM];
    int posr[MAXM], posc[MAXM];

    void init(int _n, int _m){
        row = _n, col = _m;
        for(int i = 0; i <= col; ++i){
            sz[i] = 0;
            up[i] = dn[i] = i;
            lf[i] = i - 1;
            rg[i] = i + 1;
        }
        rg[col] = 0;
        lf[0] = col;
        tot = col;
        for(int i = 1; i <= row; ++i) hd[i] = -1;
    }

    void lnk(int r, int c){
        ++tot;
        ++sz[c];
        dn[tot] = dn[c];
        up[tot] = c;
        up[dn[c]] = tot;
        dn[c] = tot;
        posr[tot] = r;
        posc[tot] = c;
        if(hd[r] < 0) hd[r] = lf[tot] = rg[tot] = tot;
        else{
            lf[tot] = hd[r];
            rg[tot] = rg[hd[r]];
            lf[rg[hd[r]]] = tot;
            rg[hd[r]] = tot;
        }
    }

    void remove(int c){ // 删除列时删除能覆盖其的行
        rg[lf[c]] = rg[c];
        lf[rg[c]] = lf[c];
        for(int i = dn[c]; i != c; i = dn[i])
            for(int j = rg[i]; j != i; j = rg[j]){
                dn[up[j]] = dn[j];
            }
    }
}
```

```

        up[dn[j]] = up[j];
        --sz[posc[j]];
    }
}

void resume(int c){
    rg[lf[c]] = c;
    lf[rg[c]] = c;
    for(int i = dn[c]; i != c; i = dn[i])
        for(int j = rg[i]; j != i; j = rg[j]){
            up[dn[j]] = j;
            dn[up[j]] = j;
            ++sz[posc[j]];
        }
}

bool dance(int dpth){
    if(rg[0] == 0){
        printf("%d", dpth);
        for(int i = 0; i < dpth; ++i) printf(" %d", chosen[i]);
        puts("");
        return true;
    }

    int c = rg[0];
    for(int i = rg[0]; i; i = rg[i]) if(sz[i] < sz[c]) c = i;
    remove(c); // 当前消去第c列
    for(int i = dn[c]; i != c; i = dn[i]){ // 第c列是由第i行覆盖的
        chosen[dpth] = posr[i];
        for(int j = rg[i]; j != i; j = rg[j]) remove(posc[j]); // 删除第i行能覆盖的其余列 因为它们只能被覆盖一次
        if(dance(dpth + 1)) return true;
        for(int j = lf[i]; j != i; j = lf[j]) resume(posc[j]);
    }
    resume(c);
    return false;
}

};

DancingLinks dlx;
int n, m;
void work(){
    dlx.init(n, m);
    for(int i = 1; i <= n; ++i){
        int k, j;
        scanf("%d", &k);
        while(k--){
            scanf("%d", &j);

```

```

        dlx.lnk(i, j);
    }
}
if(!dlx.dance(0)) puts("NO");
}
// 重复覆盖
// 给定一个  $n$  行  $m$  列的 0/1 矩阵, 选择某些行使得每一列至少有一个 1
struct DancingLinks{
    int row, col, tot;
    int up[MAXM], dn[MAXM], lf[MAXM], rg[MAXM];
    int head[MAXM], sz[MAXM];
    void init(int _n, int _m){
        row = _n, col = _m;
        for(int i = 0; i <= col; ++i){
            sz[i] = 0;
            up[i] = dn[i] = i;
            lf[i] = i - 1;
            rg[i] = i + 1;
        }
        rg[col] = 0;
        lf[0] = col;
        tot = col;
        for(int i = 1; i <= row; ++i) head[i] = -1;
    }
    void lnk(int r, int c){
        ++tot;
        ++sz[c];
        dn[tot] = dn[c];
        up[dn[c]] = tot;
        up[tot] = c;
        dn[c] = tot;
        if(head[r] < 0) head[r] = lf[tot] = rg[tot] = tot;
        else{
            rg[tot] = rg[head[r]];
            lf[rg[head[r]]] = tot;
            lf[tot] = head[r];
            rg[head[r]] = tot;
        }
    }
}
void remove(int c){ // 删除列时不删除行 因为列可被重复覆盖
    for(int i = dn[c]; i != c; i = dn[i]){
        rg[lf[i]] = rg[i];
        lf[rg[i]] = lf[i];
    }
}
void resume(int c){
    for(int i = up[c]; i != c; i = up[i]){
        rg[lf[i]] = i;
    }
}

```



```

        lf[rg[i]] = i;
    }
}
void dance(int d){
    if(ans <= d) return;
    if(rg[0] == 0){
        ans = min(ans, d);
        return;
    }
    int c = rg[0];
    for(int i = rg[0]; i != 0; i = rg[i]) if(sz[i] < sz[c]) c = i;
    for(int i = dn[c]; i != c; i = dn[i]){ // 枚举c列是被哪行覆盖
        remove(i);
        for(int j = rg[i]; j != i; j = rg[j]) remove(j); // 删除可被i行覆盖的列 因为不需要再考虑它们的覆盖问题
        dance(d + 1);
        for(int j = lf[i]; j != i; j = lf[j]) resume(j);
        resume(i);
    }
}
};
DancingLinks dlx;

```

6.2 序列莫队

```

const int maxn = 50005;
const int maxb = 233;
int n, m, cnt[maxn], a[maxn];
long long answ[maxn], ans;
int bk, sz, bel[maxn];
int lf[maxn], rh[maxn], rnk[maxn];
bool cmp(int i, int j){
    if(bel[lf[i]] != bel[lf[j]]) return bel[lf[i]] < bel[lf[j]];
    else return bel[rh[i]] < bel[rh[j]];
}
void widden(int i){ans += cnt[a[i]]++;}
void shorten(int i){ans -= --cnt[a[i]];}
long long gcd(long long a, long long b){
    if(b == 0) return a;
    else return gcd(b, a % b);
}
int main(){
    scanf("%d%d", &n, &m);
    bk = sqrt(n); sz = n / bk;

```

```

while(bk * sz < n) ++bk;
for(int b = 1, i = 1; b <= bk; ++b)
    for(; i <= b * sz && i <= n; ++i) bel[i] = b;
for(int i = 1; i <= n; ++i) scanf("%d", &a[i]);
for(int i = 1; i <= m; ++i) scanf("%d%d", &lf[i], &rh[i]);
for(int i = 1; i <= m; ++i) rnk[i] = i;
sort(rnk + 1, rnk + 1 + m, cmp);
lf[0] = rh[0] = 1; widden(1);
for(int i = 1; i <= m; ++i){
    int k = rnk[i], kk = rnk[i-1];
    for(int j = lf[k]; j < lf[kk]; ++j) widden(j);
    for(int j = rh[k]; j > rh[kk]; --j) widden(j);
    for(int j = lf[kk]; j < lf[k]; ++j) shorten(j);
    for(int j = rh[kk]; j > rh[k]; --j) shorten(j);
    answ[k] = ans;
}
for(int i = 1; i <= m; ++i){
    if(answ[i] == 0){
        puts("0/1");
        continue;
    }
    int lnth = rh[i] - lf[i] + 1;
    long long t = 1LL * lnth * (lnth - 1) / 2;
    long long g = gcd(answ[i], t);
    printf("%lld/%lld\n", answ[i] / g, t / g);
}
return 0;
}

```

6.3 模拟退火

```

int n;
double A,B;
struct Point{
    double x,y;
    Point(){}
    Point(double x,double y):x(x),y(y){}
    void modify(){
        x = max(x,0.0);
        x = min(x,A);
        y = max(y,0.0);
        y = min(y,B);
    }
}p[1000000];
double sqr(double x){
    return x * x;
}

```

```

double Sqrt(double x){
    if(x < eps) return 0;
    return sqrt(x);
}
Point operator + (const Point &a,const Point &b){
    return Point(a.x + b.x, a.y + b.y);
}
Point operator - (const Point &a,const Point &b){
    return Point(a.x - b.x, a.y - b.y);
}
Point operator * (const Point &a,const double &k){
    return Point(a.x * k, a.y * k);
}
Point operator / (const Point &a,const double &k){
    return Point(a.x / k, a.y / k);
}
double det (const Point &a,const Point &b){
    return a.x * b.y - a.y * b.x;
}
double dist(const Point &a, const Point &b){
    return Sqrt(sqr(a.x - b.x)+sqr(a.y - b.y));
}
double work(const Point &x){
    double ans = 1e9;
    for(int i=1;i<=n;i++){
        ans = min(ans,dist(x,p[i]));
    }
    return ans;
}
int main(){
    srand(time(NULL));
    int numcase;
    cin>>numcase;
    while (numcase--){
        scanf("%lf%lf%d",&A,&B,&n);
        for(int i=1;i<=n;i++){
            scanf("%lf%lf",&p[i].x,&p[i].y);
        }
        double total_ans = 0;
        Point total_aaa;
        for(int ii = 1;ii<=total/n;ii++){
            double ans = 0;
            Point aaa;
            Point p;
            p.x = (rand() % 10000) * A / 10000;
            p.y = (rand() % 10000) * B / 10000;
            double step = 2 * max(A,B);
            for(double T = 1e6;T > 1e-2;T = T * 0.98){
                double thi = (rand() % 10000) * pi2 / 10000;

```

```

        Point now = p + Point(cos(thi), sin(thi)) * step * (rand() %
            10000)/10000;
        now.modify();
        double now_ans = work(now);
        double delta = now_ans -ans;
        if(delta > 0) {
            p = now;
            ans = now_ans;
            aaa = now;
        }
        else{
            if((rand() % 10000) / 10000.0 > exp(delta / T)) p = now;
        }
        step = max(step * 0.9,1e-3);
    }
    if(ans > total_ans) total_ans = ans, total_aaa = aaa;
}
printf("The safest point is (%.1f, %.1f).\n",total_aaa.x,total_aaa.y
);
}
}

```

6.4 Java

```

import java.io.*;
import java.util.*;
import java.math.*;
public class Main{
    public static BigInteger n,m;
    public static Map<BigInteger,Integer> M = new HashMap();
    // public static BigInteger dfs(BigInteger x){
    //     if(M.get(x)!=null)return M.get(x);
    //     if(x.mod(BigInteger.valueOf(2))==1){
    //         }else{
    //             }
    //         }
    //     M.put();
    // }
    static int NNN = 1000000;
    static BigInteger N;
    static BigInteger M;
    static BigInteger One = new BigInteger("1");
    static BigInteger Two = new BigInteger("2");
    static BigInteger Zero = new BigInteger("0");
    static BigInteger[] queue = new BigInteger[NNN];
    static BigInteger[] num_step = new BigInteger[NNN];
    public static void main(String []arg){
        Scanner cin = new Scanner(System.in);

```

```

        while(true){
int p = cin.nextInt();
n = cin.nextBigInteger();
m = cin.nextBigInteger();
n.multiply(m);
M.clear();
if(n.compareTo(BigInteger.ZERO)==0) break;
if(n.compareTo(m)<=0){
                System.out.println(m.subtract(n));
                continue;
        }
BigInteger[] QB = new BigInteger[5000*20];
Integer[] QD = new Integer[5000*20];
int head=0,tail=0;
QB[tail]=n;
QD[tail]=0;
tail++;
BigInteger ans = n.subtract(m).abs();
while(head<tail){
    BigInteger now = QB[head],nxt;
    int dep = QD[head];
    //System.out.println("now is "+now+" dep is "+dep);
    if(ans.compareTo(BigInteger.valueOf(dep).add(m.subtract(now).abs
    ()))>0)
        ans=BigInteger.valueOf(dep).add(m.subtract(now).abs());
    head++;
    if(now.mod(BigInteger.valueOf(2)).compareTo(BigInteger.ONE)!=0){
        nxt=now.divide(BigInteger.valueOf(2));
        if(M.get(nxt)==null){
            QB[tail]=nxt;
            QD[tail]=dep+1;
            tail++;
            M.put(nxt,1);
        }
    }else{
        nxt=now.subtract(BigInteger.ONE);
        if(M.get(nxt)==null&&nxt.compareTo(BigInteger.ZERO)!=0){
            QB[tail]=nxt;
            QD[tail]=dep+1;
            tail++;
            M.put(nxt,1);
        }
        nxt=now.add(BigInteger.ONE);
        if(M.get(nxt)==null){
            QB[tail]=nxt;
            QD[tail]=dep+1;
            tail++;
            M.put(nxt,1);
        }
    }
}

```

```

        }
    }
}
System.out.println(ans);
}
}
}

```

还有这样的 `hashset` 用法：

```

static Collection c = new HashSet();
if(c.contains(p) == false)

```

6.5 博弈论相关

1. Anti-SG: 规则与 Nim 基本相同, 取最后一个的输。先手必胜当且仅当: (1) 所有堆的石子数都为 1 且游戏的 SG 值为 0; (2) 有些堆的石子数大于 1 且游戏的 SG 值不为 0。
2. SJ 定理: 对于任意一个 Anti-SG 游戏, 如果我们规定当局面中, 所有的单一游戏的 SG 值为 0 时, 游戏结束, 则先手必胜当且仅当: (1) 游戏的 SG 函数不为 0 且游戏中某个单一游戏的 SG 函数大于 1; (2) 游戏的 SG 函数为 0 且游戏中没有单一游戏的 SG 函数大于 1。
3. Multi-SG 游戏: 可以将一堆石子分成多堆。
4. Every-SG 游戏: 每一个可以移动的棋子都要移动。对于我们可以赢的单一游戏, 我们一定要拿到这一场游戏的胜利。只需要考虑如何让我们必胜的游戏尽可能长的玩下去, 对手相反。于是就来一个 DP, $\text{step}[v] = 0$; (v 为终止状态) $\text{step}[v] = \max \text{step}[u] + 1$; ($\text{sg}[v] > 0, \text{sg}[u] = 0$) $\text{step}[v] = \min \text{step}[u] + 1$; ($\text{sg}[v] = 0$)
5. 翻硬币游戏: N 枚硬币排成一排, 有的正面朝上, 有的反面朝上。游戏者根据某些约束翻硬币 (如: 每次只能翻一或两枚, 或者每次只能翻连续的几枚), 但他所翻动的硬币中, 最右边的必须是从正面翻到反面。谁不能翻谁输。结论: 局面的 SG 值为局面中每个正面朝上的棋子单一存在时的 SG 值的异或和。可用数学归纳法证明。
6. 无向树删边游戏: 规则如下: 给出一个有 N 个点的树, 有一个点作为树的根节点。游戏者轮流从树中删去边, 删去一条边后, 不与根节点相连的部分将被移走。谁无路可走谁输。结论: 叶子节点的 SG 值为 0; 中间节点的 SG 值为它的所有子节点的 SG 值加 1 后的异或和。是用数学归纳法证明。
7. Christmas Game(PKU3710): 题目大意: 有 N 个局部联通的图。Harry 和 Sally 轮流从图中删边, 删去一条边后, 不与根节点相连的部分将被移走。Sally 为先手。图是通过从基础树中加一些边得到的。所有形成的环保证不共用边, 且只与基础树有一个公共点。谁无路可走谁输。环的处理成为了解题的关键。性质: (1) 对于长度为奇数的环, 去掉其中任意一个边之后, 剩下的两个链长度同奇偶, 抑或之后的 SG 值不可能为奇数, 所以它的 SG 值为 1; (2) 对于长度为偶数的环, 去掉其中任意一个边之后, 剩下的两个链长度异奇偶, 抑或之后的 SG 值不可能为 0, 所以它的 SG 值为 0; 所以我们可以去掉所有的偶环, 将所有的奇环变为长短为 1 的链。这样的话, 我们已经将这道题改造成了上一节的模型。
8. 无向图的删边游戏: 我们将 Christmas Game 这道题进行一步拓展——去掉对环的限制条件, 这个模型应该怎样处理? 无向图的删边游戏: 一个无向联通图, 有一个点作为图的根。游戏者轮流从图中删去边, 删去一条边后, 不与根节点相连的部分将被移走。谁无路可走谁输。结论: 对无向图做如下改动: 将图中的任意一个偶环缩成一个新点, 任意一个奇环缩成一个新点加一个新边; 所有连到原先环上的边全部改为与新点相连。这样的改动不会影响图的 SG 值。

9. Staircase nim: 楼梯从地面由下向上编号为 0 到 n 。游戏者在每次操作时可以将楼梯 $j(1 \leq j \leq n)$ 上的任意多但至少一个硬币移动到楼梯 $j-1$ 上。将最后一枚硬币移至地上的人获胜。结论: 设该游戏 Sg 函数为奇数格棋子数的 Xor 和 S 。如果 $S=0$, 则先手必败, 否则必胜。

7 Tips

判斜率 $(x/gcd, y/gcd)$ 直接丢 map 里 unique

无方案和答案 $\% MOD$ 为 0 是有区别的

打标记使用时间戳

$a = 10 * a + 1$ 可以用矩乘加速

数组要开 $1e5 [+ 5]!$

$\text{pow}(a, b)$ 会调用 c++ 自带函数

强联通、双联通要考虑一个孤立点

MOD 的时候: $(a - b + MOD) \% MOD$ $(a + b * c \% MOD) \% MOD$

stack 里有时存的边, 这种时候大小不要开错了

选择性段错误: 没 return 没赋初值

凸包排序后数组顺序会改变, 不可以在这之后求重心

位运算优先级小于 $==$

$(\text{int})x \neq \text{round}(x)$

hash 字符串: $t = t * 27(!) + s[i] - 'A' + 1$

有些 dfs 里用到的数组开全局会跪

$n = 1e4$ 时明摆着要 n^2 bitset 压位

$\text{fact}[0] = 1$

在打表找规律之前要先自己试几组数据, 确保暴力程序的正确性

到最后阶段如果还卡算法应该去冲一冲暴力。

没有测一些极小的数据, 为 0 或 1 的情况没有考虑, 有时候需要特判。

个性坑点

cjy:

$\text{vector} < \text{int} > v$; $\text{for}(\text{int } i = 0; i < (\text{没有}) v.\text{size}(); ++i)$

Hash map $< \text{unsigned long long}, \text{int} >$ hash 时乘的常数, 以及 $\text{idx}()$ 返回值均需 ULL

double 不要开成 int

long long 读入别忘开 ll 读

读题还是要有重点的去读

求最短路上的边的集合, 要用 $\text{dist1}[u] + \text{dist2}[v] + \text{len}(u, v) == \text{dis}(S, T)$ 。 $\text{dist1}[v] + \text{dist2}[v] == \text{dis}(S, T)$ 只是说明点 v 在最短路上。

改动代码之后要检查对原来对的输出结果有没有影响, 不能只关注改动的结果变化。

树链剖分搜出 DFS 序要先访问 size 最大的儿子, 来保证一条重链在 DFS 序中为一段连续的区间。

行列 n/m 写错 (经常出现), 可以自己测一些行列差别较大的数据。这可能也会出现 RE 的情况。

分解质因数, 注意 $n=1$ 的情况, 质因数个数为零。

位运算 $<<$, 范围超过 int 需要用到 long long 的时候, 要写 1LL 左移。

对题目中的一些数据进行了重新标号 (如离散化、排序、dfs 序、拓扑序) 之后, 使用的时候要注意是原标号还是新的标号, 主要区分是用到标号的数组还是数组下标。

想到了正解高斯消元, 因为看到精度要到 $1e-8$, 感觉精度会有问题而没有进行尝试。

用实数进行高斯消元，找系数非零的方程，直接找系数绝对值最大的，可以不用到`eps`

网络流的时候要注意不要漏算连向源和汇的边数。

多组数据时中途-1不要`return 0`.

xxxxxyt:

1、审题方面:

- (1) 对题目中的重点应采取恰当的勾画，需要重点勾画出的内容有：明确提出要求的句子、关键词 (`distinct`, `successive`, `directed` etc)、数据范围、特殊的要求或条件、有疑问的地方
- (2) 尽量不要按照自己的思维模式对不清楚的题意进行猜测，而且也不要过于相信生活经验（因为题目的模型往往与现实又很大差别），即便有这样的猜测也应当明确标注出并告诉队长
- (3) 不能为了节省一点点时间而跳过某些自以为无聊的句子（条件也可能出现在背景描述中）不读
- (4) 在听完队友讲述的题意后也应该读一遍`input/output`确认格式

2、算法方面:

- (1) 有时会将具体问题过分抽象化，反而导致忽略了最直观的模拟算法
- (2) 想到一个算法时没有完全`check`清它的正确性就告诉队长，导致有时队长没有看出错的话就会浪费大量机时，所以想到算法后不应该先急于表达，而且`check`的时候要带入题目中的所有关键点以查看有没有考虑漏的情况
- (3) 有时会出错的反例导致思维偏离正确方向，出反例的时候应该更加严谨
- (4) 敢冲敢过
- (5) 有时会在仔细思考如何递推之前盲目地打表找规律，浪费了大量时间

3、实现方面:

- (1) 准备的时候需要考虑这些事：需要用到几个函数以及这些函数应该怎么写、需要用到哪些变量以及与其相关的初值问题清零问题、边界情况和特殊情况，但没有必要将它们都写在纸上
- (2) 有时候会犯一些粗心的错误，如：忘记删掉调试语句（交之前一定要浏览一次整个代码及跑一遍样例`check`）、数组大小算错
- (3) 代码常数经常会很大（暂时还不知道怎么改善）
- (4) 对待多组测试数据时要有效地进行预处理与反复利用记忆化搜索的结果

做法向

博弈题做法：1.由最终态BFS（类似构了一颗树）2.打表找`sg`函数规律

没辙时想`dp`和网络流

启发式合并 `nlgn`

$$n / 1 + n / 2 + \dots = nlgn$$