## **Problem Set 3**

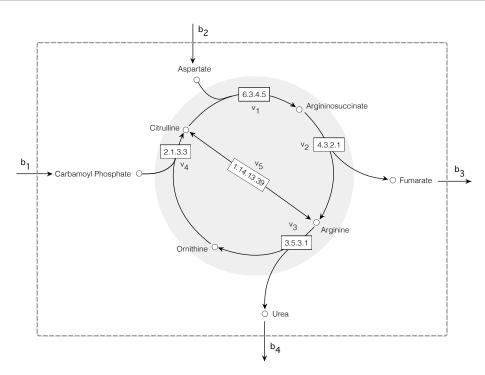


Figure 1: Schematic of the Urea cycle.

1. The urea cycle eliminates excess nitrogen from the cell (Fig. 1). Let's explore this cycle in a growing population of human cells with a doubling time of  $\tau_d$  = 20 hr.

**Assume**: (i)  $k_{cat}$ 's for the enzymes in the pathway are: EC:3.5.3.1 = 249s<sup>-1</sup>; EC:2.1.33 = 88.1s<sup>-1</sup>; EC:4.3.2.1 = 34.5s<sup>-1</sup>; EC:6.3.4.5 = 203s<sup>-1</sup> and EC:1.14.13.39 = 13.7s<sup>-1</sup>; (ii) the approximate steady-state concentration for enzymes in the pathway (E) is uniform, and given by  $E \simeq 0.01~\mu \text{mol gDW}^{-1}$ ; (iii) use Park *et al* Nat Chem Biol 12:482-9, 2016 for  $K_m$  and metabolite concentrations to calculate the saturation term for the flux bounds (see supplemental materials); (iv) all enzymes are maximally active.

- a) Use KEGG (Arginine biosynthesis in human) to construct the stoichiometric matrix **S** for the urea cycle shown in Fig. 1.
- b) Determine if your urea cycle reconstruction is elementally balanced for C,H,N,O,P and S. If not, how can you correct the balances? (**hint**: write elemental balances around C,H,N,O,P and S).

c) Calculate the maximum rate of urea production ( $b_4$  mmol/gDW-hr) given: 0  $\le$   $b_j \le$  10 mmol/gDW-hr  $\forall j$  using Flux Balance Analysis (FBA). If additional inputs/outputs are required, assume they obey the same bounds constraints.