

# 递归方程

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$$f(n) = 6f(n-1) - 8(n-2)$$

$$f(1) = 1$$

$$f(2) = 0$$

求下面特征方程的解

$$n^2 - 6n + 8 = 0$$

得到  $n = 2, 4$

$$f(n) = C1 * 2^n + C2 * 4^n$$

根据初始条件

$$f(1) = C1 * 2 + C2 * 4 = 1$$

$$f(2) = C1 * 4 + C2 * 16 = 0$$

得

$$C1 = 1$$

$$C2 = -\frac{1}{4}$$

$$f(n) = 2^n - \frac{1}{4} * 4^n = 2^n - 4^{n-1}$$