
Algorithm 1: Naïve Single-Pass Insertion-Streaming Algorithm for Neighbourhood Detection

require: Stream $\{(s_0, t_0) \dots (s_n, t_n)\}$, degree bound d , precision bound c

- 1 $N \leftarrow \{\{\}\}$ {neighbourhoods}
- 2 **for** $i = 0 \dots n$ **do**
- 3 append t_i to $N[s_i]$
- 4 **if** $\text{size}(N[s_i]) = \frac{d}{c}$ **then return** $(s_i, N[s_i])$;
- 5 **return** *FAIL*

Algorithm 2: One-pass c -approximation Insertion-Only Streaming Algorithm for Neighbourhood Detection

require: Space s , degree bound d .

- 1 $s \leftarrow \lceil \ln(n) \cdot n^{\frac{1}{c}} \rceil$
- 2 **for** $i \in [0, c-1]$ **in parallel do**
- 3 $(a_i, S_i) \leftarrow \text{Deg-Res-Sampling}(\max\{1, i \cdot \frac{d}{c}\}, \frac{d}{c}, s)$
- 4 **return** *Uniform random neighbourhood (a_i, S_i) from the successful runs*

Algorithm 3: One-pass c -approximation Insertion-Deletion Streaming Algorithm for Neighbourhood Detection. (Vertex Sampling)

require: Space s , degree bound d .

- 1 Let $x = \max\{\frac{n}{c}, \sqrt{n}\}$
- 2 Sample a uniform random subset $A' \subseteq A$ of size $10 x \ln n$ of vertices.
- 3 **for** $a \in A'$ **do**
- 4 Run $10 \frac{d}{c} \ln n$ l_0 -samplers on the set of edges incident to a .
- 5 **return** *Any neighbourhood of size $\frac{d}{c}$ among the stored edges, if there is one.*

Algorithm 4: One-pass c -approximation Insertion-Deletion Streaming Algorithm for **Neighbourhood Detection**. (Edge Sampling)

require: Space s , degree bound d .

- 1** Let $x = \max \left\{ \frac{n}{c}, \sqrt{n} \right\}$
 - 2** Run $20 \frac{nd}{c} \left(\frac{1}{x} + \frac{1}{c} \right) \ln(n)$ l_0 samplers on the stream, in parallel. Each producing a uniform random edge.
 - 3 return** *Any neighbourhood of size $\frac{d}{c}$ among the stored edges, if there is one.*
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