

Image Processing and Computer Vision - Notes

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Contents

1	Image Acquisition	2
2	Image Representation	2

1 Image Acquisition

Proposition 1.1 - Common Challenges with Image Acquisition

Below are some common challenges that are faced/produced by image acquisition

Viewpoint Variation	Several images may be taken of the same object but will vary the angle
Illumination	Images may be taken in low/high light
Occlusion	Object may be partly obscured
Scale	Objects may look vary different when placed next to other objects due to their relative scale
Deformation	Objects may have slight variations on the perfect form
Background Clutter	Lots happening behind an object may work to obscure it
Object Intra-Class Variation	Some objects in the same class can vary a lot in shape (<i>e.g.</i> chairs)
Local Ambiguity	Certain regions of an image can be missinturped without the rest of the scene being accounted for
World Behind the Image	Depth may need to be accounted for to make sense of an image.

Definition 1.1 - Dirac Delta-Function, δ

The *Dirac Delta-Function* is used to map continuous distributions to discrete distributions by sampling at particular intervals. Intuitively

$$\delta(t) = \begin{cases} 1 & , t = 0 \\ 0 & , t \neq 0 \end{cases} \implies \delta(t - \alpha) = \begin{cases} 1 & , t = \alpha \\ 0 & , t \neq \alpha \end{cases}$$

Definition 1.2 - Sifting Property

We can apply the *Dirac Delta-Function* to a function to sample a particular value

$$\int_{-\infty}^{\infty} f(t)\delta(t)dt = f(0) \implies \int_{-\infty}^{\infty} f(t)\delta(t - \alpha)dt = f(\alpha)$$

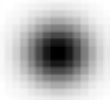
This can be applied to 2D objects (such as images) as

$$\int_{-\infty}^{\infty} f(a,b)\delta(a - x, b - y)dadb = f(x, y)$$

Definition 1.3 - Point Spread-Function

A *Point Spread-Function* is applied after sampling an image. It takes the value of a pixel & transforms pixels around it using this value in some way.

e.g.



2 Image Representation

Definition 2.1 - Colour Space

Colour Space are different techniques for representing colours. These are generally made up of 3D vectors.

Colour Space	Vector Description
RGB	(Red $\in [0, 255]$, Green $\in [0, 255]$, Blue $\in [0, 255]$)
HSI	(Hue $\in [0, 360]$, Saturation $\in [0, 1]$, Intensity $\in [0, 1]$) Hue gives the colour in degrees
YUV	(Brightness $\in [0, 255]$, Blue Projection $\in [0, 255]$, Red Projection $\in [0, 255]$)
La*b*	(Luminance $\in [0, 100]$, Red/Green $\in \{-a, +b\}$, Blue/Yellow $\in \{+b, -b\}$)

Remark 2.1 - Representing Video

To represent video each fixel is given a third parameter, *time* so we now have

$$f(x, y, t) \mapsto (R, G, B)$$

or any other *Colour Space*.

Definition 2.2 - Quantisation

Quantisation is representing a continuous single channel function with discrete single channel function that groups the continuous values into a set number of levels.

Example 2.1 - Quantisation

16 levels



6 levels



2 levels

Definition 2.3 - Aliasing

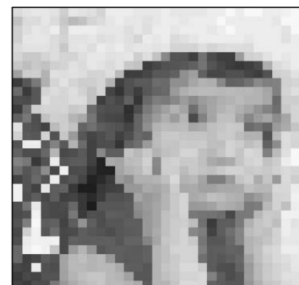
Aliasing is the result of sparse sampling since single pixels represent too large an area to get any detail out of it.

Example 2.2 - Aliasing

256 x 256



64x64



32x32

Definition 2.4 - Anti-Aliasing

Anti-Aliasing is the process for avoiding *Aliasing*. This can be achieved by using a sampling rate which is a critical limit defined by the *Shannon-Nyquist Theorem*.

Theorem 2.1 - Shannon-Nyquist Theorem

An analogue signal with maximum frequency x Hz may be completely reconstructed if regular samples are taken with frequency $2x$ Hz.

Definition 2.5 - Convolution

Convolution is an operation which takes two functions & produces a third which describes how the shape of one of the two functions is changed by the other.

For functions f & g

$$(f * g)(x) := \int_{-\infty}^{\infty} f(x - t)h(x)\partial t$$

N.B. $*$ is the symbol for convolution.

