Problems Sheet 1

Statistics 2

Dom Hutchinson

Question 4

Part a)

```
xobs <- rexp(10,rate=0.3) # Sample 10 values from Exp(0.3) distribution
xobs

## [1] 0.5703693 4.2013839 1.7229474 5.4031092 2.5544691 0.7798337 6.5379667
## [8] 5.5766792 7.6785288 0.5681968

Part b)

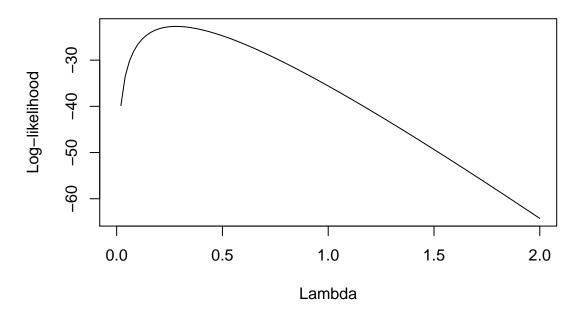
# Returns log-likelihood for different values of lambda, using observed values
ell <- function(lambda,obs) {
   n <- length(obs)
   n*log(lambda)-lambda*n*mean(xobs) # Log-likelihood function for exponential distribution</pre>
```

Part c)

```
# Generate 101 equally seperated values between 0 & 2
lvals <- seq(from=0,to=2,length=101)

# Plot log-likelihood value for each element of lvals, using observed values
plot(lvals,ell(lvals,xobs),type = 'l',
main = 'Log-likelihood for lambda', xlab = 'Lambda',
ylab = 'Log-likelihood')</pre>
```

Log-likelihood for lambda



Part d)

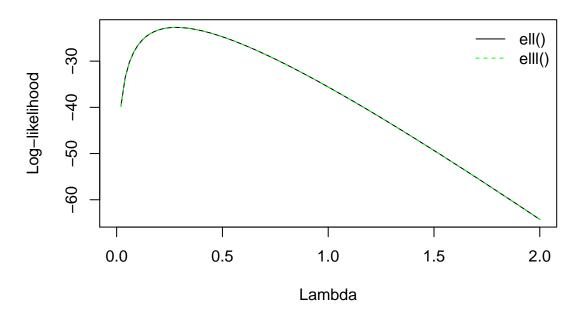
```
# For each element in lambda return sum of dexp for observed values
elll <- function(lambda,obs) {
    sapply(lambda, function(lv) sum(dexp(obs, rate=lv, log=TRUE)))
}

# Line produced by ell()
plot(lvals,ell(lvals,xobs),type = 'l',
main = 'Log-likelihood for lambda', xlab = 'Lambda',
ylab = 'Log-likelihood')

# Line produced by elll()
lines(lvals,elll(lvals,xobs),col="green",lty=2)

legend("topright",legend=c('ell()','elll()'),lty=c(1,2),col=c('black','green'),pch=NA,bty='n')</pre>
```

Log-likelihood for lambda



Part e)

```
x<-1:5 # [1,2,3,4,5]

# Print each element
sapply(x,function(xv) xv)

## [1] 1 2 3 4 5

# Print square of each element
sapply(x,function(xv) xv^2)

## [1] 1 4 9 16 25

# For each element, print 'foo'
sapply(x, function(xv) 'foo')

## [1] "foo" "foo" "foo" "foo" "foo"</pre>
```