Statistical Machine Learning HWZ H(x,Y) = H(Y/X) tH(X) 1. WJ HLX17) - HLX(7) - H(1/1/X) - 1-1 (71x) + 1-1 (x) -1-1(x)) - (-1(x)) = 1-(CX) - H(X|X) = I6(X;Y)ub, (i) Initial Entropy of Usage 13 H(S) = - P(Lon) · log; (P(Lon))-P(Medium)·log; (P(Med) 1:7 - P(High). logz (P(High)) M: J - (7/15).(og, (7/15) - (5/15).log, (5/15)-13/15).byz(3/4) (-(- 3 - 1.2028 ii) I want to choose the attribute which yields the

maximum internation gain First Attribute - Income Kijh Medim Categorical values - lon LMH LMH 2 4 9 H(Income: Lon) = - (J/5). log/JJJ)-0-0=0 H (Income = [Medium] = - (2/6) · (092(2/6) - (4/6) · log2(4/6)-0=0.918} 14 (Invance = 14 17 h) = -0 - ((/4).log,(1/4) - (3/4).log,(3/4)=0.81127 Average Entropy intormation for Income. H (Usage | Ireame) = P(Lon). H(Ireame = Lon) + P(Med). H(Ireame=lan) tpcltryh). HlIncome = High = £.0.81127 Tutermention gain = 1.Jat8-0.58365-0.92213/ - U LOSPL

Second Attribute Age Young Lategorium values - Old L M H 0 5 1 [-1 (Age = old)= - 17/9).log_(7/9)-0-(2/9)-log_(2/9)=0.7642 [-1 (Age = Young) = -0 - (5/6).log, (5/6)-(1/6).log, (1/6)=0.65 Average entropy Information for Age H(Usage | Age) = P(Old). H(Age=Old) + P(young). H(Age=young) = (9/15)·0.7642+(6/15)·0.65 = 0.71852Information Gam - H(S) - H(Usage | Age)

$$= 1.5058 - 0.71852$$

$$= 10.78728$$

Third Attribute - Education

[-1 (Edn = Univ) = -(3/6): log2(3/6)-9 - (3/6): log2(3/6)= H (Fedn = College) = -0 - (515). logs(515) - 0 = 0 Average Entropy Information for Education.

H(Vsuge | Edu) = P(Univ). H(Edu= Univ) + P((olkge). H(Edu=(ollege)

+ P (High). H (Edn= High) = 6/15·1+ 5/15·0+ 4/15·0 = 6/15= 0.4 Information Gain = HLS) - HLUsuge (Edn) = 1.5058 - O.4 [820],]] Fourth Attribute - (Murital Status Married Single (ategorical values -IN H C M IT H (Marital = Single) = -(2/7)-logz(2/7) - (2/7)-logz(2/7)

-(3171-602(3/7)=1.55665

H ((hurital = Marred) = - (5/8). (og. 45/8) -(3/8). (og. 43/8) -0 = 0.95443. 1-1 (Usage | Marital) = PCs ingle) ++ (Marital = Single) + PCMarial). H (Martal=mornia) = 7115·1.55665 + 8/15·0.9544} - 1.23546 Intermetini Gan- HLS) - HLVsuge (Marital) = 1.5058- 1.2354b = [0.2.7:034/

I tere, the attribute with the maximum interpretion gain is Education

University College V High School

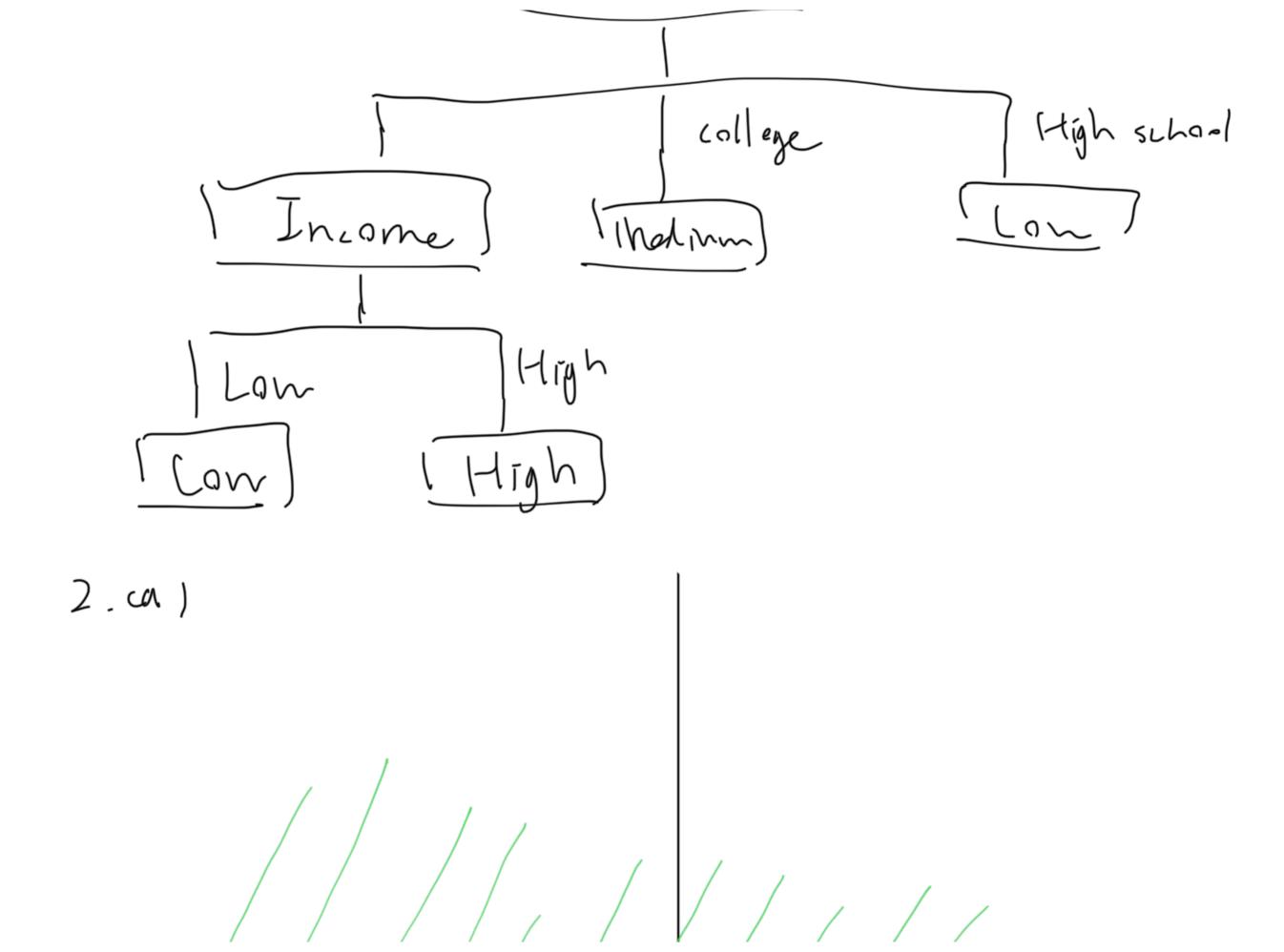
Medinm Lon Here, when advication = college, I.fs a pure closs of medium Usage. When education = High school, It's a pure class of Low usage. The only thing left is university Complete entropy at university is. H(S) = - (3/6). log, (3/6) - 0 - (3/6). log, (3/6) first Attribute, - Income. Medium High (rtegorical values, in H

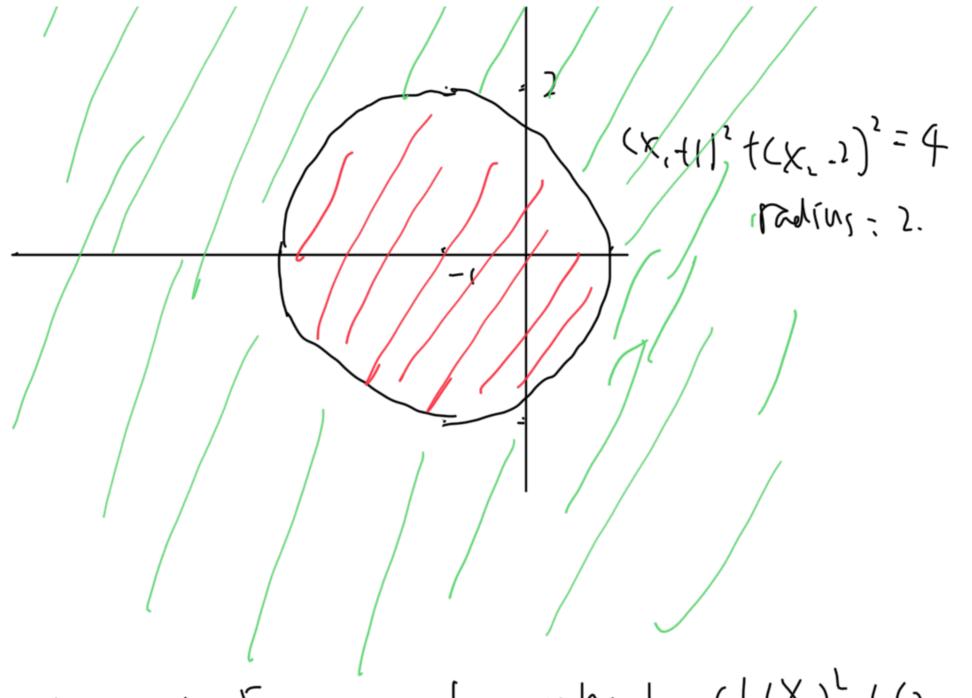
H(Univ, Income = Low) = - (3/3). loy, (3/3) -0-0=0 [-((Unir, Ipcone = Md) = -0-0-9=0 1-1 (univ, Income = High) = -0-0- (3/3) kgr (3/3/=5) [(univ, Income)= () Internation Gain: H(Univ) - I(Univ, Income)=1 Second Attribute, Age Young Categories - Old 5 L IN 11 C IN 14 3 0 2 14 (Univ, age = old) = -(3/J). (0/2/3/J) - (2/J). (0/2/2/5)-0=0.97/ H(Univ, age=yong)= -0-0-(111).logz(1/1)=0

I (Univ, age) = 516. Intermetion Gain- Hour	11 P.C (iv) -	J (Uni	v 110 v, oge)) = Q. (9084
Third Attribute - Marital					
categories —	sity l 3	L		&rrieo 3	
	(\script{0}			(
H (univ, marital status = H (univ, martal status = mara	Sirgle) = -0 - 0	0-(3/3). kg,<\	13) =0
I (univ, murity status) =	0		-)(,		•
Intermetion Gain = 1 Inthis case, both n	witn	J Sta	tus (inh.	Theome

In this case, both marital status and Income could be chosen as the next node.

(iii) choise one - choose murital status as second note Education] if High school University 1 College \ (Nedium Marital Status) Low 1 (Norried Simple 1 Law_ l High Choice two, choose theme as the second note. Education





(b) the set of points for which. (I+X1) + (1-X1) 74 is should by green.

the set et points for which (I+X1) + (2-X1) 54 is

should by red, with points on the circle classification (0,0) will fall in red class observation (-1,1) will fall in red class observation (2,2) will fall in blue class observation (3,8) will fall in blue class

(d) $(1+x_1)^2 + (2-x_2)^2 = 4$ $(x_1)^4 + 2x_1 + 1 + x_2^2 - 4x_2 + 4 = 4$ $(1+x_1)^4 + x_1^2 - 4x_2 + x_2^2 = 0$

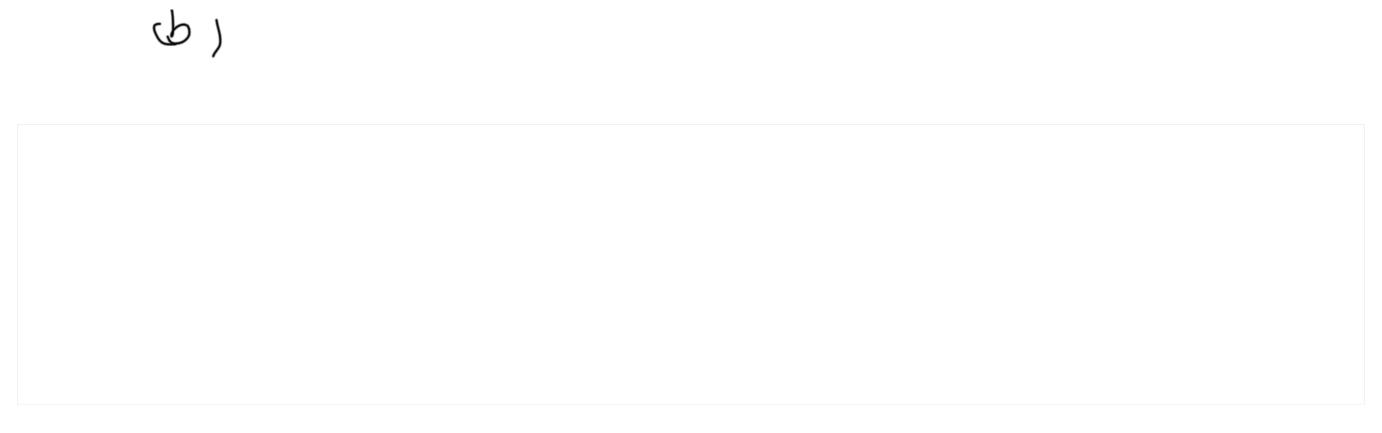
> As we can see that, through transformation. the decision boundary is in form

Botb, X, + br X, + br X, + br X, = 0

This is linear in terms of X, X, X, X, x, but

not linear in terms of only X, and Xz.

3.ca)



Graph (a) (b) (c) is linearly separable (d) is linearly separable with one miss classification.

The change from 1-NN to SVM is illustrated through graph

cc) Higher order polynomial lærnels such as quadratic lærnel could be applied to tigure (d) to male blue and red points linearly separable.

4-01 The absolute error Loss is L= 1y-f(x)1 and the epsilon insensitive loss turction will become $L_{\Sigma}(y,\hat{y}) = |y-\hat{y}|$ since $|y-\hat{y}|$ will always Z = 0 $f(x) = w^{T}x + b$ $|y-\hat{y}| = |y-\hat{y}|$

I would say, when $\varepsilon=0$, the epsilon insensitive loss function is the same as, the absolute error loss.

The E's function is that, in epsilon insensitive loss function, all the errors 1y-y | smaller than. E 1 distance of the observer value will be trented as 0.

(b) 1.... 1 5 1 (" "/x:1) + X////

· JUW) - To EI LE LD, DLMI \ 110 x1 - 1 = (1y -w1xi) - 2) + / | | w| 2 add slack variable, to the objective funition. - 小三(リールでxil-を)+人川ル川さけ 芝を; - h = ((y -w x; | - 2+2i) + > | | | | | | since the constrint is [{ [] y - ŷ (x;)] = { [] y - ŷ (x;)] - 2 , otherwise. I would like to add Si to the constraint. malary it 1 11-12015545:

LE LY, y C>11- 4) , y -y-1/- - 1 -1 1.e. y-gixi) is always smaller than £t5). mulcing it always give 0 for (E(y, gcxi)) non y-y(xi) = 2+ 2i - (y - y (xil) = 2t 2i y-g(xi) 2-2-2i The optimization function becomes Jan - 4 2 2: + 21 mll? with constraint N- ycxi) 55+ 5i

y-g(x;)?-2-5; and 2i ?0

This is an optimization problem that is differentiable and with linear constraints.

5.