## STAT406- Methods of Statistical Learning Lecture 3

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## Cross validation

We can show that

$$\begin{split} E_{\mathsf{data},Y|\mathbf{X}_0} & \left[ \left( Y - \hat{f}(\mathbf{X}_0) \right)^2 \right] \\ &= V(\hat{f}(\mathbf{X}_0)) + B^2 \left( \hat{f}(\mathbf{X}_0) \right) + V(\epsilon) \,, \end{split}$$

where V denotes variance and

$$B^{2}\left(\hat{f}(\mathbf{X}_{0})\right) = \left[E_{\mathsf{data}}\left(\hat{f}(\mathbf{X}_{0}) - f(\mathbf{X}_{0})\right)\right]^{2}.$$

is the squared bias:

## **Activity!**

## Cross validation

- Conservative lower bound for MSPE
- Discussion
- Proper way of using CV