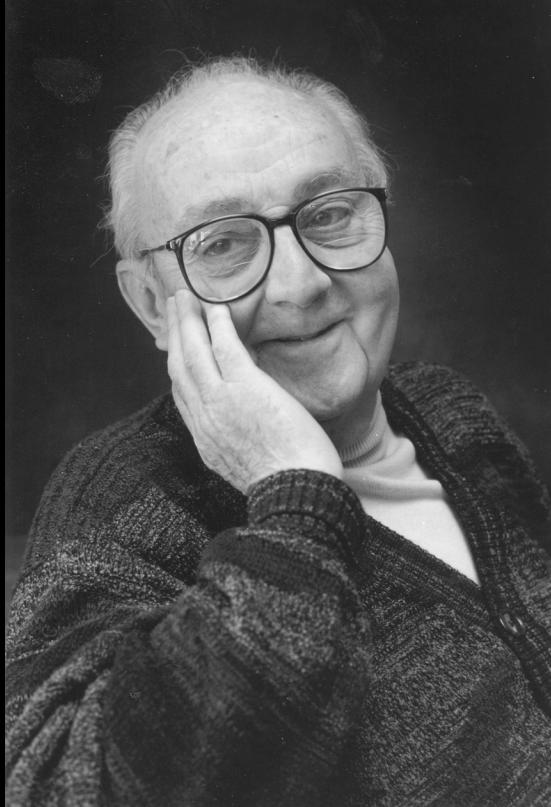


# A very short introduction to Modeling in Landscape Archaeology

Daniel Knitter



"Since all models are wrong  
the scientist cannot obtain a 'correct' one  
by excessive elaboration.

On the contrary following William of Occam  
[s]he should seek an economical description  
of natural phenomena.

Just as the ability to devise simple but evocative  
models is the signature of the great scientist  
so overelaboration and overparameterization  
is often the mark of mediocrity" (Box 1976, 792).

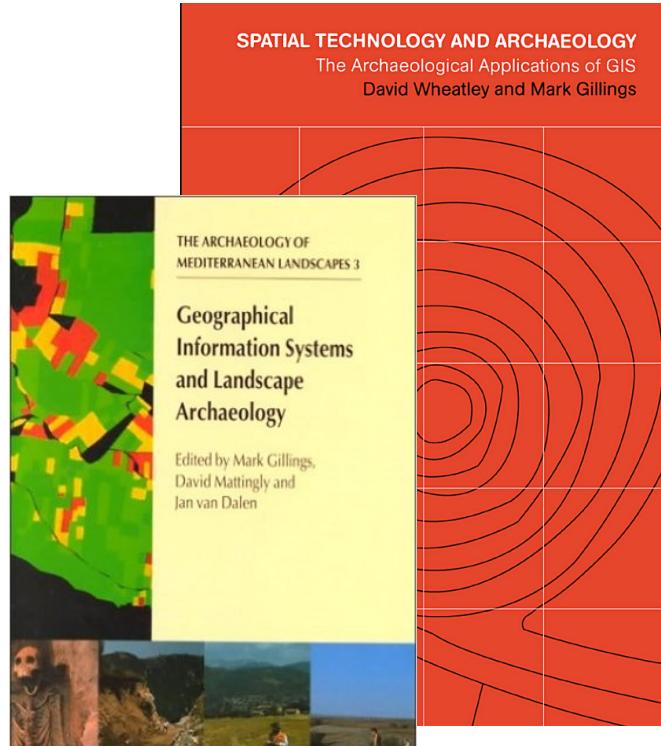
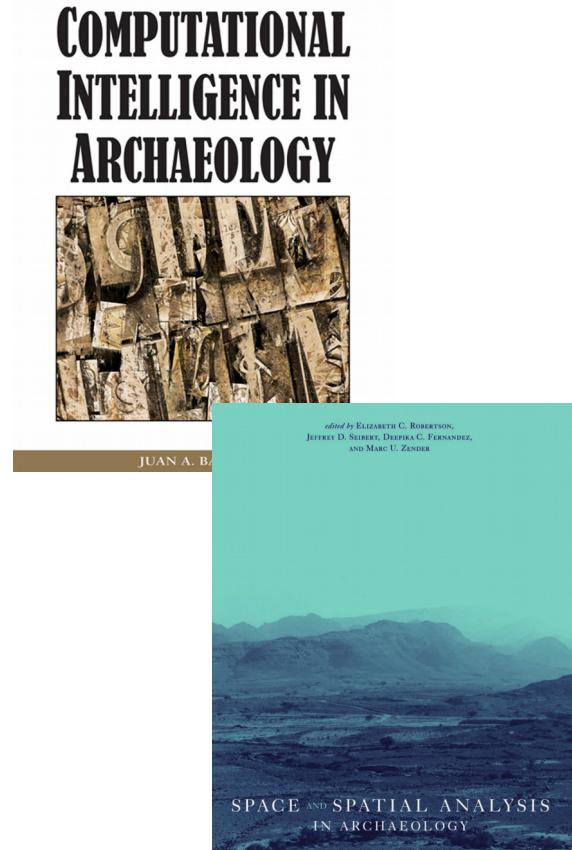
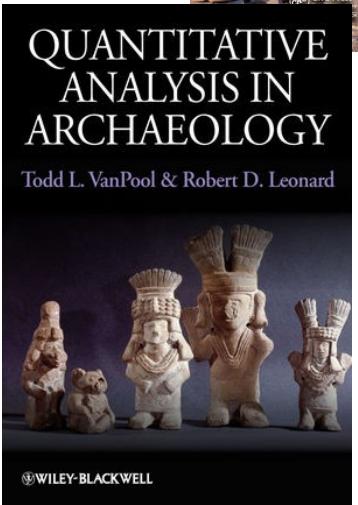
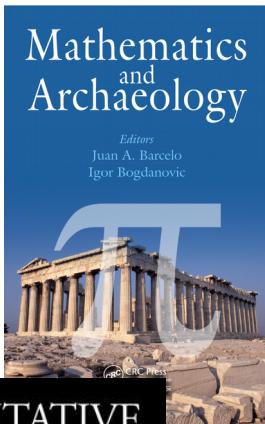
# Content

- Modeling and processes
- Why space matters: Potentials and Pitfalls of Spatial Data
- Point Pattern Analyses: What processes might have caused the distribution of findings?
  - First order processes (density based approaches)
  - Second order processes (distance based approaches)
- From single attributes to continuous surfaces: geostatistics
- Geomorphometry: What is the character of the landscape?
- Outlook

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# Modeling in (Landscape) Archaeology

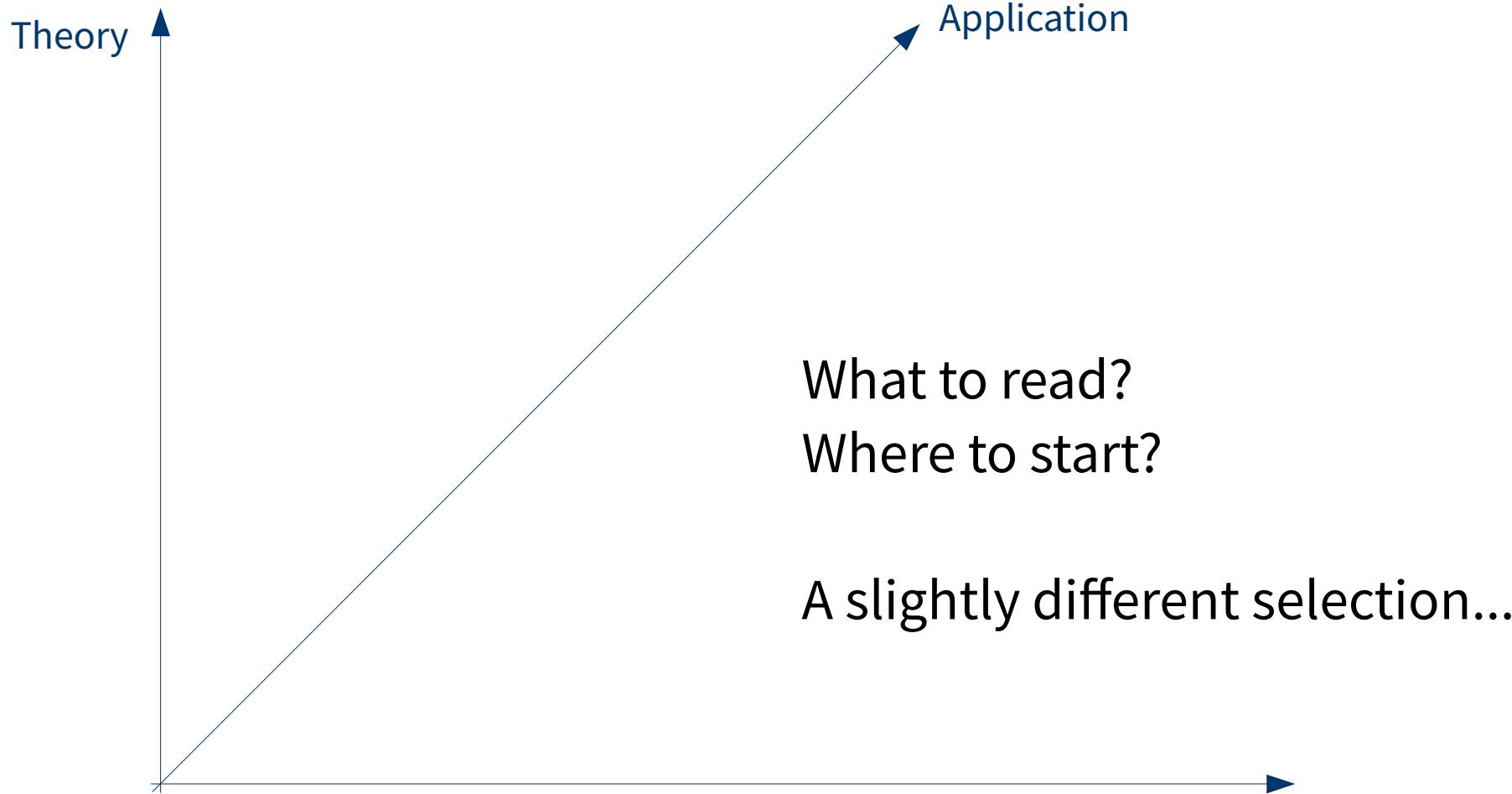


# Modeling in Landscape Archaeology

What to read?  
Where to start?

A slightly different selection...

# Modeling in Landscape Archaeology



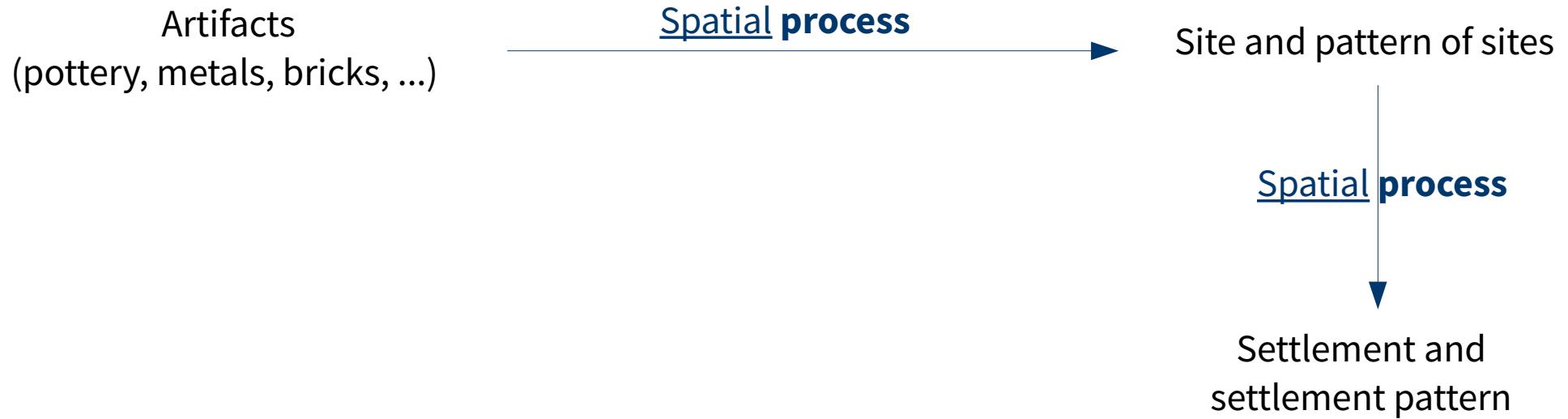


# Modeling in Landscape Archaeology

- Spatial phenomena are the result of processes
- Modeling = (re-)construction of these processes

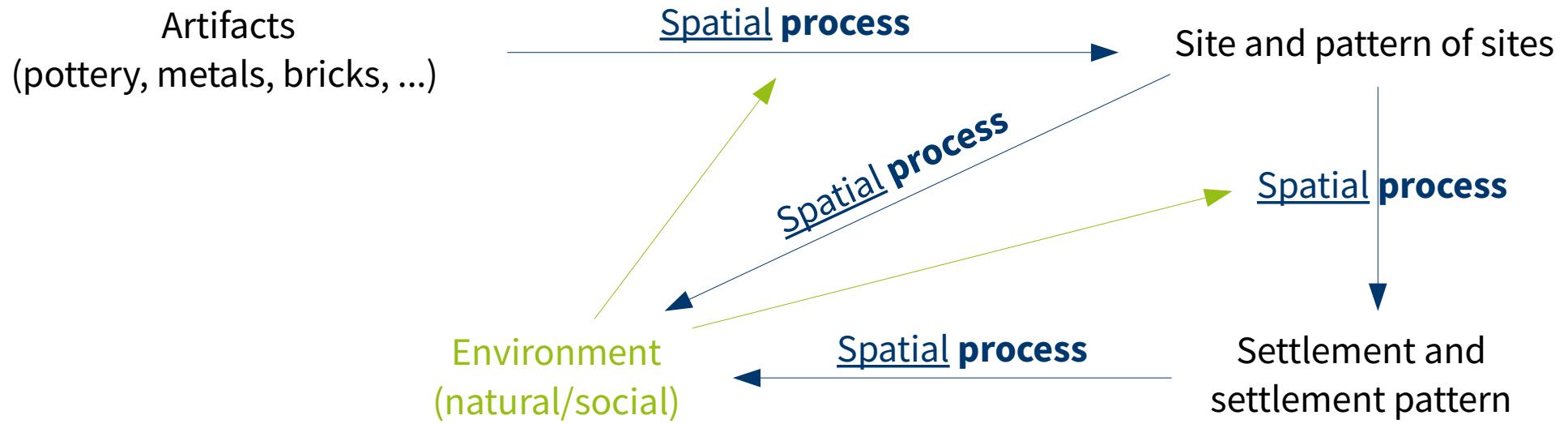
# Modeling in Landscape Archaeology

- Spatial phenomena are the result of processes
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# Modeling in Landscape Archaeology

- Spatial phenomena are the result of processes
- Modeling = (re-)construction of these processes



# Modeling in Landscape Archaeology



# Modeling in Landscape Archaeology

Modeling as a recursive activity.



# Content

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# Spatial data are special

Pitfalls of spatial data:

- spatial autocorrelation
- modifiable areal unit problem
- scale
- ecological fallacy
- non-uniformity of space
- edge effects

# Spatial autocorrelation

The Earth is not an isotropic plate

Spatial data are not random

Data from locations near to each other are usually more similar than data far away from each other

Space and location are important because of Spatial autocorrelation.

Without spatial autocorrelation, spatial analyses would be pointless

# Spatial autocorrelation



Low



High

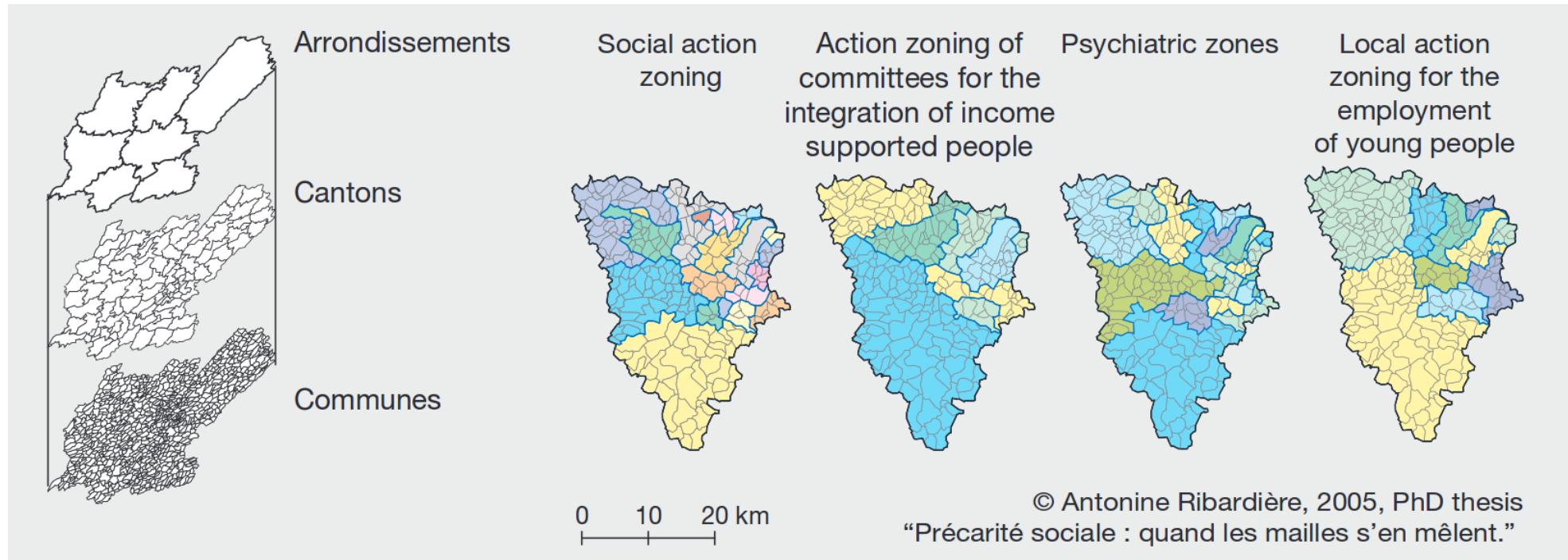


Maximum

# Modifiable Areal Unit Problem (MAUP)

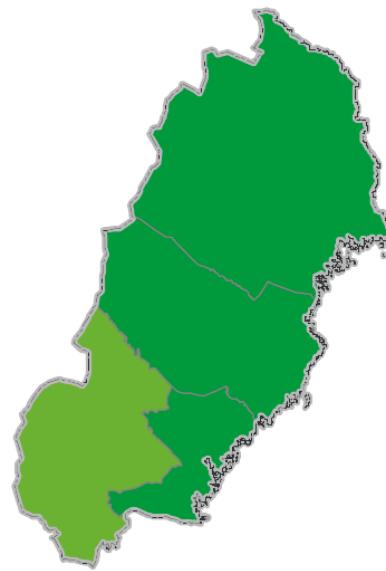
- aggregation units used are arbitrary with respect to the phenomena under investigation
  - If spatial units are specified differently, one might get very different patterns
- Openshaw, Stan (1984): The modifiable areal unit problem

# Modifiable Areal Unit Problem (MAUP)

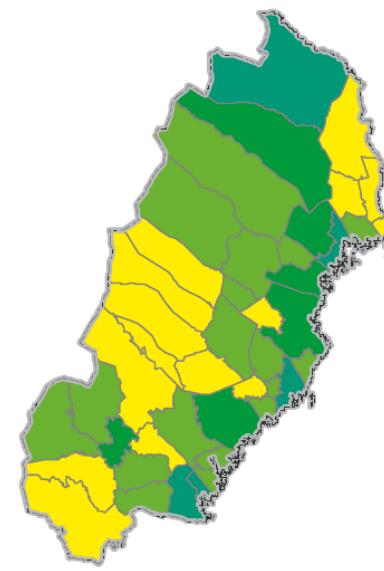


# Modifiable Areal Unit Problem (MAUP)

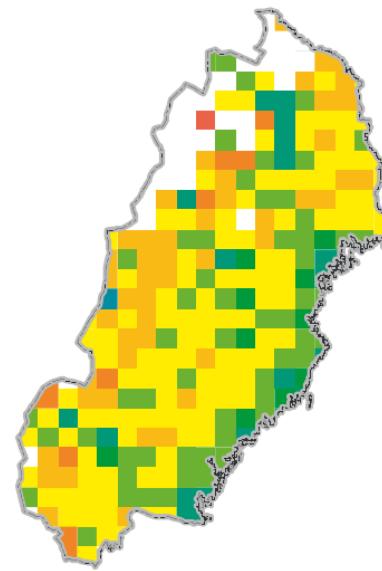
Provinzen (NUTS 3)



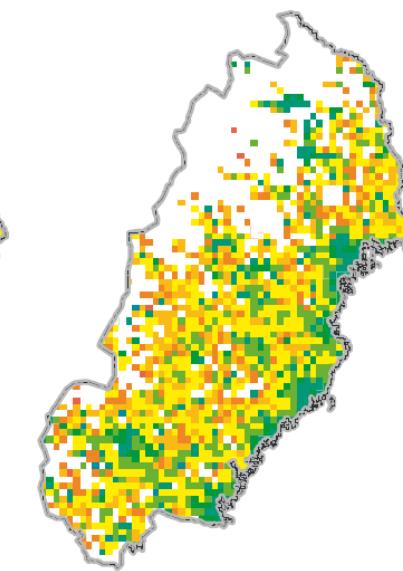
Gemeinden (NUTS 5)



30 km-Raster



10 km-Raster

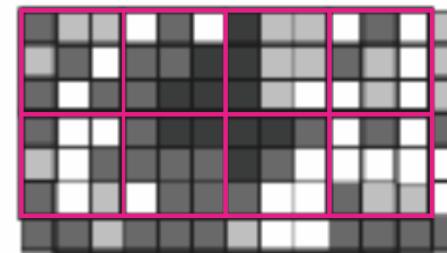
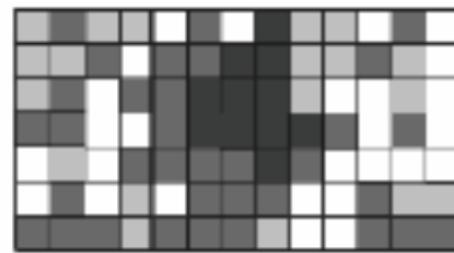


Verfügbares Einkommen  
in schwed. Kronen je  
Einwohner über 15 Jahre  
2002

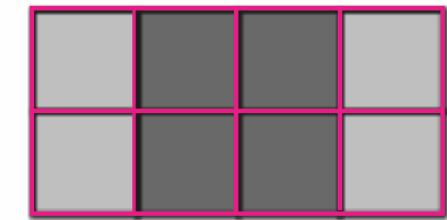


© M. Strömgren, K. Holme, E. Holm, S.M.C., Umeå University, Sweden

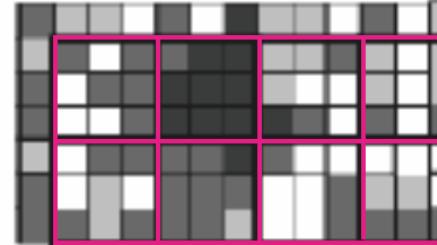
# Modifiable Areal Unit Problem (MAUP)



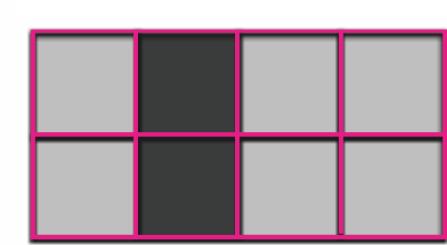
Zone A



Mean of zones



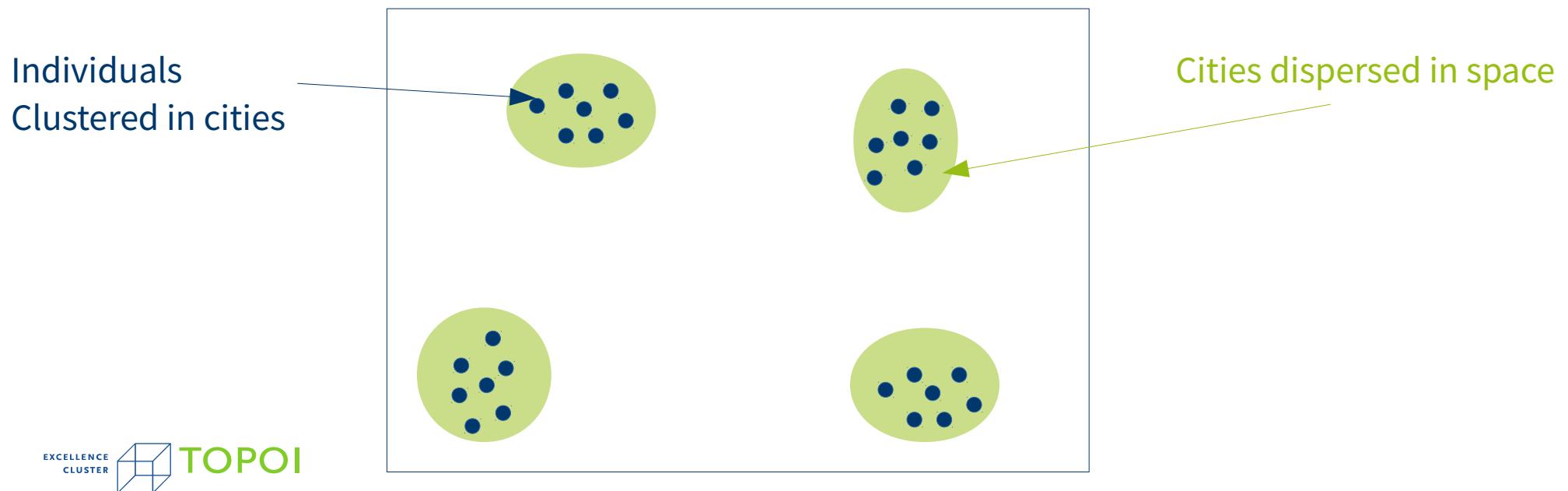
Zone B



Mean of zones

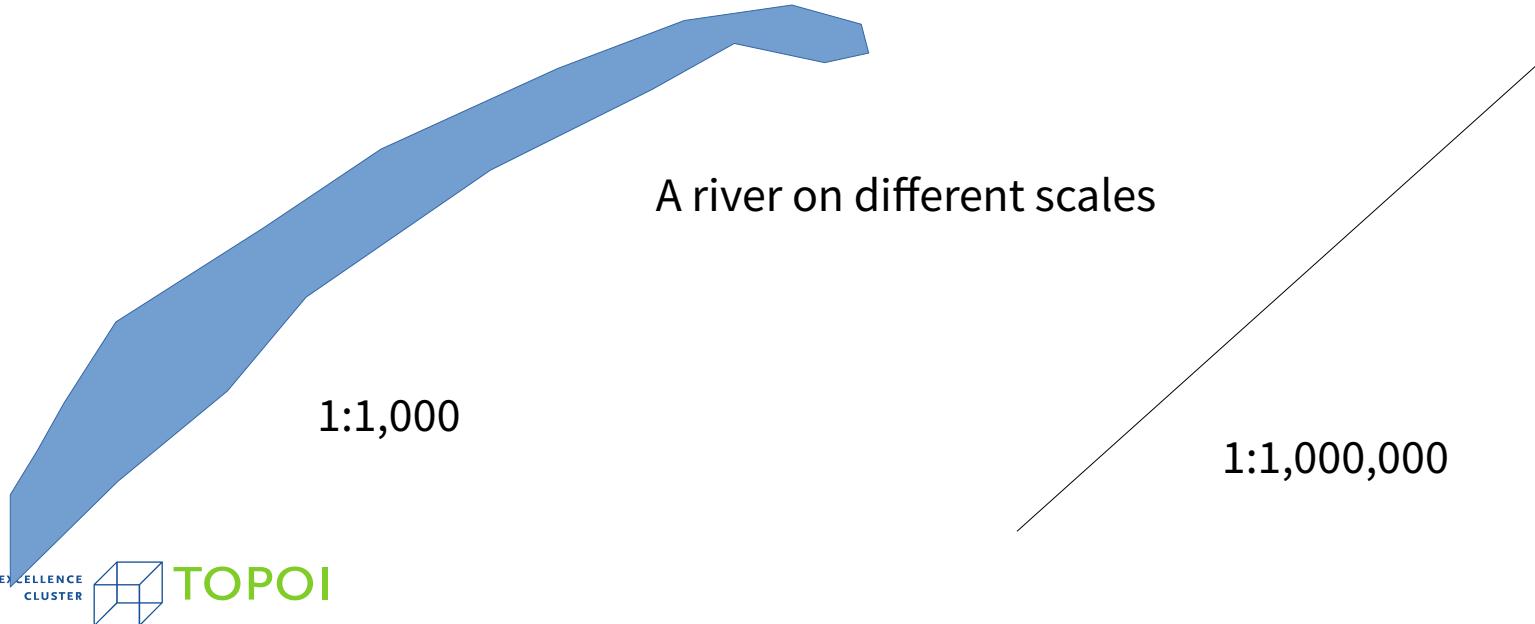
# Scale effects

- Scale affects results and representativity of data
- e.g. cities may be represented as points or polygons
- results depend on the scale of analysis, e.g. province or county → MAUP



# Scale effects

- Scale affects results and representativity of data
- e.g. cities may be represented as points or polygons
- results depend on the scale of analysis, e.g. province or county → MAUP



# Ecological fallacy

Arises when:

correlation IS NOT causation

- Statistical relationship at one level of aggregation...
- ...is assumed to hold true because it holds at a more detailed level

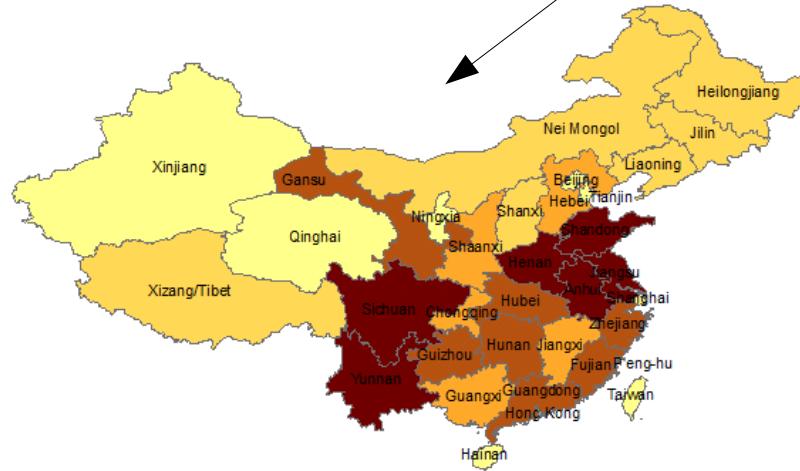
For example, we might observe a strong relationship between income and crime at the county level, with lower-income counties being associated with higher crime rates. If from this we conclude that lower-income individuals are more likely to commit a crime, then we are falling for the ecological fallacy. In fact, it is only valid to say exactly what the data say: that lower-income counties tend to experience higher crime rates. What causes the observed effect may be something entirely different

# Non-uniformity of space

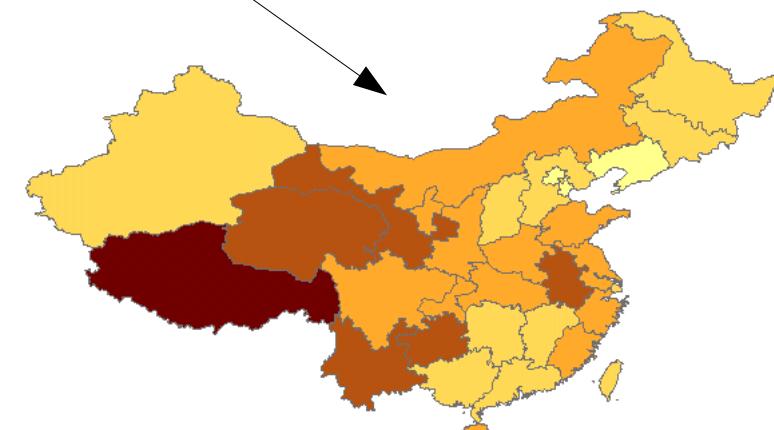
Bank robberies are clustered  
→ because banks are clustered

Diseases due to bad air are clustered  
→ because factories are clustered

Illiteracy in China  
absolute



as ratio of population



# Edge effects

- unless you study the entire world: Every study region has a boundary
- You do not have data outside your study region
- But: the “outside” data may/do affect the data of your study region (if there is spatial autocorrelation...)

# Spatial data are special

## Pitfalls of spatial data:

- spatial autocorrelation
- modifiable areal unit problem
- scale
- ecological fallacy
- non-uniformity of space
- edge effects

## Potentials of spatial data:

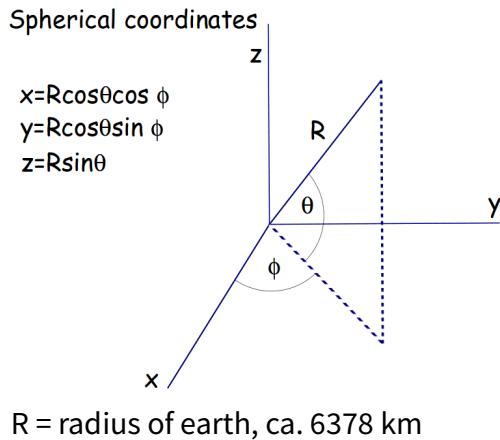
- distance
- adjacency
- interaction
- neighborhood

# Distance

$$d_{ij} = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$$

Euclidean distance as calculated using  
*Pythagoras' formula*

→ for *projected* data on the local/regional scale



Spherical distance via spherical coordinates  
and a 3D version of *Pythagoras' formula*

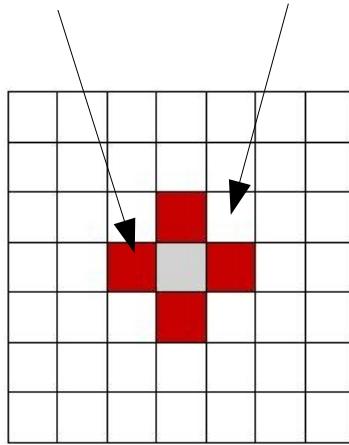
$$d^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2$$

→ for *unprojected* data on a global scale

# Distance – Adjacency – Interaction - Neighborhood

$$\mathbf{D} = \begin{bmatrix} 0 & 66 & 68 & 68 & 24 & 41 \\ 66 & 0 & 51 & 110 & 99 & 101 \\ 68 & 51 & 0 & 67 & 91 & 116 \\ 68 & 110 & 67 & 0 & 60 & 108 \\ 24 & 99 & 91 & 60 & 0 & 45 \\ 41 & 101 & 116 & 108 & 45 & 0 \end{bmatrix}$$

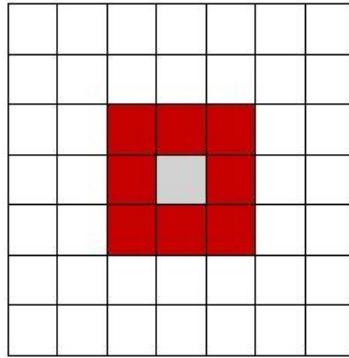
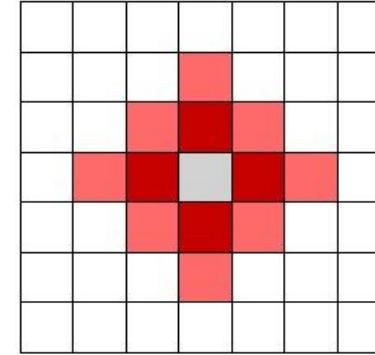
Binary  
→ things are adjacent or not



# Adjacency

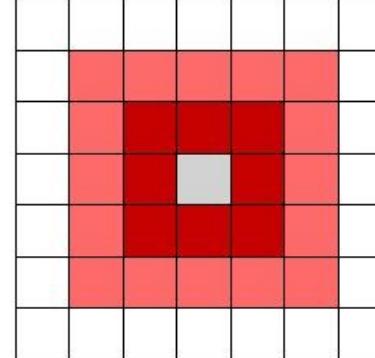
Rook case

→ sharing a boundary



Queen case  
→ sharing a boundary or point

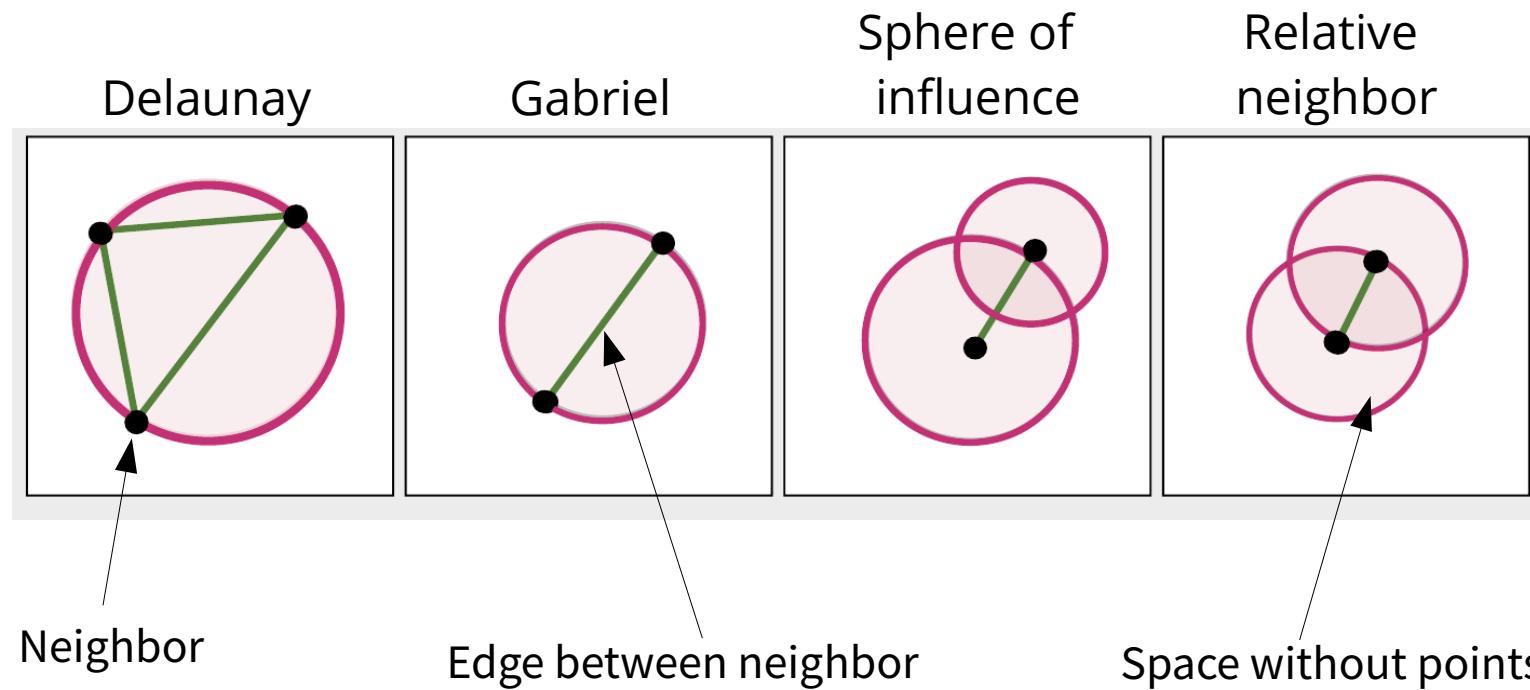
1<sup>st</sup> order neighbor



2<sup>nd</sup> order neighbor

# Adjacency

...or graph based neighbors.



# Distance – Adjacency – Interaction - Neighborhood

$$\mathbf{A}_{k=3} = \begin{bmatrix} * & 1 & 0 & 0 & 1 & 1 \\ 1 & * & 1 & 0 & 1 & 0 \\ 1 & 1 & * & 1 & 0 & 0 \\ 1 & 0 & 1 & * & 1 & 0 \\ 1 & 0 & 0 & 1 & * & 1 \\ 1 & 1 & 0 & 0 & 1 & * \end{bmatrix}$$

$$\mathbf{A}_{d \leq 50} = \begin{bmatrix} * & 0 & 0 & 0 & 1 & 1 \\ 0 & * & 0 & 0 & 0 & 0 \\ 0 & 0 & * & 0 & 0 & 0 \\ 0 & 0 & 0 & * & 0 & 0 \\ 1 & 0 & 0 & 0 & * & 1 \\ 1 & 0 & 0 & 0 & 1 & * \end{bmatrix}$$

# Interaction

- A combination of distance and adjacency
- related to Tobler's first law of geography:

*“(...) everything is related to everything else, but near things are more related than distant things”* (Tobler 1970, 236)

interaction weight between  $i$  and  $j$

rate of decline

distance between  $i$  and  $j$

$$w_{ij} \propto \frac{1}{d^k}$$

...strength of interaction between  $i$  and  $j$  is proportional to their inverse distance

# Distance – Adjacency – Interaction - Neighborhood

row totals:

$$\mathbf{W} = \begin{bmatrix} \infty & 0.0152 & 0.0147 & 0.0147 & 0.0417 & 0.0244 \\ 0.0152 & \infty & 0.0196 & 0.0091 & 0.0101 & 0.0099 \\ 0.0147 & 0.0196 & \infty & 0.0149 & 0.0110 & 0.0086 \\ 0.0147 & 0.0091 & 0.0149 & \infty & 0.0167 & 0.0093 \\ 0.0417 & 0.0101 & 0.0110 & 0.0167 & \infty & 0.0222 \\ 0.0244 & 0.0099 & 0.0086 & 0.0093 & 0.0222 & \infty \end{bmatrix} \begin{bmatrix} 0.1106 \\ 0.0639 \\ 0.0688 \\ 0.0646 \\ 0.1016 \\ 0.0744 \end{bmatrix}$$

$\mathbf{W}[1,2] = \mathbf{W}[1,] / \text{sum}(\mathbf{W}[1,])$

...

$$\mathbf{W} = \begin{bmatrix} \infty & 0.1370 & 0.1329 & 0.1329 & 0.3767 & 0.2205 \\ 0.2373 & \infty & 0.3071 & 0.1424 & 0.1582 & 0.1551 \\ 0.2136 & 0.2848 & \infty & 0.2168 & 0.1596 & 0.1252 \\ 0.2275 & 0.1406 & 0.2309 & \infty & 0.2578 & 0.1432 \\ 0.4099 & 0.0994 & 0.1081 & 0.1640 & \infty & 0.2186 \\ 0.3279 & 0.1331 & 0.1159 & 0.1245 & 0.2987 & \infty \end{bmatrix}$$

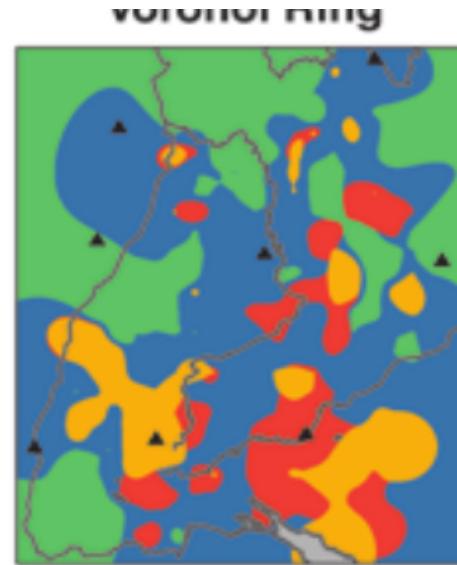
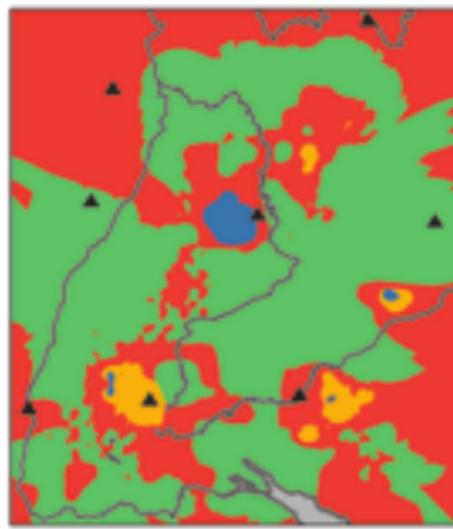
column totals:

1.4161	0.7949	0.8949	0.7805	1.2510	0.8626
--------	--------	--------	--------	--------	--------

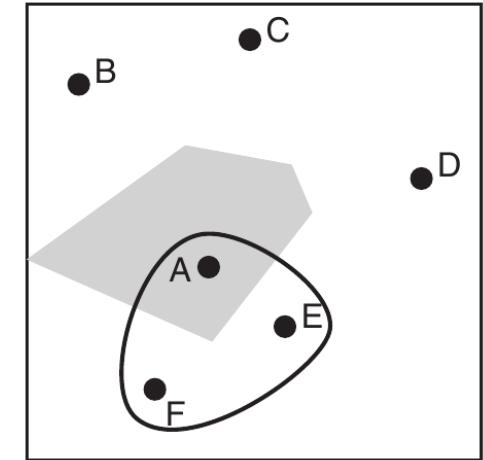
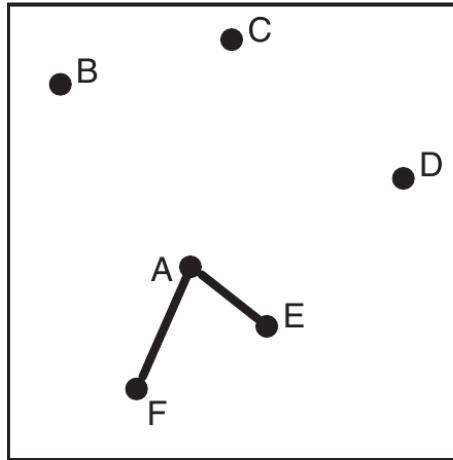
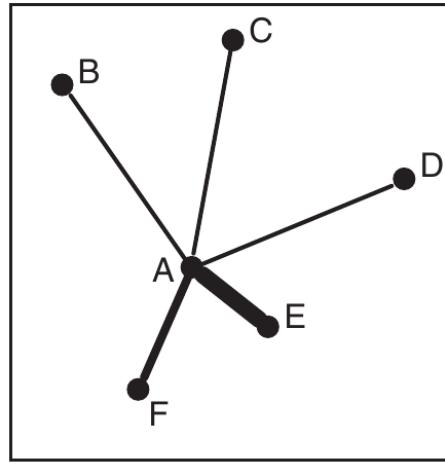
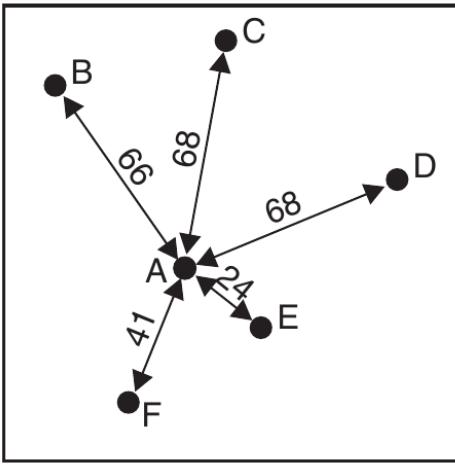
# Neighborhood

Neighborhood of X is:

- the set of adjacent cells/areas
- the set of points/cells/areas within a certain distance
- the set of points/cells/areas that share some specific attribute or that are alike



# Distance – Adjacency – Interaction - Neighborhood



# Spatial data are special

## Pitfalls of spatial data:

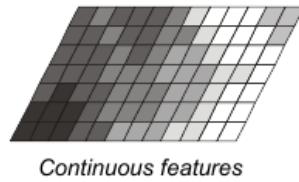
- spatial autocorrelation
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- scale
- ecological fallacy
- non-uniformity of space
- edge effects

## Potentials of spatial data:

- distance
- adjacency
- interaction
- neighborhood

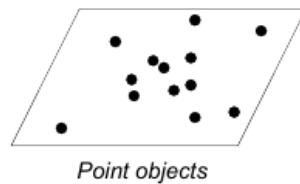
# ...it's all about processes

GEOSTATISTICS



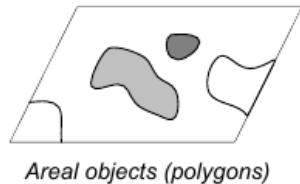
However you call it and focus on...

POINT PATTERN ANALYSIS



everything is about processes...

LATTICE STATISTICS



Because they cause spatial patterning, autocorrelation, ...

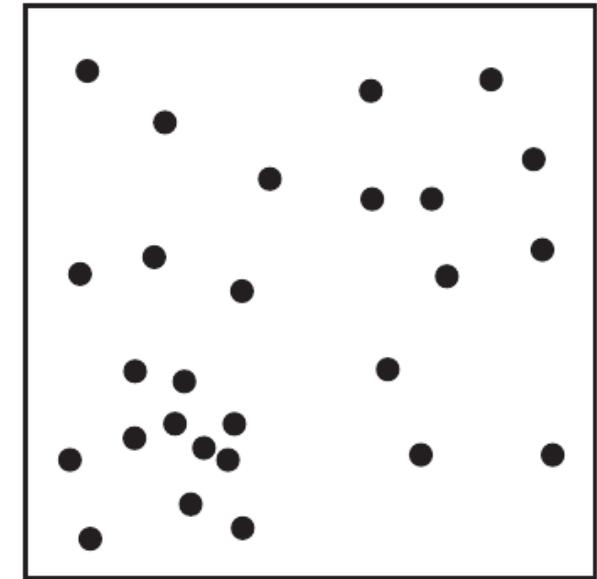
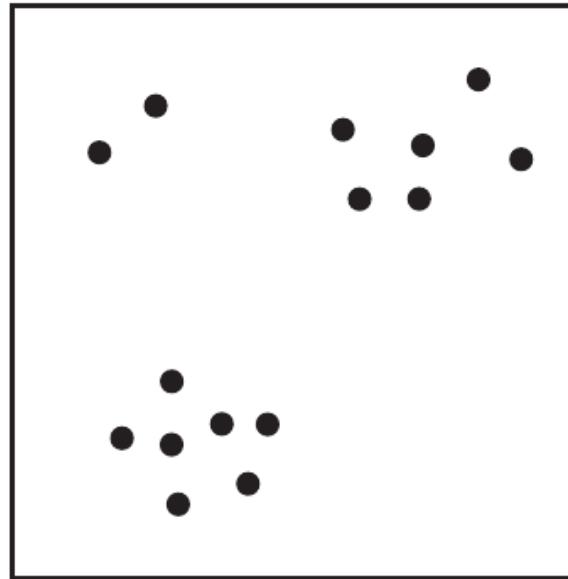
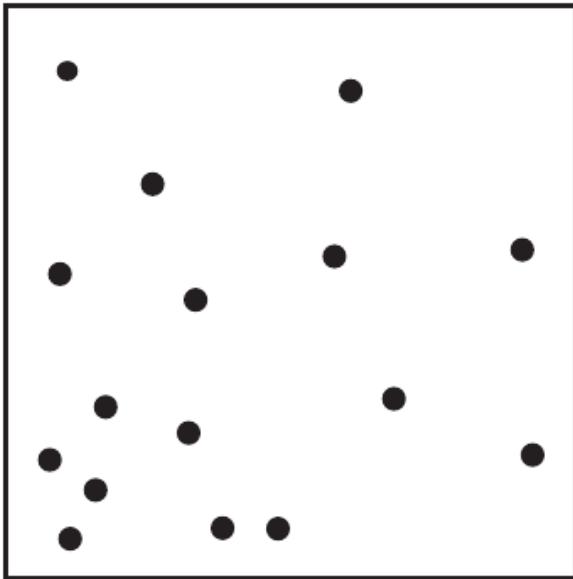
Fig. 1.2: Spatial statistics and its three major subfields after Cressie (1993).

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# Point Pattern

What caused these patterns? First- or Second order effects?

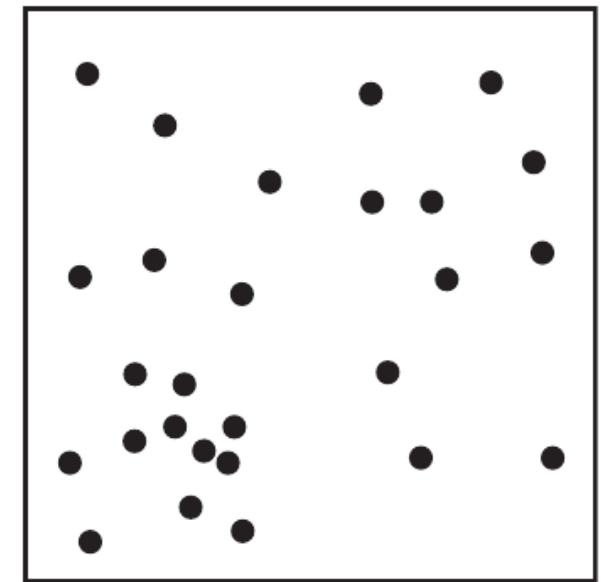
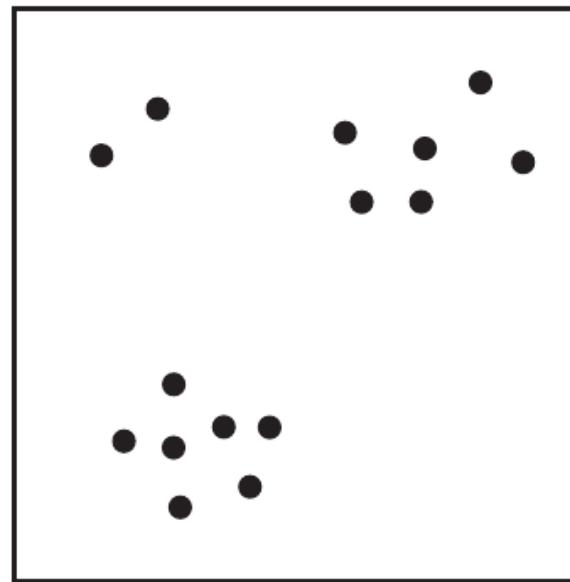
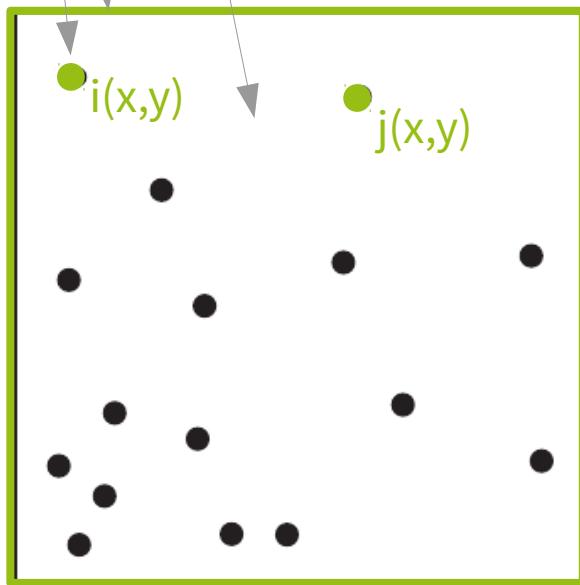


Point pattern analysis aims to distinguish between both effects  
– helping you to understand the genuine process creating the pattern –

# Point Pattern

region  
event pattern

What caused these patterns? First- or Second order effects?

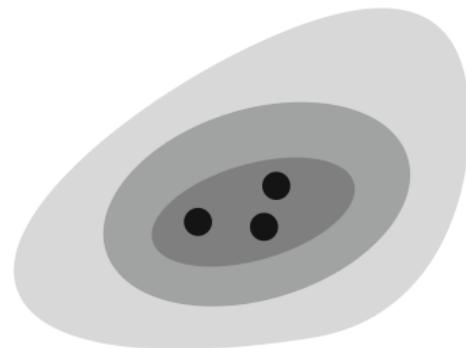


Point pattern analysis aims to distinguish between both effects  
– helping you to understand the genuine process creating the pattern –

# Point Pattern

What caused these patterns? First- or Second order effects?

e.g. mining sites  
and resources

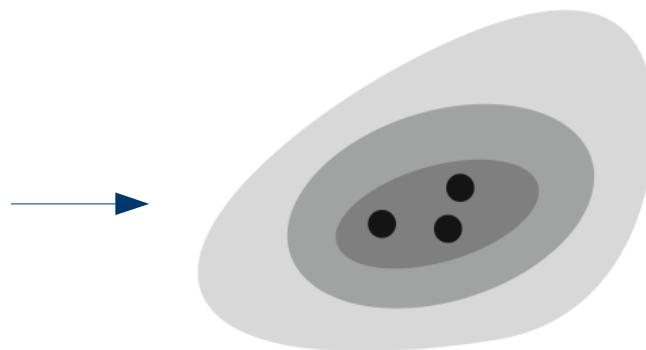


First order property:  
location depends on an  
spatial parameter

# Point Pattern

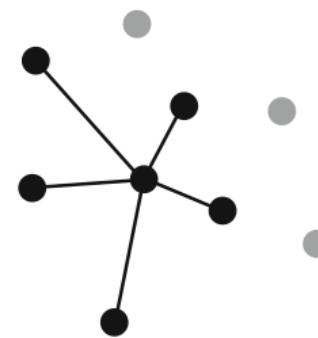
What caused these patterns? First- or Second order effects?

e.g. mining sites  
and resources



First order property:  
location depends on an  
spatial parameter

e.g. graveyard  
and settlement



Second order property:  
location depends on  
the relationship to  
other points

# Point Pattern

Simple measures:

- mean center
- standard distance
- intensity of a pattern

$$\bar{\mathbf{s}} = (\mu_x, \mu_y) = \left( \frac{\sum_{i=1}^n x_i}{n}, \frac{\sum_{i=1}^n y_i}{n} \right)$$

$$d = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu_x)^2 + (y_i - \mu_y)^2}{n}}$$

$$\hat{\lambda} = \frac{n}{a} = \frac{\#(S \in A)}{a}$$

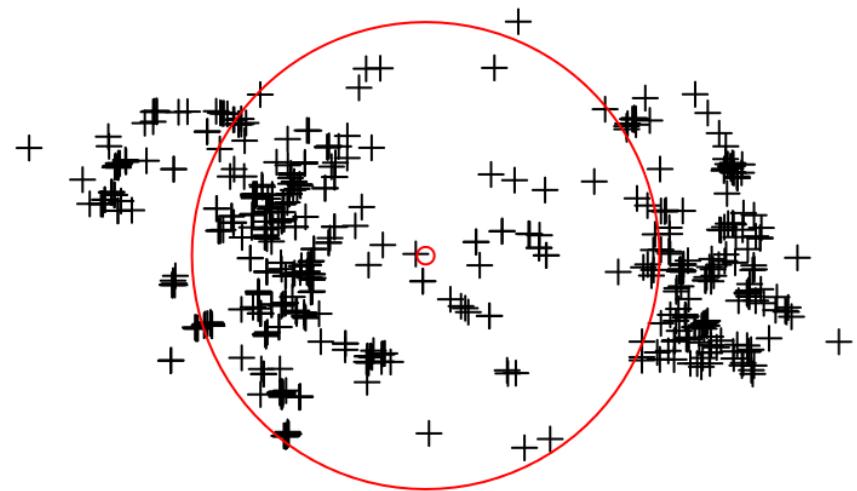
Area of study region

Number of events in the pattern found in study region

# Point Pattern

Simple measures:

- mean center
- standard distance
- intensity of a pattern



0.015 sites/sqkm

Sensitive...what is the area?

# Point Pattern – first order effects

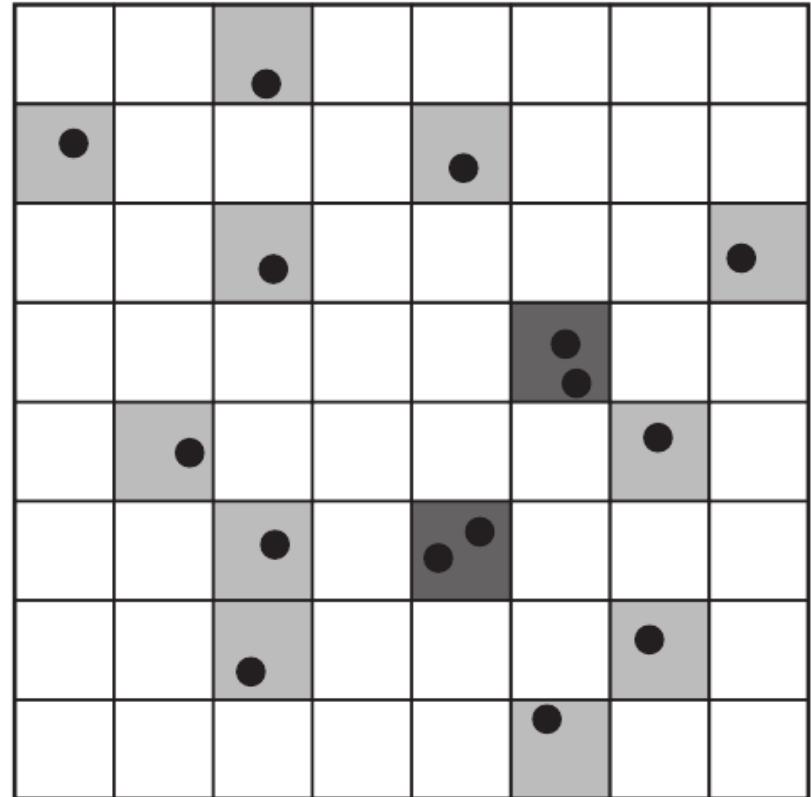
Intensity – more advanced

Independent Random Process (IRP)

= Complete Spatial Randomness (CSR)

- any event has equal probability to be located in a quadrant
- the occurrence of points is independent of the Positioning of other events

$$P(\text{event in a quadrant}) = 1/64$$



# Point Pattern – first order effects

Intensity – more advanced

Independent Random Process (IRP)

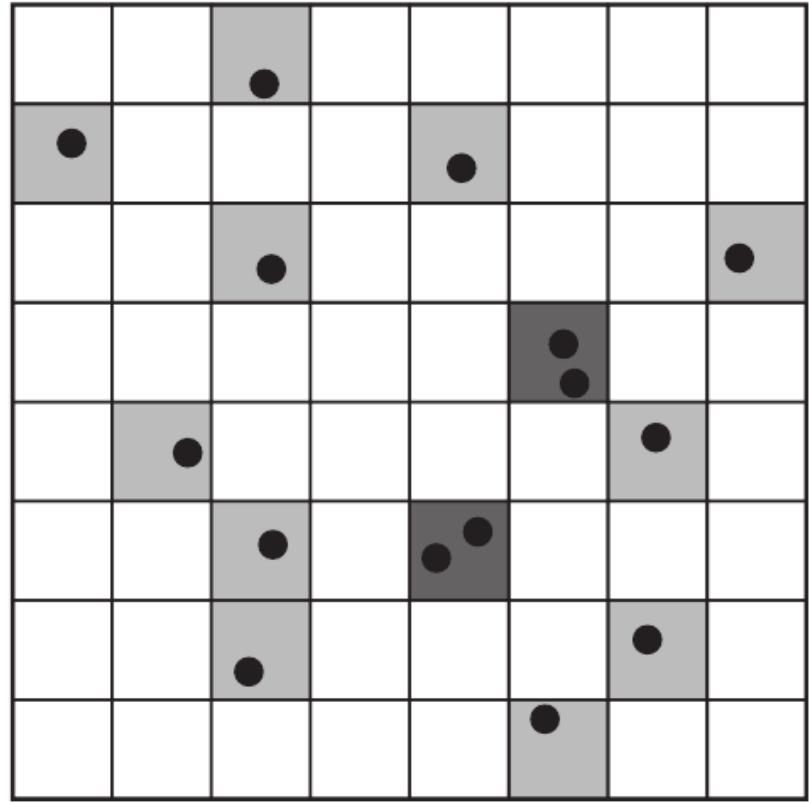
= Complete Spatial Randomness (CSR)

Probability of  $k$  events in a quadrant is calculated with  
Poisson distribution

$$P(k) = \frac{\lambda^k e^{-\lambda}}{k!}$$

intensity

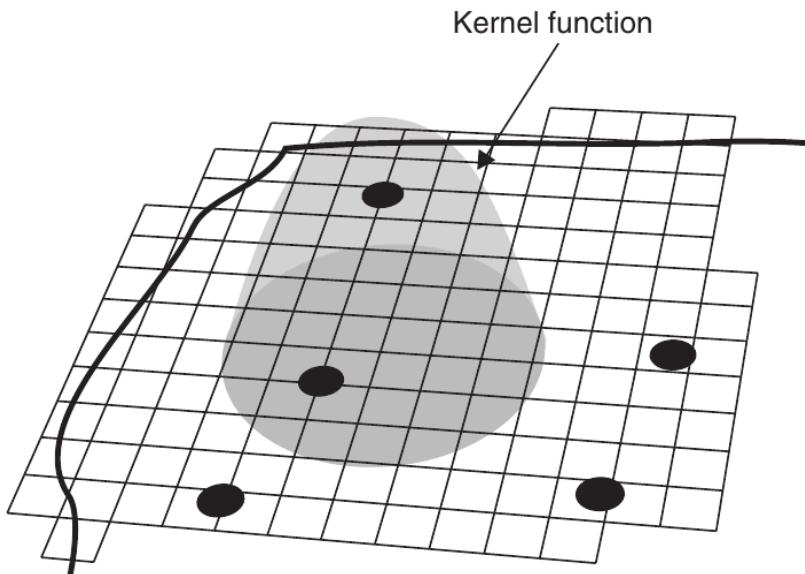
Base of natural logarithm (2.78...)



# Point Pattern – first order effects

Intensity – more advanced

Kernel density estimation (KDE)



Edge correction

$$\hat{\lambda}_p = e(p) \sum_i k(x_i - p)$$

(Gaussian) Kernel function

$$\frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

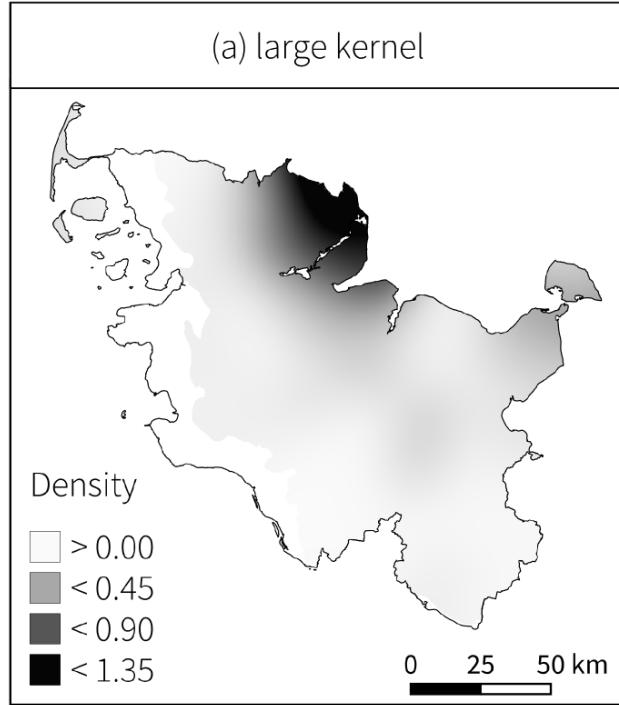
Standard deviation

kernel location

# Point Pattern – first order effects

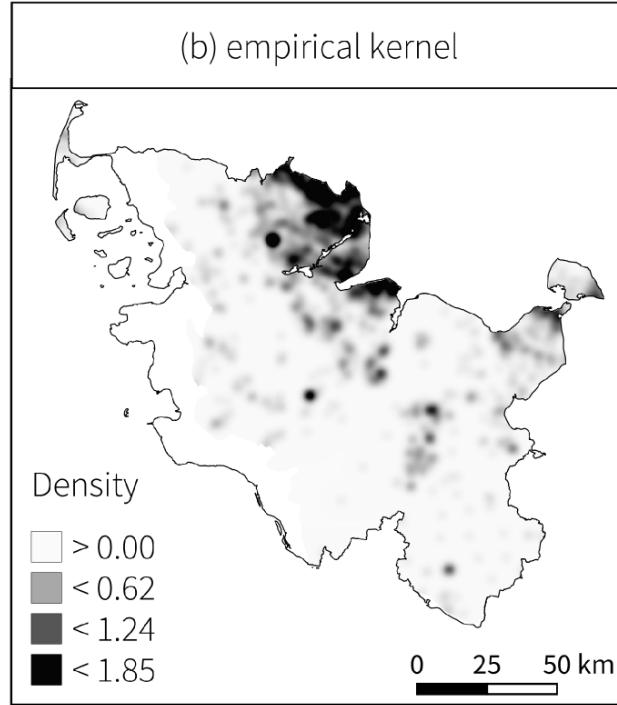
Sigma large

(a) large kernel



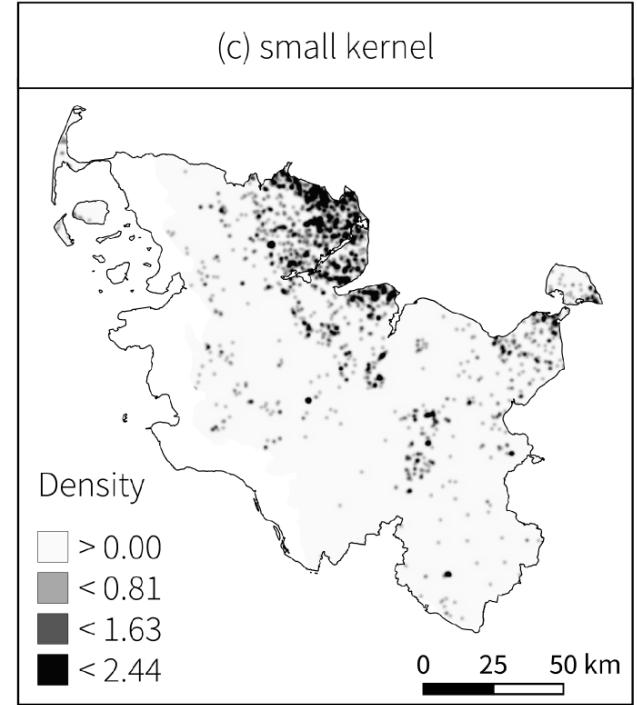
General trend

(b) empirical kernel



Sigma small

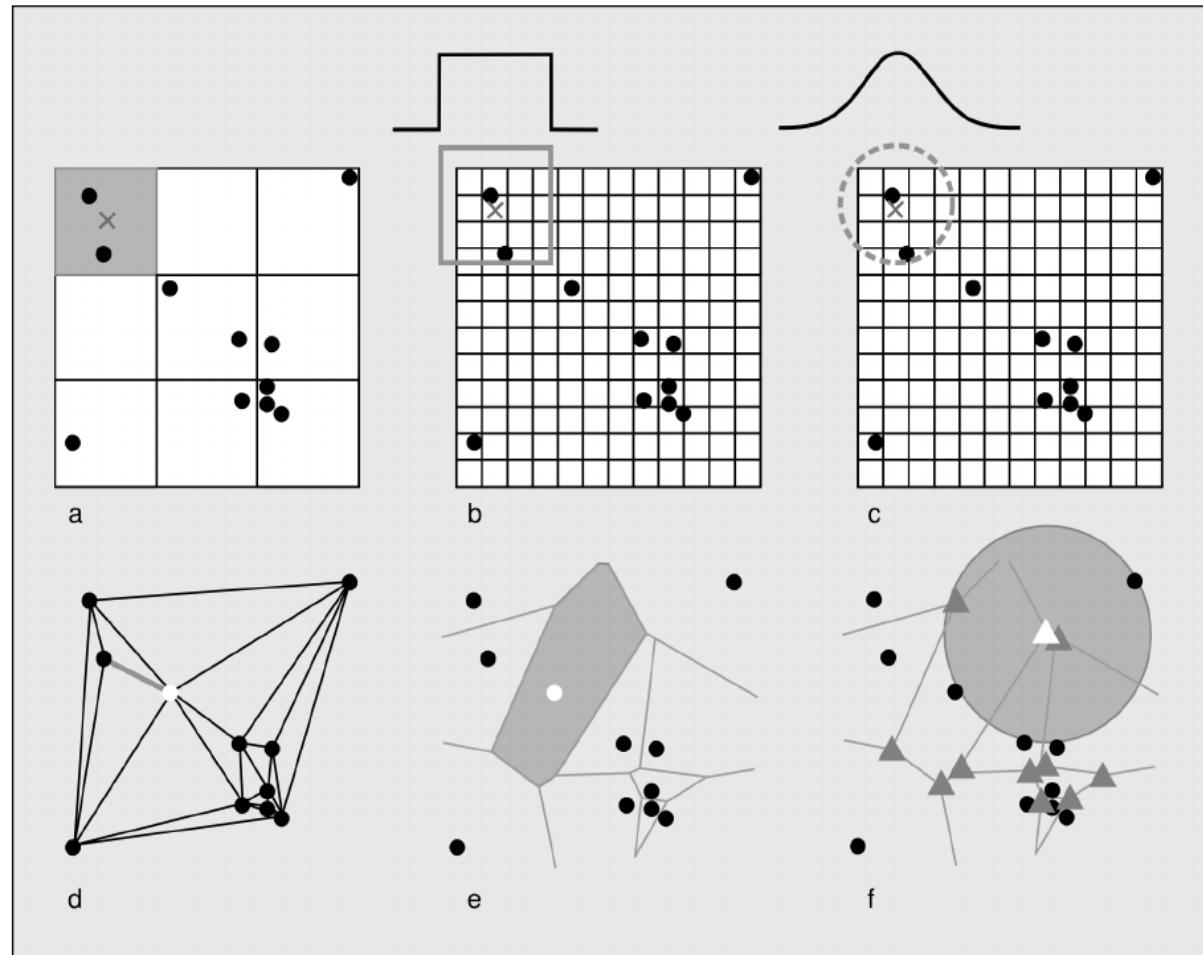
(c) small kernel



Local trend

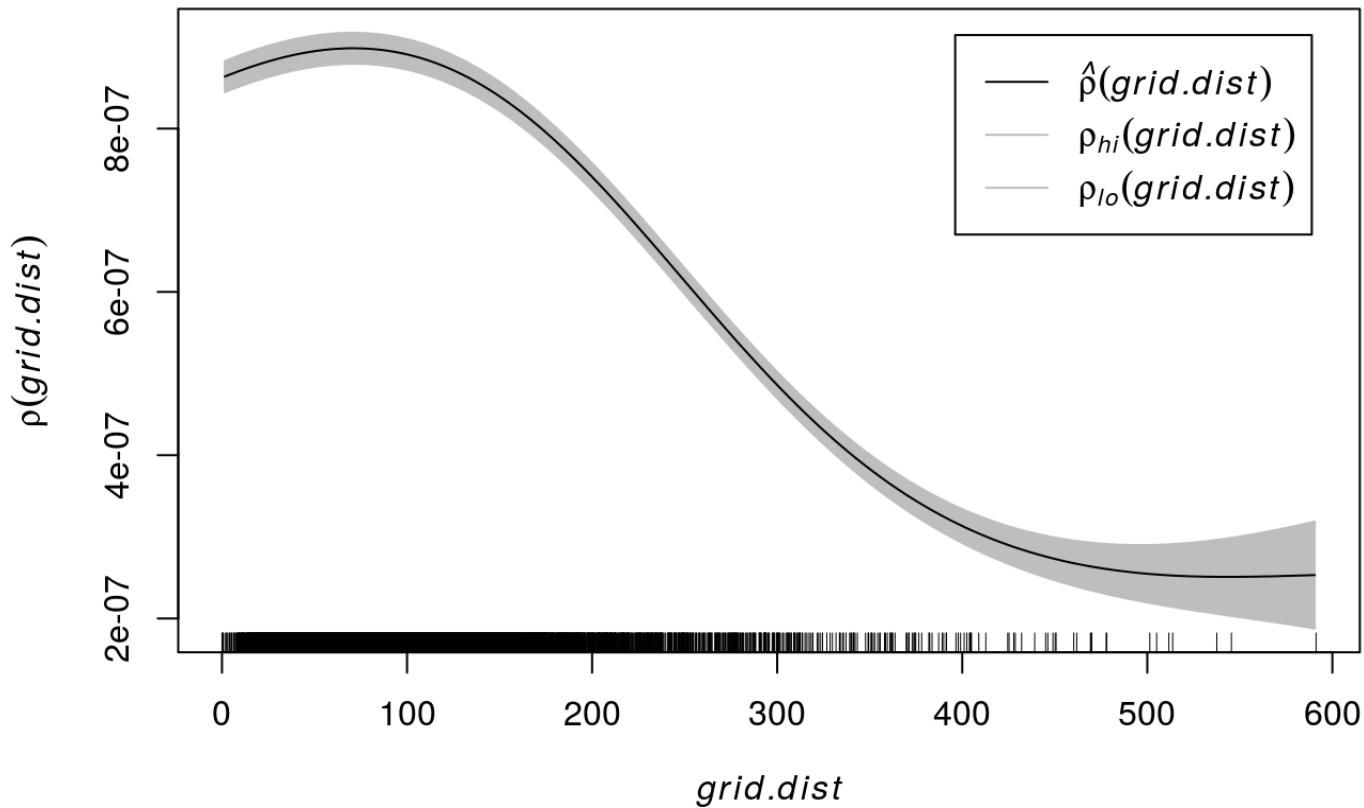
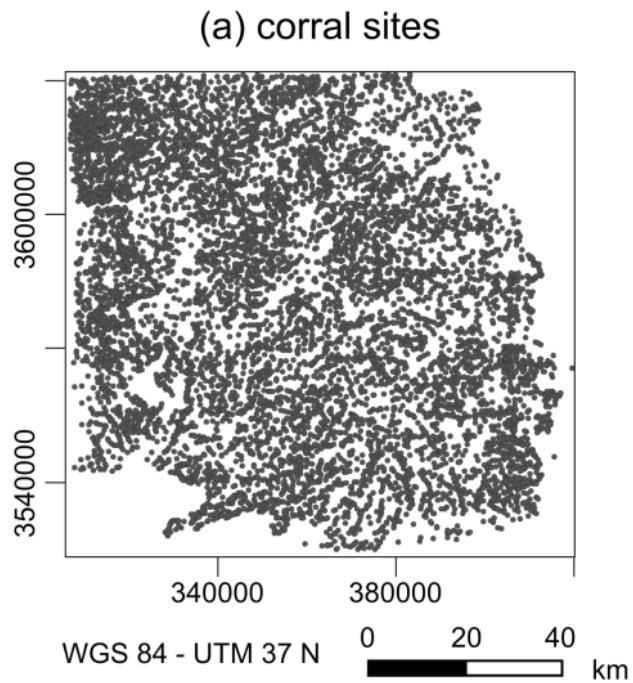
# Point Pattern – first order effects

Intensity – possibilities to calculate



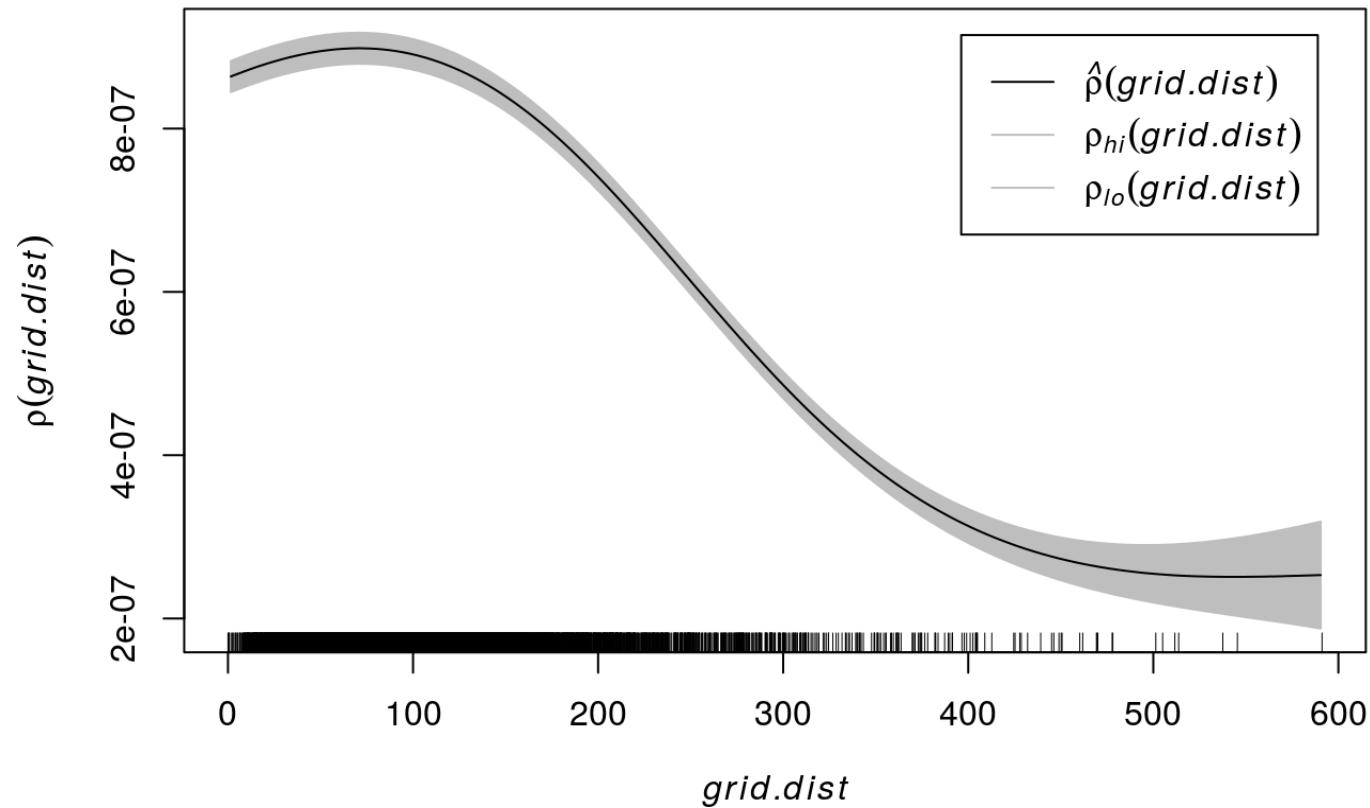
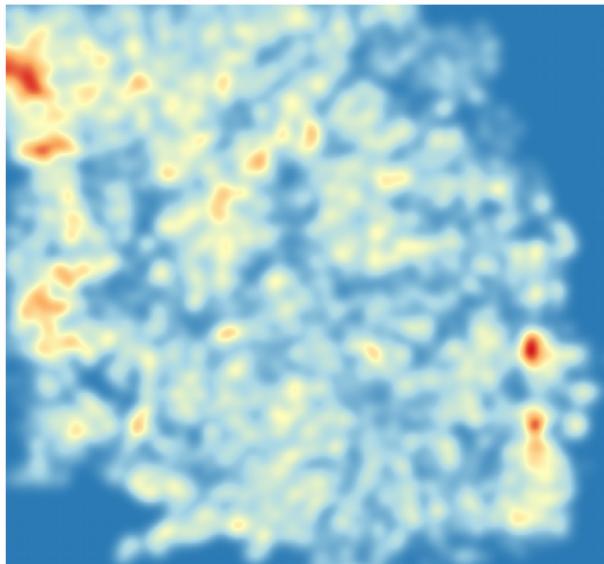
# Point Pattern – first order effects

Intensity as tool to investigate dependence on covariates



# Point Pattern – first order effects

Intensity as tool to investigate dependence on covariates



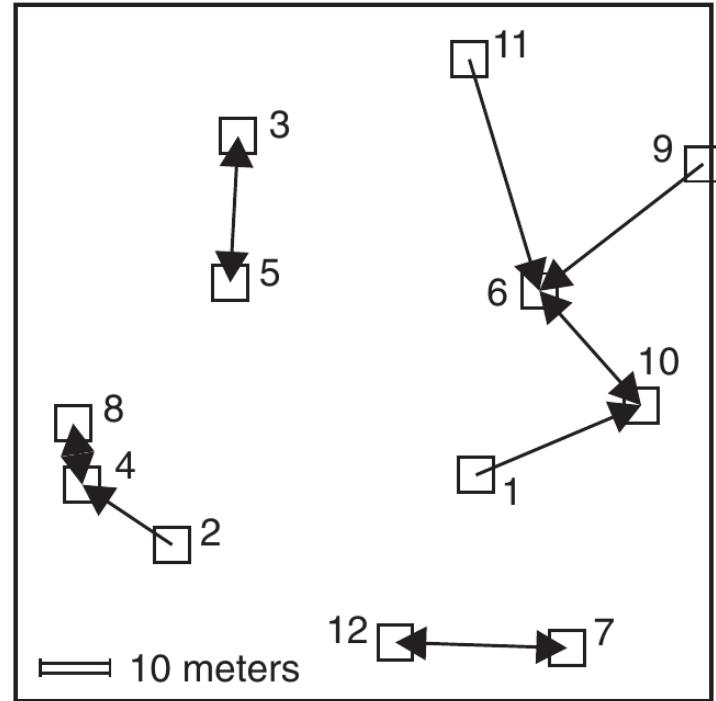
# Point Pattern – second order effects

# Point Pattern – second order effects

Point patterns described by distance measures

- nearest-neighbor distance → euclidean distance

mean nearest-neighbor distance



$$\bar{d}_{\min} = \frac{\sum_{i=1}^n d_{\min}(\mathbf{s}_i)}{n}$$

Are the points clustered or dispersed?  
Use Clark and Evan's  $R$  statistic of nearest neighbor distances

$$R = \bar{d}_{\min} \Big/ \frac{1}{(2\sqrt{\lambda})}$$

expected  
nearest-neighbor  
distance

$R < 1$ : more clustered  
 $R > 1$ : more evenly spaced

(O'Sullivan & Unwin, 2010)

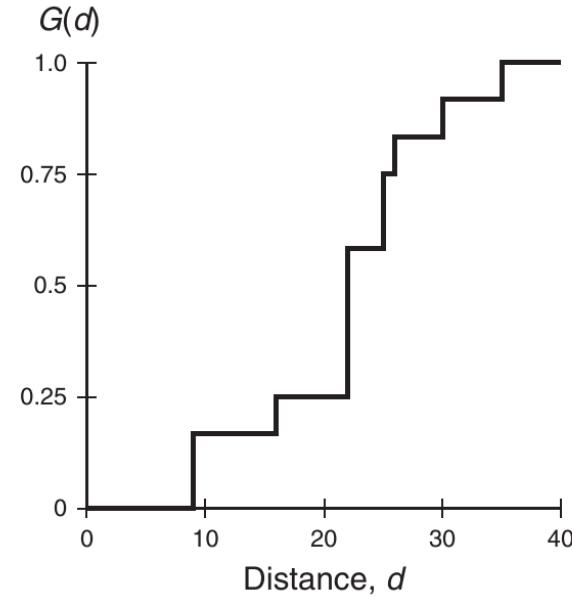
# Point Pattern – second order effects

Point patterns described by distance measures

→ cumulative frequency distribution of the nearest-neighbor distances =  $G(d)$

$$G(d) = \frac{\#(d_{\min}(\mathbf{s}_i) < d)}{n}$$

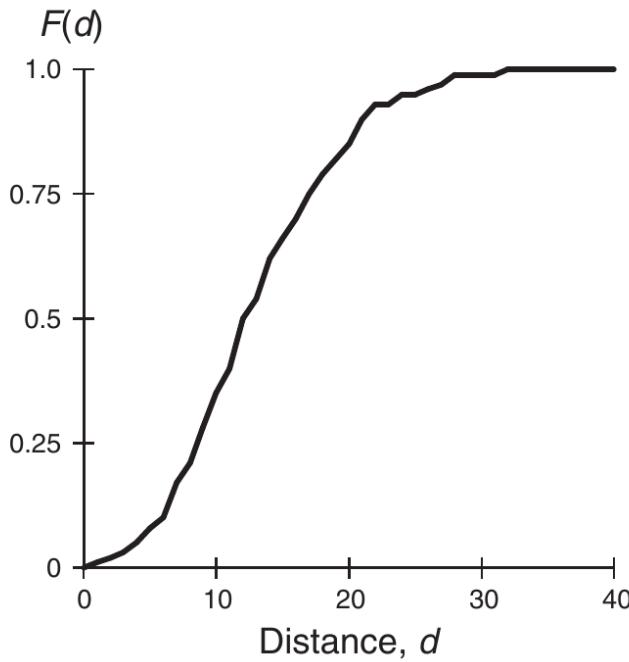
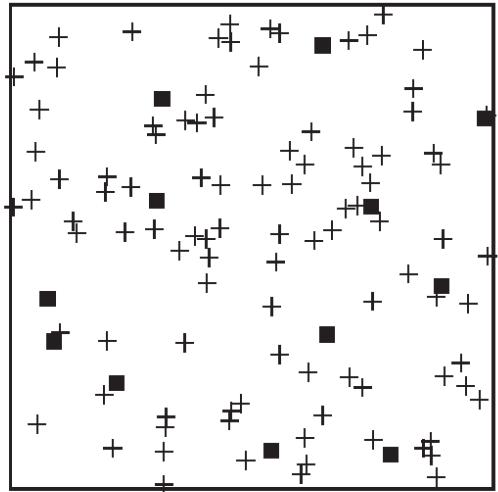
→  $G(d)$  tells us what fraction of all n-n distances is less than  $d$



# Point Pattern – second order effects

Point patterns described by distance measures

→ cumulative frequency distribution of the nearest-neighbor distances of *arbitrary events* to known events =  $F(d)$



minimum distance from  
random point  $\mathbf{p}_i$  to an event

$$F(d) = \frac{\#\{d_{\min}(\mathbf{p}_i, S) < d\}}{m}$$

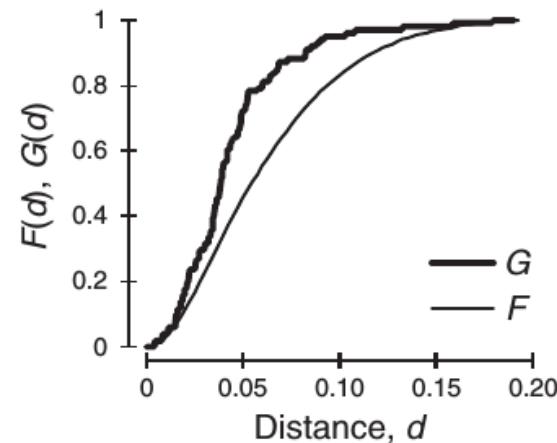
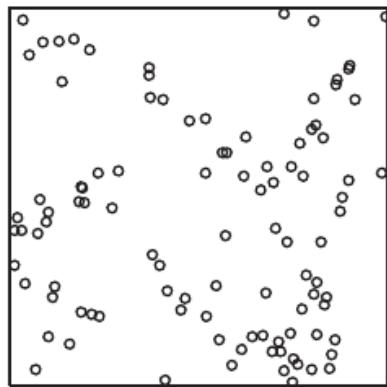
$m$

set of randomly  
selected locations

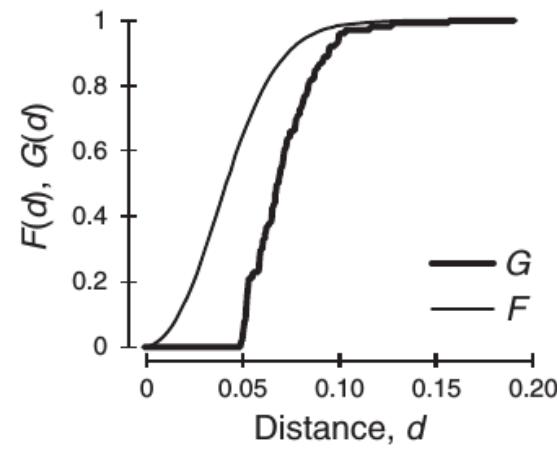
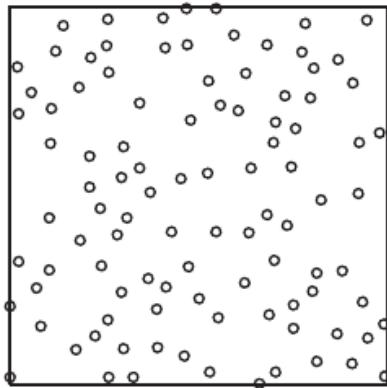
(O'Sullivan & Unwin, 2010)

# Point Pattern – second order effects

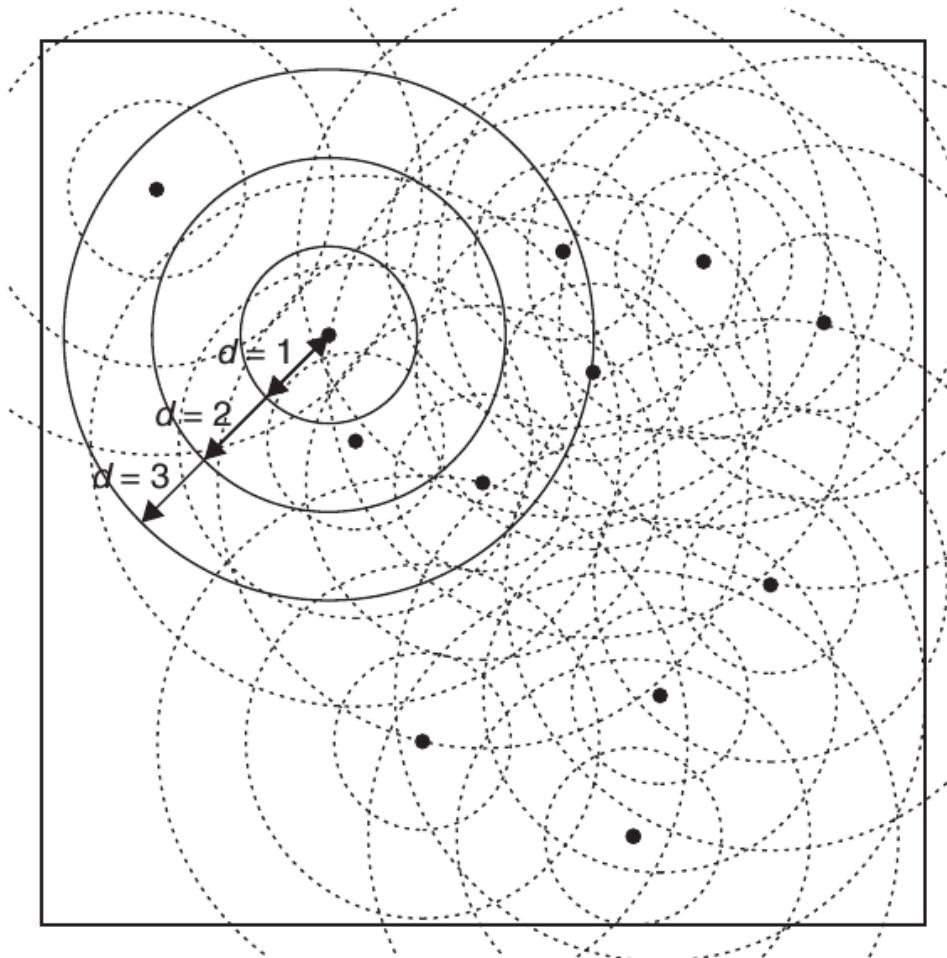
Clustered



Evenly spaced



# Point Pattern – second order effects



To get rid of the nearest-neighbor limitation:  
use the K Function

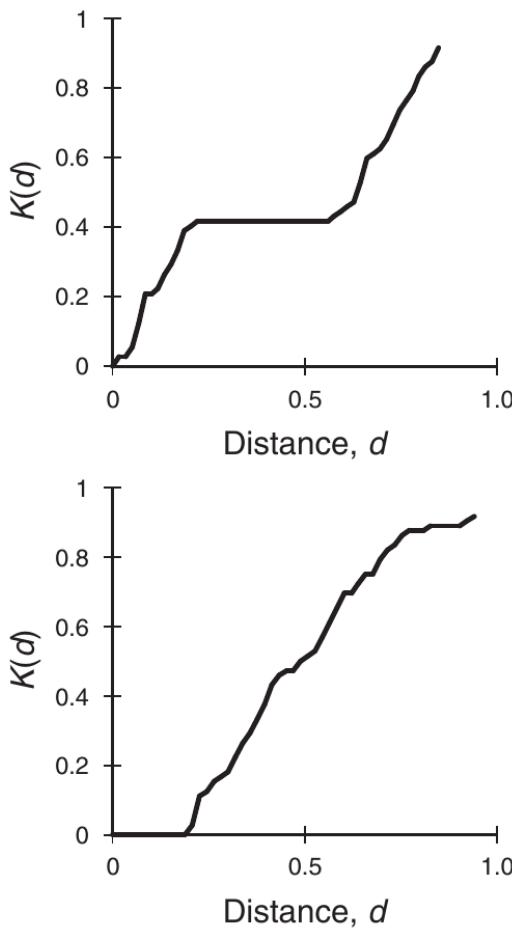
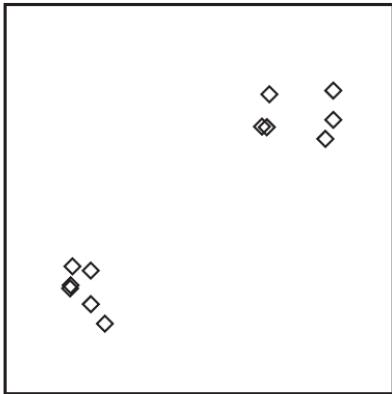
Events in circle radius  $d$  centered at  $s$

$$K(d) = \frac{\sum_{i=1}^n \# [S \in C(\mathbf{s}_i, d)]}{n\lambda}$$

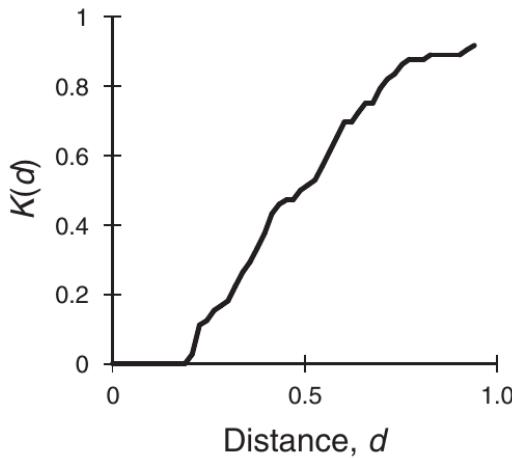
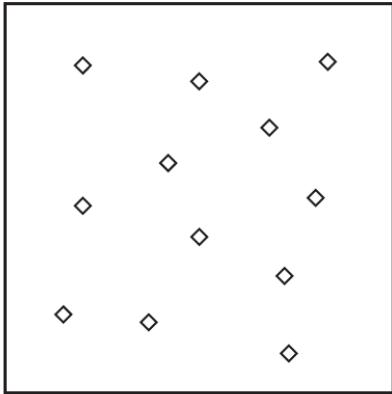
Event density in the study area/region

# Point Pattern – second order effects

Clustered



Evenly spaced



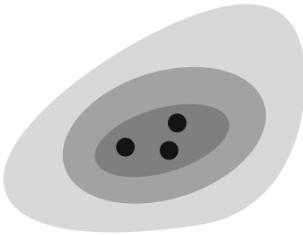
To get rid of the nearest-neighbor limitation:  
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Events in circle radius  $d$  centered at  $s$

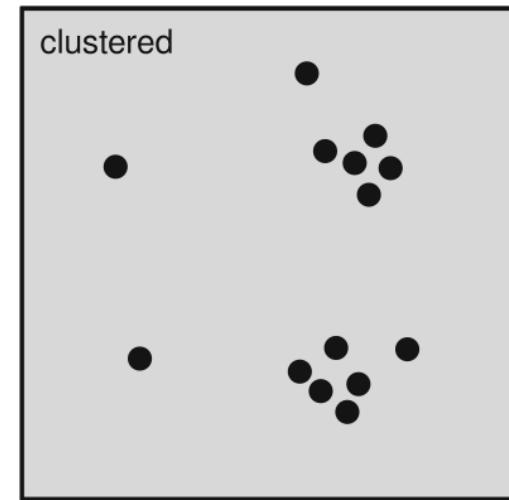
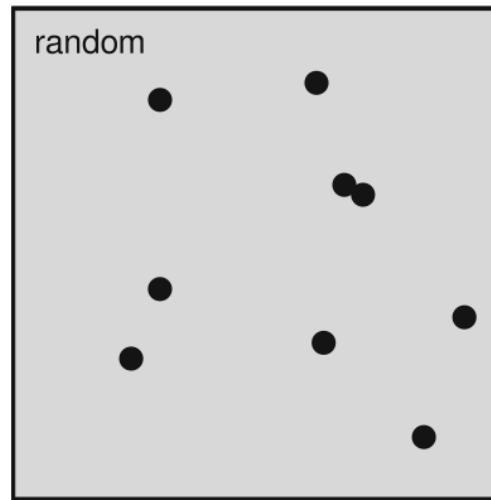
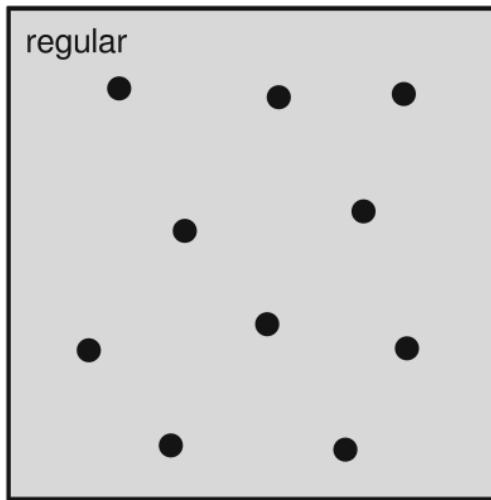
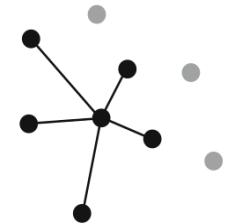
$$K(d) = \frac{\sum_{i=1}^n \# [S \in C(\mathbf{s}_i, d)]}{n\lambda}$$

Event density in the study area/region

# Point Pattern Analyses



Help to distinguish between first and second order effects that caused your spatial pattern at hand  
→ you gain insights in the underlying processes



# Content

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- Outlook

# Interpolation

We start with points

But wait...

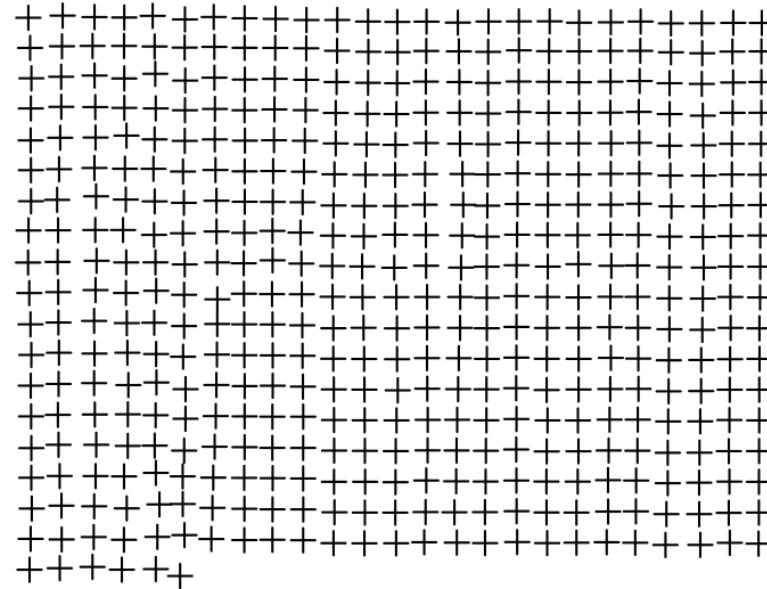
Why are the methods of point patterns not used??

Because *point data* is not necessarily a *point pattern*

e.g. sampling locations of soil samples to analyze phosphorous (=points) are *artificial* and irrelevant to the study of phosphorous distribution  
→ such points do *not* reflect a process.

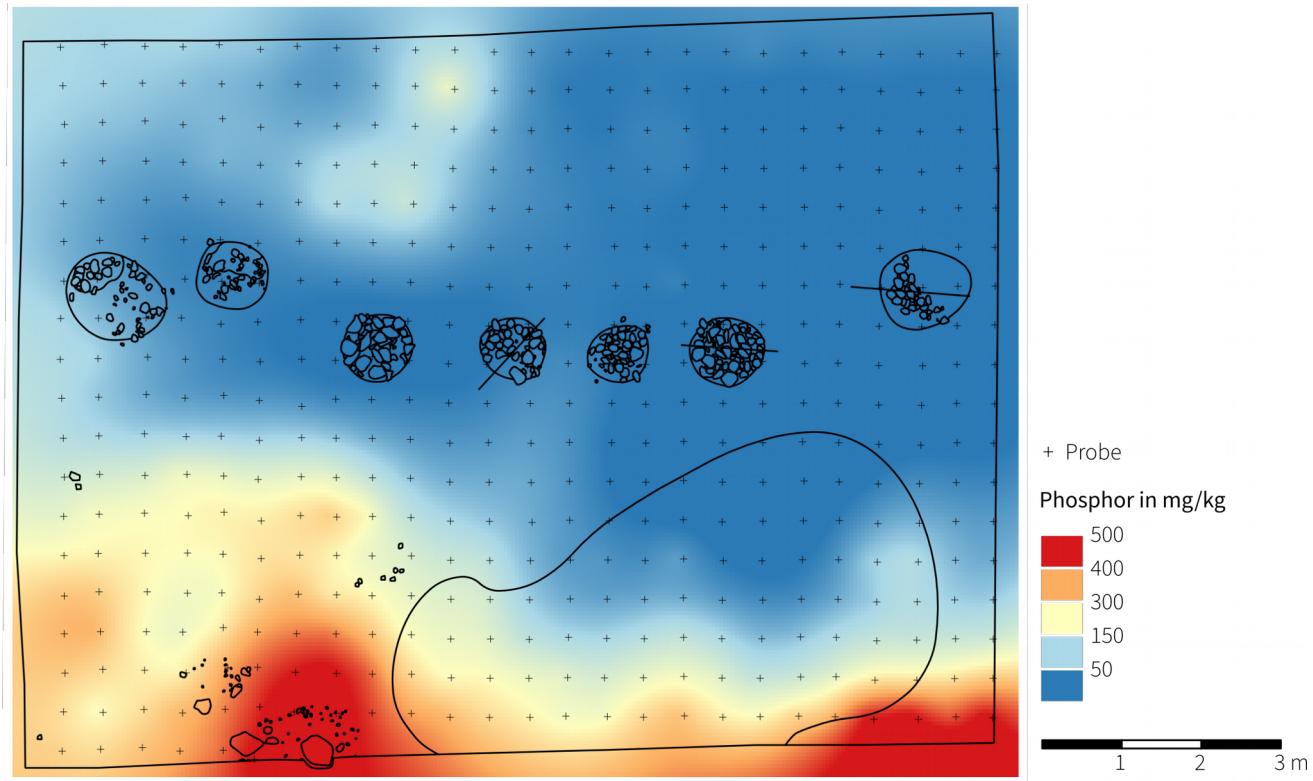
# Interpolation

Aim: get a continuous representation of attribute information.



# Interpolation

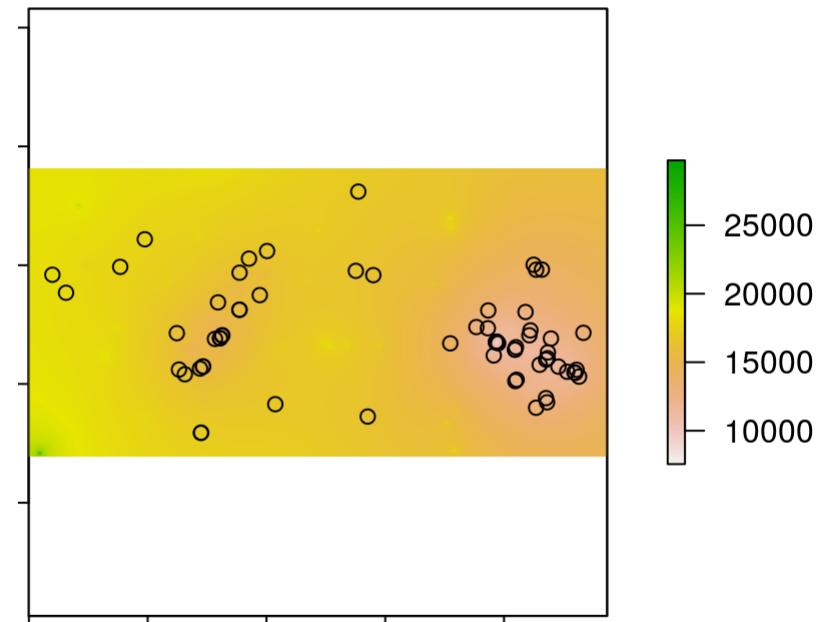
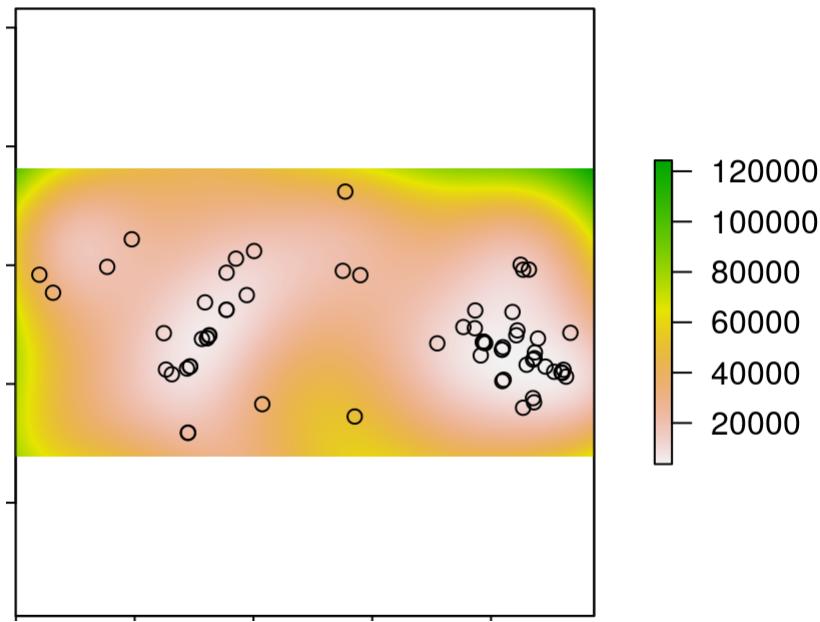
Aim: get a continuous representation of attribute information.



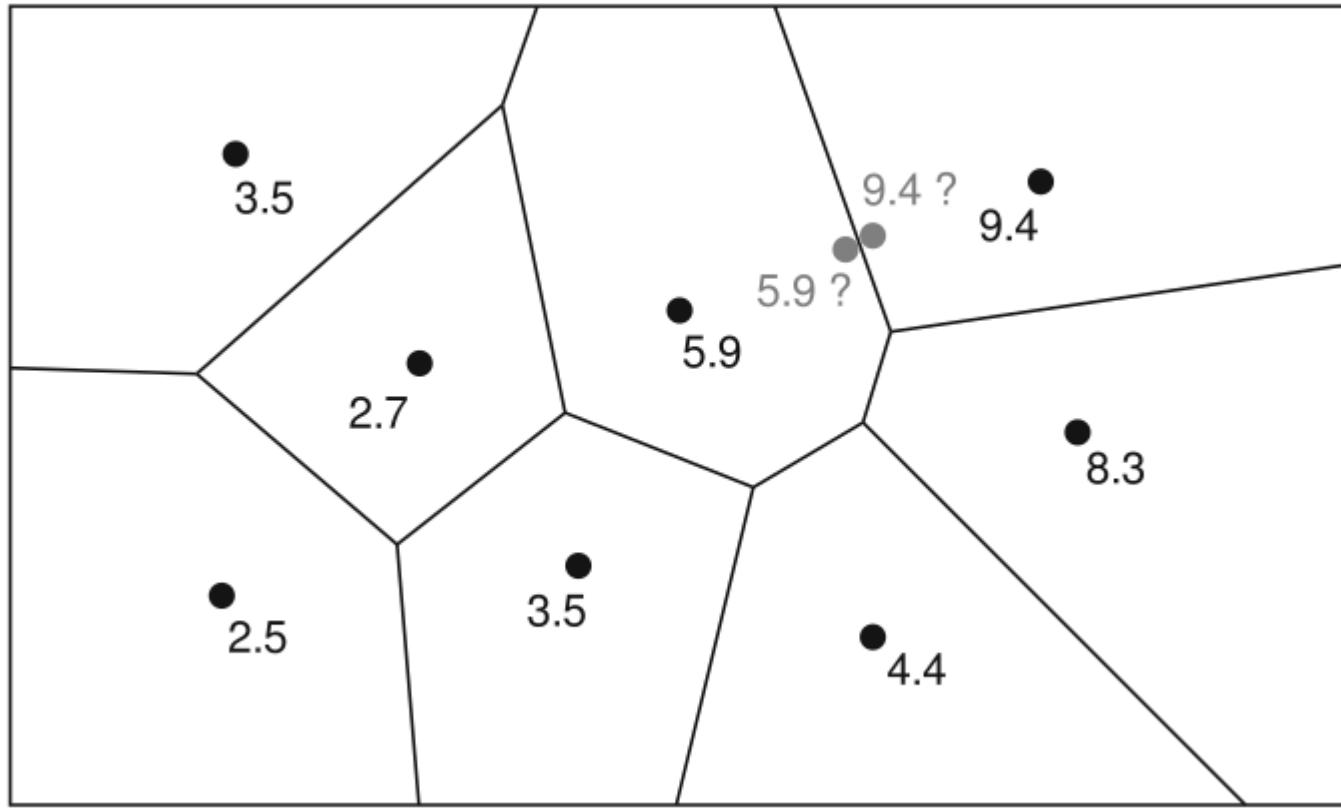
# Interpolation

Aim: get a continuous representation of settlement density.

Mission accomplished...!?



# Interpolation



# Interpolation

Inverse Distance Weighting

$$\hat{z}_j = \sum_{i=1}^m w_{ij} z_i$$

Control points  $i$  in neighborhood  $m$

Estimate at  $j$

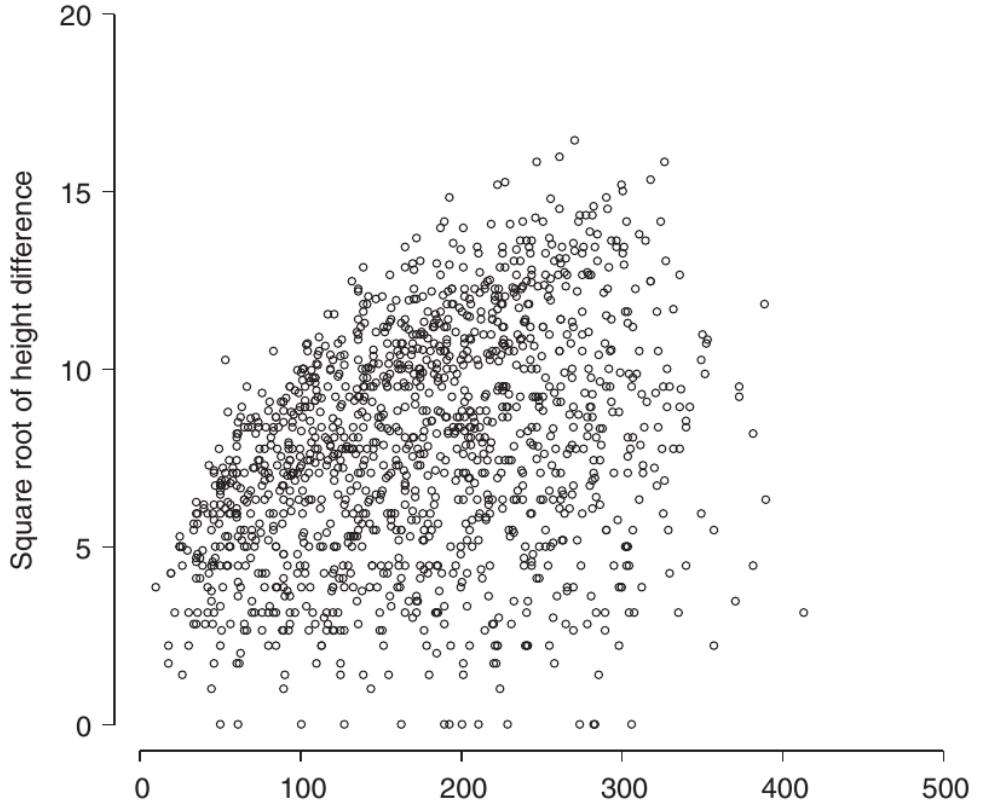
$$w_{ij} \propto \frac{1}{d_{ij}^k}$$

Kriging

# Interpolation

Square root differences cloud

1. Describing spatial variation



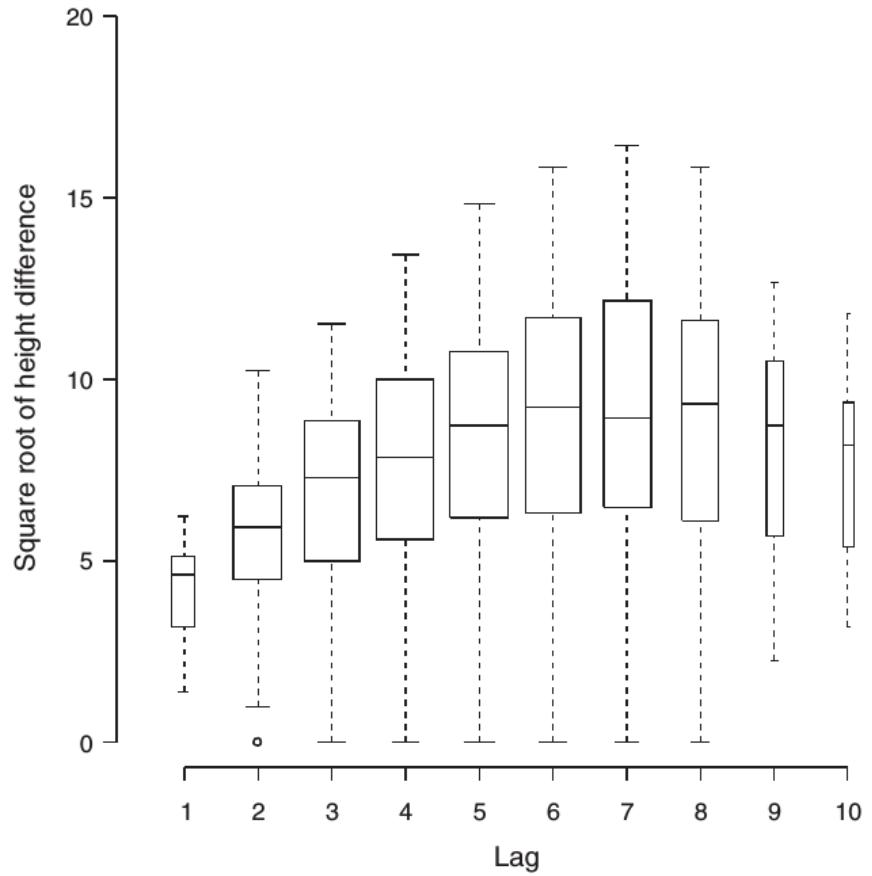
Kriging

# Interpolation

Square root differences cloud

Distance classes → lags  
and summary statistics

1. Describing spatial variation

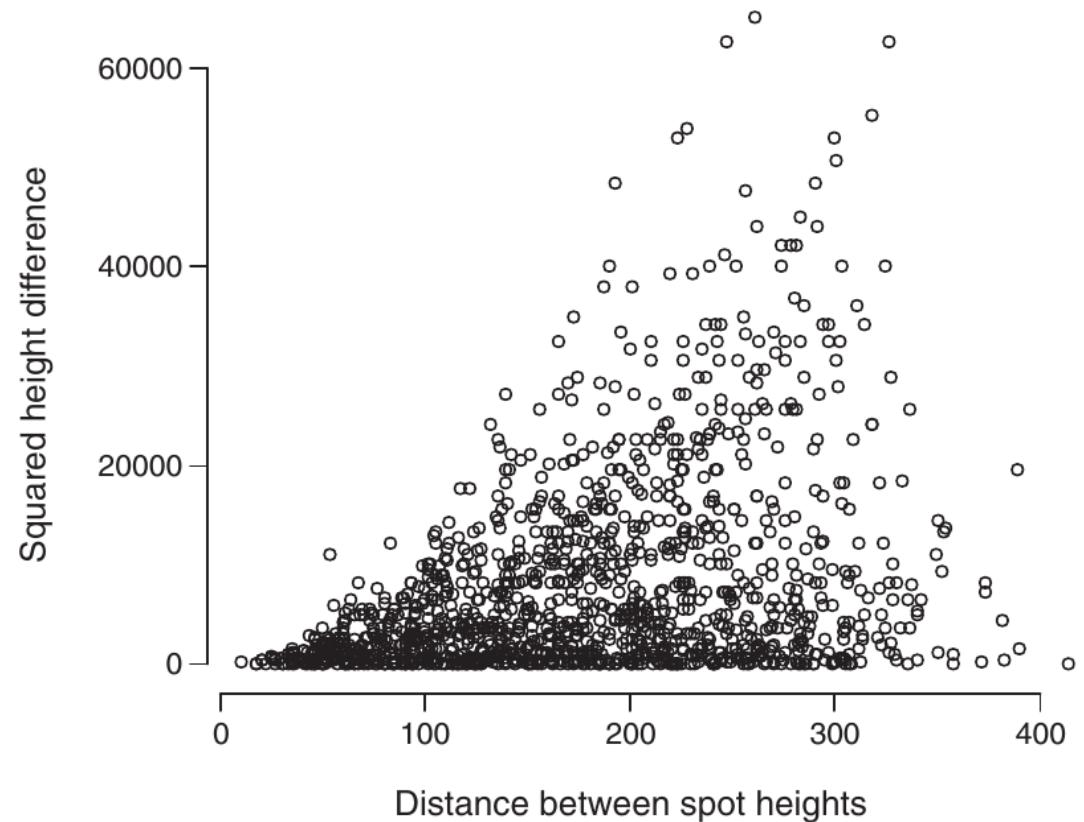


Kriging

# Interpolation

Square differences, i.e. semivariogram cloud

1. Describing spatial variation



## Kriging

# Interpolation

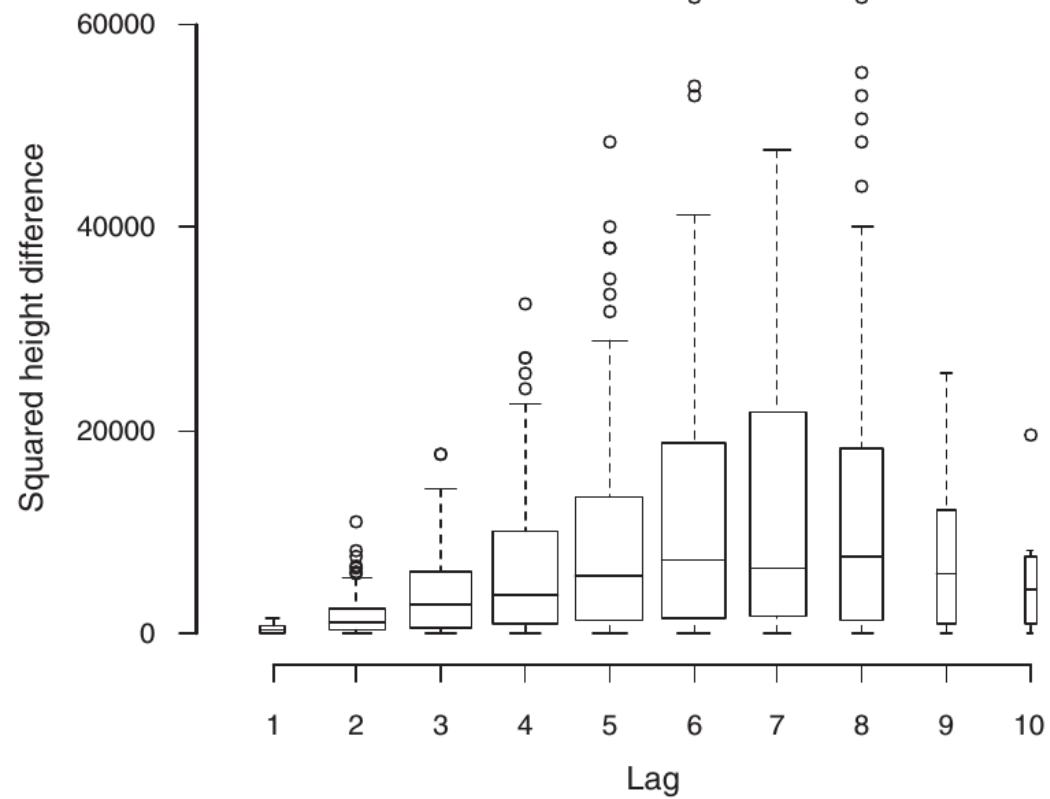
Square differences, i.e. semivariogram cloud

Distance classes → lags  
and summary statistics  
→ *experimental semivariogram*  
[or short variogram]

Semivariance

$$2\hat{\gamma}(d) = \frac{1}{n(d)} \sum_{d_{ij}=d} (z_i - z_j)^2$$

1. Describing spatial variation



## Kriging

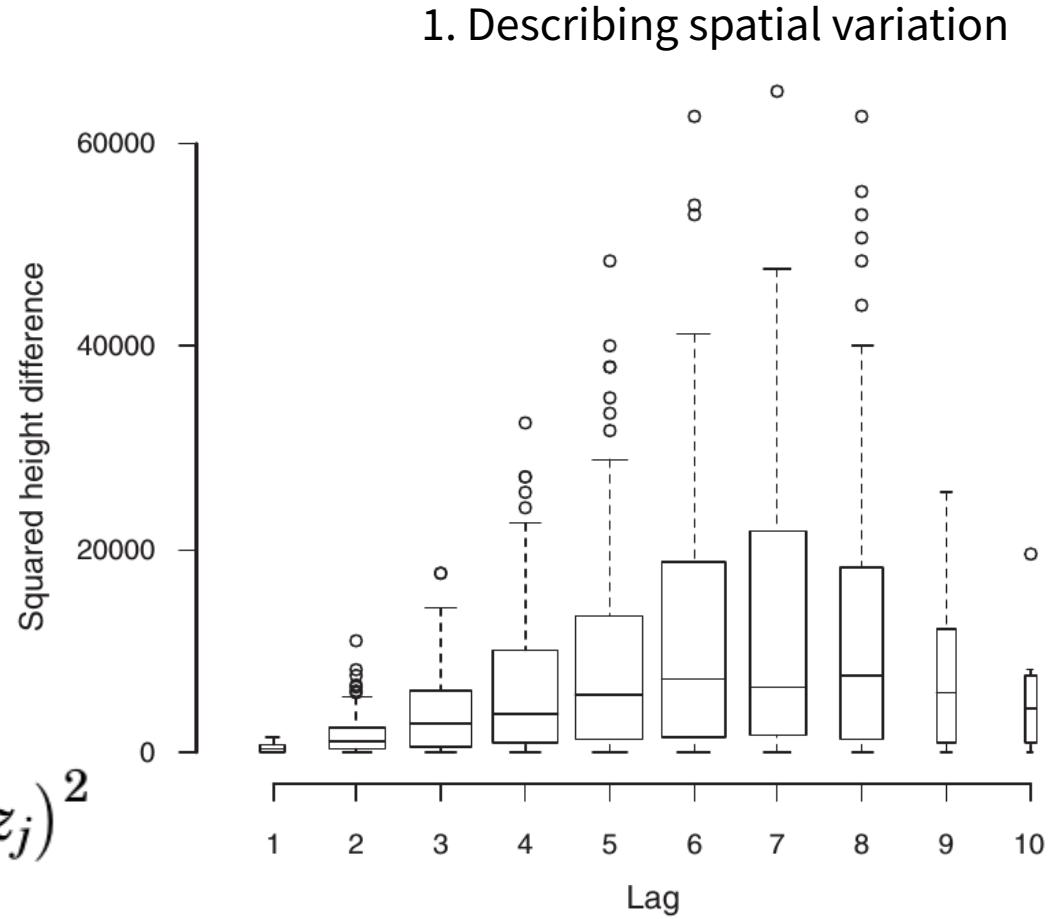
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Square differences, i.e. semivariogram cloud

Distance classes → lags  
and summary statistics  
→ *experimental semivariogram*  
[or short variogram]

Semivariance

$$2\hat{\gamma}(d) = \frac{1}{n(d \pm \Delta/2)} \sum_{d \pm \Delta/2} (z_i - z_j)^2$$



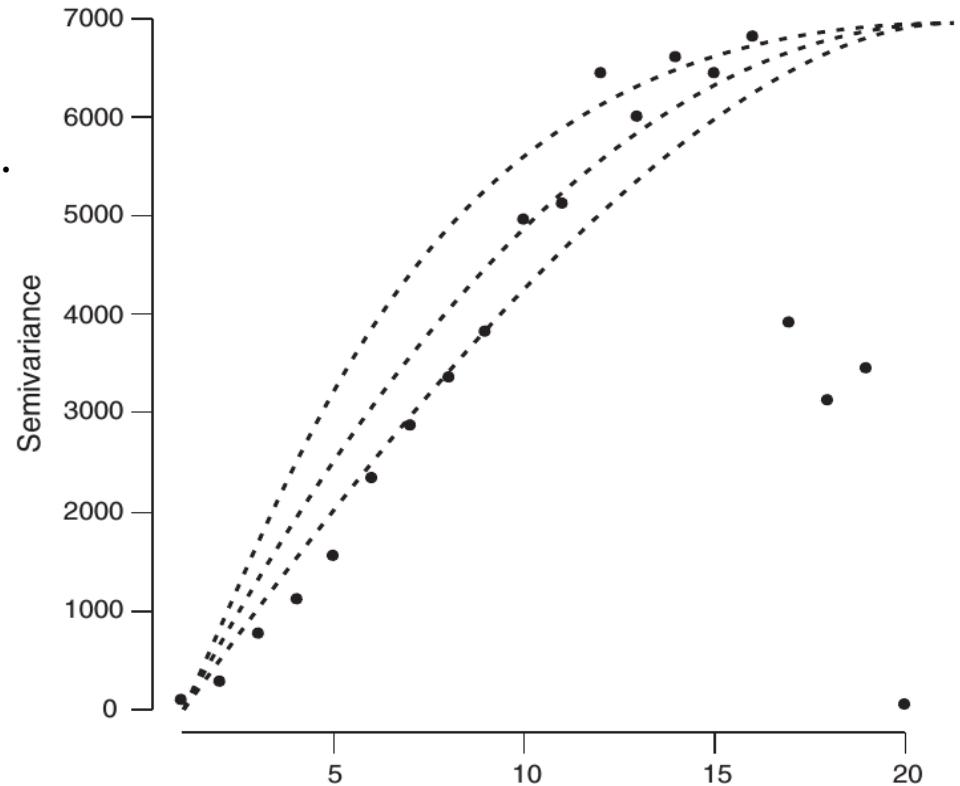
## Kriging

# Interpolation

Fitting a function to the experimental estimates from the semivariogram

Any function? No. Function has to be authorized, i.e.  
→ function can only be positive  
→ intercept at zero

2. Summarizing spatial variation



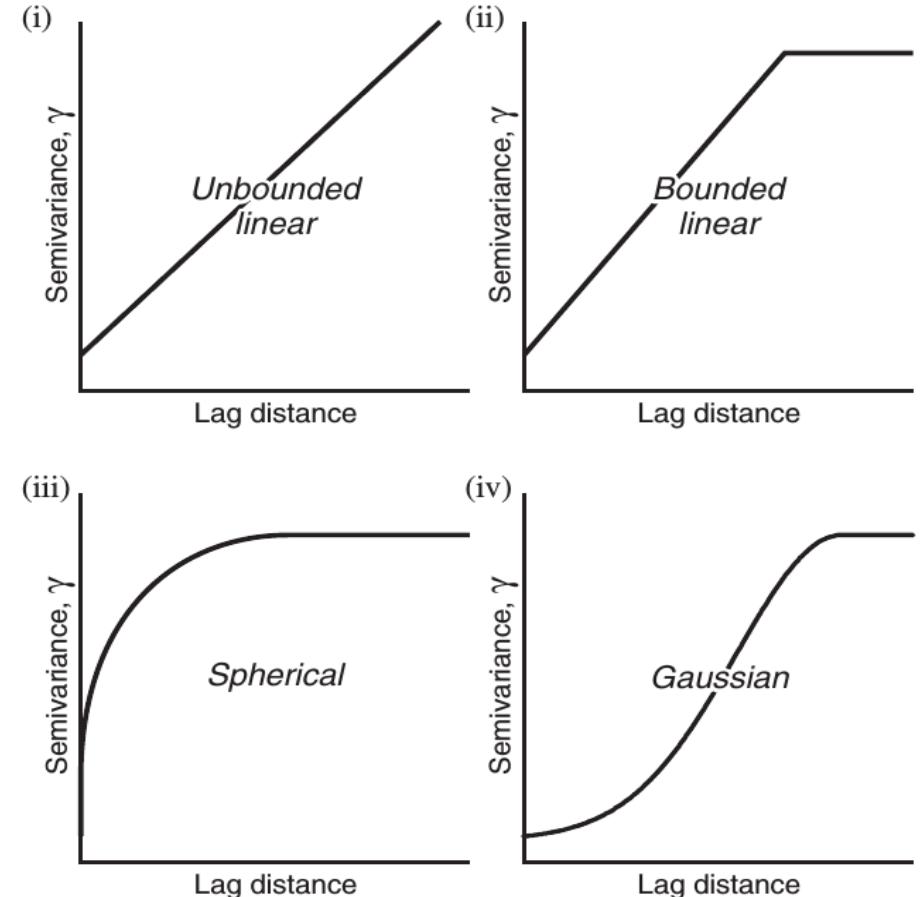
## Kriging

# Interpolation

Fitting a function to the experimental estimates from the semivariogram

Exemplary functions to fit

2. Summarizing spatial variation

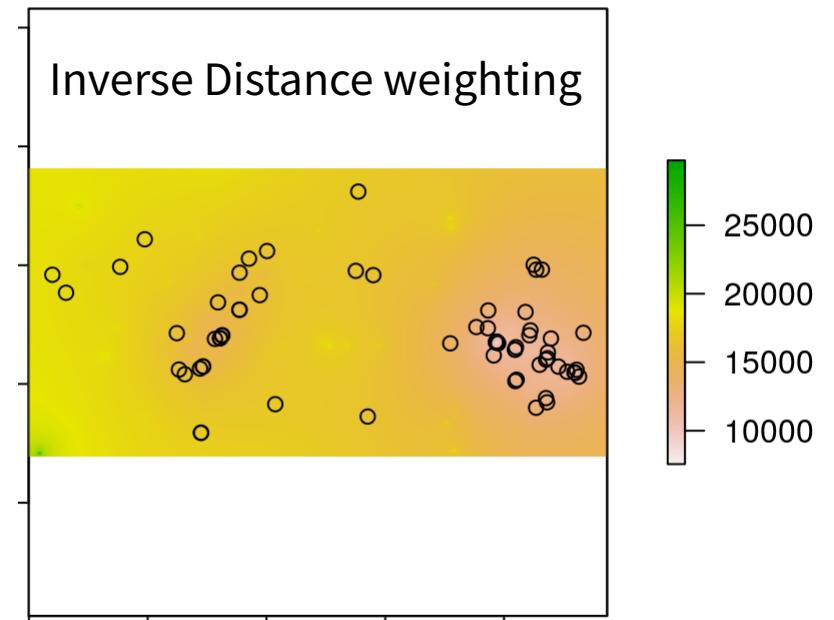
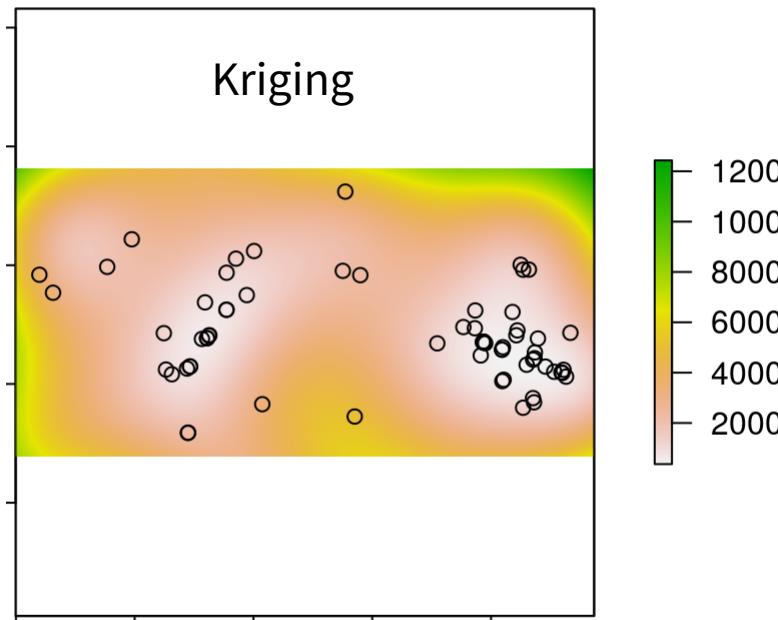


(O'Sullivan & Unwin, 2010)

# Interpolation

Aim: get a continuous representation of settlement density.

Mission accomplished...!?



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# Terrain analyses

Geomorphometry: the science of the quantitative representation of the Earth's surface

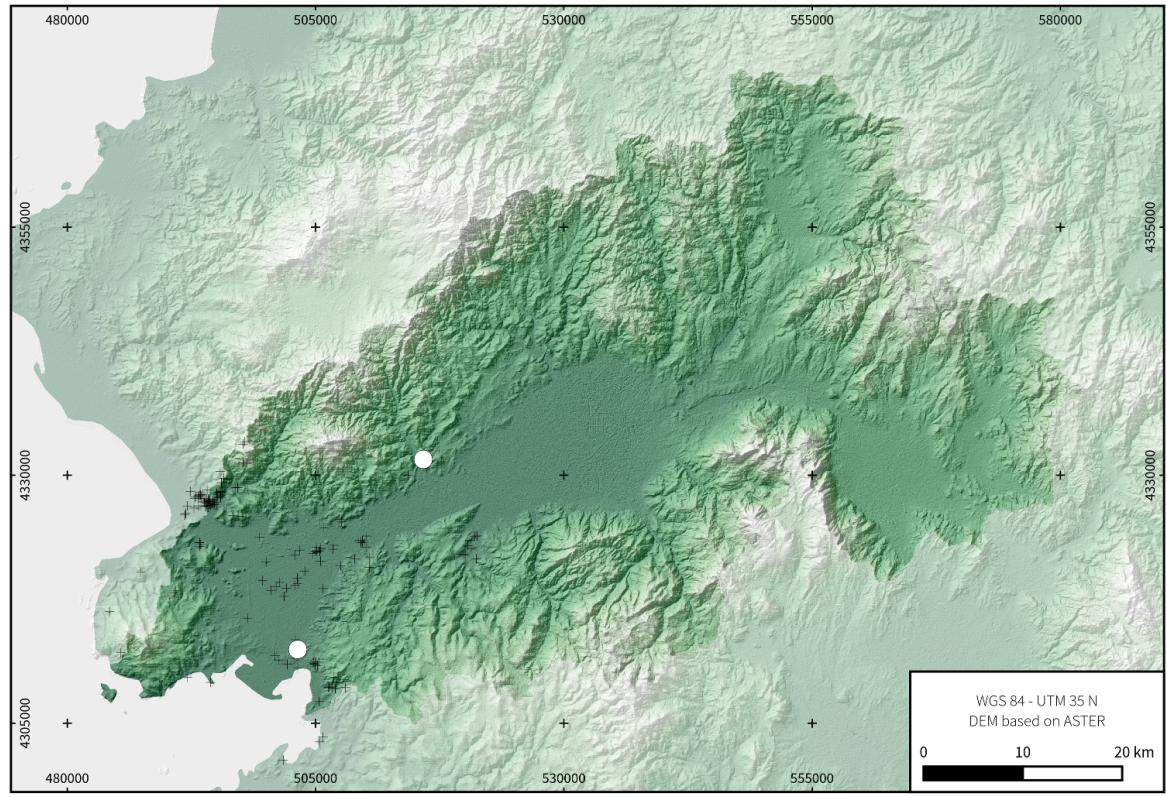
A great starting point:

Tomislav Hengl and Hannes I. Reuter (eds):  
Geomorphometry Concepts, Software, Applications.  
Developments in Soil Science, Volume 33, Pages 1-765 (2009)

# Terrain analyses

Geomorphometry: the science of the quantitative representation of the Earth's surface

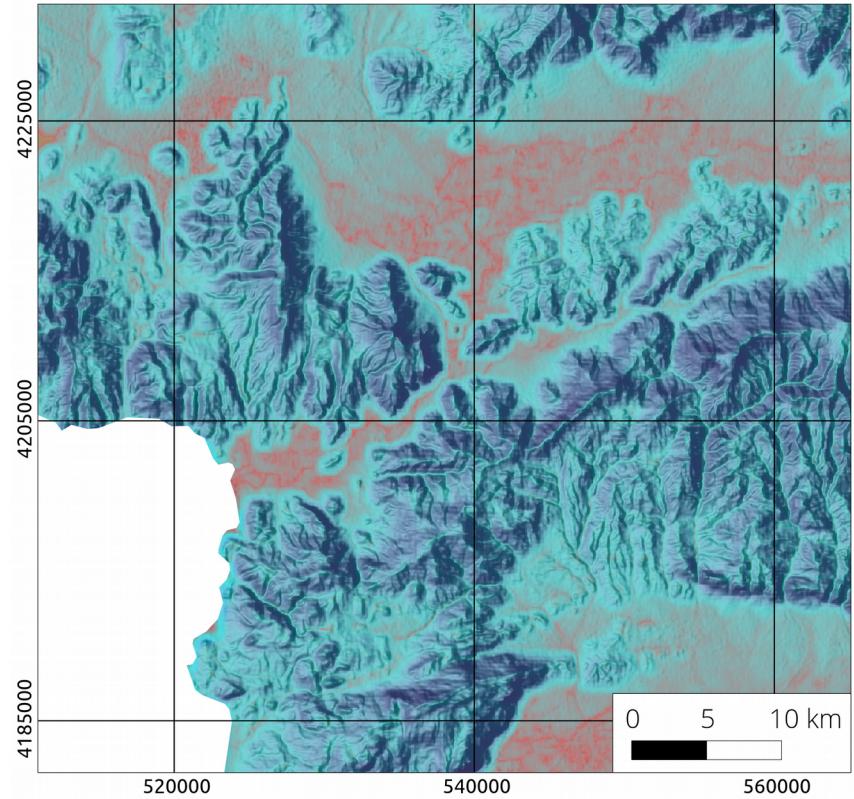
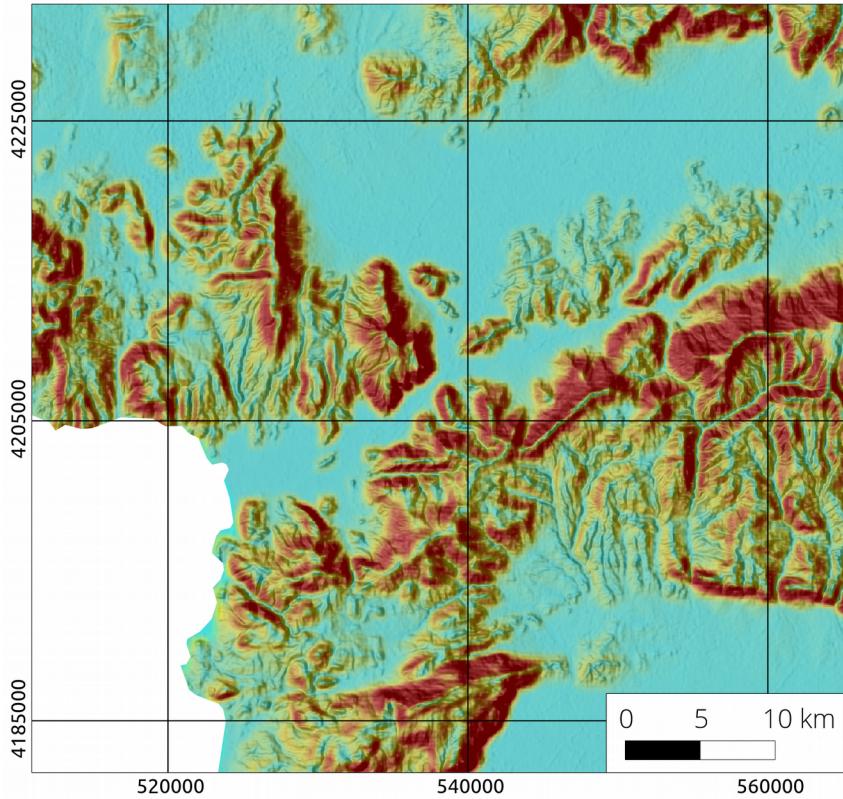
Everything starts with a DEM...



# Terrain analyses

Slope = difference length/difference height

$$MTI = \ln\left(\frac{A^n}{\tan\beta}\right)$$



# Terrain analyses – what was perceivable?



# Terrain analyses – what was perceivable?



# Terrain analyses – what was perceivable?



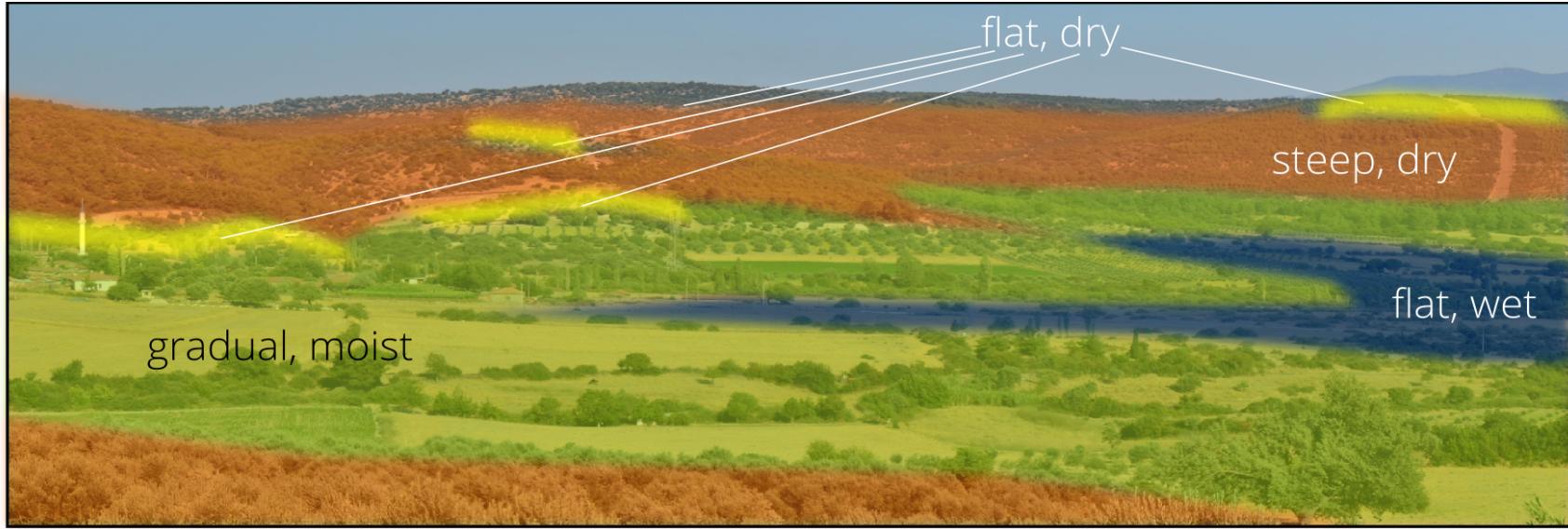
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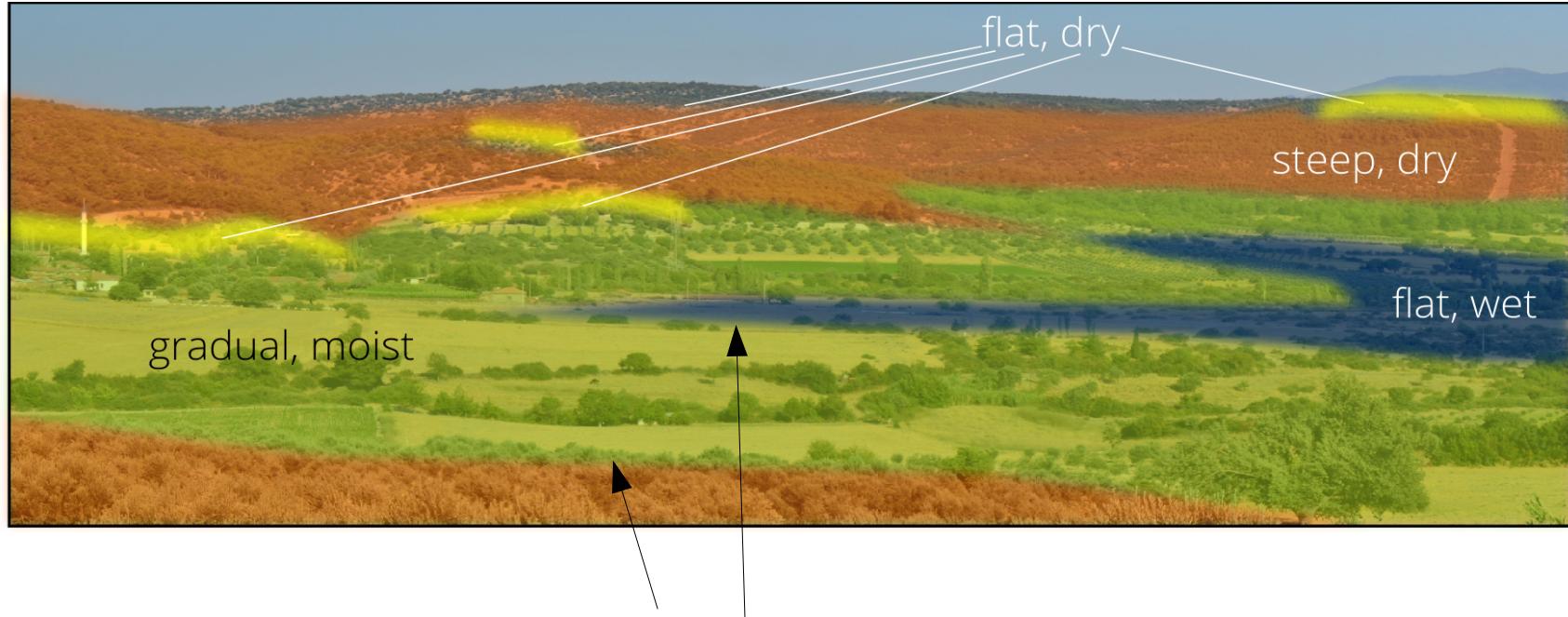
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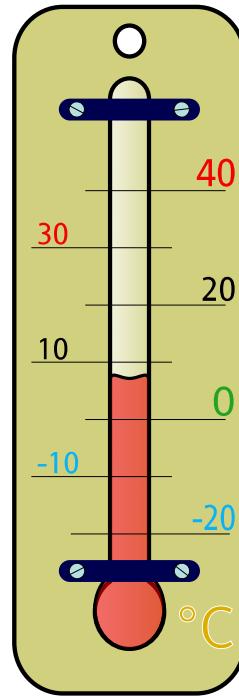
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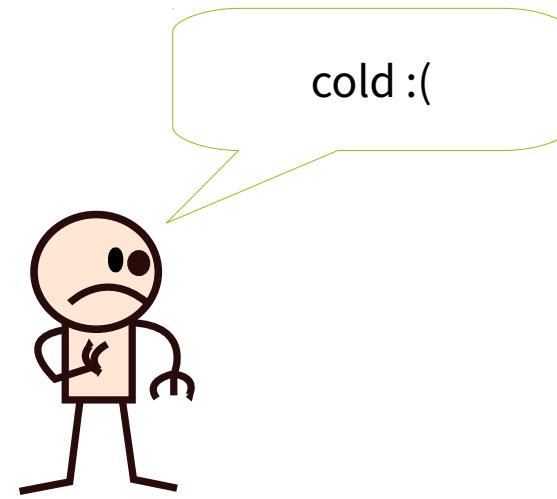
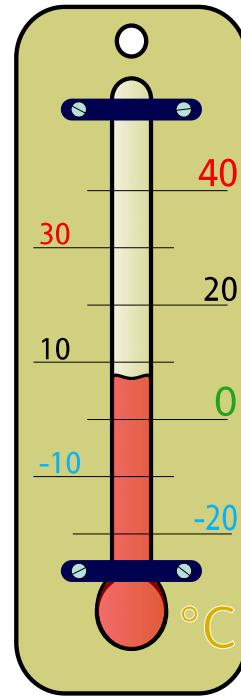
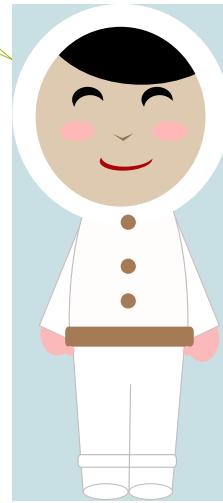


# Crisp vs. fuzzy boundaries



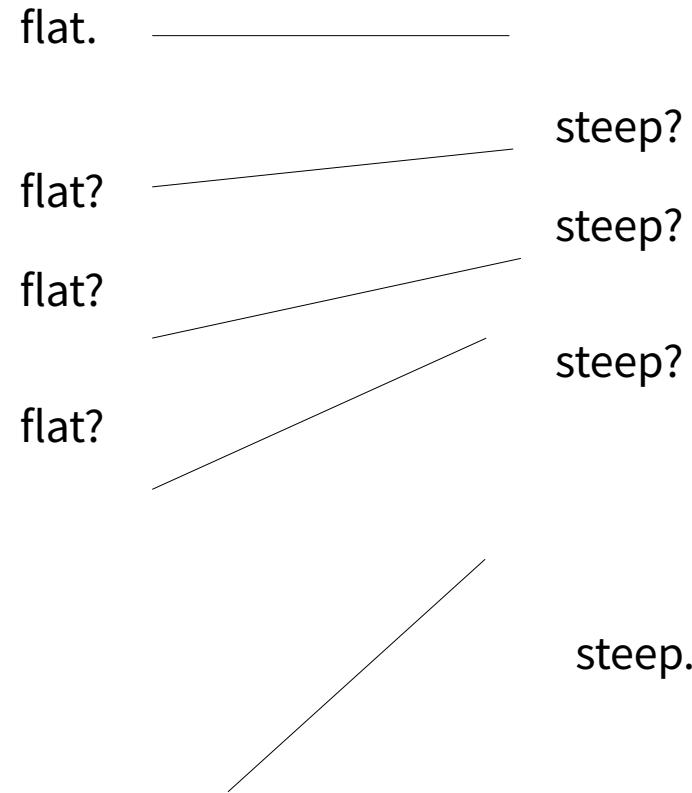
# Crisp vs. fuzzy boundaries

warm :)

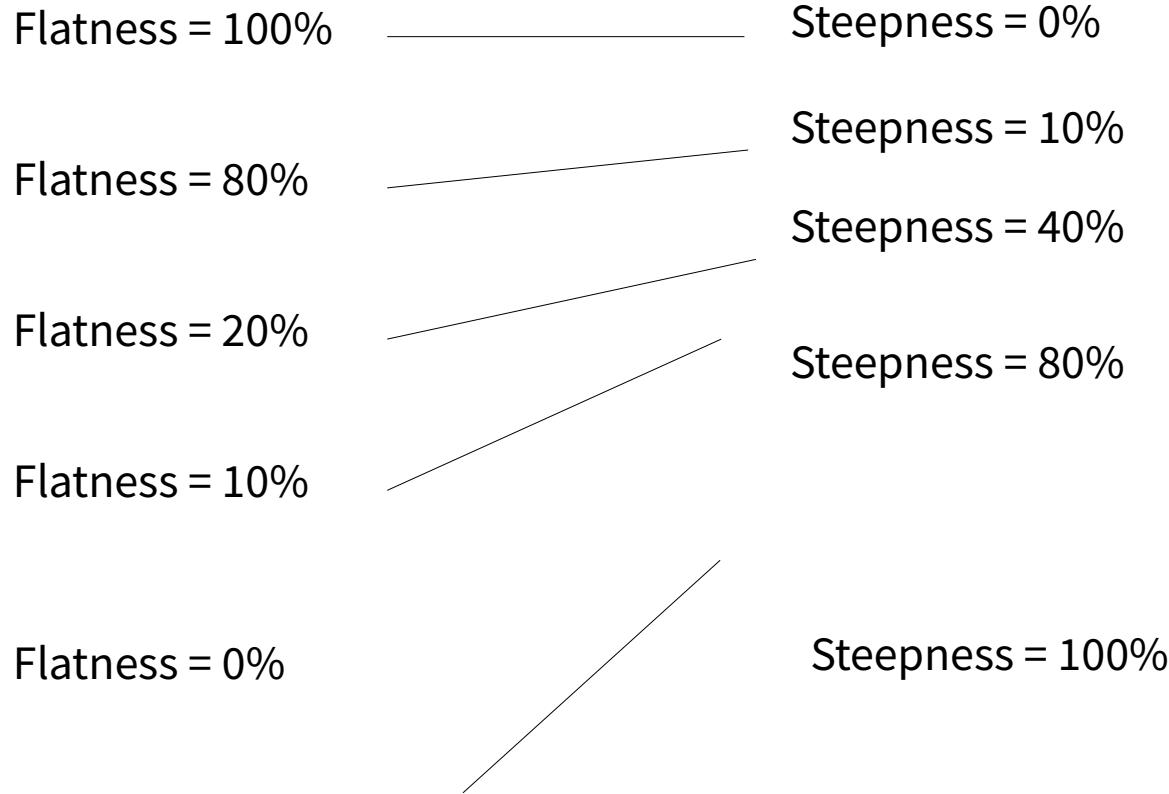


cold :(

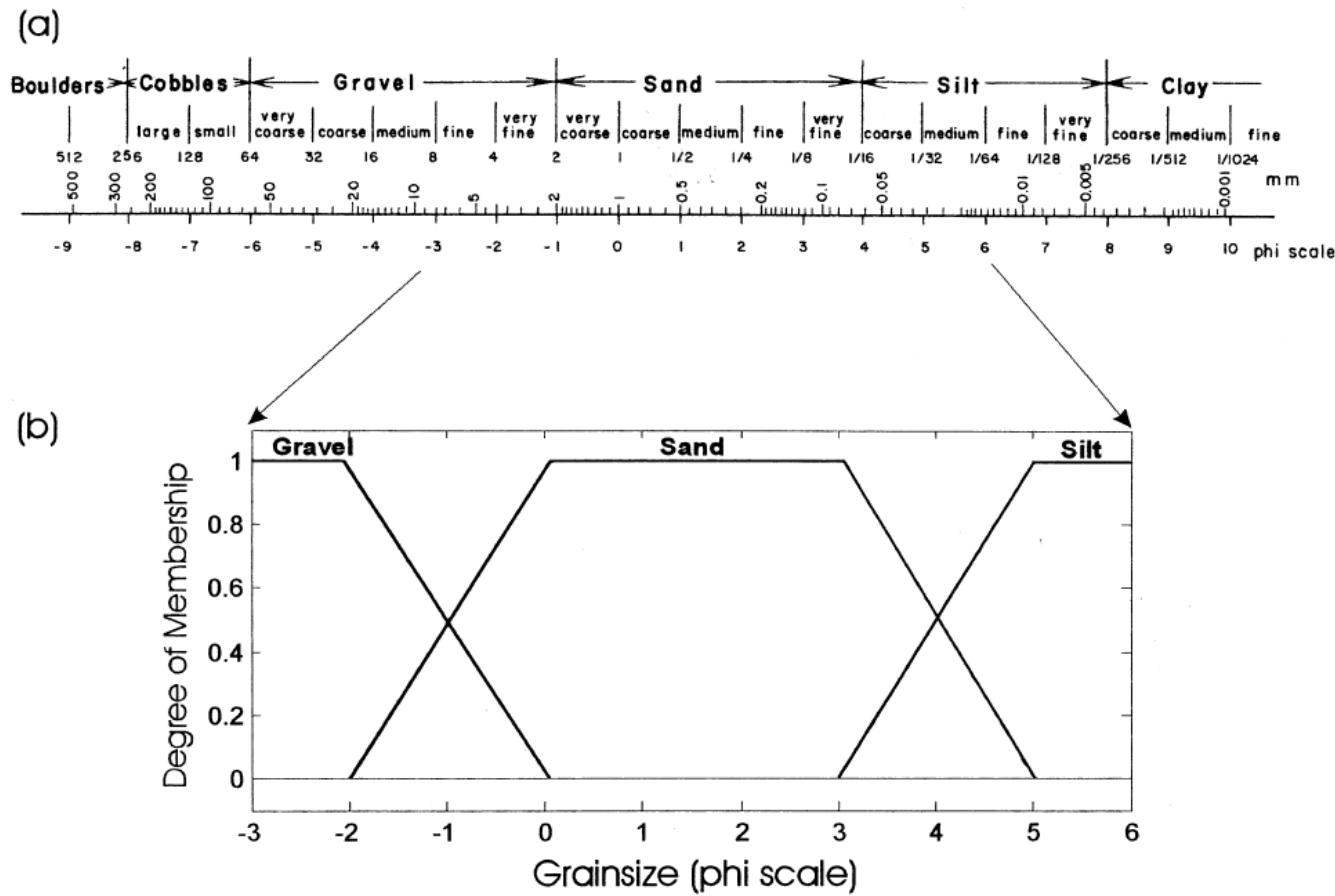
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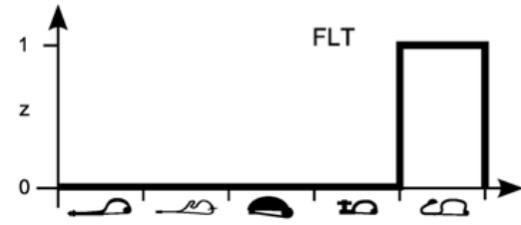
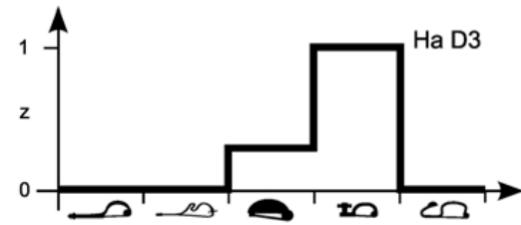
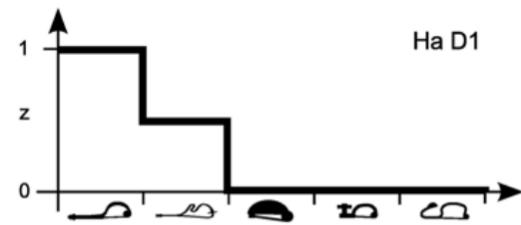
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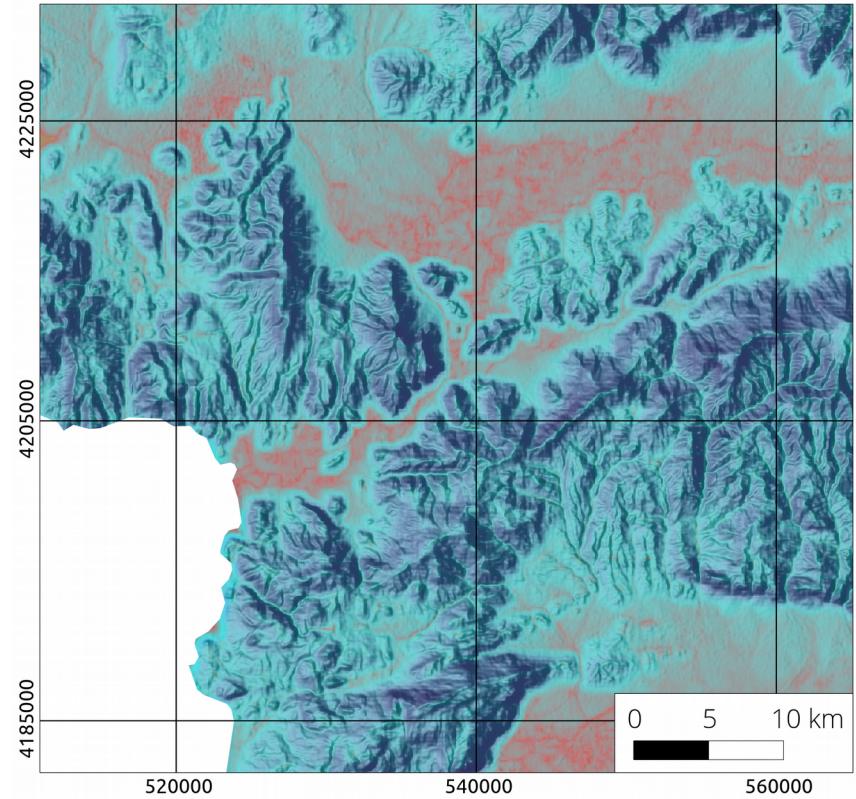
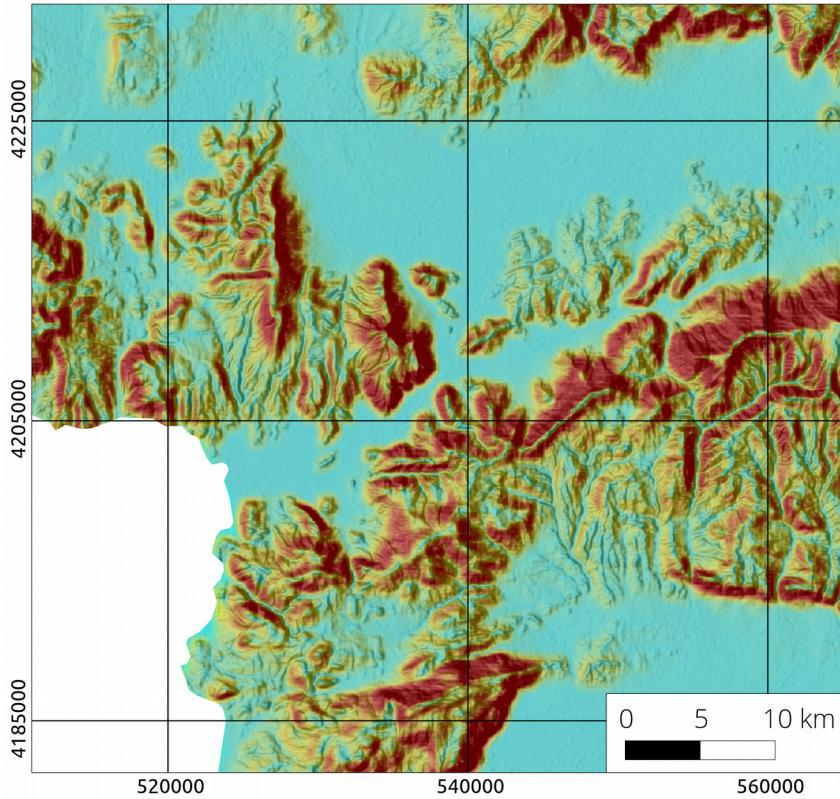
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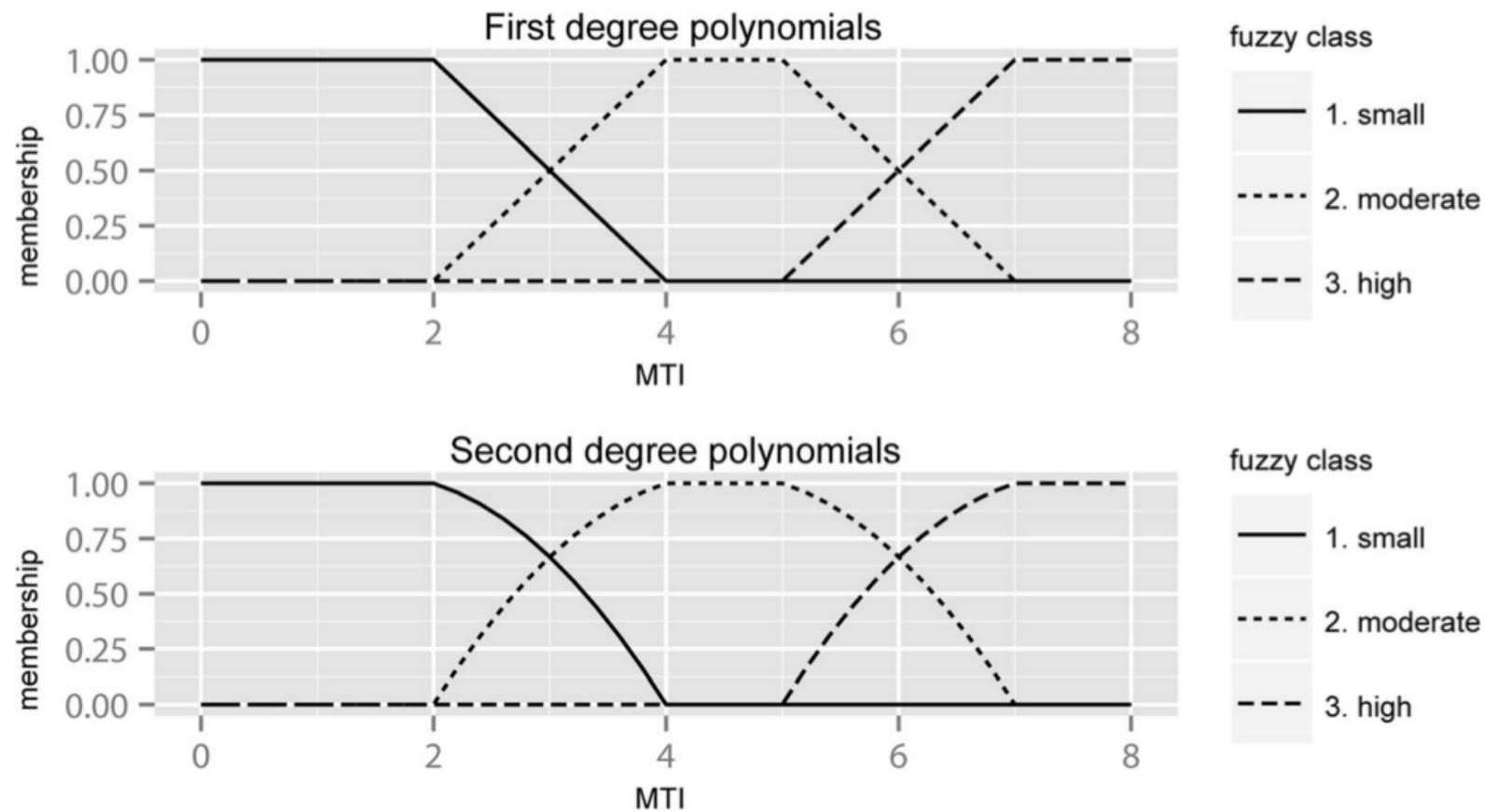
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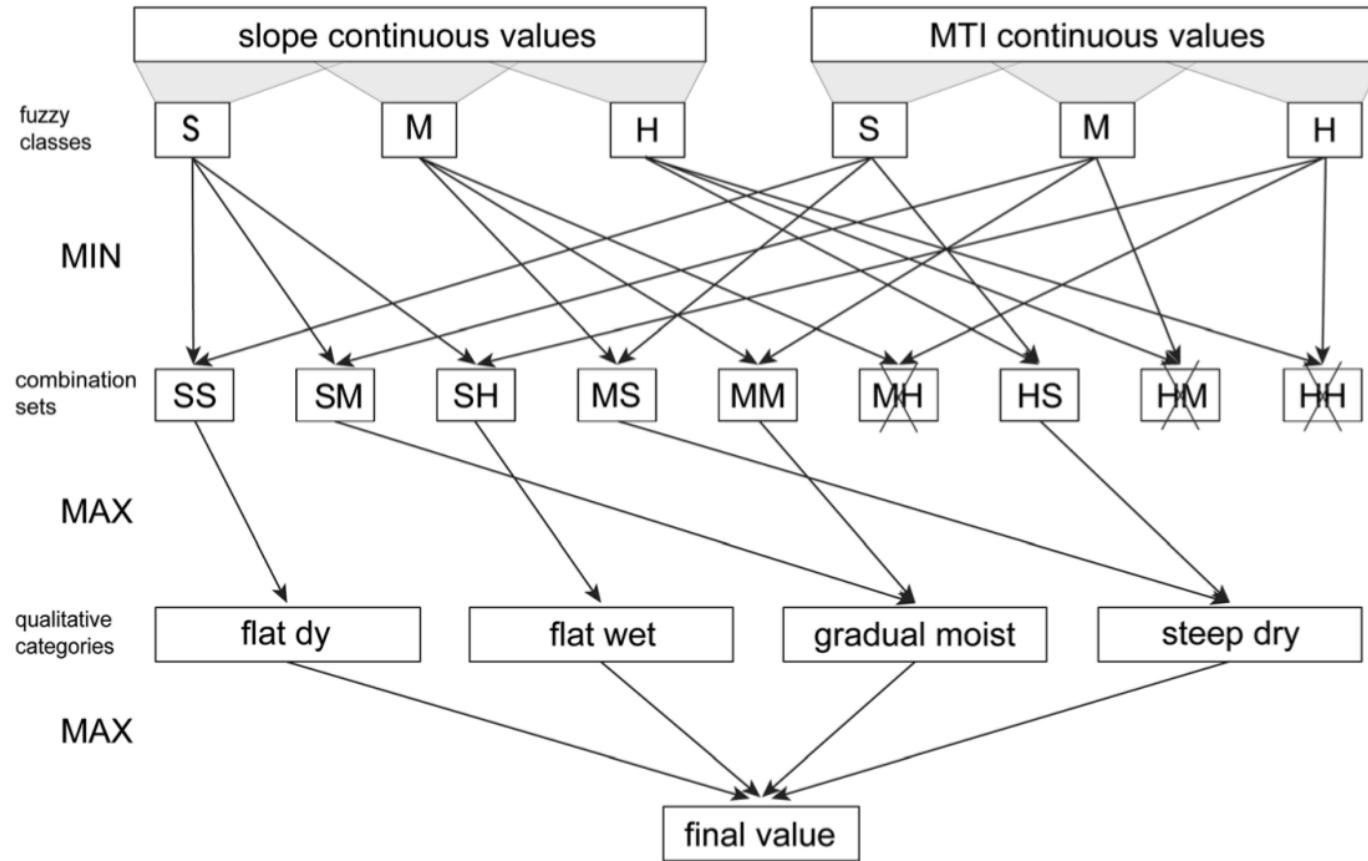
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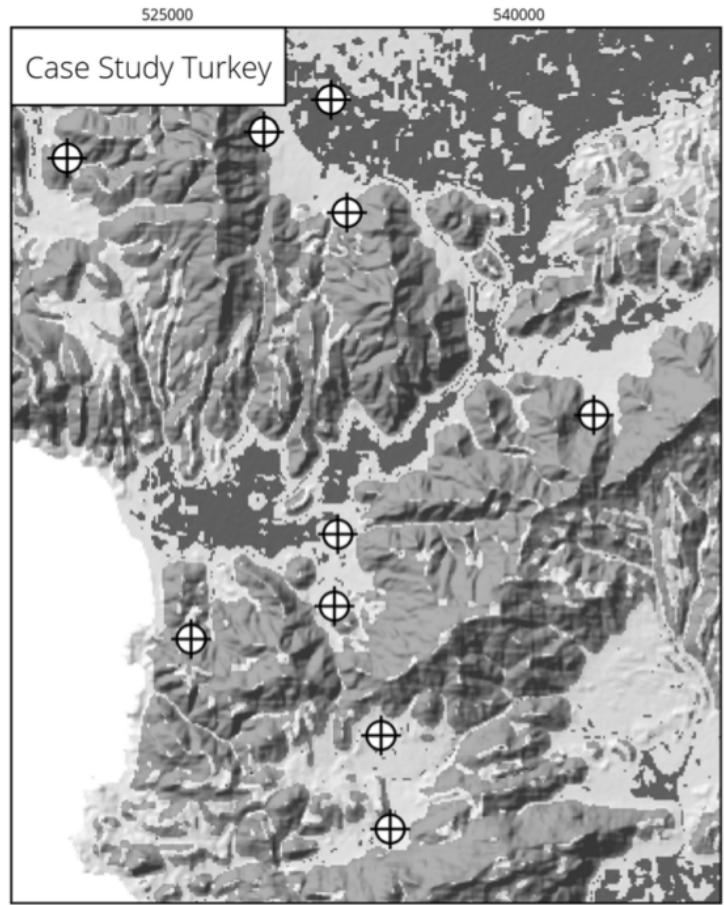
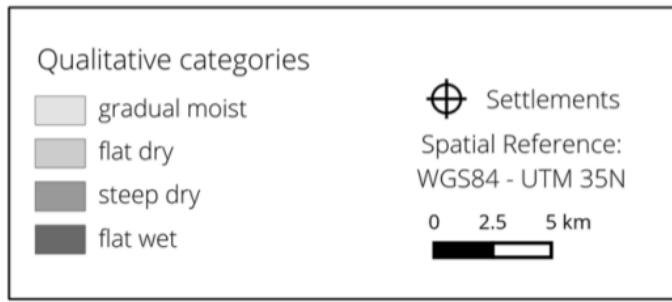
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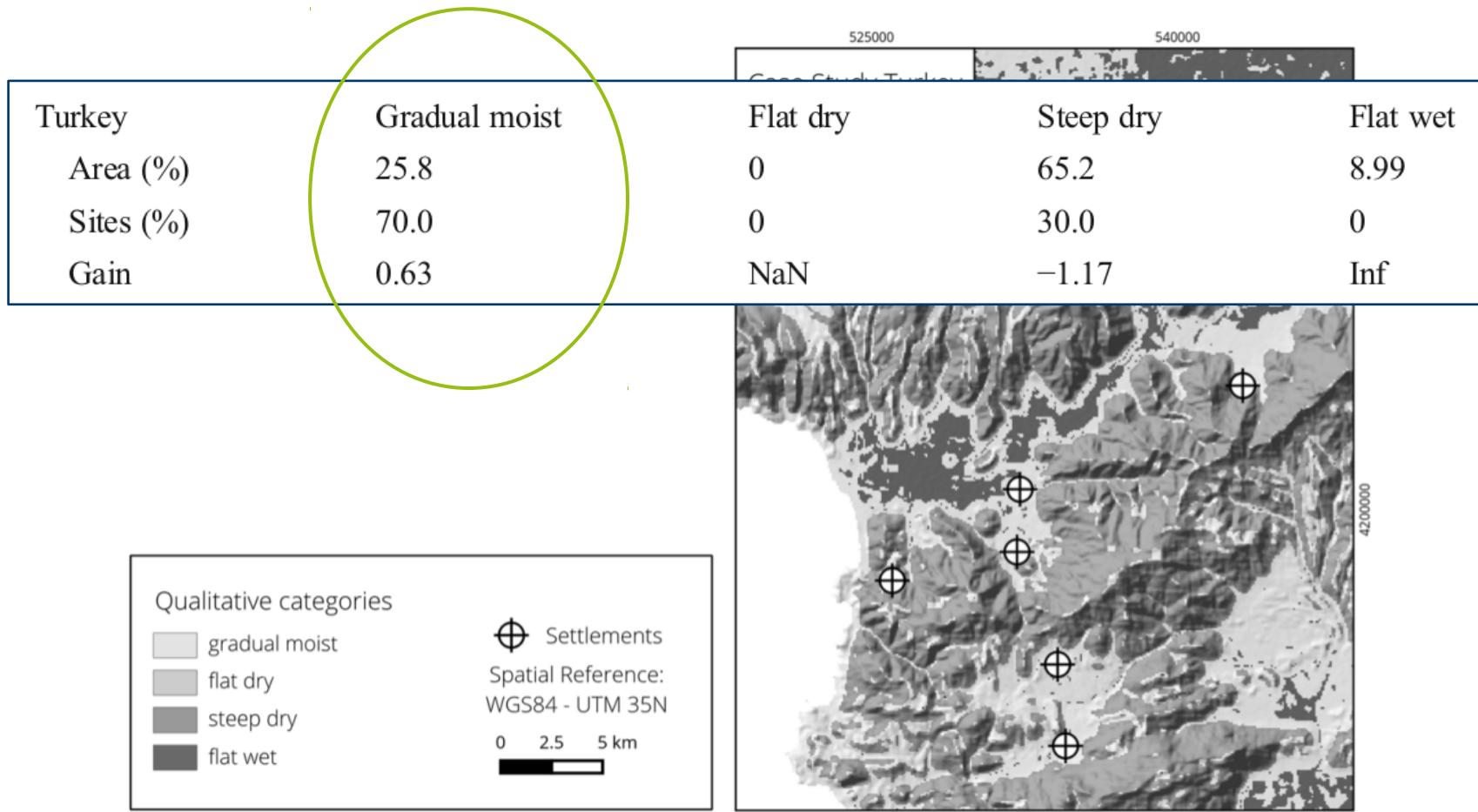
# Terrain analyses – what was perceivable?



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If “they” preferred certain areas,  
how would a resulting interaction  
network look like?

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Workflow:

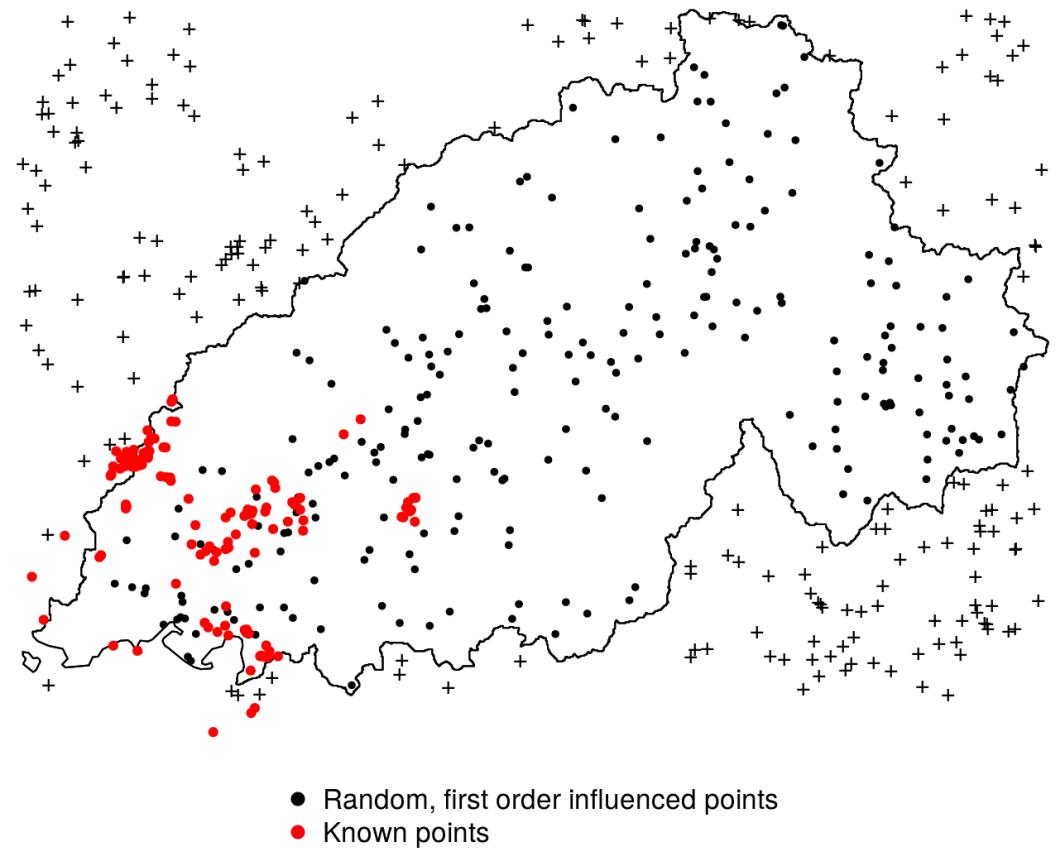
- fuzzy terrain

# Terrain analyses – what was perceivable?

If “they” preferred certain areas,  
how would a resulting interaction  
network look like?

Workflow:

- fuzzy terrain
- point pattern analyses



# Terrain analyses – what was perceivable?

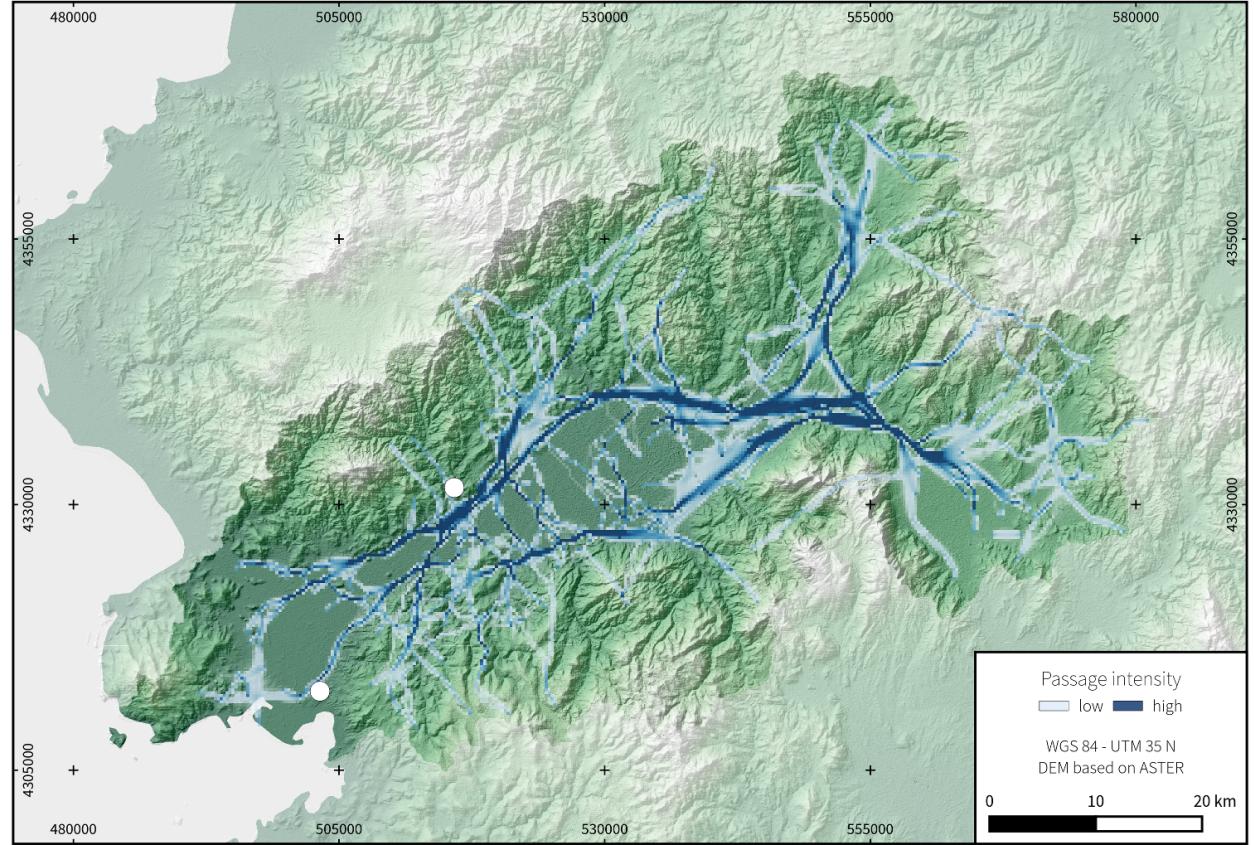
If “they” preferred certain areas, how would a resulting interaction network look like?

Workflow:

- fuzzy terrain
- point pattern analyses
- cost-surface creation
- pseudo-random walk

(the smaller the cost, the higher the probability)

- sum of all random walks

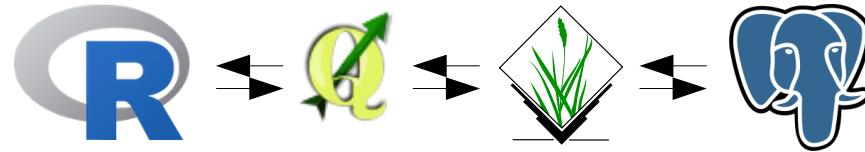


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# Outlook: personal advices

use open-source software, i.e. free software published under terms of GNU GENERAL PUBLIC LICENSE



Why?

- They grow. Fast. So you can work at the bleeding edge
  - YOU can contribute
  - others can contribute so YOU can profit from their methods and tools
  - you can investigate how methods are implemented.
- 

Publish open access. [www.sci-hub.io](http://www.sci-hub.io) is/was no alternative and science needs to be free.

---

Share your code. It is easy: [github.com](https://github.com) or better [gitlab.com](https://gitlab.com)

Thank you very much for your attention.

# Entity-Attribute Spatial Data Types

Processes caused the spatial occurrence of different entities

Ceramic types

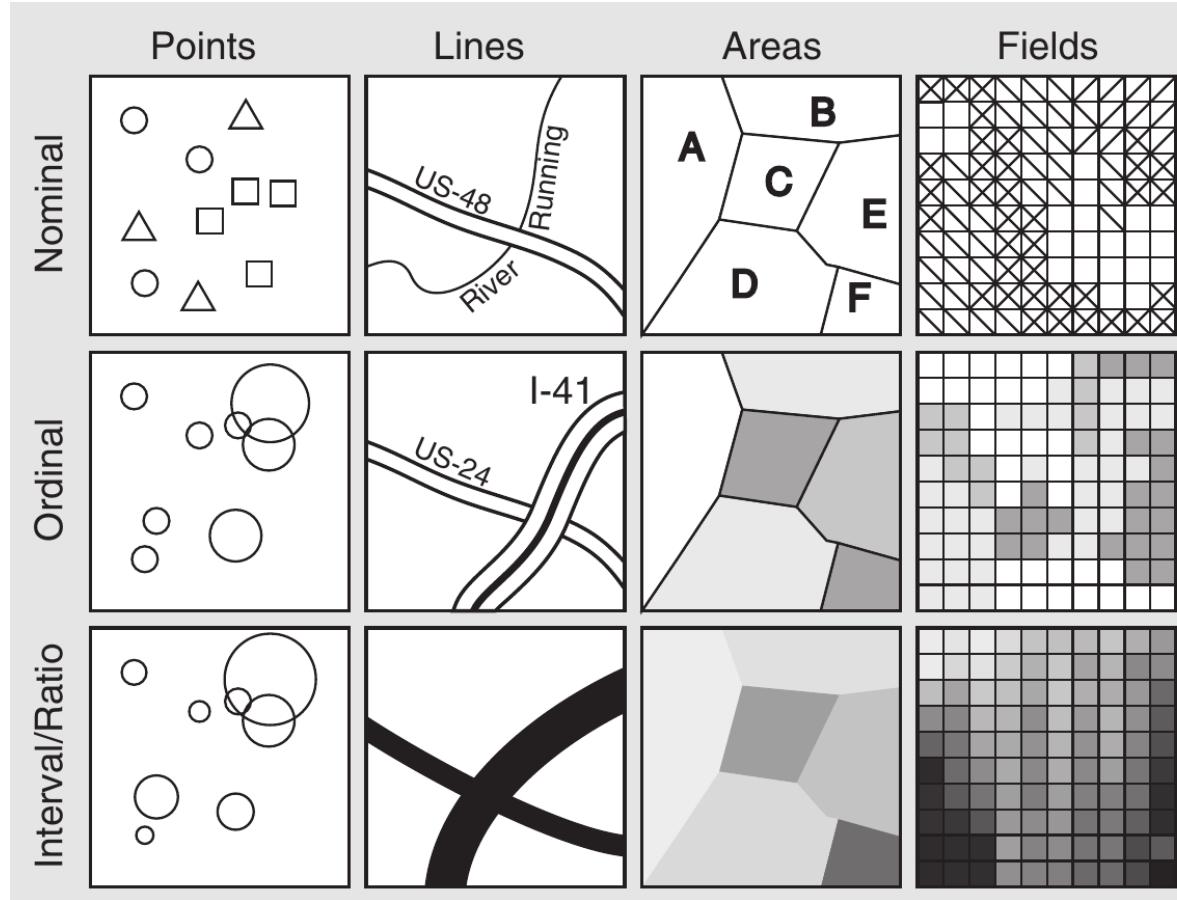
Site types

Hierarchy

Site size

Territories

Population density



# Entity-Attribute Spatial Data Types

Processes define the transformation of spatial data

		TO			
		<i>Point, L<sup>0</sup></i>	<i>Line, L<sup>1</sup></i>	<i>Area, L<sup>2</sup></i>	<i>Field, L<sup>3</sup></i>
F R O M	<i>Point, L<sup>0</sup></i>	Mean center	Network graphs	Proximity polygons TIN, point buffer	Interpolation. Kernel density estimation Distance surfaces
	<i>Line, L<sup>1</sup></i>	Intersection junction	Shortest distance path	Line buffer	Distance to nearest line object surface
	<i>Area, L<sup>2</sup></i>	Centroid City center	Graph of area skeleton	Area buffer, Polygon overlay	Pycnophylatic interpolation and other surface models
	<i>Field, L<sup>3</sup></i>	Surface specific points VIPs	Surface network	Watershed delineation, Hill masses	Equivalent vector field territories

# Spatial Autocorrelation – Moran's I

$$I = \left[ \frac{n}{\sum_{i=1}^n (y_i - \bar{y})^2} \right] \times \left[ \frac{\sum_{i=1}^n \sum_{j=1}^n w_{ij}(y_i - \bar{y})(y_j - \bar{y})}{\sum_{i=1}^n \sum_{j=1}^n w_{ij}} \right]$$

Weight from spatial weight matrix

Covariance term

Division by total data variance

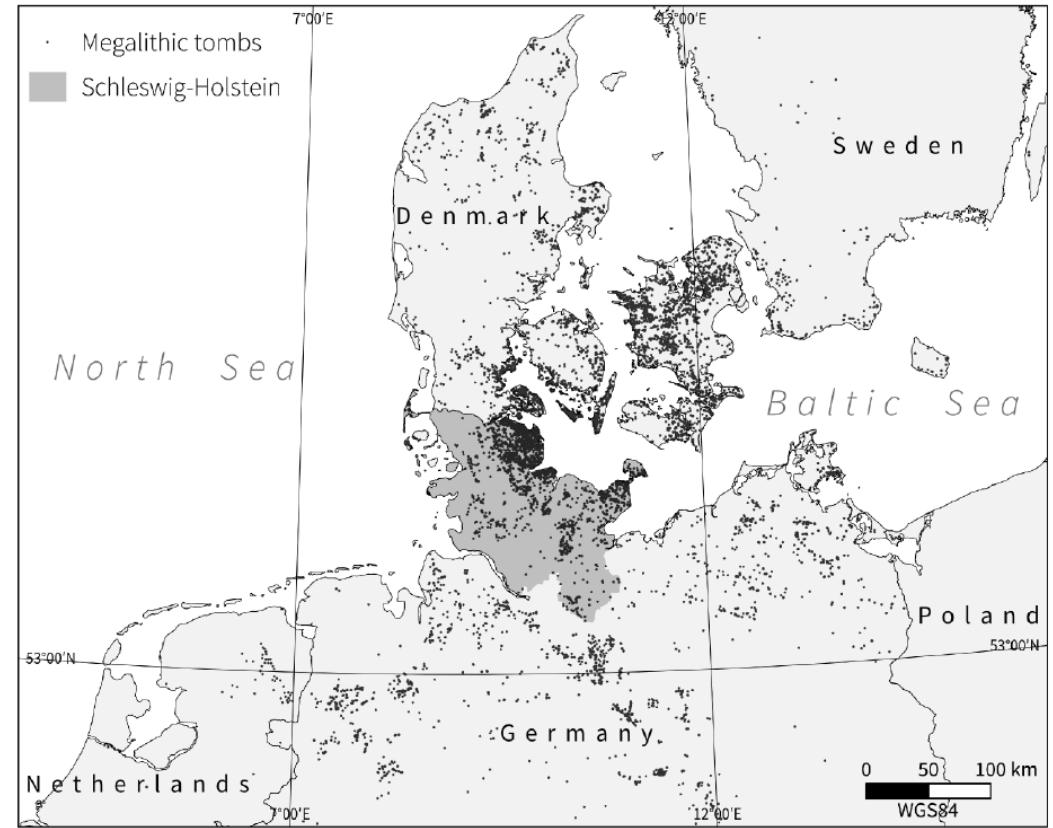
Normalize to total spatial weights

The diagram illustrates the components of the Moran's I formula. It shows the formula as a product of two matrices. The first matrix is a scalar divided by the sum of squared deviations from the mean. The second matrix is a weighted covariance term divided by the sum of weights. Annotations with arrows point to each component: 'Weight from spatial weight matrix' points to the covariance term, 'Covariance term' points to the numerator of the second matrix, 'Division by total data variance' points to the scalar in the first matrix, and 'Normalize to total spatial weights' points to the denominator of the second matrix.

# Point Pattern – second order effects

Shows the point pattern clustering/dispersion; does it deviate from CSR?

→ Simulation approach based on  
Monte Carlo simulations



# Point Pattern – second order effects

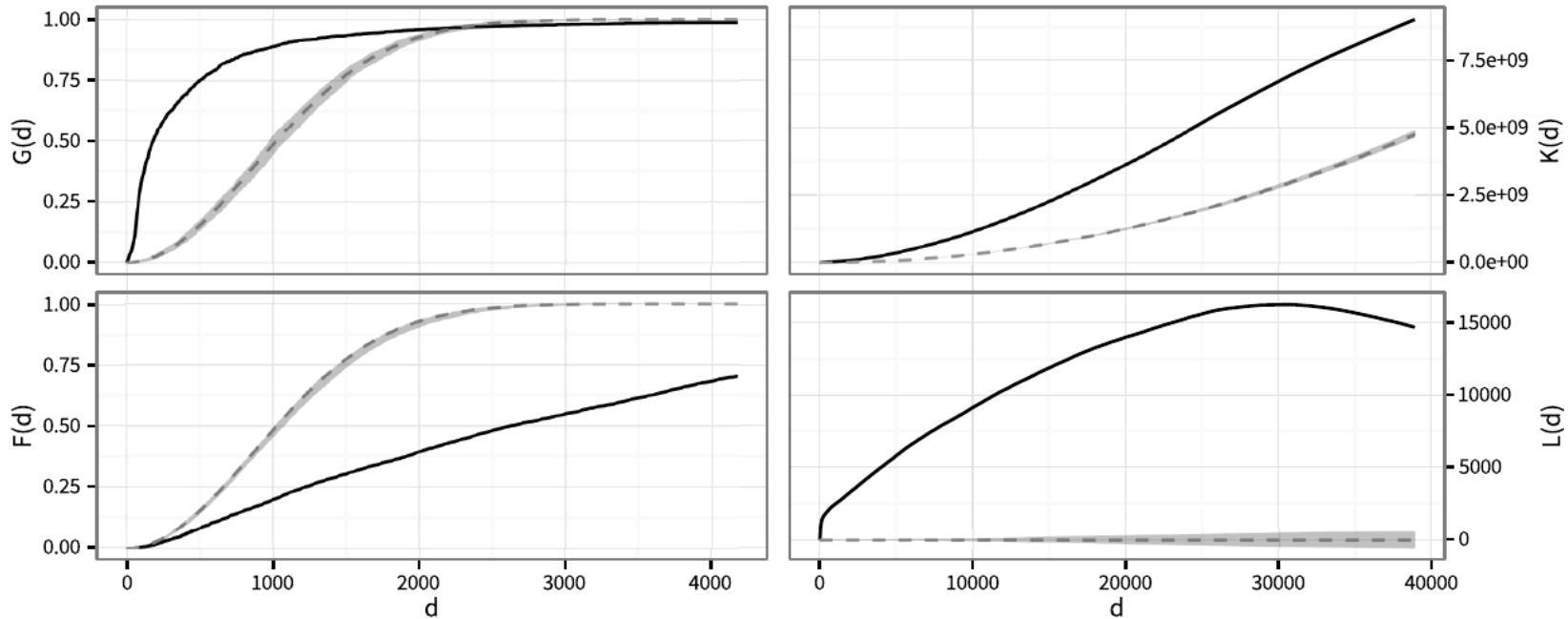
Shows the point pattern clustering/dispersion; does it deviate from CSR?

→ Simulation approach based on  
Monte Carlo simulations

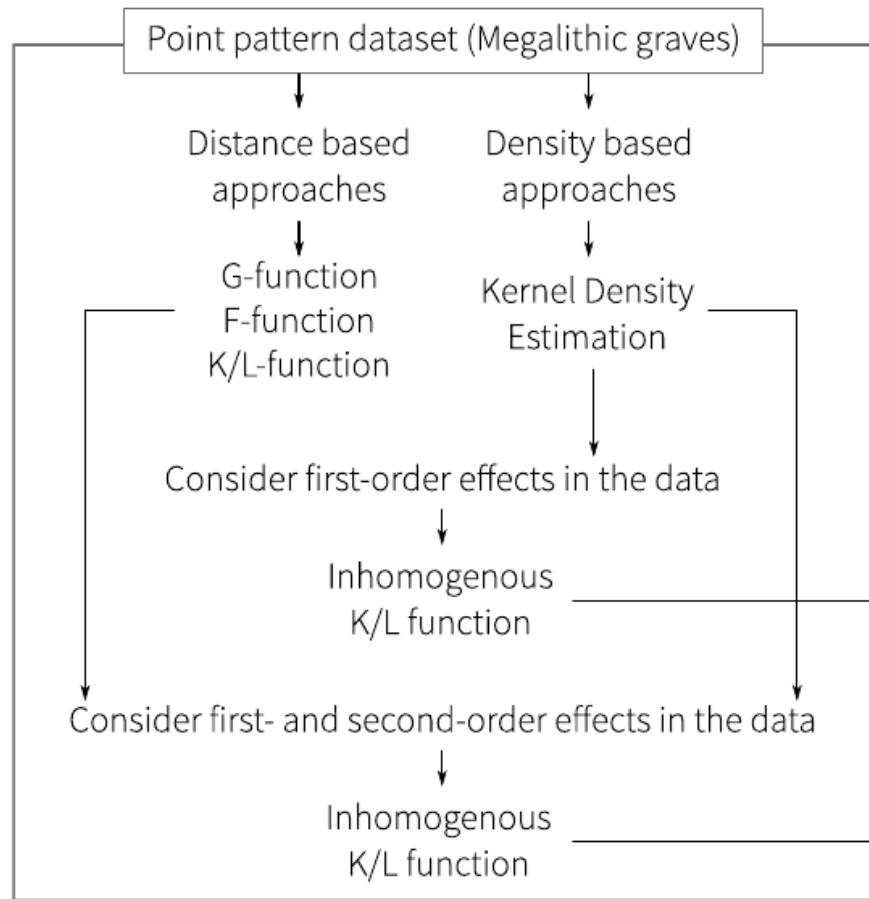
— Empirical distribution — Theoretical distribution

$$L(d) = \sqrt{\frac{K(d)}{\pi}}$$

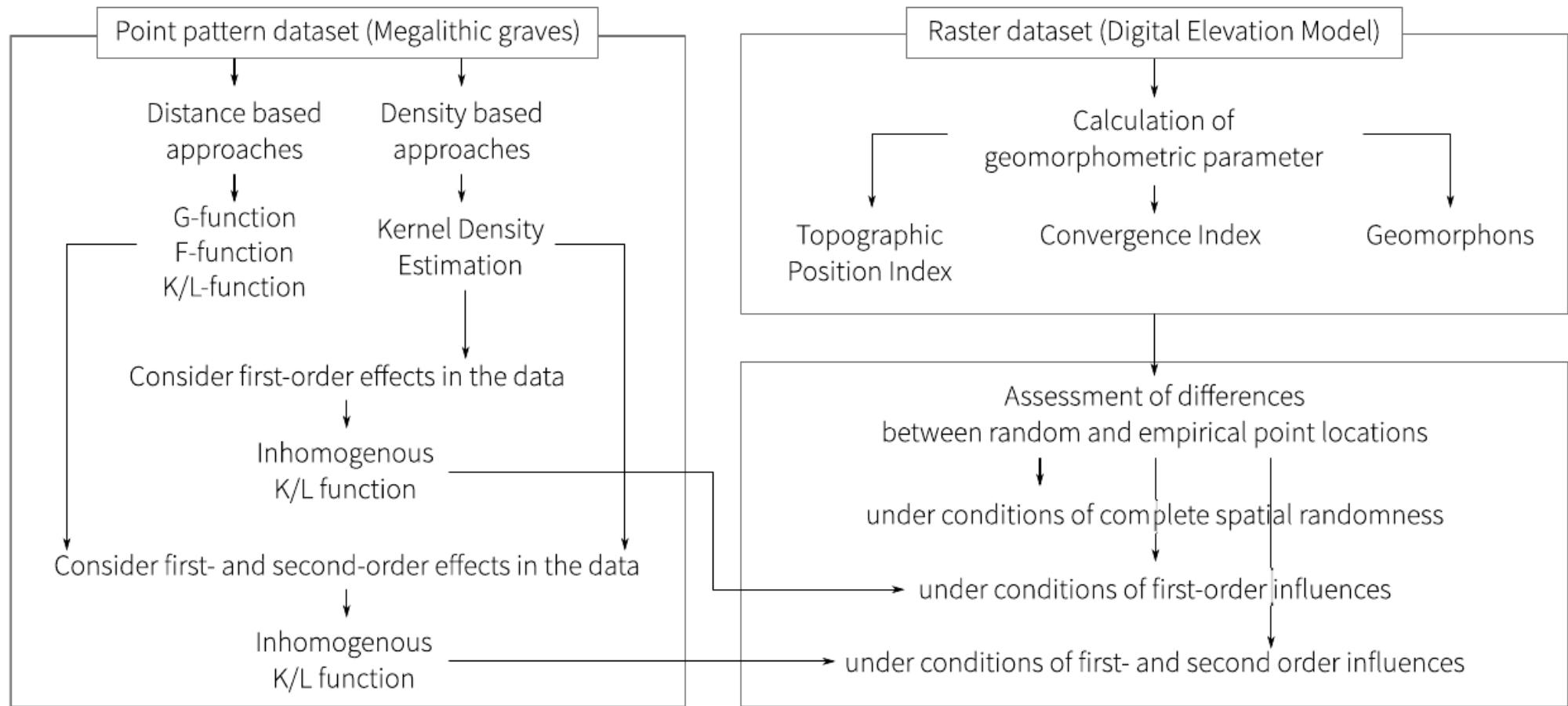
Just a  
square root  
transformation  
of  $K(d)$



# Point Pattern – a look ahead



# Point Pattern – a look ahead



## Kriging

# Interpolation

### “Elements” of a semivariogram

Nugget

→ measurement error

→ variation below shortest sampling interval

Sill

→ range of semivariance

Range

→ distance at which semivariance reaches maximal value

2. Summarizing spatial variation

