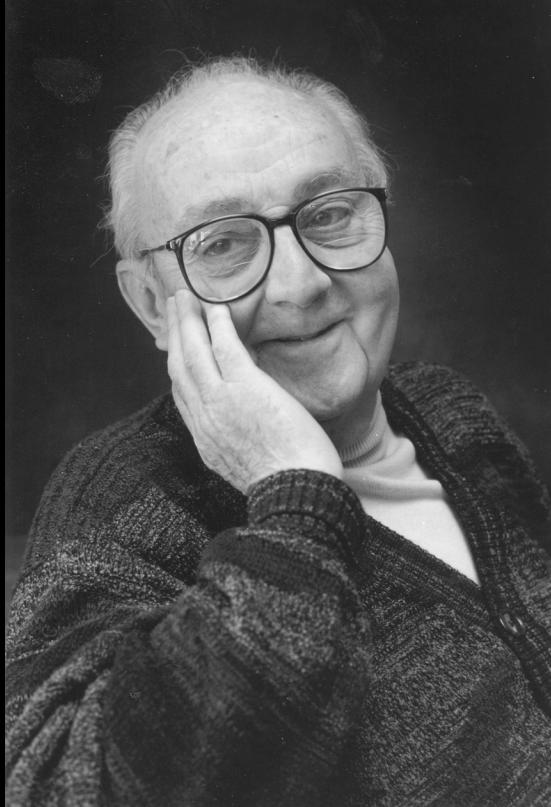


A very short introduction to Modeling in Landscape Archaeology

Daniel Knitter



"Since all models are wrong
the scientist cannot obtain a 'correct' one
by excessive elaboration.

On the contrary following William of Occam
[s]he should seek an economical description
of natural phenomena.

Just as the ability to devise simple but evocative
models is the signature of the great scientist
so overelaboration and overparameterization
is often the mark of mediocrity" (Box 1976, 792).

By DavidMCEddy at en.wikipedia, CC BY-SA 3.0,
<https://commons.wikimedia.org/w/index.php?curid=14941622>

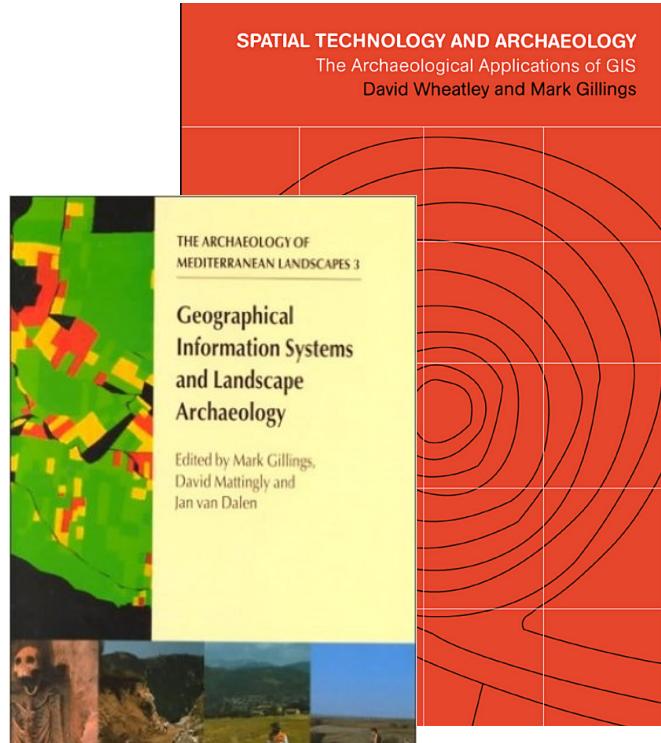
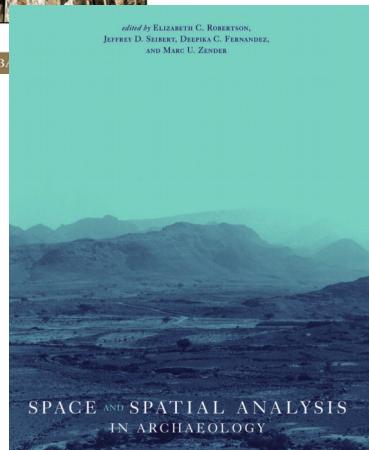
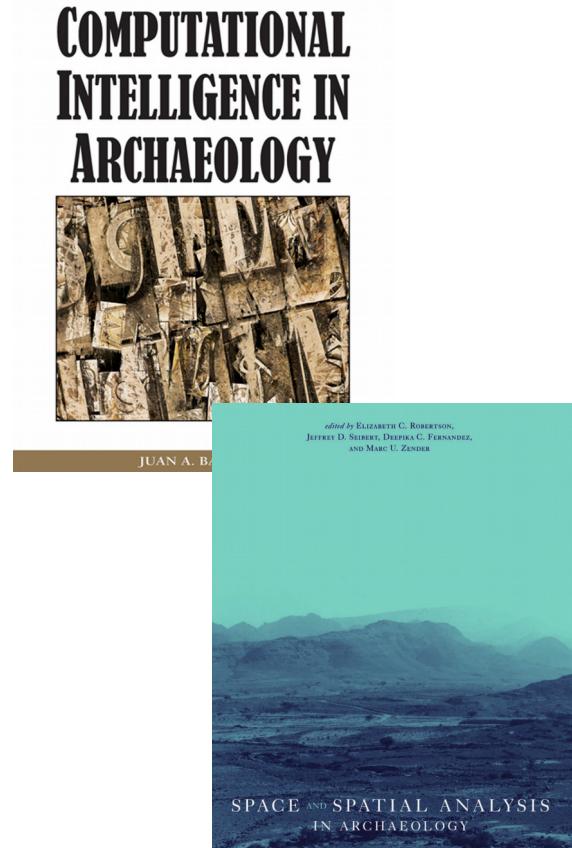
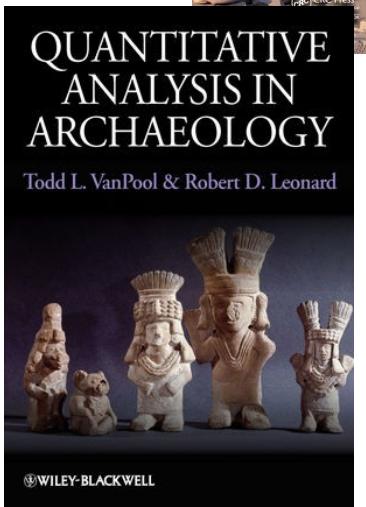
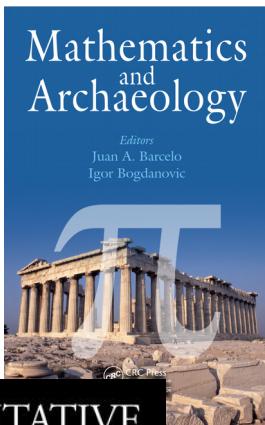
Content

- Modeling and processes
- Why space matters: Potentials and Pitfalls of Spatial Data
- Point Pattern Analyses: What processes might have caused the distribution of findings?
 - First order processes (density based approaches)
 - Second order processes (distance based approaches)
- From single attributes to continuous surfaces: geostatistics
- Geomorphometry: What is the character of the landscape?
- Outlook

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Modeling in (Landscape) Archaeology

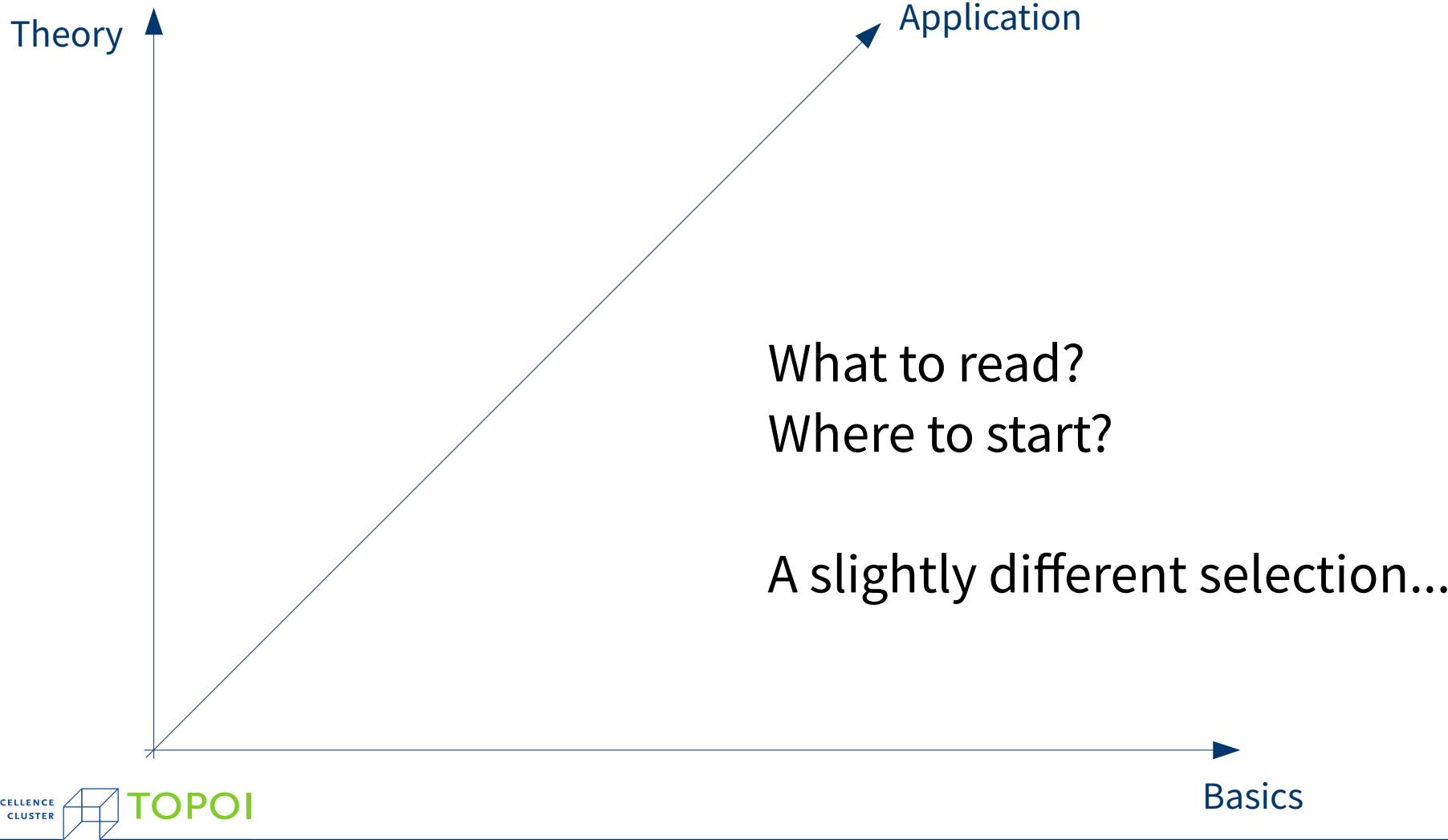


Modeling in Landscape Archaeology

What to read?
Where to start?

A slightly different selection...

Modeling in Landscape Archaeology



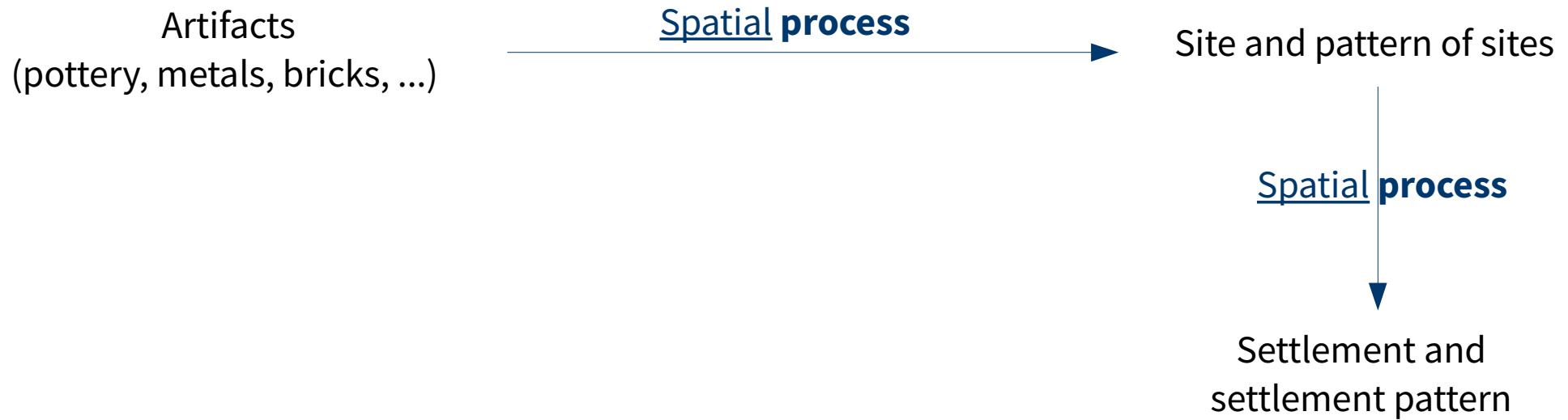


Modeling in Landscape Archaeology

- Spatial phenomena are the result of processes
- Modeling = (re-)construction of these processes

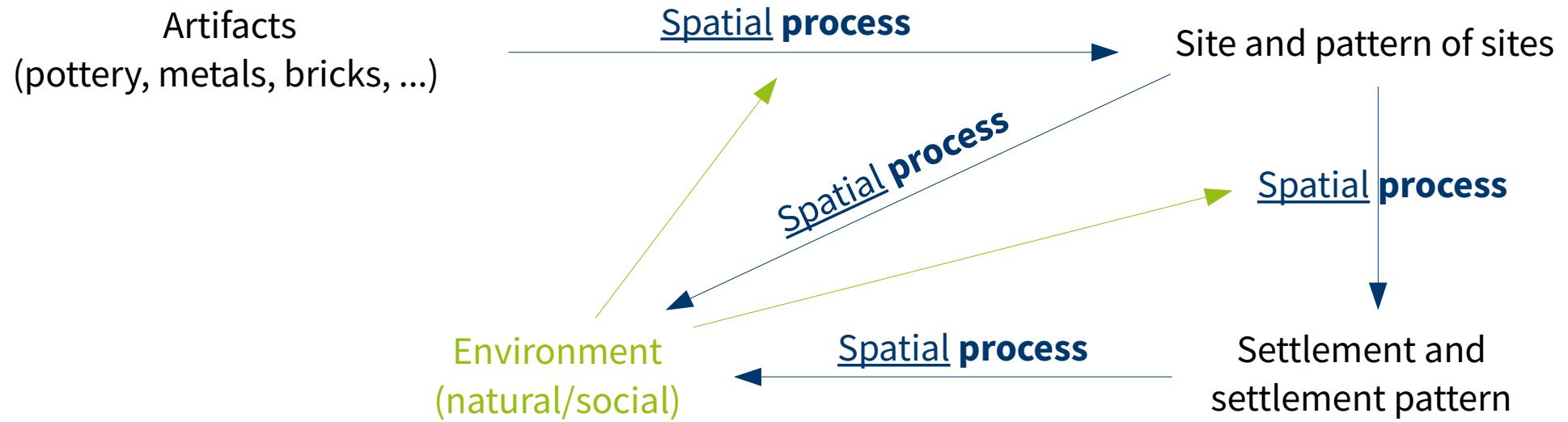
Modeling in Landscape Archaeology

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Modeling in Landscape Archaeology

- Spatial phenomena are the result of processes
- Modeling = (re-)construction of these processes



Modeling in Landscape Archaeology



Modeling in Landscape Archaeology

Modeling as a recursive activity.



Content

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Spatial data are special

Pitfalls of spatial data:

- spatial autocorrelation
- modifiable areal unit problem
- scale
- ecological fallacy
- non-uniformity of space
- edge effects

Spatial autocorrelation

The Earth is not an isotropic plate

Spatial data are not random

Data from locations near to each other are usually more similar than data far away from each other

Space and location are important because of Spatial autocorrelation.

Without spatial autocorrelation, spatial analyses would be pointless

Spatial autocorrelation



Low



High

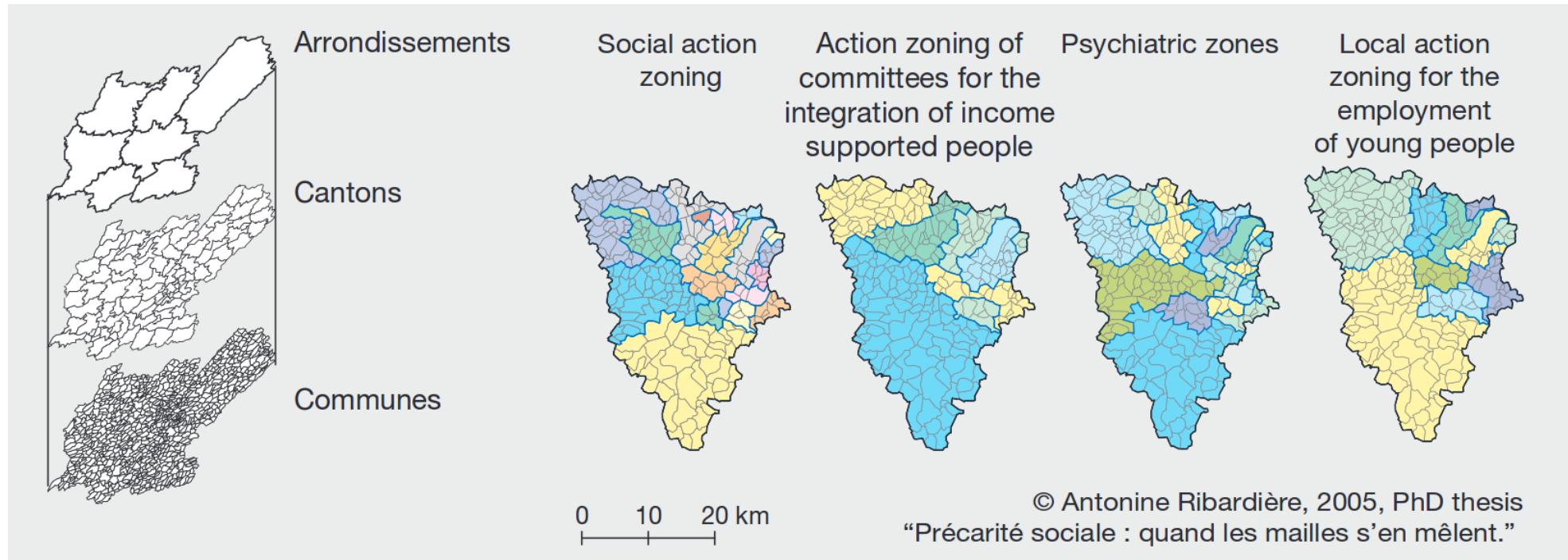


Maximum

Modifiable Areal Unit Problem (MAUP)

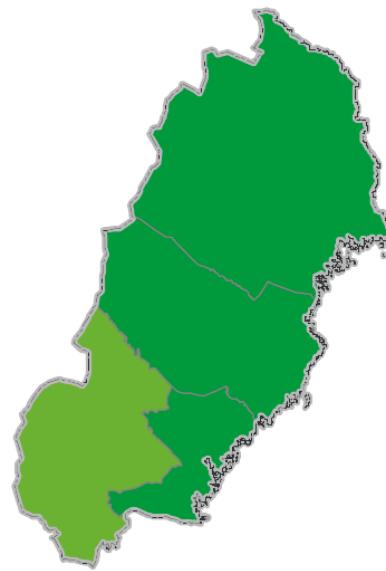
- aggregation units used are arbitrary with respect to the phenomena under investigation
 - If spatial units are specified differently, one might get very different patterns
- Openshaw, Stan (1984): The modifiable areal unit problem

Modifiable Areal Unit Problem (MAUP)

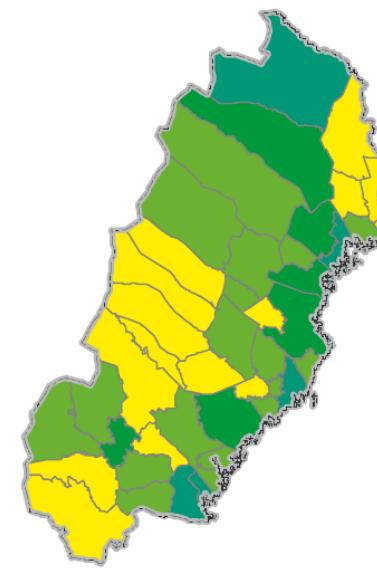


Modifiable Areal Unit Problem (MAUP)

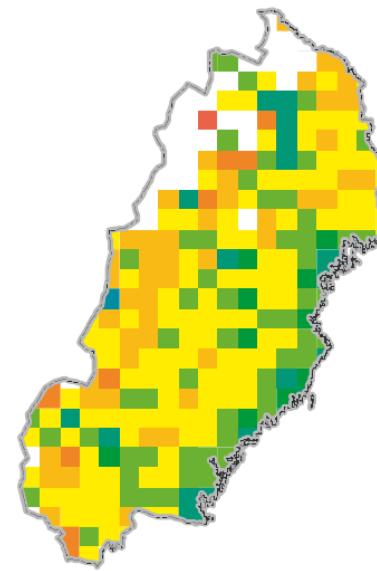
Provinzen (NUTS 3)



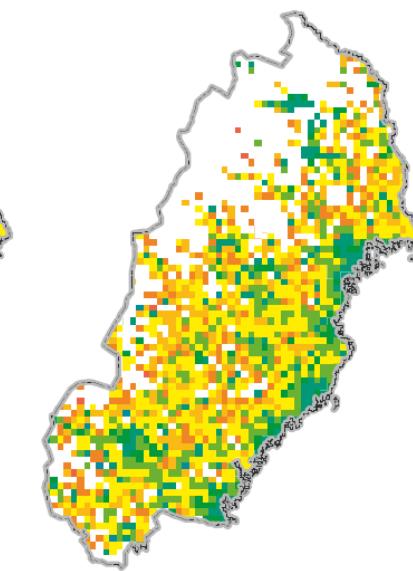
Gemeinden (NUTS 5)



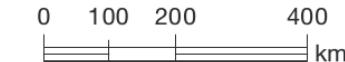
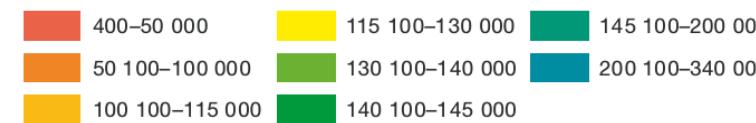
30 km-Raster



10 km-Raster

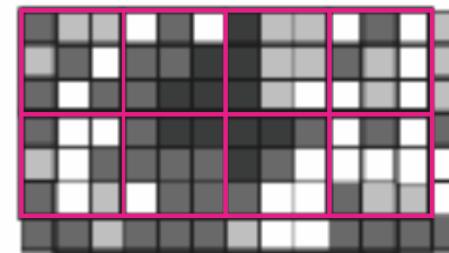
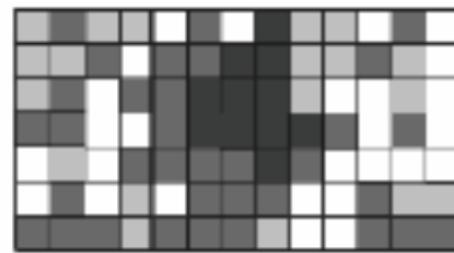


Verfügbares Einkommen
in schwed. Kronen je
Einwohner über 15 Jahre
2002



© M. Strömgren, K. Holme, E. Holm, S.M.C., Umeå University, Sweden

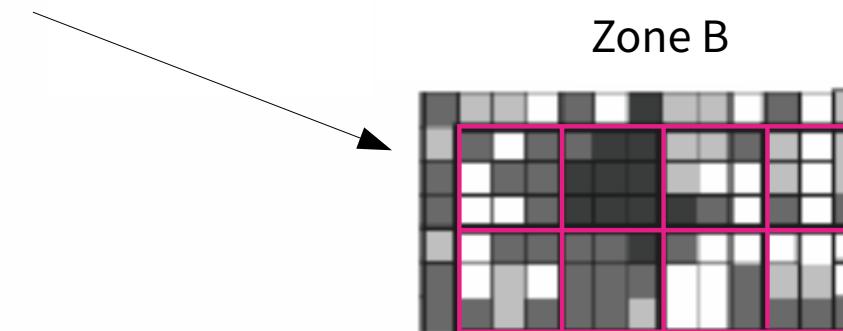
Modifiable Areal Unit Problem (MAUP)



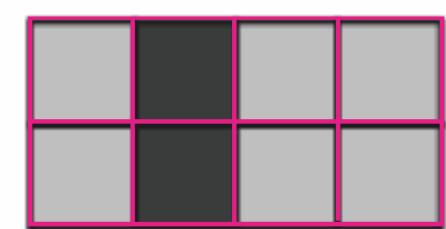
Zone A



Mean of zones



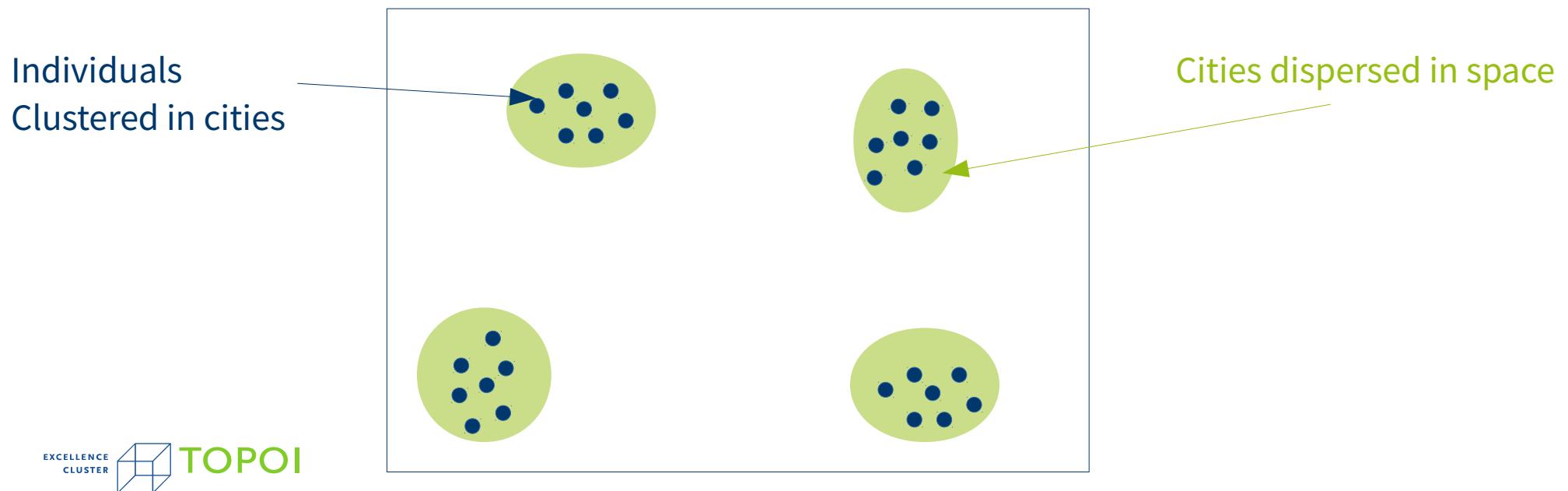
Zone B



Mean of zones

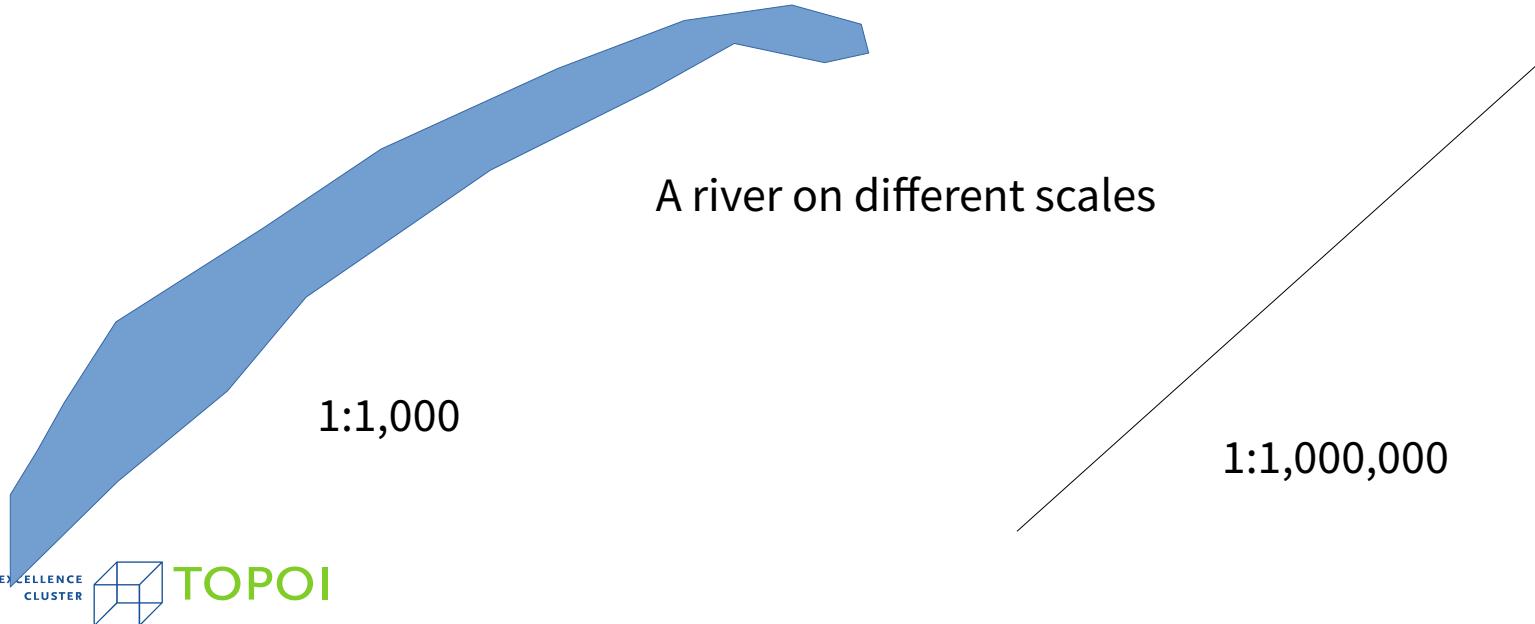
Scale effects

- Scale affects results and representativity of data
- e.g. cities may be represented as points or polygons
- results depend on the scale of analysis, e.g. province or county → MAUP



Scale effects

- Scale affects results and representativity of data
- e.g. cities may be represented as points or polygons
- results depend on the scale of analysis, e.g. province or county → MAUP



Ecological fallacy

Arises when:

- Statistical relationship at one level of aggregation...
- ...is assumed to hold true because it holds at a more detailed level

correlation IS NOT causation

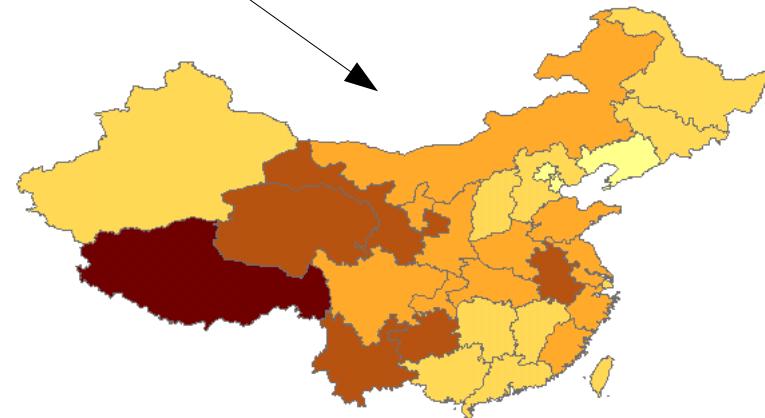
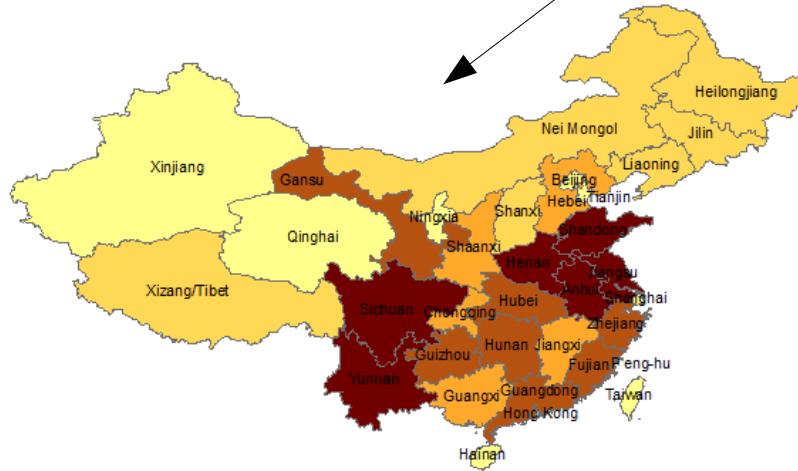
For example, we might observe a strong relationship between income and crime at the county level, with lower-income counties being associated with higher crime rates. If from this we conclude that lower-income individuals are more likely to commit a crime, then we are falling for the ecological fallacy. In fact, it is only valid to say exactly what the data say: that lower-income counties tend to experience higher crime rates. What causes the observed effect may be something entirely different

Non-uniformity of space

Bank robberies are clustered
→ because banks are clustered

Diseases due to bad air are clustered
→ because factories are clustered

Illiteracy in China
absolute



Edge effects

- unless you study the entire world: Every study region has a boundary
- You do not have data outside your study region
- But: the “outside” data may/do affect the data of your study region (if there is spatial autocorrelation...)

Spatial data are special

Pitfalls of spatial data:

- spatial autocorrelation
- modifiable areal unit problem
- scale
- ecological fallacy
- non-uniformity of space
- edge effects

Potentials of spatial data:

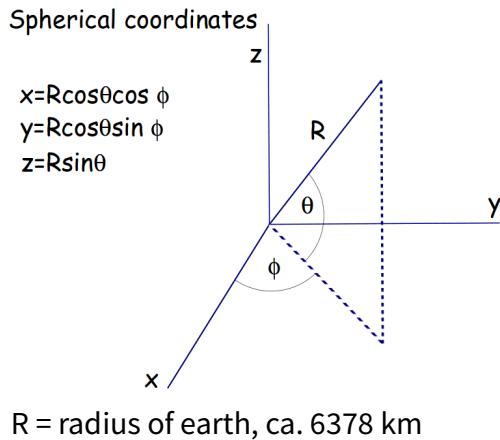
- distance
- adjacency
- interaction
- neighborhood

Distance

$$d_{ij} = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$$

Euclidean distance as calculated using
Pythagoras' formula

→ for *projected* data on the local/regional scale



Spherical distance via spherical coordinates
and a 3D version of *Pythagoras' formula*

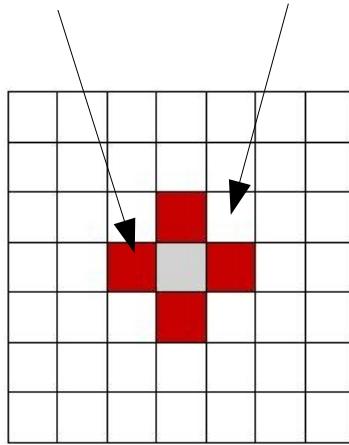
$$d^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2$$

→ for *unprojected* data on a global scale

Distance – Adjacency – Interaction - Neighborhood

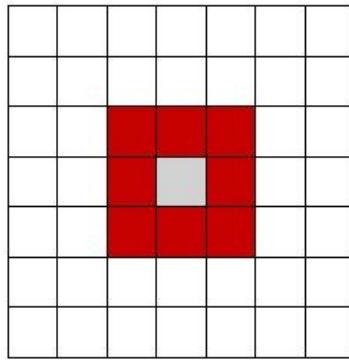
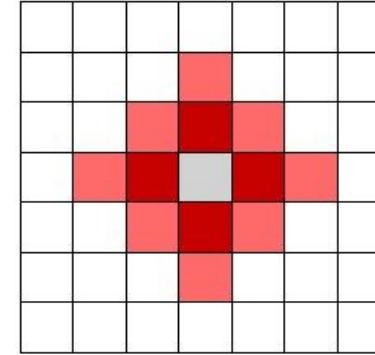
$$\mathbf{D} = \begin{bmatrix} 0 & 66 & 68 & 68 & 24 & 41 \\ 66 & 0 & 51 & 110 & 99 & 101 \\ 68 & 51 & 0 & 67 & 91 & 116 \\ 68 & 110 & 67 & 0 & 60 & 108 \\ 24 & 99 & 91 & 60 & 0 & 45 \\ 41 & 101 & 116 & 108 & 45 & 0 \end{bmatrix}$$

Binary
→ things are adjacent or not



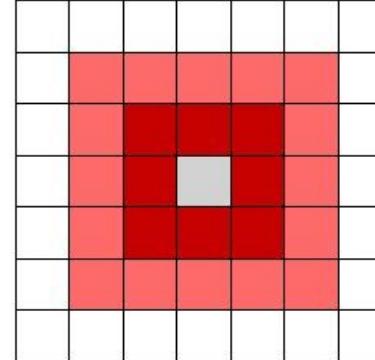
Adjacency

Rook case
→ sharing a boundary



1st order neighbor

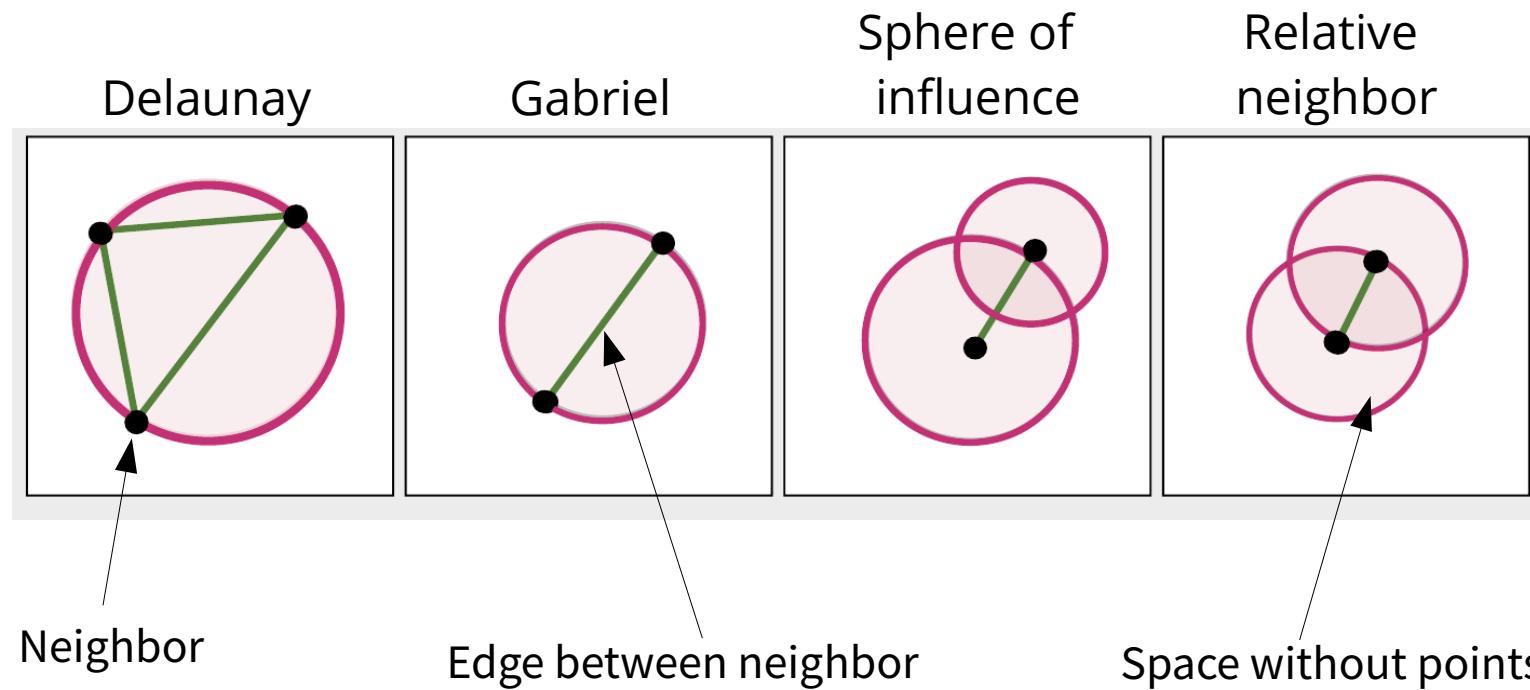
Queen case
→ sharing a boundary or point



2nd order neighbor

Adjacency

...or graph based neighbors.



Distance – Adjacency – Interaction - Neighborhood

$$\mathbf{A}_{k=3} = \begin{bmatrix} * & 1 & 0 & 0 & 1 & 1 \\ 1 & * & 1 & 0 & 1 & 0 \\ 1 & 1 & * & 1 & 0 & 0 \\ 1 & 0 & 1 & * & 1 & 0 \\ 1 & 0 & 0 & 1 & * & 1 \\ 1 & 1 & 0 & 0 & 1 & * \end{bmatrix}$$

$$\mathbf{A}_{d \leq 50} = \begin{bmatrix} * & 0 & 0 & 0 & 1 & 1 \\ 0 & * & 0 & 0 & 0 & 0 \\ 0 & 0 & * & 0 & 0 & 0 \\ 0 & 0 & 0 & * & 0 & 0 \\ 1 & 0 & 0 & 0 & * & 1 \\ 1 & 0 & 0 & 0 & 1 & * \end{bmatrix}$$

Interaction

- A combination of distance and adjacency
- related to Tobler's first law of geography:

“(...) everything is related to everything else, but near things are more related than distant things” (Tobler 1970, 236)

The diagram illustrates the formula for interaction weight w_{ij} . It shows the term $\propto \frac{1}{d^k}$ with three arrows pointing to its components: "interaction weight between i and j" points to the w_{ij} term; "rate of decline" points to the exponent k ; and "distance between i and j" points to the denominator d .

$$w_{ij} \propto \frac{1}{d^k}$$

...strength of interaction between i and j is proportional to their inverse distance

Distance – Adjacency – Interaction - Neighborhood

row totals:

$$\mathbf{W} = \begin{bmatrix} \infty & 0.0152 & 0.0147 & 0.0147 & 0.0417 & 0.0244 \\ 0.0152 & \infty & 0.0196 & 0.0091 & 0.0101 & 0.0099 \\ 0.0147 & 0.0196 & \infty & 0.0149 & 0.0110 & 0.0086 \\ 0.0147 & 0.0091 & 0.0149 & \infty & 0.0167 & 0.0093 \\ 0.0417 & 0.0101 & 0.0110 & 0.0167 & \infty & 0.0222 \\ 0.0244 & 0.0099 & 0.0086 & 0.0093 & 0.0222 & \infty \end{bmatrix} \begin{bmatrix} 0.1106 \\ 0.0639 \\ 0.0688 \\ 0.0646 \\ 0.1016 \\ 0.0744 \end{bmatrix}$$

$\mathbf{W}[1,2] = \mathbf{W}[1,] / \text{sum}(\mathbf{W}[1,])$

...

$$\mathbf{W} = \begin{bmatrix} \infty & 0.1370 & 0.1329 & 0.1329 & 0.3767 & 0.2205 \\ 0.2373 & \infty & 0.3071 & 0.1424 & 0.1582 & 0.1551 \\ 0.2136 & 0.2848 & \infty & 0.2168 & 0.1596 & 0.1252 \\ 0.2275 & 0.1406 & 0.2309 & \infty & 0.2578 & 0.1432 \\ 0.4099 & 0.0994 & 0.1081 & 0.1640 & \infty & 0.2186 \\ 0.3279 & 0.1331 & 0.1159 & 0.1245 & 0.2987 & \infty \end{bmatrix}$$

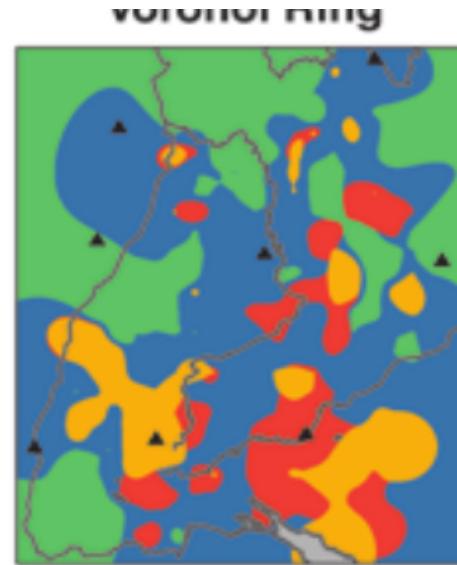
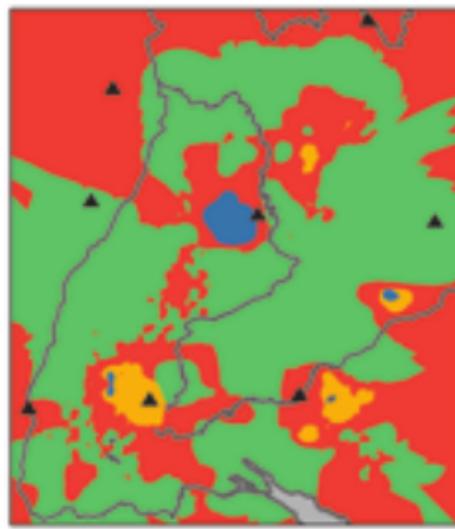
column totals:

1.4161	0.7949	0.8949	0.7805	1.2510	0.8626
--------	--------	--------	--------	--------	--------

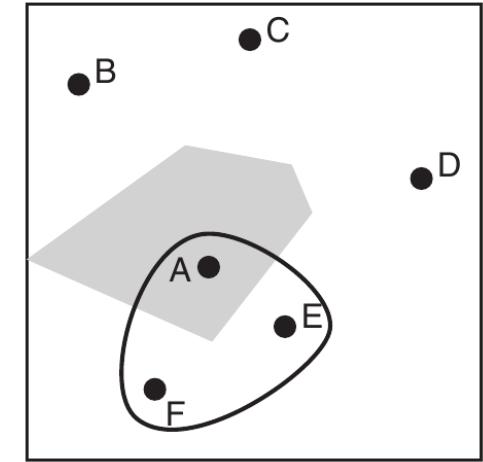
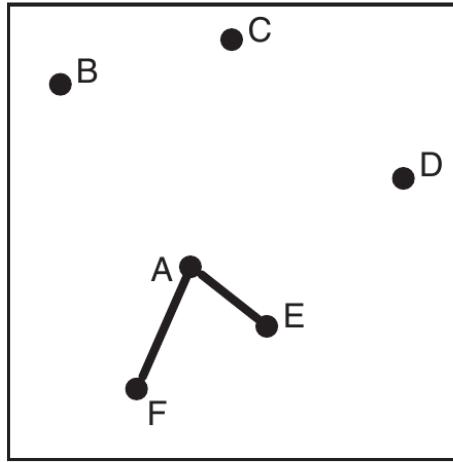
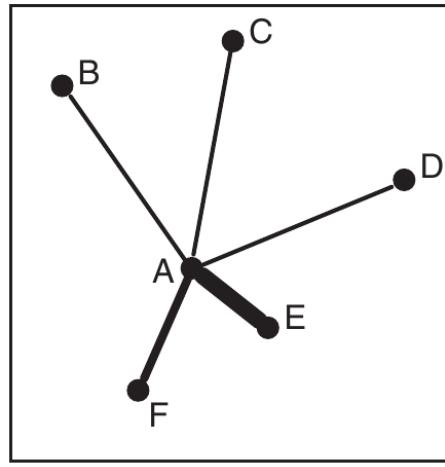
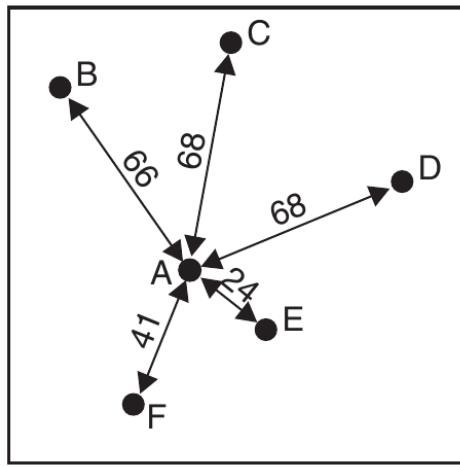
Neighborhood

Neighborhood of X is:

- the set of adjacent cells/areas
- the set of points/cells/areas within a certain distance
- the set of points/cells/areas that share some specific attribute or that are alike



Distance – Adjacency – Interaction - Neighborhood



Spatial data are special

Pitfalls of spatial data:

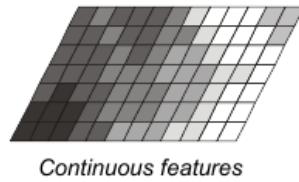
- spatial autocorrelation
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- non-uniformity of space
- edge effects

Potentials of spatial data:

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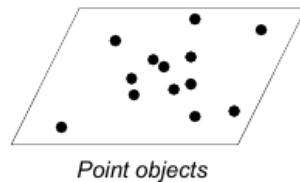
...it's all about processes

GEOSTATISTICS



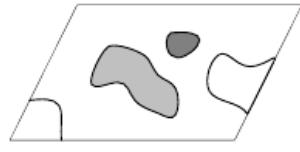
Continuous features

POINT PATTERN ANALYSIS



Point objects

LATTICE STATISTICS



Areal objects (polygons)

However you call it and focus on...

everything is about processes...

Because they cause spatial patterning, autocorrelation, ...

Fig. 1.2: Spatial statistics and its three major subfields after Cressie (1993).

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- Modeling and processes
- Why space matters: Potentials and Pitfalls of Spatial Data
- **Point Pattern Analyses: What processes might have caused the distribution of findings?**

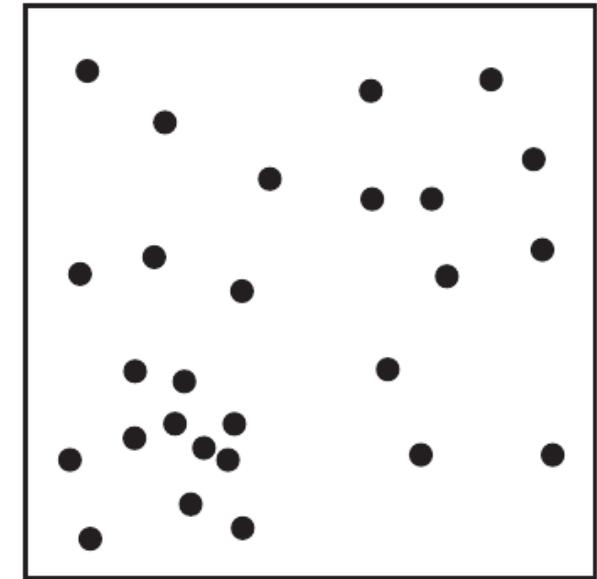
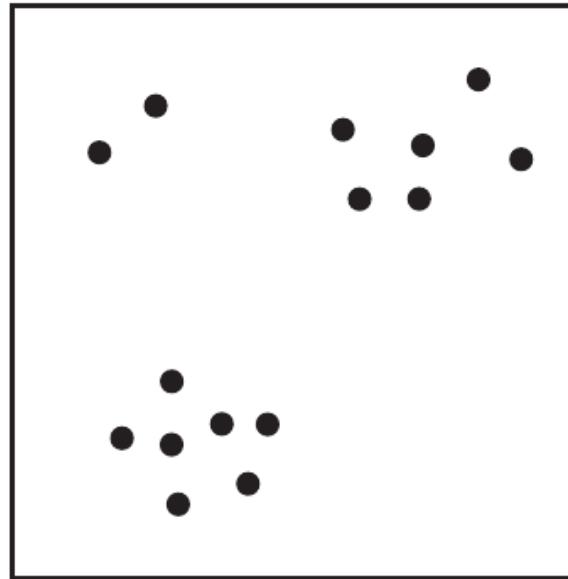
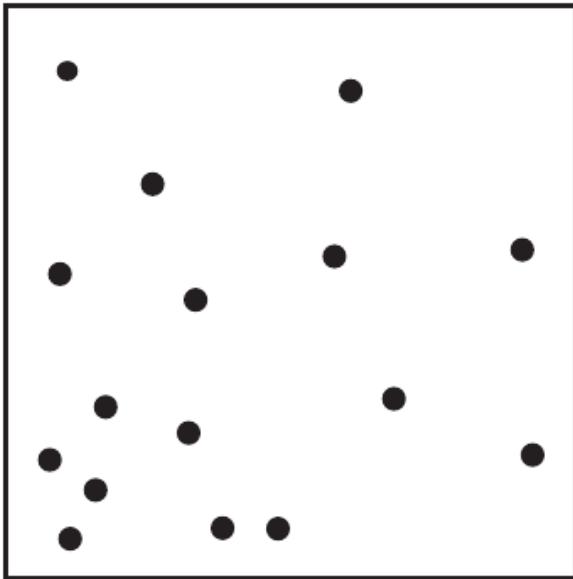
First order processes (density based approaches)

Second order processes (distance based approaches)

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- Geomorphometry: What is the character of the landscape?
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Point Pattern

What caused these patterns? First- or Second order effects?

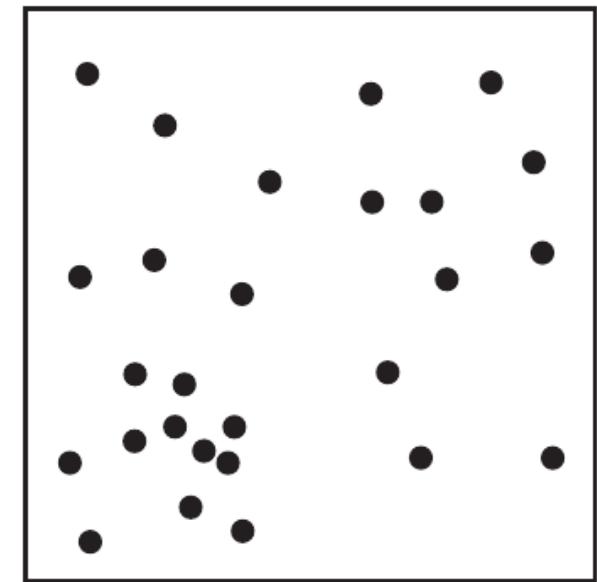
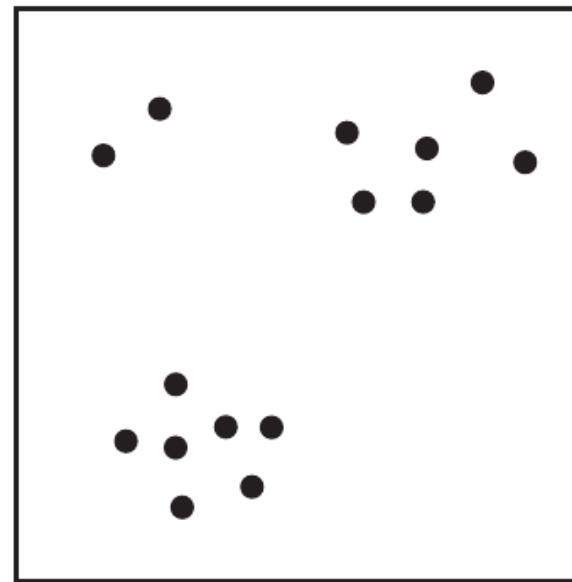
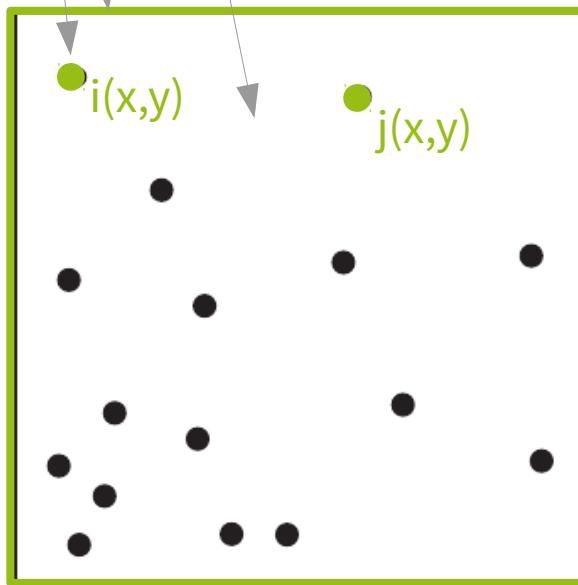


Point pattern analysis aims to distinguish between both effects
– helping you to understand the genuine process creating the pattern –

Point Pattern

region
event pattern

What caused these patterns? First- or Second order effects?

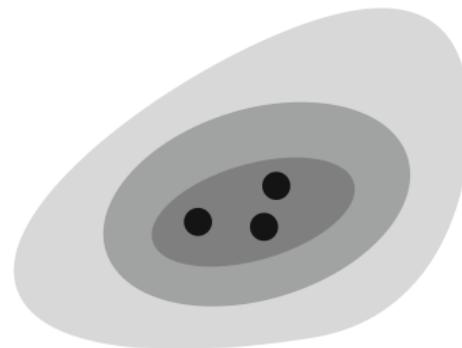


Point pattern analysis aims to distinguish between both effects
– helping you to understand the genuine process creating the pattern –

Point Pattern

What caused these patterns? First- or Second order effects?

e.g. mining sites
and resources

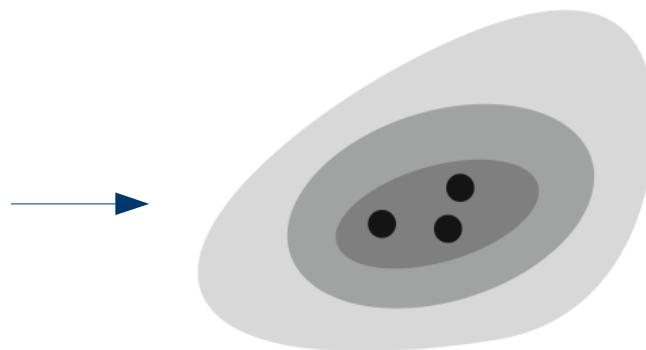


First order property:
location depends on an
spatial parameter

Point Pattern

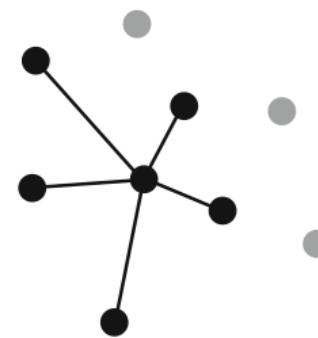
What caused these patterns? First- or Second order effects?

e.g. mining sites
and resources



First order property:
location depends on an
spatial parameter

e.g. graveyard
and settlement



Second order property:
location depends on
the relationship to
other points

Point Pattern

Simple measures:

- mean center
- standard distance
- intensity of a pattern

$$\bar{\mathbf{s}} = (\mu_x, \mu_y) = \left(\frac{\sum_{i=1}^n x_i}{n}, \frac{\sum_{i=1}^n y_i}{n} \right)$$

$$d = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu_x)^2 + (y_i - \mu_y)^2}{n}}$$

$$\hat{\lambda} = \frac{n}{a} = \frac{\#(S \in A)}{a}$$

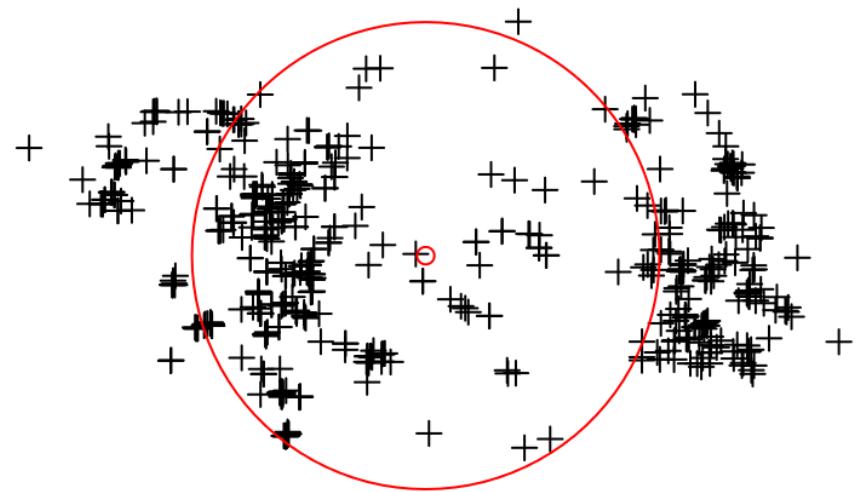
Area of study region

Number of events in the pattern found in study region

Point Pattern

Simple measures:

- mean center
- standard distance
- intensity of a pattern



0.015 sites/sqkm

Sensitive...what is the area?

Point Pattern – first order effects

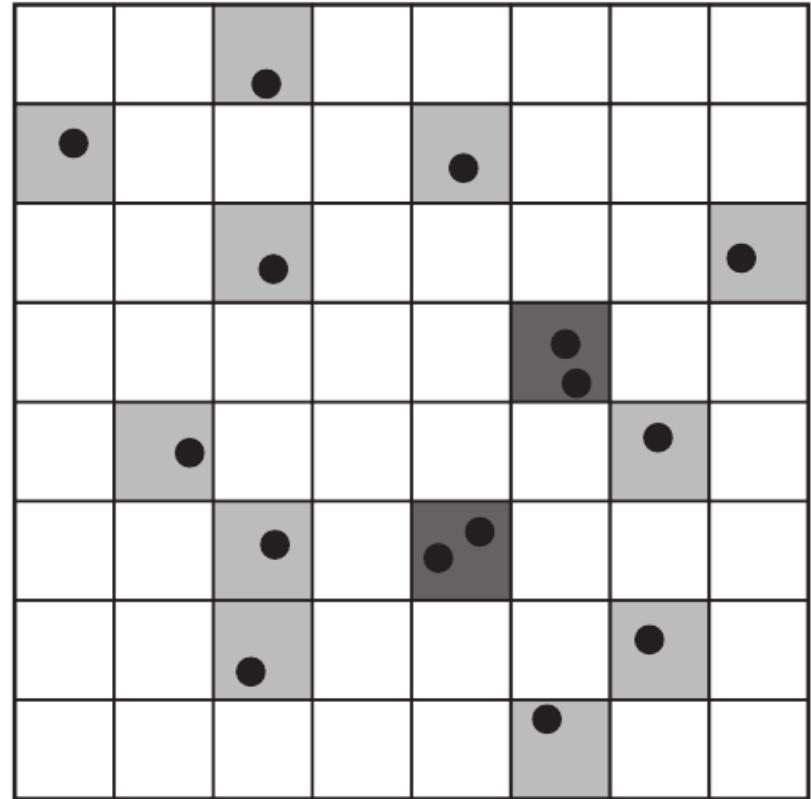
Intensity – more advanced

Independent Random Process (IRP)

= Complete Spatial Randomness (CSR)

- any event has equal probability to be located in a quadrant
- the occurrence of points is independent of the Positioning of other events

$$P(\text{event in a quadrant}) = 1/64$$



Point Pattern – first order effects

Intensity – more advanced

Independent Random Process (IRP)

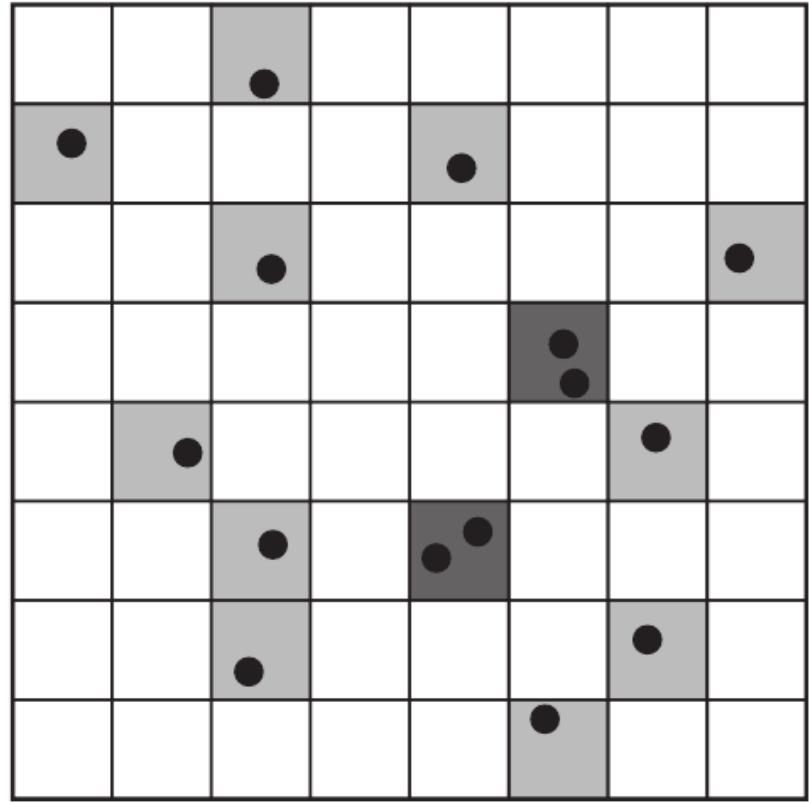
= Complete Spatial Randomness (CSR)

Probability of k events in a quadrant is calculated with Poisson distribution

$$P(k) = \frac{\lambda^k e^{-\lambda}}{k!}$$

intensity

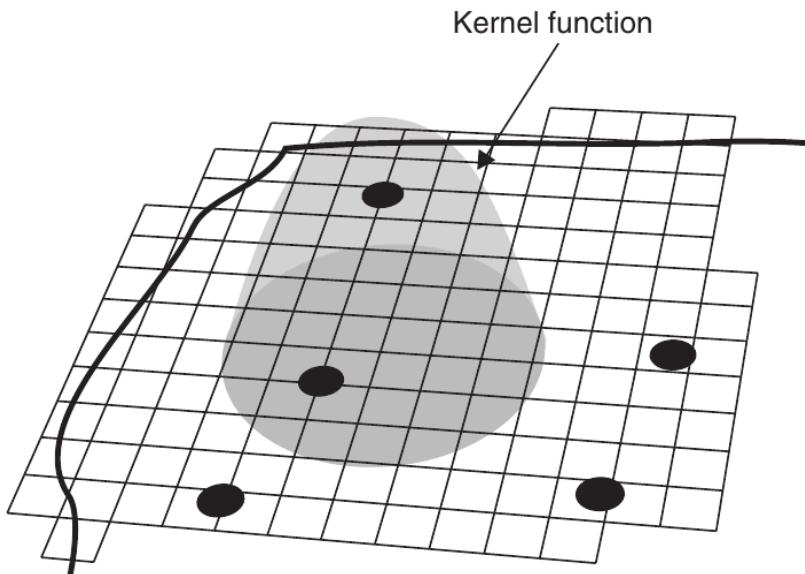
Base of natural logarithm (2.78...)



Point Pattern – first order effects

Intensity – more advanced

Kernel density estimation (KDE)



Edge correction

$$\hat{\lambda}_p = e(p) \sum_i k(x_i - p)$$

(Gaussian) Kernel function

$$\frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

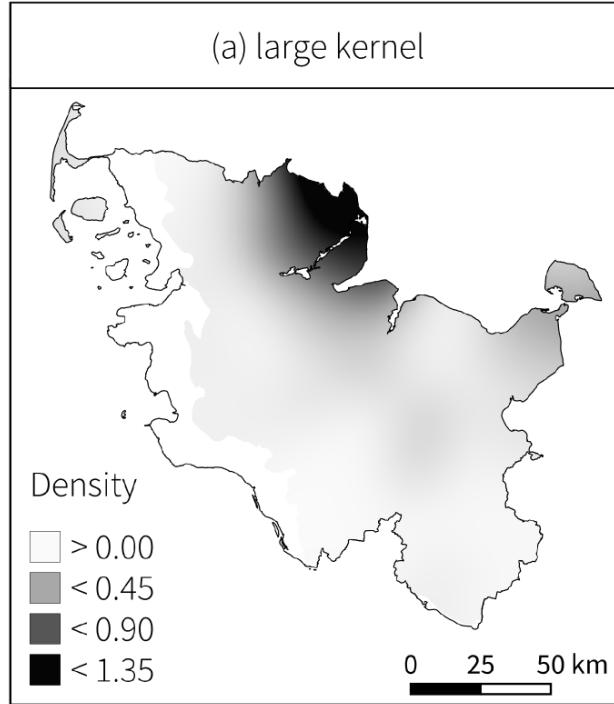
Standard deviation

kernel location

Point Pattern – first order effects

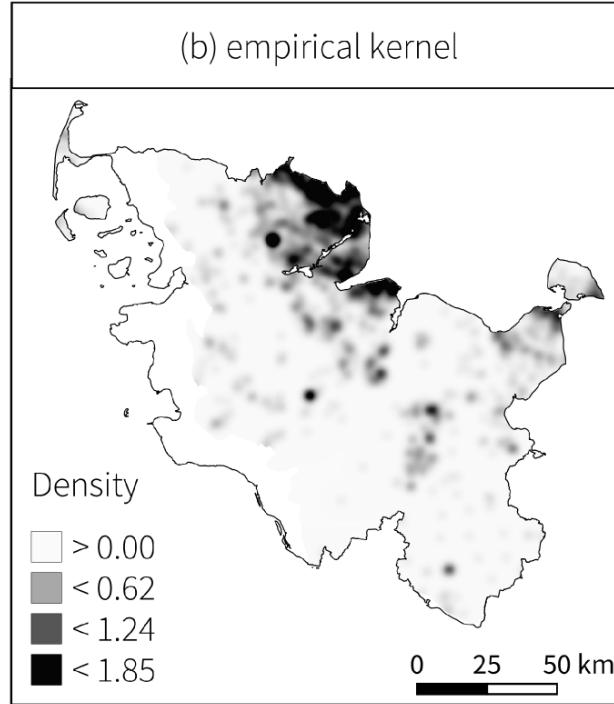
Sigma large

(a) large kernel



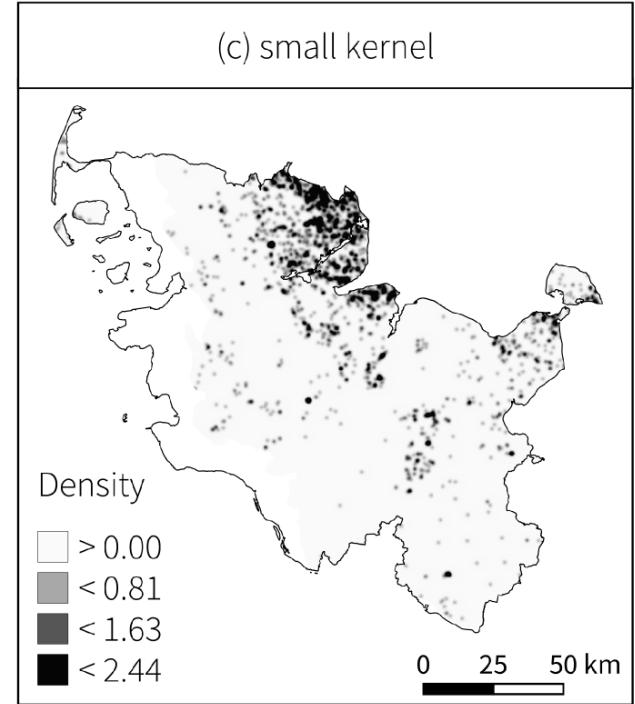
General trend

(b) empirical kernel



Sigma small

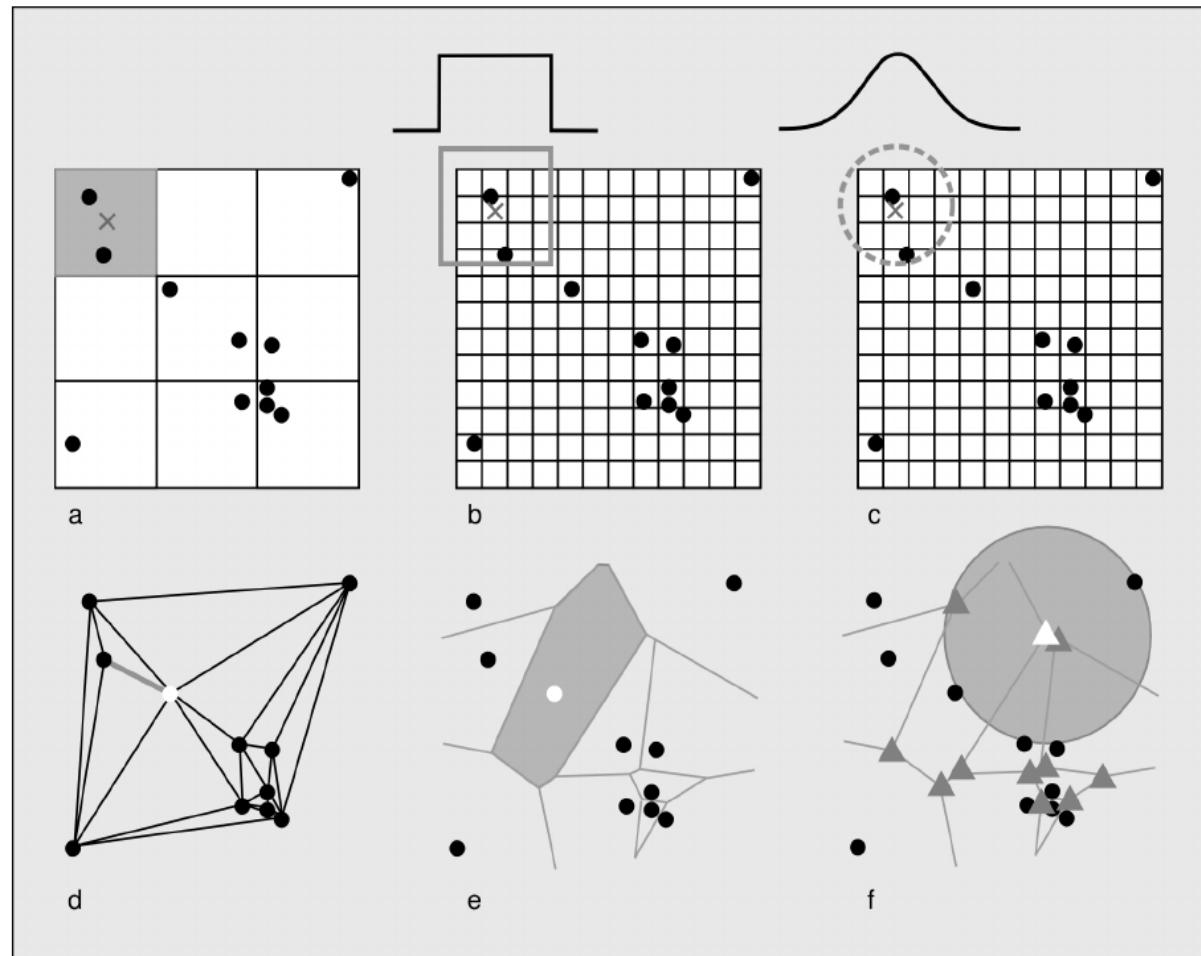
(c) small kernel



Local trend

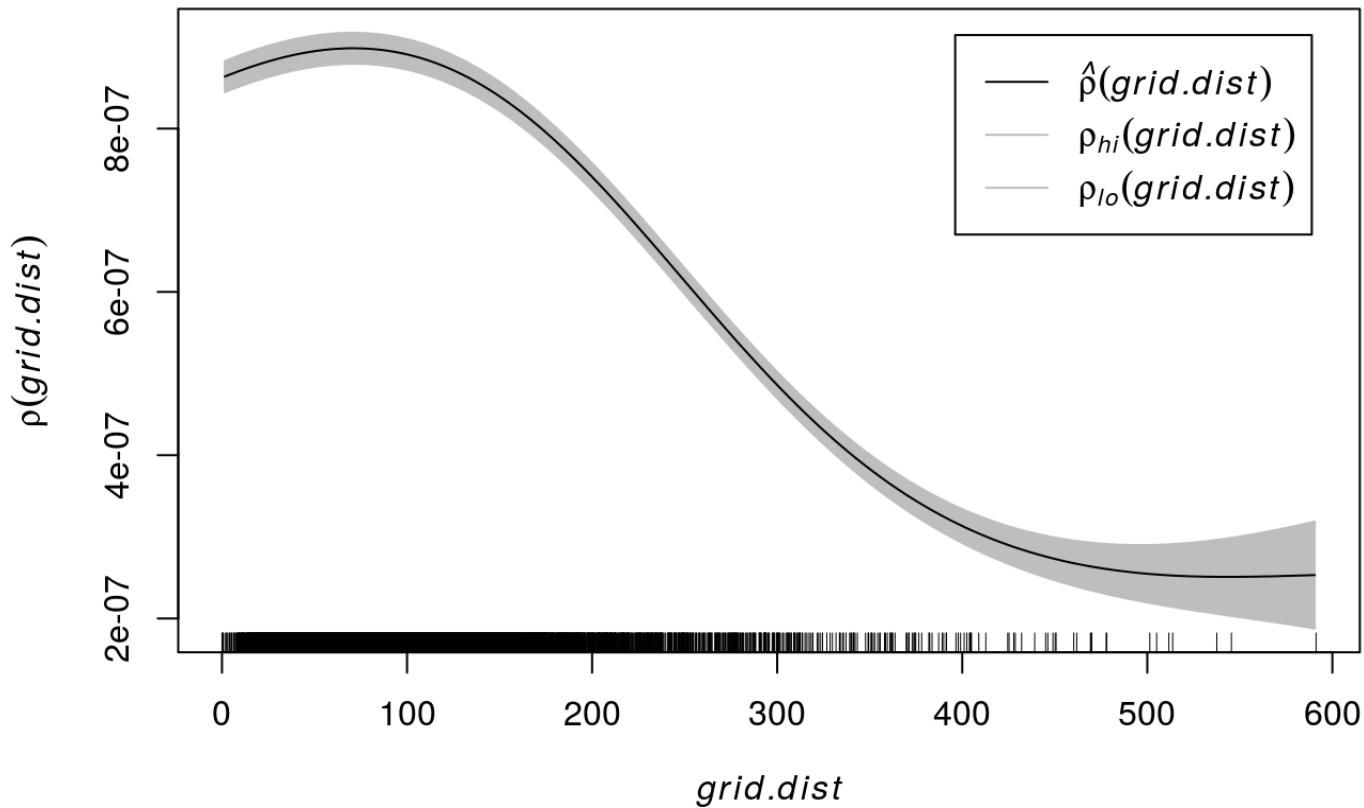
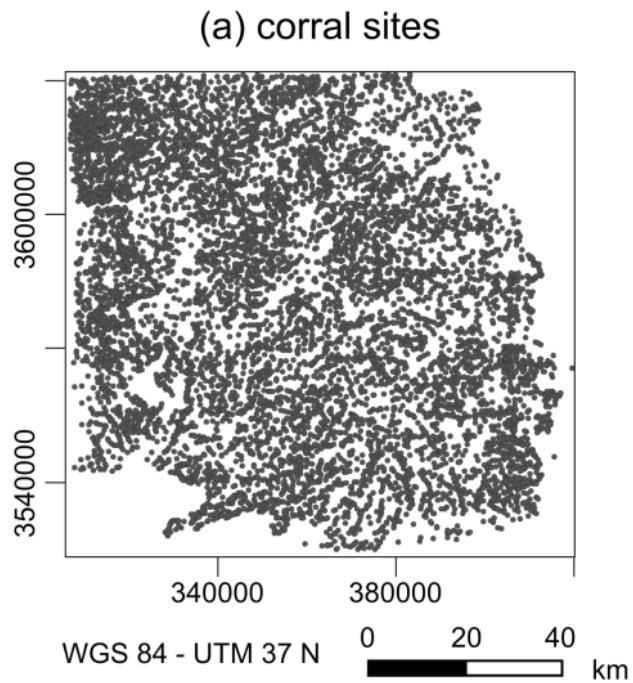
Point Pattern – first order effects

Intensity – possibilities to calculate



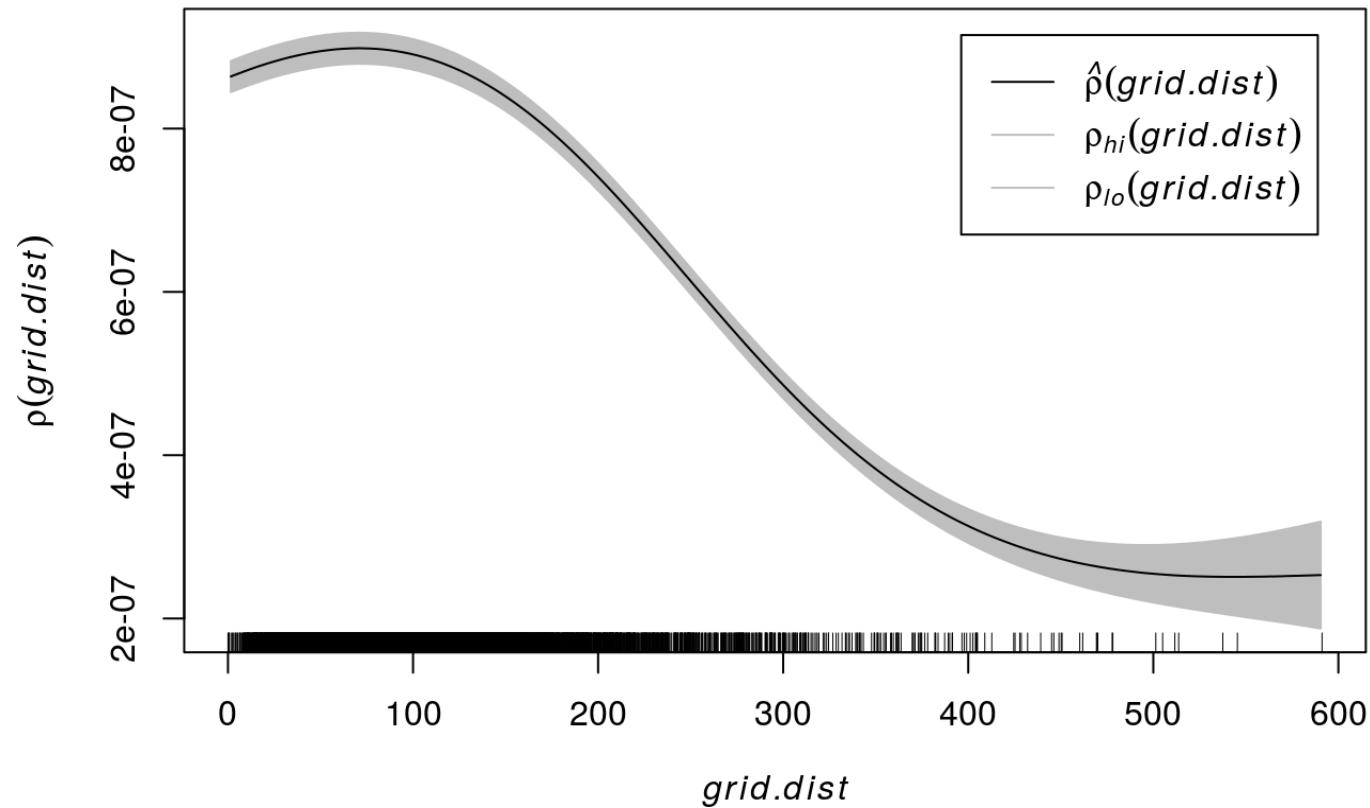
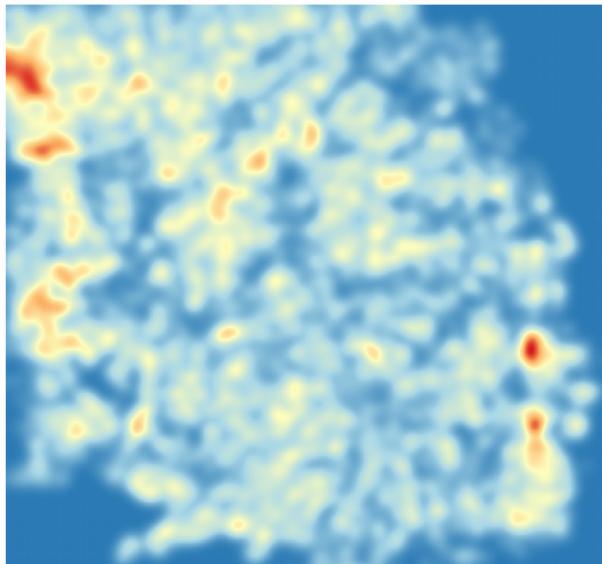
Point Pattern – first order effects

Intensity as tool to investigate dependence on covariates



Point Pattern – first order effects

Intensity as tool to investigate dependence on covariates



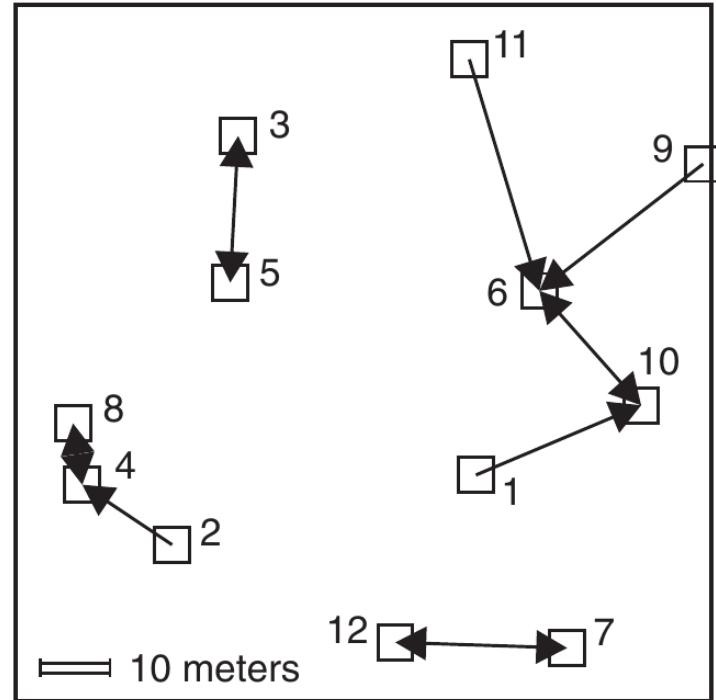
Point Pattern – second order effects

Point Pattern – second order effects

Point patterns described by distance measures

- nearest-neighbor distance → euclidean distance

mean nearest-neighbor distance



$$\bar{d}_{\min} = \frac{\sum_{i=1}^n d_{\min}(\mathbf{s}_i)}{n}$$

Are the points clustered or dispersed?

Use Clark and Evan's R statistic of nearest neighbor distances

$$R = \bar{d}_{\min} / \frac{1}{(2\sqrt{\lambda})}$$

expected
nearest-neighbor
distance

$R < 1$: more clustered

$R > 1$: more evenly spaced

(O'Sullivan & Unwin, 2010)

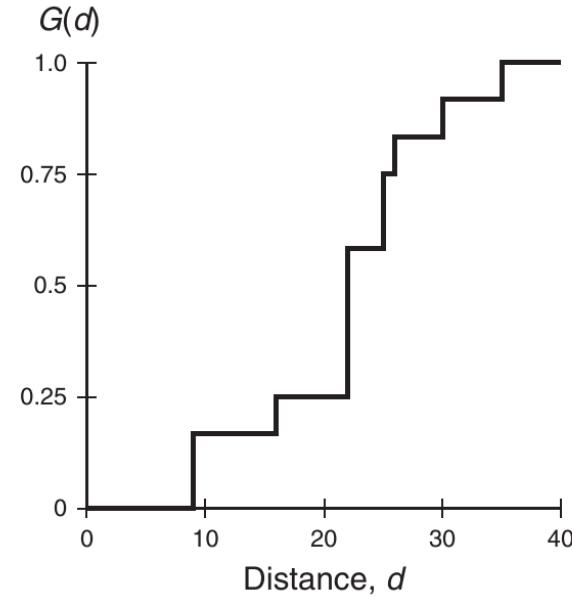
Point Pattern – second order effects

Point patterns described by distance measures

→ cumulative frequency distribution of the nearest-neighbor distances = $G(d)$

$$G(d) = \frac{\#(d_{\min}(\mathbf{s}_i) < d)}{n}$$

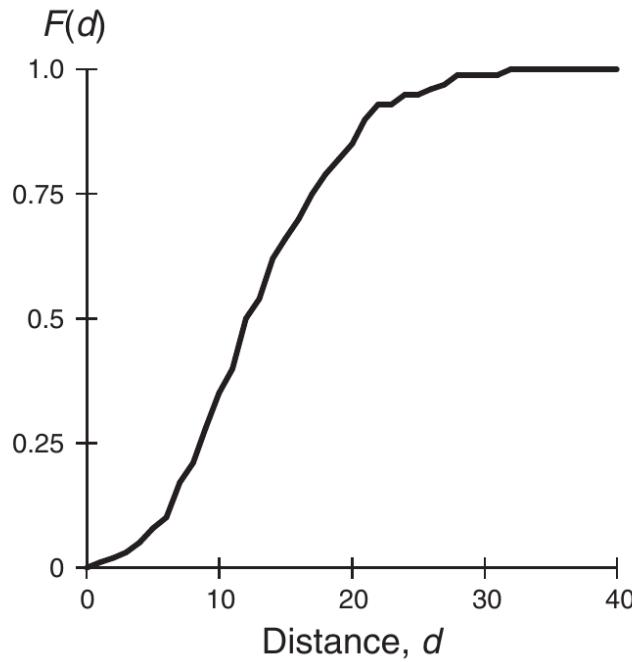
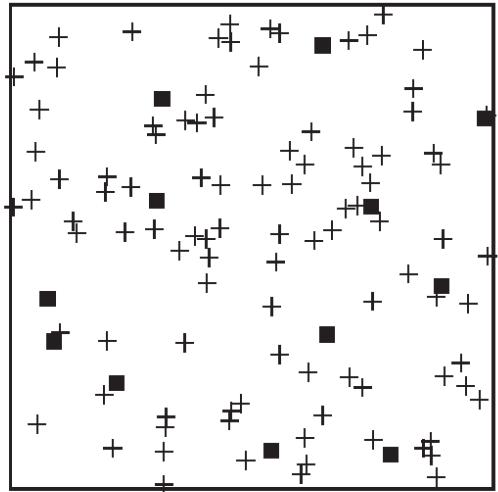
→ $G(d)$ tells us what fraction of all n-n distances is less than d



Point Pattern – second order effects

Point patterns described by distance measures

→ cumulative frequency distribution of the nearest-neighbor distances of *arbitrary events* to known events = $F(d)$



minimum distance from
random point \mathbf{p}_i to an event

$$F(d) = \frac{\#\{d_{\min}(\mathbf{p}_i, S) < d\}}{m}$$

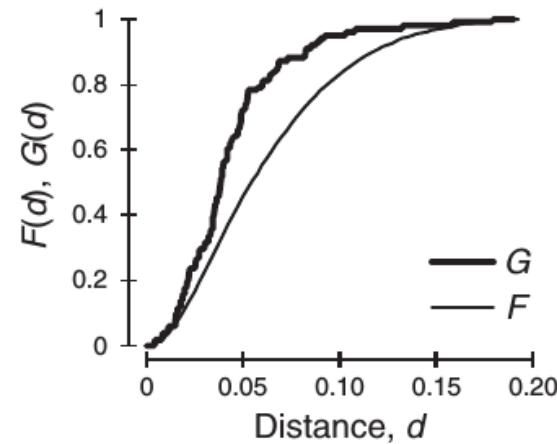
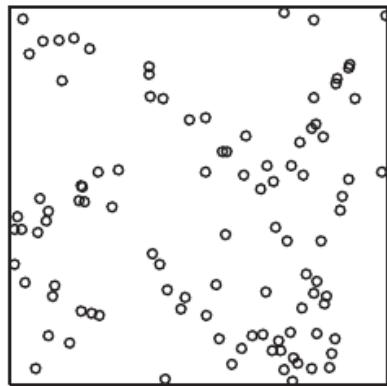
m

set of randomly
selected locations

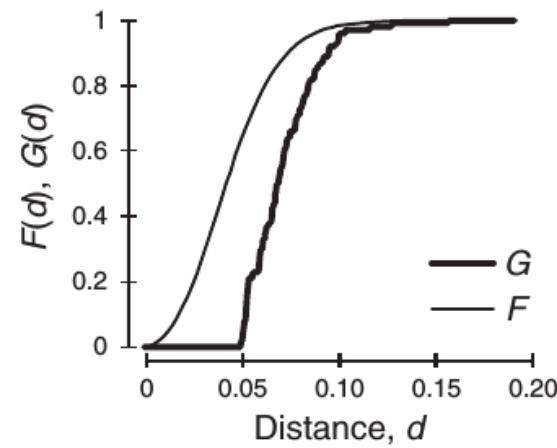
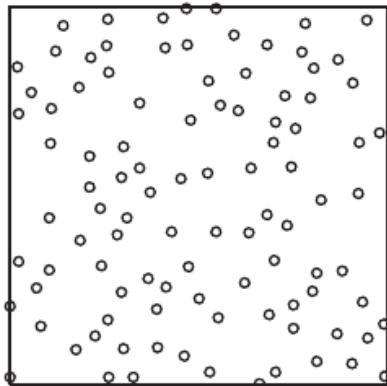
(O'Sullivan & Unwin, 2010)

Point Pattern – second order effects

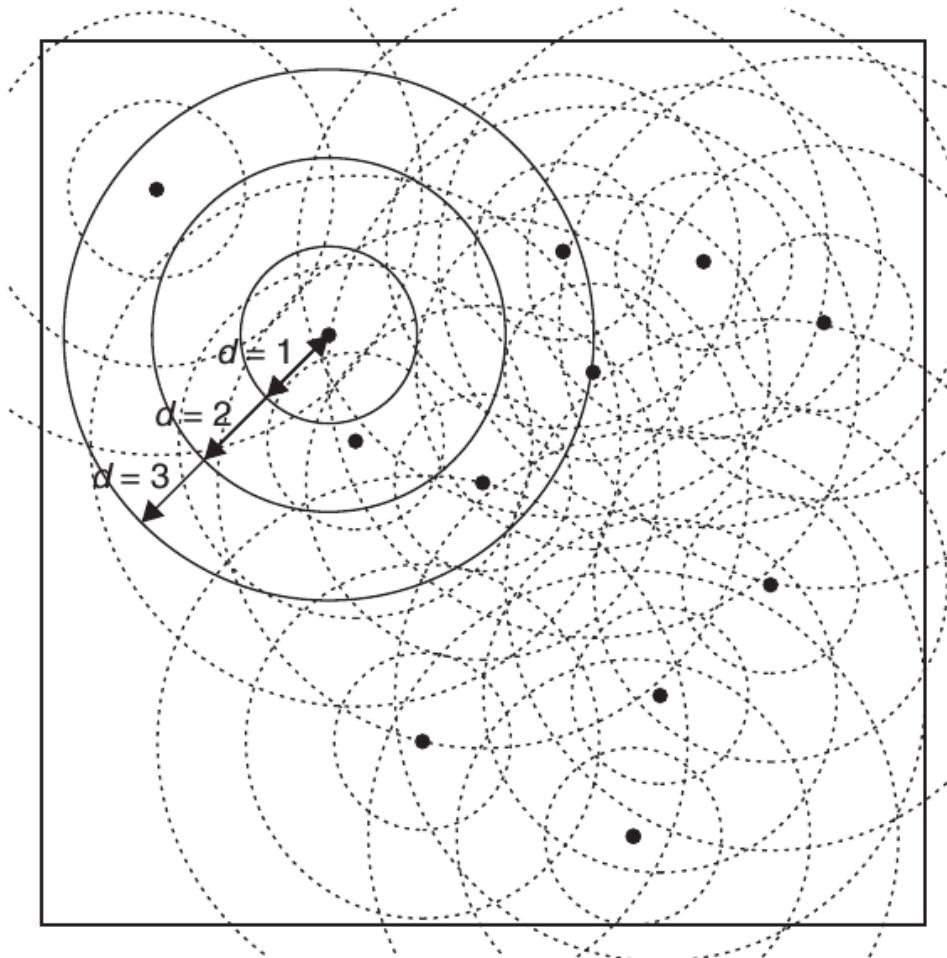
Clustered



Evenly spaced



Point Pattern – second order effects



To get rid of the nearest-neighbor limitation:
use the K Function

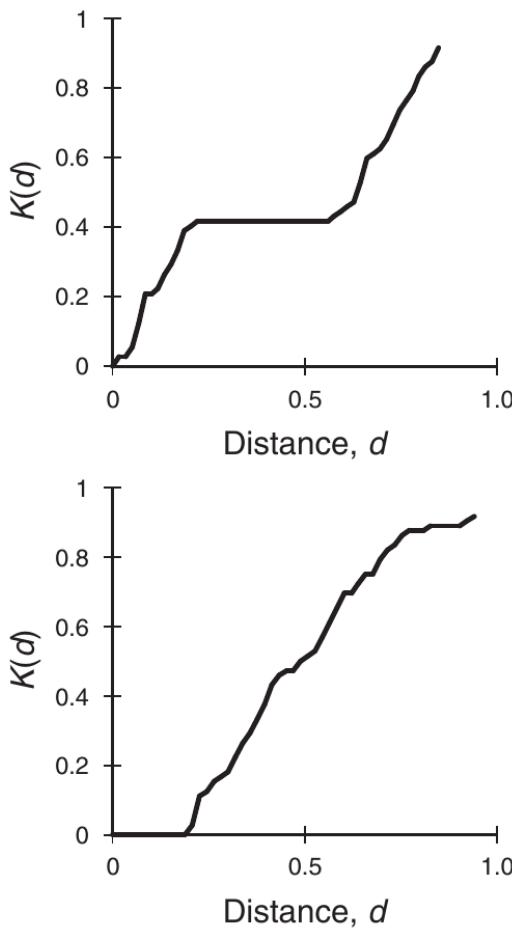
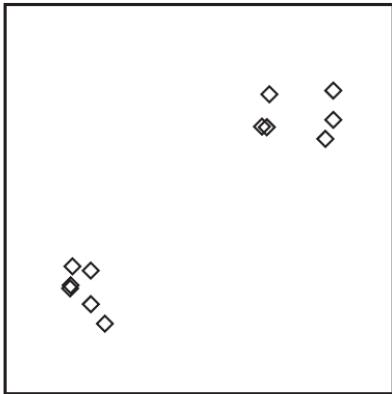
Events in circle radius d centered at s

$$K(d) = \frac{\sum_{i=1}^n \#[S \in C(\mathbf{s}_i, d)]}{n\lambda}$$

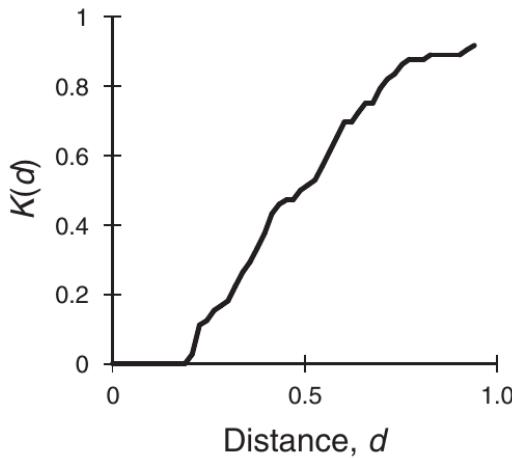
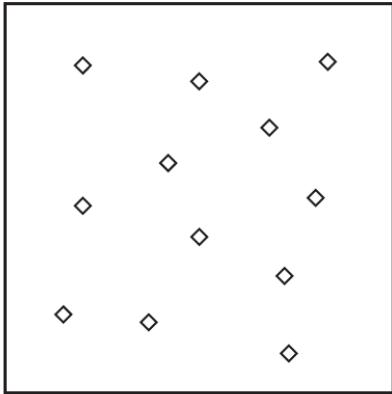
Event density in the study area/region

Point Pattern – second order effects

Clustered



Evenly spaced



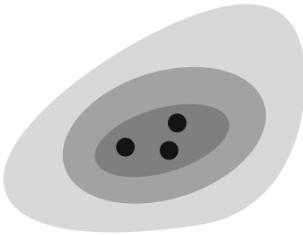
To get rid of the nearest-neighbor limitation:
use the K Function

Events in circle radius d centered at s

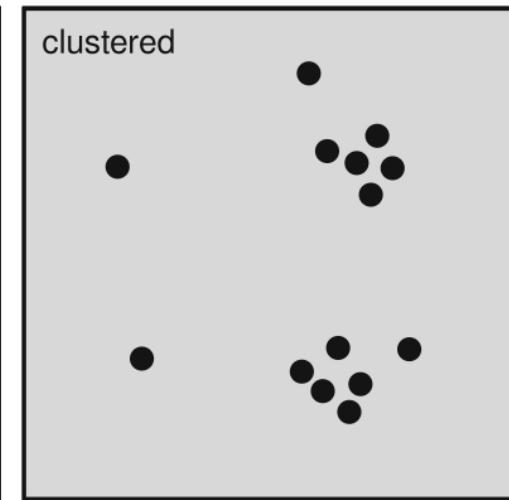
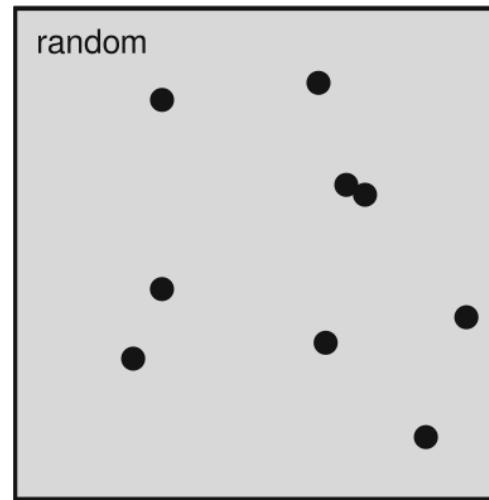
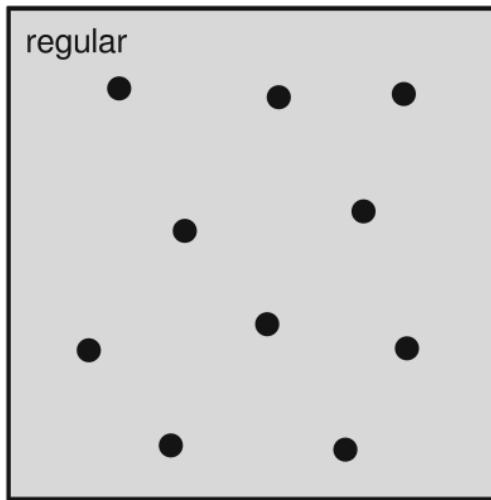
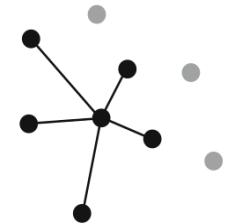
$$K(d) = \frac{\sum_{i=1}^n \# [S \in C(\mathbf{s}_i, d)]}{n\lambda}$$

Event density in the study area/region

Point Pattern Analyses



Help to distinguish between first and second order effects that caused your spatial pattern at hand
→ you gain insights in the underlying processes



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- Geomorphometry: What is the character of the landscape?
- Outlook

Interpolation

We start with points

But wait...

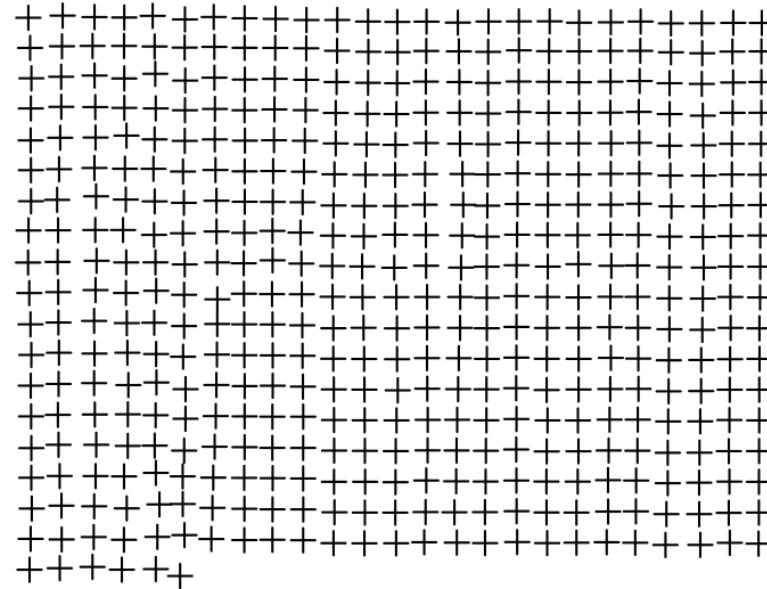
Why are the methods of point patterns not used??

Because *point data* is not necessarily a *point pattern*

e.g. sampling locations of soil samples to analyze phosphorous (=points) are *artificial* and irrelevant to the study of phosphorous distribution
→ such points do *not* reflect a process.

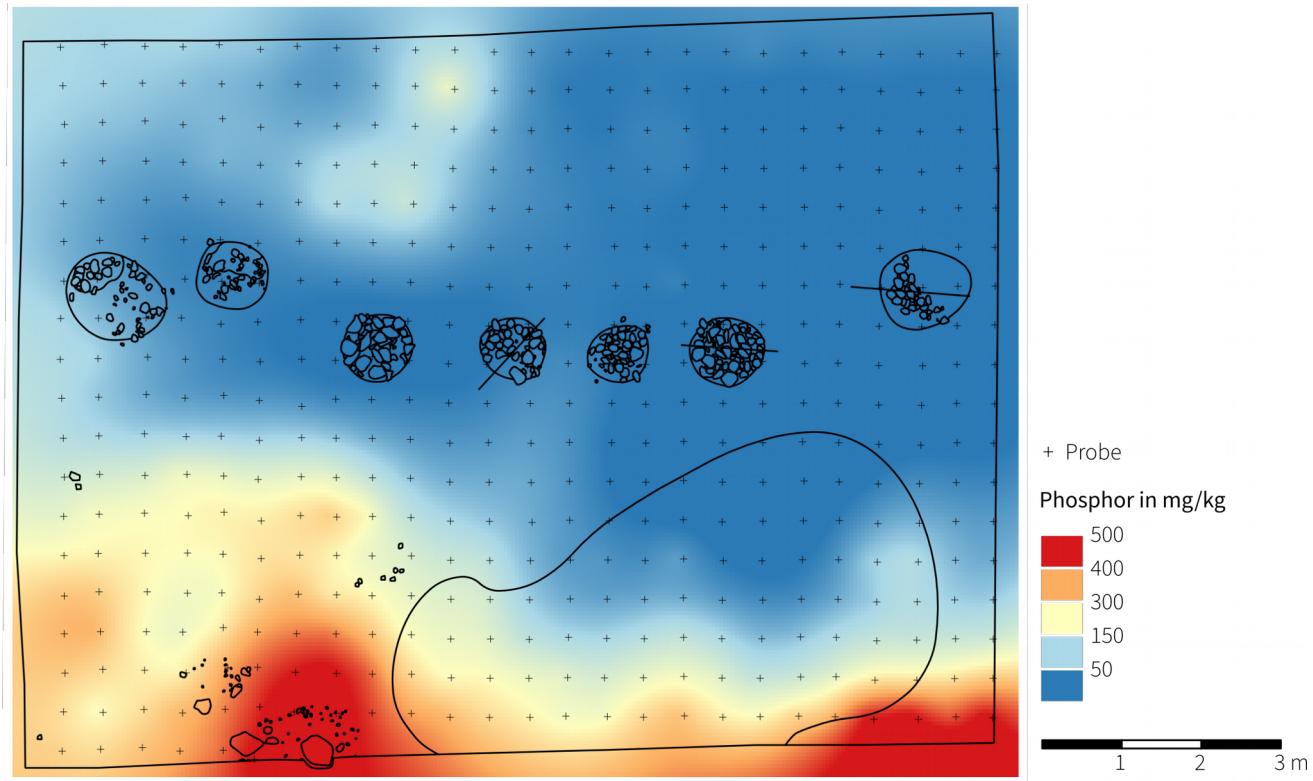
Interpolation

Aim: get a continuous representation of attribute information.



Interpolation

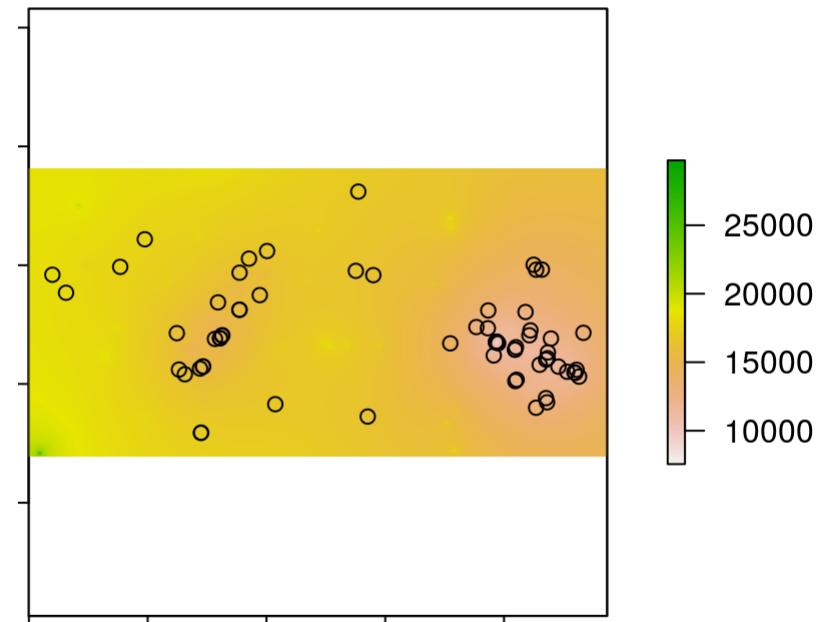
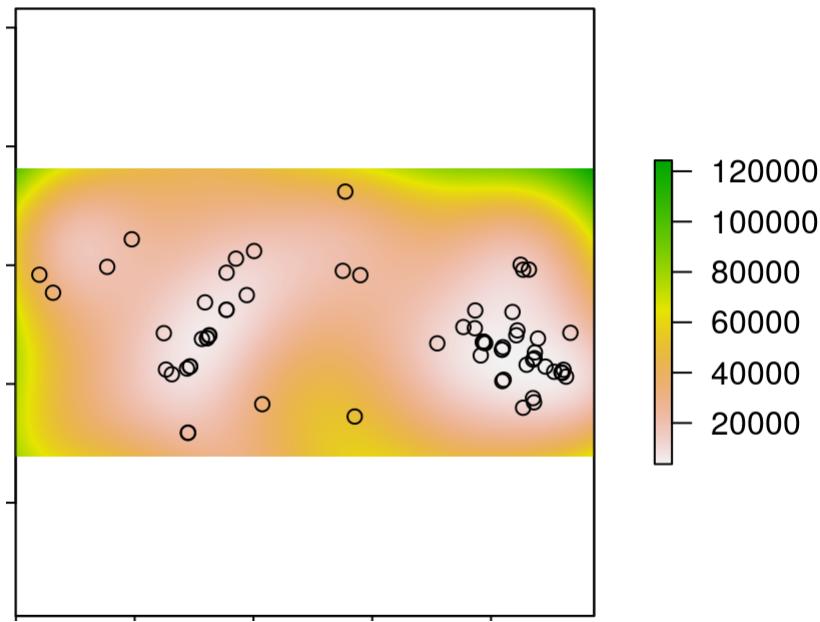
Aim: get a continuous representation of attribute information.



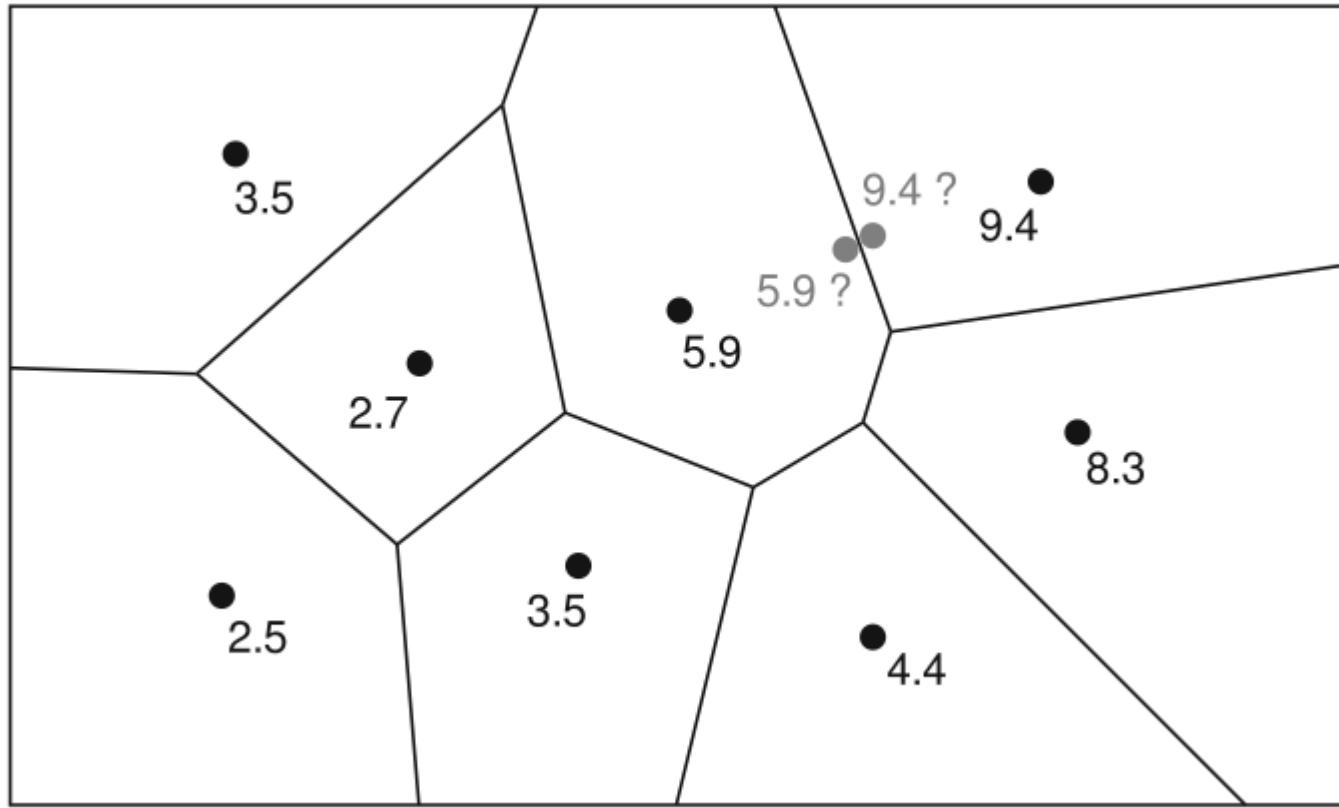
Interpolation

Aim: get a continuous representation of settlement density.

Mission accomplished...!?



Interpolation



Interpolation

Inverse Distance Weighting

$$\hat{z}_j = \sum_{i=1}^m w_{ij} z_i$$

Control points i in neighborhood m

Estimate at j

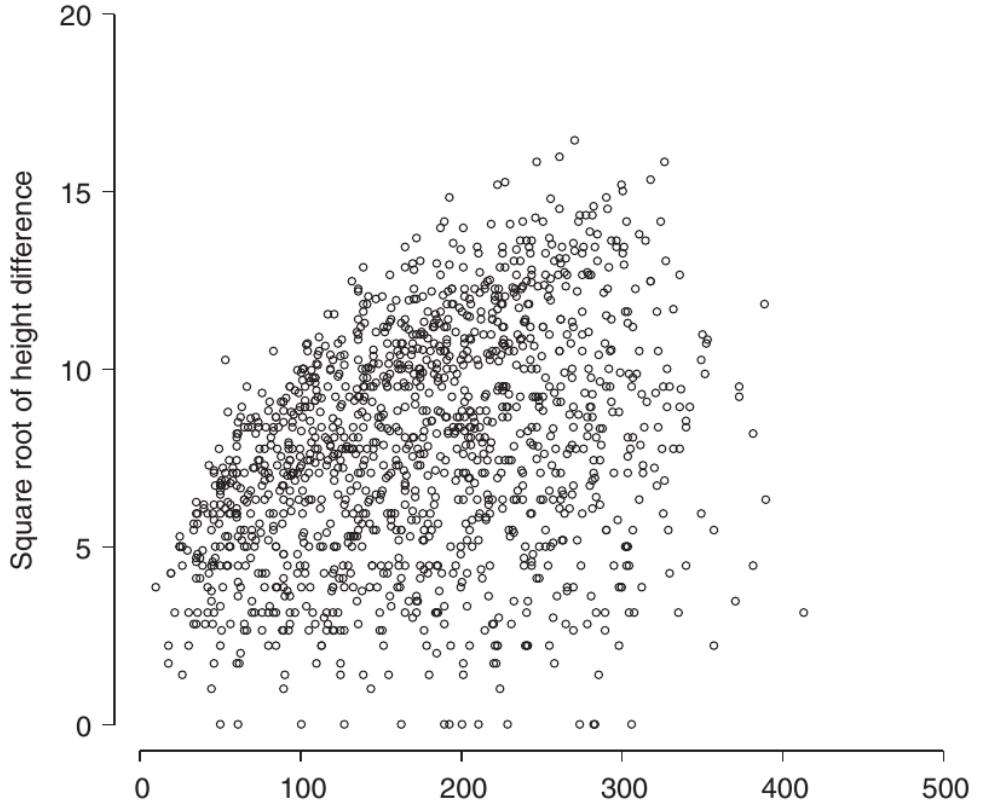
$$w_{ij} \propto \frac{1}{d_{ij}^k}$$

Kriging

Interpolation

Square root differences cloud

1. Describing spatial variation



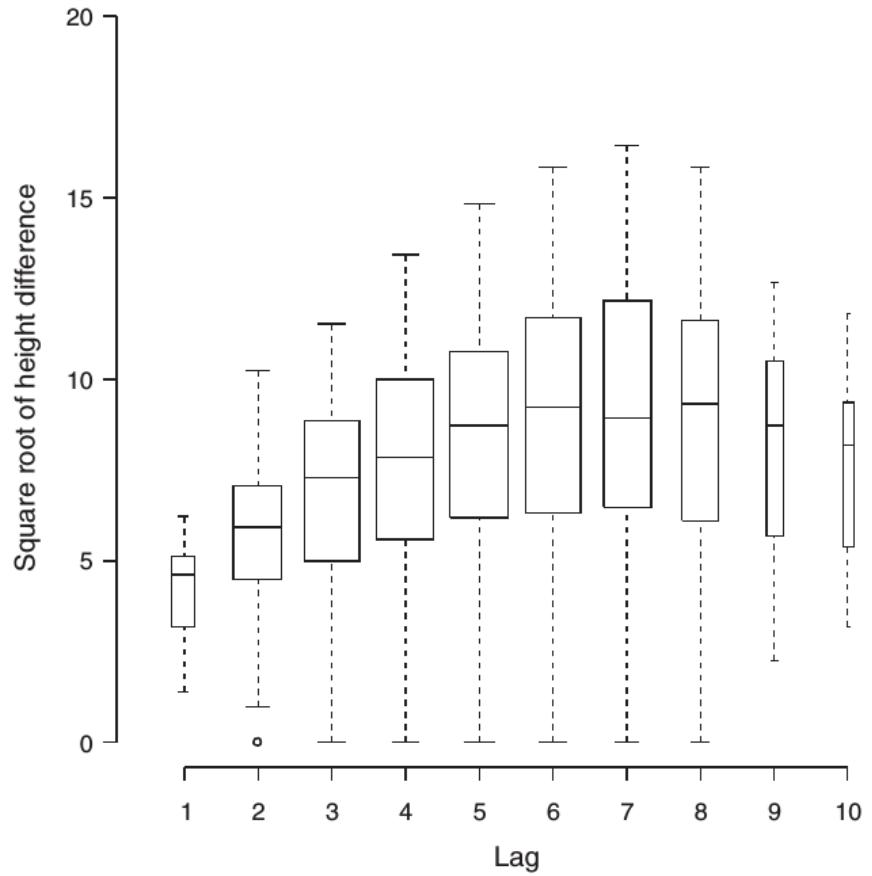
Kriging

Interpolation

Square root differences cloud

Distance classes → lags
and summary statistics

1. Describing spatial variation

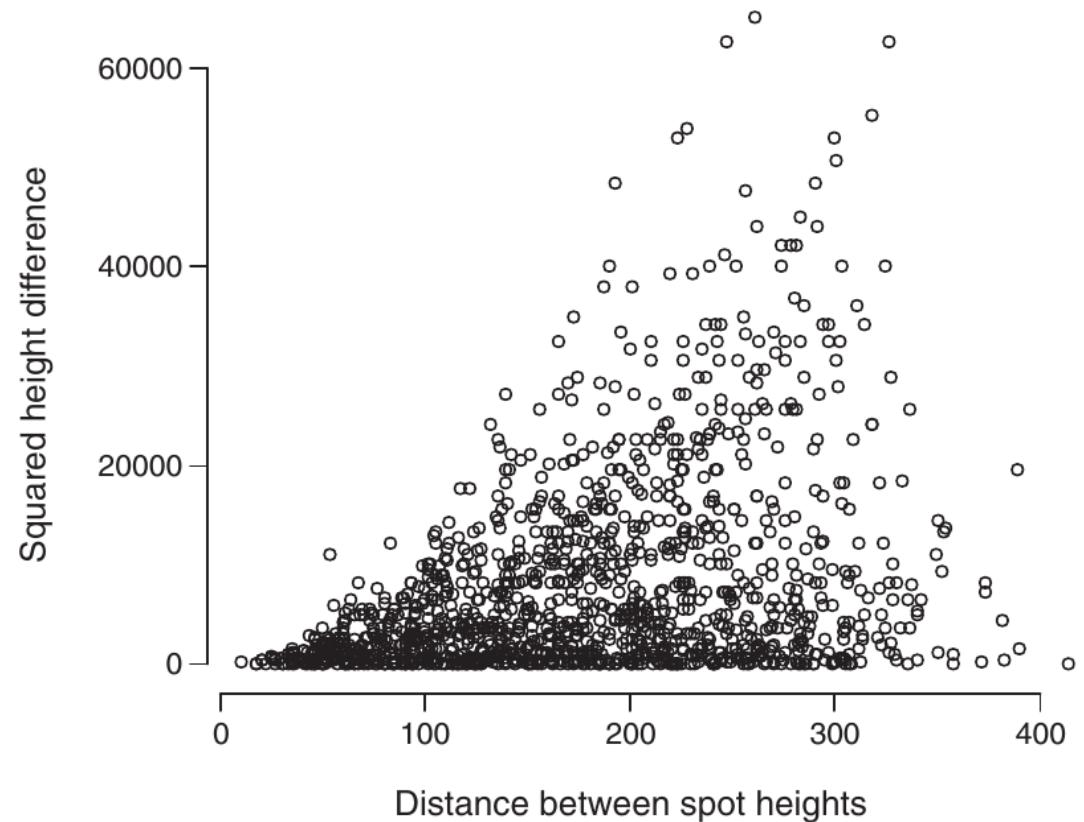


Kriging

Interpolation

Square differences, i.e. semivariogram cloud

1. Describing spatial variation



Kriging

Interpolation

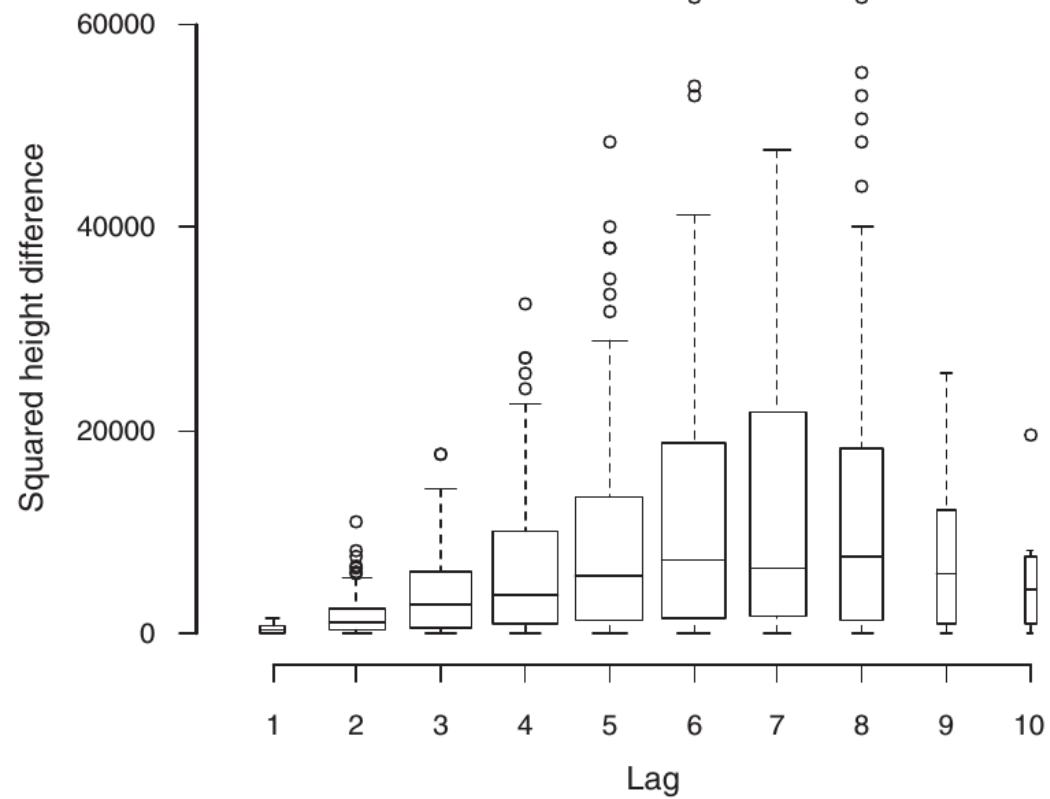
Square differences, i.e. semivariogram cloud

Distance classes → lags
and summary statistics
→ *experimental semivariogram*
[or short variogram]

Semivariance

$$2\hat{\gamma}(d) = \frac{1}{n(d)} \sum_{d_{ij}=d} (z_i - z_j)^2$$

1. Describing spatial variation



Kriging

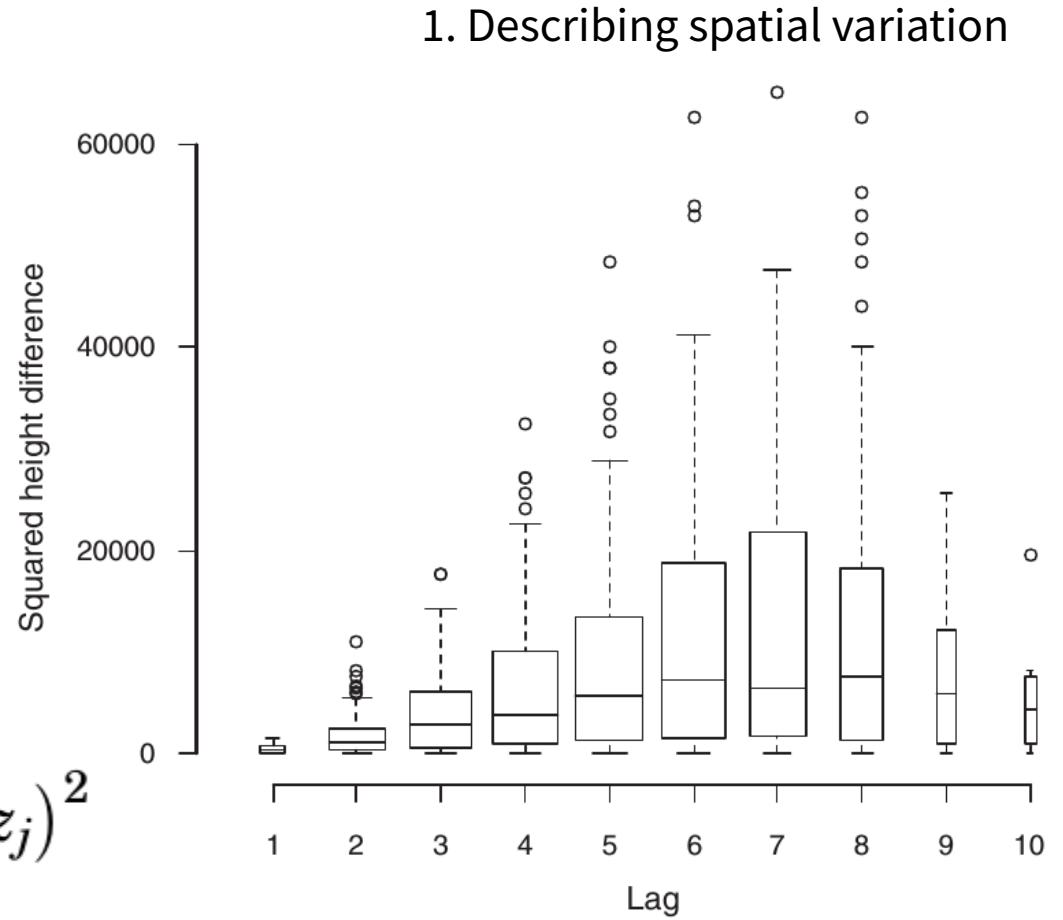
Interpolation

Square differences, i.e. semivariogram cloud

Distance classes → lags
and summary statistics
→ *experimental semivariogram*
[or short variogram]

Semivariance

$$2\hat{\gamma}(d) = \frac{1}{n(d \pm \Delta/2)} \sum_{d \pm \Delta/2} (z_i - z_j)^2$$



= mean of sum of squared differences at distance lags

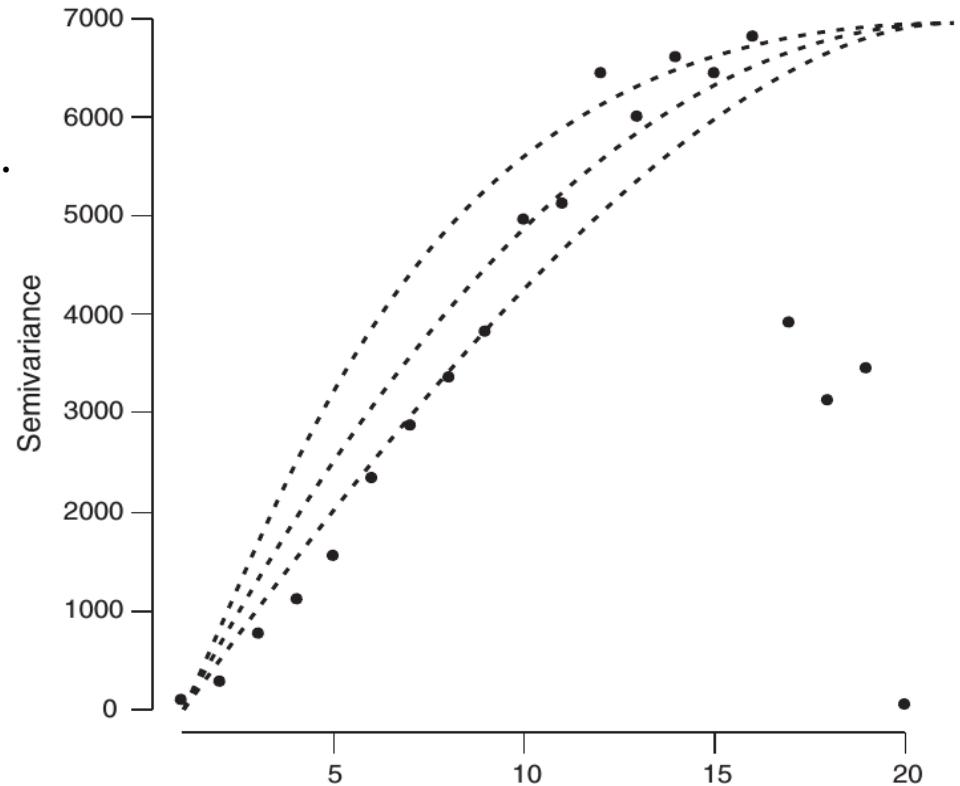
Kriging

Interpolation

Fitting a function to the experimental estimates from the semivariogram

Any function? No. Function has to be authorized, i.e.
→ function can only be positive
→ intercept at zero

2. Summarizing spatial variation



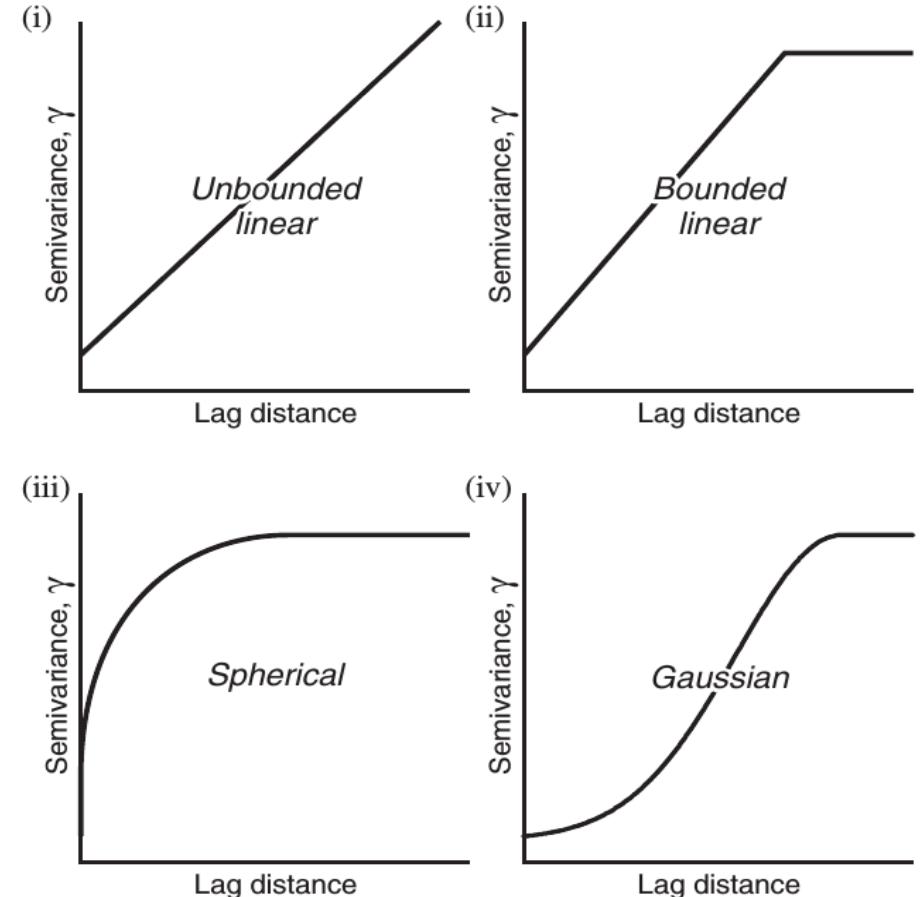
Kriging

Interpolation

Fitting a function to the experimental estimates from the semivariogram

Exemplary functions to fit

2. Summarizing spatial variation

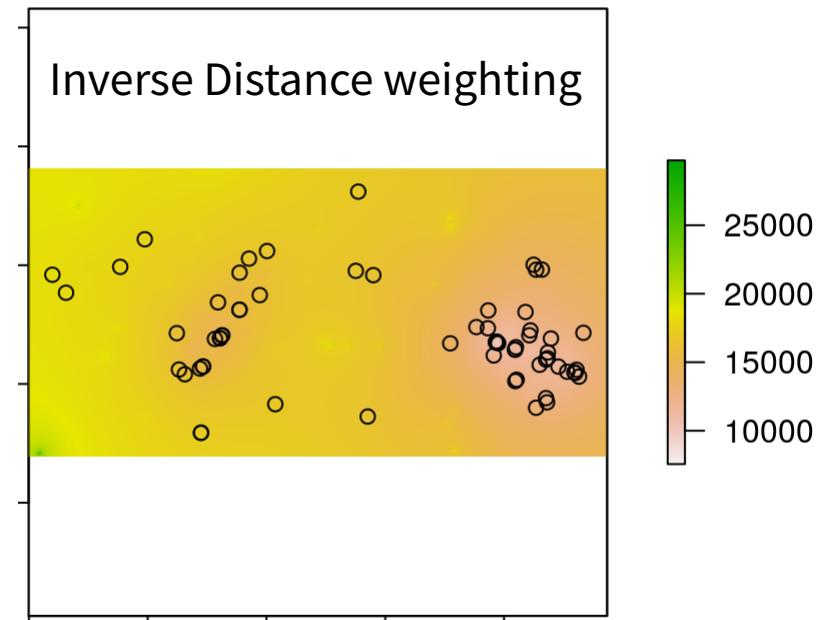
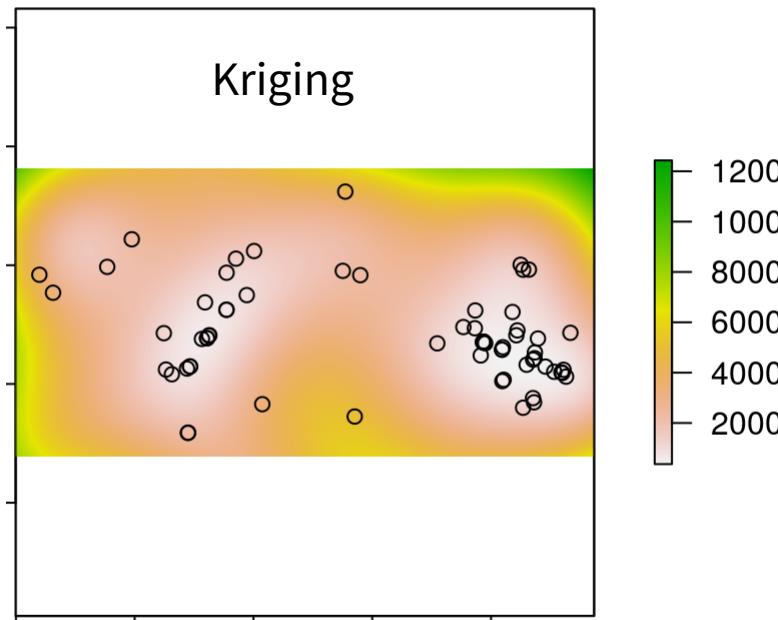


(O'Sullivan & Unwin, 2010)

Interpolation

Aim: get a continuous representation of settlement density.

Mission accomplished...!?



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Terrain analyses

Geomorphometry: the science of the quantitative representation of the Earth's surface

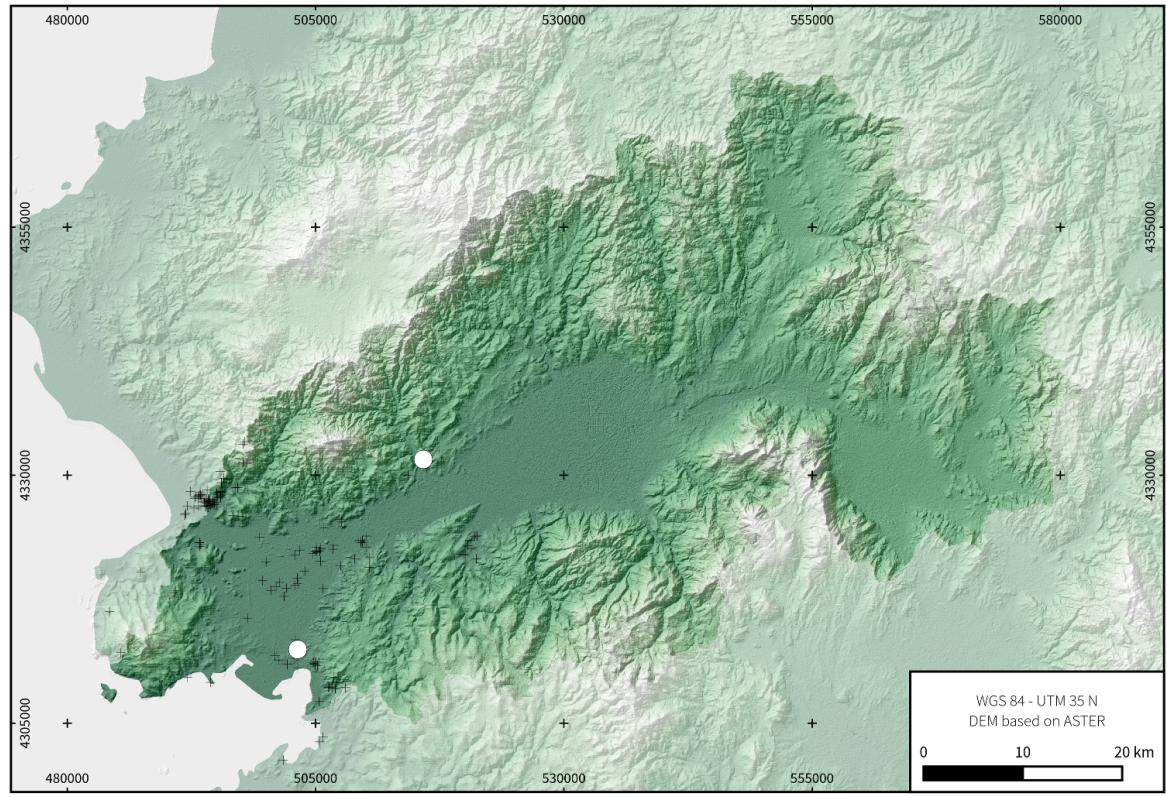
A great starting point:

Tomislav Hengl and Hannes I. Reuter (eds):
Geomorphometry Concepts, Software, Applications.
Developments in Soil Science, Volume 33, Pages 1-765 (2009)

Terrain analyses

Geomorphometry: the science of the quantitative representation of the Earth's surface

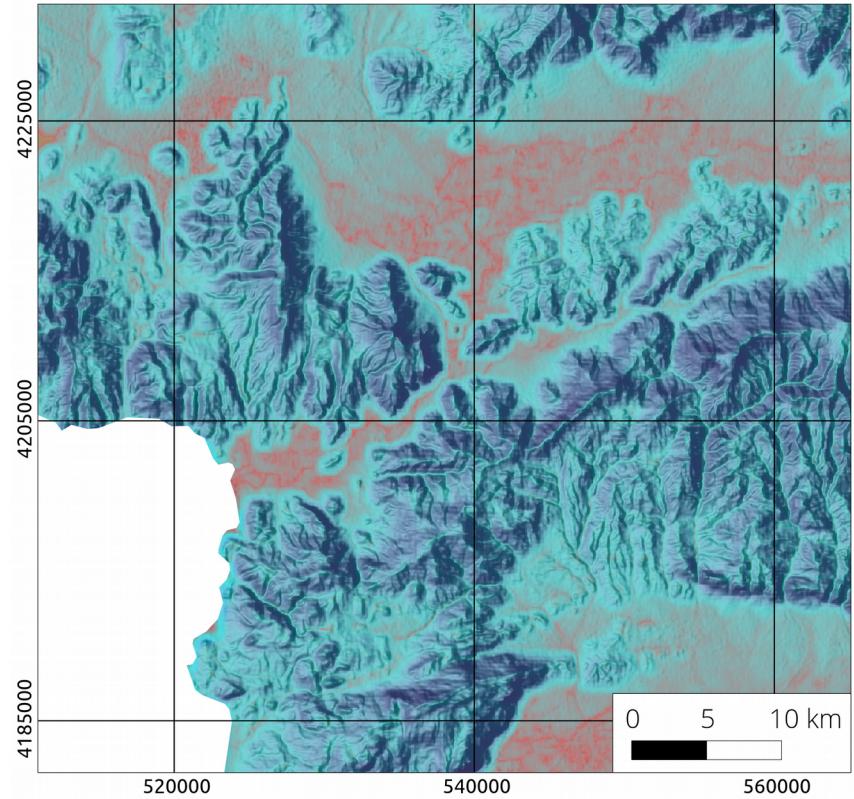
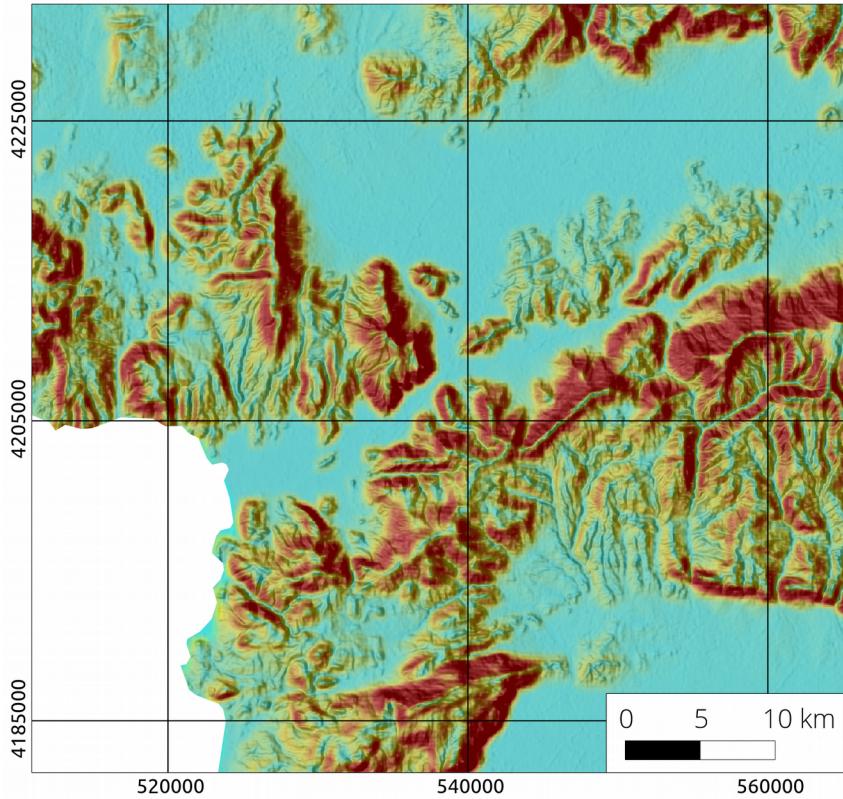
Everything starts with a DEM...



Terrain analyses

Slope = difference length/difference height

$$MTI = \ln\left(\frac{A^n}{\tan\beta}\right)$$



Terrain analyses – what was perceivable?



Terrain analyses – what was perceivable?



Terrain analyses – what was perceivable?



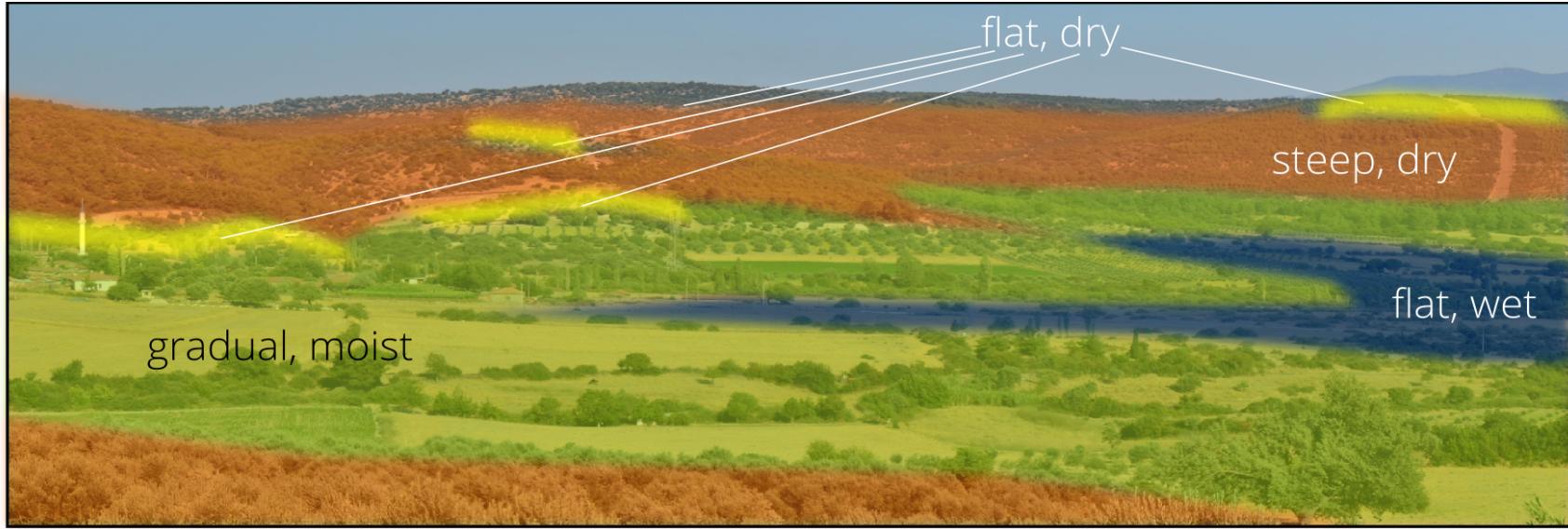
Terrain analyses – what was perceivable?



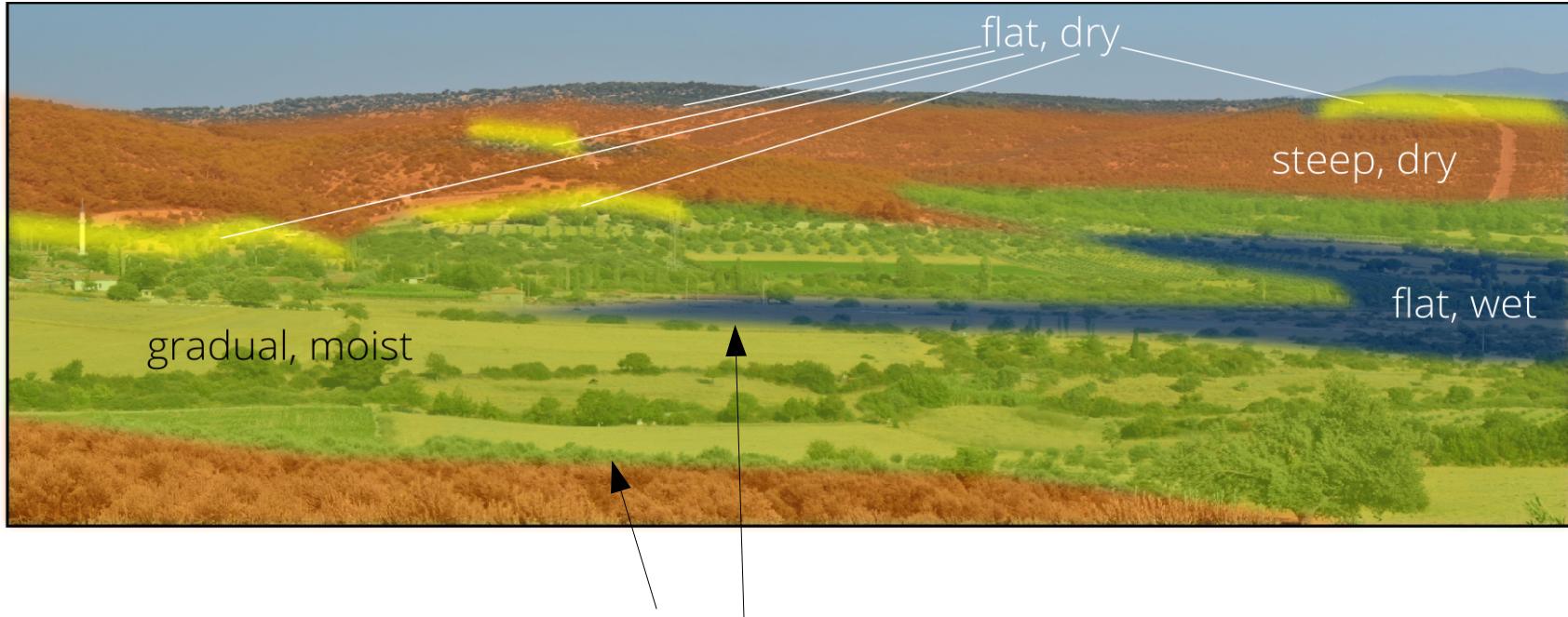
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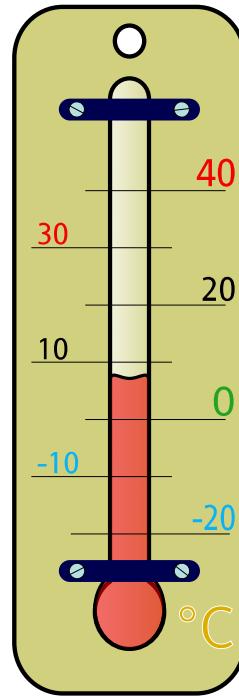
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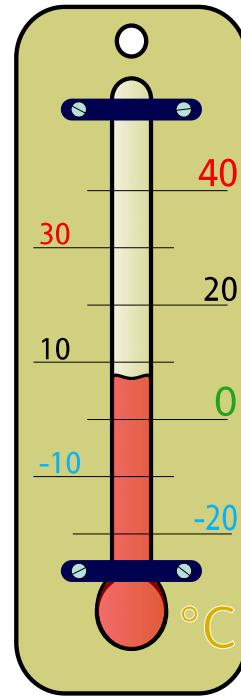
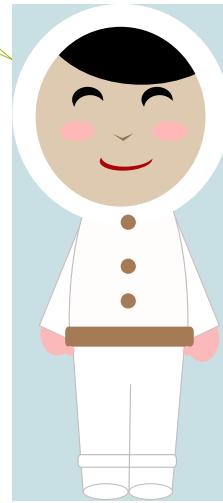


Crisp vs. fuzzy boundaries

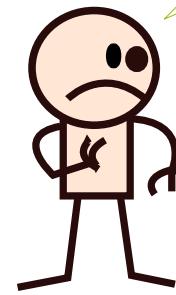


Crisp vs. fuzzy boundaries

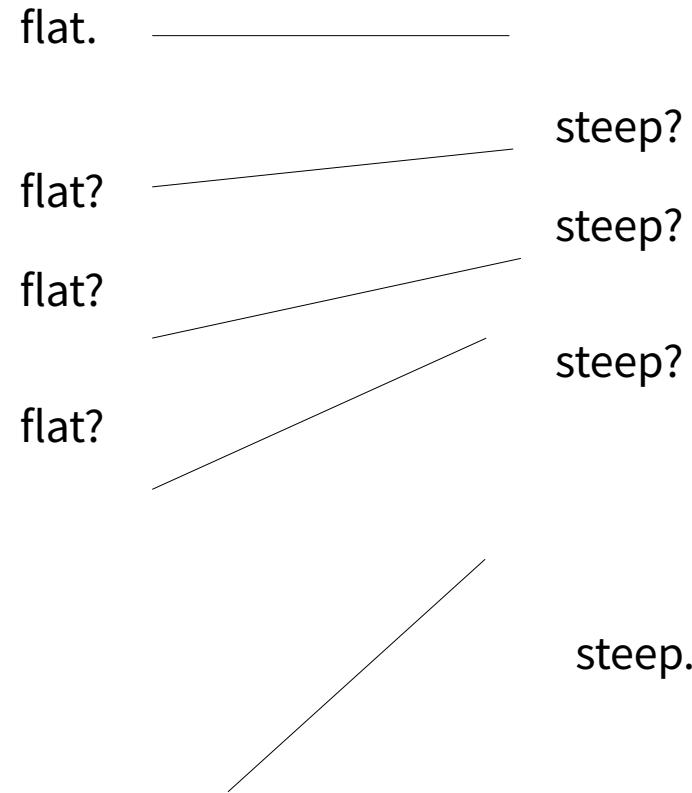
warm :)



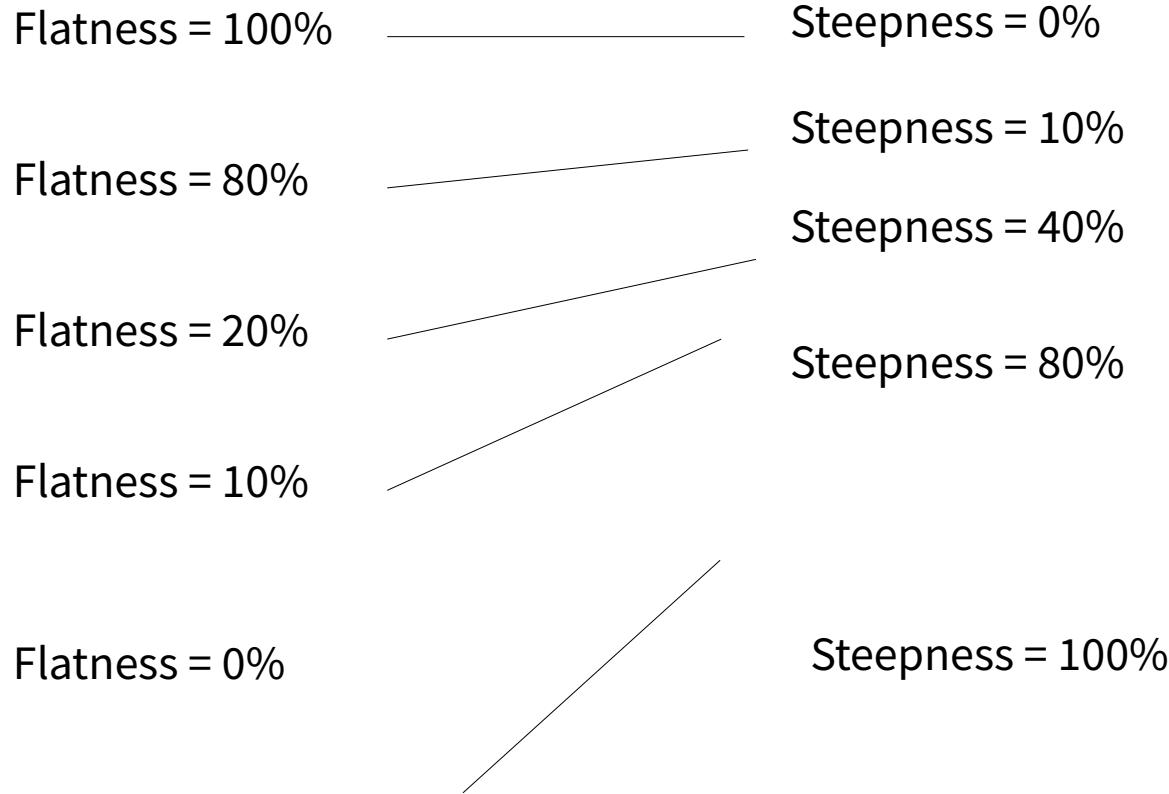
cold :(



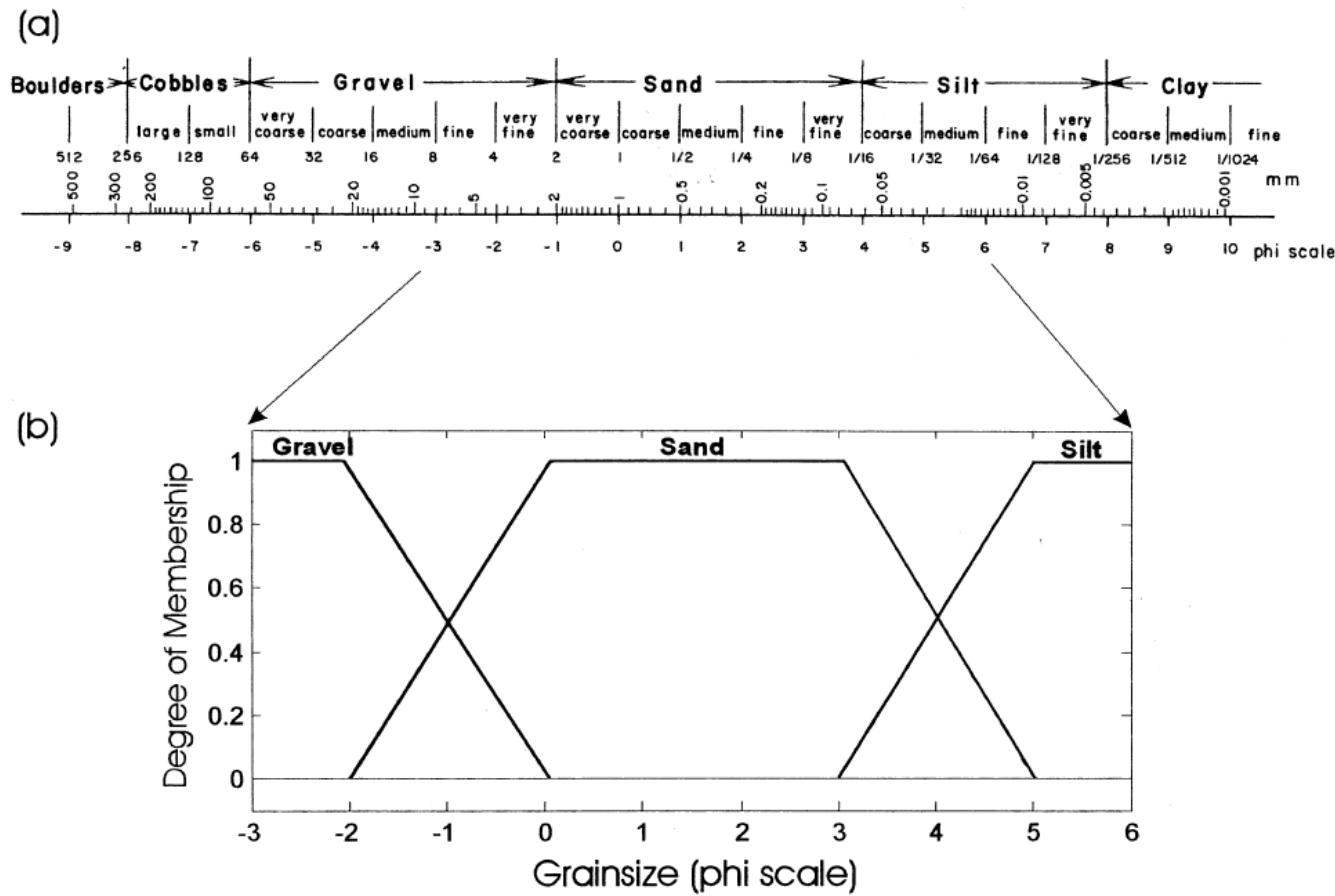
Crisp vs. fuzzy boundaries



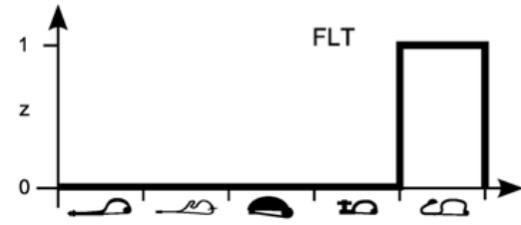
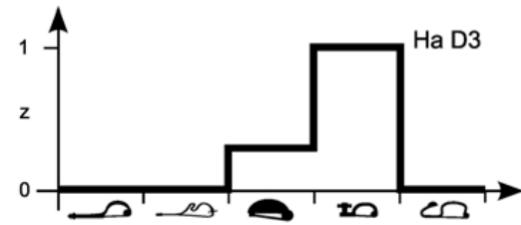
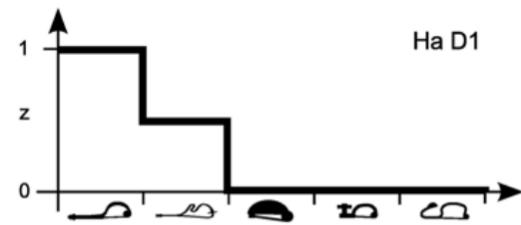
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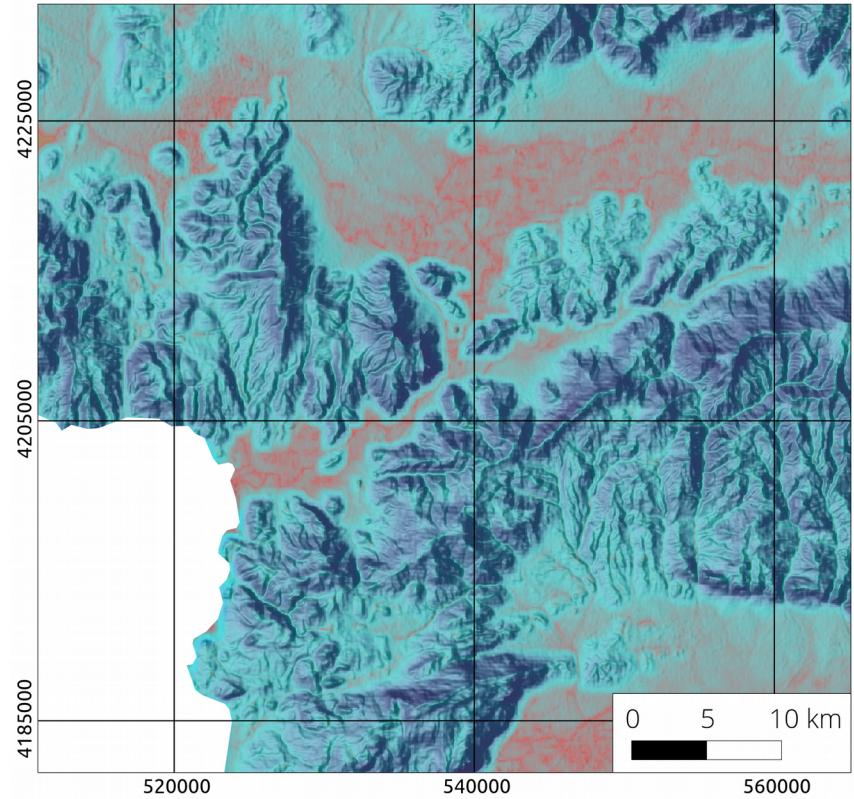
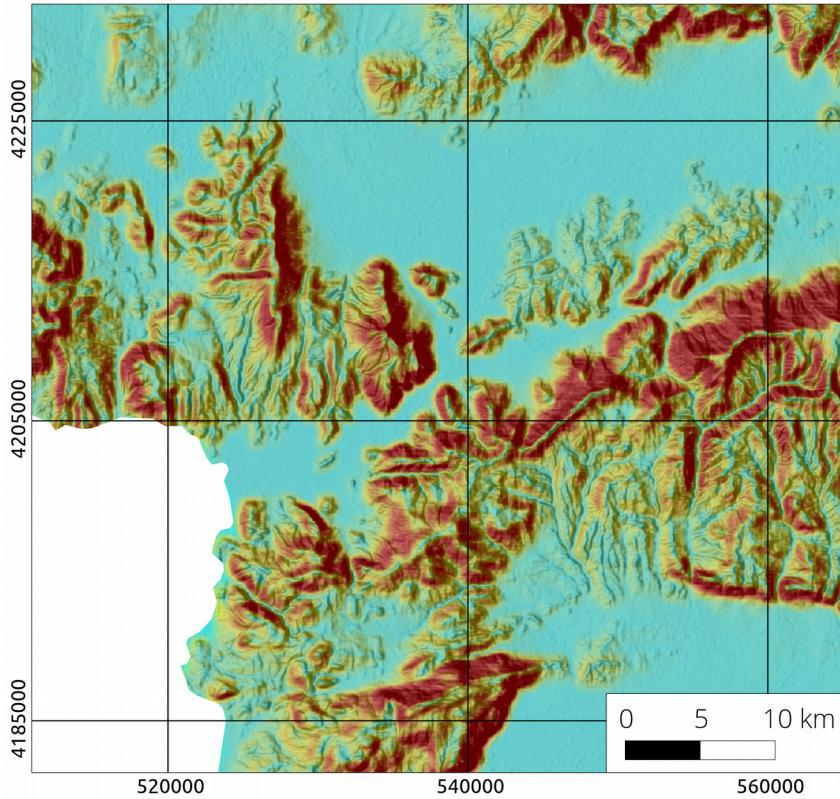
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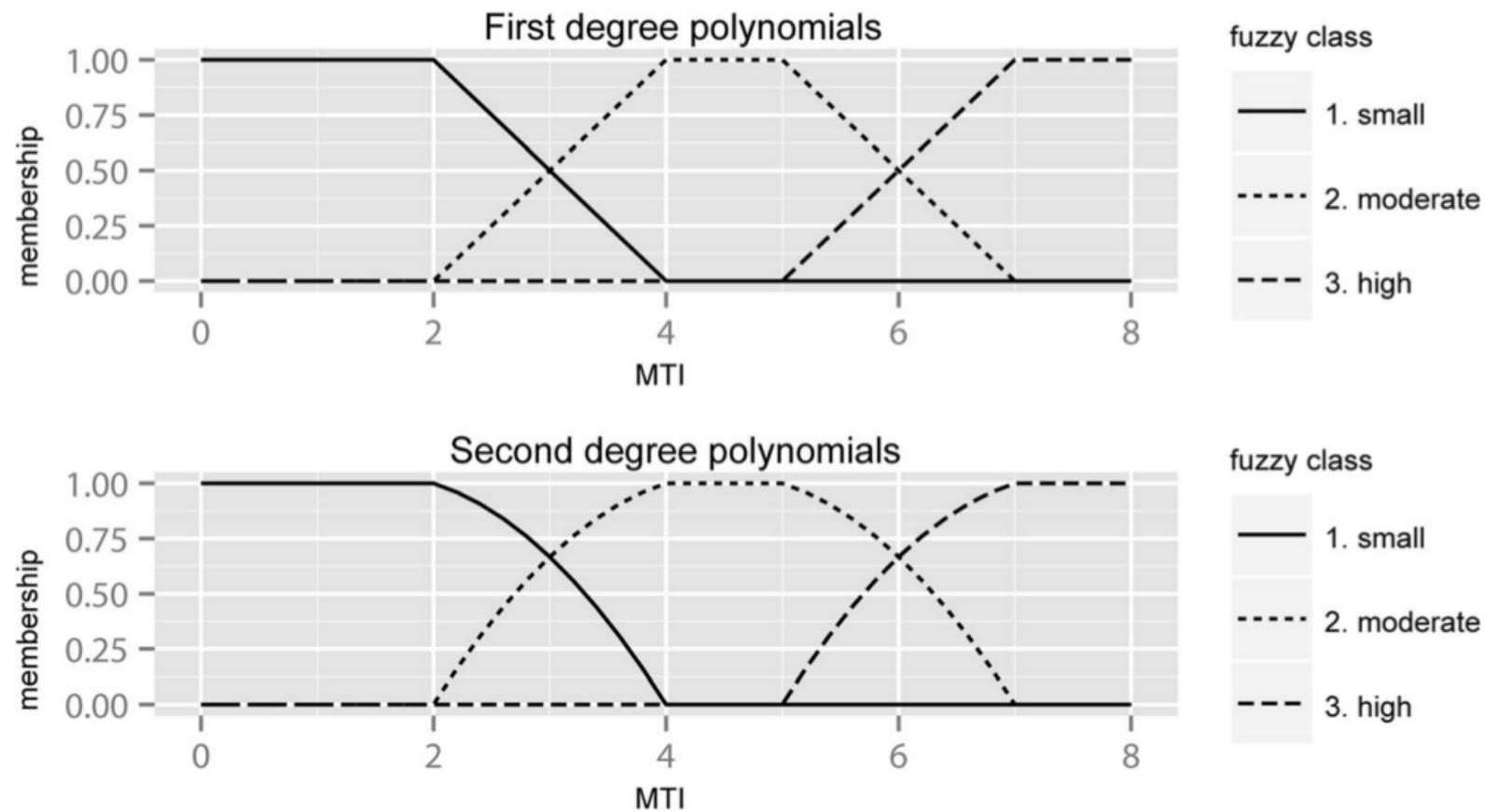
Terrain analyses – what was perceivable?

Slope = difference length/difference height

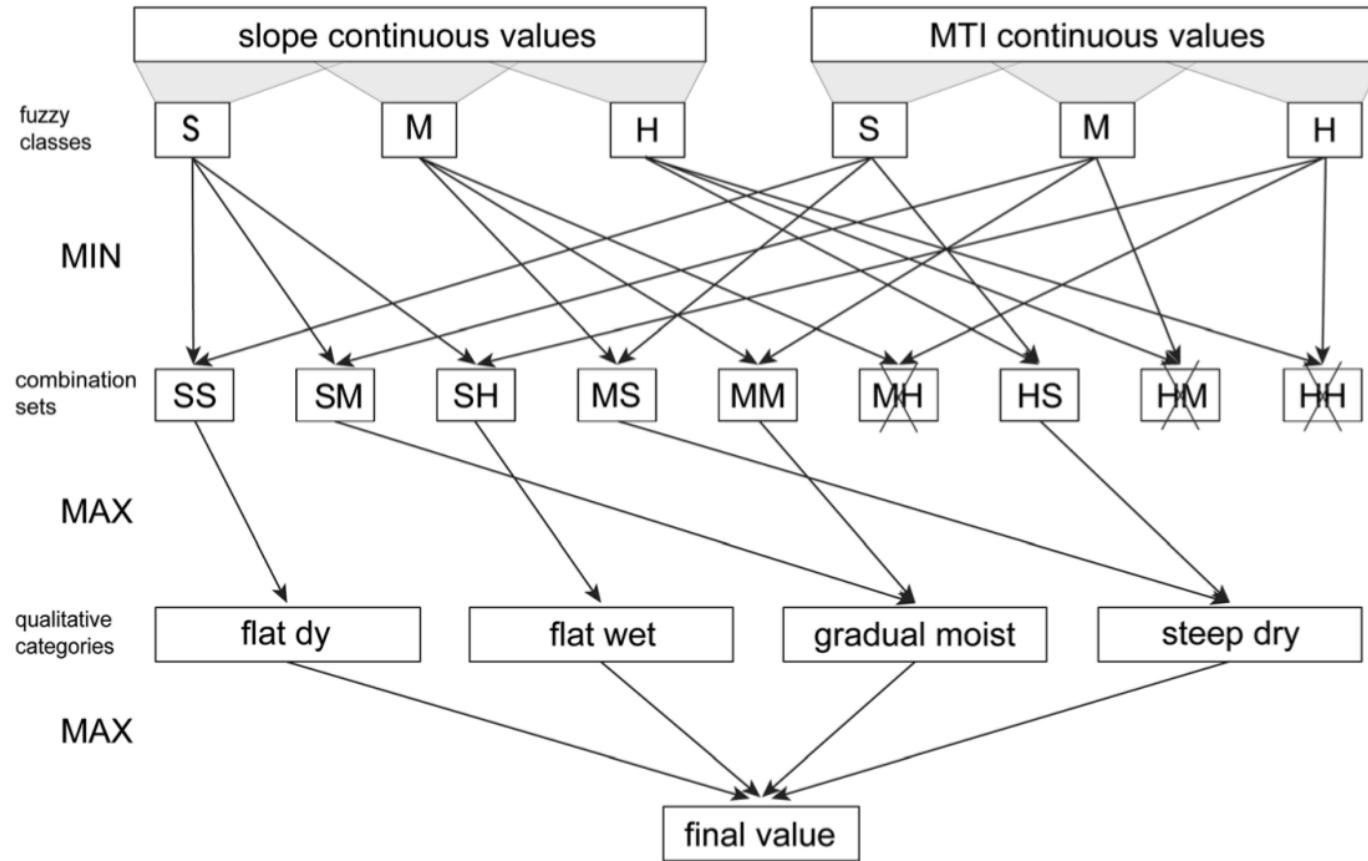
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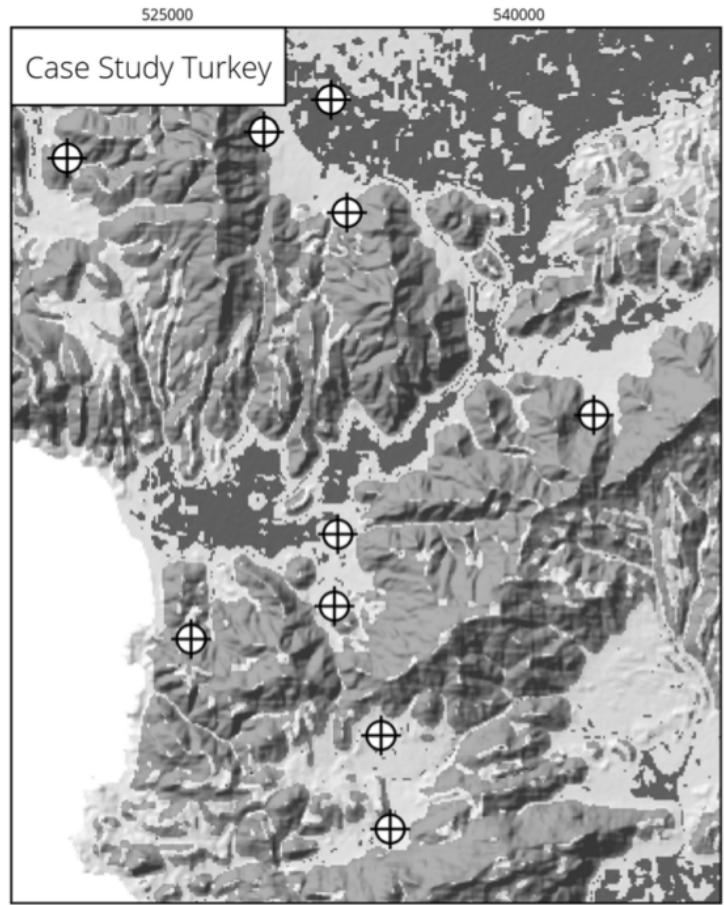
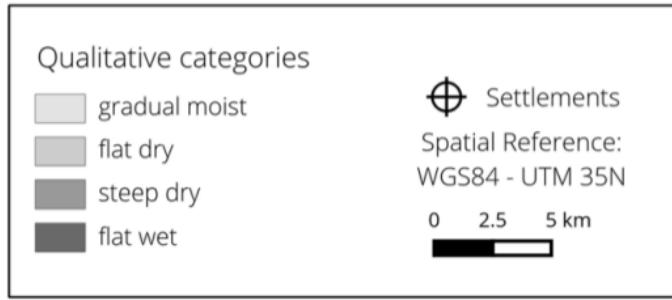
Terrain analyses – what was perceivable?



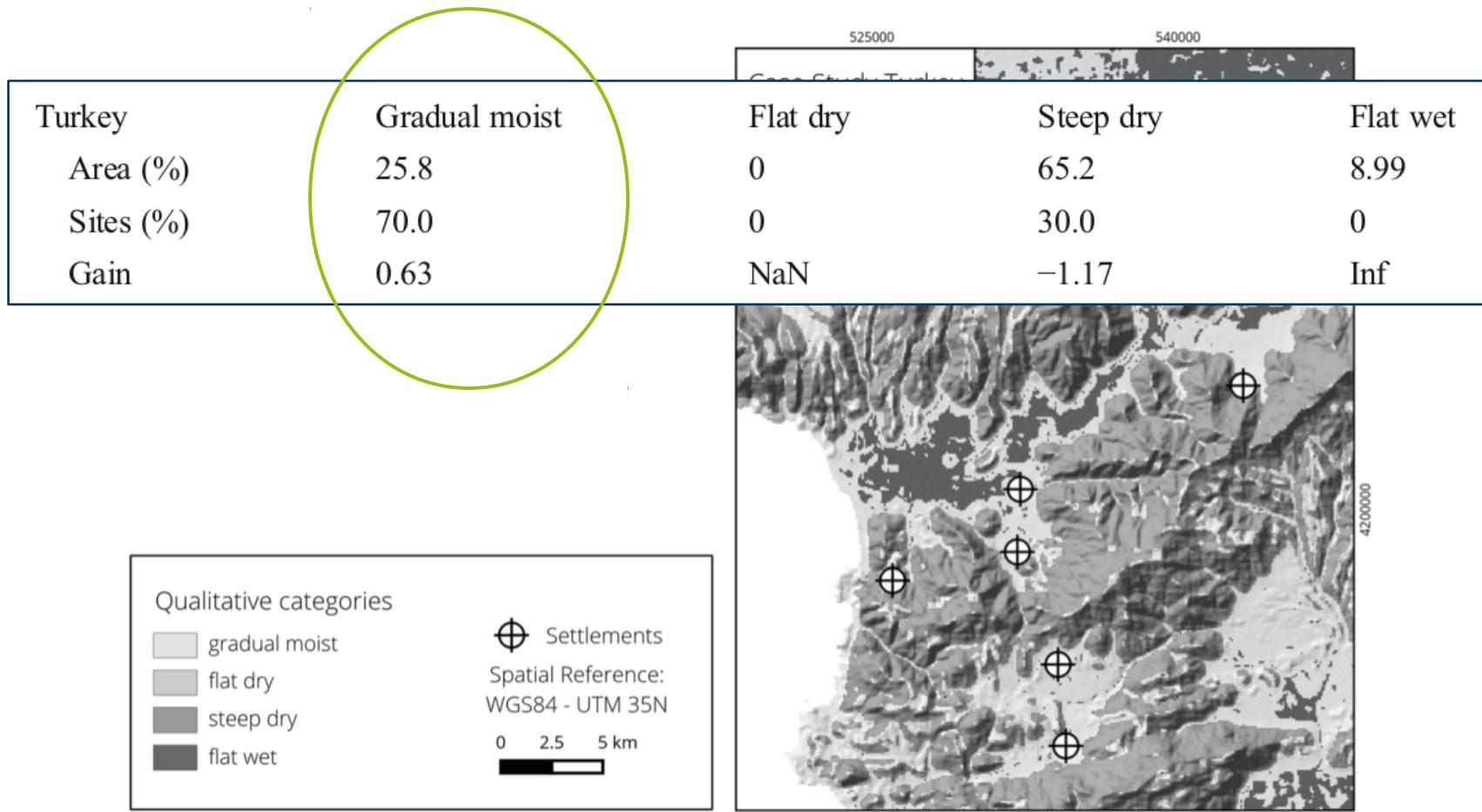
Terrain analyses – what was perceivable?



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Terrain analyses – what was perceivable?



Terrain analyses – what was perceivable?

If “they” preferred certain areas,
how would a resulting interaction
network look like?

Terrain analyses – what was perceivable?

If “they” preferred certain areas,
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Workflow:

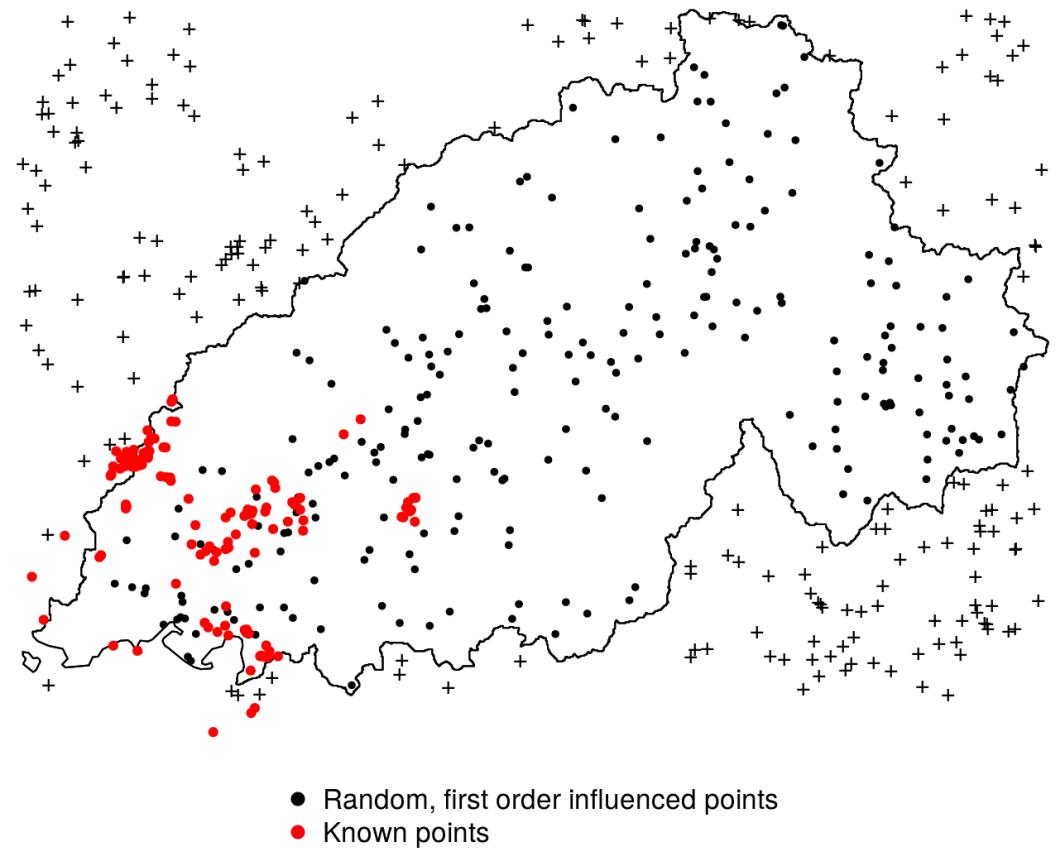
- fuzzy terrain

Terrain analyses – what was perceivable?

If “they” preferred certain areas,
how would a resulting interaction
network look like?

Workflow:

- fuzzy terrain
- point pattern analyses



Terrain analyses – what was perceivable?

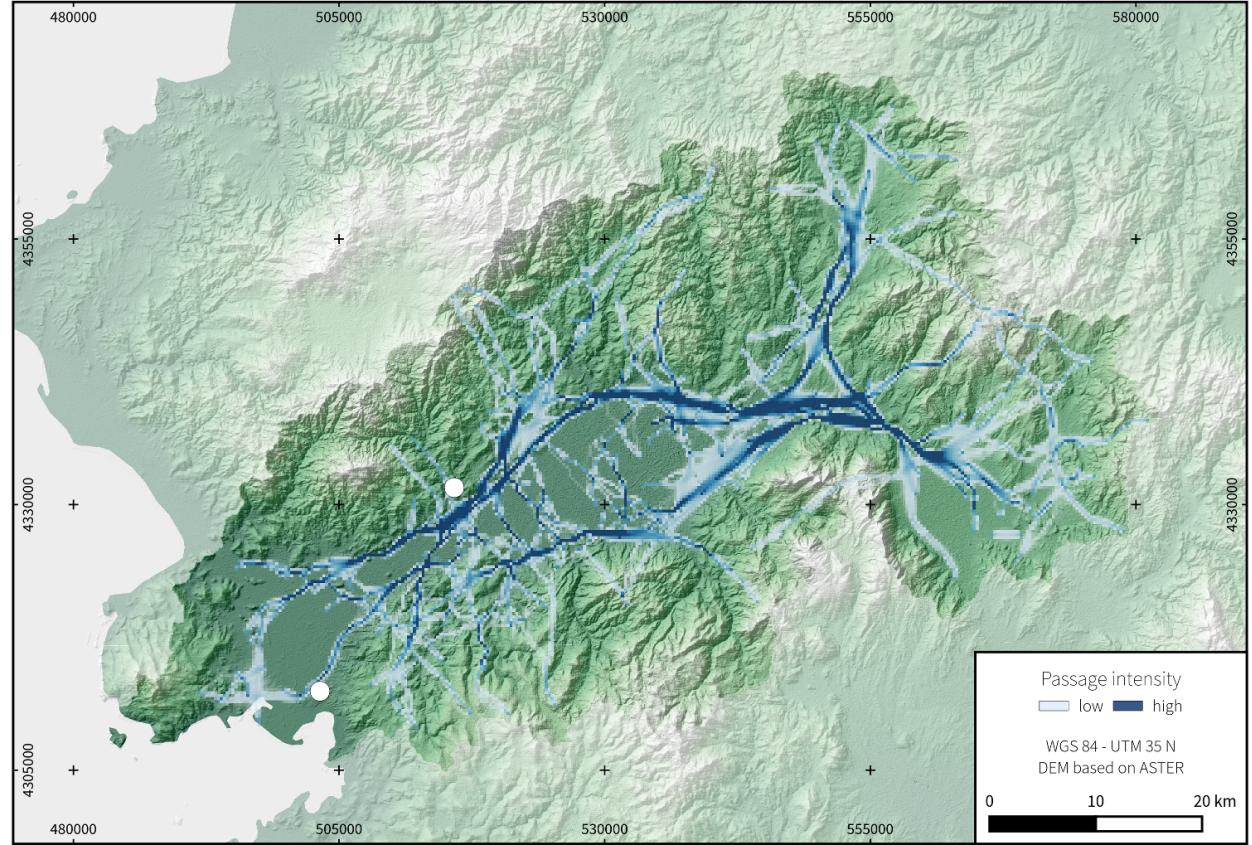
If “they” preferred certain areas, how would a resulting interaction network look like?

Workflow:

- fuzzy terrain
- point pattern analyses
- cost-surface creation
- pseudo-random walk

(the smaller the cost, the higher the probability)

- sum of all random walks

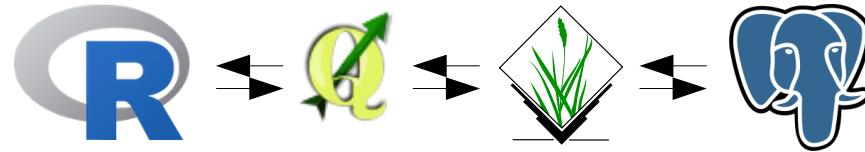


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Outlook: personal advices

use open-source software, i.e. free software published under terms of GNU GENERAL PUBLIC LICENSE



Why?

- They grow. Fast. So you can work at the bleeding edge
 - YOU can contribute
 - others can contribute so YOU can profit from their methods and tools
 - you can investigate how methods are implemented.
-

Publish open access. www.sci-hub.io is/was no alternative and science needs to be free.

Share your code. It is easy: github.com or gitlab.com

Thank you very much for your attention.

Entity-Attribute Spatial Data Types

Processes caused the spatial occurrence of different entities

Ceramic types

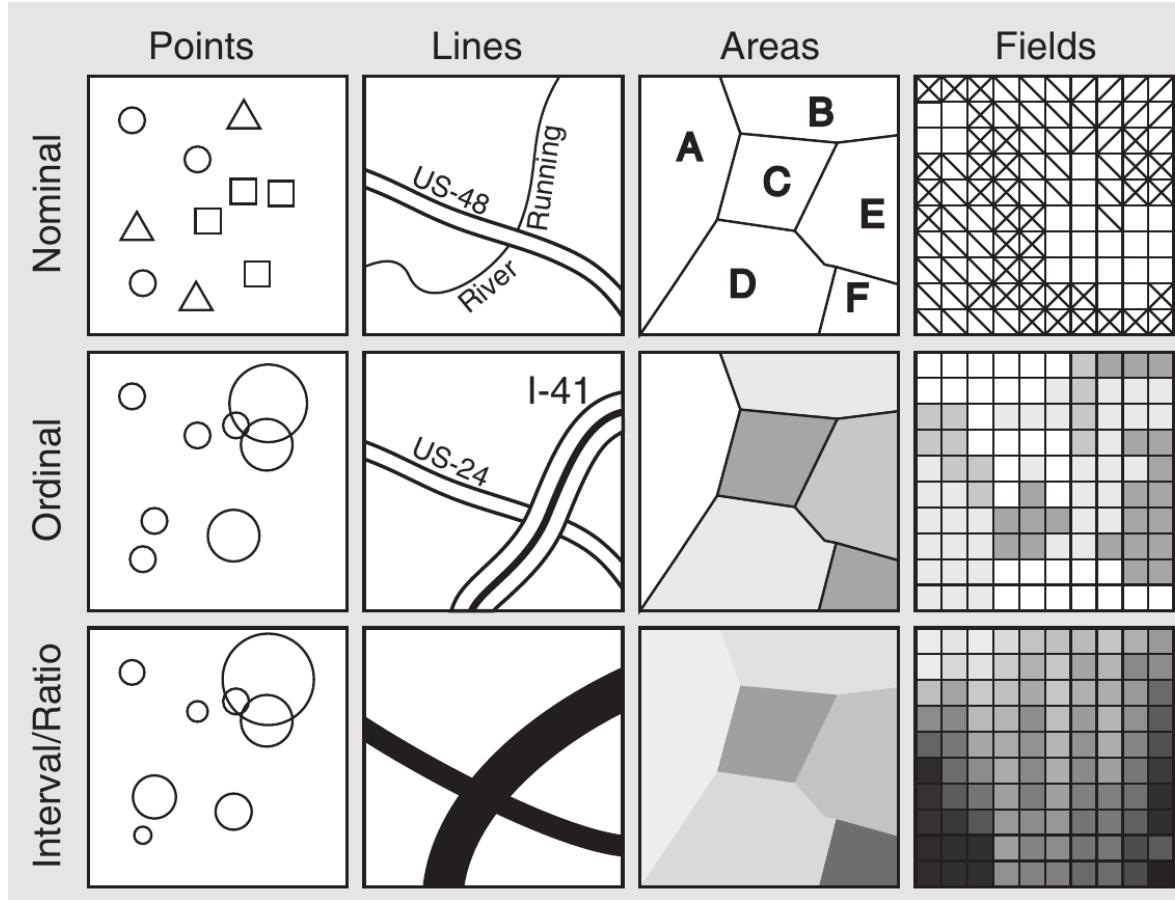
Site types

Hierarchy

Site size

Territories

Population density



Entity-Attribute Spatial Data Types

Processes define the transformation of spatial data

		TO			
		<i>Point, L⁰</i>	<i>Line, L¹</i>	<i>Area, L²</i>	<i>Field, L³</i>
F R O M	<i>Point, L⁰</i>	Mean center	Network graphs	Proximity polygons TIN, point buffer	Interpolation. Kernel density estimation Distance surfaces
	<i>Line, L¹</i>	Intersection junction	Shortest distance path	Line buffer	Distance to nearest line object surface
	<i>Area, L²</i>	Centroid City center	Graph of area skeleton	Area buffer, Polygon overlay	Pycnophylatic interpolation and other surface models
	<i>Field, L³</i>	Surface specific points VIPs	Surface network	Watershed delineation, Hill masses	Equivalent vector field territories

Spatial Autocorrelation – Moran's I

$$I = \left[\frac{n}{\sum_{i=1}^n (y_i - \bar{y})^2} \right] \times \left[\frac{\sum_{i=1}^n \sum_{j=1}^n w_{ij}(y_i - \bar{y})(y_j - \bar{y})}{\sum_{i=1}^n \sum_{j=1}^n w_{ij}} \right]$$

Weight from spatial weight matrix

Covariance term

Division by total data variance

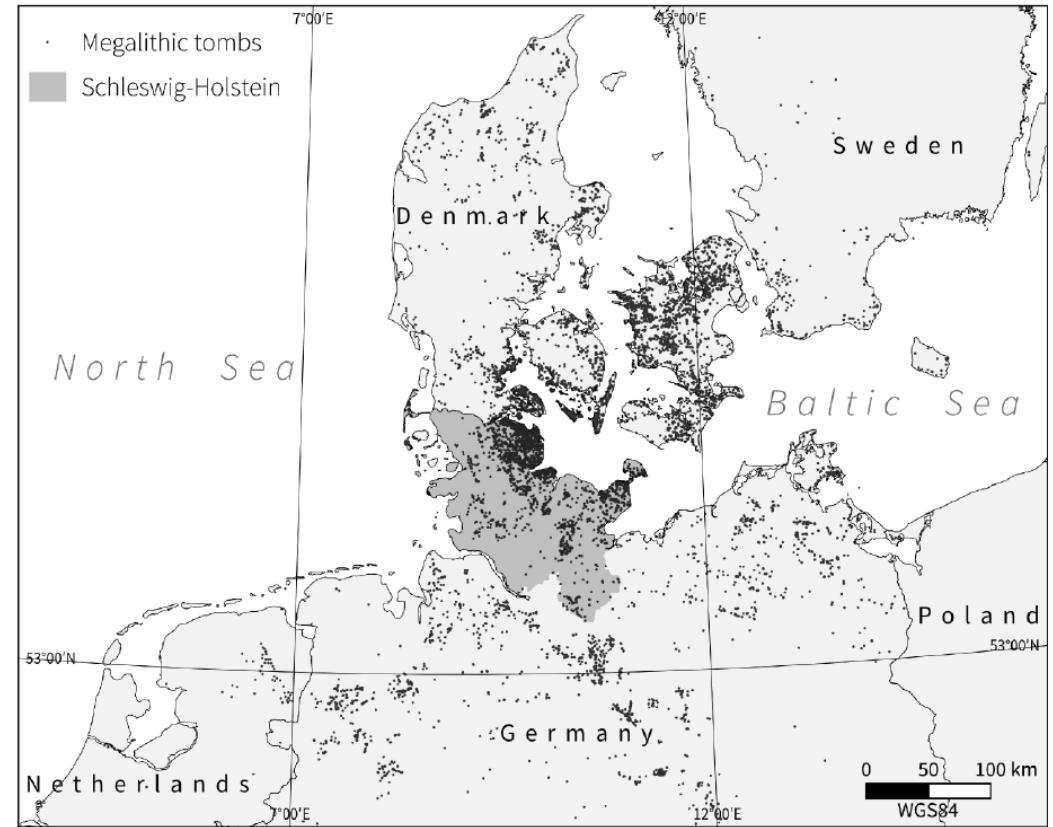
Normalize to total spatial weights

The diagram illustrates the components of the Moran's I formula. It shows the formula as a product of two matrices. The first matrix is a scalar divided by the sum of squared deviations from the mean. The second matrix is a weighted covariance term divided by the sum of weights. Annotations with arrows point to each component: 'Weight from spatial weight matrix' points to the covariance term, 'Covariance term' points to the numerator of the second matrix, 'Division by total data variance' points to the scalar in the first matrix, and 'Normalize to total spatial weights' points to the denominator of the second matrix.

Point Pattern – second order effects

Shows the point pattern clustering/dispersion; does it deviate from CSR?

→ Simulation approach based on
Monte Carlo simulations



Point Pattern – second order effects

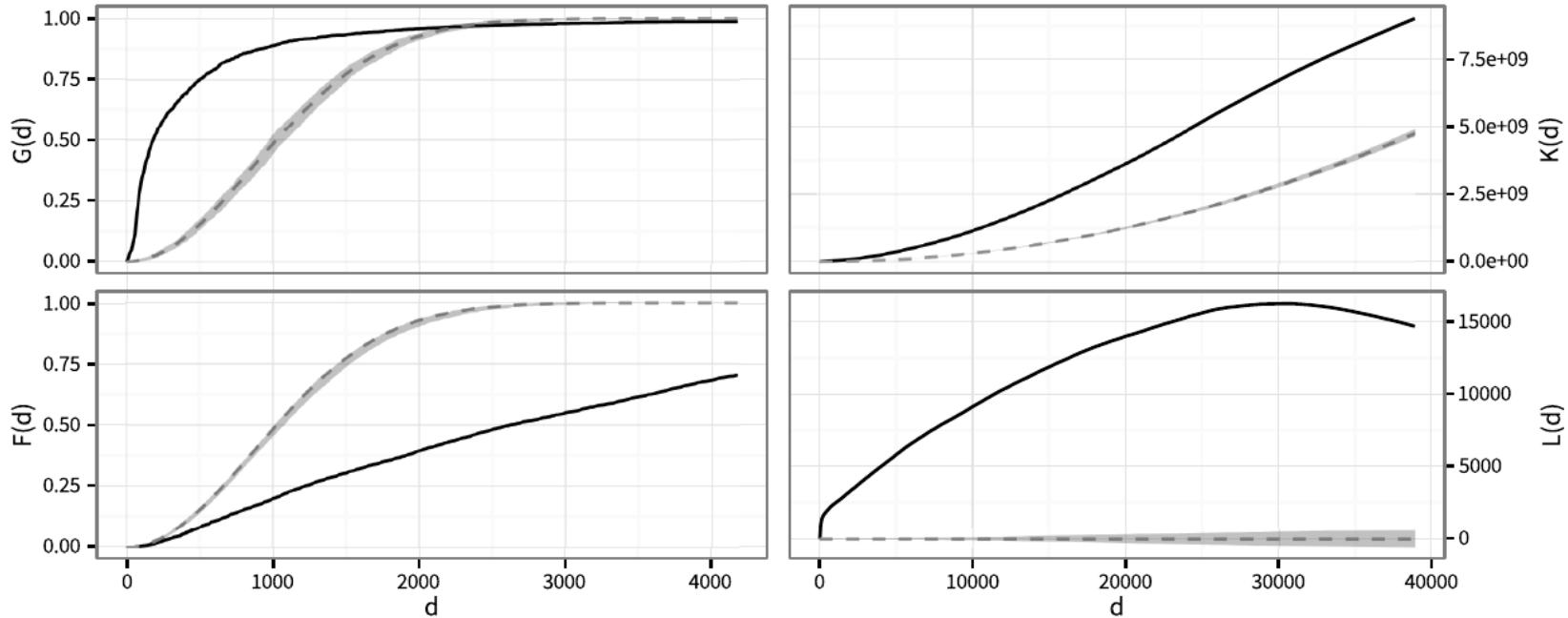
Shows the point pattern clustering/dispersion; does it deviate from CSR?

→ Simulation approach based on
Monte Carlo simulations

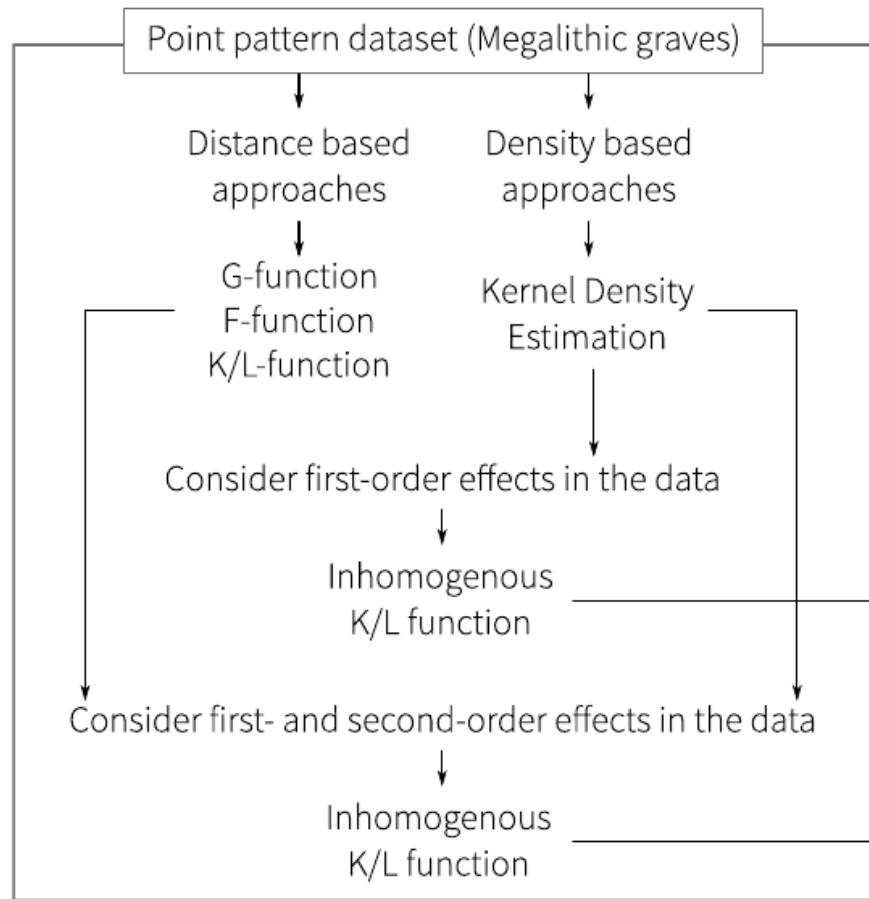
$$L(d) = \sqrt{\frac{K(d)}{\pi}}$$

Just a
square root
transformation
of $K(d)$

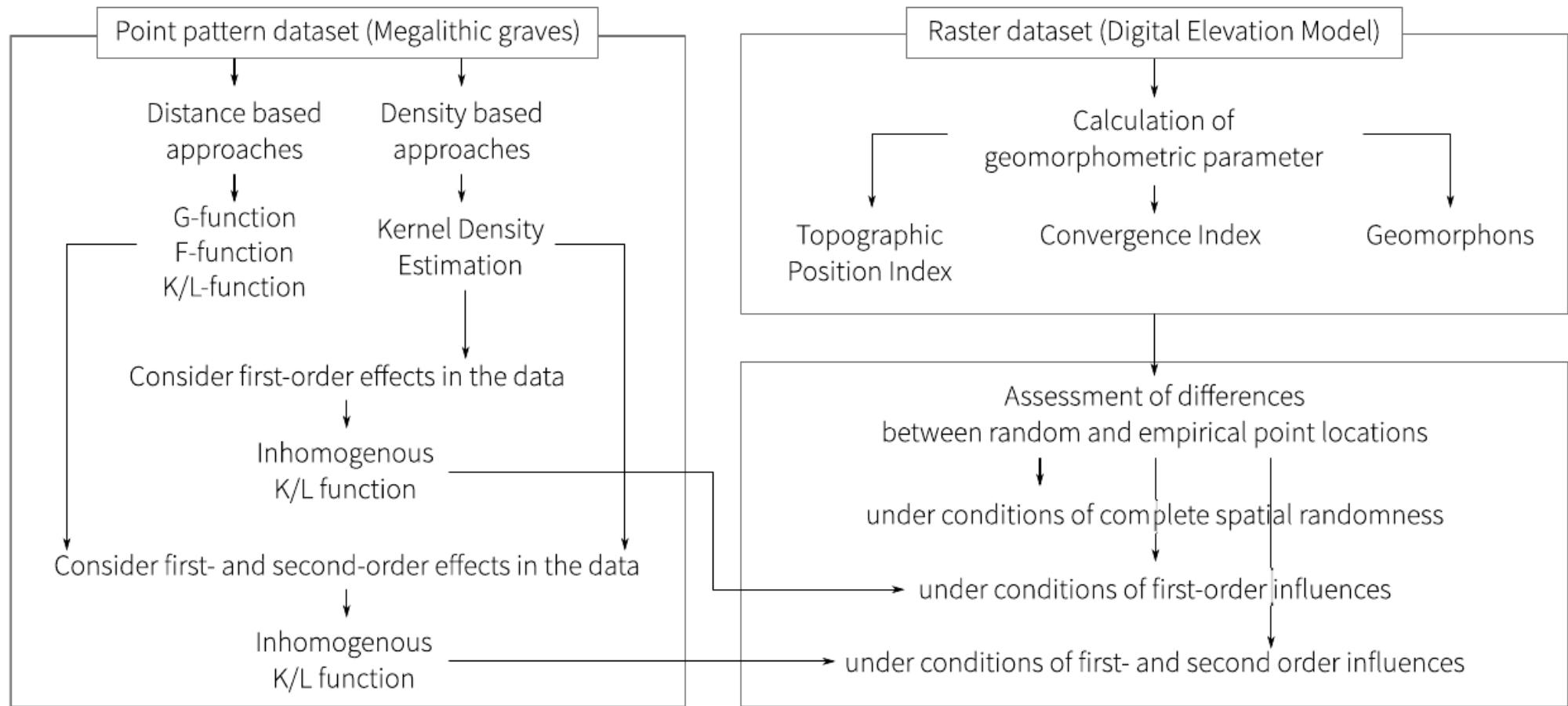
— Empirical distribution — Theoretical distribution



Point Pattern – a look ahead



Point Pattern – a look ahead



Kriging

Interpolation

“Elements” of a semivariogram

Nugget

→ measurement error

→ variation below shortest sampling interval

Sill

→ range of semivariance

Range

→ distance at which semivariance reaches maximal value

2. Summarizing spatial variation

