

Brute Force Analysis

combinationHelper():

- n is number of vertices
- Recursively generates all possible paths using permutations of the given vertices.
- combinationHelper is called $n!$ times due to checking each permutation
- Each call to combinationHelper() calls 1. test(): calls checkCycle() on updated path
- checkCycle() : runs $m - 1$ times , m being the length of the path, calls searchLinkedList inside a loop so its time complexity is $\theta(n \times m)$
- searchLinkedList() gets called inside checkCycle and has a time complexity of $\theta(n)$ since it checks every node in the linked list
- 2. Updates current path - $\theta(n)$
 - Updates remaining vertices - $\theta(n)$

Time Complexity = $\theta(n! \times (m \times n))$

But in the worst case m can = n so

Time complexity = $\theta(n! \times n^2)$