

# **DSAA Assignment-1**

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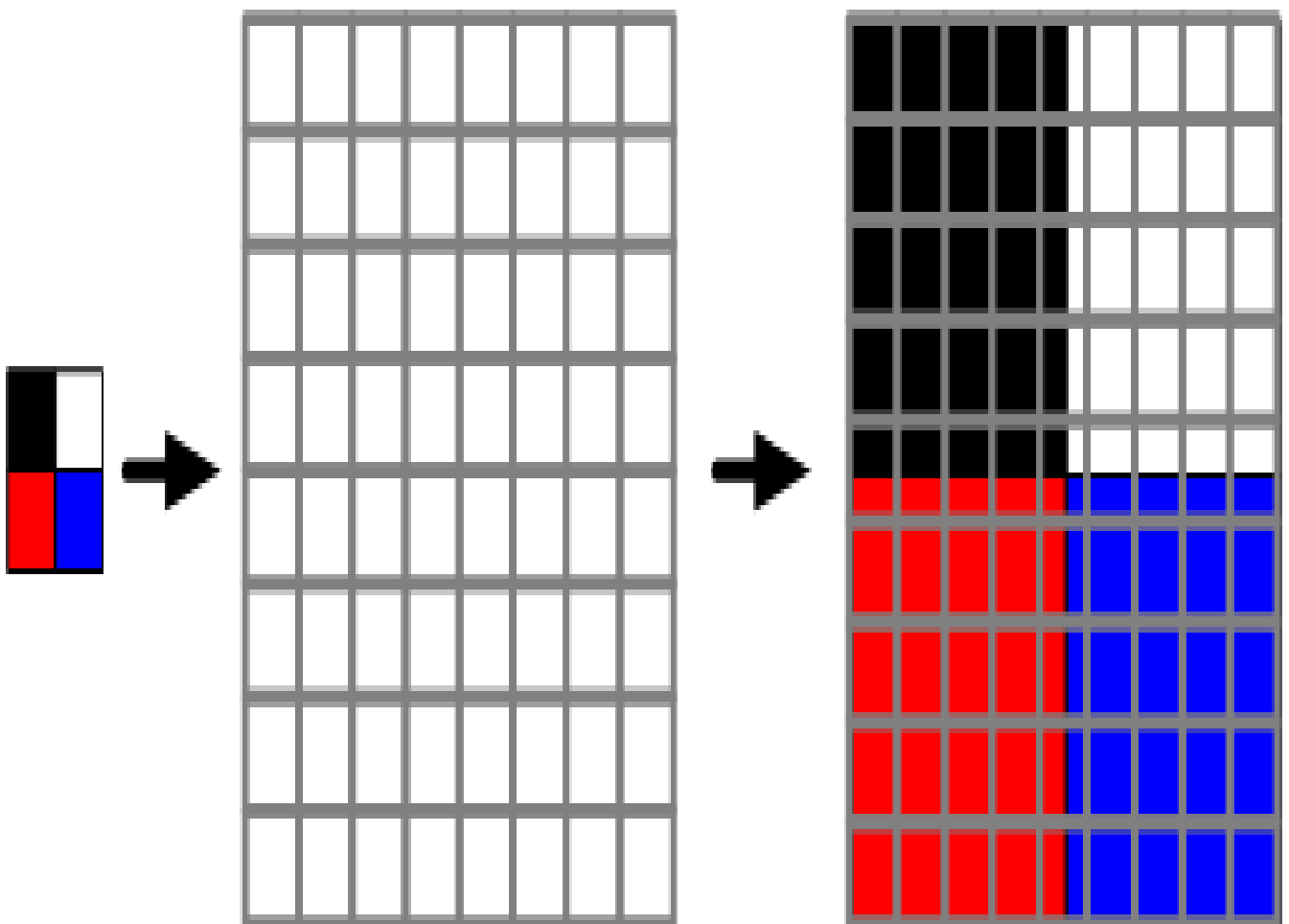
**MATLAB**

The PDF file contains report of all questions of assignment-1 including the algorithm, results and observations.

## Problem 1

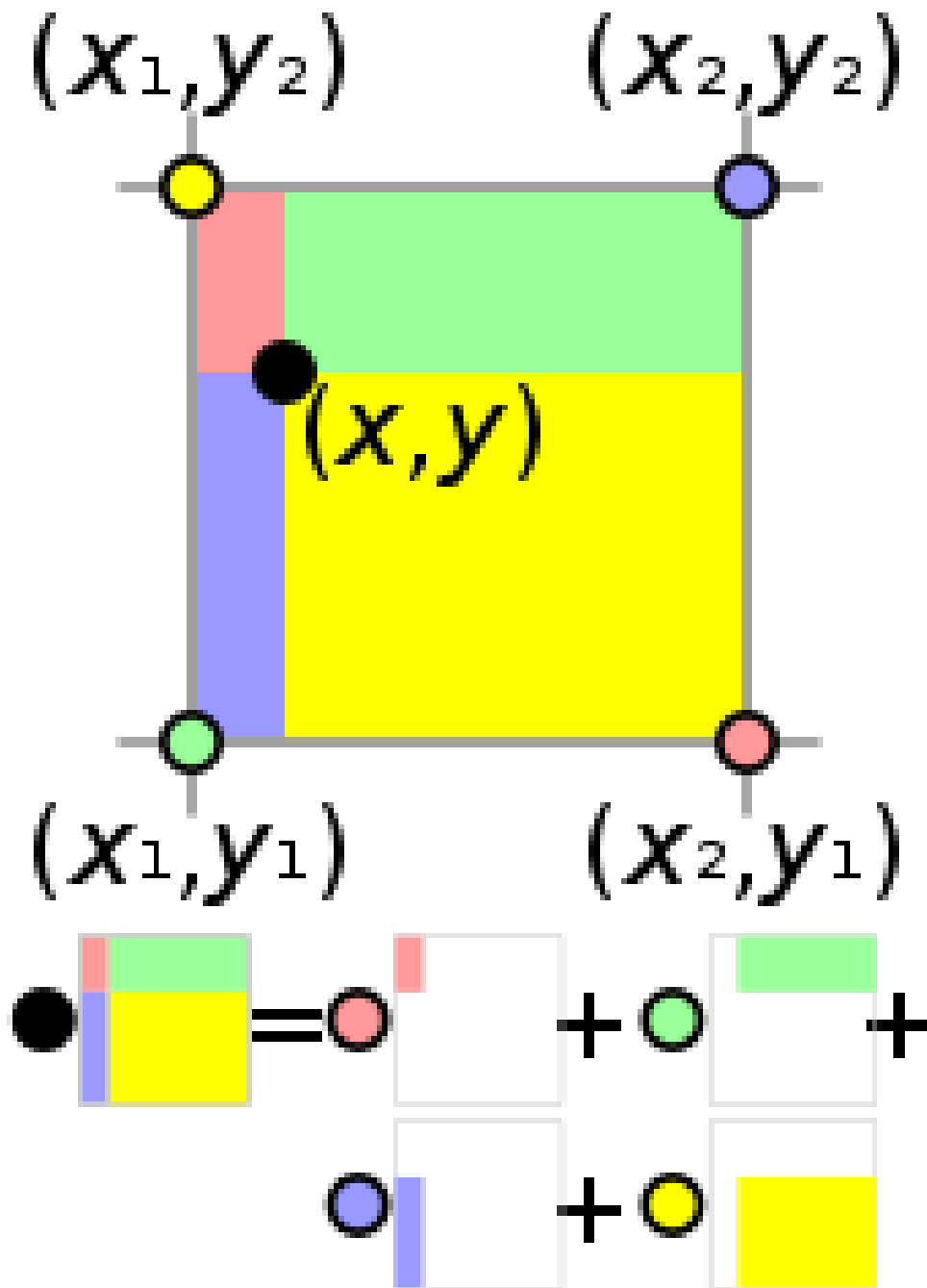
### 1) Nearest Neighbour interpolation

In this interpolation we take the value of the nearest known neighbour pixel. F



## 2) Bilinear Interpolation

In this type of interpolation instead of just replicating the values we consider the gradation in 2-D.



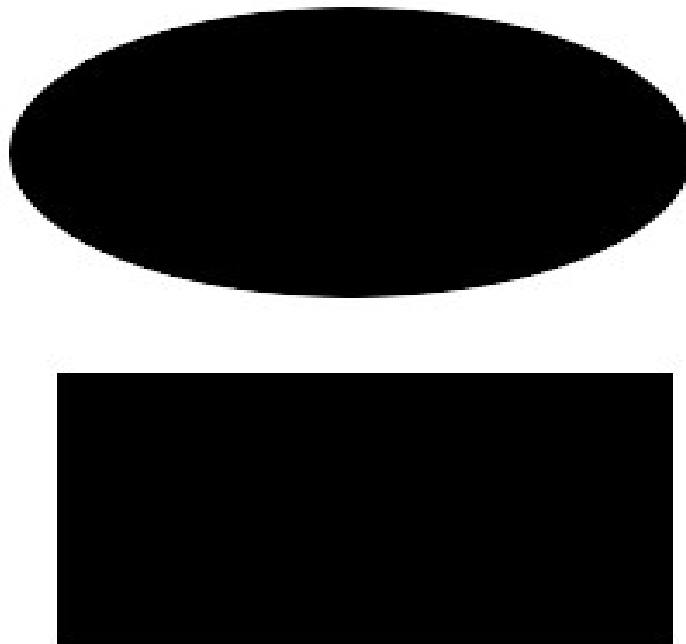
## 1). Algorithm

Given an image, we have to resize it to  $X$  times the original. In part a, an image of dimensions  $300 \times 300$  which should contain atleast 1 ellipse and 1 polygon, as shown below, was used.

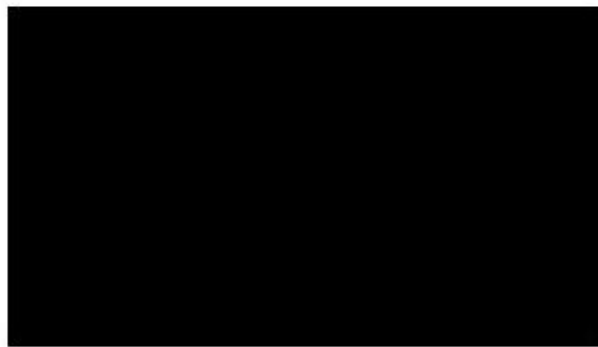
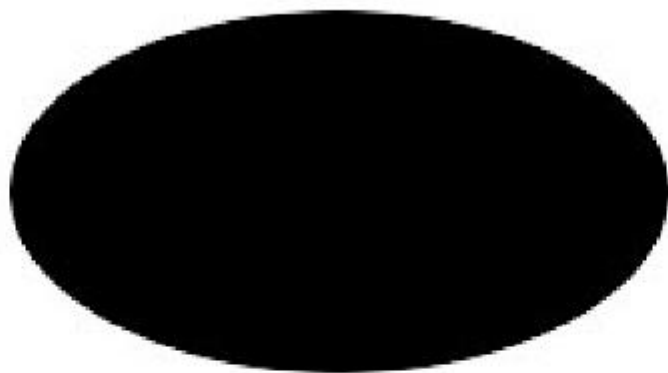
We change the pixel size to the desired  $X$  times, so that every element of size-matrix becomes  $X \times (\text{size of original matrix})$ .

Now, we fill  $X$  pixels of answer matrix, with 1 pixel of original. Bilinear Interpolation uses a weighted average of the four nearest cell centers. The closer an input cell center is to the output cell center, the higher the influence of its value is on the output cell value. Whereas, Nearest Neighbour can be used on continous data. It takes the nearest possible pixel from the original and outputs accordingly.

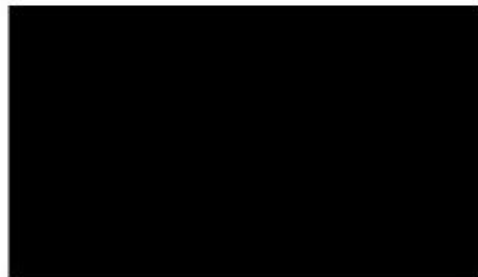
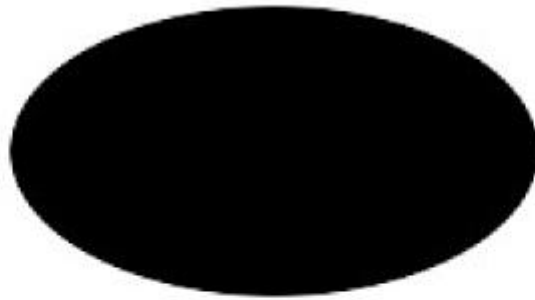
## 2). Result & Observations



**Original Image**



**X=5 Nearest Neighbour**



**X=2 Bilinear Interpolation**



**Black&White Original**



**Black&White X=5 Nearest  
Neighbour**



**Black&White X=2  
Bilinear Interpolation**



**Chrome Original**





**Chrome X=5 Nearest  
Neighbour**



**Chrome X=2  
Bilinear  
Interpolation**

## Problem 2

### 1) Algorithm

The matrix provided is known as 'Sobel Filter'. It detects transition wherever colour change occurs and draws a white line. (This is done using conv2 function as well as for-loop).

### 2) Result & Observation

When we perform convolution by M, we get Horizontal lines which detects vertical transitions among colours and when we do convolution by Transpose of the matrix, we get vertical lines which detects horizontal transitions among colours.

in the x direction:

-1	0	1
-2	0	2
-1	0	1

in the y direction:

-1	-2	-1
0	0	0
1	2	1

### Sobel Matrices



Convolution with M



Convolution with M-  
Transpose

### Problem 3

A) The formula for just 1 convolution will be

$$W = ((\text{Width} - F + 2Z) + S)/S$$

$$H = ((\text{Height} - F + 2Z) + S)/S$$

Where W is the Width of the output and H is the Height of the output.

But here we are doing N convolutions and so we have to keep in mind the dimensions of the previous output matrix to calculate the dimensions of the new output matrix. Suppose we are doing (i)th convolution and so we need the dimensions of the (i-1)th convolution.

Suppose the dimensions of the (i-1)th convolution are  $W_{i-1}$  and  $H_{i-1}$ . So the dimensions of after (i)th convolution will be

$$W_i = ((W_{i-1} - F + 2Z_T) + S)/S$$

$$H_i = ((H_{i-1} - F + 2Z_T) + S)/S$$

Z-transpose is such that when  $Z \leq F-1$ ,  $Z_T$  will be taken as Z and when it is greater than  $F-1$ ,  $Z_T$  will be taken as  $F-1$  to avoid filter from going out of range.

We do the above calculation till we get  $W_N$  and  $Z_n$  starting from  $W_0$  and  $Z_0$  which is the actual width and height of the image.

B) There will be  $F^2$  multiplications and  $F^2 - 1$  additions for each convolution at each channel. So in total there will be

$\sum W_i * H_i * F^2 * \text{Channels} : i = 0 \text{ to } n-1$   
this much number of multiplications and

$\sum W_i * H_i * (F^2 - 1) * \text{Channels} : i = 0 \text{ to } n-1$   
this much number of additions.

## **Problem 4**

**A)** Audio file is read using `audioread(<file_name>,fs);`

**B)** Let the points for which the values are known be  $x_1$  and  $x_3$  and the values being  $y_1$  and  $y_3$ . Suppose we have to find the value at some point between  $x_1$  and  $x_3$ , let this be  $x_2$ .

$$y_2 = (((x_2 - x_1) * (y_3 - y_1)) / (x_3 - x_1)) + y_1$$

$$x_2 = (((y_2 - y_1) * (x_3 - x_1)) / (y_3 - y_1)) + x_1$$

**C)** Here we can convolve the sound with the impulse response captured in different environments to simulate.

## **Problem 5**

If the filter is used on a region with same colour it sums to zero ( $1+2+1-1-2-2 = 0$ ) which makes it black. Hence, the upper and lower region in `sample_imp.png`, when convolved, gives black colour all over except in the middle. This is because, Transition change occurs in middle from black to white so, on convolving it results as :

3 ( $1+2+1$ ) of white and -3 ( $-1-2-1$ ) of black ,giving the white line.



5A) Convolved with M (Horizontal Stripes)



5B) Convolved with M-transpose (Verticle Stripes)





5C) Convolver with M and M-transpose

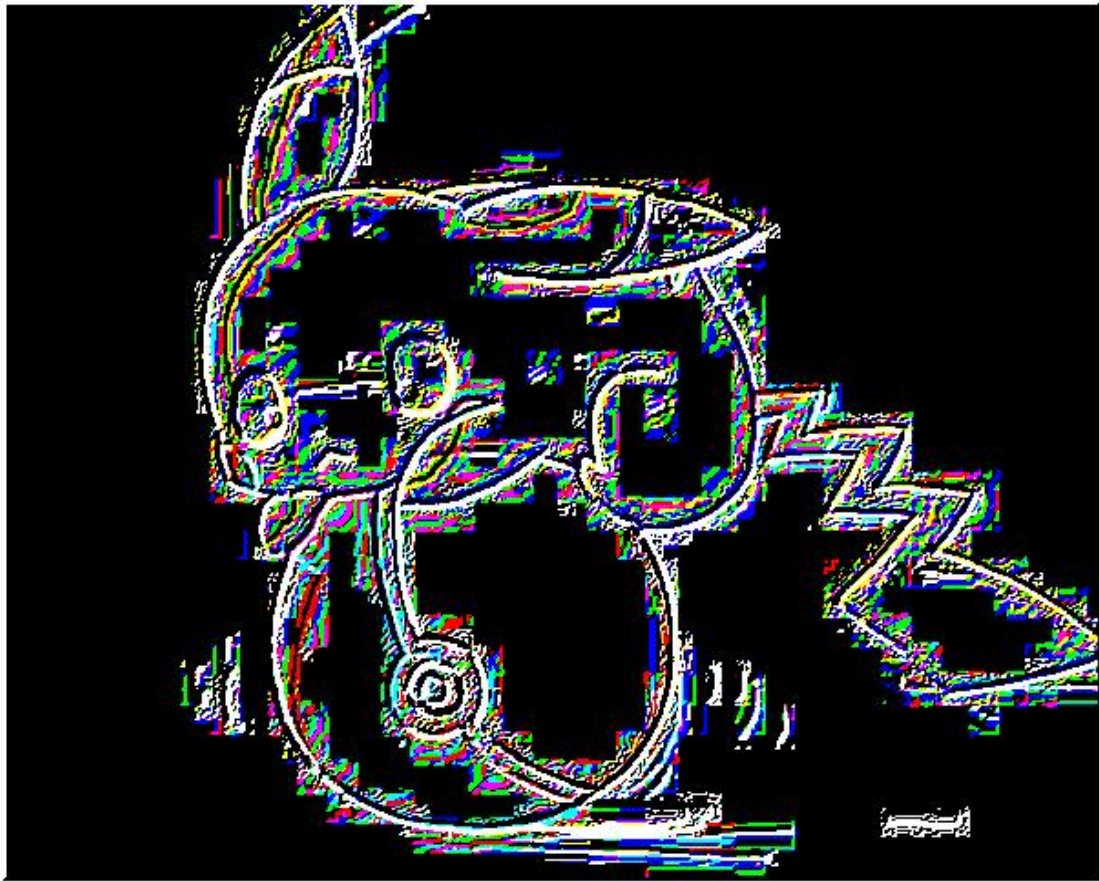


5D) With other 3 images:

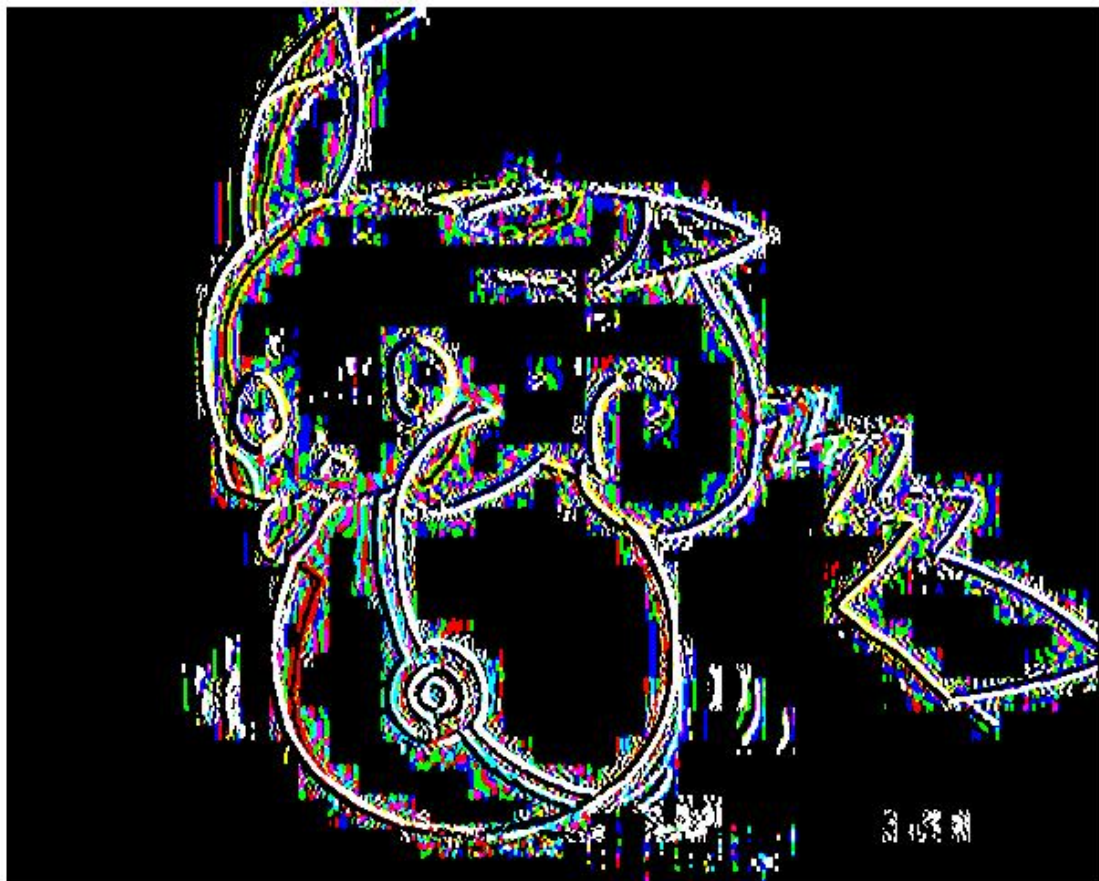




i) Convolved with M (Horizontal Stripes)



ii) Convolved with M-transpose (Verticle Stripes)





iii) Convoluting with M and M-transpose



Other 2 images are vegeta.jpg and a18.jpg, and their results can be seen by replacing the file name in the codes.

## **Problem 6**

### Algorithm

Iterating the F1.jpg over the Faces.jpg and calculating the absolute difference of both matrices' values, the minimum among whome will be the closest possible result.



## **Problem 7**

### **Algorithm**

Here, we exactly need to calculate the impulse function, given the input and output when convolved over by impulse function.

So we are given input= $X$ , output= $Y$  and let impulse fxn be  $M$  matrix.

So  $X * M = Y$

$$M = X^{-1} * Y$$

### **Result & Observation**

Answer Matrix  $M = [1 \quad -3 \quad -3 \quad 4 \quad 4 \quad 5]$