

$$f(x)=0.9x^3-1.4x^2+3x-4$$

$$f'(x)=2.7x^2-2.8x+3$$

$$f''(x)=5.4x-2.8$$

$$f'''(x)=5.4$$

$$f(0.4)=0.9(0.4)^3-1.4(0.4)^2+3(0.4)-4$$

$$f'(0.4)=2.7(0.4)^2-2.8(0.4)+3$$

$$f''(0.4)=5.4(0.4)-2.8$$

$$f'''(0.4)=5.4$$

$$f(x) \approx f(0.4) + f'(0.4)(x-0.4) + \frac{f''(0.4)}{2!}(x-0.4)^2 + \frac{f'''(0.4)}{3!}(x-0.4)^3$$

$$f(x) \approx f(0.4) + f'(0.4)(x-0.4) + \frac{f''(0.4)}{2!}(x-0.4)^2 + \frac{f'''(0.4)}{3!}(x-0.4)^3$$

$$f(x) \approx -3.234 + 3.69(x-0.4) + 0.81(x-0.4)^2 + 0.9(x-0.4)^3$$

b)

$$f(0.5)=1.4e^{0.5}-3.2(0.5)+3.2$$

$$f'(0.5)=1.4e^{0.5}-3.2$$

$$f''(0.5)=1.4e^{0.5}$$

$$f'''(0.5)=1.4e^{0.5}$$

$$(x) \approx f(0.5) + f'(0.5)(x-0.5) + \frac{f''(0.5)}{2!}(x-0.5)^2 + \frac{f'''(0.5)}{3!}(x-0.5)^3$$

$$f(x) \approx 2.108 + 0.7(x-0.5) + 0.35(x-0.5)^2 + 0.2333(x-0.5)^3$$

