

Homework 11

Due Wed Dec. 9 by 11:59 pm

Problem 1 [30 pts]

Use Matlab to make the Bode plots for each below and determine the gain and phase margins.

$$(a) L(s) = \frac{2000}{s(s + 200)}$$

$$(b) L(s) = \frac{100}{s(0.1s + 1)(0.5s + 1)}$$

$$(c) L(s) = \frac{1}{s(s + 1)(0.02s + 1)}$$

Problem 2 [20 pts]

Use Matlab to make the Bode plots for each below and determine the gain and phase margins.

$$(a) L(s) = \frac{(s + 2)}{s(s + 10)(s^2 + 2s + 2)}$$

$$(b) L(s) = \frac{(s + 2)}{s^2(s + 10)(s^2 + 6s + 25)}$$

Problem 3 [40 pts]

Consider the unity feedback system with the open-loop transfer function

$$G(s) = \frac{K}{s(s + 1)[(s^2/25) + 0.4(s/5) + 1]}$$

- (a) Use MATLAB to draw the Bode plots for $G(j\omega)$ assuming $K = 1$.
- (b) What gain K is required for a PM of 45° ? What is the GM for this value of K ?
- (c) What is K_v when the gain K is set for PM = 45° ?
- (d) Create a root locus with respect to K , and indicate the roots for a PM of 45° .

Note for Part (c), K_v is the velocity constant from the steady-state error analysis lecture.