

BİLGİSAYAR MÜHENDİSLİĞİ BÖLÜMÜ  
OLASILIK VE İSTATİSTİK DERSİ ARASINAV SORULARI

Cansu DAL  
18253039  
~~0804~~

$$1) \quad 65 + 105 - 15 = 155 \\ 155 / 250 = \boxed{\frac{31}{50}}$$

$$2) \quad \frac{25}{95} = \boxed{\frac{5}{19}}$$

3)  $x < \text{med} < \text{mod}$  olduğu için sağa eğilimli sola çarpık

$$4) \quad k \cdot \left(\frac{1}{3}\right)^0 + k \cdot \left(\frac{1}{3}\right)^1 + k \cdot \left(\frac{1}{3}\right)^2 + k \cdot \left(\frac{1}{3}\right)^3 = 1$$

$$\frac{k}{1} + \frac{k}{3} + \frac{k}{9} + \frac{k}{27} = 1$$

(27) (9) (3)

$$\frac{40k}{27} = 1$$

$$k = \boxed{\frac{27}{40}}$$

$$5) \quad k=0$$

$$\int_{-\infty}^0 f_x(x) dx + \int_0^1 f_x(x) dx + \int_1^{\infty} f_x(x) dx = 1$$

$$\int_0^1 f_x(x) dx = 1 \Rightarrow k \int_0^1 x - x^2 = k \left( \int_0^1 x - \int_0^1 x^2 \right) = k \left[ \frac{x^2}{2} \Big|_0^1 - \frac{x^3}{3} \Big|_0^1 \right]$$

$$= k \left( \frac{1}{2} - 0 - \left( \frac{1}{3} - 0 \right) \right) = k \cdot \left( \frac{1}{2} - \frac{1}{3} \right) = \frac{k}{6} = 1$$

$$\boxed{k=6}$$



Canlı DAL  
18253039  
~~Canlı~~

$$6) P(0,5 \leq x \leq 0,9) = \int_{0,5}^{0,9} 6(x-x^2)$$

$$6 \cdot \left[ \frac{x^2}{2} \Big|_{0,5}^{0,9} - \frac{x^3}{3} \Big|_{0,5}^{0,9} \right] = 6 \cdot \left[ \left( \frac{0,81}{2} - \frac{0,25}{2} \right) - \left( \frac{0,729}{3} - \frac{0,125}{3} \right) \right]$$

$$= 6 \left( \frac{0,28}{1} - \frac{0,604}{3} \right) = 1,68 - 1,208 = \underline{\underline{0,472}}$$

$$7) E(x) = 1 \cdot \frac{4}{9} + 2 \cdot \frac{2}{9} + 3 \cdot \frac{2}{9} + 4 \cdot \frac{1}{9} = \frac{4}{9} + \frac{4}{9} + \frac{6}{9} + \frac{4}{9} = \frac{18}{9} = 2$$

$$E(x) = \underline{\underline{2}}$$

$$8) E = (y - \mu)^2 = \frac{4}{9} \cdot (1-0)^2 + \frac{2}{9} \cdot (2-0)^2 + \frac{2}{9} \cdot (3-0)^2 + \frac{2}{9} \cdot (4-0)^2 \\ = \frac{4}{9} \cdot 1 + \frac{2}{9} \cdot 4 + \frac{2}{9} \cdot 9 + \frac{2}{9} \cdot 16 = \frac{46}{9}$$

$$E(x) = 2 \quad (E(x))^2 = 4 \quad V(x) = \frac{46}{9} - \frac{4}{1} = \underline{\underline{\frac{16}{9}}}$$

$$9) (2,5)(1,5) + (3,75)(8) + (2,75)(6,5) + (3,25)(2) + (1,75)(3) + \\ (2,25)(5) + (4)(1,5) + (0)(2,5) = 80,625$$

$$\text{Toplam kredi} = 1,5 + 8 + 6,5 + 2 + 3 + 5 + 1,5 + 2,5 = 30$$

$$\text{Ortalama} = 80,625 / 30 = \underline{\underline{2,68}}$$



Canlı DAL

18253039

~~Canlı~~

10)

a) Örnek uzay =  $\{(1,2), (1,5), (2,1), (2,4), (3,3), (4,2), (4,5), (5,1), (5,4), (6,3), (6,6)\}$

b)

$x$	3	6	9	12
$P(x)$	$\frac{2}{12}$	$\frac{5}{12}$	$\frac{4}{12}$	$\frac{1}{12}$

$$E(x) = \sum_{-\infty}^{\infty} P(x) = 3 \cdot \frac{2}{12} + 6 \cdot \frac{5}{12} + 9 \cdot \frac{4}{12} + 12 \cdot \frac{1}{12} = 7$$

$$E(2x-1) = 13$$