

Problem 3.5.2

c)  $\{www : w \in \{a,b\}^*\}$

$k > 0 \quad w \in L$

$|w| \geq k \quad u, v, x, y, z \in \Sigma^*$

$w = uvxyz, |uxy| \leq k, uv \neq \epsilon$

$uv^nxy^n \in L \quad n \geq 0$

$w = a^k b a^k b a^k b$

$uv^2xy^2z = a^{k+p} b a^{k+q} b$

Problem 3.5.5

(a) by applying the Pumping Theorem

$$|vy| = |uv^2xy^2z| - |uvxyz| = |w_{k+2}| - |w_k| = \frac{(k+3)(k+2)}{2} - \frac{(k+1)(k)}{2} = \frac{4k+10}{2} = 2k+5$$

$$|xy| = |uvxyz| - |uxz| = |w_k| - |w_{k-2}| = \frac{(k+1)(k+2)}{2} - \frac{(k-1)(k)}{2} = 2k+1$$

$$|vy| = |uv^2xy^2z| - |uvxyz| = |w_{k+1}| - |w_k| = \frac{(k+2)(k+3)}{2} - \frac{(k+1)(k+2)}{2} = k+2$$

$$|vy| = |uvxyz| - |uxz| = |w_k| - |w_k| = \frac{(k+1)(k+2)}{2} - \frac{(k)(k+1)}{2} = \frac{2k+2}{2} = k+1$$

Problem 3.5.16

(a)  $\{a^m b^n c^p : m=n \text{ or } n=p \text{ or } m=p\}$

bu dil bağımlıdır bağımsızdır

$\{a^n b^n c^n : n, m \in \mathbb{N}\} \cup \{a^n b^m c^n : n, m \in \mathbb{N}\}$

her biri esasen bağımsızdır  $\{a^n b^n : n \in \mathbb{N}\}$

(c)  $\{a^m b^n c^p : m=n \text{ and } n=p \text{ and } m=p\}$

bu dil bağımlıdır bağımsız değildir.

$\{a^n b^n c^n : n \in \mathbb{N}\}$  ile benzerlik gösterir