24784:	Trustworthy	\mathbf{AI}
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Mar 15, 2024

Challenge 1

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• IoU Calculation

IoU is computed following these steps:

- 1. The intersection area is computed by finding the overlapping area between the ground truth box and the predicted box, where we use the relatively small value of each entry of the input arrays to calculate the intersection area.
- 2. The union area is computed by summing the area of the ground truth box and the predicted box while subtracting the union area.
- 3. The IoU scores for each box are calculated by dividing the intersection area with the union area.

The concept is illustrated as follow:

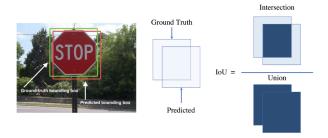


Figure 1: Calculation of IoU (source: Challenge 1 description)

• Results Discussion

The calculations if precision and recall are as follow:

$$precision = \frac{TP}{TP + FP}$$

$$recall = \frac{TP}{TP + FN}$$

With varying IoU thresholds, we can expect that the higher the threshold, the likelihood of FalsePositive instances appearing will decrease due to the increased confidence of the model. This occurs because the criterion for making positive predictions becomes stricter, essentially forcing the model to be more certain about all the positive predictions it makes. Therefore, at IoU thresholds greater than 0.7, we can start to observe a noticeable deviation between the Raw curves and the Orange curves, and the later is calculated by $p(r) = \max_{r' < r} p(r')$. As the

FP rate decreases, at the same level of recall rate, a lower precision could be expected and is understandable. From Table 1, we can see that the average precision (AP) trend reflects our initial assumption about the effect of the IoU threshold. Starting at an IoU threshold of 0.7, we observe a drop in AP, which continues as the threshold increases.

• P-R curves to each IoU

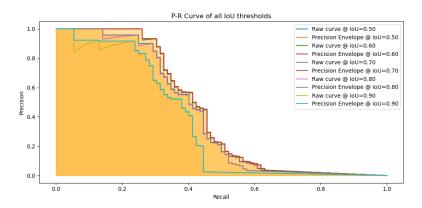


Figure 2: All P-R Curves

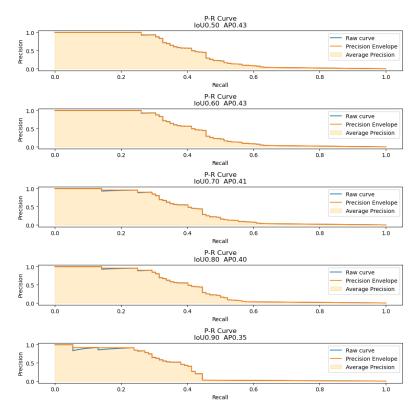


Figure 3: P-R Curves

\bullet IoU Threshold & Average Precision

IoU Threshold	AP
0.50	0.4272559074361477
0.60	0.4272559074361477
0.70	0.40686292416368364
0.80	0.4018855902817313
0.90	0.3466670309329718

Table 1: IoU Threshold vs AP

C1.1 Evaluation on Object Detection

Introduction

- Task: Evaluate the average precision of the data collected from SafeBench.
- Submission: the plotted P-R curve, as well as the average precision at different IoU threshold level.

```
In []: import joblib
import numpy as np
import pandas as pd
from matplotlib import pyplot as plt

In []: # !git clone https://github.com/HenryLHH/24784-c1-data.git
# !cp /content/24784-c1-data/results.pkl ./
# !rm -r /content/24784-c1-data/
```

Load the Detection Results from SafeBench_v2

```
In []: inputs = joblib.load('results.pkl') # move the files to your current folder
inputs.keys() # dict_keys(['image_id', 'predicted_class', 'ground_truth_bbox',

Out[]: dict_keys(['image_id', 'predicted_class', 'ground_truth_bbox', 'predicted_bbo
    x', 'conf_scores', 'num_labels'])
```

Compute the IoU

```
In []:|
        def box_area(box):
            """ Compute the box area, given all the vertices
            # Arguments
                box: (N,4) ndarray
            # Returns
                areas: (N, ) ndarray
            (x1, y1, x2, y2) = box.T
            areas = np.abs((x1-x2) * (y1-y2)) # TODO, compute the rectangle areas base
            return areas # (N, ) ndarray
        def box_iou(box1, box2):
              Compute the iou between box1 and box2
              ONLY consider the SINGLE ground truth, which is a simplified case
              box1: (N, 4) ndarray
              box2: (N, 4) ndarray
              return: (N, ) iou scores
            eps = 1e-7
            a1, a2 = np.split(box1, 2, axis=1) # ground truth boxes
            b1, b2 = np.split(box2, 2, axis=1) # predicted boxes
```

```
# intersections' boundaries
x1 = np.maximum(a1, b1)
x2 = np.minimum(a2, b2)

inter = np.abs((x1[:,0] - x2[:,0])*(x1[:,1] - x2[:,1]))
union = box_area(box1) + box_area(box2) - inter
return inter / (union + eps)

# TODO: get the box iou scores from the function you implemented above
iou scores = box iou(inputs['ground truth bbox'], inputs['predicted bbox'])
```

```
In []: # TODO: get the box iou scores from the function you implemented above
iou_scores = box_iou(inputs['ground_truth_bbox'], inputs['predicted_bbox'])

# Build your dataframe from the dictionary
input_dict = {
        'image_id': inputs['image_id'],
        'predicted_class': inputs['predicted_class'],
        'conf_scores': inputs['conf_scores'],
        'iou_scores': iou_scores,
    }

df = pd.DataFrame.from_dict(input_dict)
df
```

Out[]: image_id predicted_class conf_scores iou_scores
--

	iiiago_ia	prodrotod_ordoo	00111_000100	104_000100
0	0	None	-1.000000	-1.001914
1	1	car	0.671808	-1.223964
2	1	car	0.563249	-1.642660
3	1	car	0.452749	0.800520
4	1	car	0.428004	0.229486
•••				
1631	91	train	0.219339	0.680153
1632	91	bus	0.173378	0.722757
1633	91	person	0.101061	0.203605
1634	91	sink	0.088729	0.044596
1635	91	dining table	0.073306	0.030152

1636 rows × 4 columns

```
In []: df = df[df.conf_scores >= 0] # drop all the frames without detection (conf scole # get all the detection results of stop signs df_stopsign = df.loc[(df.predicted_class=='stopsign')] df_stopsign
```

Out[]:		image_id	predicted_class	conf_scores	iou_scores
	160	7	stopsign	0.071092	0.812147
	345	15	stopsign	0.052572	0.823549
	712	33	stopsign	0.110136	0.814429
	731	34	stopsign	0.159796	0.844884
	772	36	stopsign	0.128940	0.850620
	•••				
	1606	88	stopsign	0.119673	0.025573
	1610	89	stopsign	0.997623	0.932374
	1622	90	stopsign	0.995437	0.923847
	1628	90	stopsign	0.052746	0.032057
	1629	91	stopsign	0.995099	0.614191

66 rows × 4 columns

Compute the Avereage Precision

In []: def compute_ap(df, num_gt, iou_thres):

```
In []: def interp_ap(recall, precision, method = 'interp'):
            """ Compute the average precision, given the recall and precision curves
            # Arguments
                           The recall curve (list)
                recall:
                precision: The precision curve (list),
                methods: 'continuous', 'interp'
            # Returns
                Average precision, precision curve, recall curve
            # TODO: Append sentinel values to beginning and end
            # Recall should start with 0.0 and end with 1.0
            # Precision should start with 1.0 and end with 0.0
            appended_recall = np.concatenate(([0.0], recall, [1.0]))
            appended_prec_input = np.concatenate(([1.0], precision, [0.0]))
            # Compute the precision envelope
            appended_prec = np.flip(np.maximum.accumulate(np.flip(appended_prec_input)
            # Integrate area under curve
            if method == 'interp':
                x = np.linspace(0, 1, 101) # 101-point interp (COCO)
                ap = np.trapz(np.interp(x, appended_recall, appended_prec), x)
            else: # 'continuous'
                i = np.where(appended_recall[1:] != appended_recall[:-1])[0] # points
                ap = np.sum((appended_recall[i + 1] - appended_recall[i]) * appended_p
            return ap, appended_prec_input, appended_prec, appended_recall
```

""" Compute the average precision, given the recall and precision curves

```
# Arguments
                DataFrame inputs containing predicted classes, iou_scores,
   df:
   num_gt:
               The precision curve (list),
   iou_thres: IoU threshold of True Positive (TP) detection
# Returns
   Average precision, precision curve, recall curve
df = df.sort_values(by='conf_scores', ascending=False)
tp_fp = np.arange(1, len(df)+1, 1)
tp = ((df['iou_scores'] >= iou_thres) & (df['predicted_class'] == 'stopsign')
precision = tp / tp_fp # array (N, )
recall = tp / num_gt
                          # array (N, )
ap, prec_raw, prec, recall = interp_ap(recall, precision)
                                                                    # get
return ap, prec_raw, prec, recall
```

Visualization

```
def plot_pr_curves(recall, prec_raw, prec, title = None):
In []:
             """ Visualize the P-R curves
                Visualize the areas under P-R curves
            # plt.figure()
            plt.plot(recall, prec_raw)
            plt.plot(recall, prec)
            plt.fill_between(recall, np.zeros_like(recall), prec, color='orange', alpha
            plt.legend(['Raw curve', 'Precision Envelope', 'Average Precision'])
            plt.title('P-R Curve' + title)
            plt.xlabel('Recall')
            plt.ylabel('Precision')
        def plot_all_pr_curves(recall, prec_raw, prec, threshold):
             """ Visualize the P-R curves
                Visualize the areas under P-R curves all in one plot
            .....
            # plt.figure()
            plt.plot(recall, prec_raw, label='Raw curve @ IoU={:.2f}'.format(threshold
            plt.plot(recall, prec, label = 'Precision Envelope @ IoU={:.2f}'.format(th
            plt.fill_between(recall, np.zeros_like(recall), prec, color='orange', alpha
            plt.legend(['Raw curve', 'Precision Envelope', 'Average Precision'])
            # plt.title('P-R Curve')
            plt.xlabel('Recall')
            plt.ylabel('Precision')
```

Execute the AP calculation

```
In []: # Traverse over IoU threshold, get AP@[0.5:0.1:0.9]
    plt.figure(figsize=(10, 10))
    logs = {}
    for i, iou_thres in enumerate(np.arange(0.5, 1.0, 0.1)):
        ap, prec_raw, prec, recall = compute_ap(df, inputs['num_labels'], iou_three
        print('IoU Threshold: {:.2f}'.format(iou_thres), ' | AP@{:.2f}'.format
        logs['IoU Threshold: {:.2f}'.format(iou_thres)] = ap
        plt.subplot(len(np.arange(0.5, 1.0, 0.1)), 1, i+1)
        plot_pr_curves(recall, prec_raw, prec, title="\n" + f"IoU{iou_thres:.2f} /
        plt.tight_layout()
```

```
plt.show()
# plotting all the results in the same plot
plt.figure(figsize=(10, 5))
for i, iou_thres in enumerate(np.arange(0.5, 1.0, 0.1)):
     ap, prec_raw, prec, recall = compute_ap(df, inputs['num_labels'], iou_thres
     print('IoU Threshold: {:.2f}'.format(iou_thres), ' |
                                                                            AP@{:.2f}'.format
     logs['IoU Threshold: {:.2f}'.format(iou_thres)] = ap
     plot_all_pr_curves(recall, prec_raw, prec, threshold=iou_thres)
plt.legend()
plt.title('P-R Curve of all IoU thresholds')
plt.tight_layout()
plt.show()
IoU Threshold: 0.50
                                 AP@0.50 0.4272559074361477
IoU Threshold: 0.60
                                 AP@0.60 0.4272559074361477
IoU Threshold: 0.70
                                 AP@0.70 0.40686292416368364
IoU Threshold: 0.80
                                 AP@0.80 0.4018855902817313
IoU Threshold: 0.90
                                 AP@0.90 0.3466670309329718
                                               P-R Curve
                                            IoU0.50 AP0.43
  1.0
                                                                                  Raw curve
                                                                                  Precision Envelope
 0.5
                                                                                  Average Precision
  0.0
                         0.2
        0.0
                                         0.4
                                                          0.6
                                                                           0.8
                                                                                           1.0
                                                 Recall
                                               P-R Curve
                                            IoU0.60 AP0.43
  1.0
                                                                                  Raw curve
                                                                                  Precision Envelope
  0.5
                                                                                  Average Precision
  0.0
        0.0
                         0.2
                                         0.4
                                                          0.6
                                                                           0.8
                                                                                           1.0
                                                 Recall
                                               P-R Curve
                                            IoU0.70 AP0.41
  1.0
                                                                                  Raw curve
Precision
9.0
                                                                                  Precision Envelope
                                                                                  Average Precision
  0.0
        0.0
                         0.2
                                         0.4
                                                          0.6
                                                                           0.8
                                                                                           1.0
                                                 Recall
                                               P-R Curve
                                            IoU0.80 AP0.40
  1.0
                                                                                  Raw curve
                                                                                  Precision Envelope
  0.5
                                                                                  Average Precision
  0.0
                         0.2
                                         0.4
        0.0
                                                          0.6
                                                                           0.8
                                                                                           1.0
                                                 Recall
                                               P-R Curve
                                            IoU0.90 AP0.35
  1.0
                                                                                   Raw curve
Precision
                                                                                   Precision Envelope
 0.5
                                                                                  Average Precision
  0.0
        0.0
                         0.2
                                         0.4
                                                                           0.8
                                                          0.6
                                                                                           1.0
                                                 Recall
```

```
      IoU Threshold:
      0.50
      |
      AP@0.50
      0.4272559074361477

      IoU Threshold:
      0.60
      |
      AP@0.60
      0.4272559074361477

      IoU Threshold:
      0.70
      |
      AP@0.70
      0.40686292416368364

      IoU Threshold:
      0.80
      |
      AP@0.80
      0.4018855902817313

      IoU Threshold:
      0.90
      |
      AP@0.90
      0.3466670309329718
```

