

Indian Institute of Technology Dharwad

CS 202: Assignment 2

Release date: 18 February 2022
Submission Deadline : 2200 hours, 25 February 2022.

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1. Let G be the grammar given as follows:

$$\begin{aligned} S &\rightarrow aB \mid bA \\ A &\rightarrow a \mid aS \mid bAA \\ B &\rightarrow b \mid bS \mid aBB \end{aligned}$$

- (a) For the string $aaabbabbba$ find:
 - i. a leftmost derivation
 - ii. a rightmost derivation
 - iii. a parse tree
- (b) Is the grammar given above unambiguous? Justify.

2. Write context-free grammar for the following languages:

- (a) $\{w \in \{0,1\}^* \mid w \text{ contains at least three } 1\text{'s}\}$
- (b) $\{w \in \{0,1\}^* \mid \text{length of } w \text{ is odd and middle symbol is } 0\}$
- (c) $\{a^i b^j c^k \mid i, j, k \geq 0, i + j = k\}$

3. Construct a PDA equivalent to the following grammar:

$$\begin{aligned} S &\rightarrow aAA \\ A &\rightarrow aS \mid bS \mid a \end{aligned}$$

4. Give a context-free grammar for generating regular expressions defined over alphabet $\Sigma = \{a, b\}$.

Optional: Can you write a program to translate regular expression to finite automaton. Firstly, you need to generate a CFG for regular expressions, write a parser and finally the automaton-generating routines.

5. Show that if all productions of a CFG G are of the form $A \rightarrow wB$ or $A \rightarrow w$, then $L(G)$ is a regular set.
 6. Construct a CFG equivalent to the NPDA shown in Figure.1, using the algorithm done in the class.
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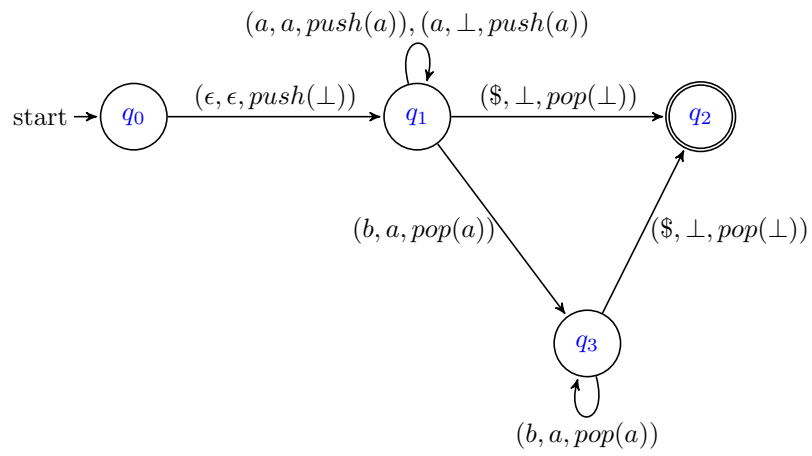


Figure 1: NPDA