

## Digital Systems

### Assignment – 1

**Q-1** Which of the following is an invalid state in an 8-4-2-1 Binary Coded Decimal counter. [1 Mark]

- a) 1 0 0 0      b) 1 0 0 1  
c) 0 0 1 1      d) 1 1 0 0

**Q-2**  $f(A,B,C,D) = \prod M(0,1,3,4,5,7,9,11,12,13,14,15)$  is a maxterm representation of a Boolean function  $f(A,B,C,D)$  where  $A$  is the MSB and  $D$  is the LSB. The equivalent minimized representation of this function is [2 Mark]

- a)  $(A + \bar{C} + D)(\bar{A} + B + D)$   
b)  $\bar{A}\bar{C}D + \bar{A}BD$   
c)  $\bar{A}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}BC\bar{D}$   
d)  $(B + \bar{C} + D)(A + \bar{B} + \bar{C} + D)(\bar{A} + B + C + D)$

**Q-3** [1 Mark]

The Boolean expression  $\overline{(a + b + c + d) + (b + c)}$  Simplifies to

- a) 1      b)  $\overline{a.b}$   
c)  $a.b$       d) 0

**Q-4** [2 Mark]

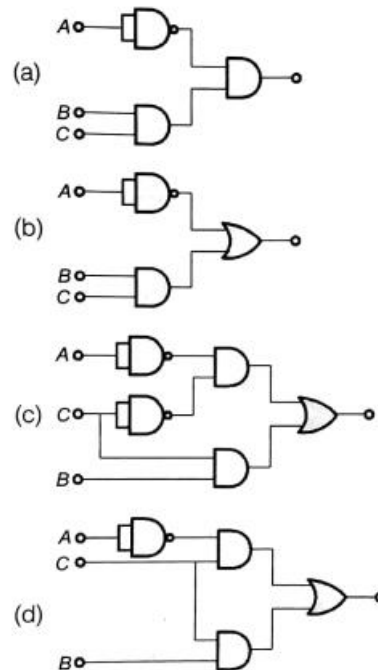
Digital input signals  $A, B, C$  with  $A$  as the MSB and  $C$  as the LSB are used to realize the Boolean function  $F = m_0 + m_2 + m_3 + m_5 + m_7$ , where  $m_i$  denotes the  $i^{\text{th}}$  minterm. In addition,  $F$  has a don't care for  $m_1$ . The simplified expression for  $F$  is given by

- a)  $\bar{A}\bar{C} + \bar{B}C + AC$   
b)  $\bar{A} + C$   
c)  $\bar{C} + A$   
d)  $\bar{A}C + BC + A\bar{C}$

**Q-5** [1 Mark]

Which of the following logic circuits is a realization of the function  $F$  whose Karnaugh map is shown in figure.

C \ AB	00	01	11	10
0	1	1		
1		1	1	



**Q-6** [1 Mark]

The range of signed decimal numbers that can be represented by 6-bit 1's complement number is

- a) -31 to +31      b) -63 to +63  
c) -64 to +63      d) -32 to +31

**Q-7** [2 Mark]

11001, 1001 and 111001 correspond to the 2's complement representation of which one of the following sets of number?

- a) 25, 9 and 57 respectively  
b) -6, -6 and -6 respectively  
c) -7, -7 and -7 respectively  
d) -25, -9 and -57 respectively

**Q-8** [2 Mark]

Decimal 43 in Hexadecimal and BCD number system is respectively

- a) B2, 0100 0011      b) 2B, 0100 0011  
c) 2B, 0011 0100      d) B2, 0100 0100

**Q-9** [2 Mark]

A new Binary coded Pentary (BCP) number system is proposed in which every digit of a base -5 number is represented by its corresponding 3-bit binary code. For example, the base -5 number 24 will be

represented by its BCP code 010100. In this numbering system, the BCP code 100010011001 corresponds to the following number in base -5 system

- a) 423
- b) 1324
- c) 2201
- d) 4231

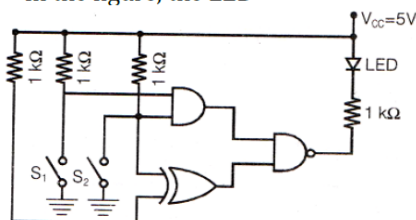
#### Q-10 [1 Mark]

The Boolean express to  $(X + Y)(X + \bar{Y}) + (X + \bar{Y}) + \bar{X}$  simplifies to

- a) X
- b) Y
- c) XY
- d) X + Y

#### Q-11 [2 Mark]

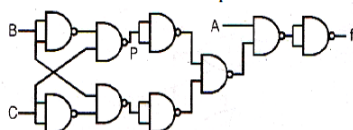
In the figure, the LED



- a) emits light when both  $S_1$  and  $S_2$  are closed
- b) emits light when both  $S_1$  and  $S_2$  are open.
- c) emits light when only of  $S_1$  and  $S_2$  is closed.
- d) does not emit light, irrespective of the switch positions.

#### Q-12 [2 Mark]

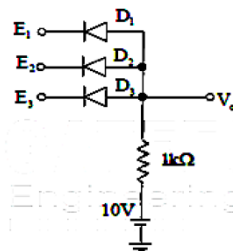
The point P in the following figure is stuck at -1 The output f will be



- a) ABC
- b) A
- c) ABC
- d)  $\bar{A}$

#### Q-13 [1 Mark]

In the circuit shown, diodes  $D_1, D_2$  and  $D_3$  are ideal, and the inputs  $E_1, E_2$  and  $E_3$



- a) 3 input OR gate
- b) 3 input NOR gate
- c) 3 input AND gate
- d) 3 input XOR gate

#### Q-14 [2 Mark]

The product of sum expression of a Boolean function  $F(A, B, C)$  of three variables is given by

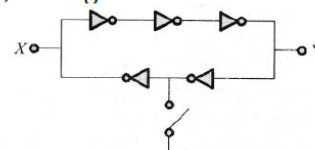
$$F(A, B, C) = (A + B + \bar{C})(A + \bar{B} + \bar{C})(\bar{A} + B + C)(\bar{A} + \bar{B} + \bar{C})$$

The canonical sum of product expression of  $F(A, B, C)$  is given by

- a)  $\bar{A}\bar{B}C + \bar{A}BC + A\bar{B}\bar{C} + ABC$
- b)  $\bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C}$
- c)  $ABC + \bar{A}\bar{B}\bar{C} + \bar{A}BC + A\bar{B}\bar{C}$
- d)  $\bar{A}\bar{B}\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + ABC$

#### Q-15 [1 Mark]

In the circuit shown, the switch is momentarily closed and then opened. Assuming the logic gates to have equal non-zero delay, at steady state, the logic states of X and Y are



- a) X is latched, Y toggles continuously
- b) X and Y are both latched
- c) Y is latched, X toggles continuously
- d) X and Y both toggle continuously

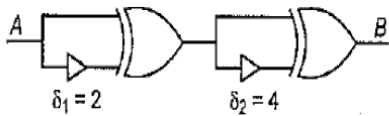
#### Q-16 [1 Mark]

The range of integers that can be represented by an  $n$  bit 2's complement number system is

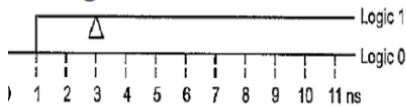
- a)  $-2^{n-1}$  to  $(2^{n-1}-1)$
- b)  $-(2^{n-1}-1)$  to  $(2^{n-1}-1)$
- c)  $-2^{n-1}$  to  $2^{n-1}$
- d)  $-(2^{n-1}+1)$  to  $(2^{n-1}-1)$

**Q-17 [2 Mark]**

Consider the following circuit compose of XOR gates and non-inverting buffers:



The non-inverting buffers have delays  $\delta_1 = 2\text{ns}$  and  $\delta_2 = 4\text{ns}$  as shown in the figure. Both XOR gates and all wires have zero delay. Assume that all gate inputs, output and wires are stable at logic level 0 at time 0. If the following waveform is applied at input A, how many transition(s) (change of logic levels) occur(s) at B during the interval from 0 to 10 ns?

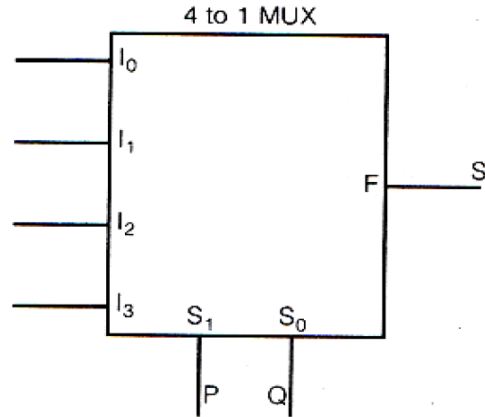


- a) 1
- b) 2
- c) 3
- d) 4

**Q-18 [2 Mark]**

Note: Mux/Demux will be covered soon

Figure shows a 4 to 1 MUX to be used to implement the sum  $S$  of a 1-bit full adder with input bits  $P$  and  $Q$  and the carry input  $C_{in}$ . Which of the following combinations of inputs to  $I_0, I_1, I_2$  and  $I_3$  of the MUX will realize the sum  $S$ ?

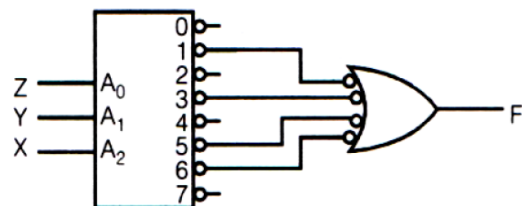


- a)  $I_0 = I_1 = C_{in}; I_2 = I_3 = \bar{C}_{in}$
- b)  $I_0 = I_1 = \bar{C}_{in}; I_2 = I_3 = C_{in}$
- c)  $I_0 = I_3 = C_{in}; I_1 = I_2 = \bar{C}_{in}$
- d)  $I_0 = I_3 = \bar{C}_{in}; I_1 = I_2 = C_{in}$

**Q-19 [2 Mark]**

Note: Encoder/Decoder will be covered soon

A 3 line to 8 line decoder, with active low outputs is used to implement a 3-variable Boolean function as shown in the figure



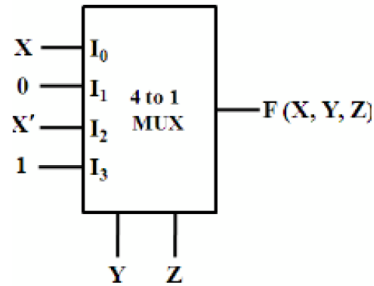
The simplified form of Boolean function  $F(A,B,C)$  implemented in 'Product of Sum' form will be

- a)  $(X + Z) \cdot (\bar{X} + \bar{Y} + \bar{Z}) \cdot (Y + Z)$
- b)  $(\bar{X} + \bar{Z}) \cdot (X + Y + Z) \cdot (\bar{Y} + \bar{Z})$
- c)  $(\bar{X} + \bar{Y} + Z) \cdot (\bar{X} + Y + Z) \cdot (X + \bar{Y} + Z) \cdot (X + Y + \bar{Z})$
- d)  $(\bar{X} + \bar{Y} + Z) \cdot (\bar{X} + Y + \bar{Z}) \cdot (X + \bar{Y} + Z) \cdot (X + \bar{Y} + \bar{Z})$

**Q-20 [2 Mark]**

Note: Mux/Demux will be covered soon

A 4 to 1 multiplexer to realize a Boolean function  $F(X, Y, Z)$  is shown in the figure below. The inputs  $Y$  and  $Z$  are connected to the selectors of the MUX ( $Y$  is more significant). The canonical sum-of product expression for  $F(X, Y, Z)$  is



- a)  $\sum m(2, 3, 4, 7)$       b)  $\sum m(1, 3, 5, 7)$   
c)  $\sum m(0, 2, 4, 6)$       d)  $\sum m(2, 3, 5, 6)$