



Electronic Devices

Tutorial-3: PN Junctions

Q. 1

Consider a silicon pn junction which is in equilibrium condition at room temperature having $N_a = 5 \times 10^{17} / \text{cm}^3$ and $N_d = 10^{16} / \text{cm}^3$

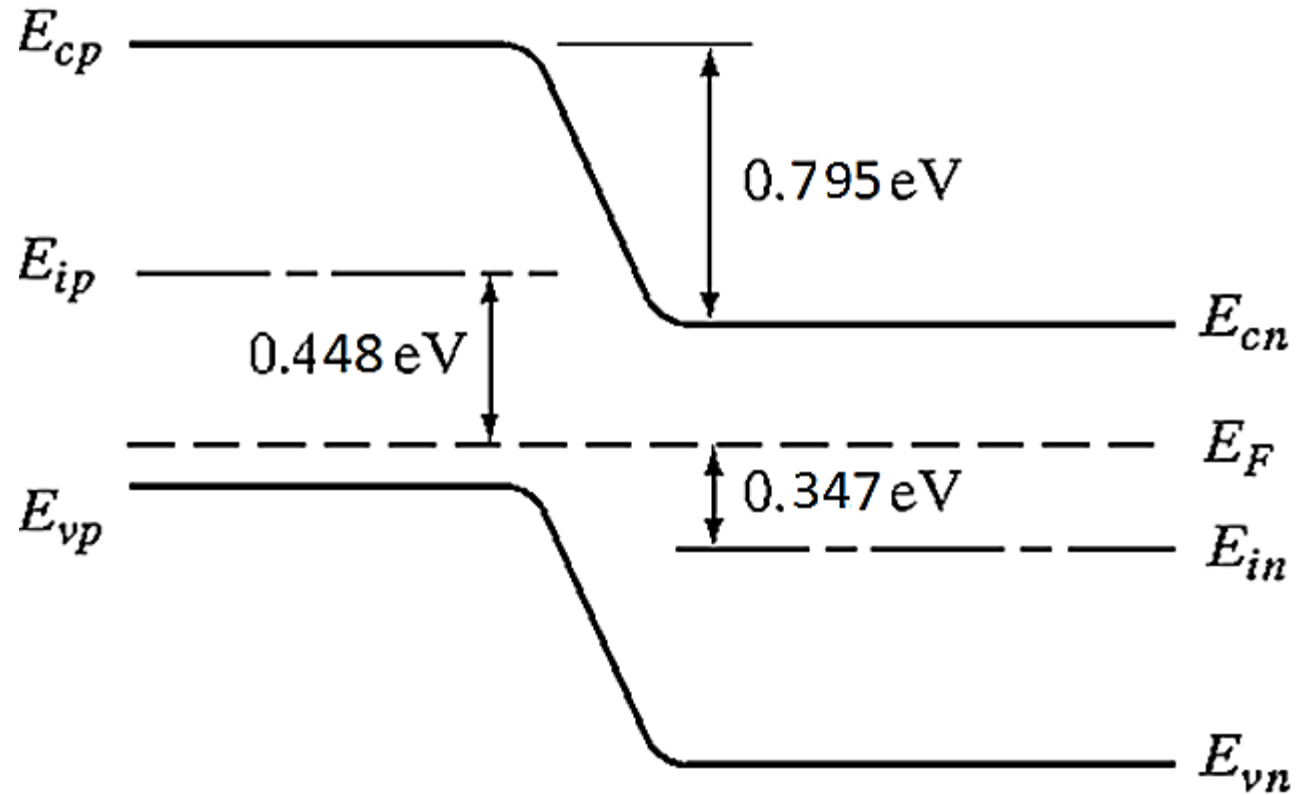
- (a) Calculate the built-in potential at the junction
- (b) Find out the Fermi level positions for p and n-region w.r.t the Fermi energy level of the junction
- (c) Draw the equilibrium band diagram for the pn junction

$$V_0 = 0.795V$$

$$E_p - E_F = 0.4486eV$$

$$E_F - E_n = 0.347eV$$

(c) The band diagram at equilibrium,



Q. 2

A GaAs p-n junction has doping concentrations of $N_d = 5 \times 10^{16}/\text{cm}^3$ and $N_a = 5 \times 10^{15}/\text{cm}^3$. Consider that the junction is not biased and at room temperature. Find out the values of width of transition region in n and p-region (x_{n0} , x_{p0}), the total width of depletion region, W and the value of maximum electric field developed at the junction, E_{max} . Given that the dielectric constant of GaAs, $\epsilon = 12.9$ and $n_i = 1.8 \times 10^6/\text{cm}^3$

$$W = 6.1 \times 10^{-5} \text{ cm}$$

$$x_{n0} = 5.55 \times 10^{-6} \text{ cm}$$

$$x_{p0} = 5.55 \times 10^{-5} \text{ cm}$$

$$E_0 = -3.889 \times 10^4 \text{ V/cm}$$

Q. 3

A Si p⁺-n junction, has a donor doping of $5 \times 10^{16} \text{ cm}^{-3}$ on the n side and a cross sectional area of 10^{-3} cm^2 . If $\tau_p = 1 \text{ } \mu\text{s}$ and $D_p = 10 \text{ cm}^2/\text{s}$, calculate the current with a forward bias of 0.5 V and a reverse bias of 0.6V at 300 K.

Sol.

Current under forward bias:

$$I = q \cdot A \cdot \frac{D_p}{L_p} \cdot p_n \cdot e^{\frac{q \cdot V}{kT}} = q \cdot A \cdot \frac{D_p}{\sqrt{D_p \cdot \tau_p}} \cdot \frac{n_i^2}{n_n} \cdot e^{\frac{q \cdot V}{kT}}$$

$$I = 1.6 \cdot 10^{-19} \text{C} \cdot 10^{-3} \text{cm}^2 \cdot \frac{10 \frac{\text{cm}^2}{\text{s}}}{\sqrt{10 \frac{\text{cm}^2}{\text{s}} \cdot 10^{-6} \text{s}}} \cdot \frac{(1.5 \cdot 10^{10} \frac{1}{\text{cm}^3})^2}{5 \cdot 10^{16} \frac{1}{\text{cm}^3}} \cdot e^{\frac{0.5 \text{eV}}{0.0259 \text{eV}}} = 0.55 \mu\text{A}$$

Current under reverse bias:

$$I = q \cdot A \cdot \frac{D_p}{L_p} \cdot p_n = q \cdot A \cdot \frac{D_p}{\sqrt{D_p \cdot \tau_p}} \cdot \frac{n_i^2}{n_n}$$

As the reverse bias is $\gg 3kT$

$$I = 2.25 \times 10^{-15} \text{ A}$$

Q. 4

A Si p-n junction with cross sectional area $A = 0.001 \text{ cm}^2$ is formed with $N_a = 10^{15}/\text{cm}^3$ and $N_d = 10^{20}/\text{cm}^3$. Calculate:

- (a) Contact Potential
- (b) Space charge width at equilibrium
- (c) Current with forward bias of 0.7 V. Assume that the current is diffusion dominated and the mobilities of electron and hole are $1350 \text{ cm}^2/\text{V-s}$ and $450 \text{ cm}^2/\text{V-s}$ respectively, the minority carriers lifetime 2.5 ms. Which carriers contributes more current?

Sol.

$$V_0 = \frac{kT}{q} \ln\left(\frac{N_a N_d}{n_i^2}\right) = 0.0259 \times \ln\left(\frac{10^{15} \times 10^{20}}{(1.5 \times 10^{10})^2}\right)$$

$$= 0.873 \text{ V}$$

$$W = \left[\frac{2\varepsilon V_0}{q} \left(\frac{N_a + N_d}{N_a N_d} \right) \right]^{1/2}$$

$$W = \left[\frac{2 \times 8.85 \times 10^{-14} \times 11.8 \times 0.873}{1.6 \times 10^{-19}} \left(\frac{10^{20} + 10^{15}}{10^{20} \times 10^{15}} \right) \right]^{1/2}$$

$$W = \left[\frac{2 \times 8.85 \times 10^{-14} \times 12.9 \times 0.873}{1.6 \times 10^{-19}} \left(\frac{10^{20} + 10^{15}}{10^{20} \times 10^{15}} \right) \right]^{1/2}$$

$$= 1.06 \times 10^{-4} \text{ cm}$$

Sol.

$$I_D = q \cdot A \cdot \left(\frac{D_p}{L_p} p_{n0} + \frac{D_n}{L_n} n_{p0} \right) (e^{\frac{V_f}{V_T}} - 1)$$

Since $p_{n0} \ll n_{p0}$, as $N_A \ll N_D$

Current will be majorly contributed by the diffusion of electrons in p-region

$$D_n = \mu_n V_T = 1350 \times 0.026 = 35.1 \text{ cm}^2/\text{s}$$

$$L_n = \sqrt{D_n \tau_n} = \sqrt{35.1 \times 2.5 \times 10^{-3}} = 0.296 \text{ cm}$$

$$I \approx 1.6 \times 10^{-19} \times 0.001 \times \frac{35.1}{0.296} \times \left(\frac{(1.5 \times 10^{10})^2}{10^{15}} \right) \times (e^{\frac{0.7}{0.026}} - 1)$$

$$I \approx (4.26 \times 10^{-15})(4.92 \times 10^{11})\text{A} = 2.1 \text{ mA}$$