

End-Sem Answer Keys

Sol.1)

Given $R = 2 \text{ k}\Omega$

$$L = 200 \mu\text{m}$$

$$A = 10^{-6} \text{ cm}^2$$

$$\mu_n = 8000 \text{ cm}^2/\text{V}\cdot\text{s}$$

$$\text{Doping efficiency} = 90\%$$

$$\rho = \frac{R \times A}{L} = \frac{2 \times 10^3 \times 10^{-6}}{200 \times 10^{-4}}$$

$$\rho = 0.1 \Omega\text{-cm}$$

$$\therefore \boxed{\sigma = 10 \text{ S/cm}} \quad \text{--- 1m}$$

$$\sigma = \mu n e \Rightarrow 10 = 8000 \times n \times 1.6 \times 10^{-19}$$

$$\Rightarrow \boxed{n = 7.8125 \times 10^{15} / \text{cm}^3} \quad \text{--- 0.5m}$$

Since doping efficiency, $\eta = 90\% = \frac{n}{N_D}$

$$\Rightarrow N_D = \frac{7.8125 \times 10^{15}}{90} \times 100$$

$$\Rightarrow \boxed{N_D = 8.68 \times 10^{15} / \text{cm}^3} \quad \text{--- 0.5m}$$

sol-2) Given, $N_D = 3 \times 10^{15} \text{ /cm}^3$

$n_i = n_o = p_o = 5\% \text{ of } 3 \times 10^{15} \text{ /cm}^3$

$\Rightarrow \boxed{n_i = n_o = p_o = 1.5 \times 10^{14} \text{ /cm}^3}$

We know, $n_i(T) = \sqrt{N_c N_v} e^{-E_g / 2kT}$ — 1m

$n_i(300) = 2.43 \times 10^{13} \text{ /cm}^3$

$n_i(T) = 1.5 \times 10^{14} \text{ /cm}^3$

$\frac{n_i(T)}{n_i(300)} = \frac{1.5 \times 10^{14}}{2.43 \times 10^{13}} = \left(\frac{T}{300}\right)^{3/2} e^{-E_g / 2k \left(\frac{1}{T} - \frac{1}{300}\right)}$

$\Rightarrow 6.17 = \left(\frac{T}{300}\right)^{3/2} e^{-3882.4 \left(\frac{1}{T} - \frac{1}{300}\right)}$ — 1.5m

This equation has a non-trivial solution and can be found through numerical methods or hit-trial method.

$\boxed{T \approx 580 \text{ K}}$ — 0.5m

sol-3) a) The built-in potential is the area under the triangle

$V_0 = \frac{1}{2} E_m W = \frac{1}{2} E_m (x_n - x_p)$

$$\Rightarrow V_0 = \frac{1}{2} \times 10^4 \times 1 \times 10^{-4}$$

$$\Rightarrow \boxed{V_0 = 0.5 \text{ V}} \quad \text{--- 1m}$$

$$b) \quad \boxed{\frac{N_A}{N_D} = \frac{x_n}{x_p} = \frac{0.4}{0.6} = \frac{2}{3}} \quad \text{--- 1m}$$

$$c) \quad E_m = \frac{q}{\epsilon} N_A x_p \quad \text{[By Poisson's Equation]}$$

$$\Rightarrow N_A = \frac{\epsilon E_m}{q x_p} = \frac{8.85 \times 10^{-14} \times 11.8 \times 10^4}{1.6 \times 10^{-19} \times 0.6 \times 10^{-4}}$$

$$\Rightarrow \boxed{N_A = 10.87 \times 10^{14} \text{ cm}^{-3}} \quad \text{--- 1.5m}$$

$$\boxed{N_D = \frac{3}{2} N_A = 1.63 \times 10^{15} \text{ cm}^{-3}} \quad \text{--- 1.5m}$$

Ans 4 a) EB - reverse biased } --- 0.5m
CB - reverse biased }

\therefore Cut-off (npn BJT) --- 0.5m

b) EB - reverse biased } --- 0.5m

CB- forward biased -

\therefore Reverse active (npn BJT) - 0.5m

sol. 5)

a) $C_{ox} = 0.34 \mu F/cm^2$

\hookrightarrow From the C-V plot

$$\epsilon_{ox} = \frac{C_{ox}}{C_{ox}} = \frac{3.9 \times 8.85 \times 10^{-14}}{0.34 \times 10^{-6}}$$

$\Rightarrow \boxed{t_{ox} = 1.015 \times 10^{-6} \text{ cm}} - 1m$

b) $C_{min} = 0.24 \mu F/cm^2$

$$C_{min} = \frac{C_{ox} \cdot C_{d,min}}{C_{ox} + C_{d,min}}$$

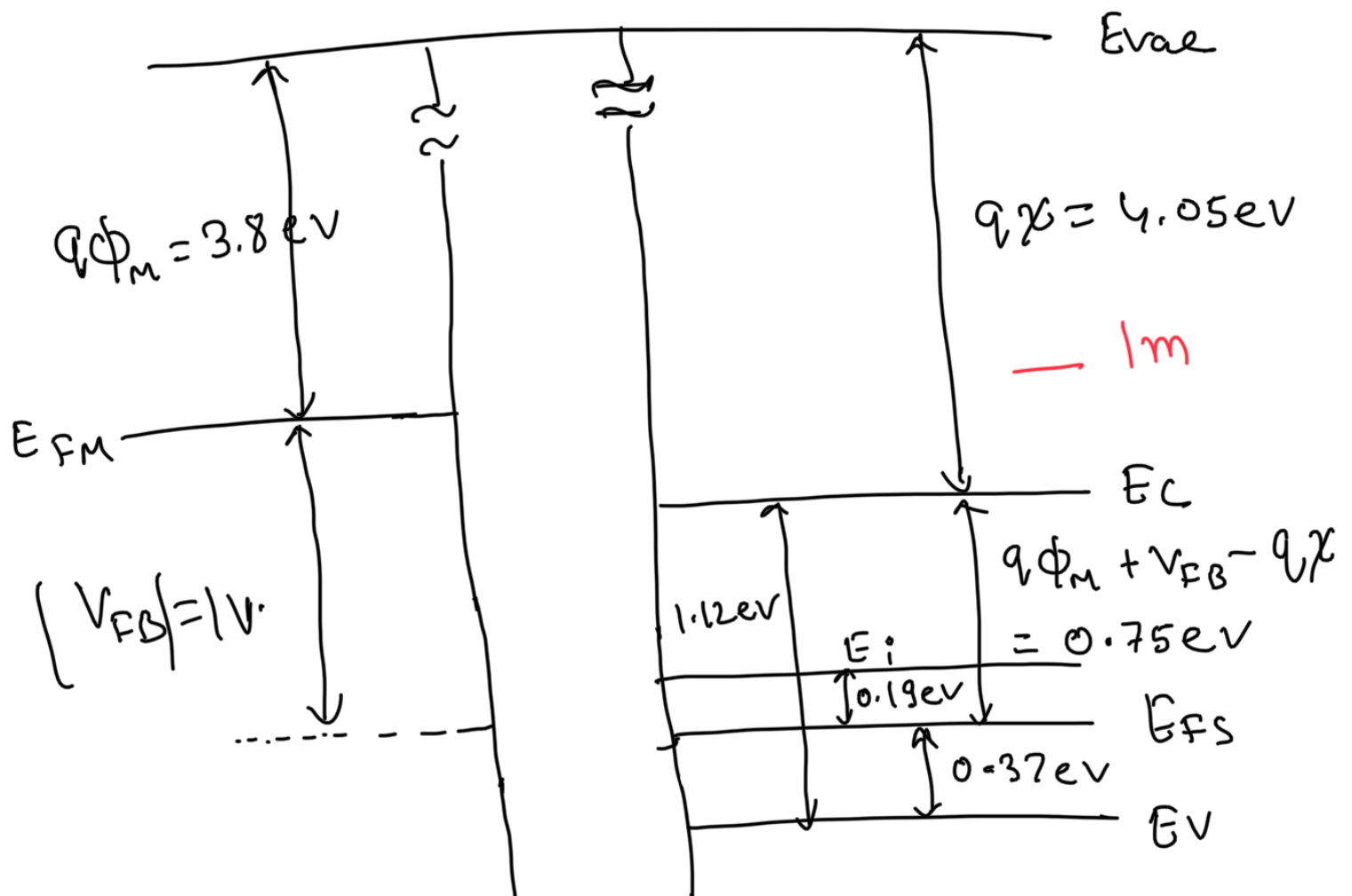
$$\Rightarrow 0.24 \times 10^{-6} = \frac{0.34 \times 10^{-6} \times C_{d,min}}{0.34 \times 10^{-6} + C_{d,min}}$$

$\Rightarrow \boxed{C_{d,min} = 0.816 \mu F/cm^2} - 1m$

$$W_{max} = \frac{\epsilon_{SiO_2}}{C_{d,min}} = \frac{11.8 \times 8.85 \times 10^{-14}}{0.816 \times 10^{-6}}$$

$$\Rightarrow W_{\max} = 1.279 \times 10^{-6} \text{ cm} \quad \text{--- Im}$$

c) The given band structure is as follows:



$$E_i - E_F = 0.19 = kT \ln \left(\frac{N_A}{n_i} \right)$$

Assuming RT, $n_i(\text{Si}) = 1.5 \times 10^{10} / \text{cm}^3$

$$N_A = n_i e^{0.19/0.026}$$

$$\Rightarrow N_A = 2.23 \times 10^{13} / \text{cm}^3 \quad \text{--- Im}$$

Sol. 6) We know

$$I_E = I_{ES} (e^{V_{EB}/V_T} - 1)$$

If $V_{EB} \gg V_T$, then $e^{V_{EB}/V_T} \gg 1$

$$I_E = I_{ES} e^{V_{EB}/V_T}$$

$$\text{If } I_E' = 2 I_E$$

$$\therefore \frac{I_E'}{I_E} = 2 = \frac{e^{V_{EB}'/V_T}}{e^{V_{EB}/V_T}}$$

$$\Rightarrow e^{(V_{EB}' - V_{EB})/V_T} = 2$$

$$\Rightarrow \frac{V_{EB}' - V_{EB}}{V_T} = \ln 2$$

$$\Rightarrow V_{EB}' = V_{EB} + V_T \ln 2$$

$$\Rightarrow \boxed{V_{EB}' = V_{EB} + 0.018 \text{ V}} \quad - 2m$$

Sol. 7)

$$I_D = I_0 (e^{V_g/V_T} - 1)$$

$$\sim I_0 e^{V_g/V_T}$$

$$\therefore V_g \gg V_T$$

$$\Rightarrow 50 \times 10^{-3} = I_0 e^{0.7/0.026}$$

$$\Rightarrow I_0 = \frac{50 \times 10^{-3}}{4.926 \times 10^{11}}$$

$$\Rightarrow \boxed{I_0 = 1.014 \times 10^{-13} \text{ A}} \text{ — 2m}$$

Sol. 8)

$$I_{D, \text{sat}} = \mu_n C_{ox} \frac{Z}{2L} (V_{GS} - V_{TH})^2$$

$$= 450 \times \frac{3.9 \times 8.85 \times 10^{-14}}{35 \times 10^{-7}} \times \frac{30}{2 \times 2} (4 - 0.8)^2$$

$$z) \boxed{I_{D, \text{sat}} = 3.408 \text{ mA}} \text{ — 2m}$$

$$g_m = \frac{\partial I_{D, \text{sat}}}{\partial V_{GS}} = \mu_n C_{ox} \frac{Z}{L} (V_{GS} - V_{TH})$$

$$= 450 \times \frac{3.9 \times 8.85 \times 10^{-14}}{35 \times 10^{-7}} \times \frac{30}{2} (4 - 0.8)$$

$$\boxed{g_m = 2.12 \text{ mA/V}} \text{ — 2m}$$

$$\int \partial_m = 2.15 \text{ m}^2 \text{ v} \quad \text{---}$$