

# Lecture Notes on Operating Systems

## Practice Problems: Concurrency

1. Answer yes/no, and provide a brief explanation.

(a) Is it necessary for threads in a process to have separate stacks?

(b) Is it necessary for threads in a process to have separate copies of the program executable?

**Ans:**

(a) Yes, so that they can have separate execution state, and run independently.

(b) No, threads share the program executable and data.

2. Can one have concurrent execution of threads/processes without having parallelism? If yes, describe how. If not, explain why not.

**Ans:**

Yes, by time-sharing the CPU between threads on a single core.

3. Consider a multithreaded webserver running on a machine with  $N$  parallel CPU cores. The server has  $M$  worker threads. Every incoming request is put in a request queue, and served by one of the free worker threads. The server is fully saturated and has a certain throughput at saturation. Under which circumstances will increasing  $M$  lead to an increase in the saturation throughput of the server?

**Ans:** When  $M < N$  and the workload to the server is CPU-bound.

4. Consider a process that uses a user level threading library to spawn 10 user level threads. The library maps these 10 threads on to 2 kernel threads. The process is executing on a 8-core system. What is the maximum number of threads of a process that can be executing in parallel?

**Ans:** 2

5. Consider a user level threading library that multiplexes  $N > 1$  user level threads over  $M \geq 1$  kernel threads. The library manages the concurrent scheduling of the multiple user threads that map to the same kernel thread internally, and the programmer using the library has no visibility or control on this scheduling or on the mapping between user threads and kernel threads. The  $N$  user level threads all access and update a shared data structure. When (or, under what conditions) should the user level threads use mutexes to guarantee the consistency of the shared data structure?

- A. Only if  $M > 1$ .
- B. Only if  $N \geq M$ .
- C. Only if the  $M$  kernel threads can run in parallel on a multi-core machine.
- D. User level threads should always use mutexes to protect shared data.

**Ans:** D (because user level threads can execute concurrently even on a single core)

6. Creating user level threads in a Linux application via any threading library always leads to the creation of corresponding kernel-level threads. [T/F]

**Ans:** F

7. Consider a Linux application with two threads T1 and T2 that both share and access a common variable  $x$ . Thread T1 uses a `pthread` mutex lock to protect its access to  $x$ . Now, if thread T2 tries to write to  $x$  without locking, then the Linux kernel generates a trap. [T/F]

**Ans:** F

8. In a single processor system, the kernel can simply disable interrupts to safely access kernel data structures, and does not need to use any spin locks. [T/F]

**Ans:** T

9. In the `pthread` condition variable API, a process calling wait on the condition variable must do so with a mutex held. State one problem that would occur if the API were to allow calls to wait without requiring a mutex to be held.

**Ans:** Wakeup happening between checking for condition and sleeping causing missed wakeup.

10. Consider  $N$  threads in a process that share a global variable in the program. If one thread makes a change to the variable, is this change visible to other threads? (Yes/No)

**Ans:** Yes

11. Consider  $N$  threads in a process. If one thread passes certain arguments to a function in the program, are these arguments visible to the other threads? (Yes/No)

**Ans:** No

12. Consider a user program thread that has locked a `pthread` mutex lock (that blocks when waiting for lock to be released) in user space. In modern operating systems, can this thread be context switched out or interrupted while holding the lock? (Yes/No)

**Ans:** Yes

13. Repeat the previous question when the thread holds a `pthread` spinlock in user space.

**Ans:** Yes

14. Consider a process that has switched to kernel mode and has acquired a spinlock to modify a kernel data structure. In modern operating systems, will this process be interrupted by external hardware before it releases the spinlock? (Yes/No)

**Ans:** No

15. Consider a process that has switched to kernel mode and has acquired a spinlock to modify a kernel data structure. In modern operating systems, will this process initiate a disk read before it releases the spinlock? (Yes/No)

**Ans:** No

16. When a user space process executes the wakeup/signal system call on a pthread condition variable, does it always lead to an immediate context switch of the process that calls signal (immediately after the signal instruction)? (Yes/No)

**Ans:** No

17. Consider a process in kernel mode that acquires a spinlock. For correct operation, it must disable interrupts on its CPU core for the duration that the spinlock is held, in both single core and multicore systems. [T/F]

**Ans.** T

18. Consider a process in kernel mode that acquires a spinlock in a multicore system. For correct operation, we must ensure that no other kernel-mode process running in parallel on another core will request the same spinlock. [T/F]

**Ans.** F

19. Multiple threads of a program must use locks when accessing shared variables even when executing on a single core system. [T/F]

**Ans:** T

20. Recall that the atomic instruction compare-and-swap (CAS) works as follows:  
`CAS(&var, oldval, newval)` writes `newval` into `var` and returns true if the old value of `var` is `oldval`. If the old value of `var` is not `oldval`, CAS returns false and does not change the value of the variable. Write code for the function to acquire a simple spinlock using the CAS instruction.

**Ans:** `while(!CAS(&lock, 0, 1));`

21. The simple spinlock implementation studied in class does not guarantee any kind of fairness or FIFO order amongst the threads contending for the spin lock. A ticket lock is a spinlock implementation that guarantees a FIFO order of lock acquisition amongst the threads contending for the lock. Shown below is the code for the function to acquire a ticket lock. In this function, the variables `next_ticket` and `now_serving` are both global variables, shared across all threads, and initialized to 0. The variable `my_ticket` is a variable that is local to a particular thread, and is not shared across threads. The atomic instruction `fetch_and_increment(&var)` atomically adds 1 to the value of the variable and returns the old value of the variable.

```

acquire():
    my_ticket = fetch_and_increment(&next_ticket)
    while(now_serving != my_ticket); //busy wait

```

You are now required to write the code to release the spinlock, to be executed by the thread holding the lock. Your implementation of the release function must guarantee that the next contending thread (in FIFO order) will be able to acquire the lock correctly. You must not declare or use any other variables.

```

release(): //your code here

```

**Ans:**

```

release(): //your code here
now_serving++;

```

22. Consider a multithreaded program, where threads need to acquire and hold multiple locks at a time. To avoid deadlocks, all threads are mandated to use the function `acquire_locks`, instead of acquiring locks independently. This function takes as arguments a variable sized array of pointers to locks (i.e., addresses of the lock structure), and the number of lock pointers in the array, as shown in the function prototype below. The function returns once all locks have been successfully acquired.

```

void acquire_locks(struct lock *la[], int n);
//i-th lock in array can be locked by calling lock(la[i])

```

Describe (in English, or in pseudocode) one way in which you would implement this function, while ensuring that no deadlocks happen during lock acquisition. Your solution must not use any other locks beyond those provided as input. Note that multiple threads can invoke this function concurrently, possibly with an overlapping set of locks, and the lock pointers can be stored in the array in any arbitrary order. You may assume that the locks in the array are unique, and there are no duplicates within the input array of locks.

**Ans.** Sort locks by address `struct lock *`, and acquire in sorted order.

23. Consider the classic readers-writers synchronization problem described below. Several processes/threads wish to read and write data shared between them. Some processes only want to read the shared data (“readers”), while others want to update the shared data as well (“writers”). Multiple readers may concurrently access the data safely, without any correctness issues. However, a writer must not access the data concurrently with anyone else, either a reader or a writer. While it is possible for each reader and writer to acquire a regular mutex and operate in perfect mutual exclusion, such a solution will be missing out on the benefits of allowing multiple readers to read at the same time without waiting for other readers to finish. Therefore, we wish to have special kind of locks called reader-writer locks that can be acquired by processes/threads in such situations. These locks have separate lock/unlock functions, depending on whether the thread asking for a lock is a reader or writer. If one reader asks for a lock while another reader already has it, the second reader will also be granted a read lock (unlike in the case of a regular mutex), thus encouraging more concurrency in the application.

Write down pseudocode to implement the functions `readLock`, `readUnlock`, `writeLock`, and `writeUnlock` that are invoked by the readers and writers to realize reader-writer locks. You must use condition variables and mutexes only in your solution.

**Ans:** A boolean variable `writer_present`, and two condition variables, `reader_can_enter` and `writer_can_enter`, are used.

```
readLock:
lock(mutex)
while(writer_present)
    wait(reader_can_enter)
read_count++
unlock(mutex)

readUnlock:
lock(mutex)
read_count--
if(read_count==0)
    signal(writer_can_enter)
unlock(mutex)

writeLock:
lock(mutex)
while(read_count > 0 || writer_present)
    wait(writer_can_enter)
writer_present = true
unlock(mutex)

writeUnlock:
lock(mutex)
writer_present = false
```

```
signal(writer_can_enter)
signal_broadcast(reader_can_enter)
unlock(mutex)
```

24. Consider the readers and writers problem discussed above. Recall that multiple readers can be allowed to read concurrently, while only one writer at a time can access the critical section. Write down pseudocode to implement the functions readLock, readUnlock, writeLock, and writeUnlock that are invoked by the readers and writers to realize read/write locks. You must use **only** semaphores, and no other synchronization mechanism, in your solution. Further, you must avoid using more semaphores than is necessary. Clearly list all the variables (semaphores, and any other flags/counters you may need) and their initial values at the start of your solution. Use the notation down(x) and up(x) to invoke atomic down and up operations on a semaphore x that are available via the OS API. Use sensible names for your variables.

**Ans:**

```
sem lock = 1; sem writer_can_enter = 1; int readCount = 0;
```

```
readLock:
down(lock)
readCount++
if(readCount ==1)
    down(writer_can_enter) //don't coexist with a writer
up(lock)
```

```
readUnlock:
down(lock)
readCount--
if(readCount == 0)
    up(writer_can_enter)
up(lock)
```

```
writeLock:
down(writer_can_enter)
```

```
writeUnlock:
up(writer_can_enter)
```

25. Consider the readers and writers problem as discussed above. We wish to implement synchronization between readers and writers, while giving **preference to writers**, where no waiting writer should be kept waiting for longer than necessary. For example, suppose reader process R1 is actively reading. And a writer process W1 and reader process R2 arrive while R1 is reading. While it might be fine to allow R2 in, this could prolong the waiting time of W1 beyond the absolute minimum of waiting until R1 finishes. Therefore, if we want writer preference, R2 should not be allowed before W1. Your goal is to write down pseudocode for read lock, read unlock, write lock, and write unlock functions that the processes should call, in order to realize read/write locks with writer preference. You must use only simple locks/mutexes and conditional variables in your solution. Please pick sensible names for your variables so that your solution is readable.

**Ans:**

```
readLock:
lock(mutex)
while(writer_present || writers_waiting > 0)
    wait(reader_can_enter, mutex)
readcount++
unlock(mutex)
```

```
readUnlock:
lock(mutex)
readcount--
if(readcount==0)
    signal(writer_can_enter)
unlock(mutex)
```

```
writeLock:
lock(mutex)
writer_waiting++
while(readcount > 0 || writer_present)
    wait(writer_can_enter, mutex)
writer_waiting--
writer_present = true
unlock(mutex)
```

```
writeUnlock:
lock(mutex)
writer_present = false
if(writer_waiting==0)
    signal_broadcast(reader_can_enter)
else
    signal(writer_can_enter)
unlock(mutex)
```

26. Write a solution to the readers-writers problem with preference to writers discussed above, but using only semaphores.

**Ans:**

```
sem rlock = 1; sem wlock = 1;
sem reader_can_try = 1; sem writer_can_enter = 1;
int readCount = 0; int writeCount = 0;

readLock:
down(reader_can_try) //new sem blocks reader if writer waiting
down(rlock)
readCount++
if(readCount ==1)
    down(writer_can_enter) //don't coexist with a writer
up(rlock)
up(reader_can_try)

readUnlock:
down(rlock)
readCount--
if(readCount == 0)
    up(writer_can_enter)
up(rlock)

writeLock:
down(wlock)
writerCount++
if(writerCount==1)
    down(reader_can_try)
up(wlock)
down(writer_can_enter) //release wlock and then block

writeUnlock:
down(wlock)
writerCount--
if(writerCount == 0)
    up(reader_can_try)
up(wlock)

up(writer_can_enter)
```



27. Consider the famous dining philosophers' problem.  $N$  philosophers are sitting around a table with  $N$  forks between them. Each philosopher must pick up both forks on her left and right before she can start eating. If each philosopher first picks the fork on her left (or right), then all will deadlock while waiting for the other fork. The goal is to come up with an algorithm that lets all philosophers eat, without deadlock or starvation. Write a solution to this problem using condition variables.

**Ans:** A variable `state` is associated with each philosopher, and can be one of EATING (holding both forks) or THINKING (when not eating). Further, a condition variable is associated with each philosopher to make them sleep and wake them up when needed. Each philosopher must call the `pickup` function before eating, and `putdown` function when done. Both these functions use a mutex to change states only when both forks are available.

```
bothForksFree(i) :  
return (state[leftNbr(i)] != EATING &&  
        state[rightNbr(i)] != EATING)
```

```
pickup(i) :  
    lock(mutex)  
    while(!bothForksFree(i))  
        wait(condvar[i])  
    state[i] = EATING  
    unlock(mutex)  
  
putdown(i) :  
    lock(mutex)  
    state[i] = THINKING  
    if(bothForksFree(leftNbr(i)))  
        signal(leftNbr(i))  
    if(bothForksFree(rightNbr(i)))  
        signal(rightNbr(i))  
    unlock(mutex)
```

28. Consider a clinic with one doctor and a very large waiting room (of infinite capacity). Any patient entering the clinic will wait in the waiting room until the doctor is free to see her. Similarly, the the doctor also waits for a patient to arrive to treat. All communication between the patients and the doctor happens via a shared memory buffer. Any of the several patient processes, or the doctor process can write to it. Once the patient “enters the doctors office”, she conveys her symptoms to the doctor using a call to `consultDoctor()`, which updates the shared memory with the patient’s symptoms. The doctor then calls `treatPatient()` to access the buffer and update it with details of the treatment. Finally, the patient process must call `noteTreatment()` to see the updated treatment details in the shared buffer, before leaving the doctor’s office. A template code for the patient and doctor processes is shown below. Enhance this code to correctly synchronize between the patient and the doctor processes. Your code should ensure that no race conditions occur due to several patients overwriting the shared buffer concurrently. Similarly, you must ensure that the doctor accesses the buffer only when there is valid new patient information in it, and the patient sees the treatment only after the doctor has written it to the buffer. You must use **only semaphores** to solve this problem. Clearly list the semaphore variables you use and their initial values first. Please pick sensible names for your variables.

(a) Semaphore variables and initial values:

(b) Patient process:

```
consultDoctor();
```

```
noteTreatment();
```

(c) Doctor process:

```
while(1) {  
  
    treatPatient();  
  
}
```

**Ans:**

(a) Semaphores variables:

```
pt_waiting = 0
treatment_done = 0
doc_avlbl = 1
```

(b) Patient process:

```
down(doc_avlbl)
consultDoctor()
up(pt_waiting)
down(treatment_done)
noteTreatment()
up(doc_avlbl)
```

(c) Doctor:

```
while(1) {
down(pt_waiting)
treatPatient()
up(treatment_done)
}
```

29. Consider a producer-consumer situation, where a process P produces an integer using the function `produceNext()` and sends it to process C. Process C receives the integer from P and consumes it in the function `consumeNext()`. After consuming this integer, C must let P know, and P must produce the next integer only after learning that C has consumed the earlier one. Assume that P and C get a pointer to a shared memory segment of 8 bytes, that can store any two 4-byte integer-sized fields, as shown below. Both fields in the shared memory structure are zeroed out initially. P and C can read or write from it, just as they would with any other data object. Briefly describe how you would solve the producer-consumer problem described above, using *only* this shared memory as a means of communication and synchronization between processes P and C. You must not use any other synchronization or communication primitive. You are provided template code below which gets a pointer to the shared memory, and produces/consumes integers. You must write the code for communicating the integer between the processes using the shared memory, with synchronization logic as required.

```
struct shmem_structure {  
    int field1;  
    int field2;  
};
```

(a) Producer:

```
    struct shmem_structure *shptr = get_shared_memory_structure();  
  
    while(1) {  
        int produced = produceNext();  
  
    }
```

(b) Consumer:

```
    struct shmem_structure *shptr = get_shared_memory_structure();  
  
    while(1) {  
        int consumed; //fill this value from producer  
  
        consumeNext(consumed);  
  
    }
```

**Ans:**

(a) Producer:

```
int produced = produceNext();  
shptr->field1=produced;  
shptr->field2 = 1; //indicating ready  
while(shptr->field2 == 1); //do nothing
```

(b) Consumer:

```
while(shptr->field2 == 0); //do nothing  
consumed=shptr->field1;  
consumeNext(consumed);  
shptr->field2 = 0; //indicating done
```

30. Consider a multithreaded banking application. The main process receives requests to transfer money from one account to the other, and each request is handled by a separate worker thread in the application. All threads access shared data of all user bank accounts. Bank accounts are represented by a unique integer account number, a balance, and a lock of type `mylock` (much like a `pthread_mutex`) as shown below.

```
struct account {  
    int accountnum;  
    int balance;  
    mylock lock;  
};
```

Each thread that receives a transfer request must implement the transfer function shown below, which transfers money from one account to the other. Add correct locking (by calling the `dolock(&lock)` and `unlock(&lock)` functions on a `mylock` variable) to the transfer function below, so that no race conditions occur when several worker threads concurrently perform transfers. Note that you must use the fine-grained per account lock provided as part of the account object itself, and not a global lock of your own. Also make sure your solution is deadlock free, when multiple threads access the same pair of accounts concurrently.

```
void transfer(struct account *from, struct account *to, int amount) {  
  
    from->balance -= amount; // dont write anything...  
    to->balance += amount; // ...between these two lines  
  
}
```

**Ans:** The accounts must be locked in order of their account numbers. Otherwise, a transfer from account X to Y and a parallel transfer from Y to X may acquire locks on X and Y in different orders and end up in a deadlock.

```
struct account *lower = (from->accountnum < to->accountnum)?from:to;  
struct account *higher = (from->accountnum < to->accountnum)?to:from;  
dolock(&(lower->lock));  
dolock(&(higher->lock));  
  
from->balance -= amount;  
to->balance += amount;  
  
unlock(&(lower->lock));  
unlock(&(higher->lock));
```

31. Consider a process with three threads A, B, and C. The default thread of the process receives multiple requests, and places them in a request queue that is accessible by all the three threads A, B, and C. For each request, we require that the request must first be processed by thread A, then B, then C, then B again, and finally by A before it can be removed and discarded from the queue. Thread A must read the next request from the queue only after it is finished with all the above steps of the previous one. Write down code for the functions run by the threads A, B, and C, to enable this synchronization. You can only worry about the synchronization logic and ignore the application specific processing done by the threads. You may use any synchronization primitive of your choice to solve this question.

**Ans:** Solution using semaphores shown below. The order of processing is A1–B1–C–B2–A2. All threads run in a forever loop, and wait as dictated by the semaphores.

```
sem aldone = 0; b1done = 0; cdone = 0; b2done = 0;
```

ThreadA:

```
    get request from queue and process
    up(aldone)
    down(b2 done)
    finish with request
```

ThreadB:

```
    down(aldone)
    //do work
    up(b1done)
    down(cdone)
    //do work
    up(b2done)
```

ThreadC:

```
    down(b1done)
    //do work
    up(cdone)
```

32. Consider two threads A and B that perform two operations each. Let the operations of thread A be A1 and A2; let the operations of thread B be B1 and B2. We require that threads A and B each perform their first operation before either can proceed to the second operation. That is, we require that A1 be run before B2 and B1 before A2. Consider the following solutions based on semaphores for this problem (the code run by threads A and B is shown in two columns next to each other). For each solution, explain whether the solution is correct or not. If it is incorrect, you must also point out why the solution is incorrect.

(a)	sem A1Done = 0;	sem B1Done = 0;
	//Thread A	//Thread B
	A1	B1
	down(B1Done)	down(A1Done)
	up(A1Done)	up(B1Done)
	A2	B2
(b)	sem A1Done = 0;	sem B1Done = 0;
	//Thread A	//Thread B
	A1	B1
	down(B1Done)	up(B1Done)
	up(A1Done)	down(A1Done)
	A2	B2
(c)	sem A1Done = 0;	sem B1Done = 0;
	//Thread A	//Thread B
	A1	B1
	up(A1Done)	up(B1Done)
	down(B1Done)	down(A1Done)
	A2	B2

**Ans:**

- (a) Deadlocks, so incorrect.
- (b) Correct
- (c) Correct



33. Now consider a generalization of the above problem for the case of  $N$  threads that want to each execute their first operation before any thread proceeds to the second operation. Below is the code that each thread runs in order to achieve this synchronization. `count` is an integer shared variable, and `mutex` is a mutex binary semaphore that protects this shared variable. `step1Done` is a semaphore initialized to zero. You are told that this code is wrong and does not work correctly. Further, you can fix it by changing it slightly (e.g., adding one statement, or rearranging the code in some way). Suggest the change to be made to the code in the snippet below to fix it. You must use only semaphores and no other synchronization mechanism.

```
//run first step

down(mutex);
count++;
up(mutex);
if(count == N)
    up(step1Done);
down(step1Done);

//run second step
```

**Ans:** The problem is that the semaphore is decremented  $N$  times, but is only incremented once. To fix it, we must do `up`  $N$  times when `count` is  $N$ . Or, add `up` after the last `down`, so that it is performed  $N$  times by the  $N$  threads.

34. The cigarette smokers problem is a classical synchronization problem that involves 4 threads: one agent and three smokers. The smokers require three ingredients to smoke a cigarette: tobacco, paper, and matches. Each smoker has one of the three ingredients and waits for the other two, smokes the cigar once he obtains all ingredients, and repeats this forever. The agent repeatedly puts out two ingredients at a time and makes them available. In the correct solution of this problem, the smoker with the complementary ingredient should finish smoking his cigar. Consider the following solution to the problem. The shared variables are three semaphores `tobacco`, `paper` and `matches` initialized to 0, and semaphore `doneSmoking` initialized to 1. The agent code performs `down(doneSmoking)`, then picks two of the three ingredients at random and performs `up` on the corresponding two semaphores, and repeats. The smoker with tobacco runs the following code in a loop.

```
down(paper)
down(matches)
//make and smoke cigar
up(doneSmoking)
```

Similarly, the smoker with matches waits for tobacco and paper, and the smoker with paper waits for tobacco and matches, before signaling the agent that they are done smoking. Does the code above solve the synchronization problem correctly? If you answer yes, provide a justification for why the code is correct. If you answer no, describe what the error is and also provide a correct solution to the problem. (If you think the code is incorrect and are providing another solution, you may change the code of both the agent and the smokers. You can also introduce new variables as necessary. You must use only semaphores to solve the problem.)

**Ans:** The code is incorrect and deadlocks. One fix is to add semaphores for two ingredients at a time (e.g., `tobaccoAndPaper`). The smokers wait on these and the agent signals these. So there is no possibility of deadlock.

35. Consider a server program running in an online market place firm. The program receives buy and sell orders for one type of commodity from external clients. For every buy or sell request received by the server, the main process spawns a new buy or sell thread. We require that every buy thread waits until a sell thread arrives, and vice versa. A matched pair of buy and sell threads will both return a response to the clients and exit. You may assume that all buy/sell requests are identical to each other, so that any buy thread can be matched with any sell thread. The code executed by the buy thread is shown below (the code of the sell thread would be symmetric). You have to write the synchronization logic that must be run at the start of the execution of the thread to enable it to wait for a matching sell thread to arrive (if none exists already). Once the threads are matched, you may assume that the function `completeBuy()` takes care of the application logic for exchanging information with the matching thread, communicating with the client, and finishing the transaction. You may use any synchronization technique of your choice.

```
//declare any variables here
```

```
buy_thread_function:
    //start of sync logic
```

```
    //end of sync logic
    completeBuy();
```

**Ans:**

```
sem buyer = 0; sem seller = 0;
```

```
Buyer thread:
```

```
up(buyer)
down(seller)
completeBuy()
```

36. Consider the following classical synchronization problem called the barbershop problem. A barbershop consists of a room with  $N$  chairs. If a customer enters the barbershop and all chairs are occupied, then the customer leaves the shop. If the barber is busy, but chairs are available, then the customer sits in one of the free chairs and awaits his turn. The barber moves onto the next waiting seated customer after he finishes one hair cut. If there are no customers to be served, the barber goes to sleep. If the barber is asleep when a customer arrives, the customer wakes up the barber to give him a hair cut. A waiting customer vacates his chair after his hair cut completes. Your goal is to write the pseudocode for the customer and barber threads below with suitable synchronization. You must use only semaphores to solve this problem. Use the standard notation of invoking up/down functions on a semaphore variable.

The following variables (3 semaphores and a count) are provided to you for your solution. You must use these variables and declare any additional variables if required.

```
semaphore mutex = 1, customers = 0, barber = 0;
int waiting_count = 0;
```

Some functions to invoke in your customer and barber threads are:

- A customer who finds the waiting room full should call the function `leave()` to exit the shop permanently. This function does not return.
- A customer should invoke the function `getHairCut()` in order to get his hair cut. This function returns when the hair cut completes.
- The barber thread should call `cutHair()` to give a hair cut. When the barber invokes this function, there should be exactly one customer invoking `getHairCut()` concurrently.

**Ans:**

Customer:

```
down(mutex)
if(waiting_count == N)
    up(mutex)
    leave()
waiting_count++
up(mutex)
```

```
up(customers)
down(barber)
```

```
getHairCut()
```

```
down(mutex)
waiting_count--
up(mutex)
```

Barber:

```
up(barber)
down(customers)
cutHair()
```

37. Consider a multithreaded application server handling requests from clients. Every new request that arrives at the server causes a new thread to be spawned to handle that request. The server can provide service to only one request/thread at a time, and other threads that arrive when the server is busy must wait for service using a synchronization primitive (semaphore or condition variable). In order to avoid excessive waiting times, the server does not wish to have more than  $N$  requests/threads in the system (including the waiting requests and any request it is currently serving). You may assume that  $N > 2$ . Given this constraint, a newly arriving thread must first check if  $N$  other requests are already in the system: if yes, it must exit without waiting and return an error value to the client, by calling the function `thr_exit_failure()`. This function terminates the thread and does not return.

When a thread is ready for service, it must call the function `get_service()`. Your code should ensure that no more than one thread calls this function at any point of time. This function blocks the thread for the duration of the service. Note that, while the thread receiving service is blocked, other arriving threads must be free to join the queue, or exit if the system is overloaded. After a thread returns from `get_service()`, it must enable one of the waiting threads to seek service (if any are waiting), and then terminate itself successfully by calling the function `thr_exit_success()`. This function terminates the thread and does not return.

You are required to write pseudocode of the function to be run by the request threads in this system, as per the specification above. Your solution must use only locks and condition variables for synchronization. Clearly state all the variables used and their initial values at the start of your solution.

**Ans**

```
int num_requests=0;
bool server_busy = false
cv, mutex

lock(mutex)

if(num_requests == N)
    unlock(mutex)
    the_exit_failure()

num_requests++

if(server_busy)
    wait(cv, mutex)

server_busy = true
unlock(mutex)

get_service()

lock(mutex)
num_requests--
server_busy = false

if(num_requests > 0)
    signal(cv)

unlock(mutex)
thr_exit_success()
```

38. Consider the previous problem, but now assume that  $N$  is infinity. That is, all arriving threads will wait (if needed) for their turn in the queue of a synchronization primitive, get served when their turn comes, and exit successfully. Write the pseudocode of the function to be run by the threads with this modified specification. Your solution must only use semaphores for synchronization, and only the correct solution that uses the least number of semaphores will get full credit. Clearly state all the variables used and their initial values at the start of your solution.

**Ans**

```
sem waiting = 1

down(waiting)
get_service()
up(waiting)
thr_exit_success()
```



39. Consider the following synchronization problem. A group of children are picking chocolates from a box that can hold up to  $N$  chocolates. A child that wants to eat a chocolate picks one from the box to eat, unless the box is empty. If a child finds the box to be empty, she wakes up the mother, and waits until the mother refills the box with  $N$  chocolates. Unsynchronized code snippets for the child and mother threads are as shown below:

```
//Child
while True:
    getChocolateFromBox()
    eat()

//Mother
while True:
    refillChocolateBox(N)
```

You must now modify the code of the mother and child threads by adding suitable synchronization such that a child invokes `getChocolateFromBox()` only if the box is non-empty, and the mother invokes `refillChocolateBox(N)` only if the box is fully empty. Solve this question using only locks and condition variables, and no other synchronization primitive. The following variables have been declared for use in your solution.

```
int count = 0;
mutex m; // you may invoke lock and unlock
condvar fullBox, emptyBox; //you may perform wait and signal
//or signal_broadcast
```

- (a) Code for child thread
- (b) Code for mother thread

**Ans:**

```
//Child
while True:
    lock(m)
    while(count == 0)
        signal(emptyBox)
        wait(fullBox, m)
    getChocolateFromBox()
    eat()
    count--
    signal(fullBox) //optional
    unlock(m)

//Mother
while True:
    lock(m)
    if(count > 0)
        wait(emptyBox, m)
    refillChocolateBox(N)
    count += N
    signal(fullBox)
    unlock(m)
```

There are two ways of waking up sleeping children. Either the mother does a signal broadcast to all children. Or every child that eats a chocolate wakes up another sleeping child. You may also assume that signal by mother wakes up all children.

40. Repeat the above question, but your solution now must use only semaphores and no other synchronization primitive. The following variables have been declared for use in your solution.

```
int count = 0;
semaphore m, fullBox, emptyBox;
//initial values of semaphores are not specified
//you may invoke up and down methods on a semaphore
```

- (a) Initial values of the semaphores
- (b) Code for child thread
- (c) Code for mother thread

**Ans:**

```
m = 1, fullBox = 0, emptyBox = 0
```

```
//Child
while True:
    down(m)
    if(count == 0)
        up(emptyBox)
        down(fullBox)
        count += N
    getChocolateFromBox()
    eat()
    count--
    up(m)
```

```
//Mother
while True:
    down(emptyBox)
    refillChocolateBox(N)
    up(fullBox)
```

Here the subtlety is the lock m. Mother can't get lock to update count after filling the box, as that will cause a deadlock. In general, if child sleeps with mutex m locked, then mother cannot request the same lock.

41. Consider the classic “barrier” synchronization problem, where  $N$  threads wish to synchronize with each other as follows.  $N$  threads arrive into the system at different times and in any order. The arriving threads must wait until all  $N$  threads have arrived into the system, and continue execution only after all  $N$  threads have arrived. We wish to write logic to synchronize the threads in the manner stated above using semaphores. Below are three possible solutions to the problem. You are told that one of the solutions is correct and the other two are wrong. Identify the correct solution amongst the three given options. Further, for each of the other incorrect solutions, explain clearly why the solution is wrong. The following shared variables are declared for use in each solution.

```
int count = 0;
sem mutex; //initialized to 1
sem barrier; //initialized to 0
```

- (a) `down(mutex)`  
    `count++`  
    `if(count == N) up(barrier)`  
    `up(mutex)`  
  
    `down(barrier)`  
  
    `//wait done; proceed to actual task`
- (b) `down(mutex)`  
    `count++`  
    `if(count == N) up(barrier)`  
    `up(mutex)`  
  
    `down(barrier)`  
    `up(barrier)`  
  
    `//wait done; proceed to actual task`
- (c) `down(mutex)`  
    `count++`  
    `if(count == N) up(barrier)`  
    `down(barrier)`  
    `up(barrier)`  
    `up(mutex)`  
  
    `//wait done; proceed to actual task`

**Ans:** In (a) `up` is done only once when many threads are waiting on `down`. In (c), `down(barrier)` is called when `mutex` held, so code deadlocks. (b) is correct answer.

42. Consider the barrier synchronization primitive discussed in class, where the  $N$  threads of an application wait until all the threads have arrived at a barrier, before they proceed to do a certain task. You are now required to write the code for a reusable barrier, where the  $N$  application threads perform a series of steps in a loop, and use the same barrier code to synchronize for each iteration of the loop. That is, your solution should ensure that all threads wait for each other before the start of each step, and proceed to the next step only after all threads have completed the previous step. Your solution must only use semaphores. The following functions can be invoked on a semaphore  $s$  used in this question:  $\text{down}(s)$ ,  $\text{up}(s)$ , and  $\text{up}(s, n)$ . While the first two functions are as studied in class, the function  $\text{up}(s, n)$  simply invokes  $\text{up}(s)$   $n$  times atomically.

We have provided you some code to get started. Shown below is the code to be run by each application thread, including the code to wait at the barrier. However, this is not the correct solution, as this code only works as a single-use barrier, i.e., it only ensures that the threads synchronize at the barrier once, and cannot be used to synchronize multiple times (can you figure out why?). You are required to modify this code to make it reusable, such that the threads can synchronize at the barrier multiple times for the multiple steps to be performed.

Your solution must only use the following variables: `int count = 0;` and semaphores (initial values as given): `sem mutex = 1;` `sem barrier1 = 0;` `sem barrier2 = 0;`

For each step to be executed by the threads, do:

```
//add code here if required to make barrier reusable
```

```
down(mutex)
    count++
    if(count == N) up(barrier1, N)
up(mutex)
down(barrier1)
```

```
... wait done, execute actual task of this step ...
```

```
//add code here if required to make barrier reusable for next step
```

**Ans:** The extra code to be added is at the end of completing a step, where you make all threads wait once again.

```
down(mutex)
count--
if(count==0) up(barrier2, N)
up(mutex)
down(barrier2)
```

43. Consider a web server that is supposed to serve a batch of  $N$  requests. Each request that arrives at the web server spawns a new thread. The arriving threads wait until  $N$  of them accumulate, at which point all of them proceed to get service from the server. Shown below is the code executed by each arriving thread, that causes it to wait until all the other threads arrive. The variable `count` is initialized to  $N$ . The code also uses `wait` and `signal` primitives on a condition variable; and you may assume that the signal primitive wakes up all waiting threads (not just one of them).

```
lock(mutex)
    count--;
unlock(mutex)

if(count > 0) {
    lock(mutex)
    wait(cv, mutex)
    unlock(mutex)
}
else {
    lock(mutex)
    signal(cv)
    unlock(mutex)
}

... wait done, proceed to server ...
```

You are told that the code above is incorrect, and can sometimes cause a deadlock. That is, in some executions, all  $N$  threads do not go to the server for service, even though they have arrived.

- (a) Using an example, explain the exact sequence of events that can cause a deadlock. You must write your answers as bullet points, with one event per bullet point, starting from threads arriving in the system until the deadlock.
- (b) Explain how you will fix this deadlock and correct the code shown above. You must retain the basic structure of the code. Indicate your changes next to the code snippet above.

**Ans:** The given incorrect solution may cause a missed wakeup. For example, some thread decides to wait and goes inside the if-loop, but is context switched out before calling `wait` (and before it acquires the lock). Now, if `count` hits 0 and `signal` happens before it runs again, it will wait with no one to wake it up, leading to deadlock. The fix is simply holding the lock all through the condition checking and waiting.

44. Consider an application that has  $K + 1$  threads running on a Linux-like OS ( $K > 1$ ). The first  $K$  threads of an application execute a certain task T1, and the remaining one thread executes task T2. The application logic requires that task T1 is executed  $N > 1$  times, followed by task T2 executed once, and this cycle of  $N$  executions of T1 followed by one execution of T2 continue indefinitely. All  $K$  threads should be able to participate in the  $N$  executions of task T1, even though it is not required to ensure perfect fairness amongst the threads.

Shown below is one possible set of functions executed by the threads running tasks T1 and T2. You are told that this solution has two bugs in the code run by the thread performing task T2. Briefly describe the bugs in the space below, and suggest small changes to the corresponding code to fix these bugs (you may write your changes next to the code snippet). You must not change the code corresponding to task T1 in any way. All threads share a counter `count` (initialized to 0), a mutex variable `m`, and two condition variables `t1cv`, and `t2cv`. Here, the function `signal` on a condition variable wakes up only one of the possibly many sleeping threads.

```
//function run by K threads of task T1
while True {
    lock(m)
    if(count >= N) {
        signal(t2cv)
        wait(t1cv, m)
    }
    //.. do task T1 once ..
    count++
    unlock(m)
}
//function run by thread of task T2
while True {
    lock(m)
    wait(t2cv, m)
    // .. do task T2 once
    count = 0
    signal(t1cv)
    unlock(m)
}
```

**Ans:** (a) check `count < N` and only then wait (b) signal broadcast instead of signal

45. You are now required to solve the previous question using semaphores for synchronization. You are given the pseudocode for the function run by the thread executing task T2 (which you must not change). You are now required to write the corresponding code executed by the  $K$  threads running task T1. You must use the following semaphores in your solution: `mutex`, `t1sem`, `t2sem`. You must initialize them suitably below. The variable `count` (initialized to 0) is also available for use in your solution.

**Ans:**

```
//fill in initial values of semaphores
sem_init(&mutex, 0, 1); sem_init(&t1sem, 0, 1); sem_init(&t2sem, 0, 1);
//other variables
int count = 0

//function run by thread executing T2
while True {
    down(&t2sem)
    //.. do task T2 ..
    up(&t1sem)
}

//function run by threads executing task T1
while True {

}
```

**Ans:**

```
mutex=1, t1sem=0, t2sem=0

down(&mutex)
if(count == N)
    up(&t2sem)
    down(&t1sem)
    count = 0

do task T1 once
count++
up(&mutex)
```



46. Multiple people are entering and exiting a room that has a light switch. You are writing a computer program to model the people in this situation as threads in an application. You must fill in the functions `onEnter()` and `onExit()` that are invoked by a thread/person when the person enters and exits a room respectively. We require that the first person entering a room must turn on the light switch by invoking the function `turnOnSwitch()`, while the last person leaving the room must turn off the switch by invoking `turnOffSwitch()`. You must invoke these functions suitably in your code below. You may use any synchronization primitives of your choice to achieve this desired goal. You may also use any variables required in your solution, which are shared across all threads/persons.
- (a) Variables and initial values
  - (b) Code `onEnter()` to be run by thread/person entering
  - (c) Code `onExit()` to be run by thread/person exiting

**Ans:**

```
variables: mutex, count
```

```
onEnter():  
lock(mutex)  
count++  
if(count==1) turnOnSwitch()  
unlock(mutex)
```

```
onExit():  
lock(mutex)  
count--  
if(count==0) turnOffSwitch()  
unlock(mutex)
```