

DAY 2

XOR 문제
Neural Network
역전파 알고리즘
NN Binary Classification
NN Regression

0. Day1 무엇을 배웠나요?

1. Deep Learning Overview

1. Perceptron
2. Neural Network
3. Convolution Neural Network

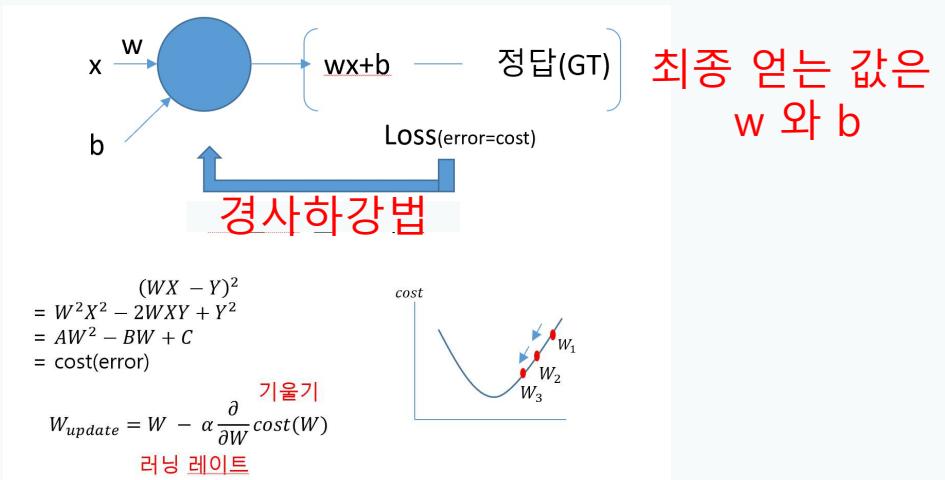
2. DeepLearning FrameWork

1. Tensorflow1.x : 그래프 기반
2. Tensorflow2.x : 즉시 모드

3. Mean Square Error Loss 함수

1. Loss 함수란 perceptron의 task를 지정
2. 정답과의 차이를 나타냄

4. Perceptron + 경사하강법



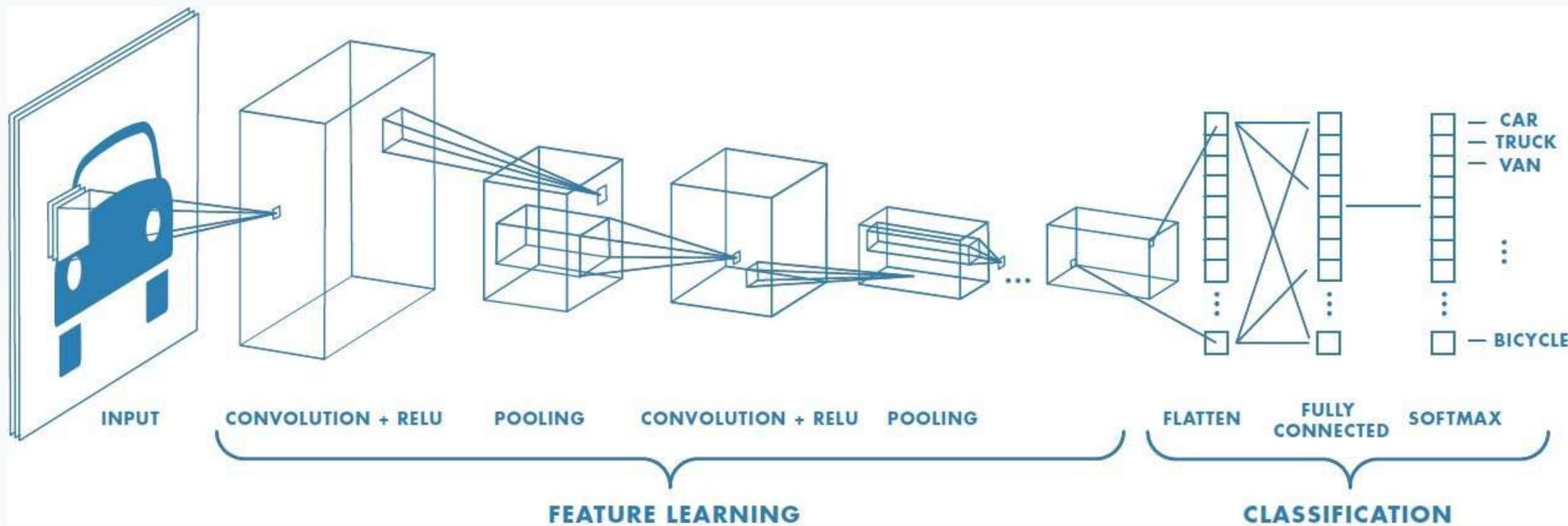
최종 얻는 값은
w 와 b

5. Regression

1. 값 예측 (ex : 여러 변수를 받아 하나의 값을 예측)
 2. Loss : Mean Square Error
6. Classification(logistic regression)
1. Sigmoid 함수를 통해서 분류 학습
 2. Loss : Cross Entropy

0. Day1 무엇을 배웠나요?

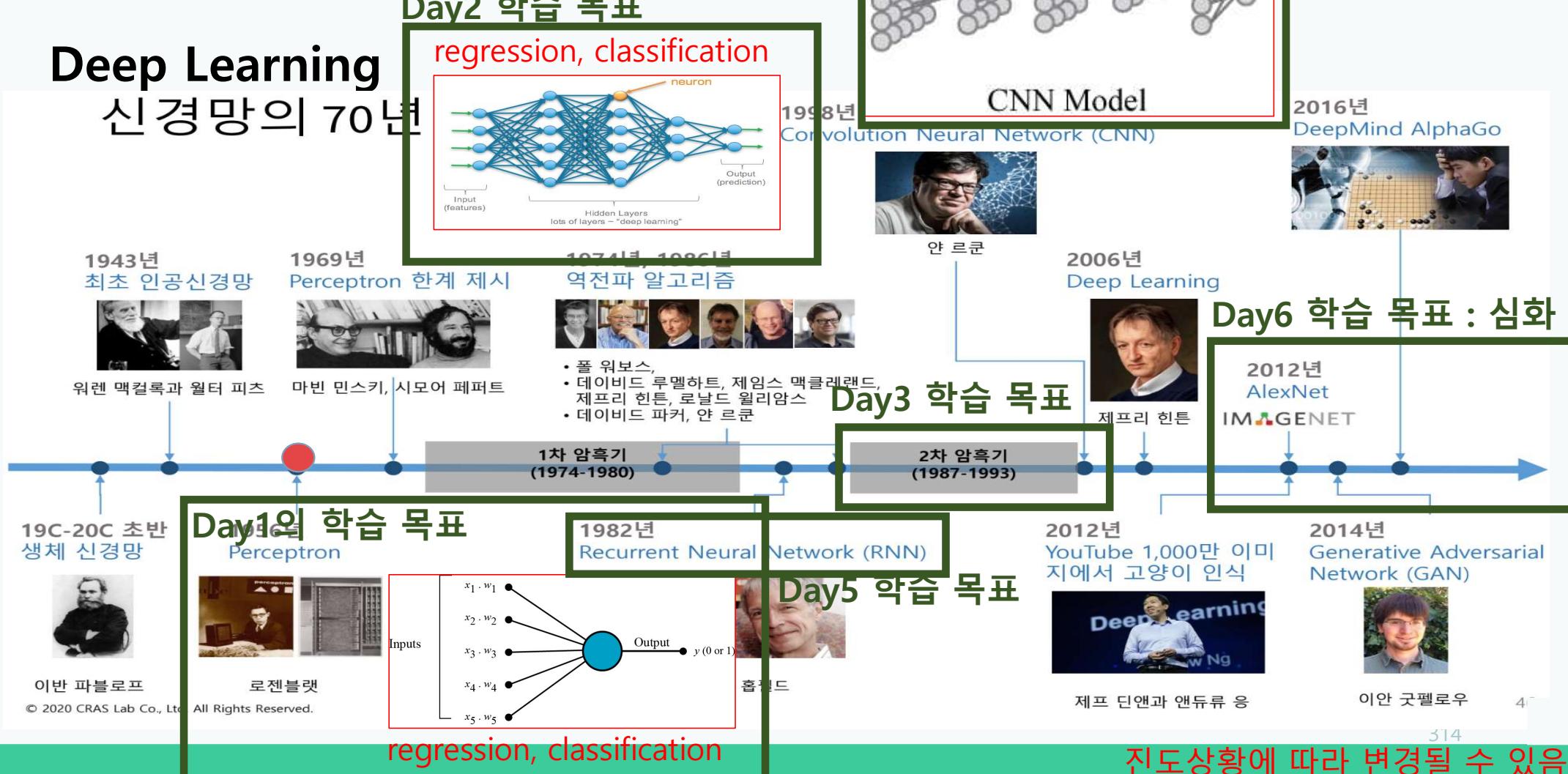
Deep Learning



5. Day1 무엇을 배웠나요?

Deep Learning

신경망의 70년



0. Day1 무엇을 배웠나요?

기계학습 (Machine Learning) – Supervised

Classification (분류)

Supervised Learning

- Classification
- Regression
- etc.

Unsupervised Learning

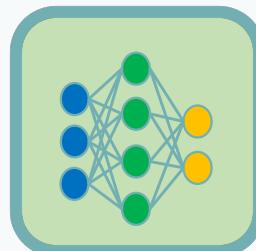
- Clustering
- Anomaly Detection
- etc.

Semi-supervised Learning



Data
(Input)
[데이터 (입력)]

“출력이 클래스다”



Model
[모델]

“고양이”
Output
[출력]

0. 어제 무엇을 배웠나요?

기계학습 (Machine Learning) – Supervised

Regression (회귀)

Supervised Learning

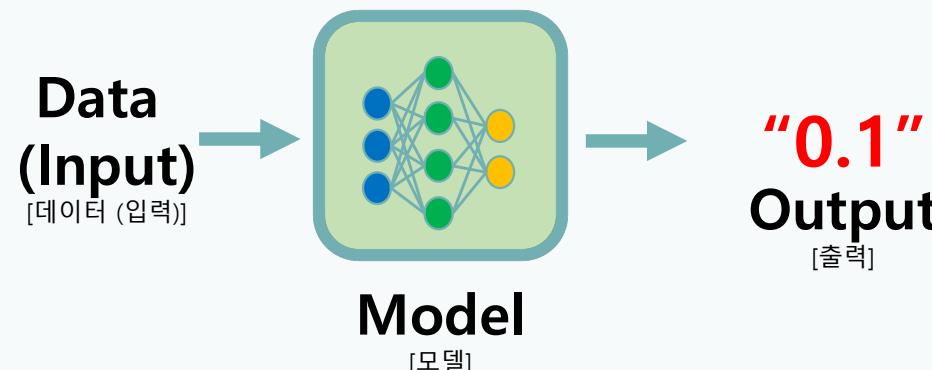
- Classification
- Regression
- etc.

Unsupervised Learning

- Clustering
- Anomaly Detection
- etc.

Semi-supervised Learning

“출력이 숫자(실수)다”



0. 어제 무엇을 배웠나요?

1. Linear Regression



$$\mathcal{L}_{mse} = \frac{1}{n} \sum_{i=1}^n (H(x_i) - y_i)^2$$

-> 문제점 : binary classification에서 사용할 시 풀리지 않을때가 존재함.

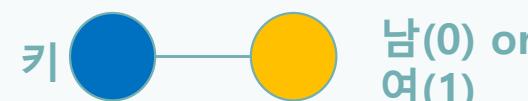
2. Logistic Linear Regression (Sigmoid만 적용)



$$\mathcal{L}_{mse} = \frac{1}{n} \sum_{i=1}^n (\sigma(H(x_i)) - y_i)^2$$

-> 해결점 : 출력할때 sigmoid 함수를 통해서 출력 0~1사이 값이며 커브피팅 효과
-> 문제점 : 기존 mse loss를 사용하면 두가지 문제가 있음 1. local min에 빠질 확률이 크고,
2. 시그모이드 미분값으로 w 학습이 잘안되거나 느림

3. Logistic Regression(Classification)



$$Cost(h_\theta(x), y) = \begin{cases} -\log(h_\theta(x)) & \text{if } y = 1 \\ -\log(1 - h_\theta(x)) & \text{if } y = 0 \end{cases}$$

-> 해결점 : mse loss 함수 대신 binary_crossentropy loss

0. 어제 무엇을 배웠나요?

로지스틱 회귀

- 두개의 값(0,1) 만 가지는 종속 변수와 독립변수들 간의 인과관계를 로지스틱 함수를 이용하여 추정하는 통계기법
- 어떤 사전이 발생할지에 대한 직접 예측이 아니라 그 사건이 발생할 확률을 예측하는 것

금융

고객 신용도 평가 (우량/불량)

통신

고객 지속 평가 (유지/번호 이동)

제과점

제과 판매 (판매/폐기)

의학

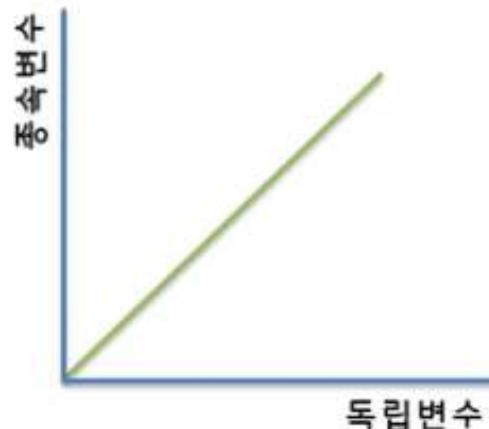
질병 예측 (간경화 유/무)

독립변수 : 연구자가 의도적으로 변화시키는 변수

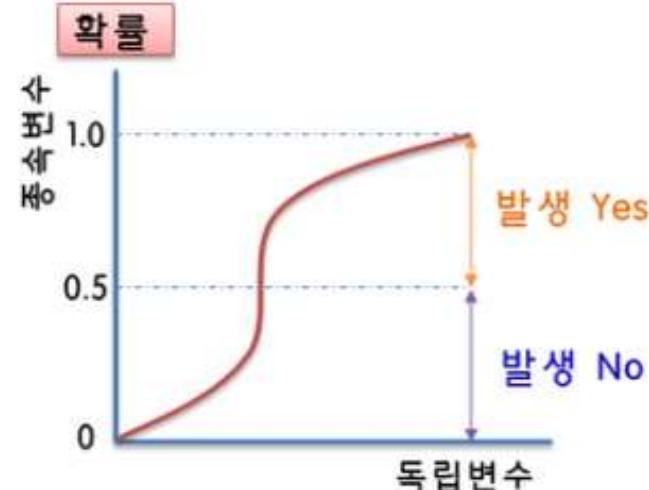
종속변수 : 연구자가 독립변수의 변화에 따라 어떻게 변하는지 알고 싶어하는 변수

0. 어제 무엇을 배웠나요?

로지스틱 회귀 모형



선형 회귀분석



로지스틱 회귀분석

0. 어제 무엇을 배웠나요?

로지스틱 회귀 모형

$$\text{odds} = \frac{\text{사건 발생함}}{\text{사건 발생안함}} = \frac{p}{1-p} = e^{\beta_0 + \beta_1 X_1 + \dots + \beta_r X_r}$$

지수함수로 표현 가능

- 오즈비는 확률과 관련된 의미로 p 가 주어졌을 때, 사건이 발생할 확률이 발생하지 않을 확률에 비해 몇배 더 높은가 의미
- 예) 종속변수가 1=True, 0=False라고 할 때, P 가 0.8이라면 오즈비는 $(0.8/(1-0.8))=4$ 가 되고 이것은 성공이 될 확률이 실패가 될 확률보다 4배 높다는 의미

0. 어제 무엇을 배웠나요?

로지스틱 회귀 모형

$$\text{odds} = \frac{\text{사건 발생함}}{\text{사건 발생안함}} = \frac{p}{1-p} = e^{\beta_0 + \beta_1 X_1 + \dots + \beta_i X_i}$$

자연지수 e를 ln으로 치환

$$\text{odds} = \ln \left(\frac{p}{1-p} \right) = \ln \left(e^{\beta_0 + \beta_1 X_1 + \dots + \beta_i X_i} \right)$$

$$\text{OR (Y)} = \underline{\beta_0 + \beta_1 X_1 + \dots + \beta_i X_i}$$

다중 회귀분석의 회귀식과 동일

0. 어제 무엇을 배웠나요?

로지스틱 회귀 모형 loss 함수

로지시트 회귀모형

$$\text{cost} = (\sigma(\hat{y}) - y)^2$$

$$\text{cost} = (\sigma(\hat{y}) - y)^2$$

$$\text{cost} = -[y \ln \sigma(\hat{y}) + (1 - y) \ln(1 - \sigma(\hat{y}))]$$

미분하면 $2\sigma(\hat{y})(\sigma(\hat{y}))'$

즉, 미분하면 1과 0에 수렴하는

부분은 굉장히 작은 값으로 나타내어
진다. 그러므로 학습이 느려짐.

성질

1. 예측 값인 $\sigma(\hat{y})$ 은 0~1사이 값. 그러므로 항상 음의 값만 존재
2. $\sigma(\hat{y})$ 가 y 에 가까운 값일 수록 0에 가까워짐.

0. 어제 무엇을 배웠나요?

1. Data 생성 or DATA 읽기
2. DATA의 변수에 따른 차원 확인
3. PERCEPTRON의 입력 차원 맞추기
4. PERCEPTRON 생성
5. PERCEPTRON LOSS 함수 지정
6. 경사하강법 (LOSS 함수의 MIN을 찾기 위한 최적화 방법 선택)
7. 학습완료에 따른 결과 보기.

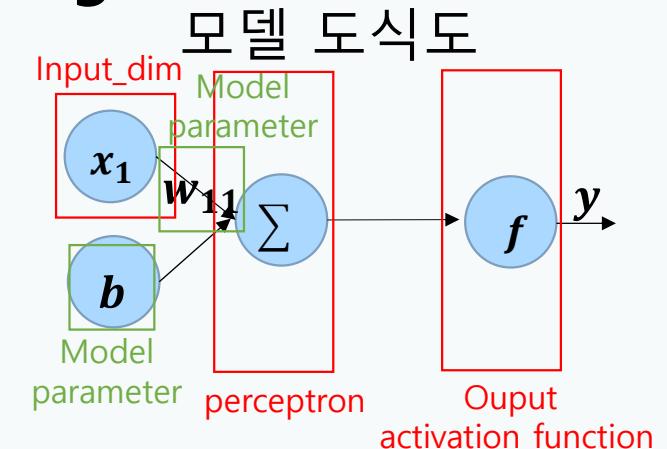
0. 어제 무엇을 배웠나요?

Single neuron model : perception logistic regression

```

3 ## data 선언
4 x_data = [[2.], [4.], [6.], [8.], [10.], [12.], [14.]]
5 y_data = [[0.], [0.], [0.], [1.], [1.], [1.], [1.]]
6 test_data= [[3.]]
7 test_data2= [[7.]]
8 test_data3= [[17.]]
9 test_data4= [[60.]]
10
11 ## tf.keras를 활용한 perceptron 모델 구현.
12 model = tf.keras.Sequential() ## 모델 선언
13 model.add(tf.keras.layers.Dense(1, input_dim=1, activation='sigmoid')) # 선언된 모델에 add를 통해 쌓아감. 은닉층
14 model.summary()
15
16 # 모델 loss, 학습 방법 결정하기
17 optimizer=tf.keras.optimizers.SGD(learning_rate=0.007) ### 경사 하강법으로 global min에 찾아가는 최적화 방법 선언.
18 loss=tf.keras.losses.binary_crossentropy
19 metrics=tf.keras.metrics.binary_accuracy
20
21 # 모델 컴파일하기 - 모델 및 loss 등 구조화한 모델을 컴퓨터가 동작 할수 있도록 변환
22 model.compile(loss=loss, optimizer=optimizer, metrics=[metrics])
23
24 # 모델 동작하기
25 model.fit(x_data, y_data, epochs=5000, batch_size=9)
26
27 # 결과를 출력합니다.
28 print(" test data [3.] 예측 값 : ", model.predict(test_data))
29 print(" test data [7.] 예측 값 : ", model.predict(test_data2))
30 print(" test data [17.] 예측 값 : ", model.predict(test_data3))
31 print(" test data [60.] 예측 값 : ", model.predict(test_data4))

```



모델 summary

Layer (type)	Output shape	Param #
<hr/>		
dense (Dense)	(None, 1)	2
<hr/>		
Total params: 2		
Trainable params: 2		
Non-trainable params: 0		
<hr/>		
Train on 7 samples		
Epoch 1/1000		

W11, b

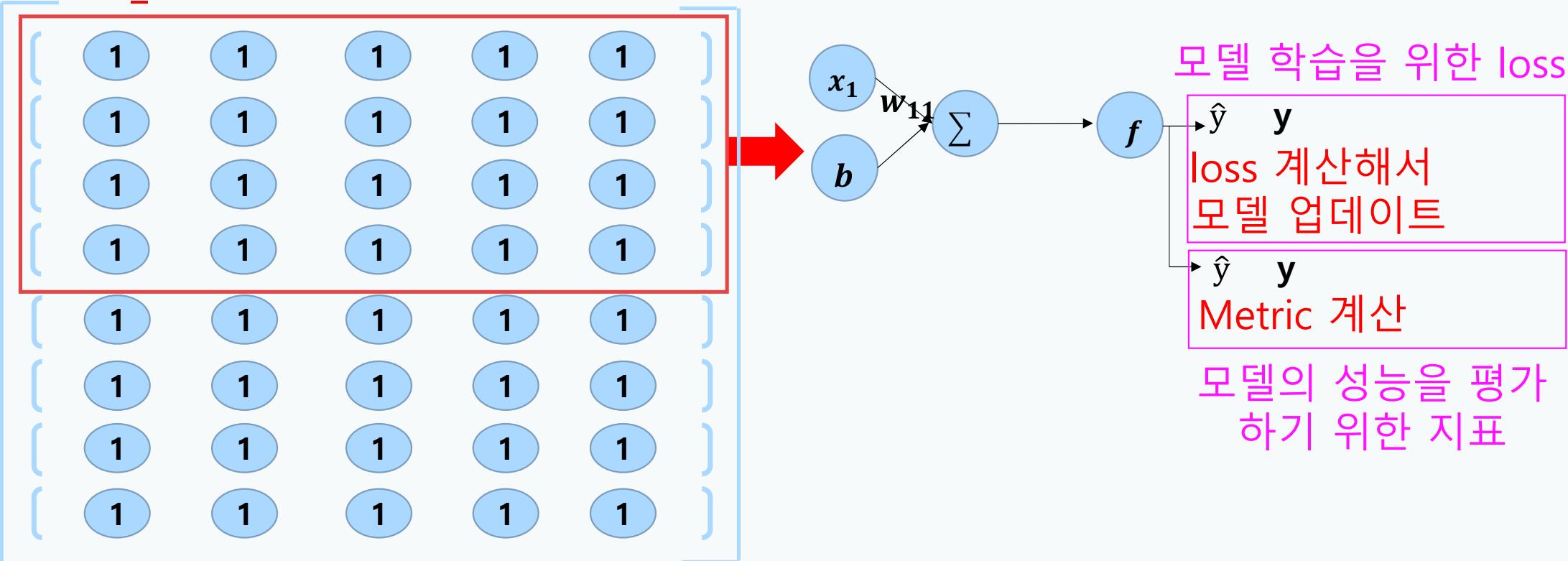
324

practice : P_01_08_tensor_cross_entropy.ipynb

0. 어제 무엇을 배웠나요?

Batch_size=4

데이터 분리 학습 과정 살펴보기



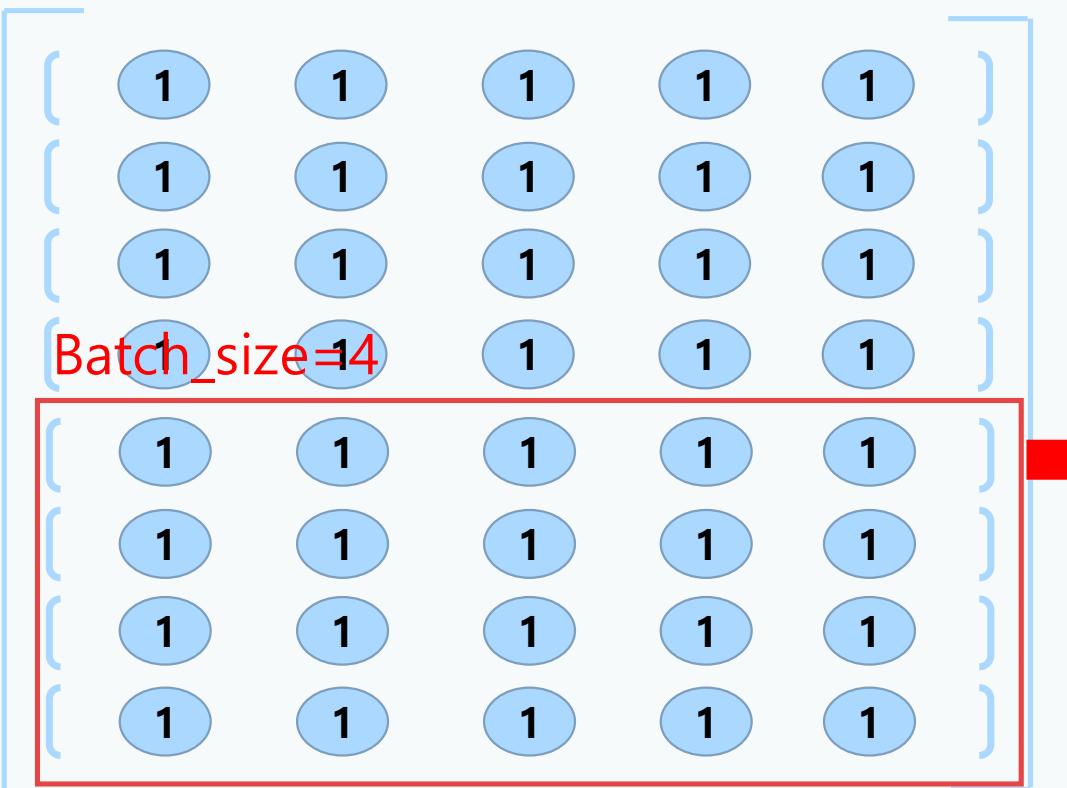
모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

325

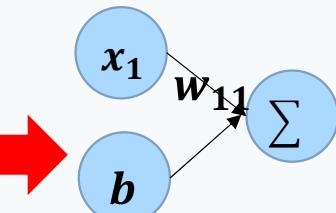
0. 어제 무엇을 배웠나요?

데이터 분리 학습 과정 살펴보기



모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```



모델 학습을 위한 loss

\hat{y} y
loss 계산해서
모델 업데이트

→ \hat{y} y

Metric 계산

모델의 성능을 평가하기 위한 지표

0. 어제 무엇을 배웠나요?

데이터 분리 학습 과정 살펴보기



모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

모델 학습을 위한 loss

loss 계산해서
모델 업데이트

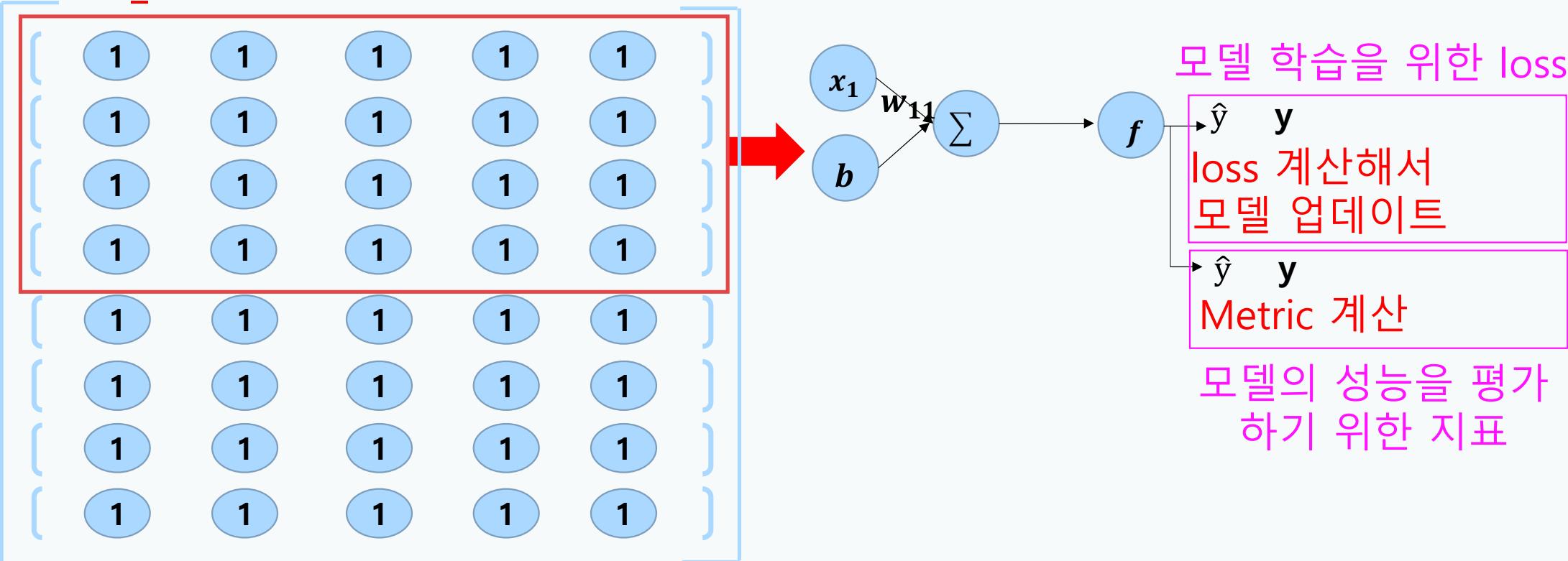
\hat{y} y
Metric 계산

모델의 성능을 평가
하기 위한 지표

0. 어제 무엇을 배웠나요?

Batch_size=4

데이터 분리 학습 과정 살펴보기



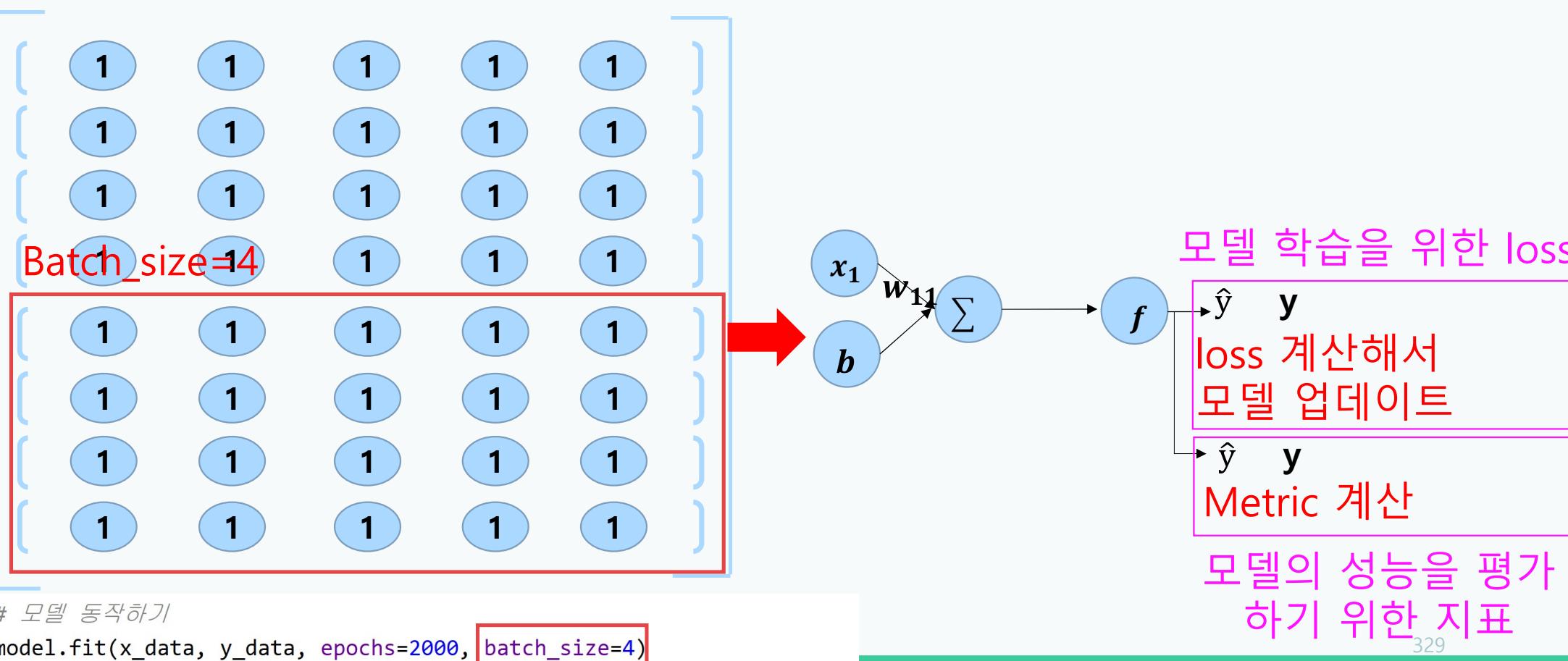
모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

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0. 어제 무엇을 배웠나요?

데이터 분리 학습 과정 살펴보기

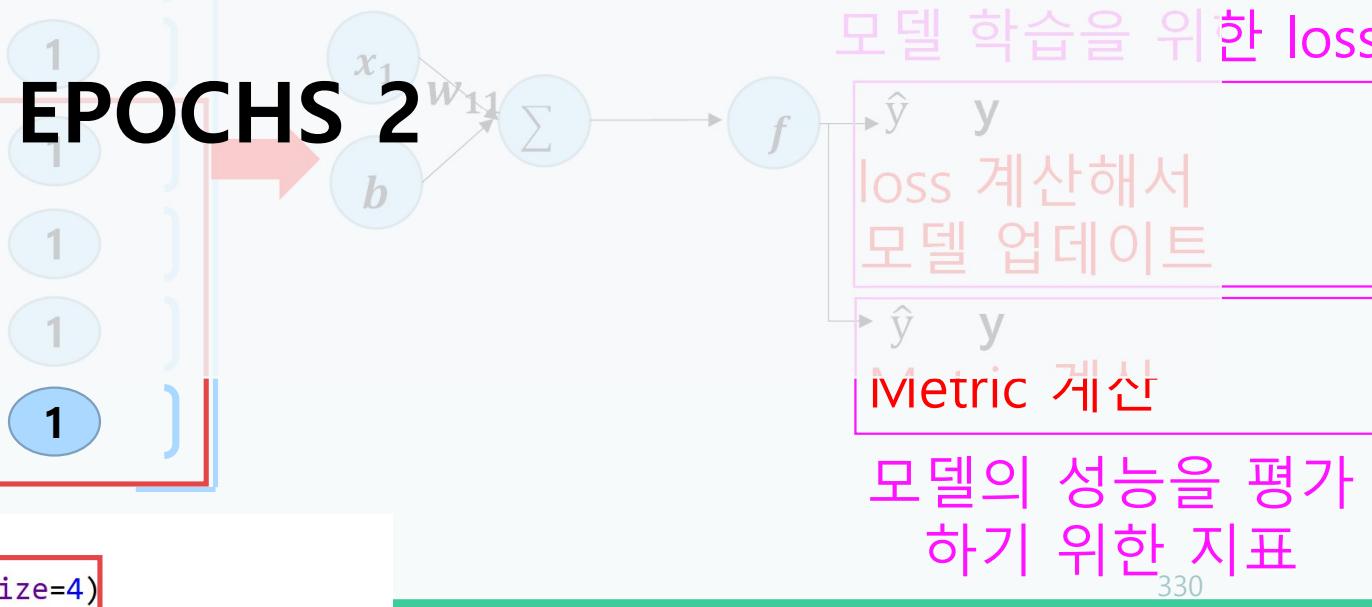


0. 어제 무엇을 배웠나요?

데이터 분리 학습 과정 살펴보기



```
# 모델 동작하기  
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

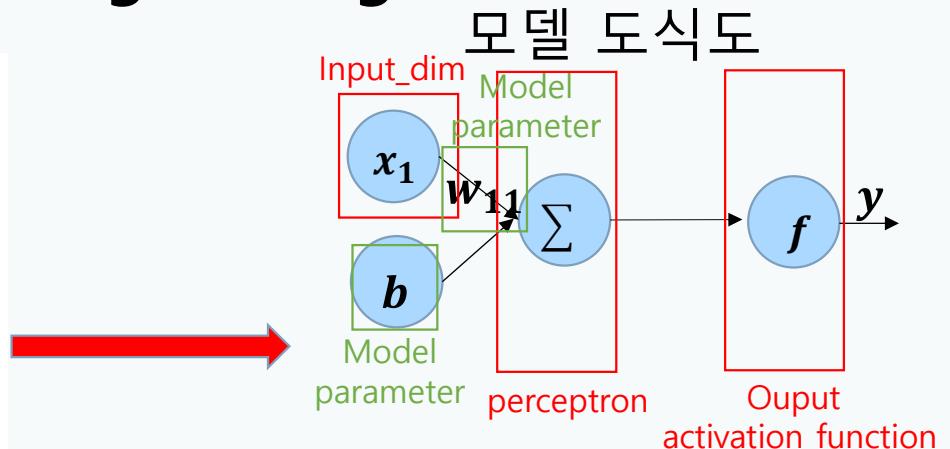


0. 어제 무엇을 배웠나요?

Single neuron model : perception logistic regression

```
Layer (type)          Output Shape         Param #  
=====            ======           ======-----  
dense (Dense)        (None, 1)           2  
=====            ======           ======-----  
Total params: 2  
Trainable params: 2  
Non-trainable params: 0  
  
Train on 7 samples  
Epoch 1/1000
```

```
x_data = [[2.], [4.], [6.], [8.], [10.], [12.], [14.]]  
y_data = [[0.], [0.], [0.], [1.], [1.], [1.], [1.]]  
  
x_data = [[2.], [4.], [6.], [8.], [10.], [12.], [14.]]  
y_data = [[0.], [0.], [0.], [1.], [1.], [1.], [1.]]
```



데이터 입력 차원 : Perceptron (node)
(4, 1) (3, 1)
Sigmoid

0. 어제 무엇을 배웠나요?

Single neuron model : perception logistic regression

Activation + Cross Entropy loss 적용

공부 일수	합격 여부(y)
5	불합격 -> 0
30	불합격 -> 0
95	불합격 -> 0
100	불합격 -> 0
265	합격 -> 1
270	합격 -> 1
290	합격 -> 1
300	합격 -> 1
365	합격 -> 1

0. 오늘 하루 동안 무엇을 하나요?

1. XOR 문제

- AND GATE
- OR GATE
- XOR GATE

2. Neural Network

3. 역전파 알고리즘

3. Neural Network 실습

- NN Regression
- Data normalization
- Data 분리 하기
- NN Binary classification

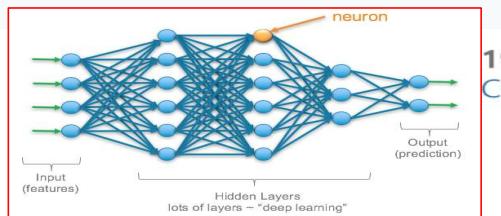
5. Perceptron Summary

오늘의 학습 목표

Deep Learning

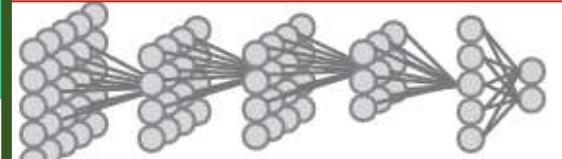
신경망의 70년

regression, classification



Day4 학습 목표

regression, classification



CNN Model

2016년
DeepMind AlphaGo



1943년
최초 인공신경망



워렌 맥컬록과 월터 피츠

1969년
Perceptron 한계 제시



마빈 민스키, 시모어 페퍼트

1974년, 1980년
역전파 알고리즘



- 폴 웨보스,
- 데이비드 루멜하트, 제임스 맥클레랜드,
- 제프리 힌튼, 로널드 윌리암스
- 데이비드 파커, 얀 르쿤

Day3 학습 목표

2006년
Deep Learning



Day6 학습 목표 : 심화

2012년
AlexNet
IMAGENET



2014년
Generative Adversarial Network (GAN)



19C-20C 초반
생체 신경망



이반 파블로프

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Day1 학습 목표

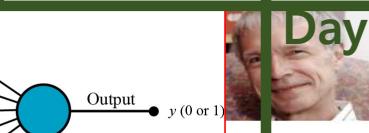
Perceptron



로젠블랫

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1982년
Recurrent Neural
Network (RNN)



Day5 학습 목표

2012년
YouTube 1,000만 이미지에서 고양이 인식



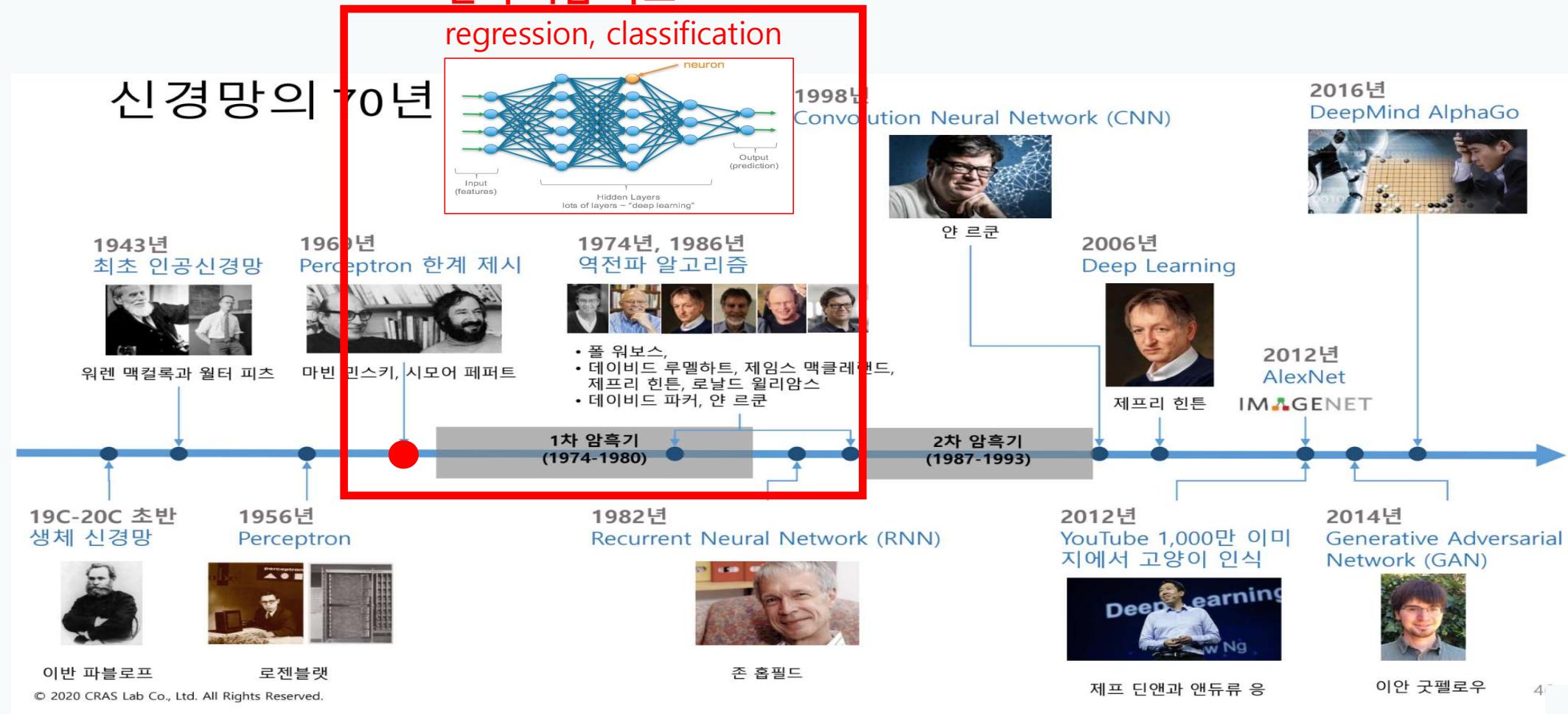
제프 딘앤과 앤드류 응

regression, classification

진도상황에 따라 변경될 수 있음

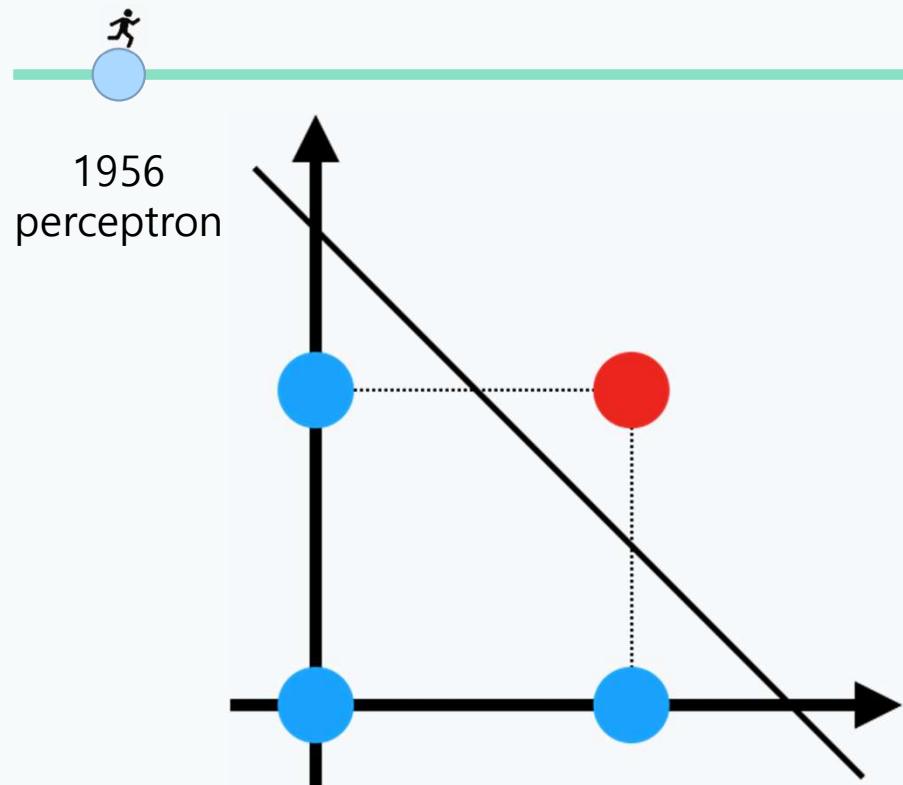
1. PERCEPTRON XOR 문제

오늘의 학습 목표



1. PERCEPTRON XOR 문제

- Perceptron – AND Gate

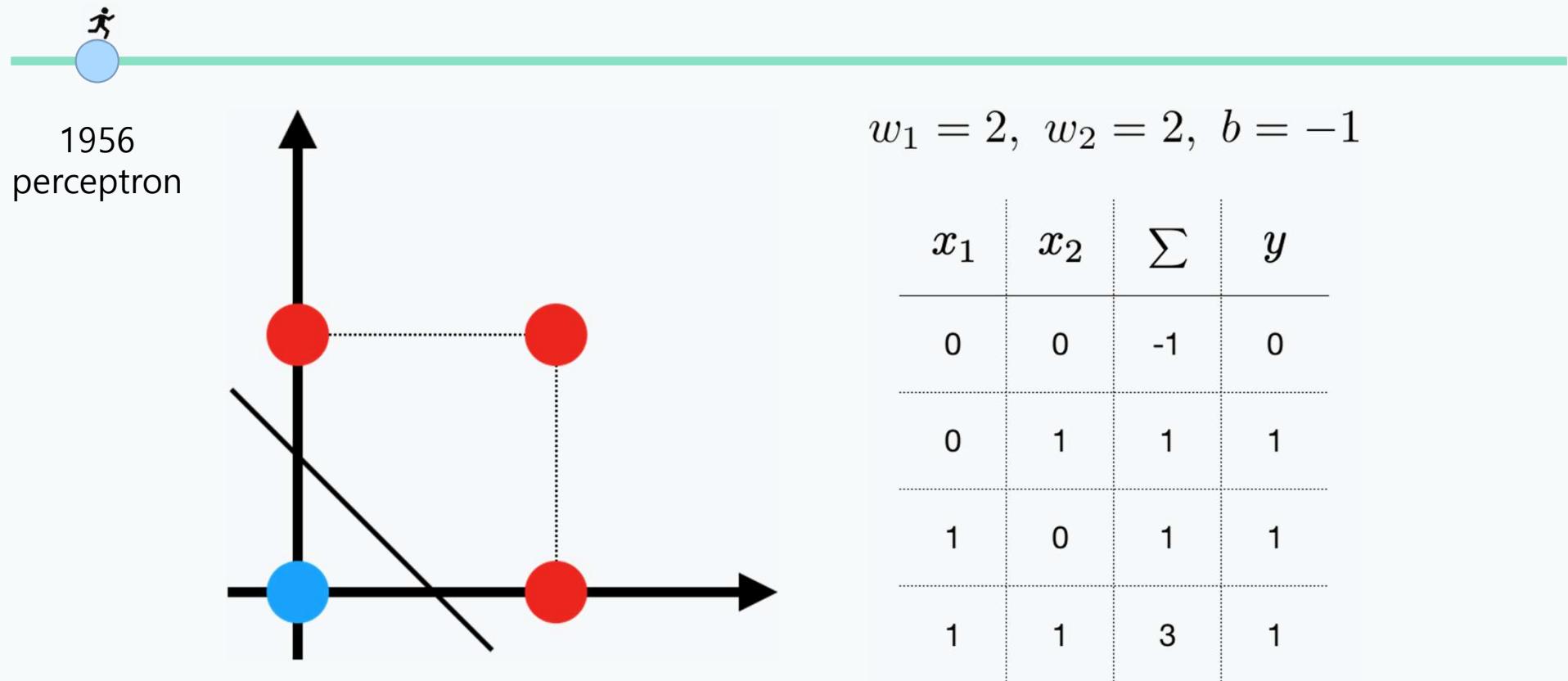


$$w_1 = 2, w_2 = 2, b = -3$$

x_1	x_2	\sum	y
0	0	-3	0
0	1	-1	0
1	0	-1	0
1	1	1	1

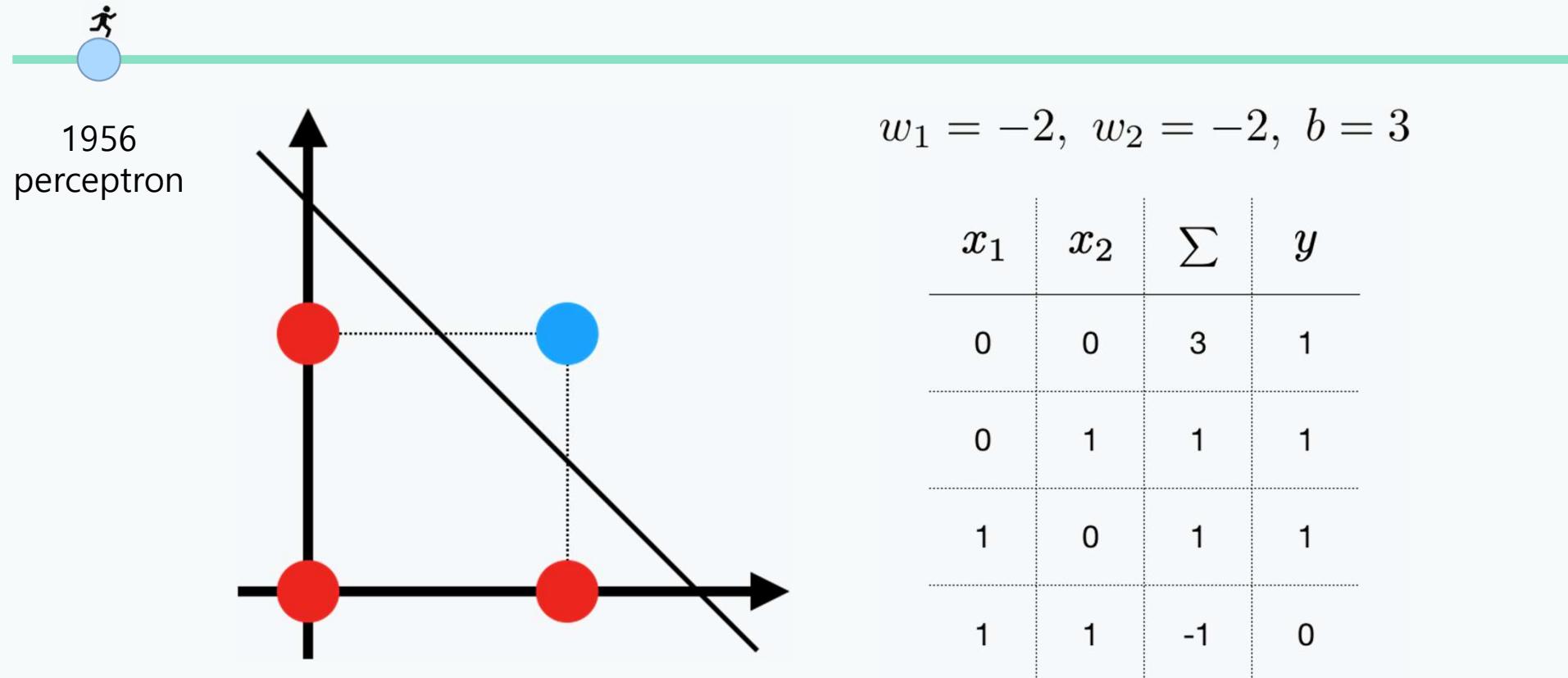
1. PERCEPTRON XOR 문제

- Perceptron – OR Gate



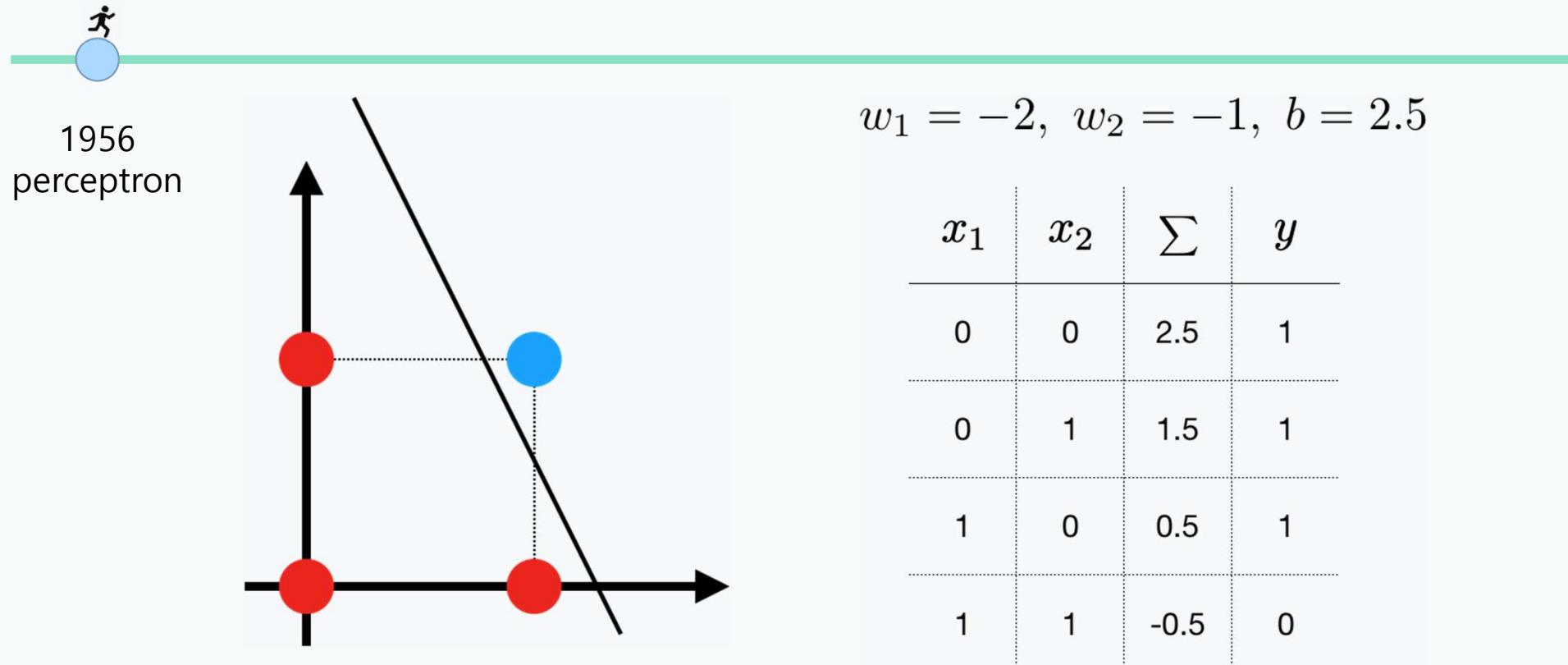
1. PERCEPTRON XOR 문제

- Perceptron – NAND Gate



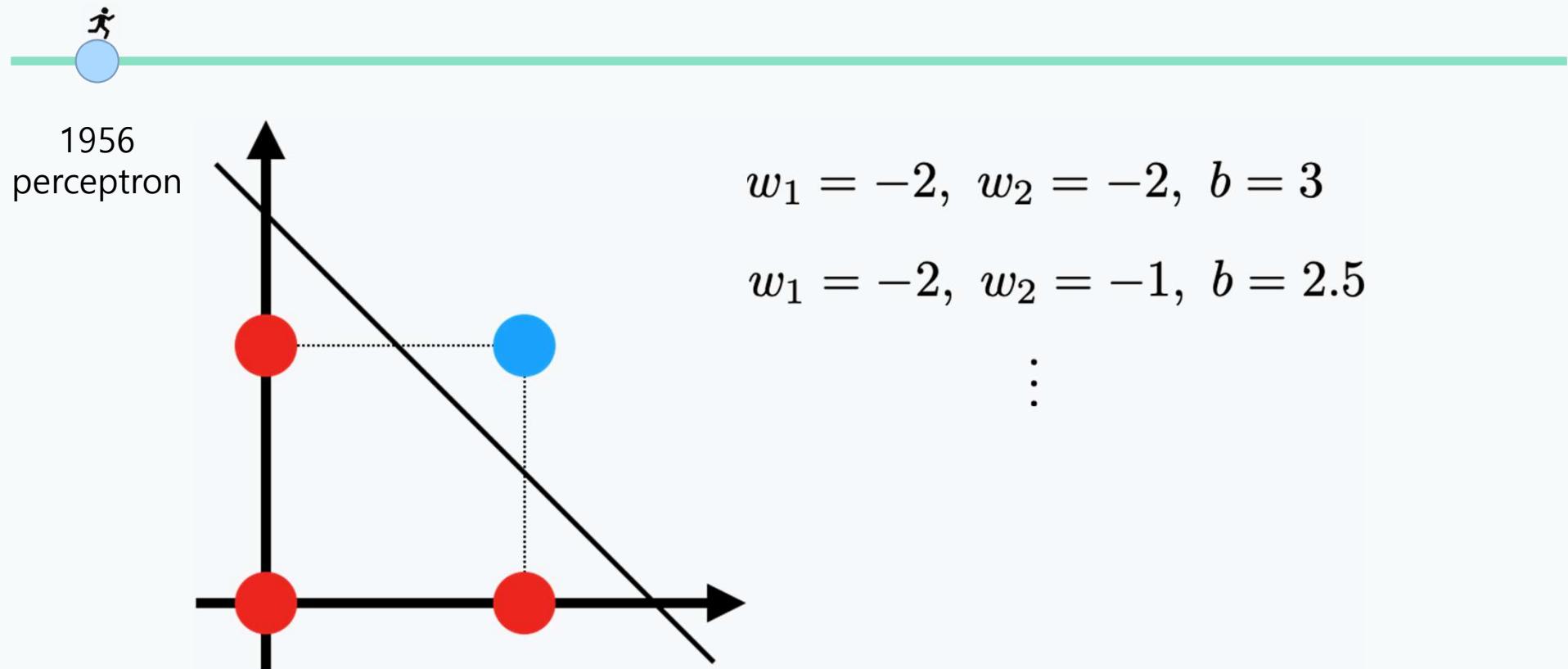
1. PERCEPTRON XOR 문제

- Perceptron – NAND Gate



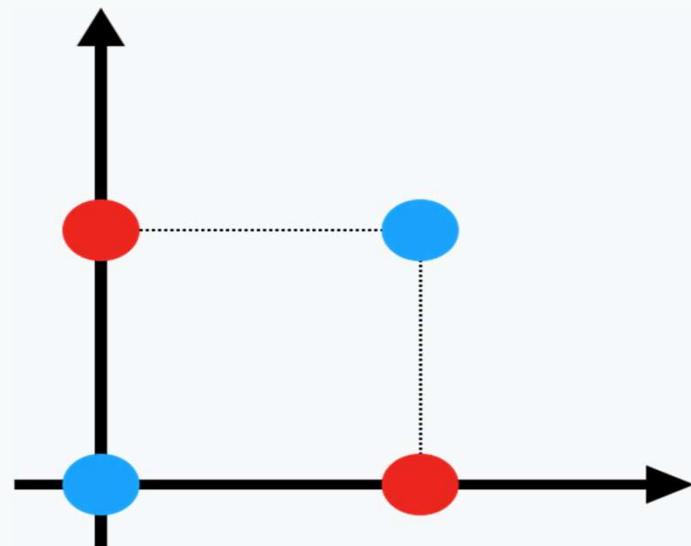
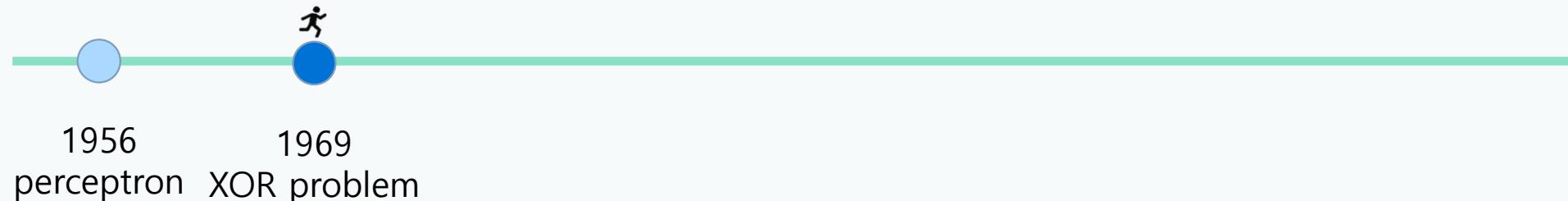
1. PERCEPTRON XOR 문제

- Perceptron – NAND Gate



1. PERCEPTRON XOR 문제

- Perceptron – XOR 문제



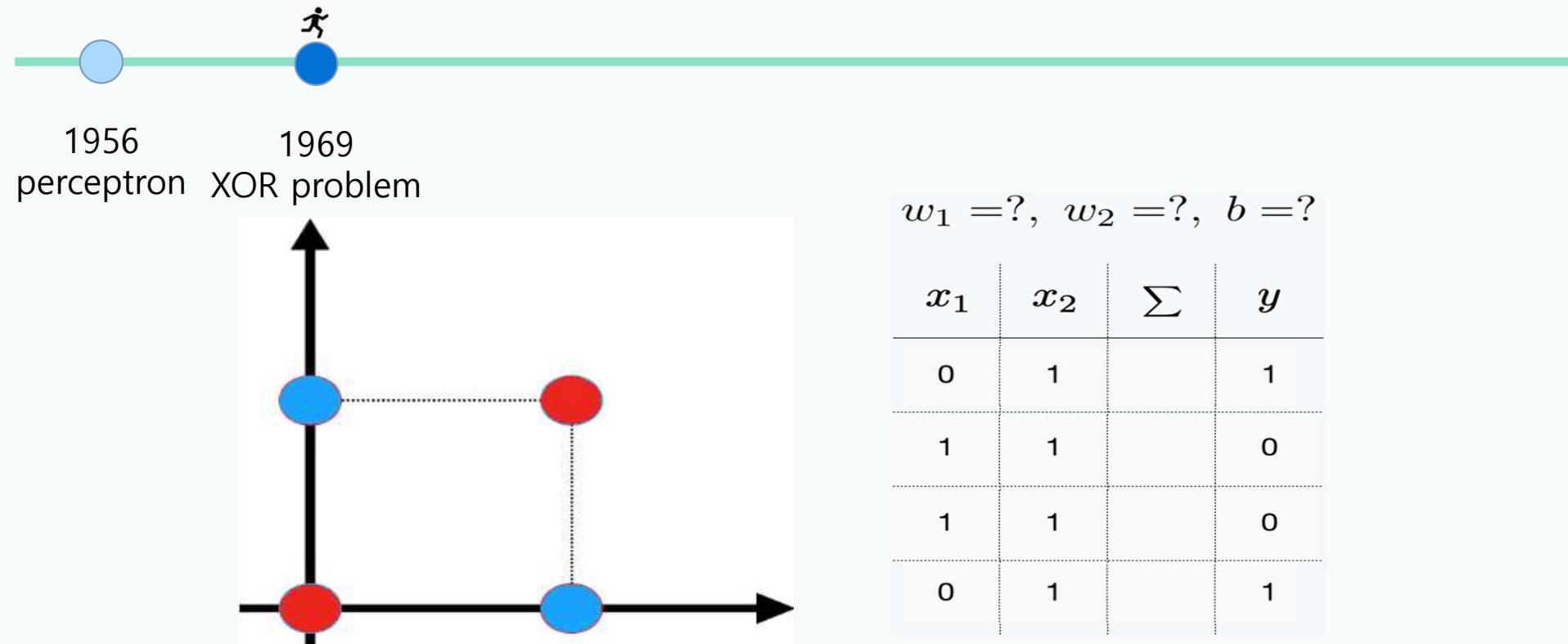
$$w_1 = ?, \quad w_2 = ?, \quad b = ?$$

x_1	x_2	Σ	y
0	0		0
0	1		1
1	0		1
1	1		0

practice : P_02_00_XOR_problem.py 341

1. PERCEPTRON XOR 문제

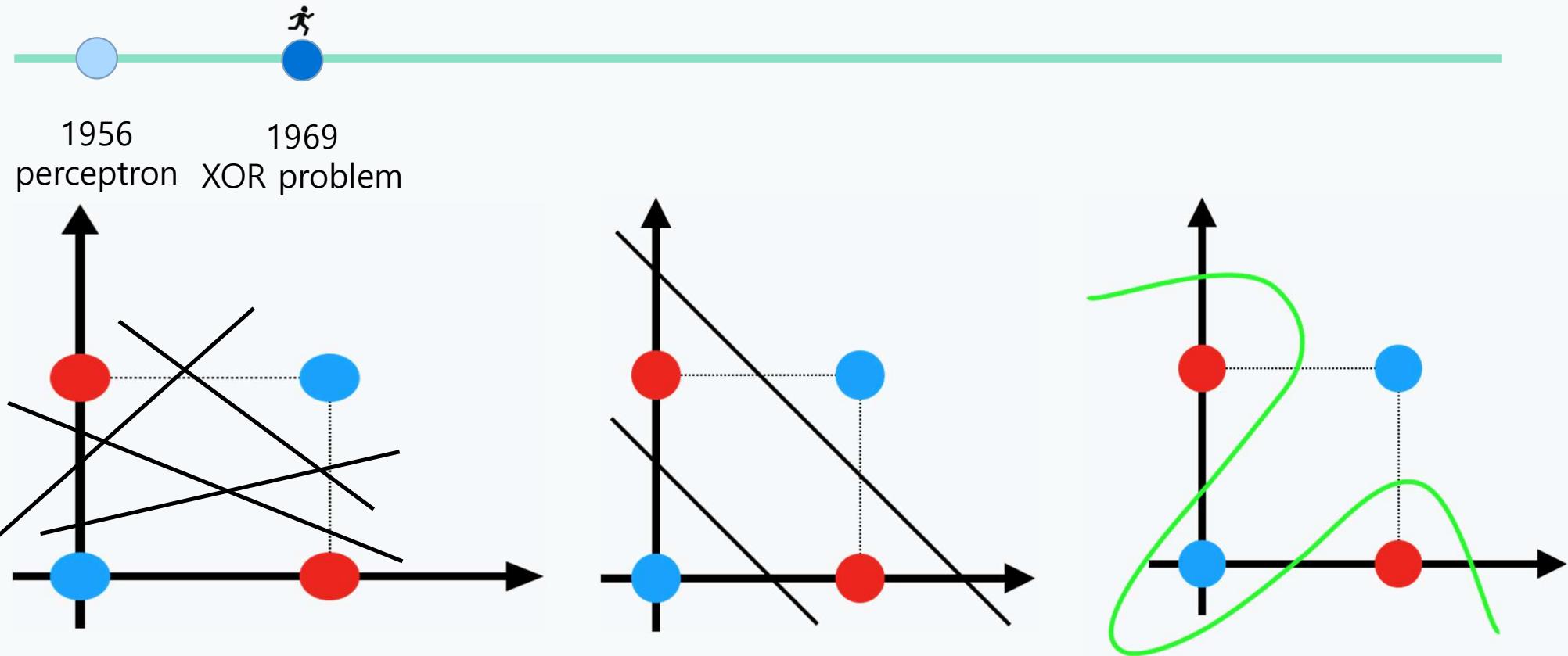
- Perceptron – XOR 문제



excise : 02_00_XOR_problem.py 342

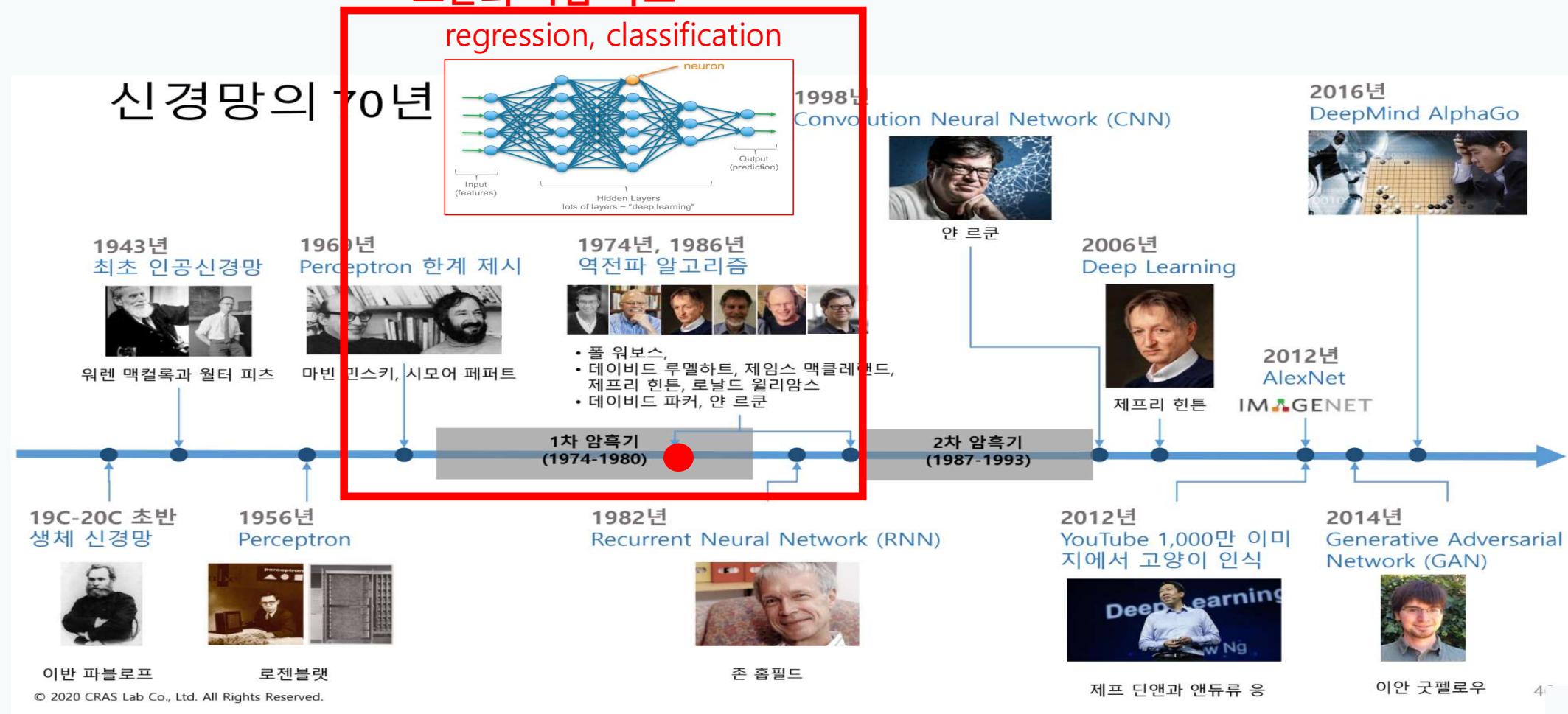
1. PERCEPTRON XOR 문제

- Perceptron – XOR 문제



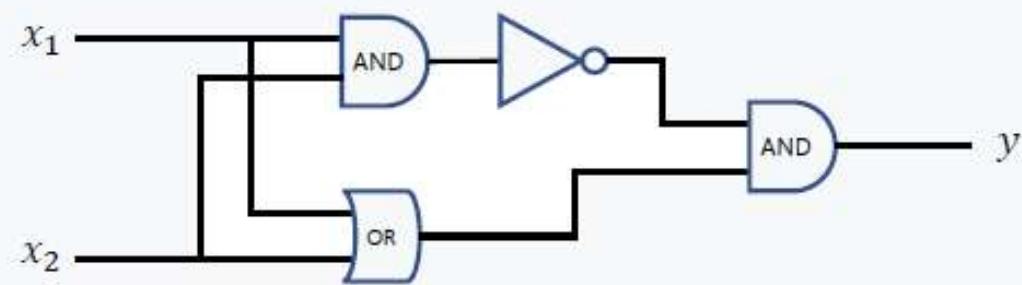
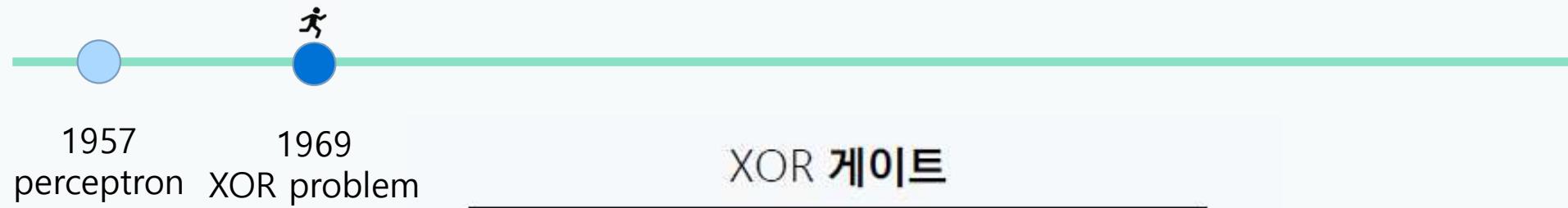
1. PERCEPTRON XOR 문제

오늘의 학습 목표



1. PERCEPTRON XOR 문제

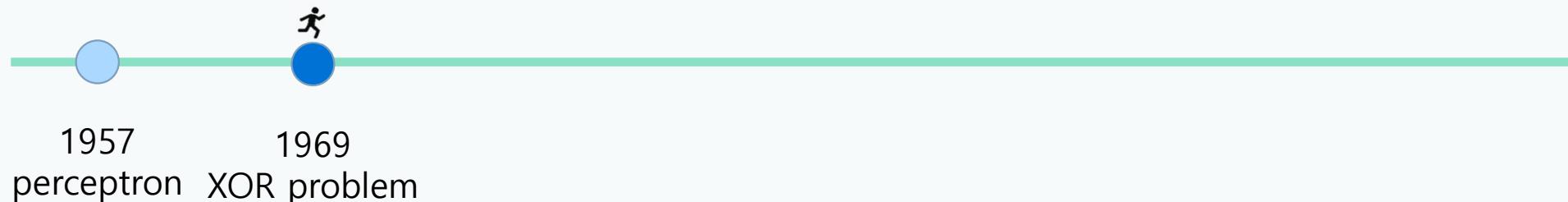
- Perceptron – XOR 문제



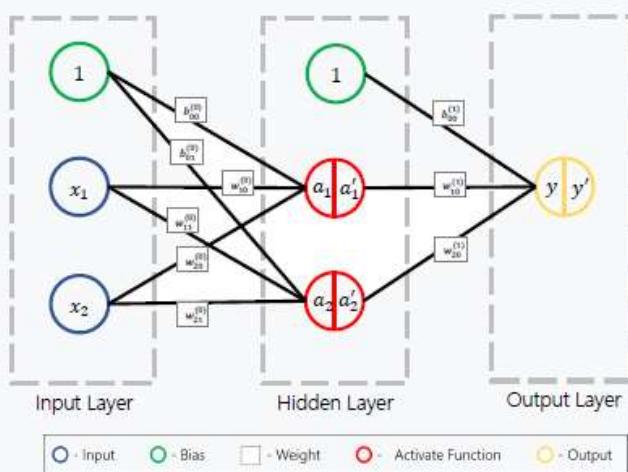
XOR 게이트는 AND 와 OR 게이트의 조합으로 만들 수 있구나

1. PERCEPTRON XOR 문제

- Perceptron – XOR 문제

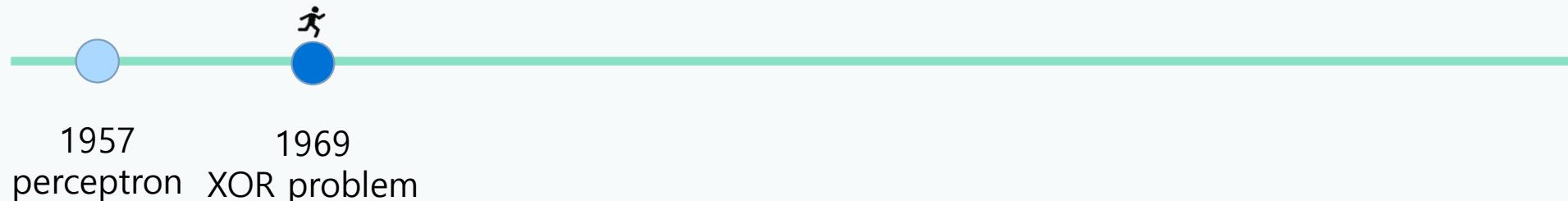


그럼 퍼셉트론 여러 개를 쌓아보자 : MLP

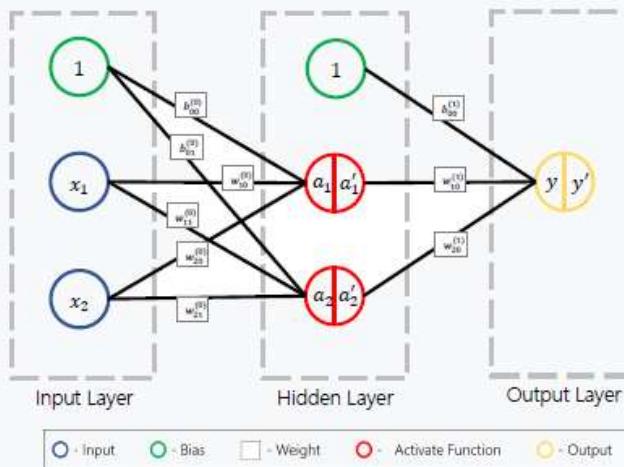


1. PERCEPTRON XOR 문제

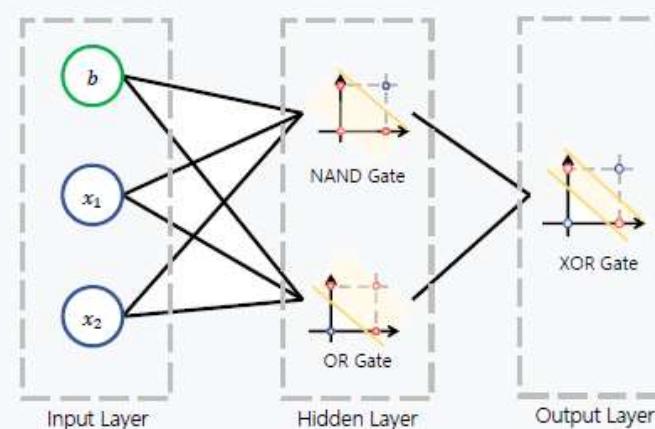
- Perceptron – XOR 문제



그럼 퍼셉트론 여러 개를 쌓아보자 : MLP



MLP로 XOR 게이트를 풀어보자



MLP로도 XOR 게이트를 만들어 낼 수 있다

1. PERCEPTRON XOR 문제

- Perceptron – XOR 문제



1957 1969

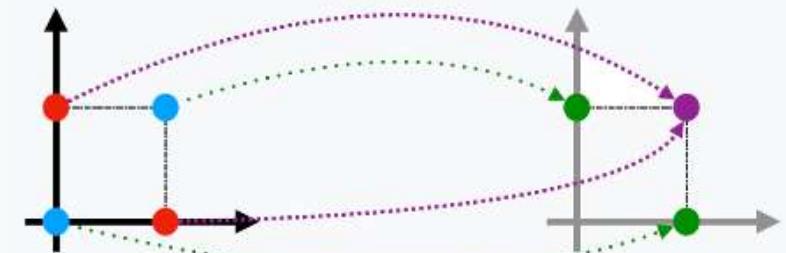
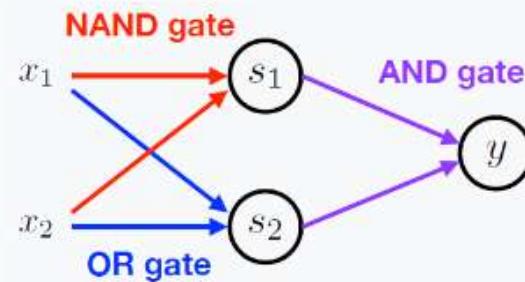
perceptron XOR problem

$w_1 = -2, w_2 = -2, b = 3$ $w_1 = 2, w_2 = 2, b = -1$ $w_1 = 2, w_2 = 2, b = -3$

x_1	x_2	Σ	s_1
0	0	3	1
0	1	1	1
1	0	1	1
1	1	-1	0

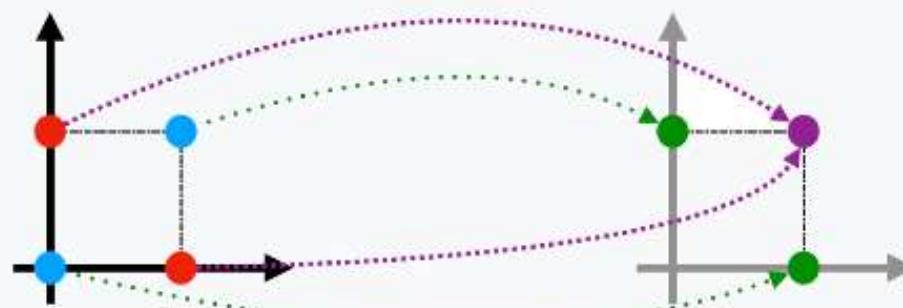
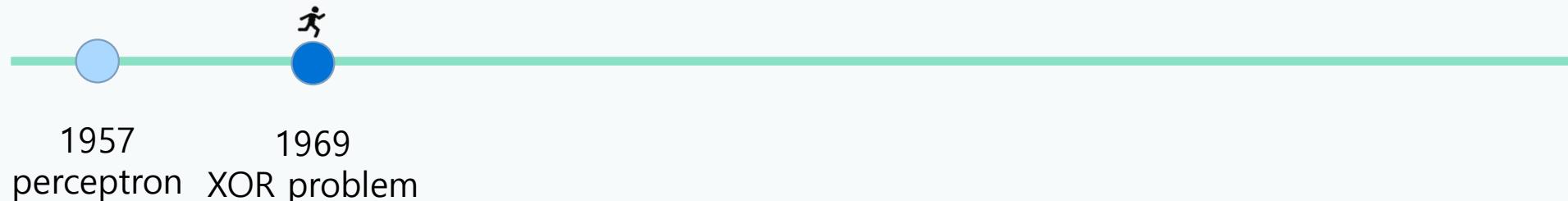
x_1	x_2	Σ	s_2
0	0	-1	0
0	1	1	1
1	0	1	1
1	1	3	1

s_1	s_2	Σ	y
1	0	-1	0
1	1	1	1
1	1	1	1
0	1	-1	0



1. PERCEPTRON XOR 문제

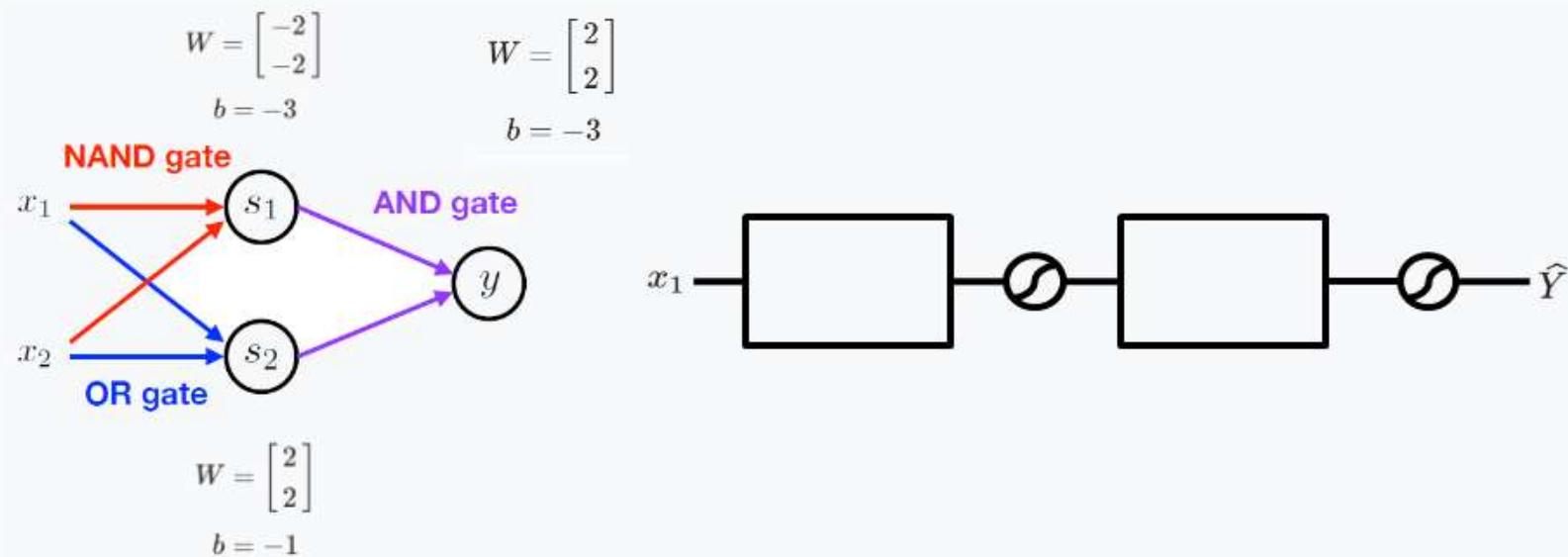
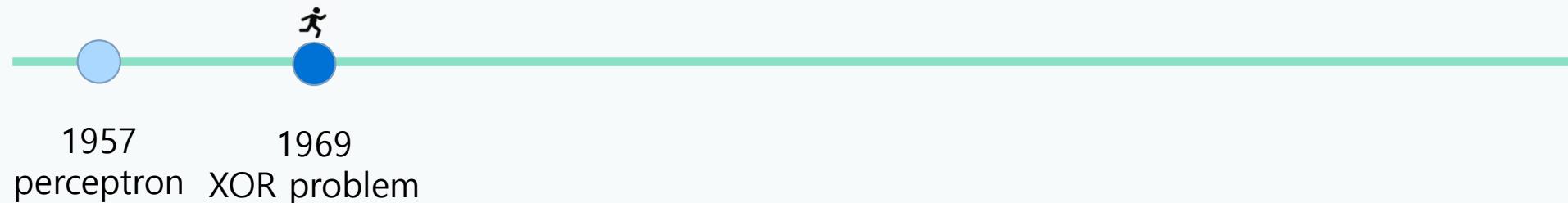
- Perceptron – XOR 문제



to map space X to space Y

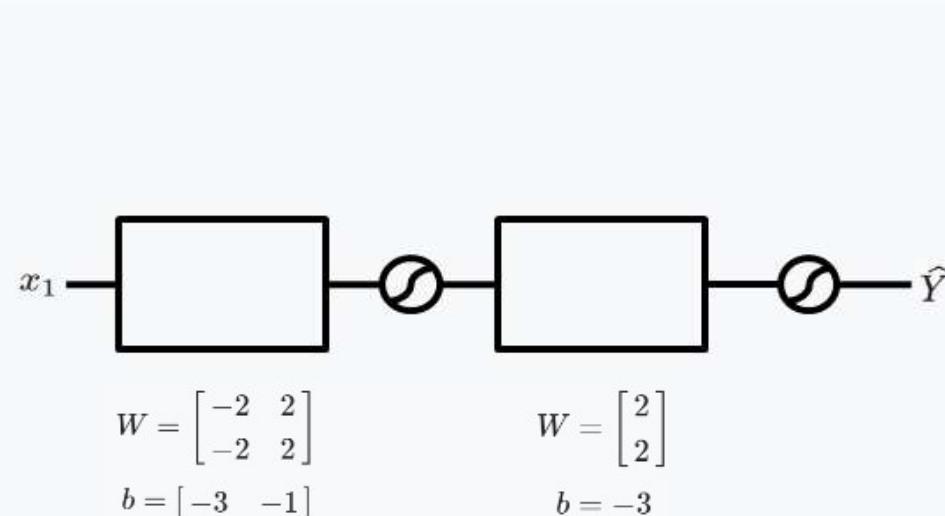
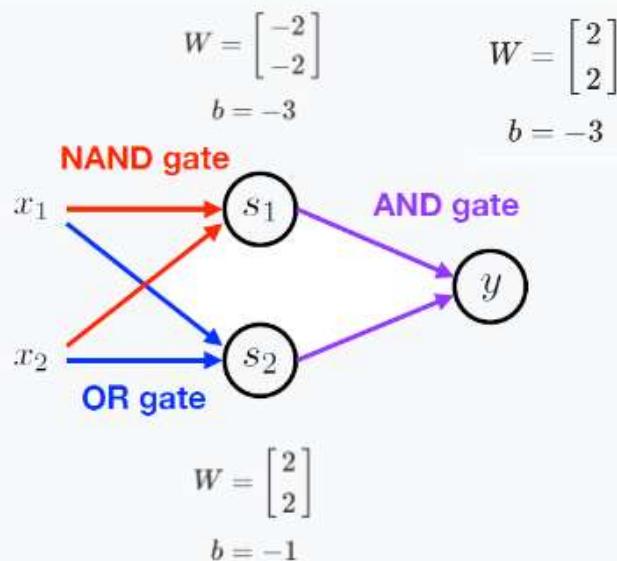
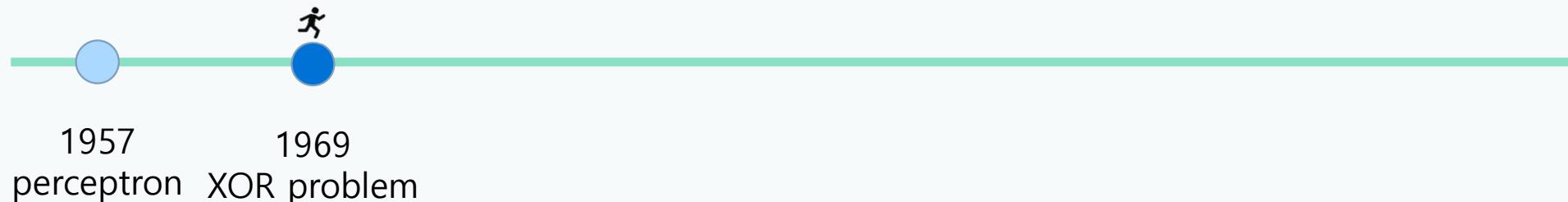
1. PERCEPTRON XOR 문제

- Perceptron – XOR 문제



1. PERCEPTRON XOR 문제

- Perceptron – XOR 문제



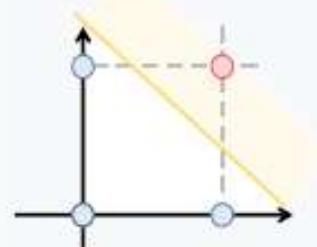
1. PERCEPTRON XOR 문제

- Perceptron – XOR 문제

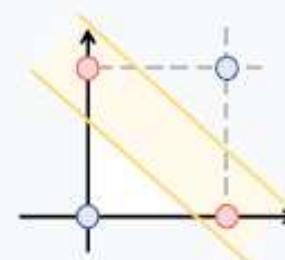


Layer 의 개수에 따라 결정할 수 있는 영역

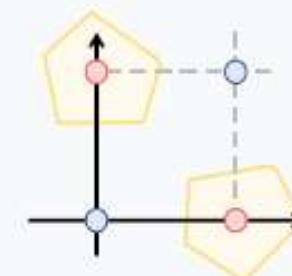
1 hidden layer



2 hidden layer

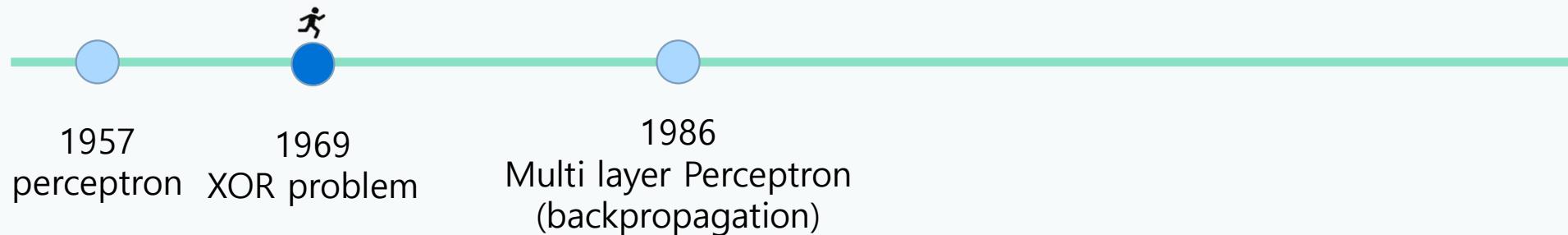


3 hidden layer



2. Neural Network

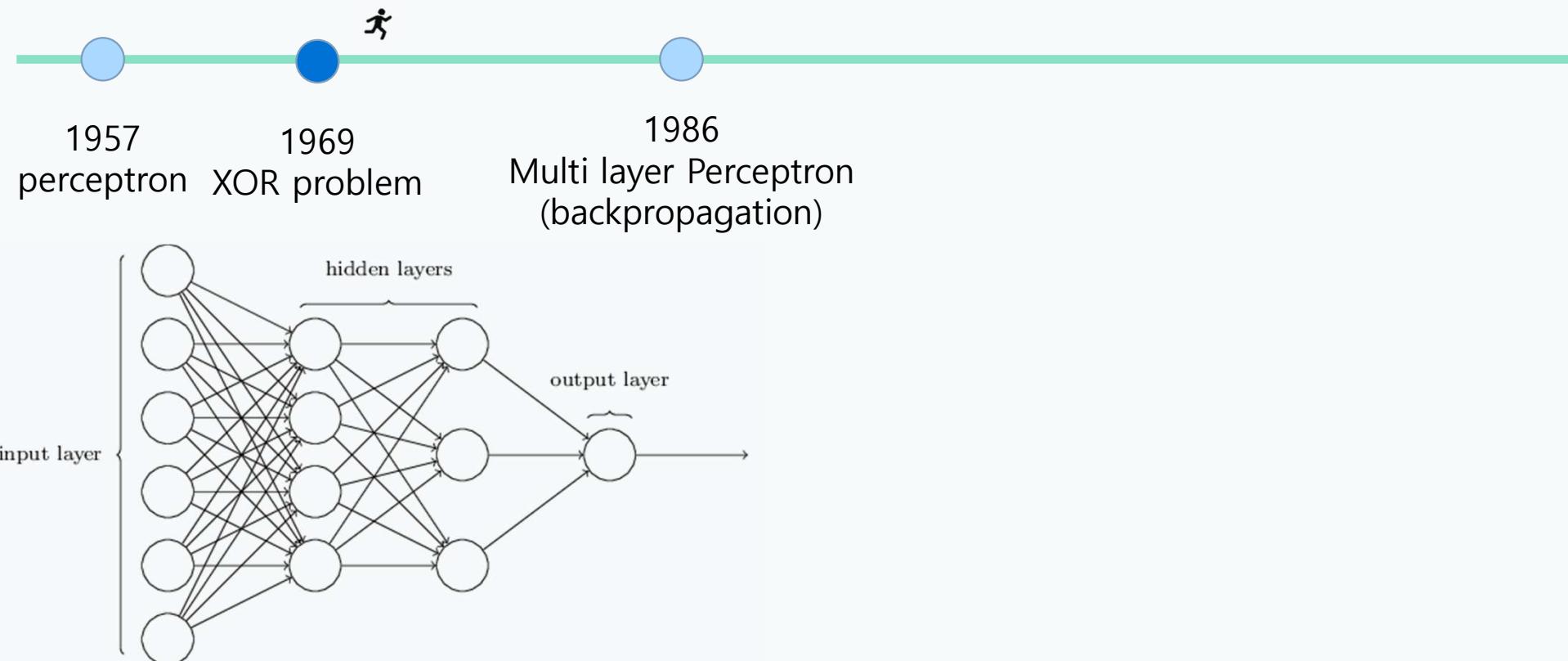
- Neural Network or Multi Layer Perceptron



많은 perceptron을 쌓아서 비선형의 데이터를
선형 분리가 가능하도록 단순화 시킴

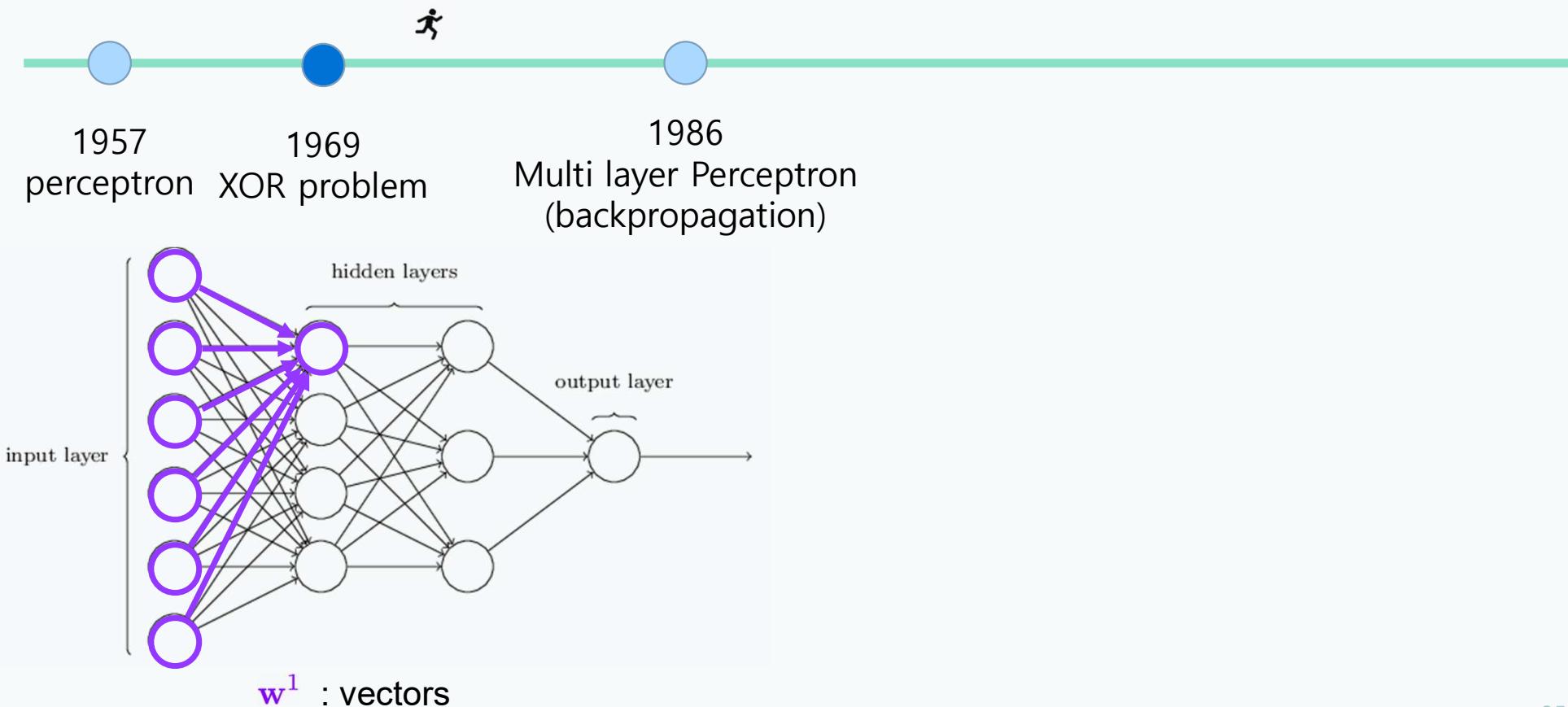
2. Neural Network

- Neural Network or Multi Layer Perceptron



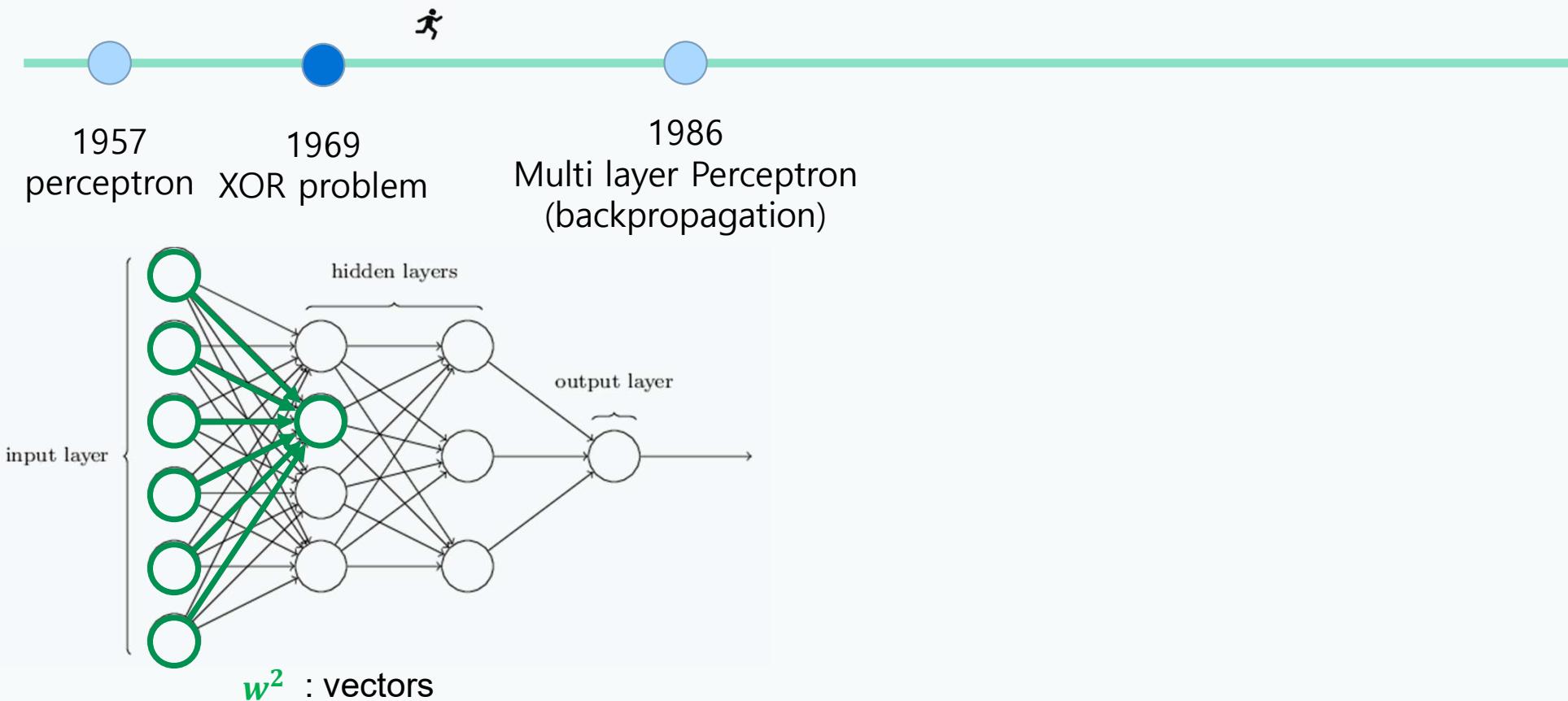
2. Neural Network

- Neural Network or Multi Layer Perceptron



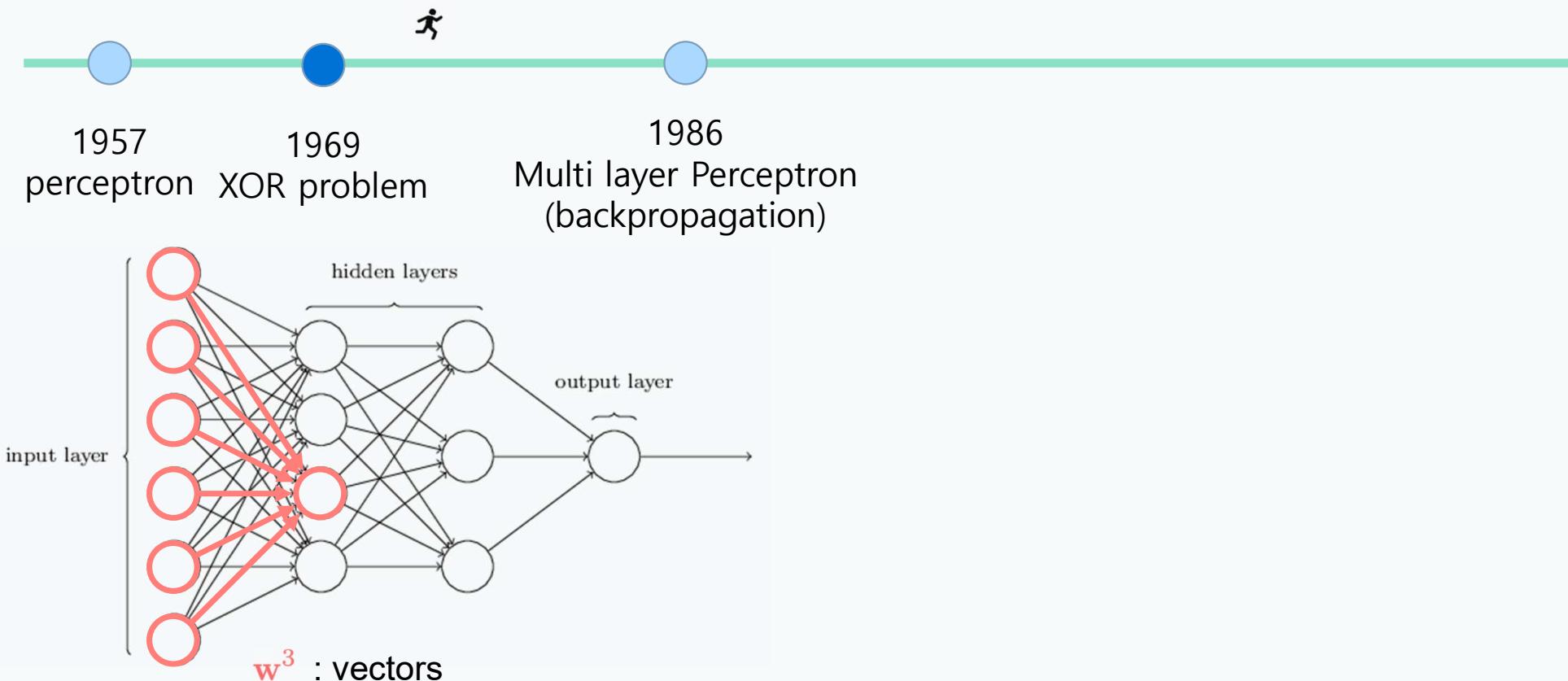
2. Neural Network

- Neural Network or Multi Layer Perceptron



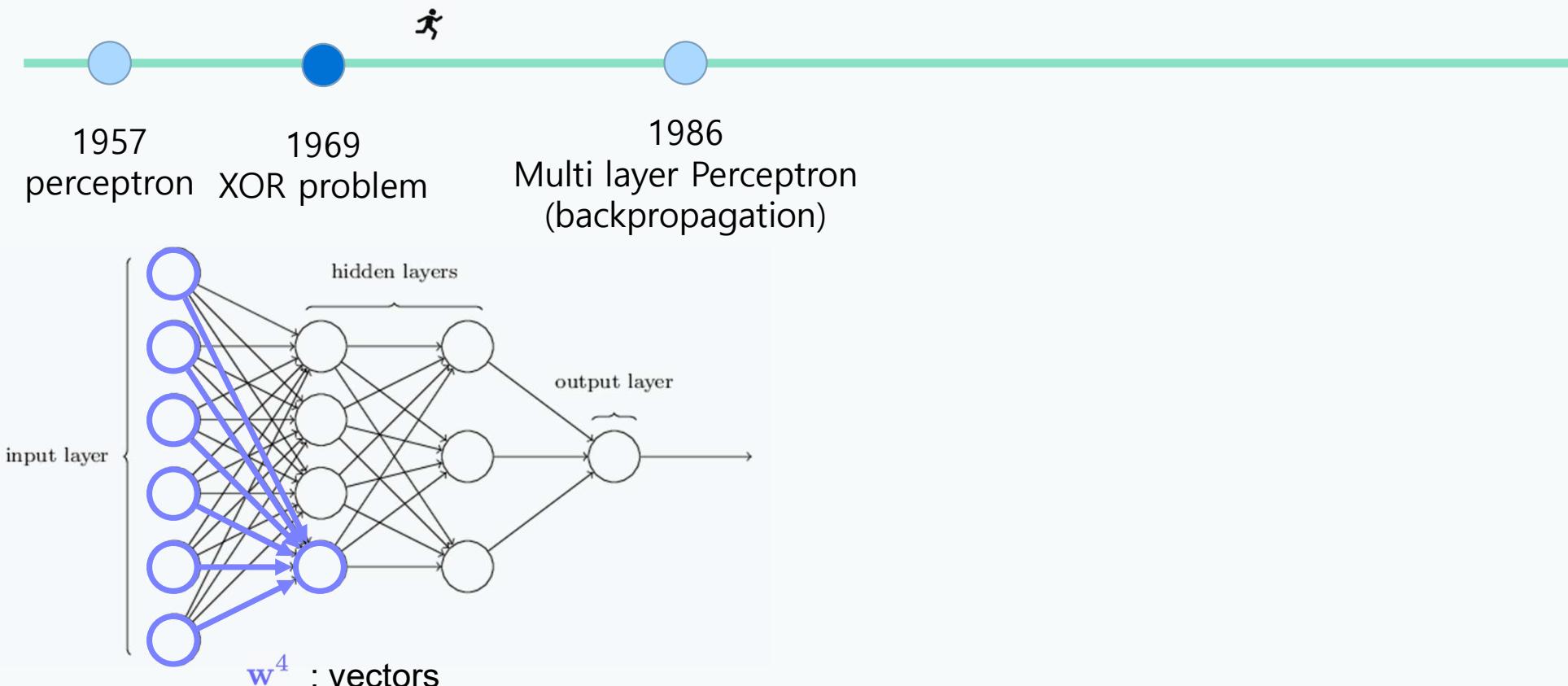
2. Neural Network

- Neural Network or Multi Layer Perceptron



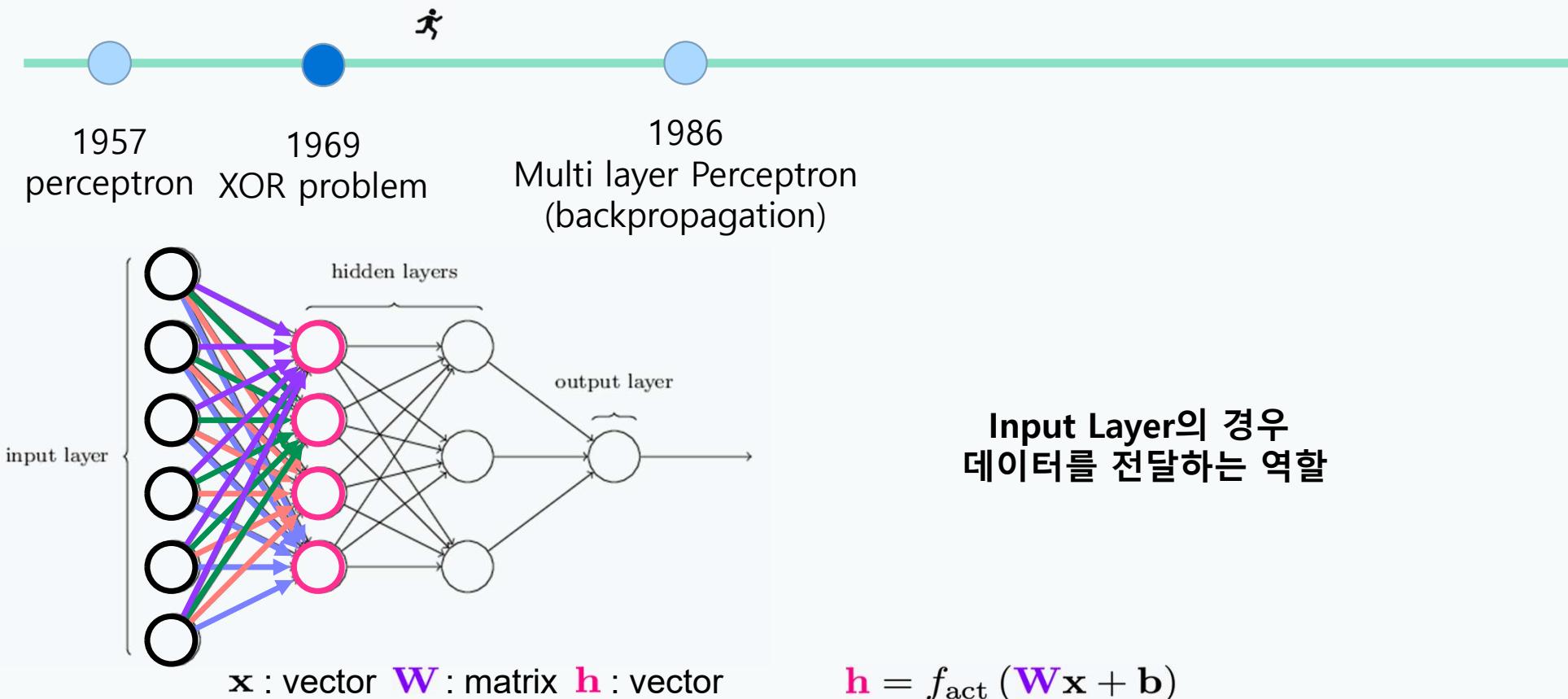
2. Neural Network

- Neural Network or Multi Layer Perceptron



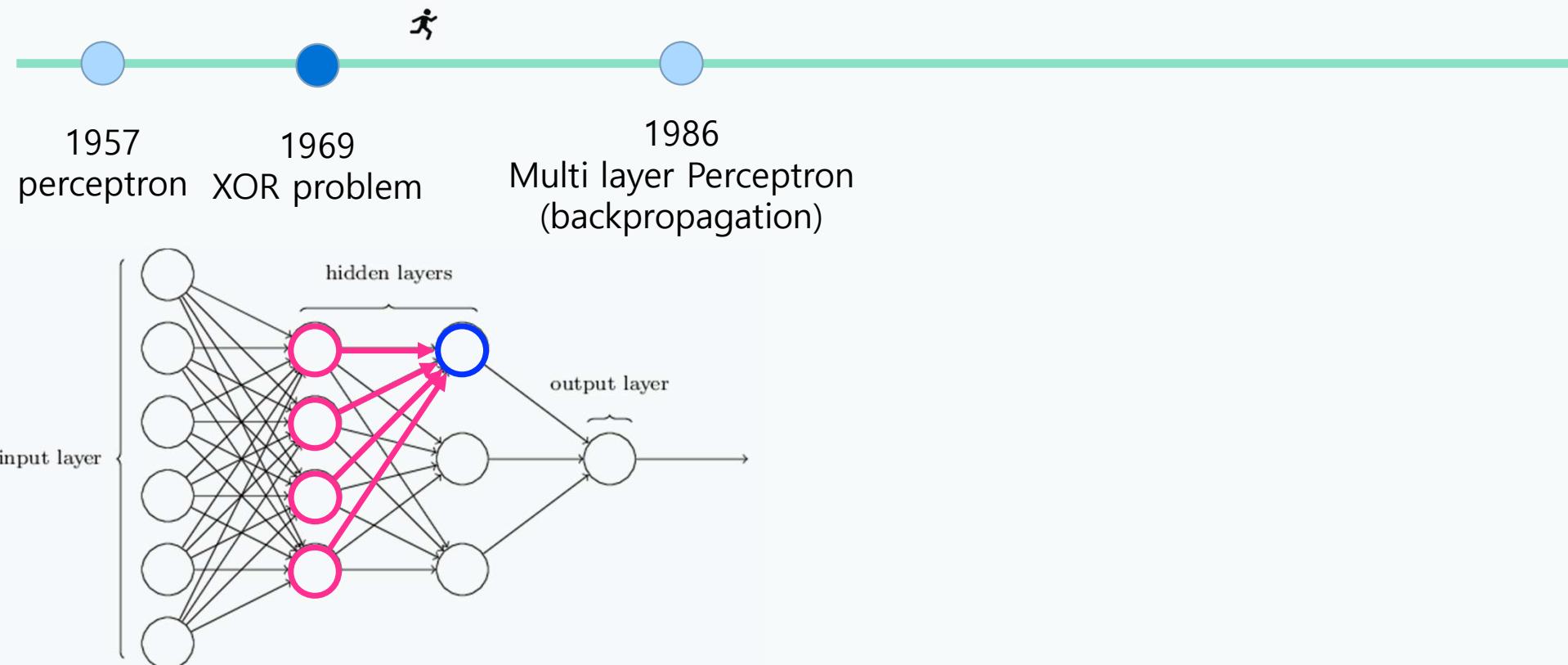
2. Neural Network

- Neural Network or Multi Layer Perceptron



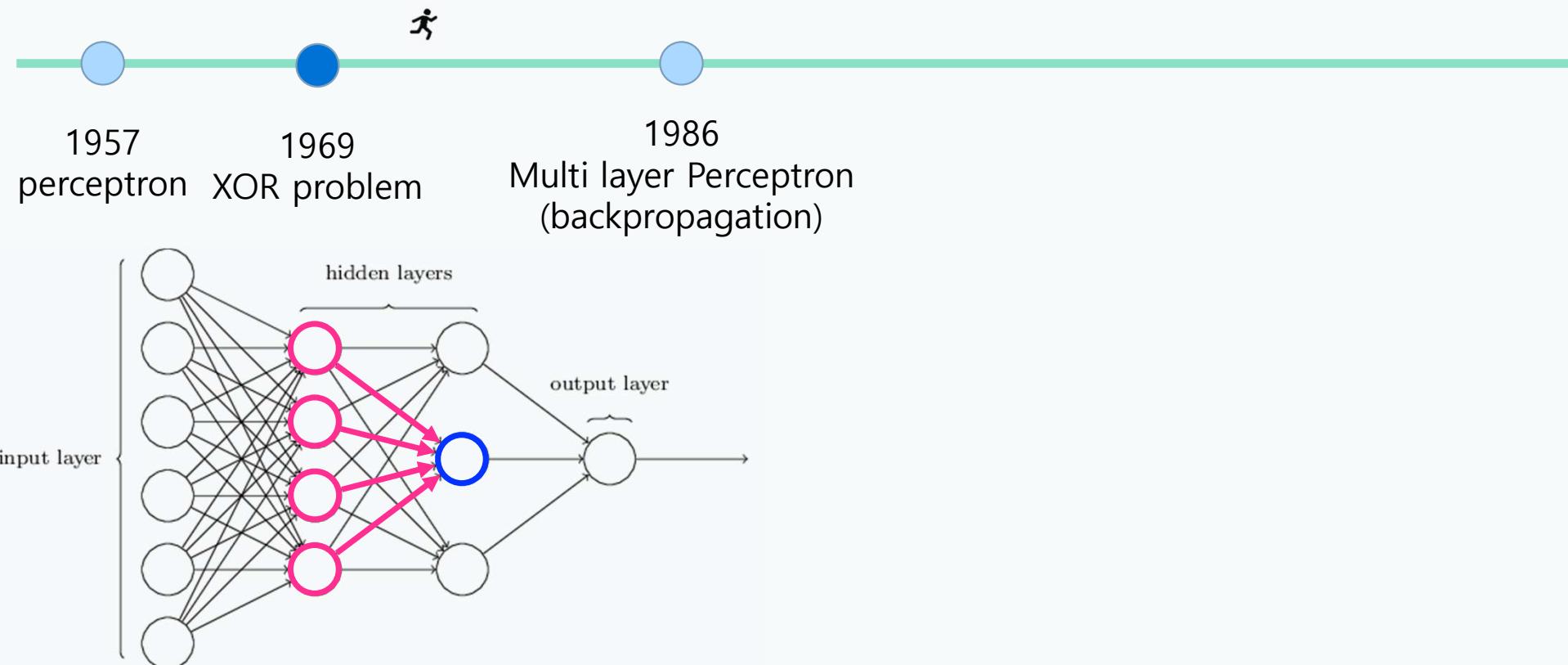
2. Neural Network

- Neural Network or Multi Layer Perceptron



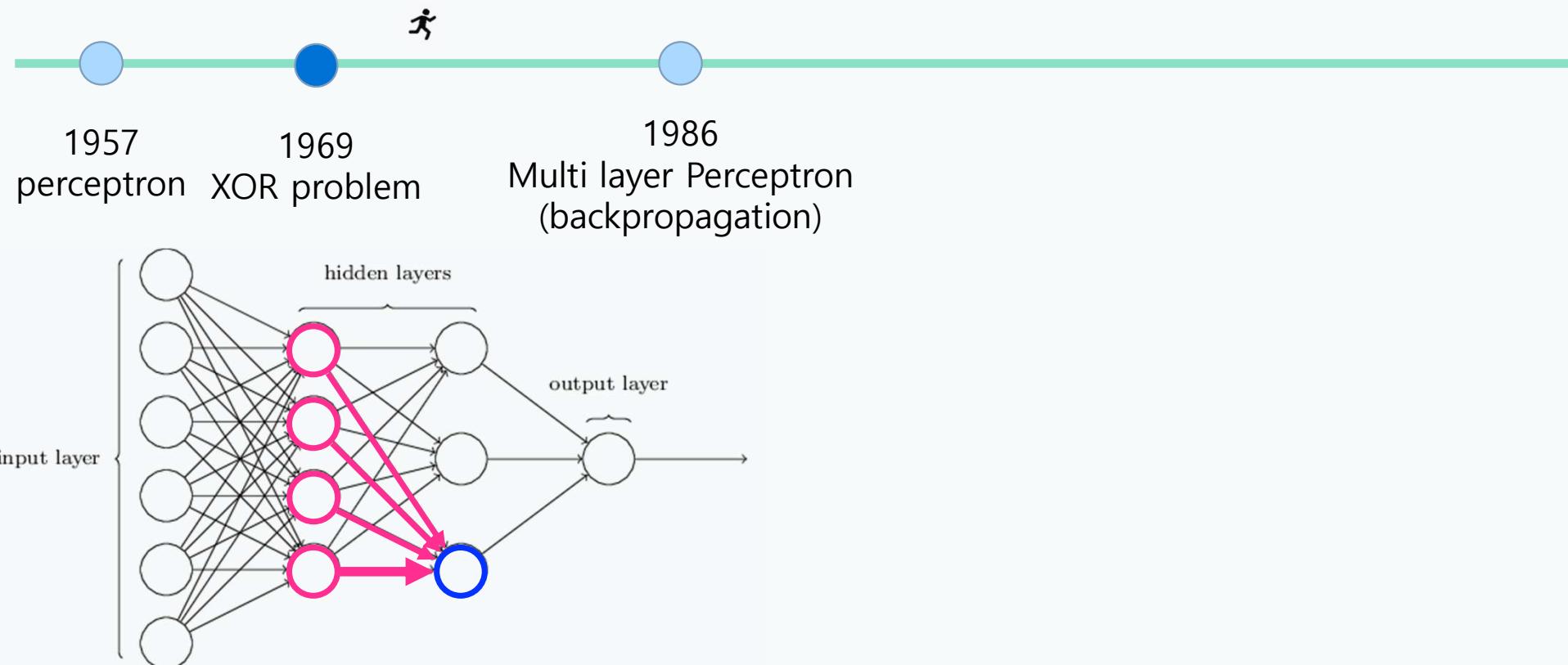
2. Neural Network

- Neural Network or Multi Layer Perceptron



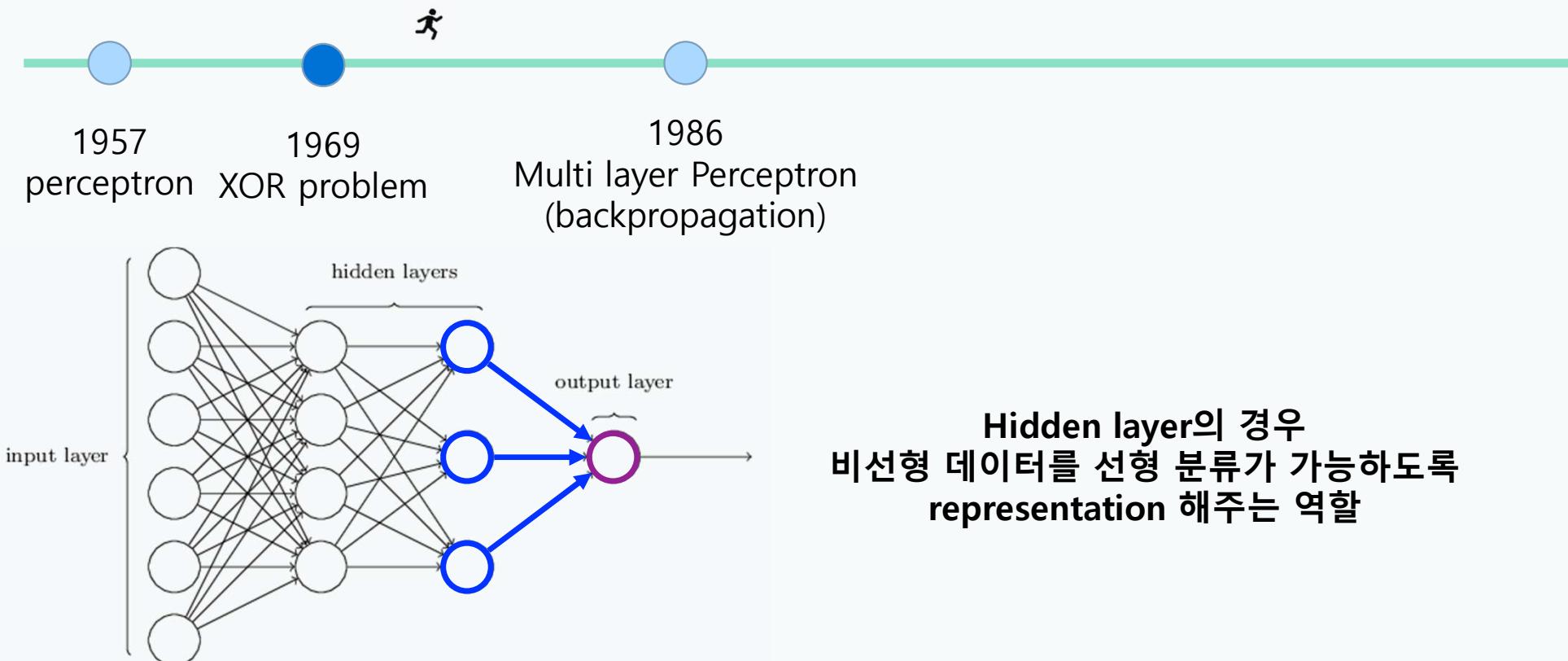
2. Neural Network

- Neural Network or Multi Layer Perceptron



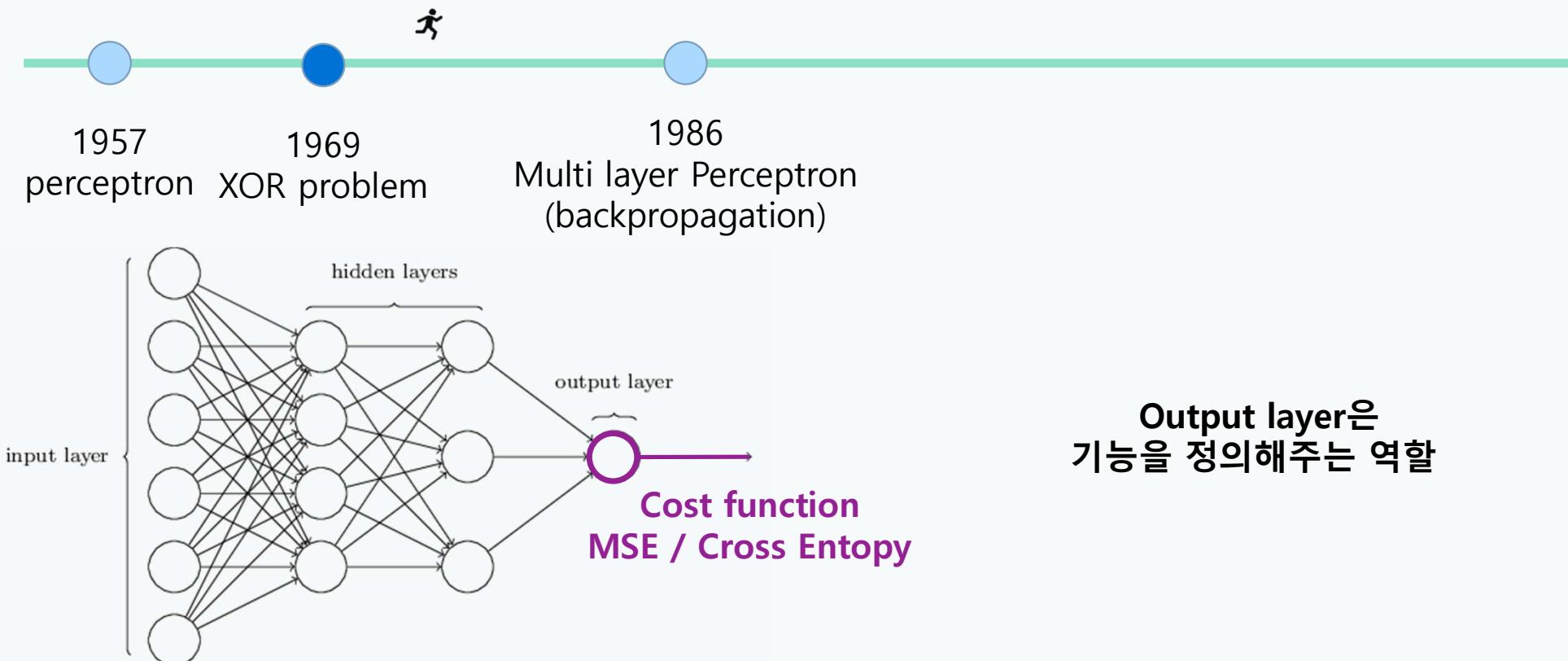
2. Neural Network

- Neural Network or Multi Layer Perceptron



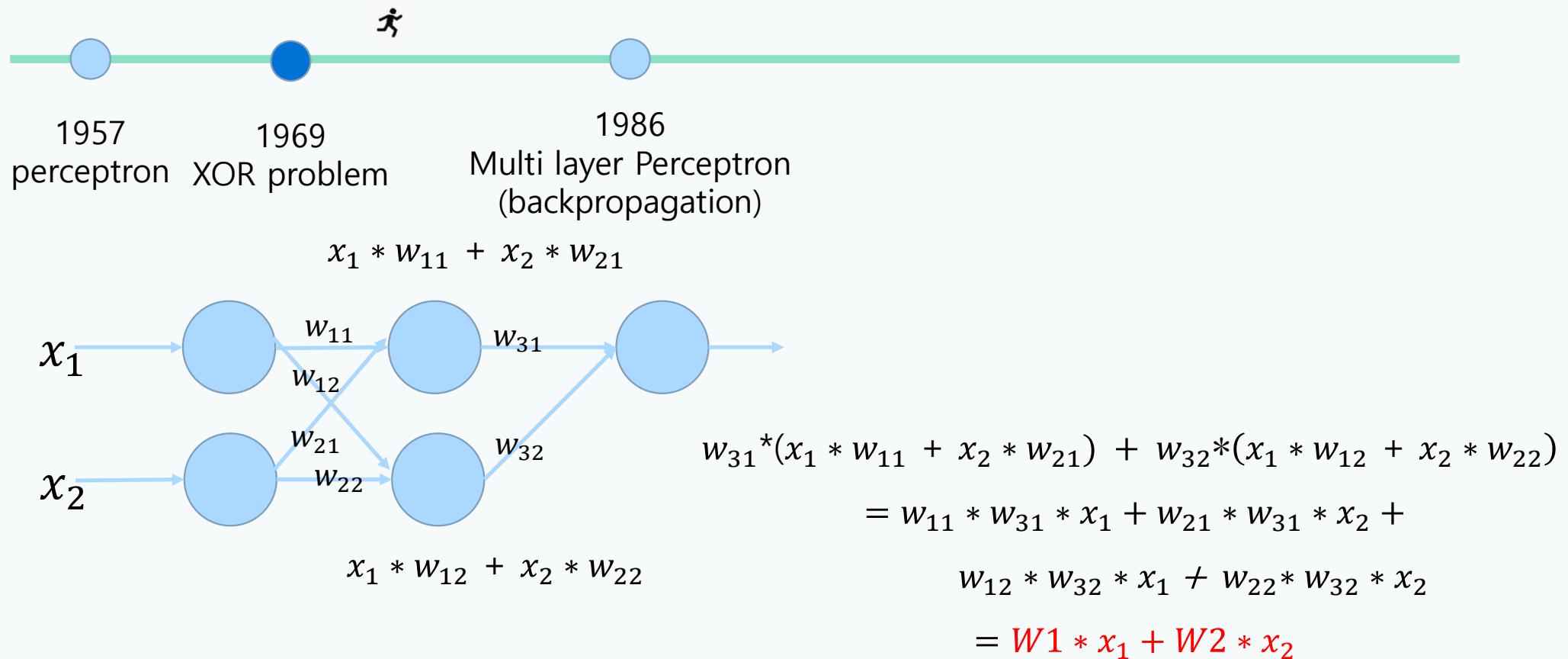
2. Neural Network

- Neural Network or Multi Layer Perceptron



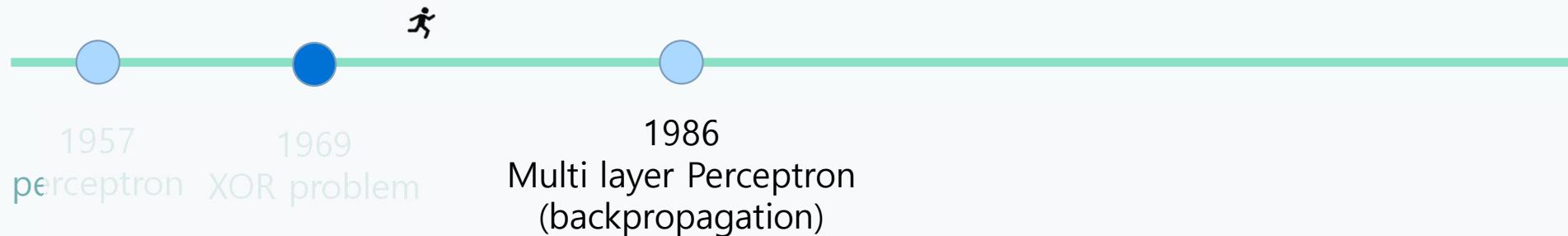
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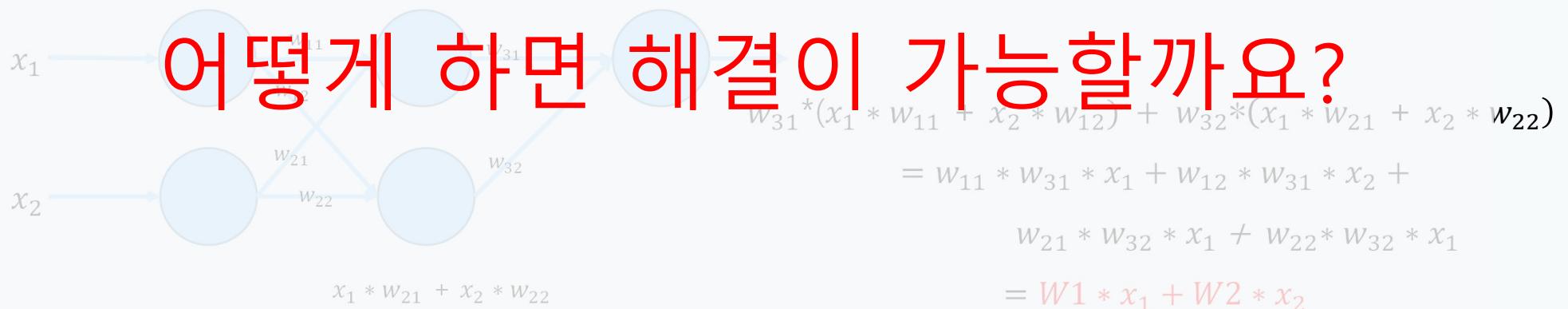
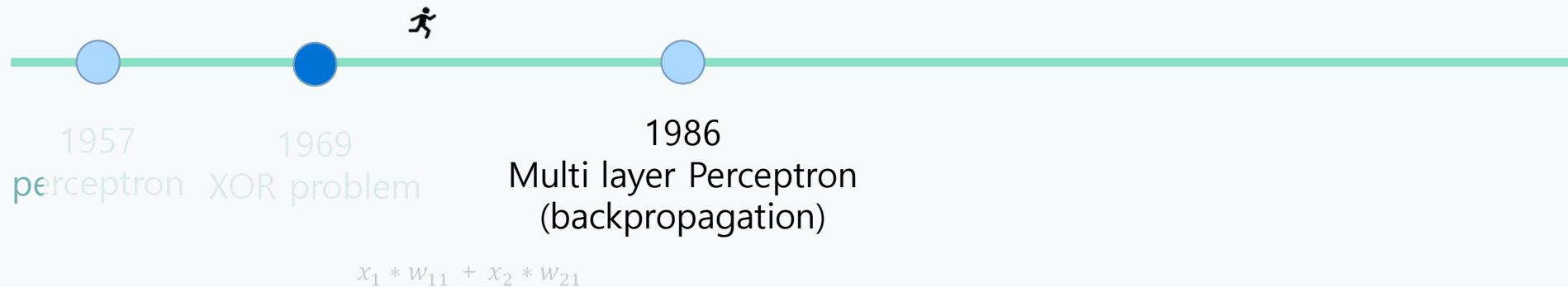
2. Neural Network

- Neural Network or Multi Layer Perceptron



2. Neural Network

- Neural Network or Multi Layer Perceptron

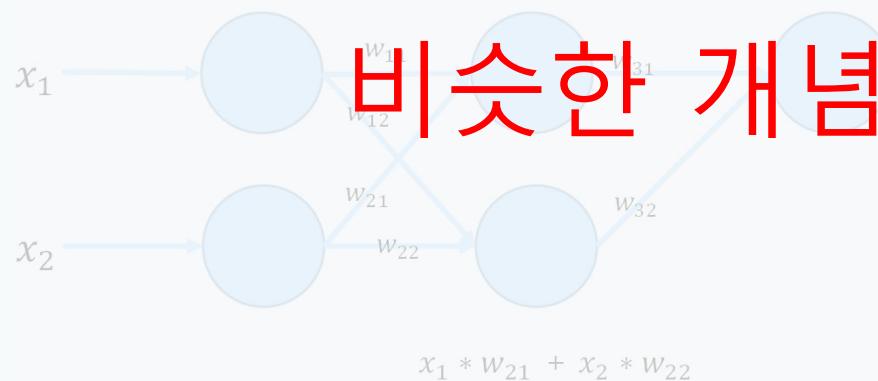


2. Neural Network

- Neural Network or Multi Layer Perceptron



$x_1 * w_{11} + x_2 * w_{21}$

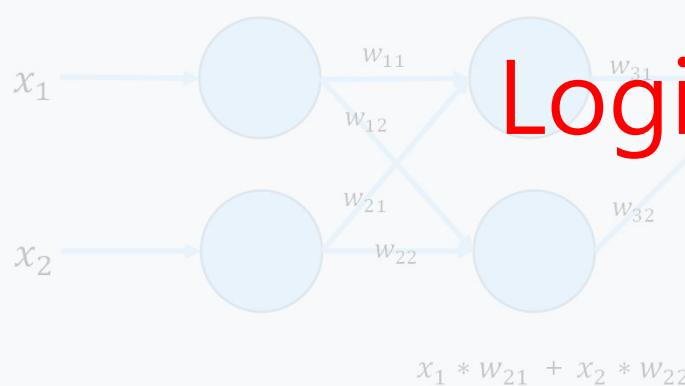
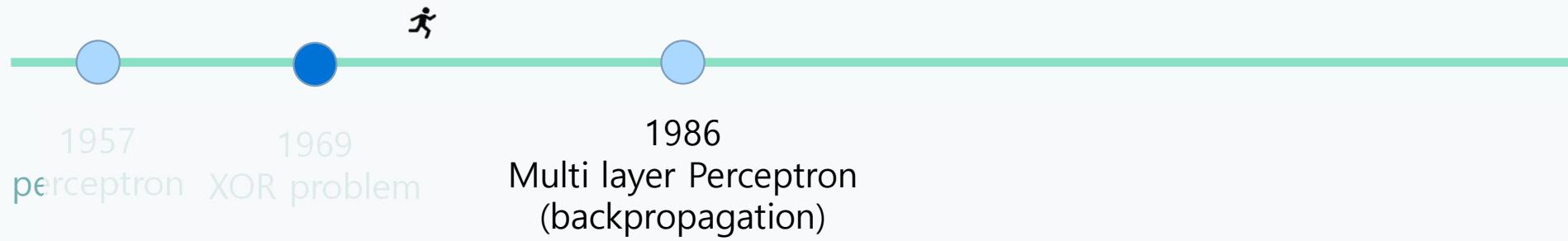


비슷한 개념을 배웠습니다

$$\begin{aligned} & w_{31} * (x_1 * w_{11} + x_2 * w_{12}) + w_{32} * (x_1 * w_{21} + x_2 * w_{22}) \\ &= w_{11} * w_{31} * x_1 + w_{12} * w_{31} * x_2 + \\ & \quad w_{21} * w_{32} * x_1 + w_{22} * w_{32} * x_1 \\ &= W1 * x_1 + W2 * x_2 \end{aligned}$$

2. Neural Network

- Neural Network or Multi Layer Perceptron

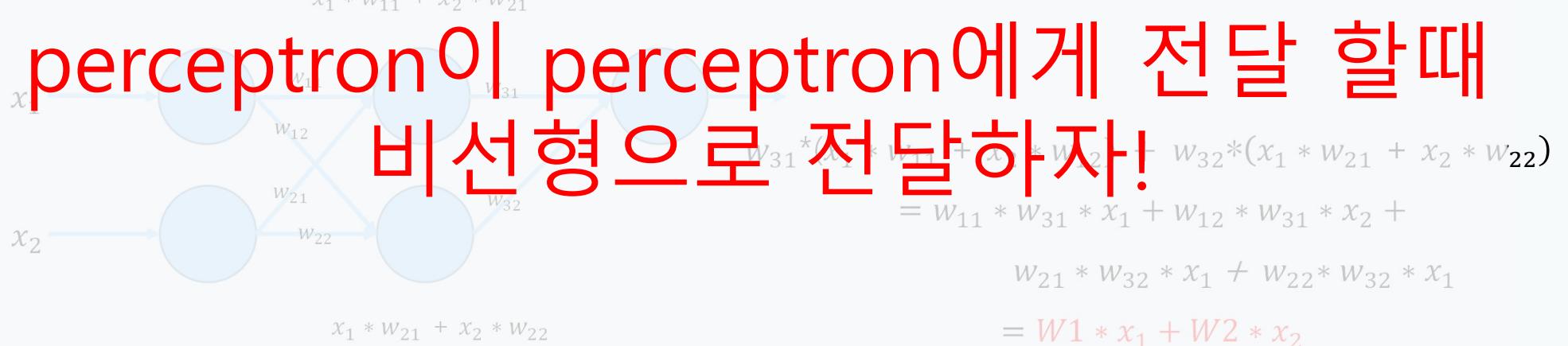


Logistic Regression

$$\begin{aligned} & w_{31} * (x_1 * w_{11} + x_2 * w_{12}) + w_{32} * (x_1 * w_{21} + x_2 * w_{22}) \\ &= w_{11} * w_{31} * x_1 + w_{12} * w_{31} * x_2 + \\ & \quad w_{21} * w_{32} * x_1 + w_{22} * w_{32} * x_1 \\ &= W1 * x_1 + W2 * x_2 \end{aligned}$$

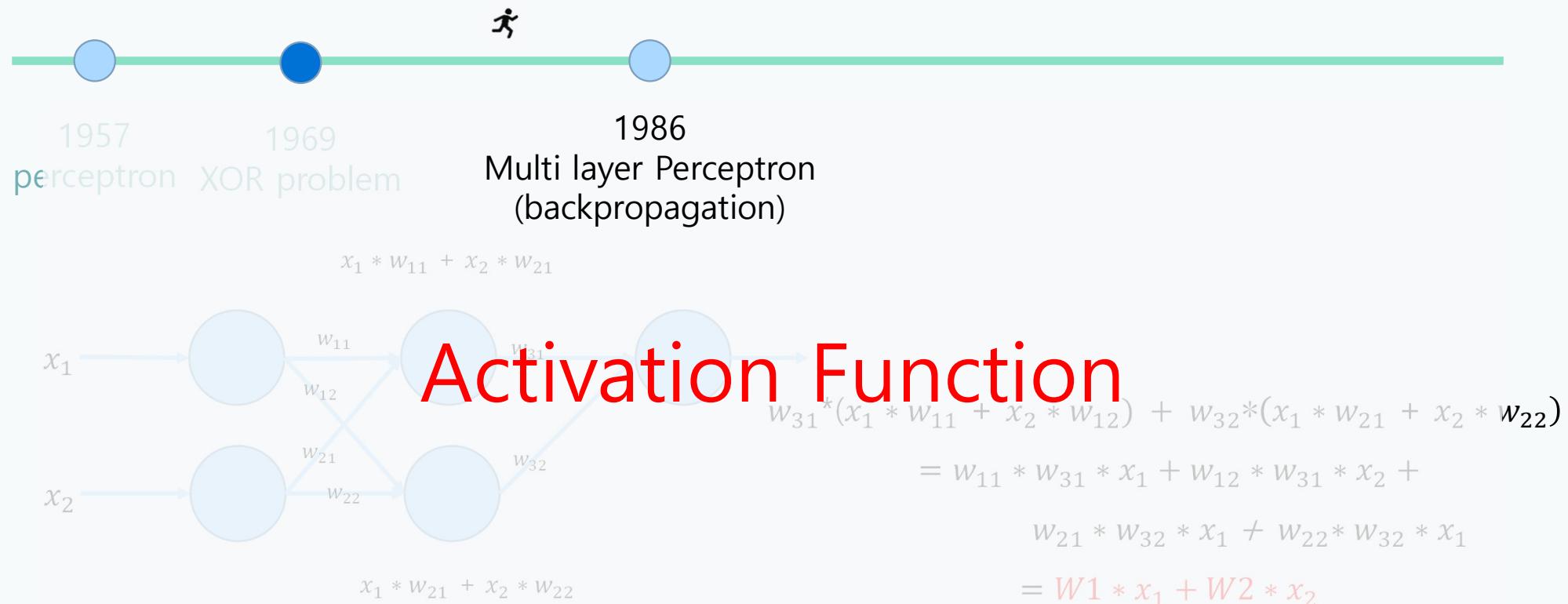
2. Neural Network

- Neural Network or Multi Layer Perceptron



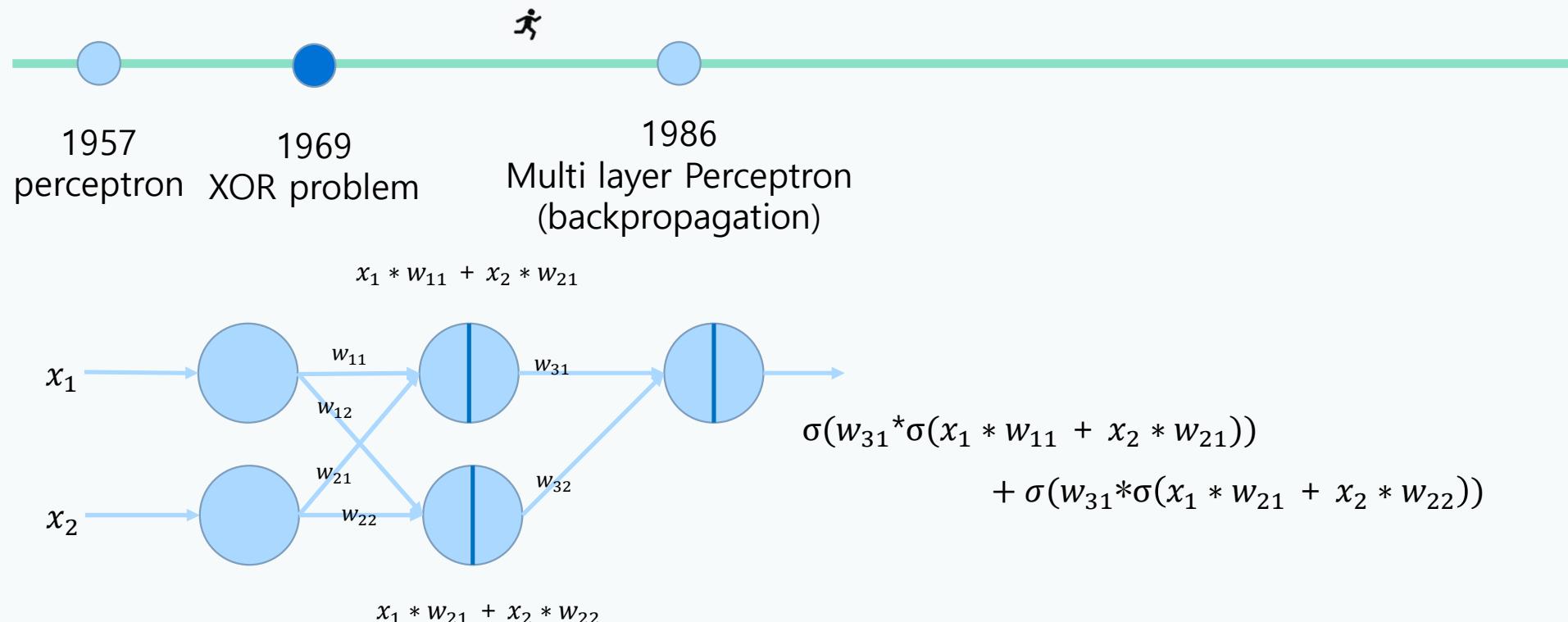
2. Neural Network

- Neural Network or Multi Layer Perceptron



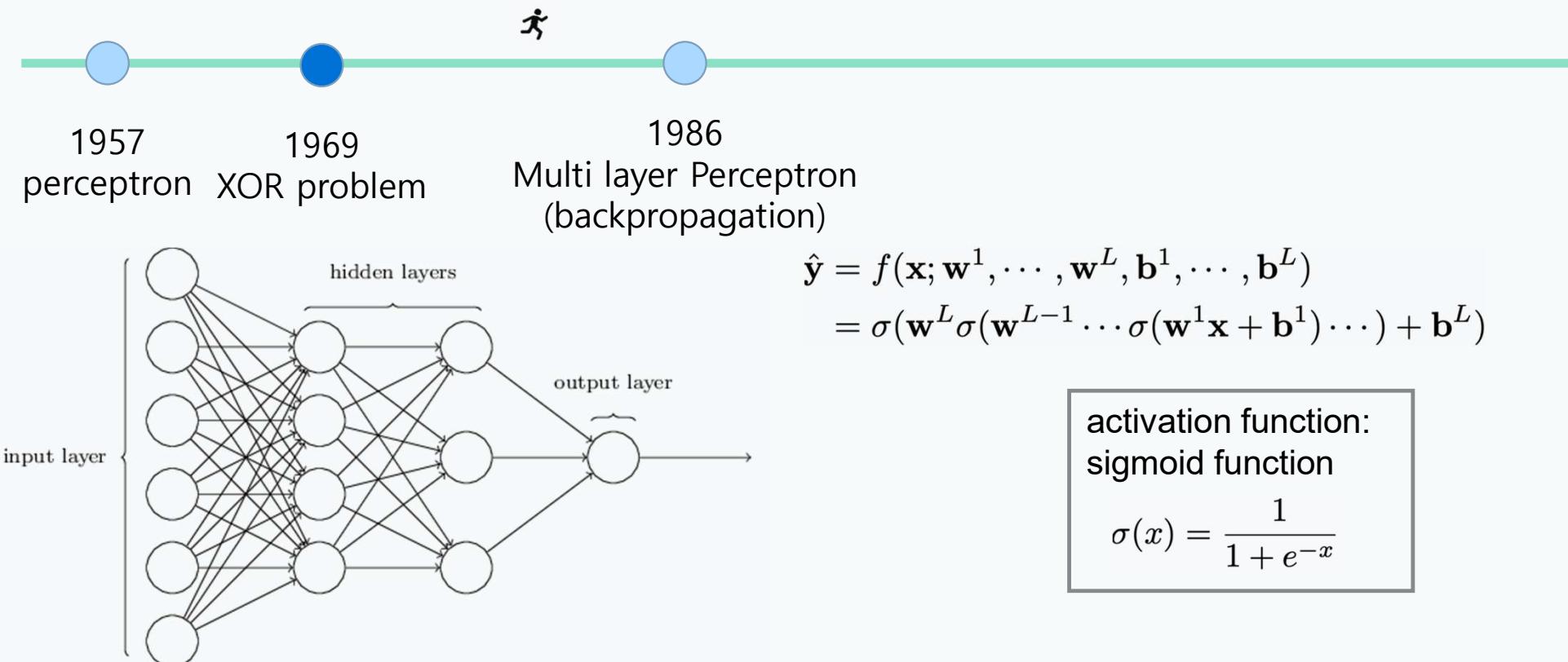
2. Neural Network

- Activation Function



2. Neural Network

- Activation Function

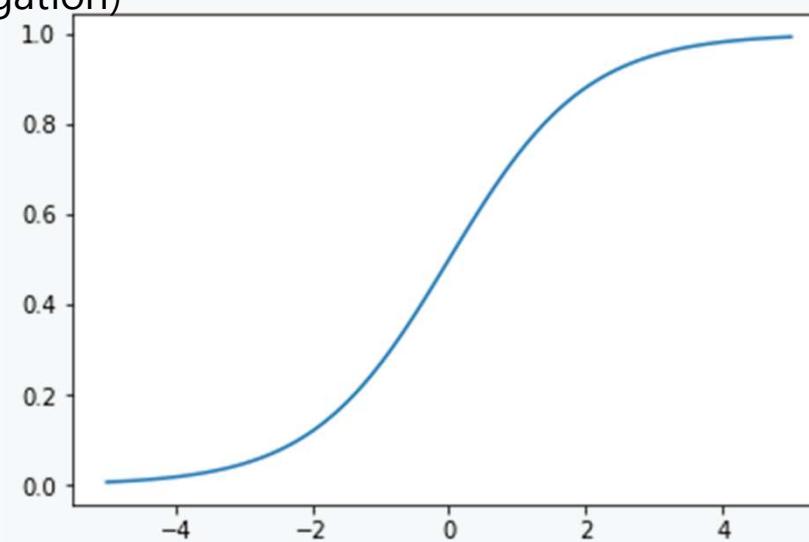


2. Neural Network

- Activation Function

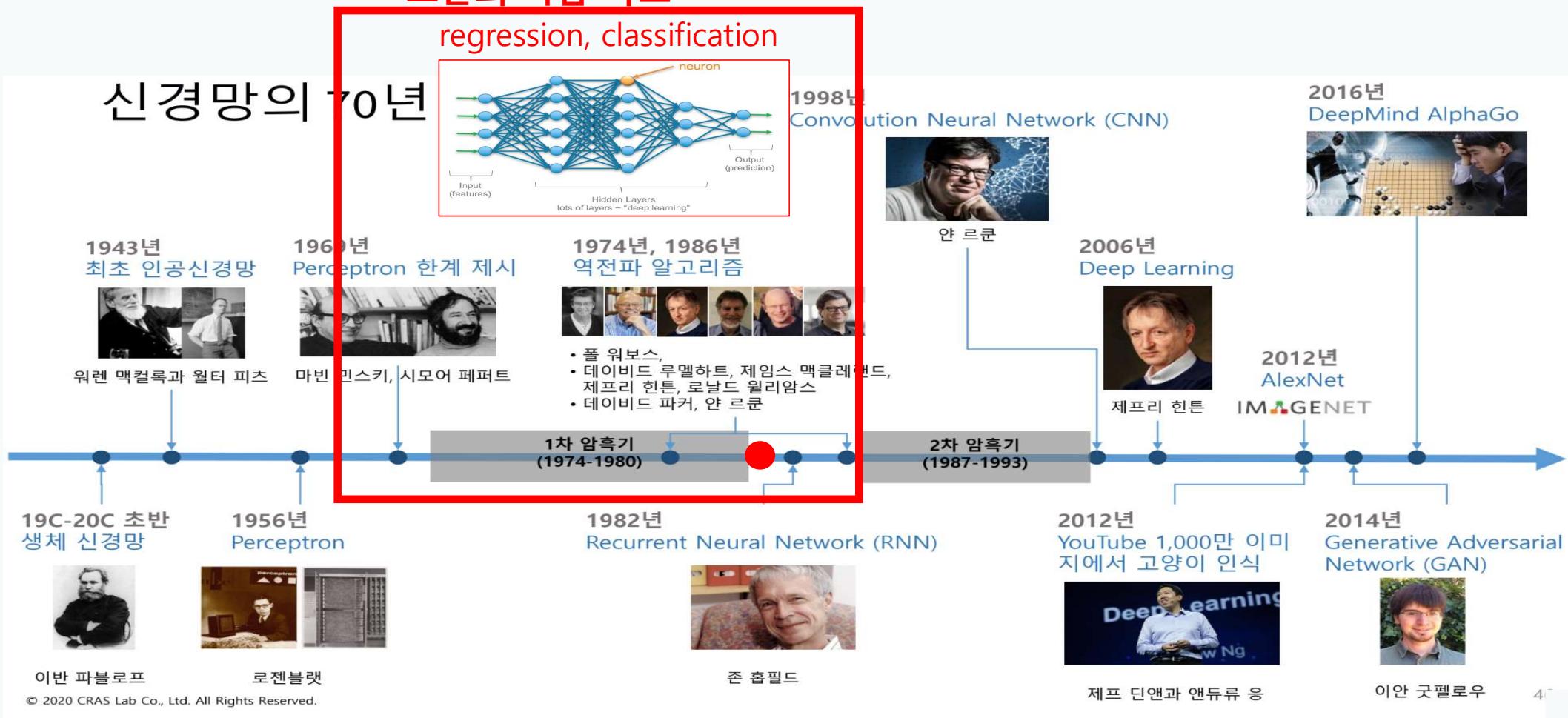


$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}$$



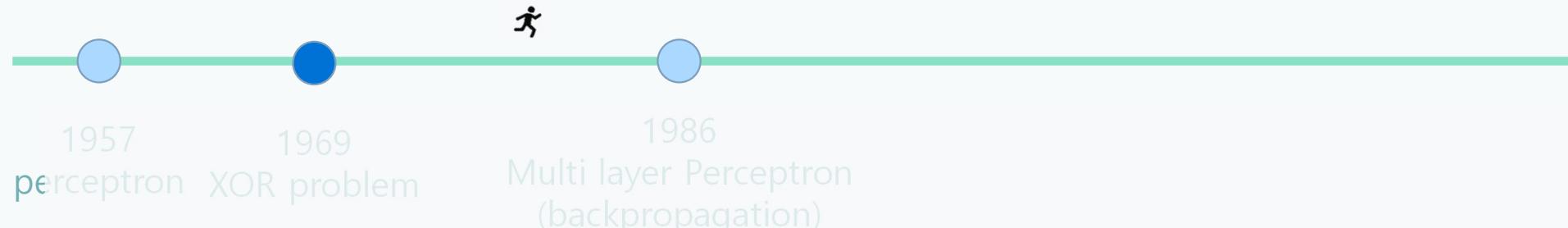
2. Neural Network

오늘의 학습 목표



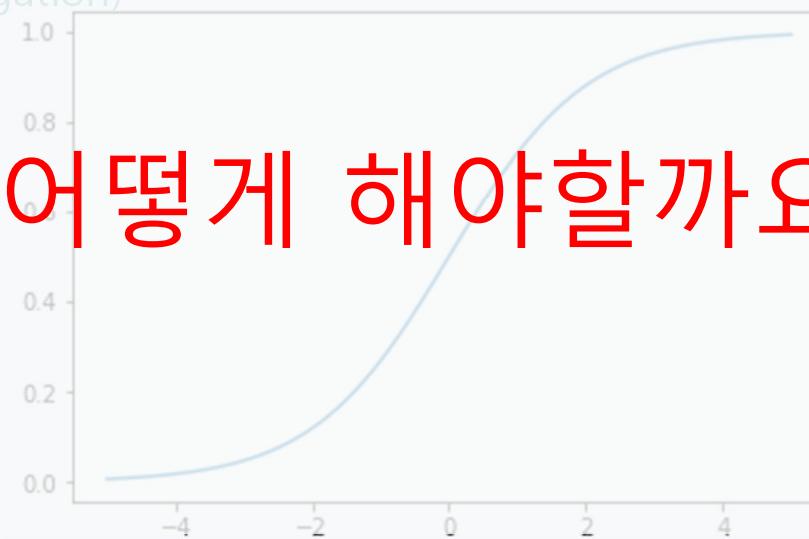
3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



그런데 학습은 어떻게 해야할까요?

$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}$$



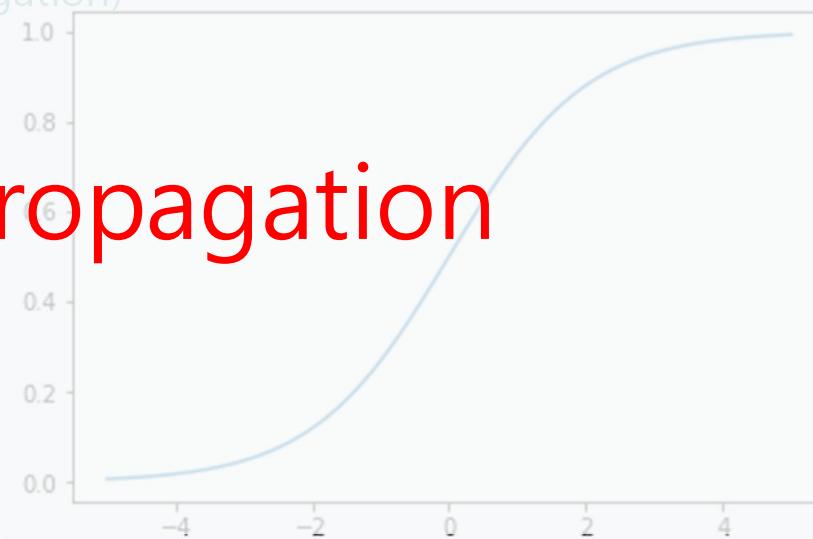
3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



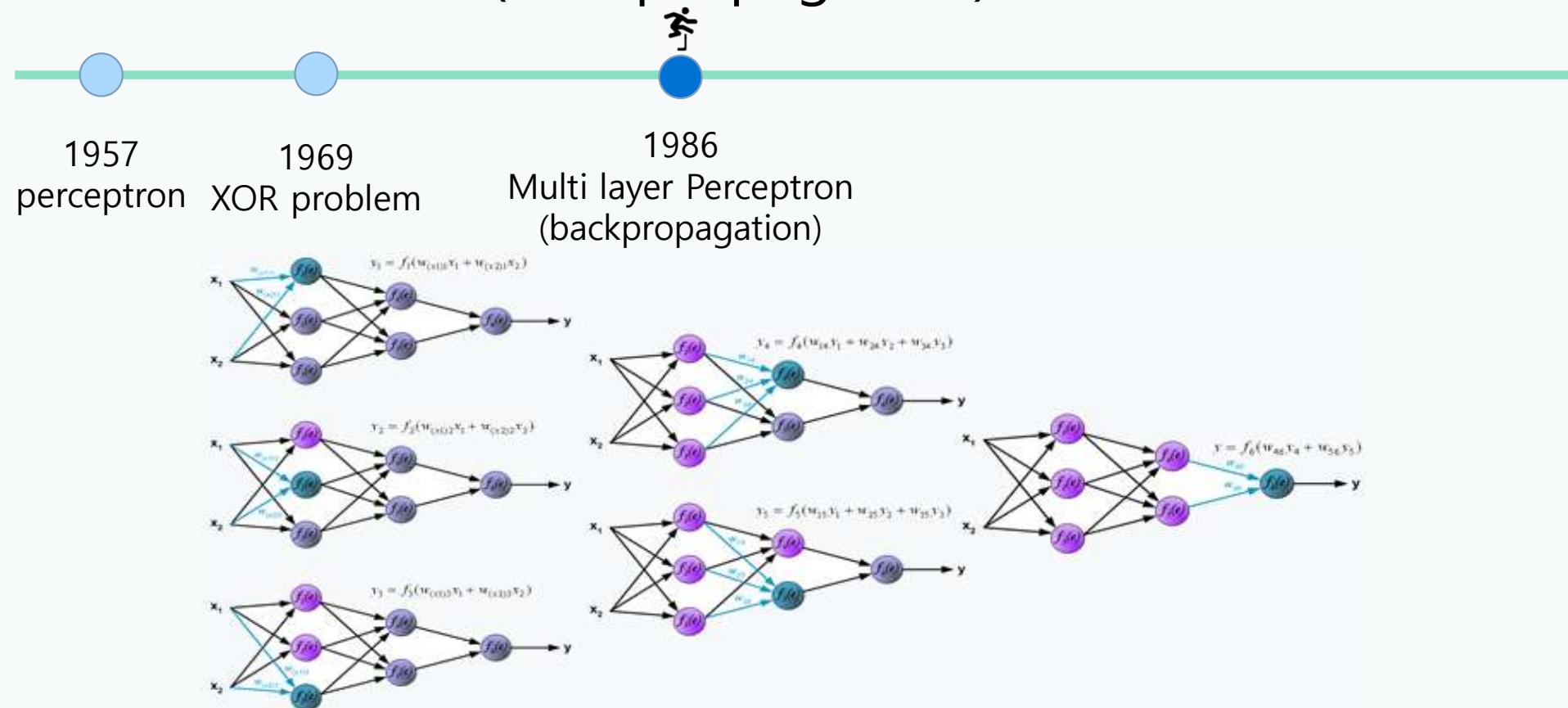
$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}$$

backpropagation



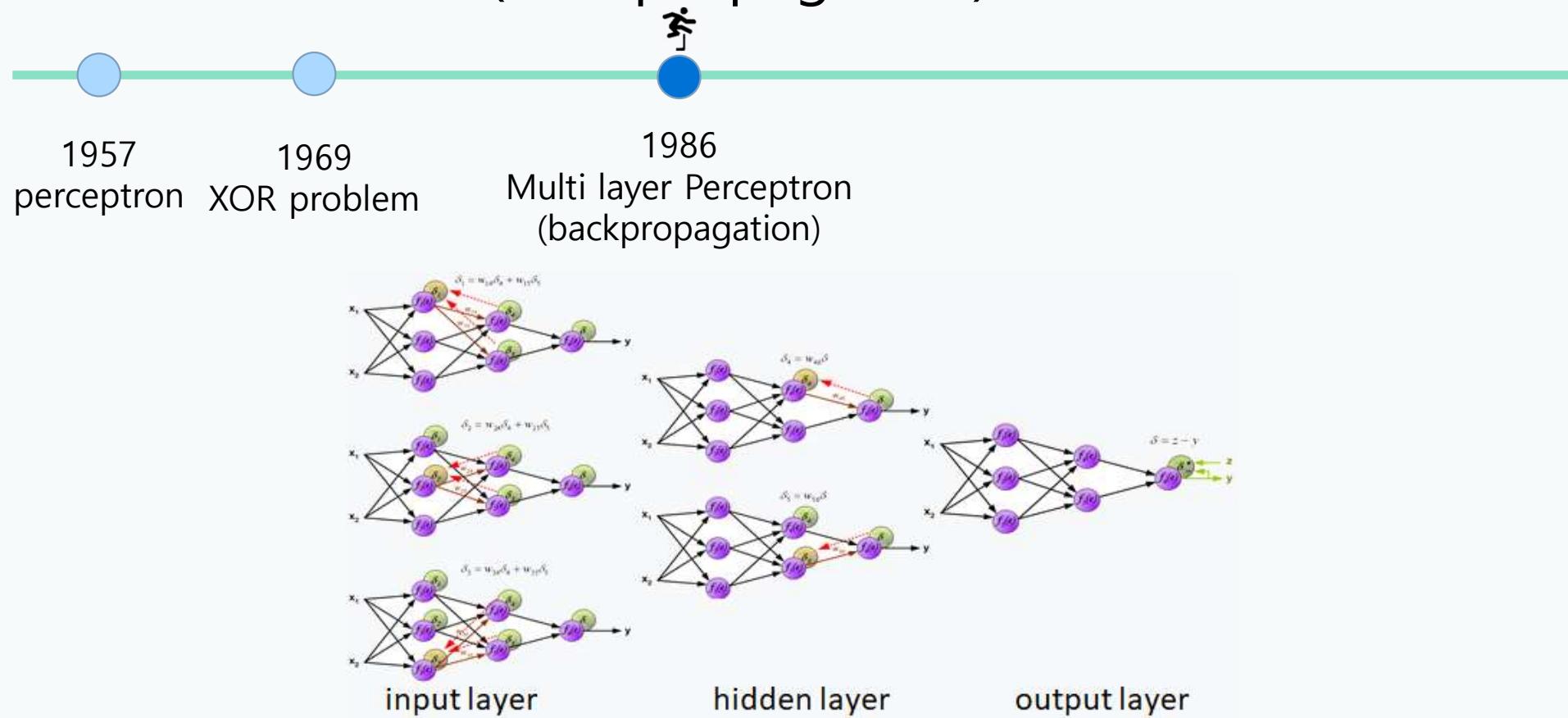
3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



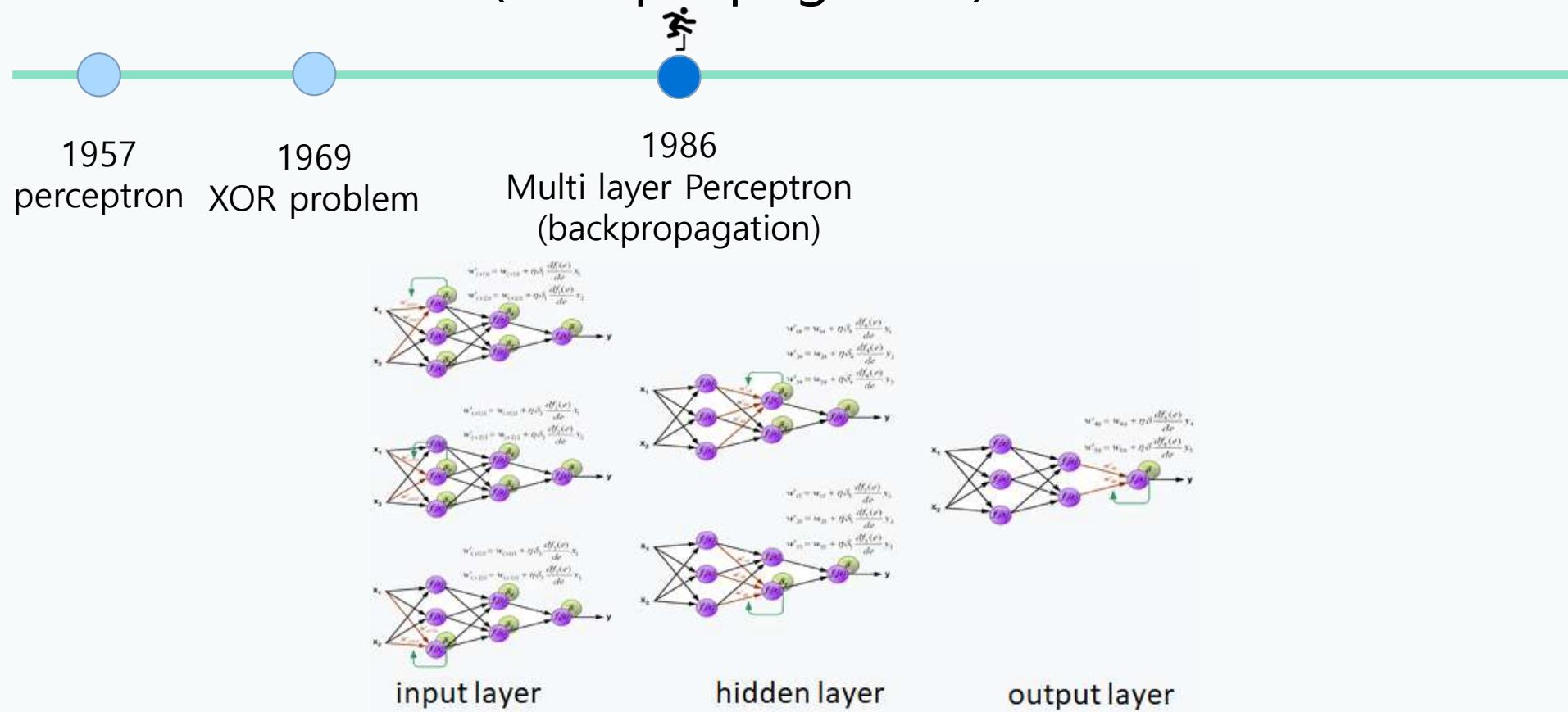
3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



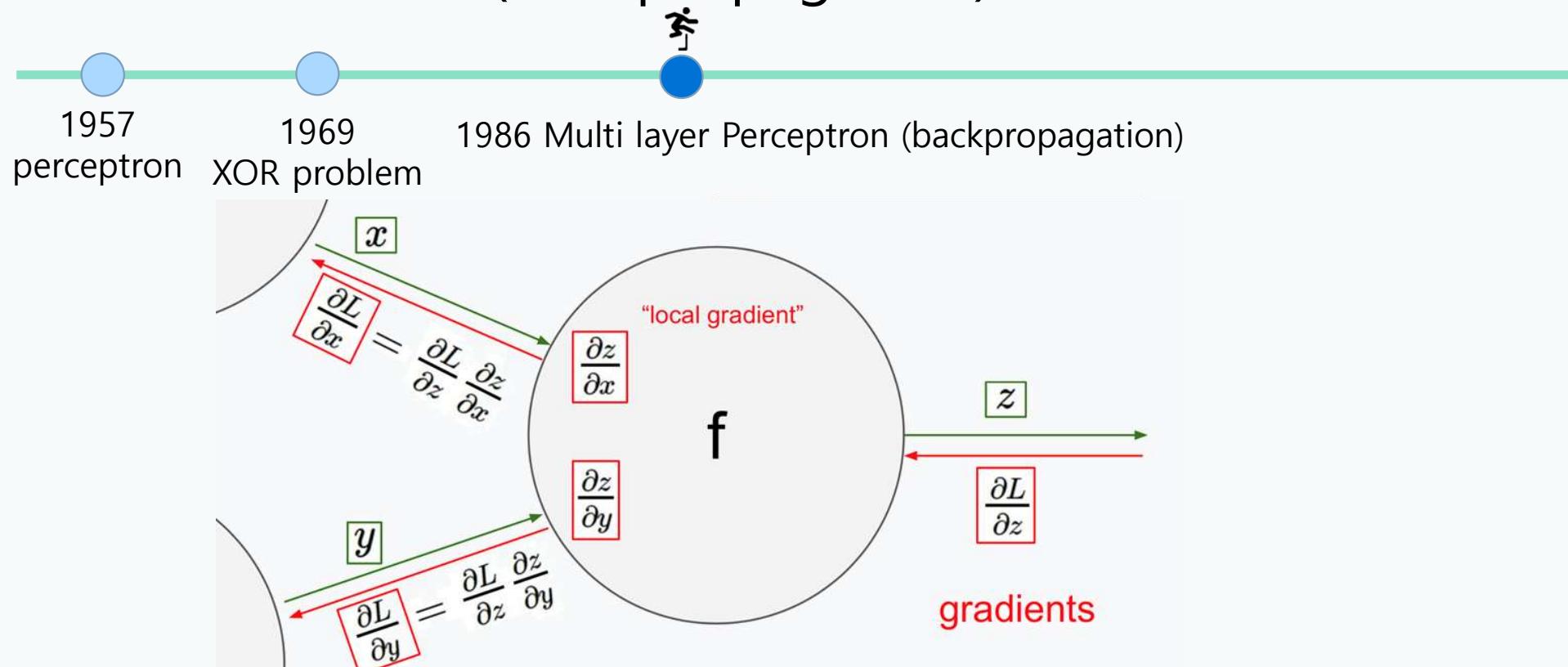
3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



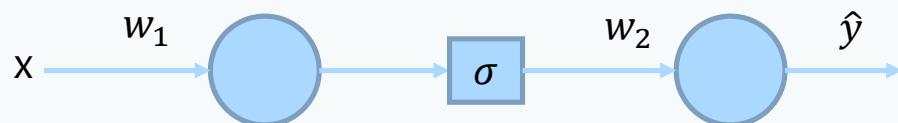
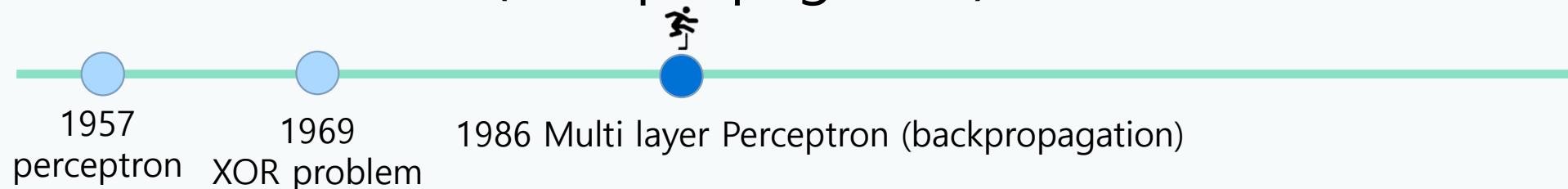
3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$h_1 = xw_1$$

$$h_2 = \sigma(h_1)$$

$$\hat{y} = w_2 h_2$$

$$L = \hat{y} - y$$

$$w_1 = w_1 - \alpha \Delta w_1$$

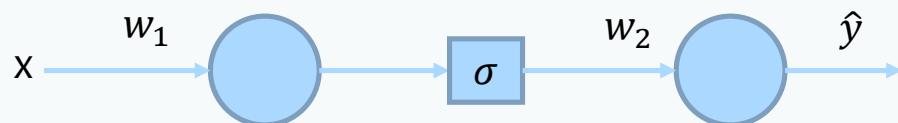
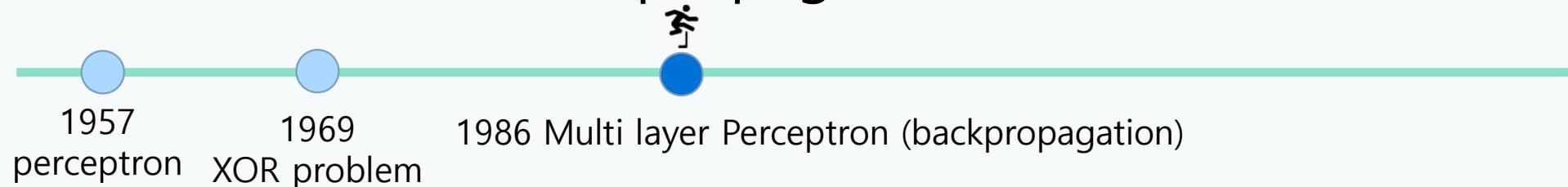
$$w_2 = w_1 - \alpha \Delta w_2$$

$$\Delta w_1 = \frac{\partial L}{\partial w_1}$$

$$\Delta w_2 = \frac{\partial L}{\partial w_2}$$

3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$h_1 = xw_1$$

$$h_2 = \sigma(h_1)$$

$$\hat{y} = w_2 h_2$$

$$L = \hat{y} - y$$

$$w_1 = w_1 - \alpha \Delta w_1$$

$$w_2 = w_1 - \alpha \Delta w_2$$

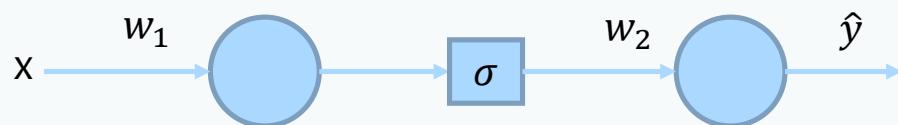
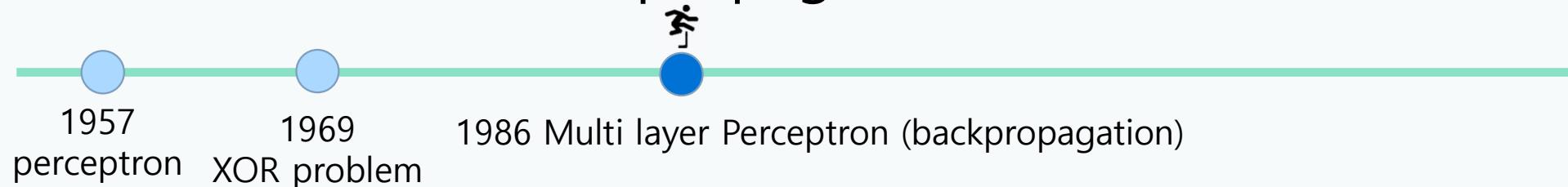
$$\Delta w_1 = \frac{\partial L}{\partial w_1} =$$

$$\Delta w_2 = \frac{\partial L}{\partial w_2} =$$

$$\frac{\partial L}{\partial \hat{y}}$$

3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$h_1 = xw_1$$

$$h_2 = \sigma(h_1)$$

$$\hat{y} = w_2 h_2$$

$$L = \hat{y} - y$$

$$w_1 = w_1 - \alpha \Delta w_1$$

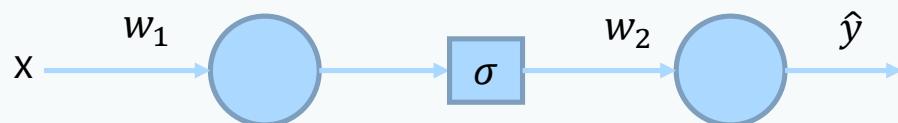
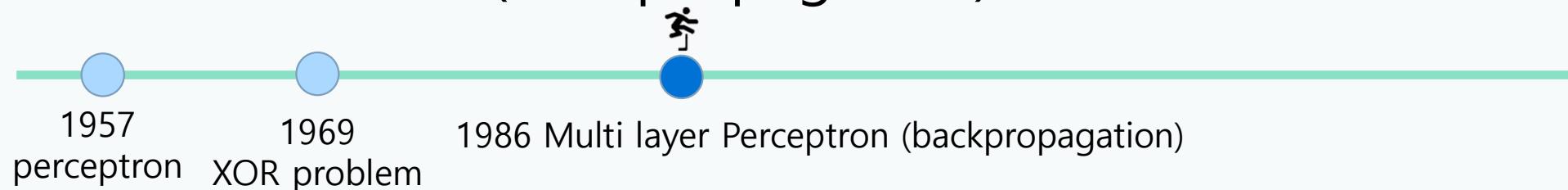
$$w_2 = w_1 - \alpha \Delta w_2$$

$$\Delta w_1 = \frac{\partial L}{\partial w_1} = \frac{\partial \hat{y}}{\partial h_2} \frac{\partial L}{\partial \hat{y}}$$

$$\Delta w_2 = \frac{\partial L}{\partial w_2} =$$

3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$h_1 = xw_1$$

$$h_2 = \sigma(h_1)$$

$$\hat{y} = w_2 h_2$$

$$L = \hat{y} - y$$

$$w_1 = w_1 - \alpha \Delta w_1$$

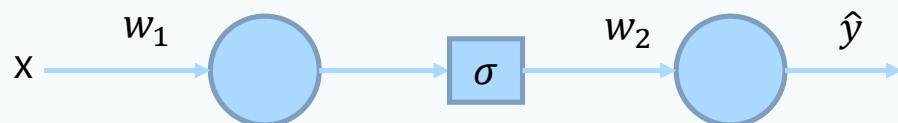
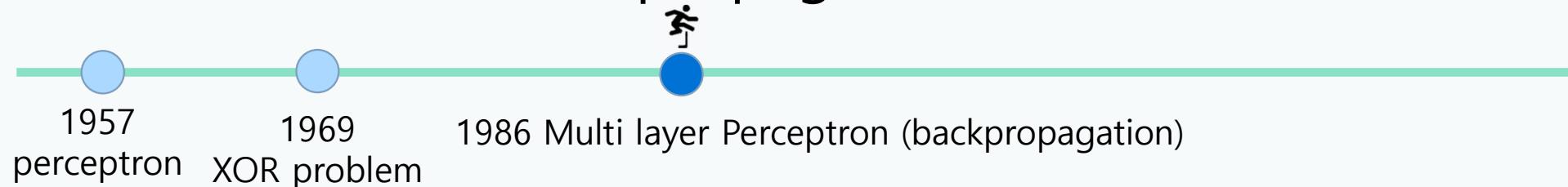
$$w_2 = w_1 - \alpha \Delta w_2$$

$$\Delta w_1 = \frac{\partial L}{\partial w_1} = \frac{\partial h_2}{\partial h_1} \frac{\partial \hat{y}}{\partial h_2} \frac{\partial L}{\partial \hat{y}}$$

$$\Delta w_2 = \frac{\partial L}{\partial w_2} =$$

3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$h_1 = xw_1$$

$$h_2 = \sigma(h_1)$$

$$\hat{y} = w_2 h_2$$

$$L = \hat{y} - y$$

$$w_1 = w_1 - \alpha \Delta w_1$$

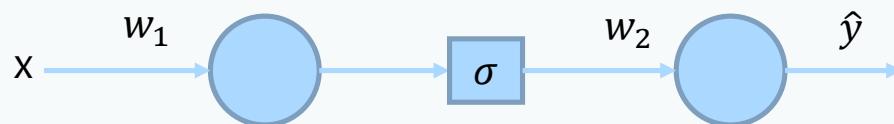
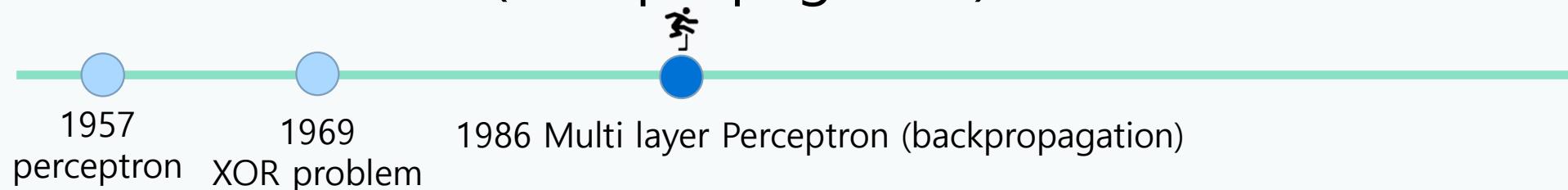
$$w_2 = w_1 - \alpha \Delta w_2$$

$$\Delta w_1 = \frac{\partial L}{\partial w_1} = \frac{\partial h_1}{\partial w_1} \frac{\partial h_2}{\partial h_1} \frac{\partial \hat{y}}{\partial h_2} \frac{\partial L}{\partial \hat{y}}$$

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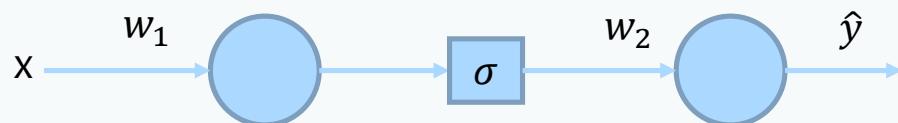
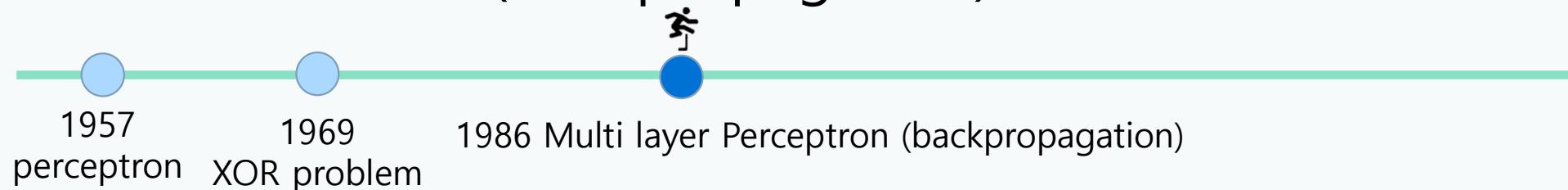
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$$\Delta w_2 = \frac{\partial L}{\partial w_2} =$$

Chain Rule

3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$h_1 = xw_1$$

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$$L = \hat{y} - y$$

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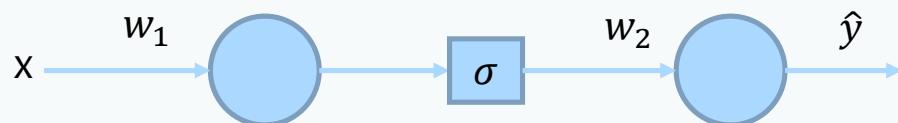
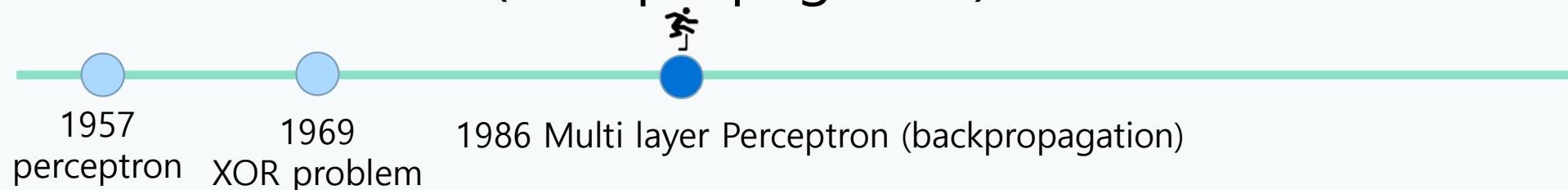
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$$\Delta w_2 = \frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial \hat{y}}$$

3. BACKPROPAGATION

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$$h_1 = xw_1$$

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$$L = \hat{y} - y$$

$$w_1 = w_1 - \alpha \Delta w_1$$

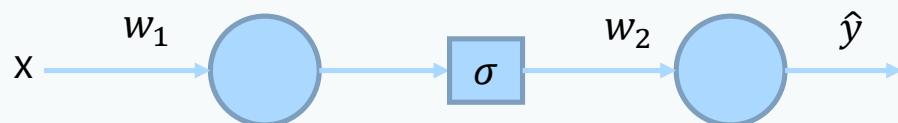
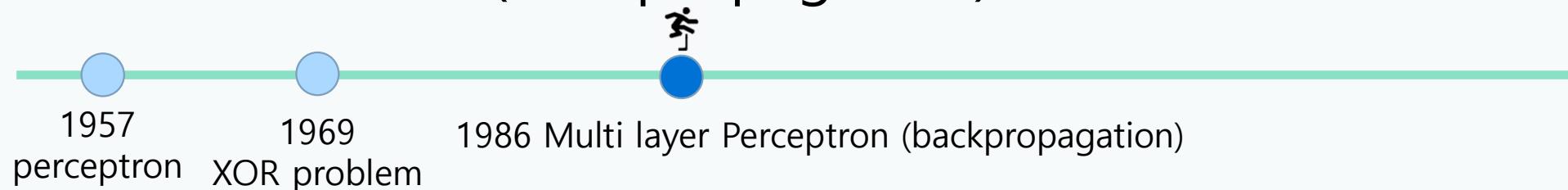
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3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$h_1 = xw_1$$

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$$w_1 = w_1 - \alpha \Delta w_1$$

$$w_2 = w_2 - \alpha \Delta w_2$$

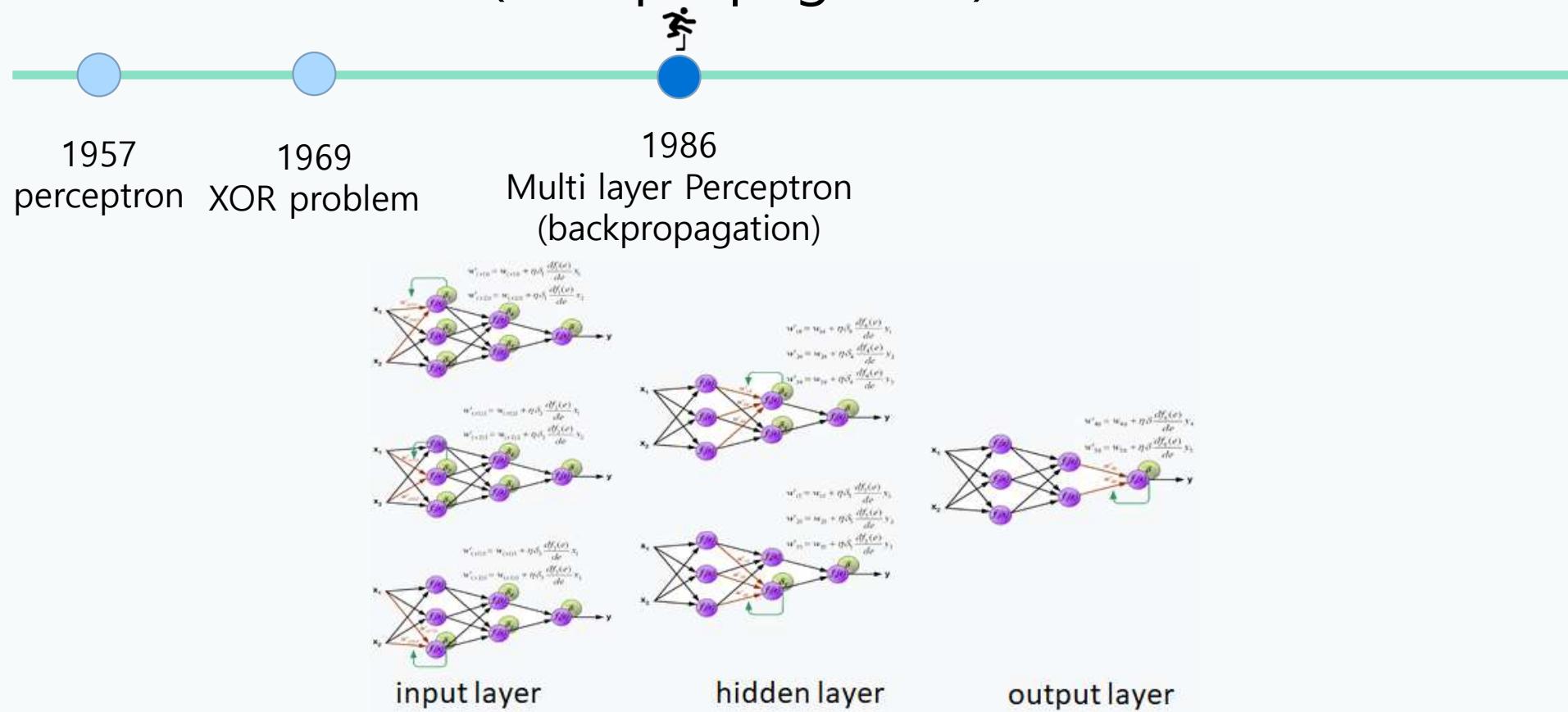
$$\Delta w_1 = \frac{\partial L}{\partial w_1} = \frac{\partial h_1}{\partial w_1} \frac{\partial h_2}{\partial h_1} \frac{\partial \hat{y}}{\partial h_2} \frac{\partial L}{\partial \hat{y}}$$

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Chain Rule

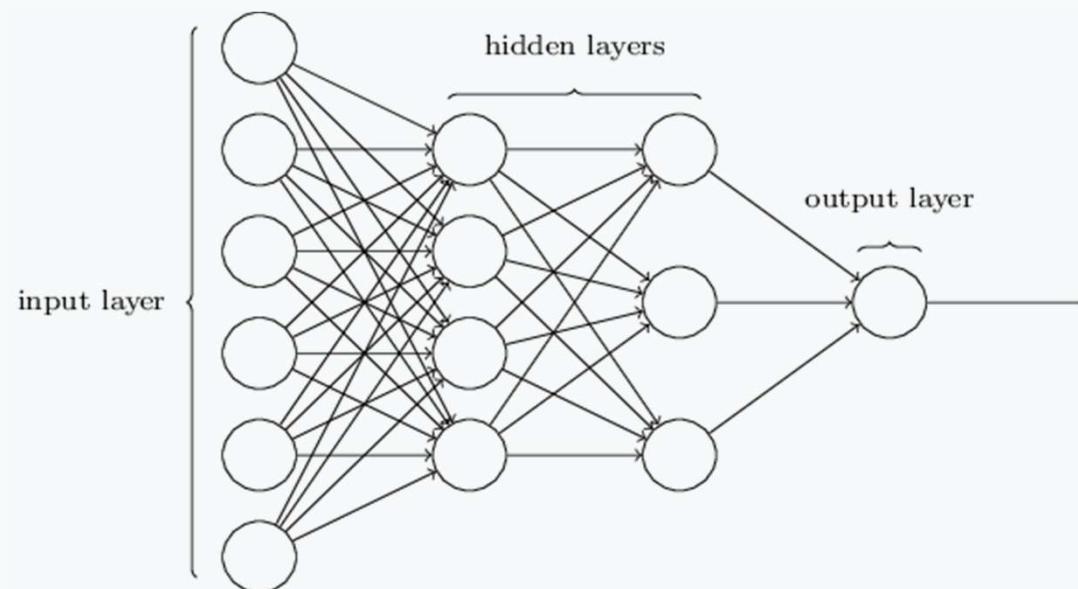
3. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



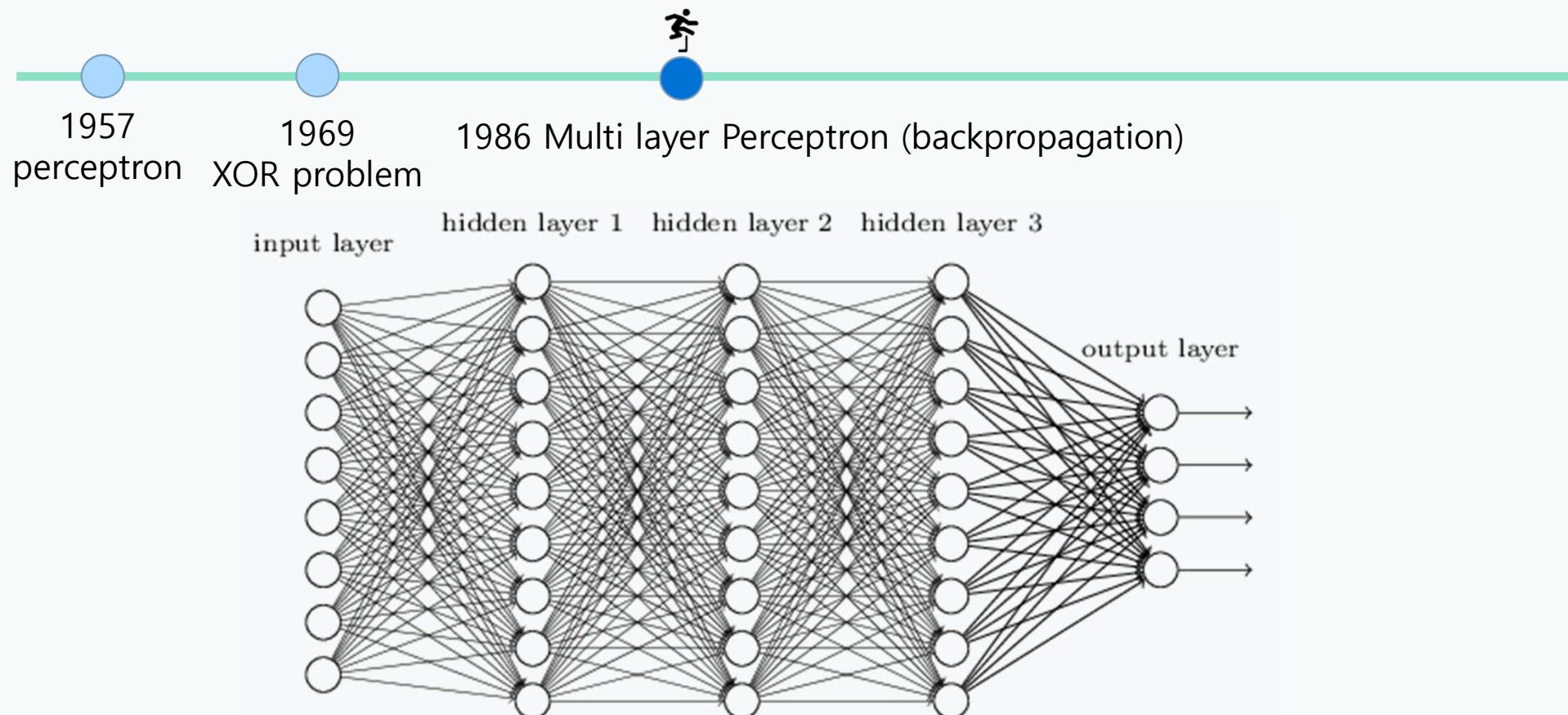
4. Neural Network 실습

- Neural Network 구조



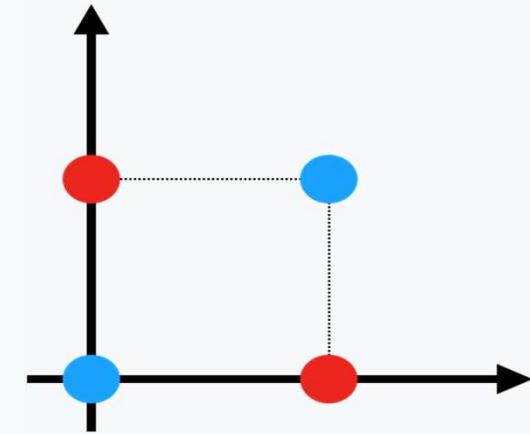
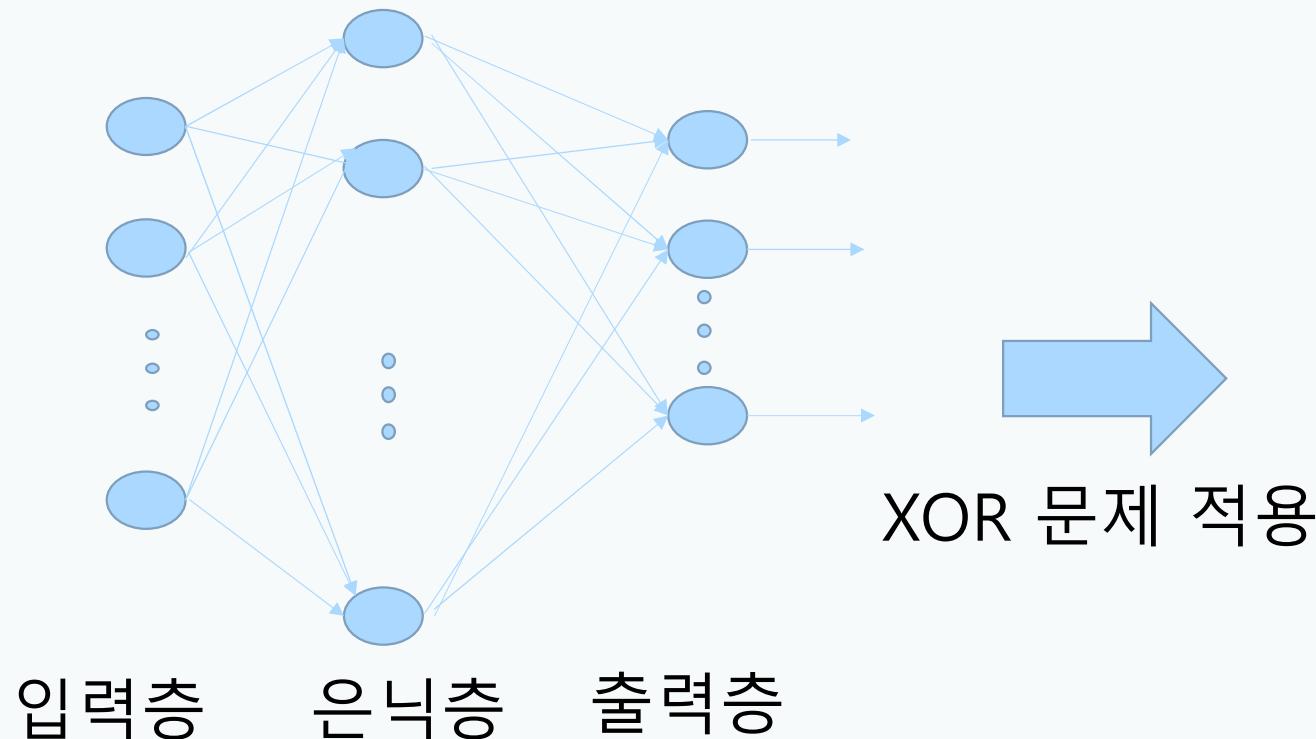
4. Neural Network 실습

- Neural Network 구조



4. Neural Network 실습

- XOR Problem 해결해보기



$$w_1 = ?, w_2 = ?, b = ?$$

x_1	x_2	Σ	y
0	0		0
0	1		1
1	0		1
1	1		0

exercise_02_01_XOR_problem_solution.ipynb
practice : P_02_01_XOR_problem_solution.ipynb

4. Neural Network 실습

Neural Network 구현하기

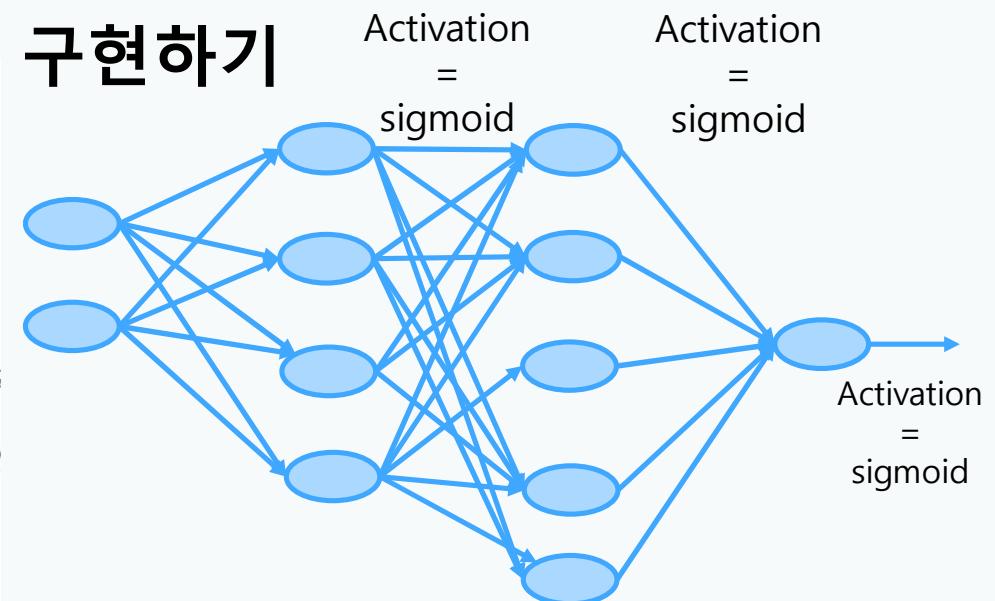
```
## data 선언
x_data = [[0.,0.], [0.,1.], [1.,0.],[1.,1.]]
y_data = [[0.], [1.], [1.], [0.]]
test_data=[[0.5, 0.5]]

## tf.keras를 활용한 perceptron 모델 구현.
model = tf.keras.Sequential() ## 모델 선언
model.add(tf.keras.layers.Dense(4, input_dim=2, activation='sigmoid')) # 선언된 노드
model.add(tf.keras.layers.Dense(5, activation='sigmoid'))
model.add(tf.keras.layers.Dense(1, activation='sigmoid')) # 선언된 모델에 add를 통해
model.summary()

# 모델 loss, 학습 방법 결정하기
optimizer=tf.keras.optimizers.SGD(learning_rate=0.5) ### 경사 하강법으로 global mi
loss=tf.keras.losses.binary_crossentropy ## 예측값과 정답의 오차값 정의.
metrics=tf.keras.metrics.binary_accuracy ### 학습하면서 평가할 메트릭스 선언

# 모델 컴파일하기
model.compile(loss=loss, optimizer=optimizer, metrics=[metrics])

# 모델 동작하기
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

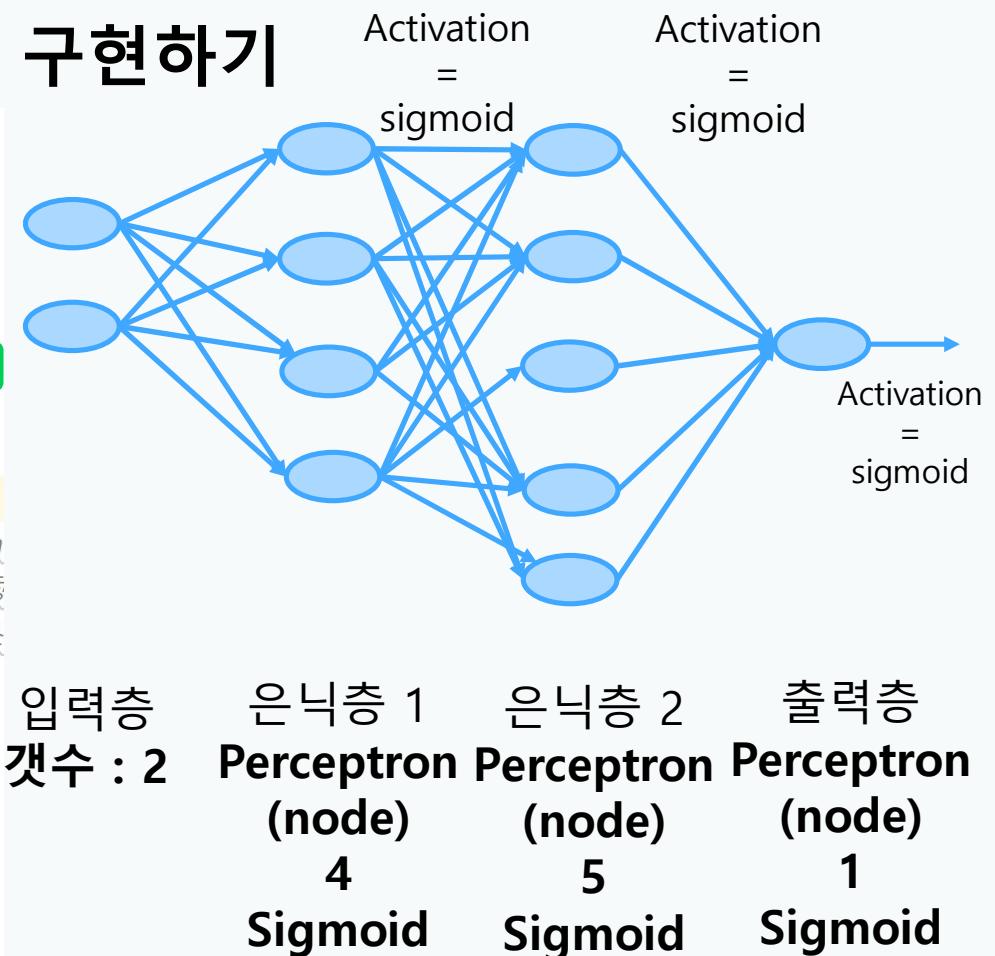


입력층 갯수 : 2	은닉층 1 Perceptron (node)	은닉층 2 Perceptron (node)	출력층 Perceptron (node)
	4	5	1
	Sigmoid	Sigmoid	Sigmoid

4. Neural Network 실습

Neural Network 구현하기

```
## tf.keras를 활용한 perceptron 모델 구현.  
input_Layer1 = tf.keras.layers.Input(shape=(2))  
x = tf.keras.layers.Dense(4, activation='sigmoid')(input_Layer1)  
x = tf.keras.layers.Dense(5, activation='sigmoid')(x)  
Out_Layer= tf.keras.layers.Dense(1, activation='sigmoid')(x)  
model = tf.keras.Model(inputs=[input_Layer1], outputs=[Out_Layer])  
model.summary()  
  
# 모델 loss, 학습 방법 결정하기  
optimizer=tf.keras.optimizers.SGD(lr=0.5) ### 경사 하강법으로 global m  
loss=tf.keras.losses.binary_crossentropy ## 예측값과 정답의 오차값 중  
metrics=tf.keras.metrics.binary_accuracy ### 학습하면서 평가할 메트릭스  
  
# 모델 컴파일하기  
model.compile(loss=loss, optimizer=optimizer, metrics=[metrics])  
  
# 모델 동작하기  
model.fit(x_data, y_data, epochs=2000, batch_size=4)  
# model.fit(x_data,y_data, epochs=1000,)
```

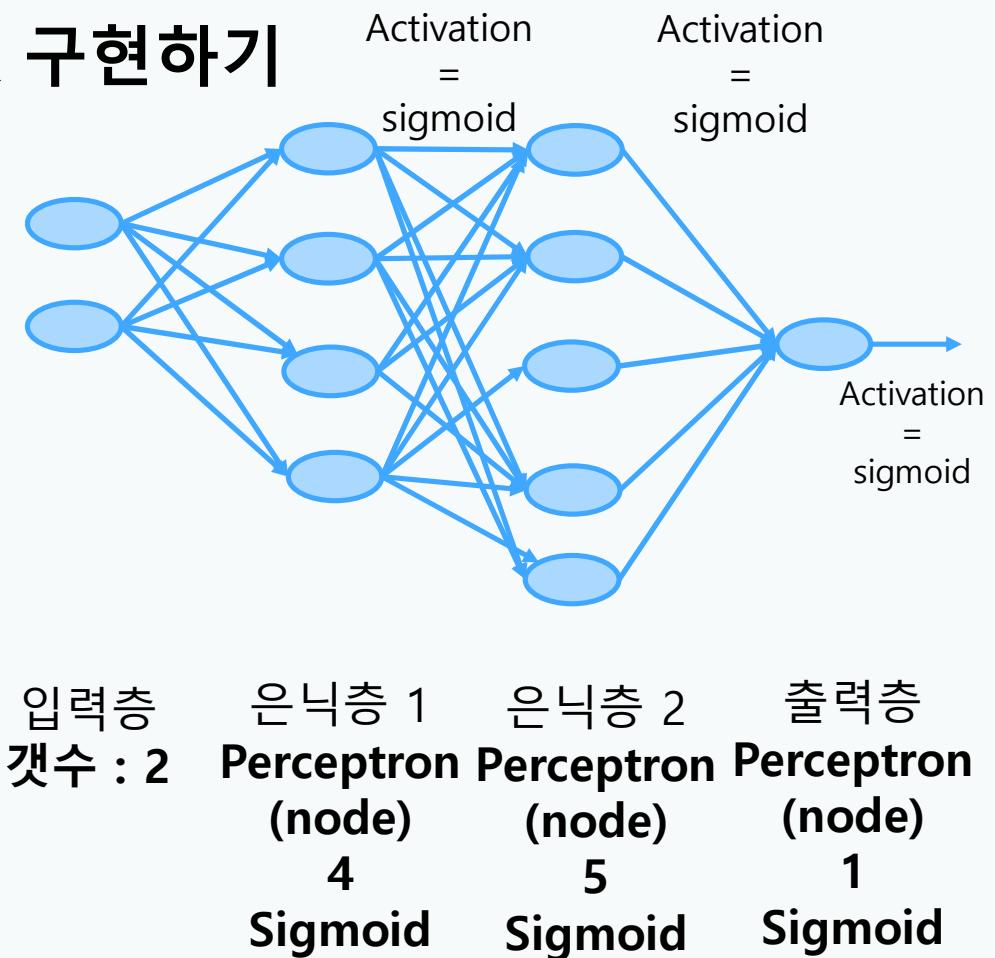


4. Neural Network 실습

Neural Network 구현하기

Model: "model"

Layer (type)	Output Shape	Param #
=====		
input_1 (InputLayer)	[None, 2]	0
dense (Dense)	(None, 4)	12
dense_1 (Dense)	(None, 5)	25
dense_2 (Dense)	(None, 1)	6
=====		
Total params: 43		
Trainable params: 43		
Non-trainable params: 0		



4. Neural Network 실습

Neural Network 구현하기

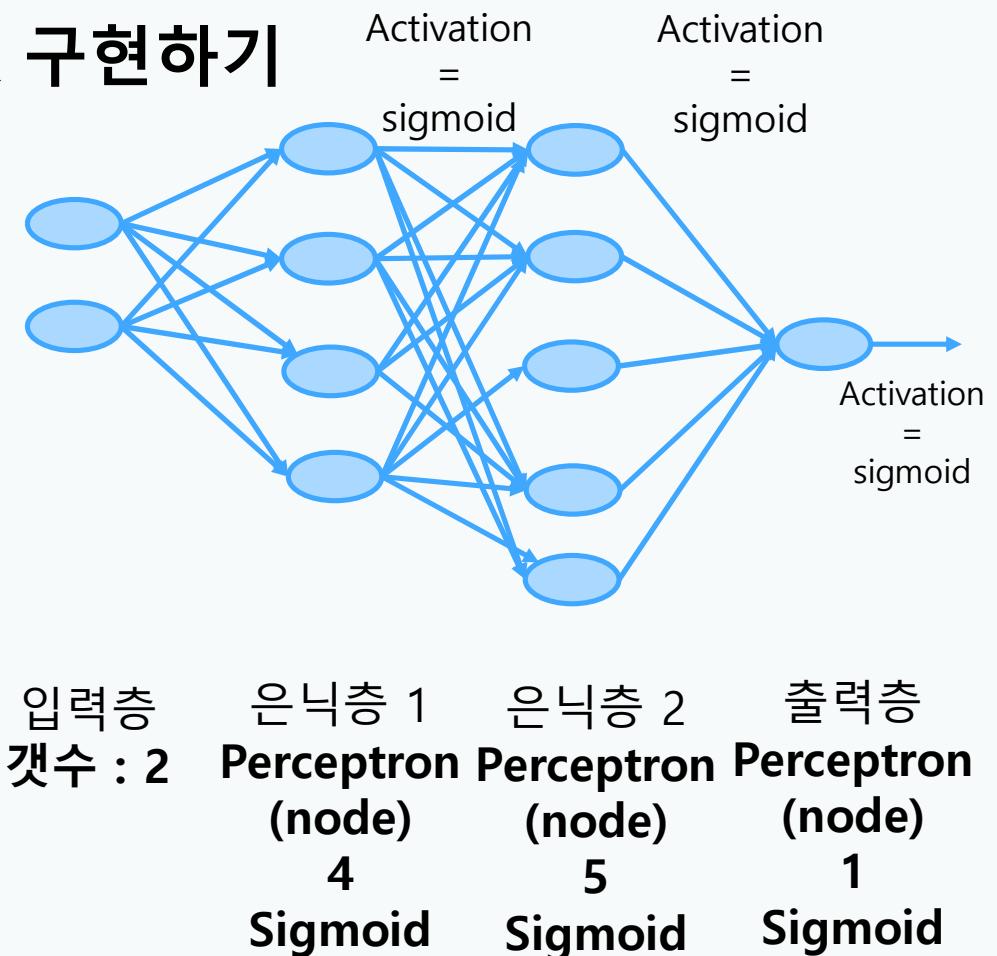
Model: "model"

Layer (type)	Output Shape	Param #
=====		
input_1 (InputLayer)	[None, 2]	0
dense (Dense)	(None, 4)	12
dense_1 (Dense)	(None, 5)	25
dense_2 (Dense)	(None, 1)	6
=====		

Total params: 43

Trainable params: 43

Non-trainable params: 0



4. Neural Network 실습

Neural Network 구현하기

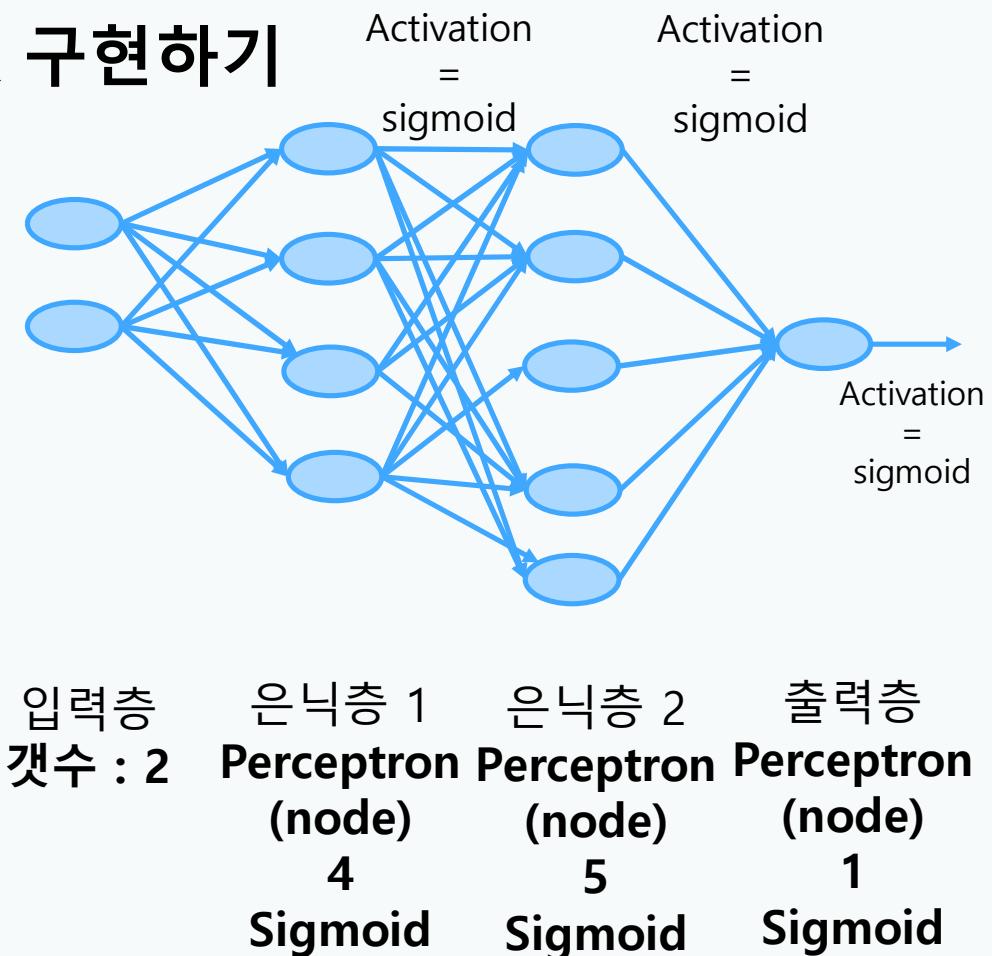
Model: "model"

Layer (type)	Output Shape	Param #
Batch Size		
input_1 (InputLayer)	[None, 2]	0
Batch Size		
dense (Dense)	(None, 4)	12
Batch Size		
dense_1 (Dense)	(None, 5)	25
Batch Size		
dense_2 (Dense)	(None, 1)	6
=====		

Total params: 43

Trainable params: 43

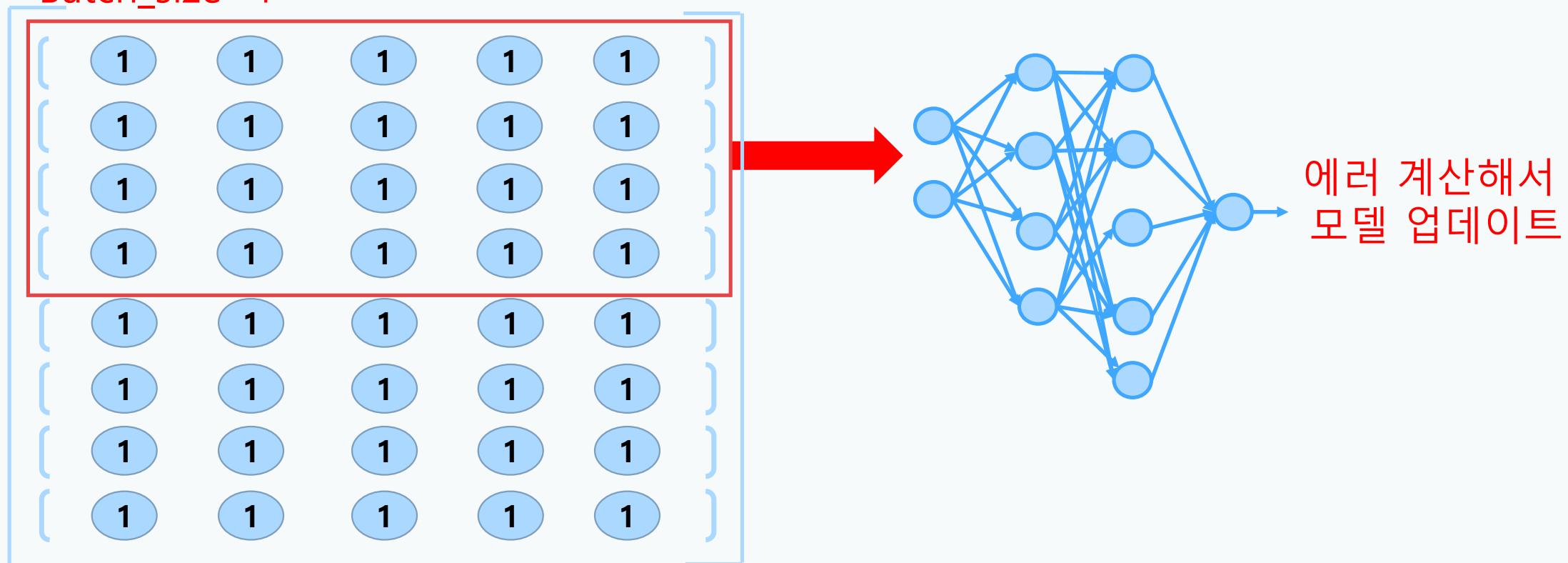
Non-trainable params: 0



4. Neural Network 실습

Batch_size=4

데이터 분리 학습 과정 살펴보기



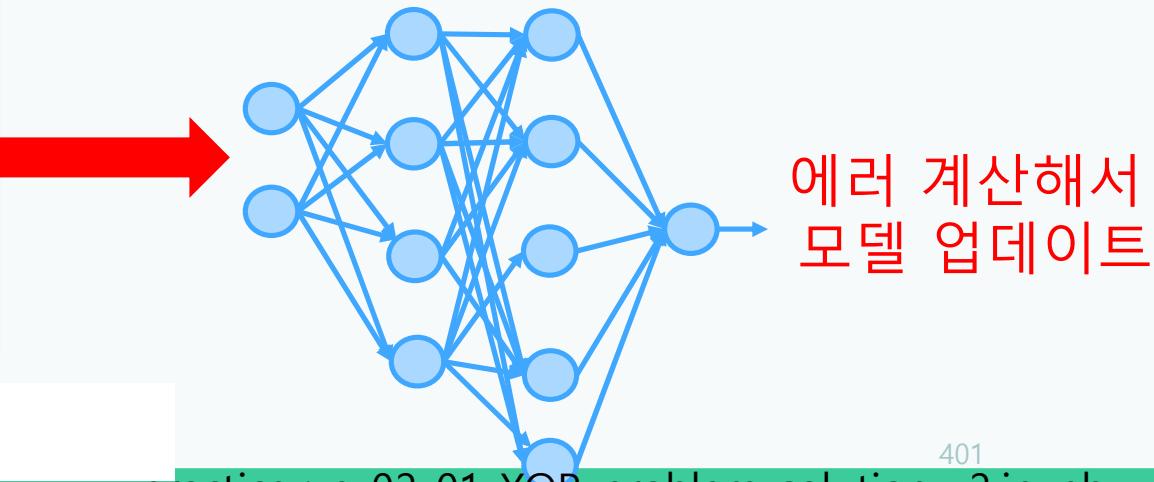
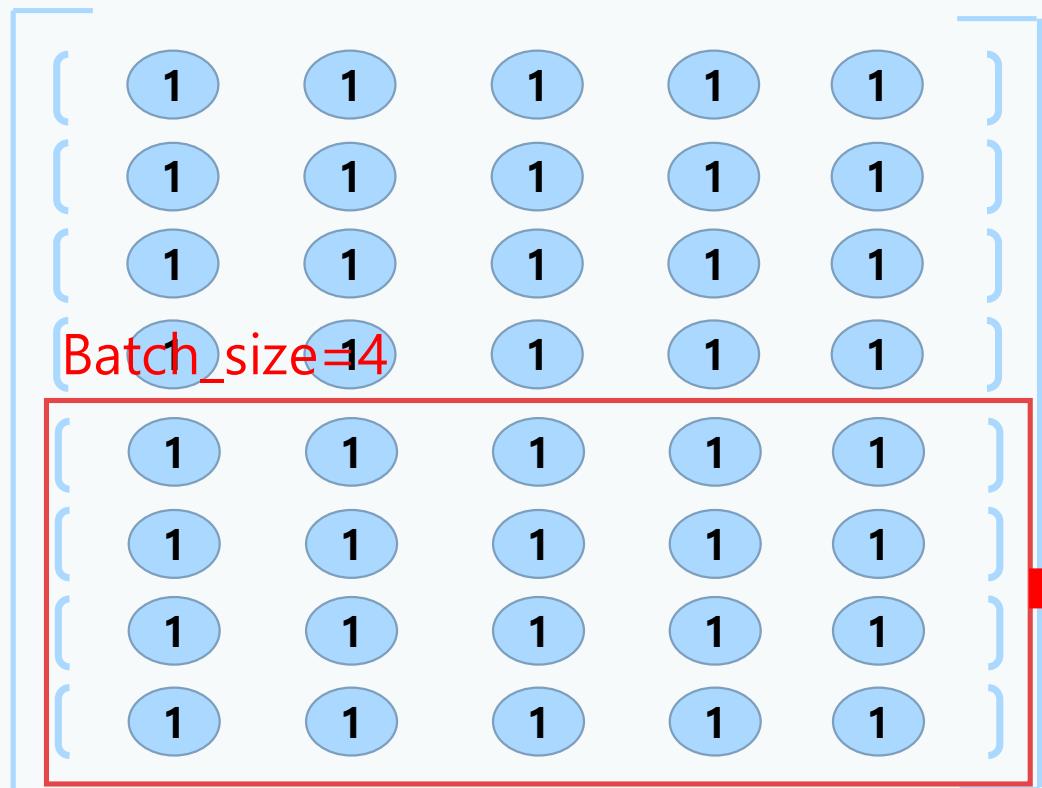
모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

practice : p_02_01_XOR_problem_solution_v2.ipynb

4. Neural Network 실습

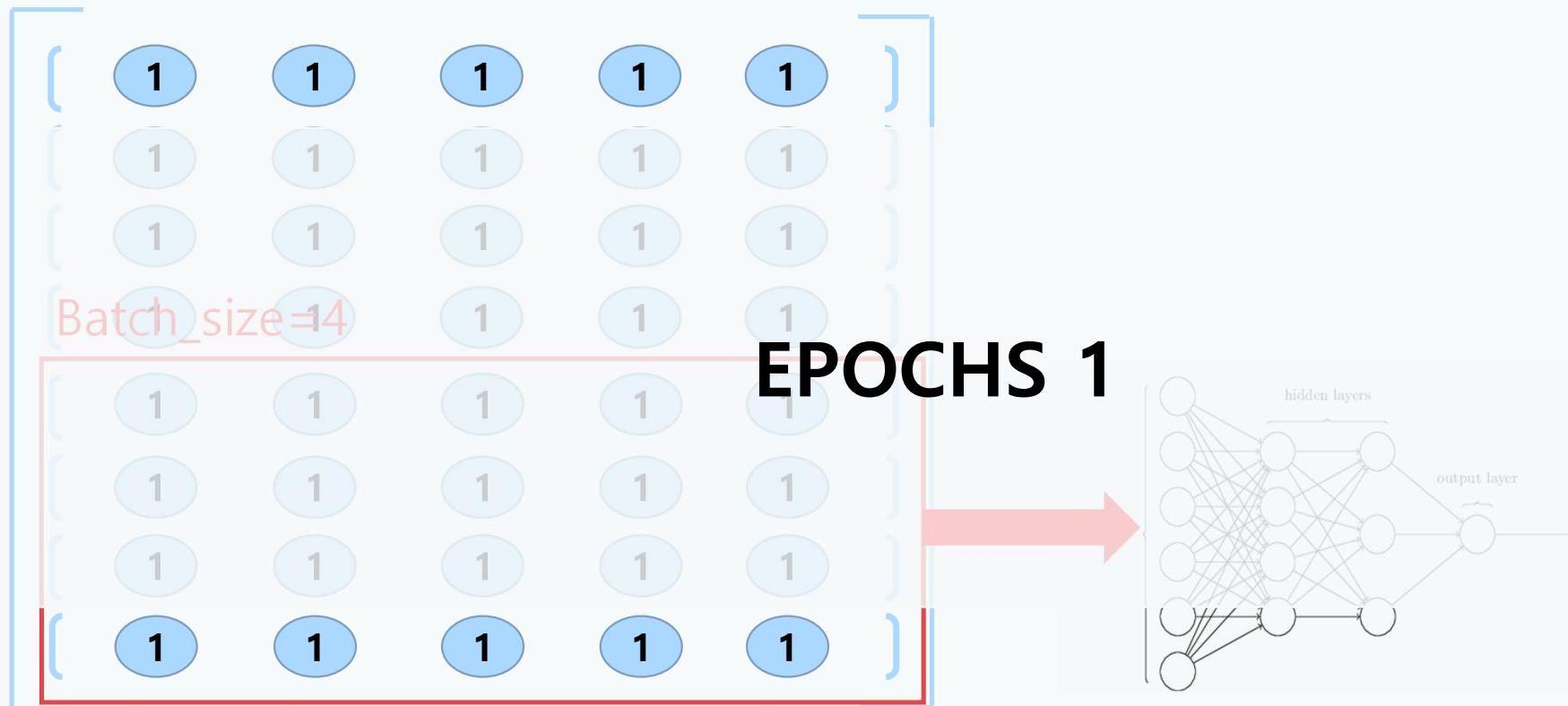
데이터 분리 학습 과정 살펴보기



```
# 모델 동작하기  
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

4. Neural Network 실습

데이터 분리 학습 과정 살펴보기



모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

에러 계산해서
모델 업데이트

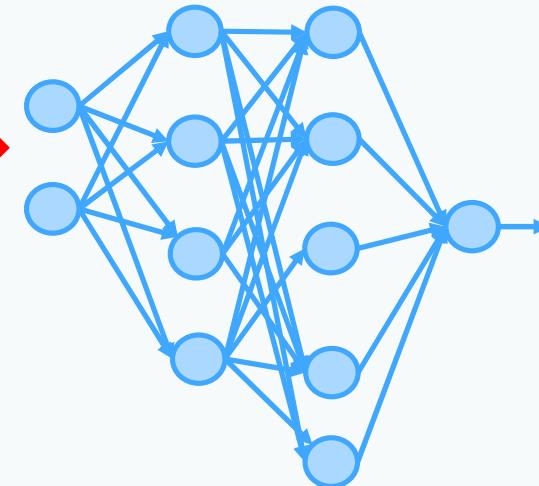
practice : p_02_01_XOR_problem_solution_v2.ipynb

4. Neural Network 실습

Batch_size=4

데이터 분리 학습 과정 살펴보기

1	1	1	1	1
1	1	1	1	1
1	1	1	1	1
1	1	1	1	1
1	1	1	1	1
1	1	1	1	1
1	1	1	1	1
1	1	1	1	1



에러 계산해서
모델 업데이트

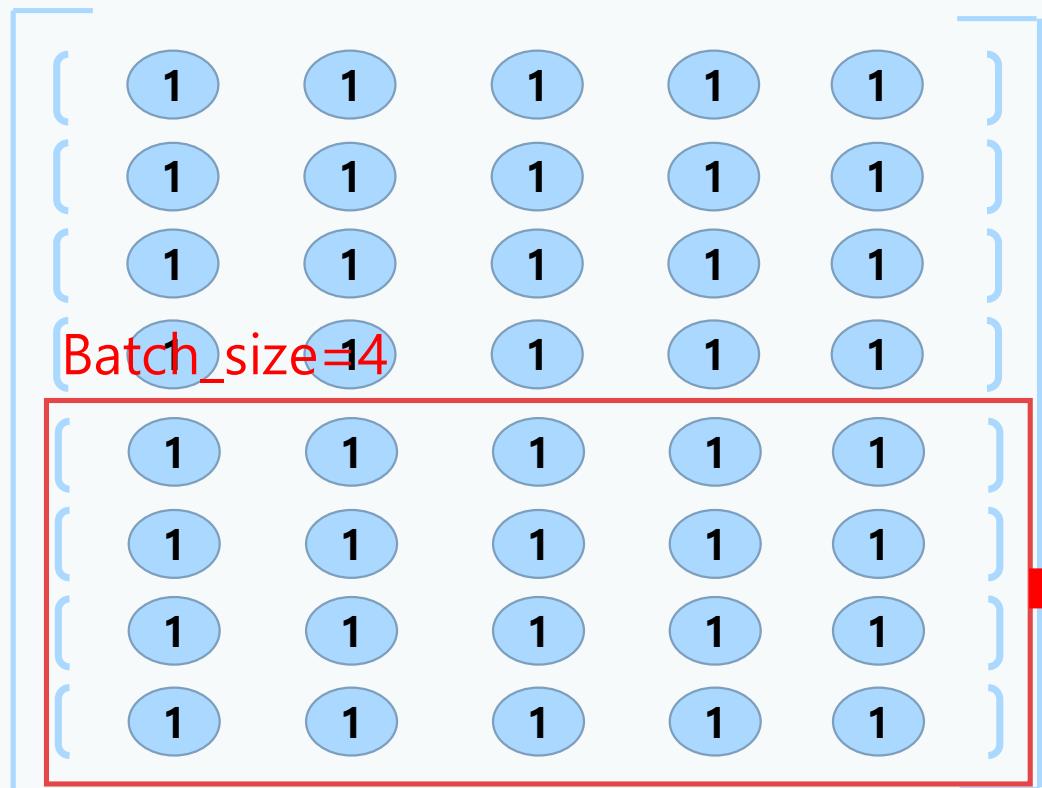
모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

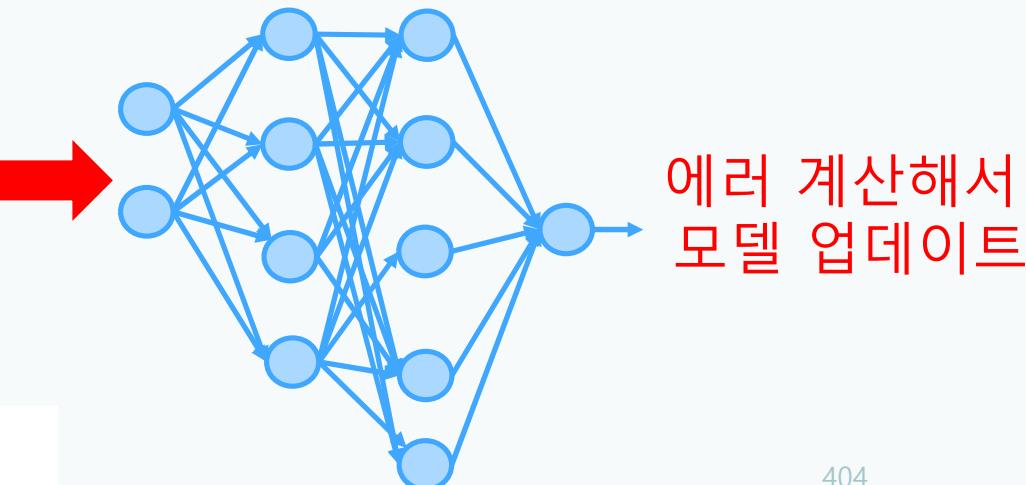
practice : p_02_01_XOR_problem_solution_v2.ipynb

4. Neural Network 실습

데이터 분리 학습 과정 살펴보기



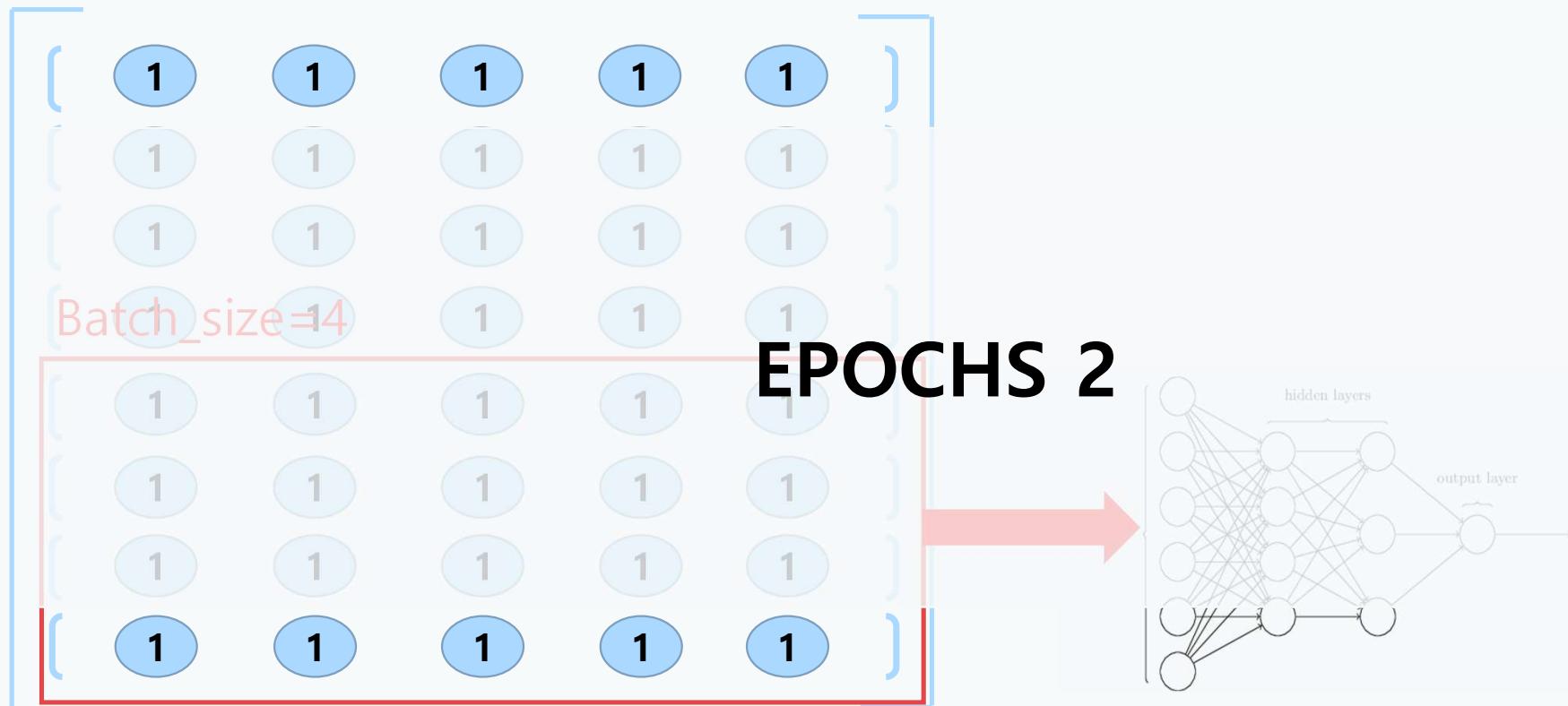
```
# 모델 동작하기  
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```



practice : p_02_01_XOR_problem_solution_v2.ipynb

4. Neural Network 실습

데이터 분리 학습 과정 살펴보기



모델 동작하기

```
model.fit(x_data, y_data, epochs=2000, batch_size=4)
```

에러 계산해서
모델 업데이트

practice : p_02_01_XOR_problem_solution_v2.ipynb

5. Neural Network 실습

Neural Network 구현하기

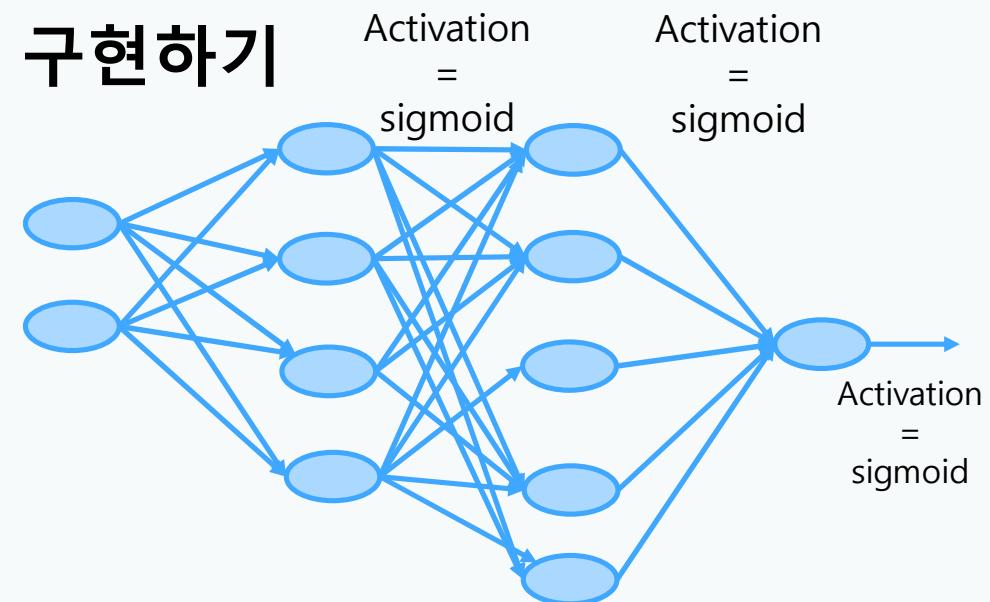
Model: "model"

Layer (type)	Output Shape	Param #
Batch Size		
input_1 (InputLayer)	[None, 2]	0
Batch Size		
dense (Dense)	(None, 4)	12
Batch Size		
dense_1 (Dense)	(None, 5)	25
Batch Size		
dense_2 (Dense)	(None, 1)	6

Total params: 43

Trainable params: 43

Non-trainable params: 0



입력층
차원 : (4, 2)
은닉층 1
(node) (4, 4)
은닉층 2
(node) (4, 5)
출력층
(node) (4, 1)
Perceptron
Perceptron
Perceptron
Sigmoid
Sigmoid
Sigmoid

4. Neural Network 실습



여기서 잠깐!!

4. Neural Network 실습



Activation function
Sigmoid function

4. Neural Network 실습

- Logistic sigmoid

- Perceptron

- 출력을 0~1사이로 변환해 주는 함수로 사용.

- Cross entropy loss 함수에 사용.

- Binary classification에 활용

- Output Layer에 적용

- Neural Network

- Hidden Layer

- Perceptron을 여러 개 쌓아서 비선형으로 만들어 주기위해 사용

- Hidden Layer에 적용

- Output Layer

- Regression / classification task를 위해 출력 activation function + loss 함수에 사용

4. Neural Network 실습

NN Regression

house_price_of_area.csv 파일을 가지고
Neural Network 를 학습하여
지역 집 가격 예측하는 모델 만들기

4. Neural Network 실습

NN Regression

house_price_of_area.csv 데이터를 살펴보겠습니다.

	x1	x2	x3	x4	x5	y
1	32	84.87	10	24.98	121.54	37.9
2	19.5	306.59	9	24.98	121.53	42.2
3	13.3	561.98	5	24.98	121.54	47.3

415	6.5	90.45	9	24.97	121.54	63.9

샘플수 : 415

속성 : 1 (house age), Length2(distance station), Length3(number of convenience stores) 등 5개

예측값 : house_price_of_area

411

practice : p_02_02_house_price_of_area_prediction.ipynb

4. Neural Network 실습

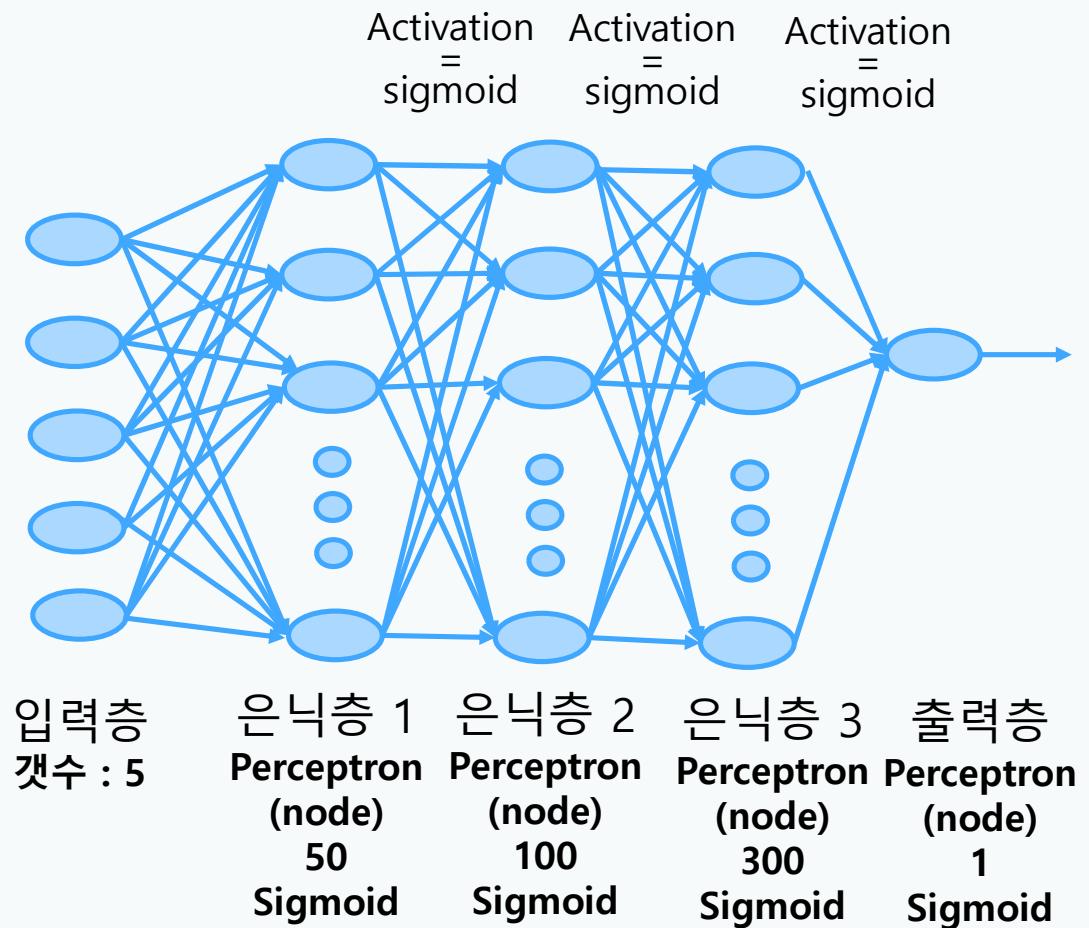
```
2 import pandas as pd
3 import tensorflow as tf
4 import matplotlib.pyplot as plt
5
6 ## 데이터 읽어오기.
7 df = pd.read_csv("../dataset/house_price_of_unit_area.csv")
8 print(df.info())
9 print(df.head())
10
11 ## data copy
12 dataset=df.copy()
13
14 ## 데이터에서 Label 데이터 추출
15 label_data=dataset.pop("house price of unit area")
16
17 # 모델의 설계
18 input_Layer = tf.keras.layers.Input(shape=(5,))
19 x = tf.keras.layers.Dense(50, activation='sigmoid')(input_Layer)
20 x= tf.keras.layers.Dense(100, activation='sigmoid')(x)
21 x= tf.keras.layers.Dense(300, activation='sigmoid')(x)
22 Out_Layer= tf.keras.layers.Dense(1, activation=None)(x)
23
24 model = tf.keras.Model(inputs=[input_Layer], outputs=[Out_Layer])
25 model.summary()
```

dataset	x1	x2	x3	x4	x5	y
1	32	84.87	10	24.98	121.54	37.9
2	19.5	306.59	9	24.98	121.53	42.2
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415	6.5	90.45	9	24.97	121.54	63.9

4. Neural Network 실습

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23
24 model = tf.keras.Model(inputs=[input_Layer], outputs=[Out_Layer])
25 model.summary()
```



4. Neural Network 실습

NN Regression

집값 예측하기
BostonHousing.csv 파일을 가지고
Neural Network 를 학습하여
집값 예측하는 모델 만들기

4. Neural Network 실습

NN Regression

BostonHousing.csv 데이터를 살펴보겠습니다.

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	B	LSTAT	MEDV
1	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98	24.0
2	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14	21.6
3	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03	34.7

506	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33	36.2

샘플수 : 506

속성 : CRIM(범죄율), ZN(거주지역비율), INDUS(토지비율), CHAS(찰스강 경계위치), NOX(일산화질소값), RM(방의갯수) ... 등 총 13개

예측값 : MEDV(집값: 단위는 \$1,000)

4. Neural Network 실습

NN Regression

성능이 잘 나오나요~?

4. Neural Network 실습

NN Regression

생각보다 성능이 잘 안나옵니다..

왜 일까요??



4. Neural Network 실습

NN Regression

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	B	LSTAT	MEDV
1	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98	24.0
2	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14	21.6
3	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03	34.7

506	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33	36.2

	Length1	Length2	Length3	Height	Width	Weight
1	23.2	25.4	30	11.52	4.02	242
2	24	26.3	31.2	12.48	4.3056	290
3	23.9	26.5	31.1	12.3778	4.6961	340

159	13.8	15	16.2	2.9322	1.8792	19.9

4. Neural Network 실습

NN Regression

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	B	LSTAT	MEDV
1	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98	24.0
2	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14	21.6
3	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03	34.7

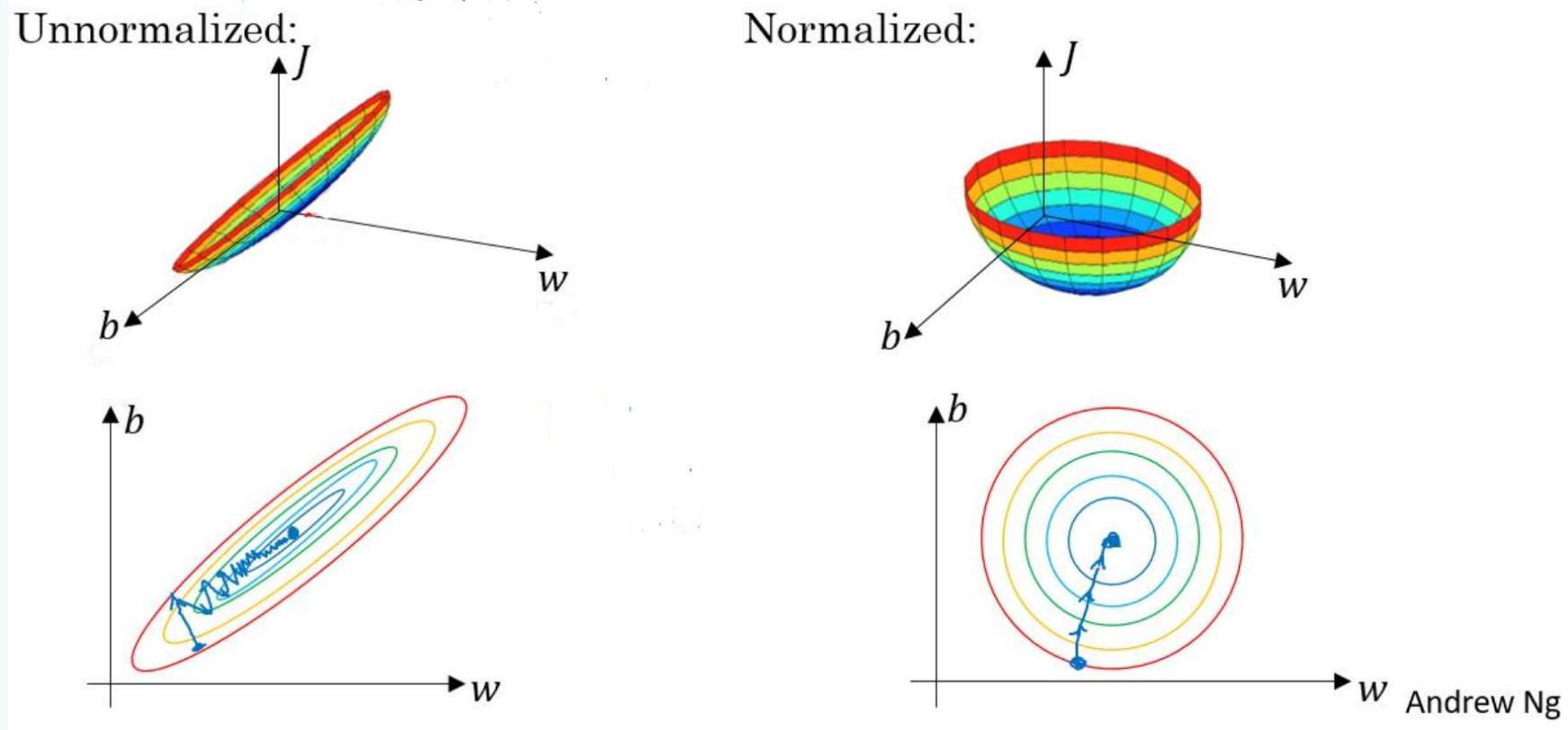
506	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33	36.2

	Length1	Length2	Length3	Height	Width	Weight
1	23.2	25.4	30	11.52	4.02	242
2	24	26.3	31.2	12.48	4.3056	290
3	23.9	26.5	31.1	12.3778	4.6961	340

159	13.8	15	16.2	2.9322	1.8792	19.9

4. Neural Network 실습

NN Regression -normalization



4. Neural Network 실습

NN Regression



4. Neural Network 실습

Normalization 대표적인 방법

1. Min max : 일정 범위(일반적으로 0~1) 사이로 scaling 함

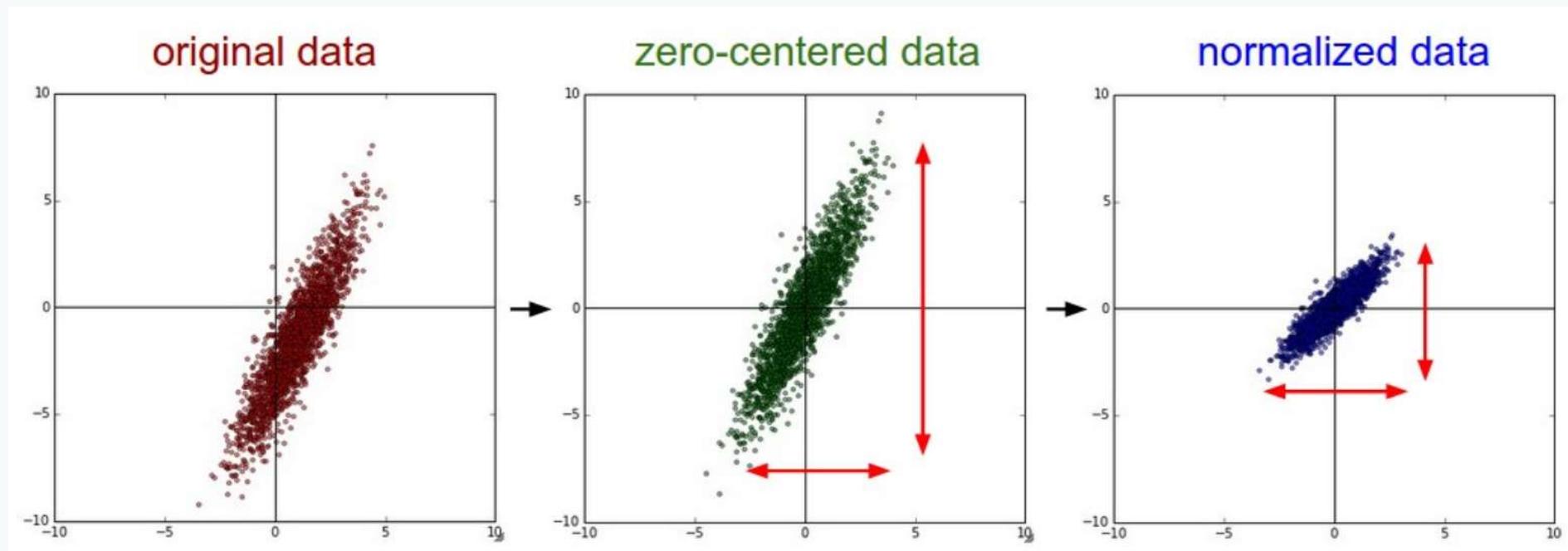
$$x = \frac{x - x_{min}}{x_{max} - x_{min}}$$

2. Standardization : mean 차감을 통해 zero-centered화 해주고 std로 나누어 주어 데이터가 일정 범위안에 머무르게 함

$$x = \frac{x - x_{mean}}{x_{std}}$$

4. Neural Network 실습

Standardization Normalization



4. Neural Network 실습

Standardization Normalization

Min Max Normalization

실습 하기

practice : P_02_03_normalization.ipynb
exersice : 02_03_normalization.ipynb
424

4. Neural Network 실습

입력과 정답분리

	A	B	C	D
1	1	10	100	2
2	2	20	200	2
3	3	30	300	2

10	10	100	1000	2

practice : P_02_03_normalization.ipynb
exersice : 02_03_normalization.ipynb
425

4. Neural Network 실습

Normalization

	A	B	C	D
1	1	10	100	2
2	2	20	200	2
3	3	30	300	2

10	10	100	1000	2

practice : P_02_03_normalization.ipynb
exersice : 02_03_normalization.ipynb
426

4. Neural Network 실습

```
5  
6 ## 데이터 읽어오기.## 데이터 읽어오기.  
7 raw_df = pd.read_csv("../dataset/test.csv")  
8 print(raw_df.info())  
9 print(raw_df.head())  
10 dataset=raw_df.copy()  
  
11 ## 데이터 분포도 확인하기.  
12 sns.pairplot(dataset[["A","B","C","D"]], diag_kind="kde")  
13 plt.show()  
  
14 train_labels = dataset.pop("D")  
  
15 ## 데이터의 min, max, mean, std 를 구하기.  
16 dataset_stats = dataset.describe()  
17 dataset_stats = dataset_stats.transpose()  
  
18 ## data normalization  
19 def min_max_norm(x):  
20     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])  
  
21 def standard_norm(x):  
22     return (x - dataset_stats['mean']) / dataset_stats['std']  
  
23 min_max_norm_train_data = min_max_norm(dataset)  
24 standard_norm_train_data = standard_norm(dataset)
```

Data 읽어오기

	A	B	C	D
1	1	10	100	2
2	2	20	200	2
3	3	30	300	2

10	10	100	1000	2

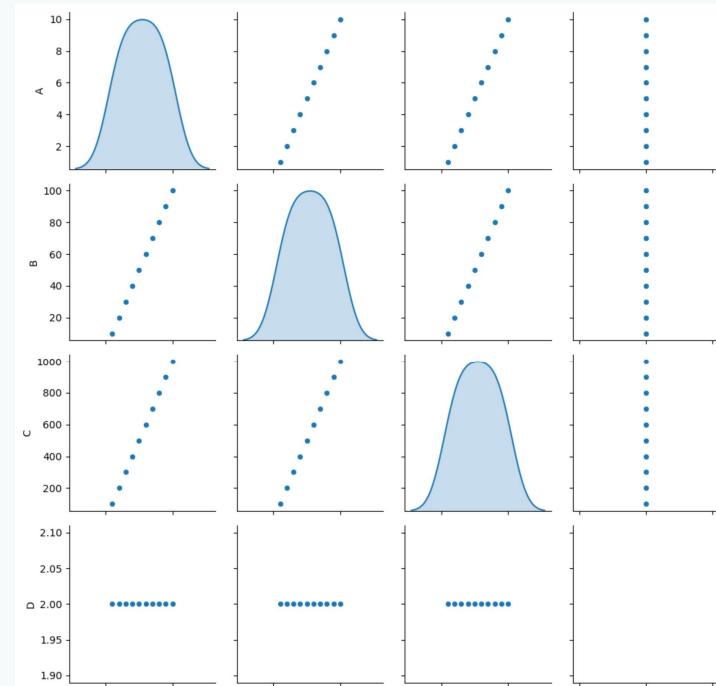
practice : P_02_03_normalization.ipynb
exersice : 02_03_normalization.ipynb

4. Neural Network 실습

```
5  
6 ## 데이터 읽어오기.## 데이터 읽어오기.  
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26 def standard_norm(x):  
27     return (x - dataset_stats['mean']) / dataset_stats['std']  
28  
29 min_max_norm_train_data = min_max_norm(dataset)  
30 standard_norm_train_data = standard_norm(dataset)  
31
```

Data 읽어오기

Data 분포도



practice : P_02_03_normalization.ipynb
exersice : 02_03_normalization.ipynb

4. Neural Network 실습

```
5 ## 데이터 읽어오기.## 데이터 읽어오기.  
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24  
25 def standard_norm(x):  
26     return (x - dataset_stats['mean']) / dataset_stats['std']  
27  
28 min_max_norm_train_data = min_max_norm(dataset)  
29 standard_norm_train_data = standard_norm(dataset)  
30  
31
```

Data 읽어오기

Data 분포도

입력/정답분리

A	B	C	D
1	10	100	2
2	20	200	2
3	30	300	2
...
10	100	1000	2

practice : P_02_03_normalization.ipynb
exersice : 02_03_normalization.ipynb

4. Neural Network 실습

```
5 ## 데이터 읽어오기.## 데이터 읽어오기.  
6 raw_df = pd.read_csv("../dataset/test.csv")  
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8 print(raw_df.head())  
9 dataset=raw_df.copy()  
10  
11 ## 데이터 분포도 확인하기.  
12 sns.pairplot(dataset[["A", "B", "C", "D"]], diag_kind="kde")  
13 plt.show()  
14  
15 train_labels = dataset.pop("D")  
16  
17 ## 데이터의 min, max, mean, std 값 구하기.  
18 dataset_stats = dataset.describe()  
19 dataset_stats = dataset_stats.transpose()  
20  
21 ## data normalization  
22 def min_max_norm(x):  
23     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])  
24  
25 def standard_norm(x):  
26     return (x - dataset_stats['mean']) / dataset_stats['std']  
27  
28 min_max_norm_train_data = min_max_norm(dataset)  
29 standard_norm_train_data = standard_norm(dataset)  
30  
31
```

Data 읽어오기

Data 분포도

입력/정답분리

데이터 특성
값 구하기

	A	B	C	D
count	10.00000	10.00000	10.00000	10.0
mean	5.50000	55.00000	550.00000	2.0
std	3.02765	30.276504	302.765035	0.0
min	1.00000	10.00000	100.00000	2.0
25%	3.25000	32.50000	325.00000	2.0
50%	5.50000	55.00000	550.00000	2.0
75%	7.75000	77.50000	775.00000	2.0
max	10.00000	100.00000	1000.00000	2.0

practice : P_02_03_normalization.ipynb
exersice : 02_03_normalization.ipynb

4. Neural Network 실습

```
5 ## 데이터 읽어오기.## 데이터 읽어오기.  
6 raw_df = pd.read_csv("../dataset/test.csv")  
7 print(raw_df.info())  
8 print(raw_df.head())  
9 dataset=raw_df.copy()  
10  
11 ## 데이터 분포도 확인하기.  
12 sns.pairplot(dataset[["A","B","C","D"]], diag_kind="kde")  
13 plt.show()  
14  
15 train_labels = dataset.pop("D")  
16  
17 ## 데이터의 min, max, mean, std 값 구하기.  
18 dataset_stats = dataset.describe()  
19 dataset_stats = dataset_stats.transpose()  
20  
21 ## data normalization  
22 def min_max_norm(x):  
23     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])  
24  
25 def standard_norm(x):  
26     return (x - dataset_stats['mean']) / dataset_stats['std']  
27  
28 min_max_norm_train_data = min_max_norm(dataset)  
29 standard_norm_train_data = standard_norm(dataset)  
30  
31
```

Data 읽어오기

Data 분포도

입력/정답분리

데이터 특성
값 구하기

데이터 특성
매트릭스 행/열 바꾸기

	A	B	C	D
count	10.00000	10.00000	10.00000	10.0
mean	5.50000	55.00000	550.00000	2.0
std	3.02765	30.276504	302.765035	0.0
min	1.00000	10.00000	100.00000	2.0
25%	3.25000	32.50000	325.00000	2.0
50%	5.50000	55.00000	550.00000	2.0
75%	7.75000	77.50000	775.00000	2.0
max	10.00000	100.00000	1000.00000	2.0



	count	mean	std	min	25%	50%	75%	max
A	10.0	5.5	3.027650	1.0	3.25	5.5	7.75	10.0
B	10.0	55.0	30.276504	10.0	32.50	55.0	77.50	100.0
C	10.0	550.0	302.765035	100.0	325.00	550.0	775.00	1000.0

practice : P_02_03_normalization.py
exersice : 02_03_normalization.py

4. Neural Network 실습

```
5 ## 데이터 읽어오기.## 데이터 읽어오기.  
6 raw_df = pd.read_csv("../dataset/test.csv")  
7 print(raw_df.info())  
8 print(raw_df.head())  
9 dataset=raw_df.copy()  
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11 ## 데이터 분포도 확인하기.  
12 sns.pairplot(dataset[["A","B","C","D"]], diag_kind="kde")  
13 plt.show()  
14  
15 train_labels = dataset.pop("D")  
16  
17 ## 데이터의 min, max, mean, std 값 구하기.  
18 dataset_stats = dataset.describe()  
19 dataset_stats = dataset_stats.transpose()  
20  
21 ## data normalization  
22 def min_max_norm(x):  
23     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])  
24  
25 def standard_norm(x):  
26     return (x - dataset_stats['mean']) / dataset_stats['std']  
27  
28 min_max_norm_train_data = min_max_norm(dataset)  
29 standard_norm_train_data = standard_norm(dataset)  
30  
31
```

→ Data 읽어오기

→ Data 분포도

→ 입력/정답분리

→ 데이터 특성
값 구하기

→ 데이터 특성
매트릭스 행/열 바꾸기

→ Min/max normalization , std normalization 함수선언

$$x = \frac{x - x_{\min}}{x_{\max} - x_{\min}} \quad X = \frac{x - x_{\text{mean}}}{x_{\text{std}}}$$

4. Neural Network 실습

```
5 ## 데이터 읽어오기.## 데이터 읽어오기.  
6 raw_df = pd.read_csv("../dataset/test.csv")  
7 print(raw_df.info())  
8 print(raw_df.head())  
9 dataset=raw_df.copy()  
10  
11 ## 데이터 분포도 확인하기.  
12 sns.pairplot(dataset[["A","B","C","D"]], diag_kind="kde")  
13 plt.show()  
14  
15 train_labels = dataset.pop("D")  
16  
17 ## 데이터의 min, max, mean, std 구하기.  
18 dataset_stats = dataset.describe()  
19 dataset_stats = dataset_stats.transpose()  
20  
21  
22 ## data normalization  
23 def min_max_norm(x):  
24     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])  
25  
26 def standard_norm(x):  
27     return (x - dataset_stats['mean']) / dataset_stats['std']  
28  
29 min_max_norm_train_data = min_max_norm(dataset)  
30 standard_norm_train_data = standard_norm(dataset)  
31
```

Min/max normalization , std normalization 적용

	A	B	C	A	B	C
0	0.000000	0.000000	0.000000	0	-1.486301	-1.486301
1	0.111111	0.111111	0.111111	1	-1.156012	-1.156012
2	0.222222	0.222222	0.222222	2	-0.825723	-0.825723
3	0.333333	0.333333	0.333333	3	-0.495434	-0.495434
4	0.444444	0.444444	0.444444	4	-0.165145	-0.165145
5	0.555556	0.555556	0.555556	5	0.165145	0.165145
6	0.666667	0.666667	0.666667	6	0.495434	0.495434
7	0.777778	0.777778	0.777778	7	0.825723	0.825723
8	0.888889	0.888889	0.888889	8	1.156012	1.156012
9	1.000000	1.000000	1.000000	9	1.486301	1.486301

exersice : 02_03_normalization.ipynb
practice : P_02_03_normalization.ipynb

4. Neural Network 실습

NN Regression

앞에서 실습하였던 지역 집값 예측 실습 코드에
normalization을 적용해 보겠습니다.

4. Neural Network 실습

NN Regression

```
7 ## 데이터 읽어오기.## 데이터 읽어오기.  
8 raw_df = pd.read_csv("../dataset/house_price_of_unit_area.csv")  
9 print(raw_df.info())  
10 print(raw_df.head())  
11  
12 ## data copy  
13 dataset=raw_df.copy()  
14  
15 ## data 분포도 확인  
16 sns.pairplot(dataset[["house age", "distance to the nearest MRT station", "number of convenience"]])  
17 plt.show()  
18  
19 ## label data 추출  
20 label_data=dataset.pop("house price of unit area")  
21  
22 ## 입력 데이터 열 별로 min, max, mean, std 구하기.  
23 dataset_stats = dataset.describe()  
24 dataset_stats = dataset_stats.transpose()  
25  
26 ## data normalization  
27 def min_max_norm(x):  
28     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])  
29 |  
30 def standard_norm(x):  
31     return (x - dataset_stats['mean']) / dataset_stats['std']  
32  
33 ## 데이터 normalization 하기.  
34 normed_train_data=standard_norm(dataset)
```

Pandas로 데이터 읽어오기

Data 분포도 확인하기.

데이터 추출하여 입력/정답 데이터로 분리

데이터 normalization을 위해
값 구하기

데이터 normalization

4. Neural Network 실습

NN Regression

앞에서 실습하였던 집값 예측 실습 코드에
normalization을 적용해 주세요

4. Neural Network 실습

NN Regression

성능이 잘 나오나요?

4. Neural Network 실습

Neural Network

당연히 잘 나옵니다.



4. Neural Network 실습

Neural Network

왜 잘 나올까요??

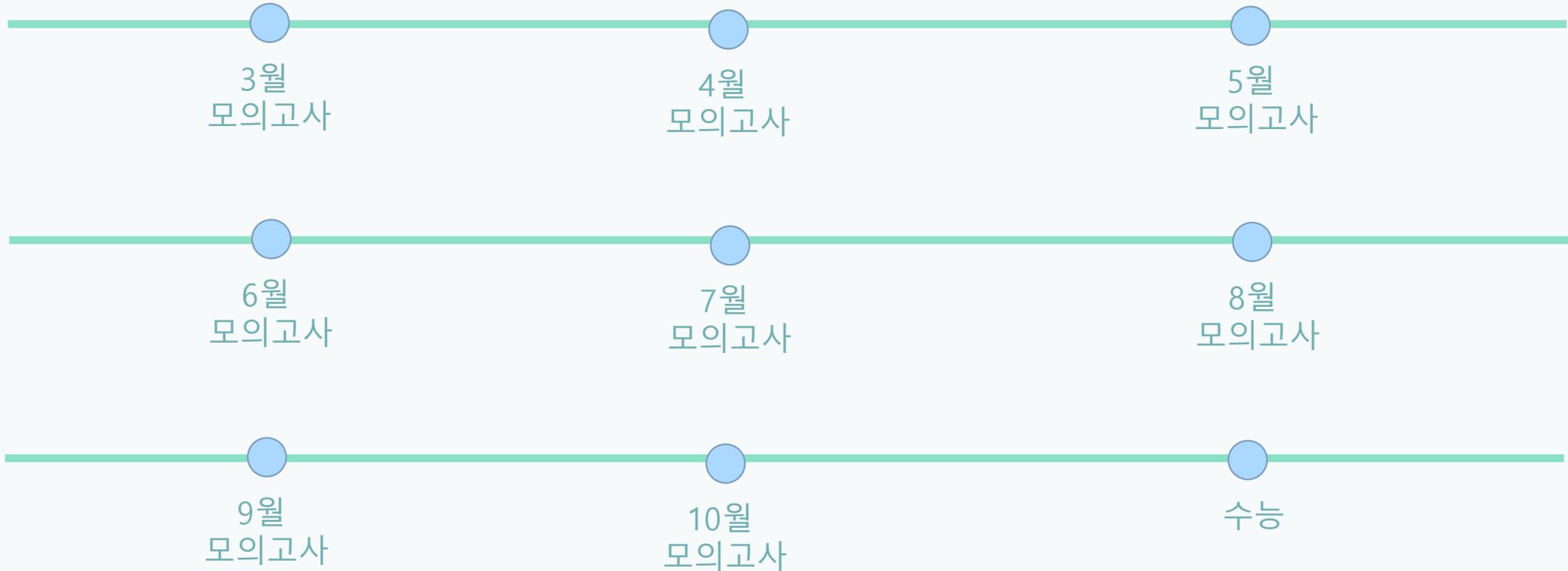


4. Neural Network 실습



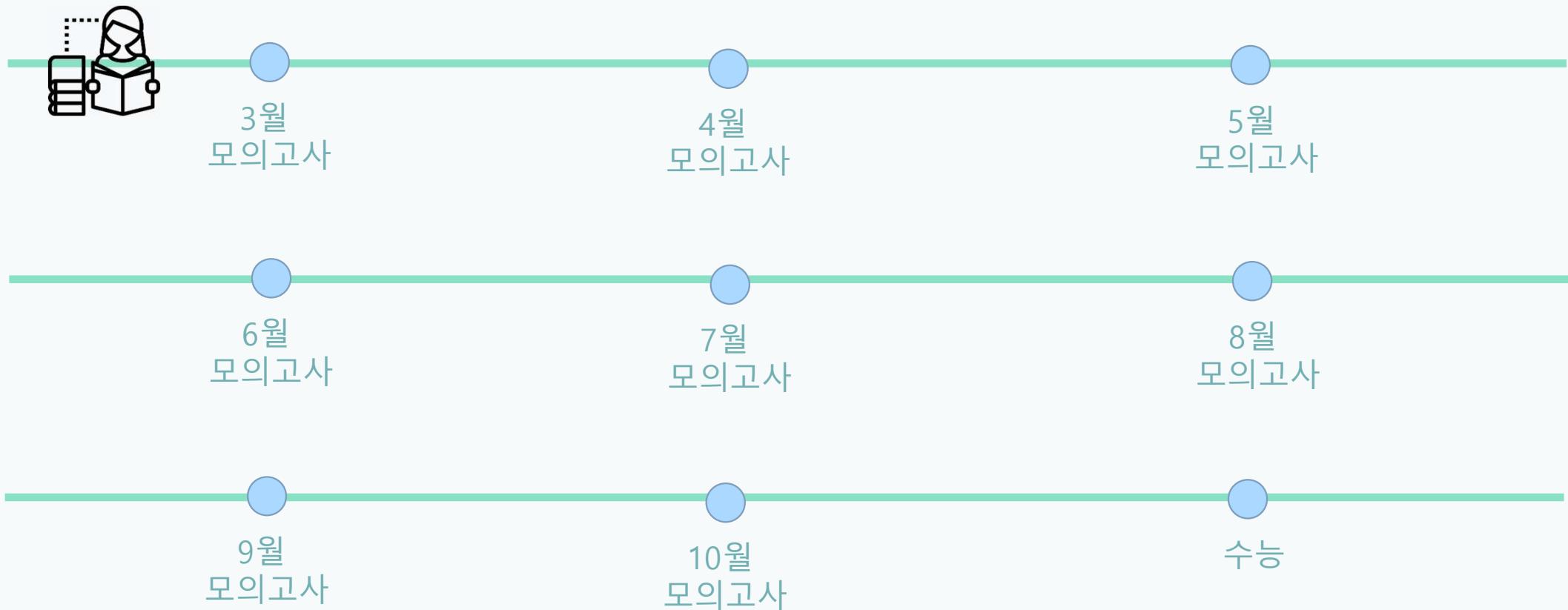
4. Neural Network 실습

Neural Network – 학습



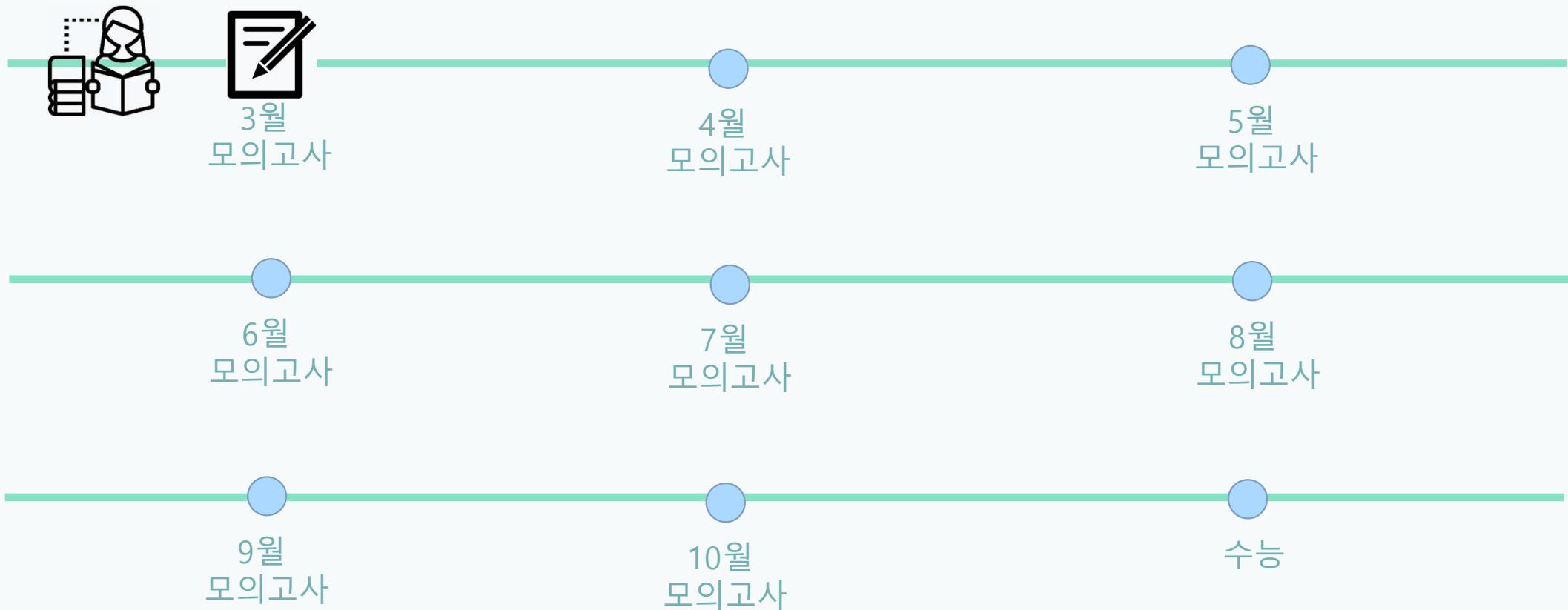
4. Neural Network 실습

Neural Network – 학습



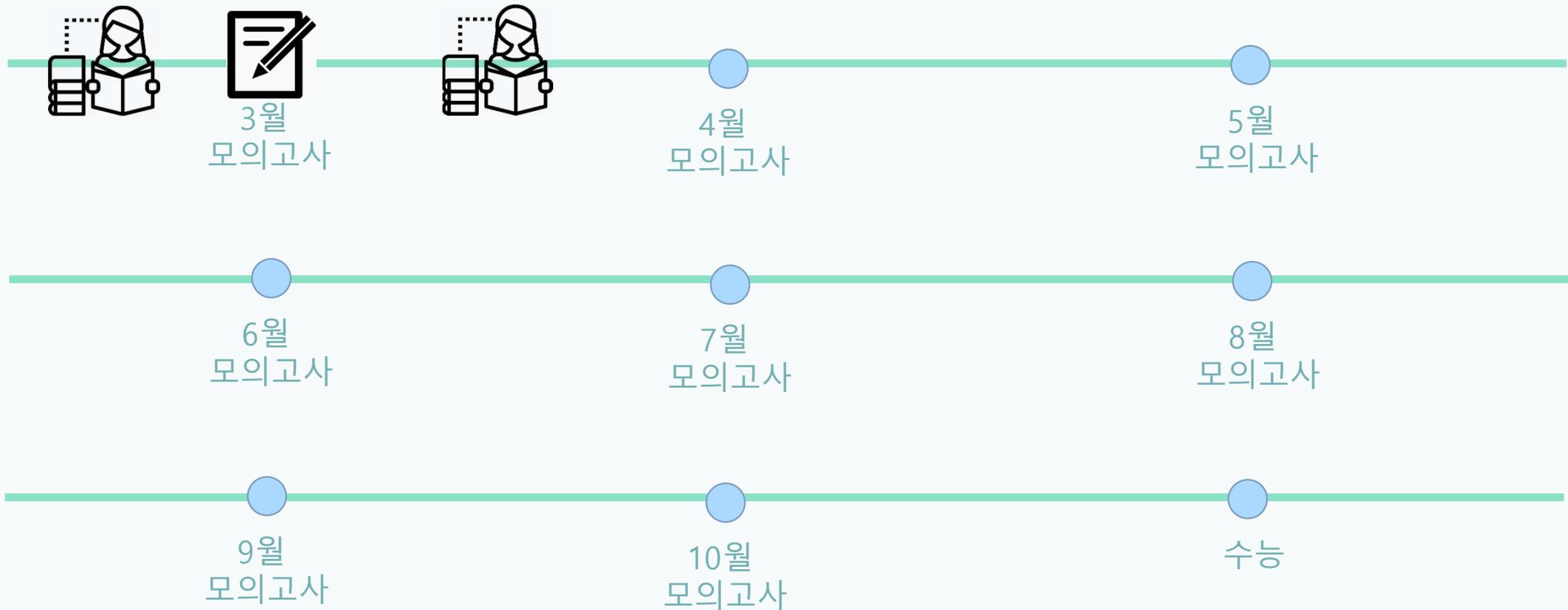
4. Neural Network 실습

Neural Network – 학습



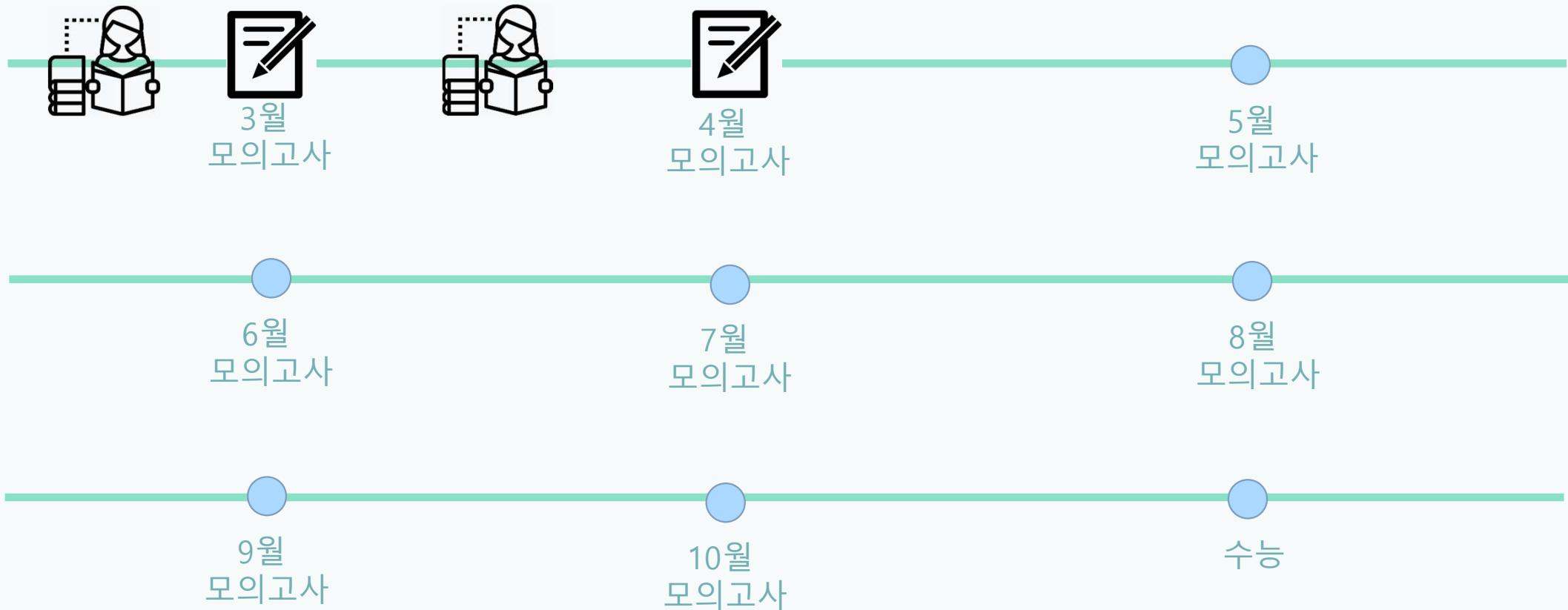
4. Neural Network 실습

Neural Network – 학습



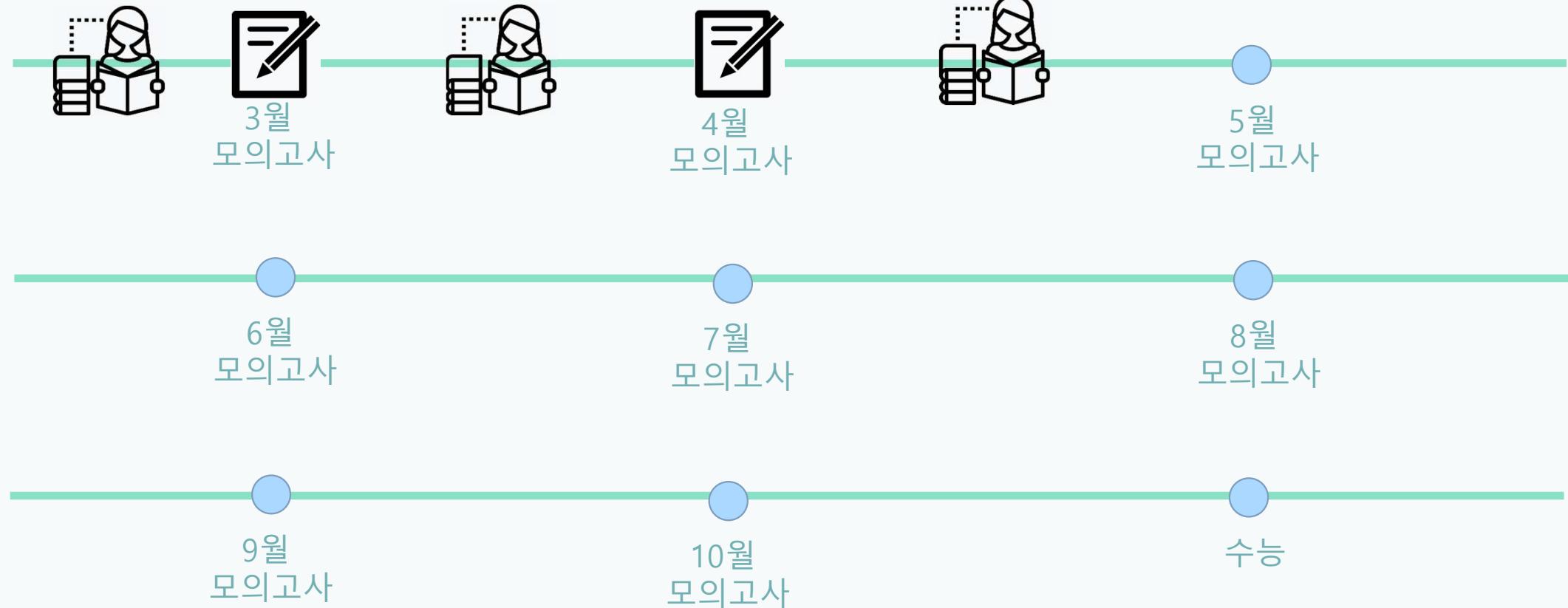
4. Neural Network 실습

Neural Network – 학습



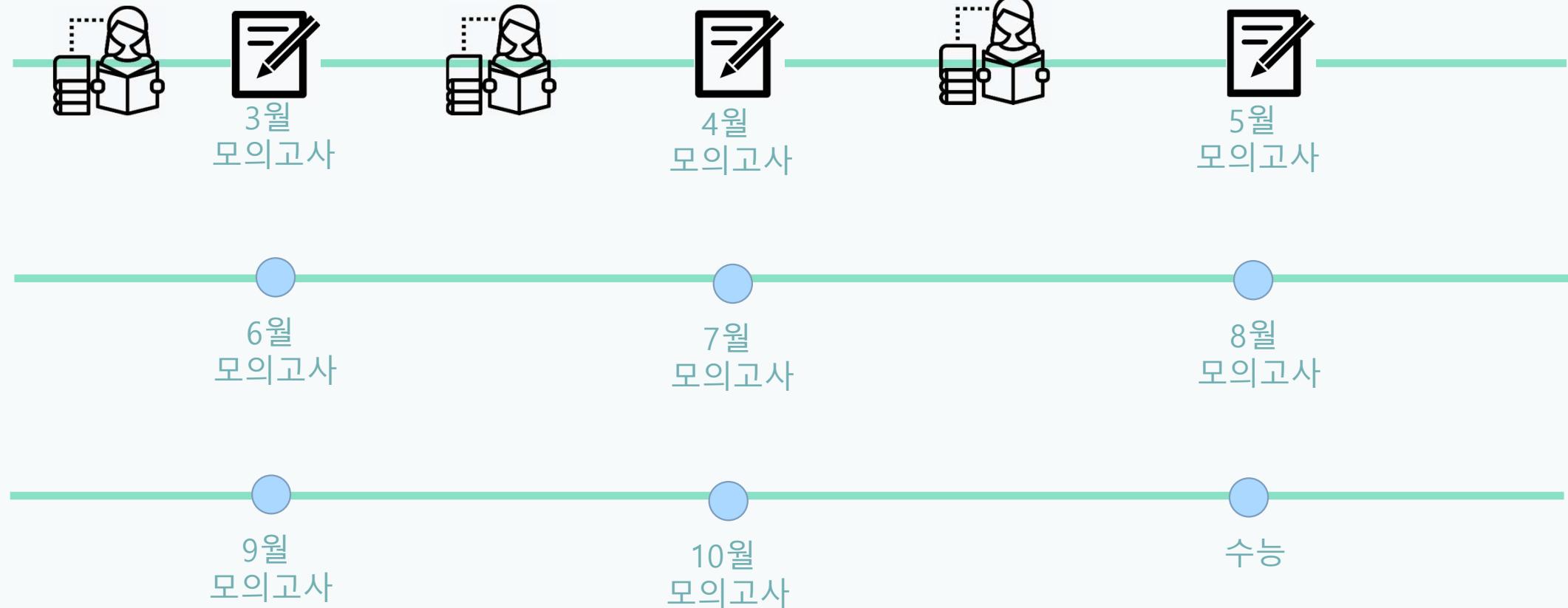
4. Neural Network 실습

Neural Network - 학습



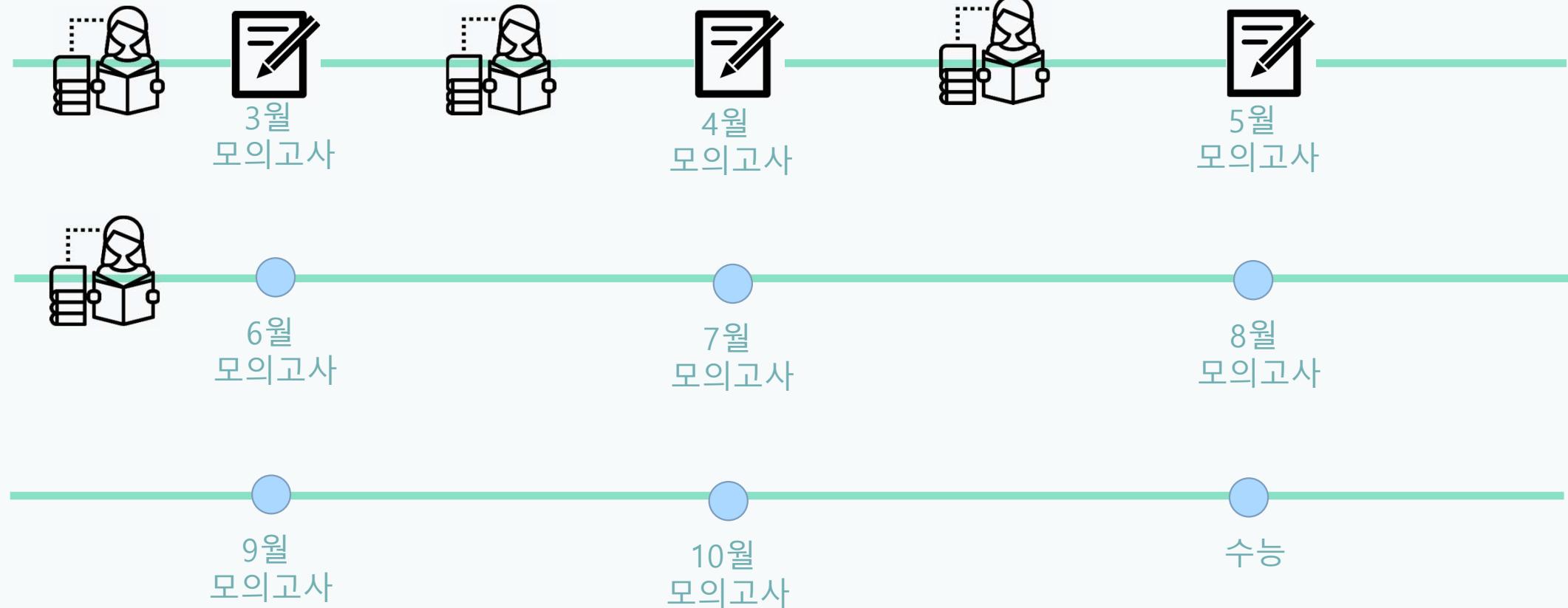
4. Neural Network 실습

Neural Network - 학습



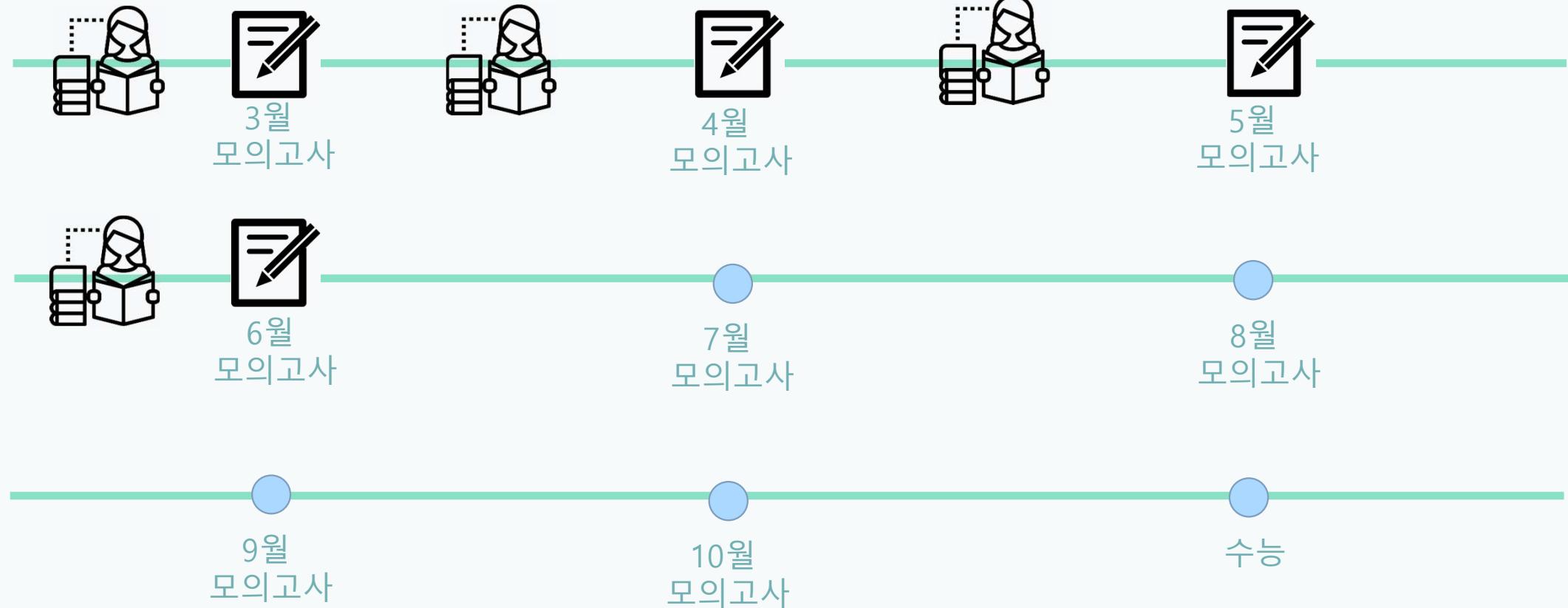
4. Neural Network 실습

Neural Network - 학습



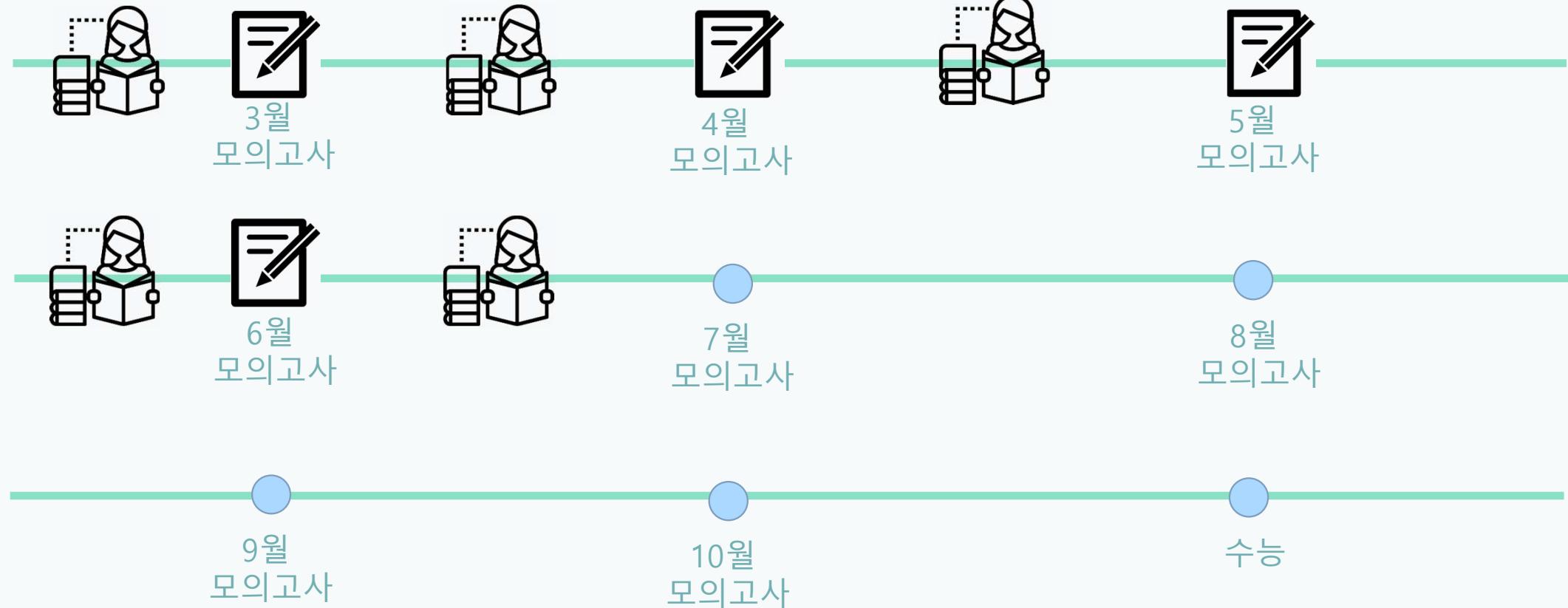
4. Neural Network 실습

Neural Network - 학습



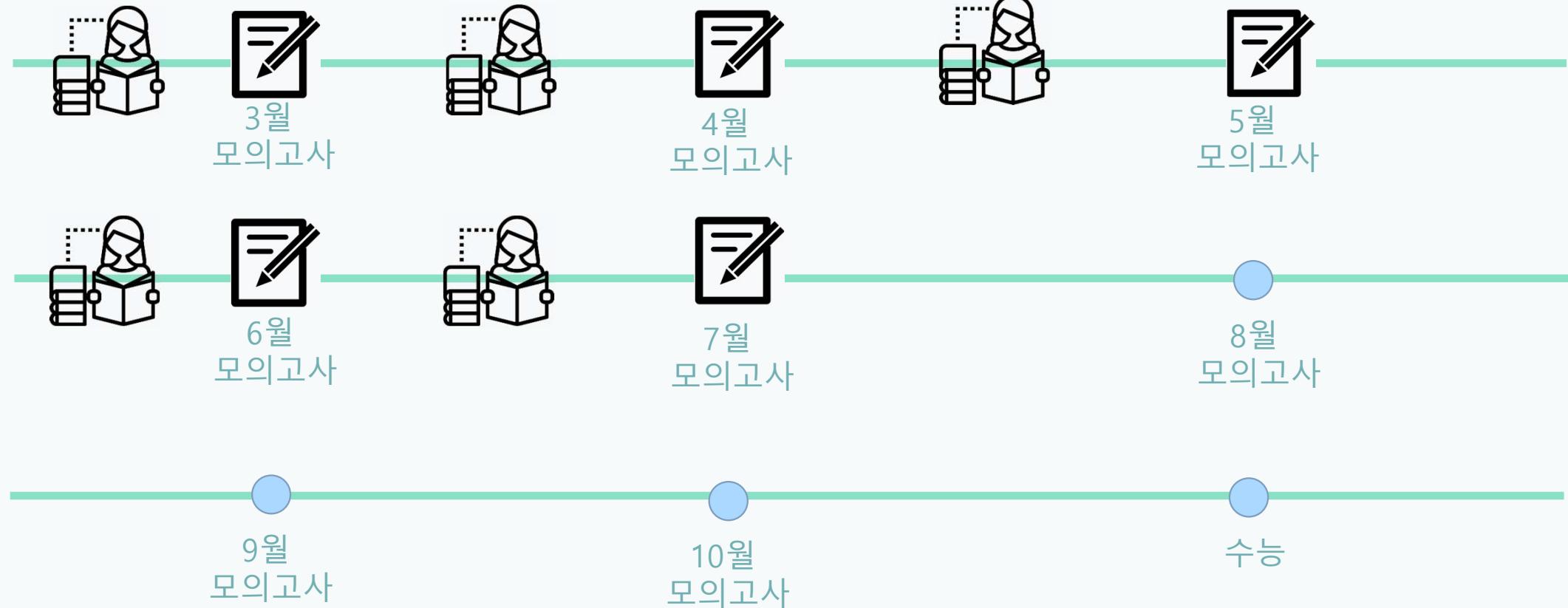
4. Neural Network 실습

Neural Network - 학습



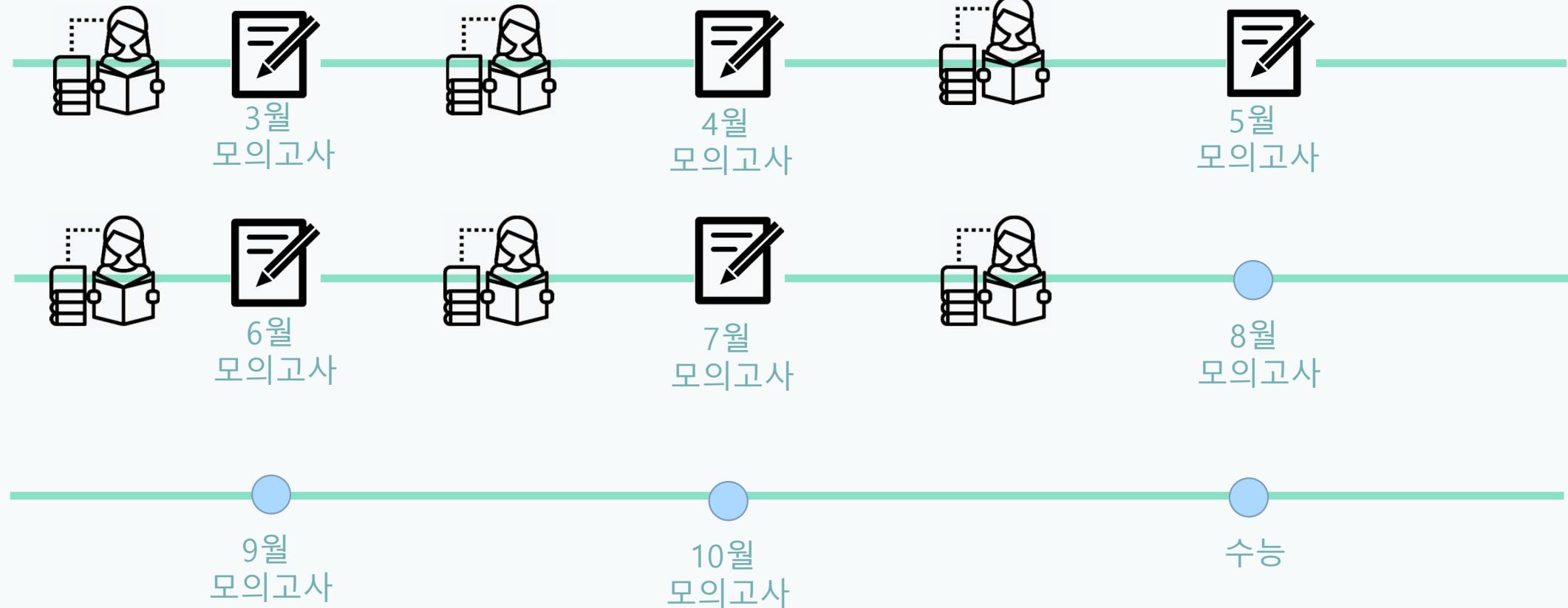
4. Neural Network 실습

Neural Network - 학습



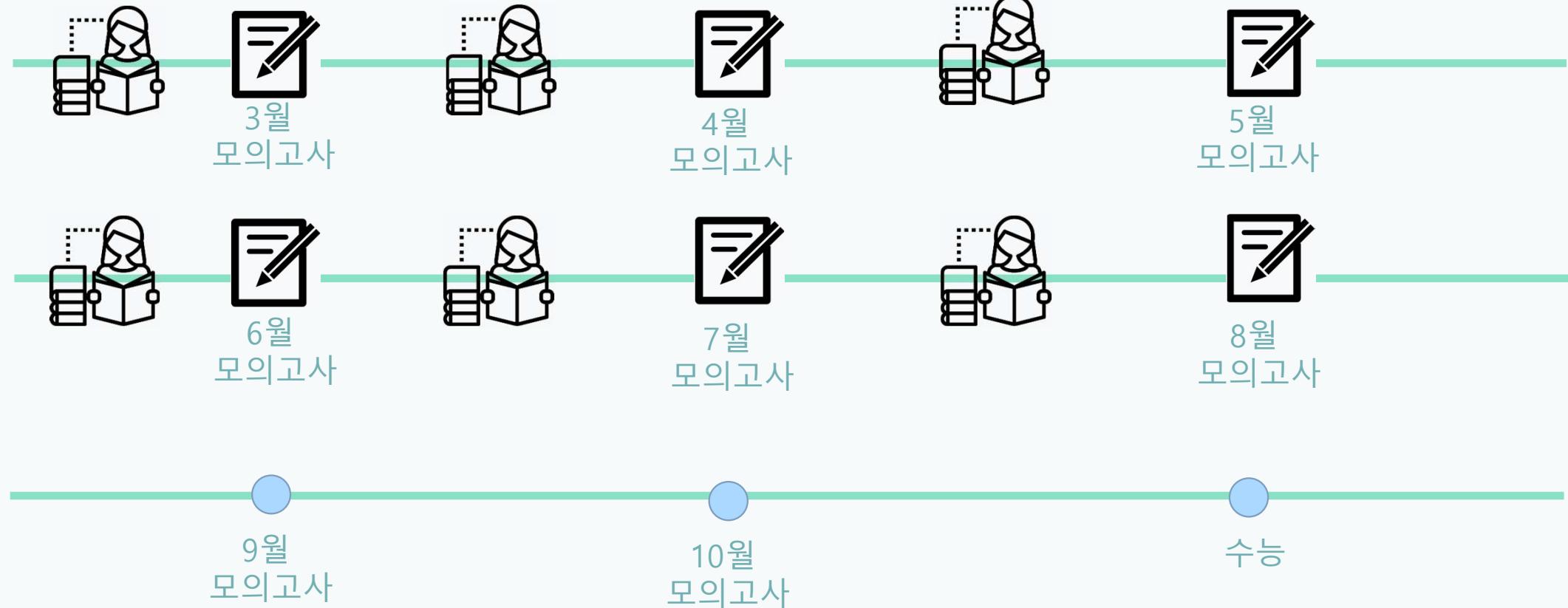
4. Neural Network 실습

Neural Network - 학습



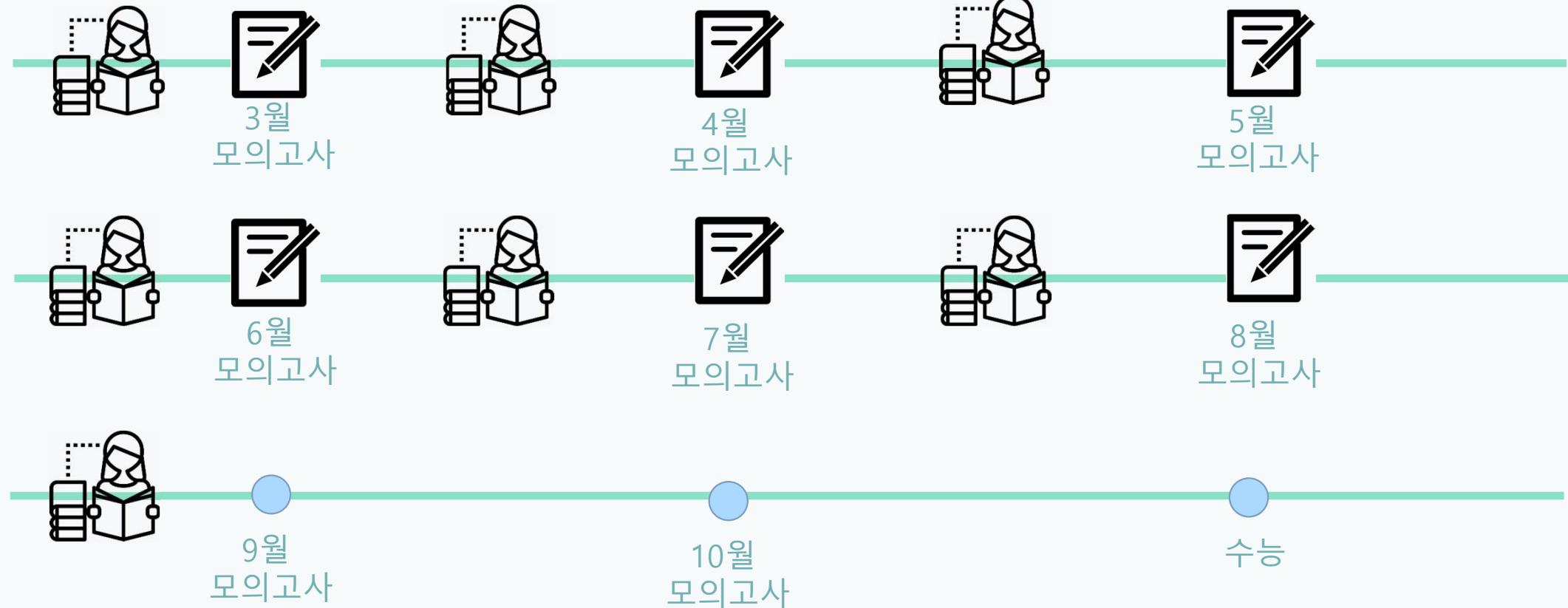
4. Neural Network 실습

Neural Network - 학습



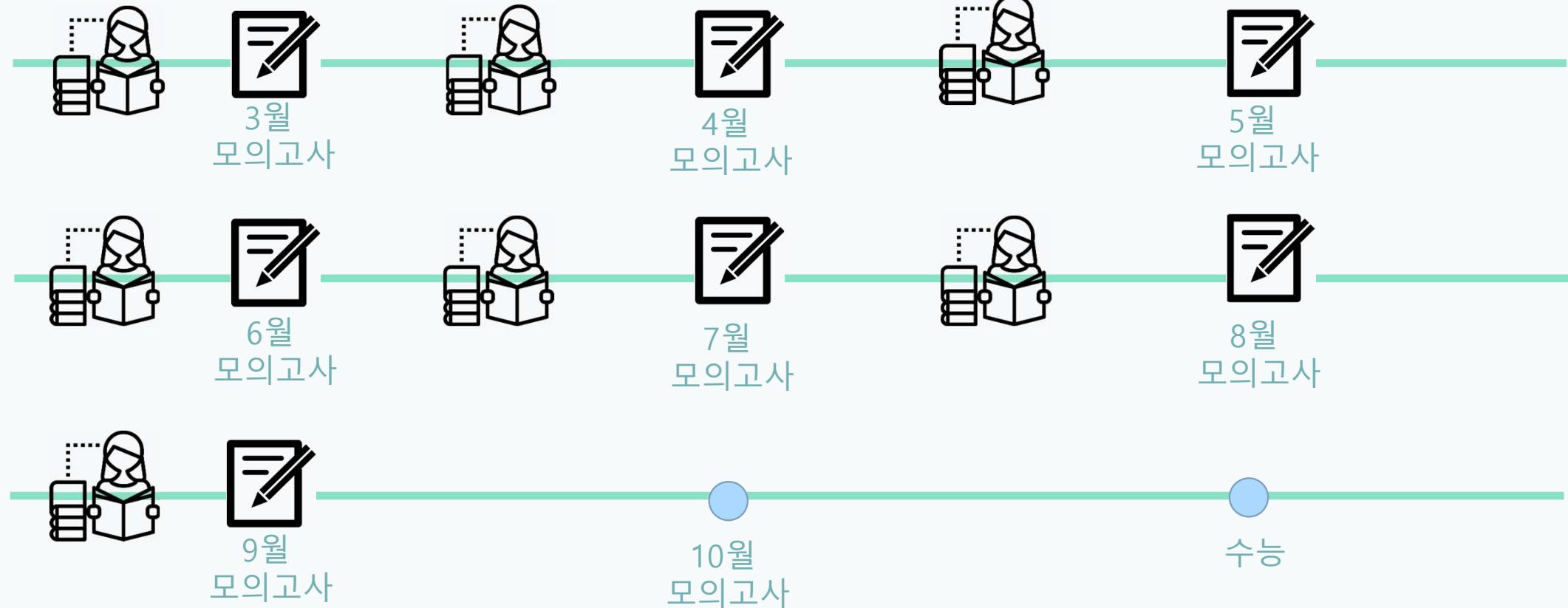
4. Neural Network 실습

Neural Network - 학습



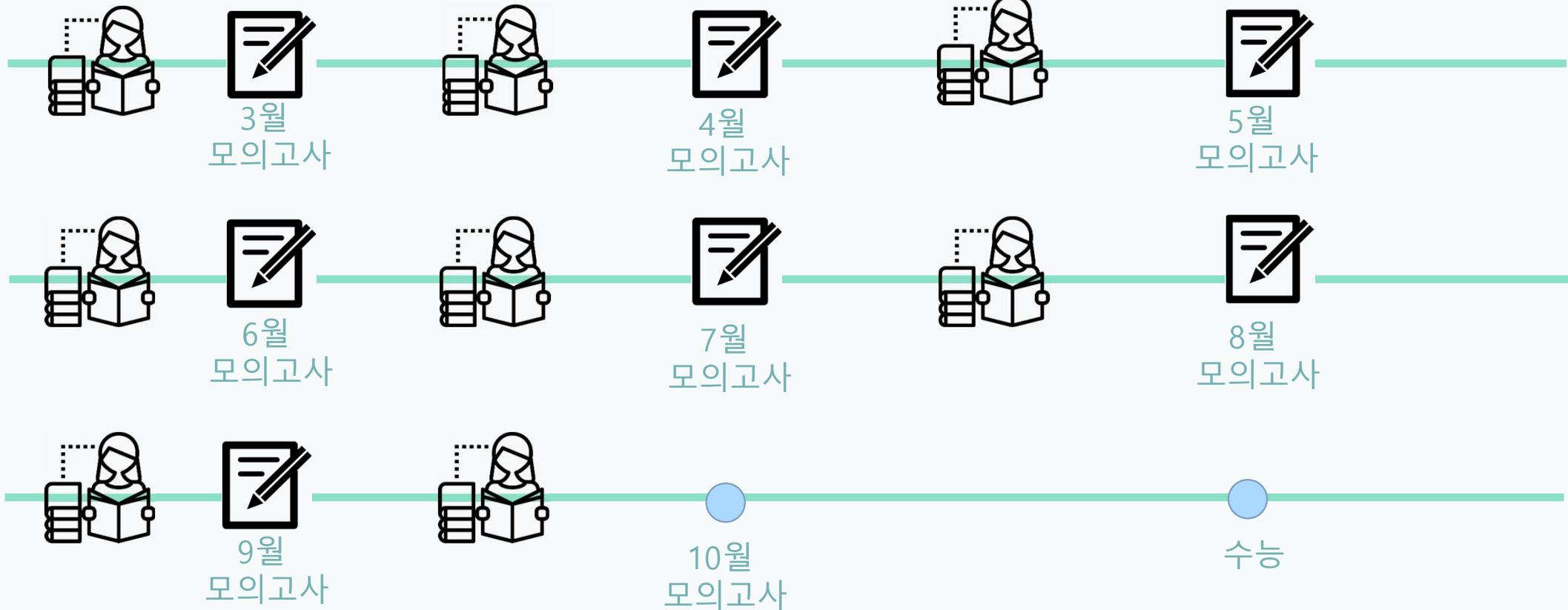
4. Neural Network 실습

Neural Network - 학습



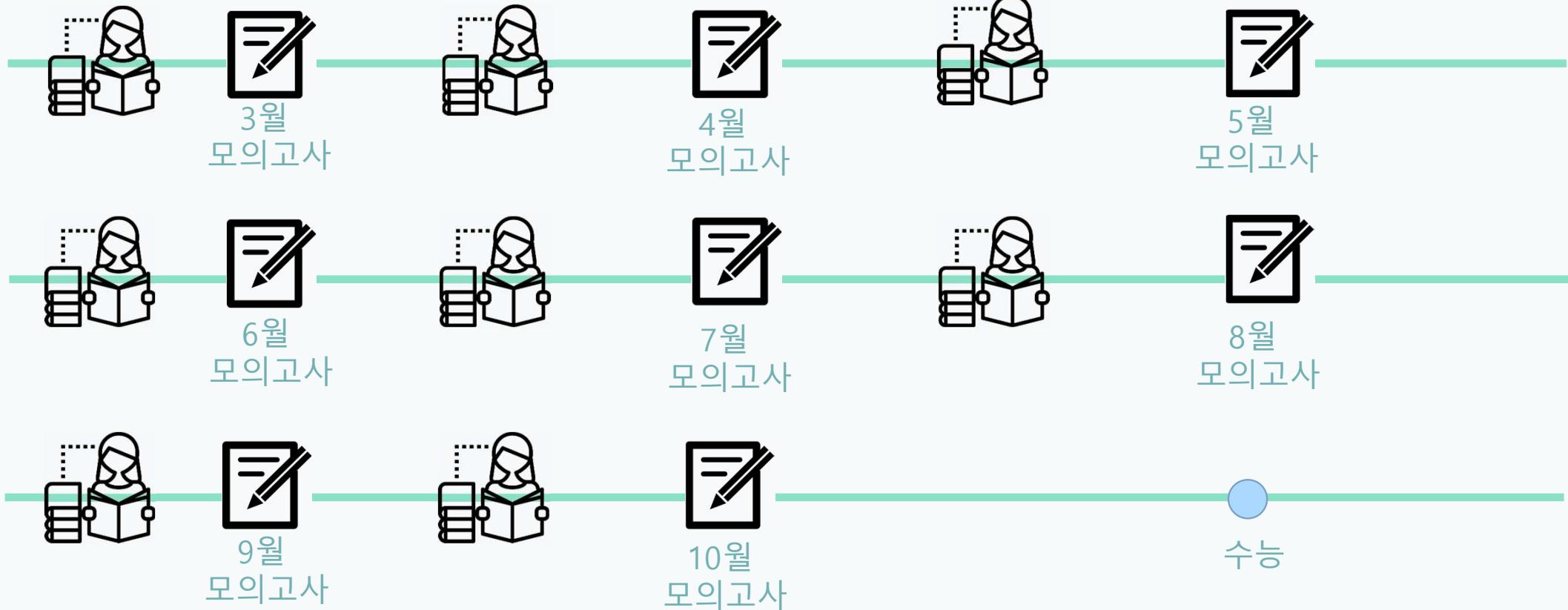
4. Neural Network 실습

Neural Network - 학습



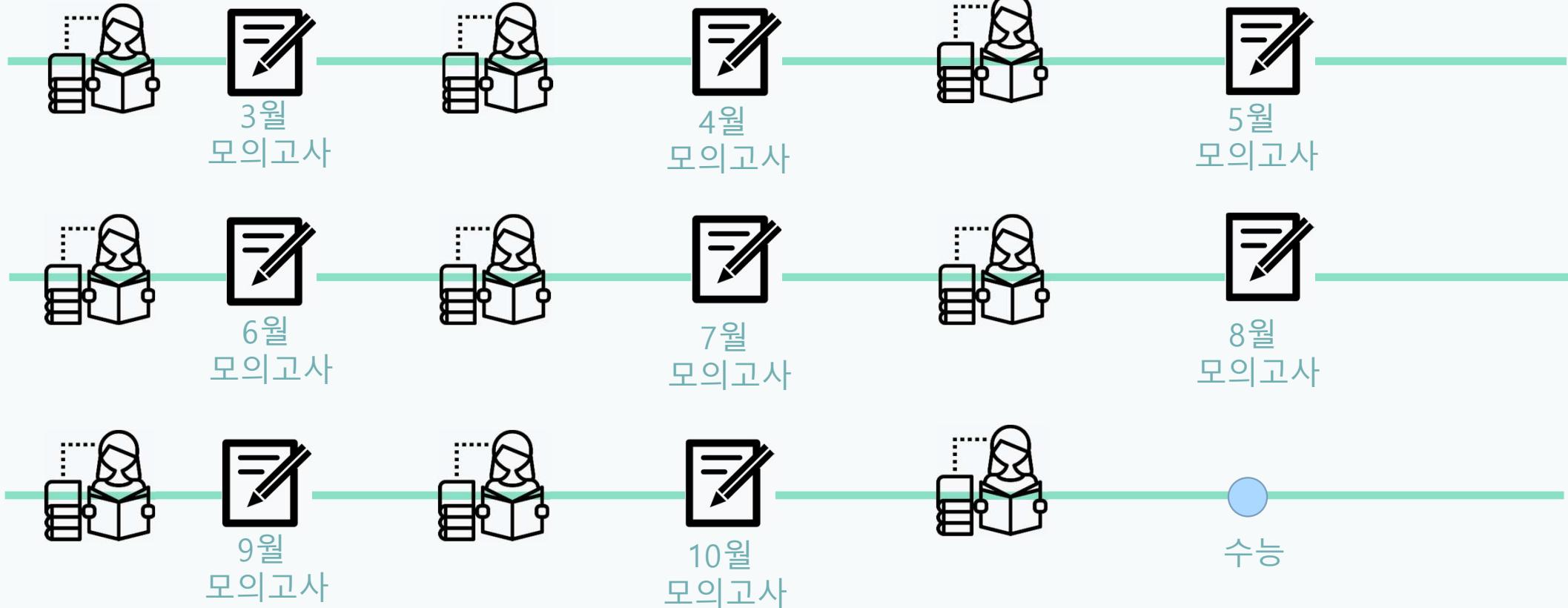
4. Neural Network 실습

Neural Network - 학습



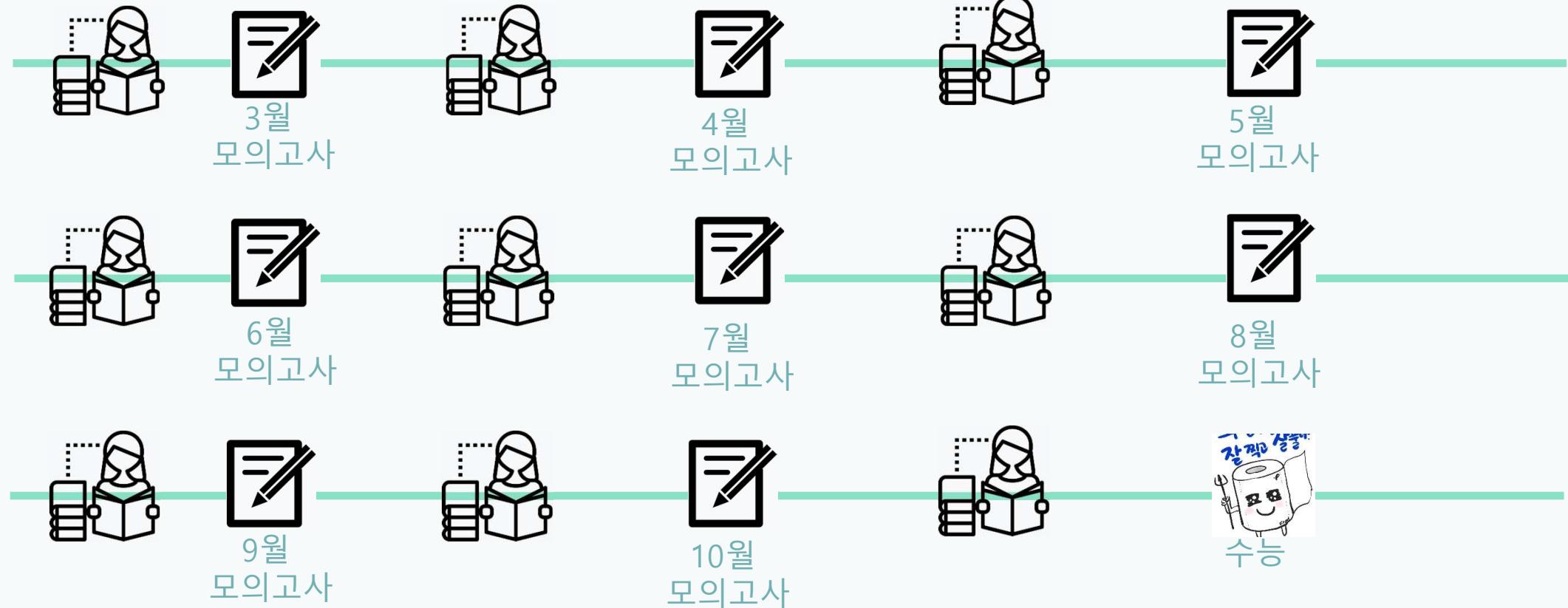
4. Neural Network 실습

Neural Network - 학습



4. Neural Network 실습

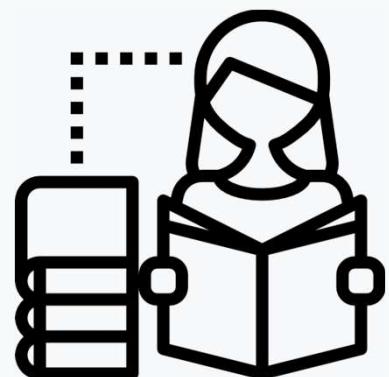
Neural Network - 학습



4. Neural Network 실습

DATA 나누기

학습
(train)



검증
(validation)



시험
(test)



4. Neural Network 실습

DATA 나누기

```
19 ## 디제이의 min, max, mean, std 구하기.
20 dataset_stats = dataset.describe()
21 dataset_stats.pop("D")
22 dataset_stats = dataset_stats.transpose()
23 |
24 train_labels = dataset.pop("D")
25
26 ## data normalization
27 def min_max_norm(x):
28     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])
29
30 def standard_norm(x):
31     return (x - dataset_stats['mean']) / dataset_stats['std']
32
33 min_max_norm_train_data = min_max_norm(dataset)
34 standard_norm_train_data = standard_norm(dataset)
35
36 print("min max : ")
37 print(min_max_norm_train_data)
38 print("standard : ")
39 print(standard_norm_train_data)
40
41 X_train1, X_test, Y_train1, Y_test = \
42     train_test_split(standard_norm_train_data, train_labels, test_size=0.2, shuffle=False)
43
44 X_train, X_val, Y_train, Y_val = \
45     train_test_split(X_train1, Y_train1, test_size=0.2, shuffle=False)
46
47 print("x train")
48 print(X_train)
49 print("label train")
50 print(Y_train)
```

data

data1

data2

data1_1

data1_2

practice : P_02_05_data_division.py

Exersice : 02_05_data_division.py

4. Neural Network 실습

DATA 나누기 적용 코드 리뷰

```
## data copy
dataset=df.copy()

## label data 추출
ori_Y = dataset.pop("house price of unit area")  
  
# train / val / test 데이터 분리
X_train1, X_test, Y_train1, Y_test = train_test_split(dataset, ori_Y, test_size=0.3, shuffle=False)
X_train, X_valid, Y_train, Y_valid = train_test_split(X_train1, Y_train1, test_size=0.2, shuffle=False)

# 모델의 설정
input_Layer = tf.keras.layers.Input(shape=(5,))
x = tf.keras.layers.Dense(50, activation='sigmoid')(input_Layer)
x= tf.keras.layers.Dense(100, activation='sigmoid')(x)
x= tf.keras.layers.Dense(300, activation='sigmoid')(x)
Out_Layer= tf.keras.layers.Dense(1, activation=None)(x)

model = tf.keras.Model(inputs=[input_Layer], outputs=[Out_Layer])
model.summary()  
  
loss=tf.keras.losses.mean_squared_error
optimizer=tf.keras.optimizers.SGD(lr=0.00004)
metrics = tf.keras.metrics.mean_squared_error ## regression으로 평가 지표는 MSE가 된다.
model.compile(loss=loss,
              optimizer=optimizer,
              metrics=[metrics])  
  
result=model.fit(X_train, Y_train, epochs=2000, batch_size=100, validation_data=(X_valid,Y_valid))
```

평가할 때 테스트 데이터

모델 만들기

학습하기

검증 데이터 넣기

학습 데이터 넣기

practice : P_02_06_house_price_of_area_prediction_data_div.py

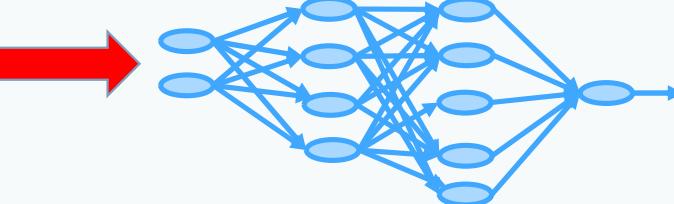
462

4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)

{	1	1	1	1	1	}
{	1	1	1	1	1	}
{	1	1	1	1	1	}
{	1	1	1	1	1	}



에러 계산해서
모델 업데이트

VALIDATION DATA(BATCH SIZE 2)

{	1	1	1	1	1	}
{	1	1	1	1	1	}

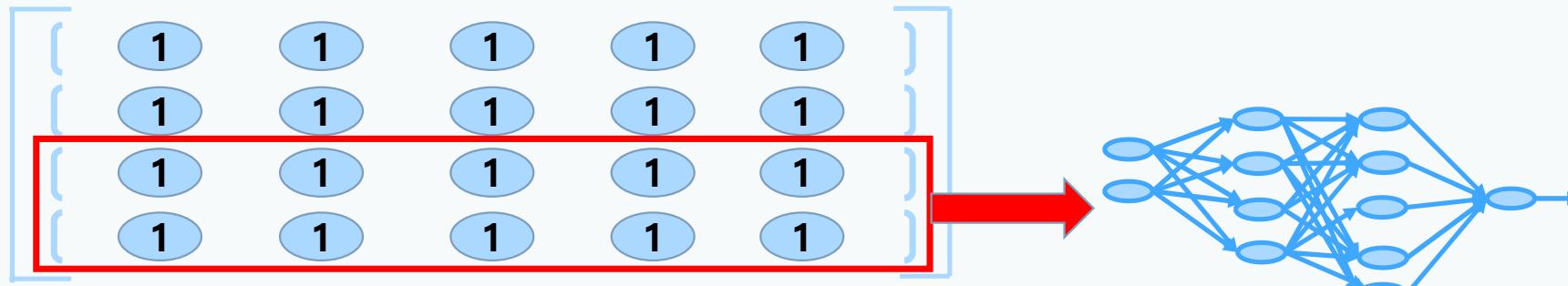
TEST DATA

{	1	1	1	1	1	}
{	1	1	1	1	1	}

4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)



예러 계산해서
모델 업데이트

VALIDATION DATA(BATCH SIZE 2)



TEST DATA



4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

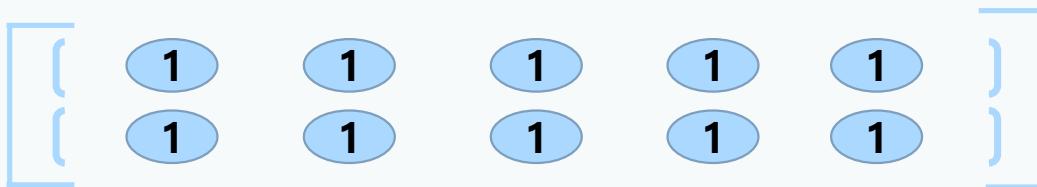
TRAIN DATA (BATCH SIZE 2)



VALIDATION DATA(BATCH SIZE 2)



TEST DATA



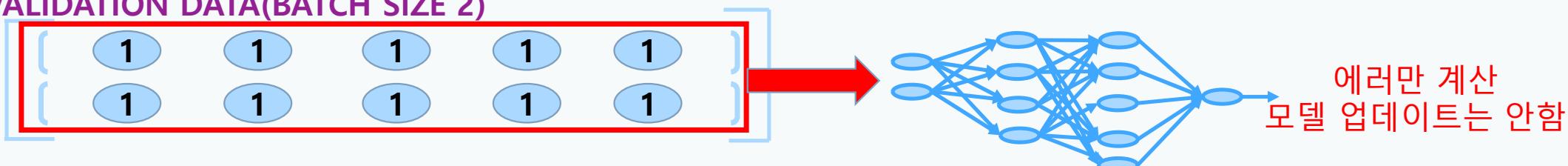
4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)



VALIDATION DATA(BATCH SIZE 2)



TEST DATA

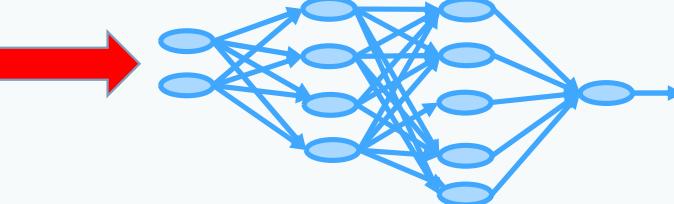


4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)

{	1	1	1	1	1	}
{	1	1	1	1	1	}
{	1	1	1	1	1	}
{	1	1	1	1	1	}



에러 계산해서
모델 업데이트

VALIDATION DATA(BATCH SIZE 2)

{	1	1	1	1	1	}
{	1	1	1	1	1	}

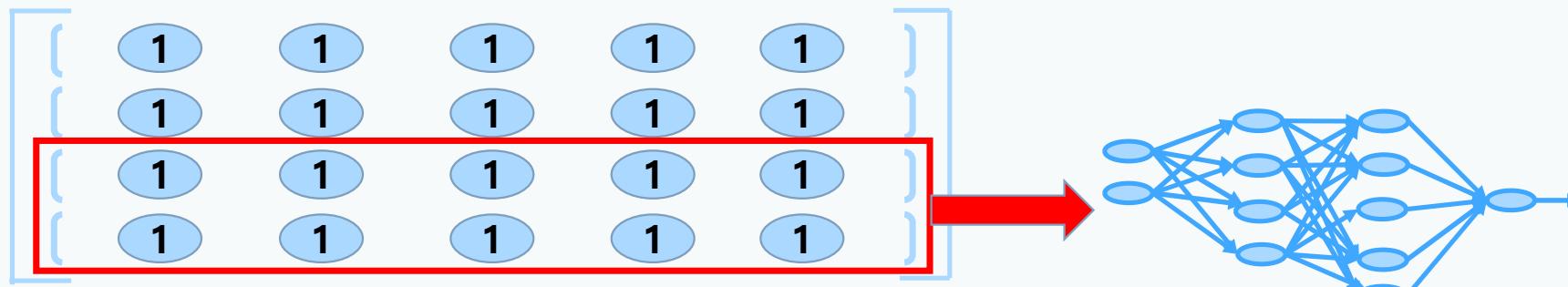
TEST DATA

{	1	1	1	1	1	}
{	1	1	1	1	1	}

4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)



예러 계산해서
모델 업데이트

VALIDATION DATA(BATCH SIZE 2)



TEST DATA



4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)



VALIDATION DATA(BATCH SIZE 2)



TEST DATA



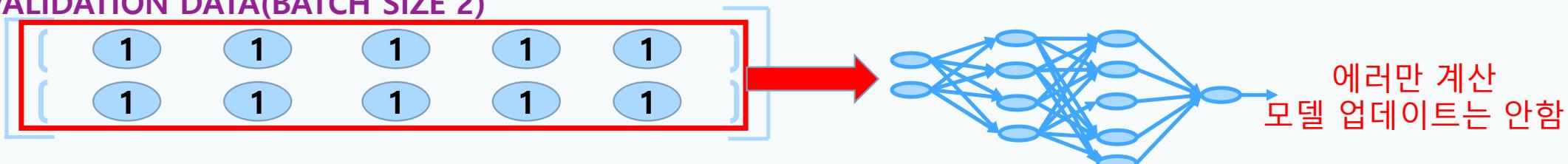
4. Neural Network 실습

데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)



VALIDATION DATA(BATCH SIZE 2)



TEST DATA



4. Neural Network 실습

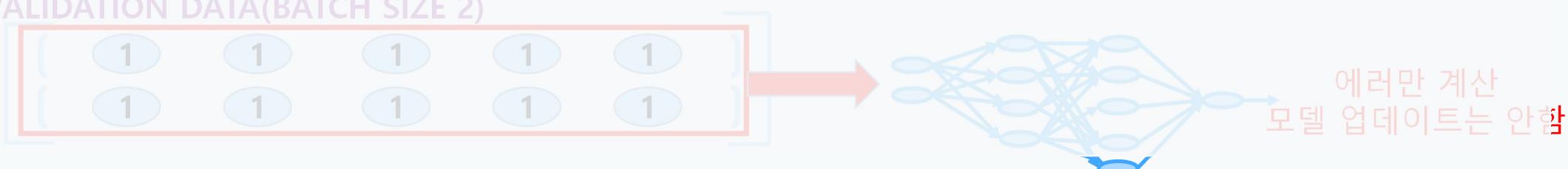
데이터 분리 학습 과정 살펴보기

TRAIN DATA (BATCH SIZE 2)



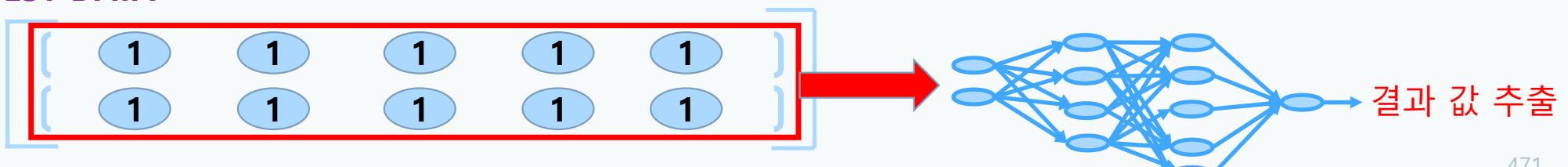
에러 계산해서
모델 업데이트

VALIDATION DATA(BATCH SIZE 2)



에러만 계산
모델 업데이트는 안함

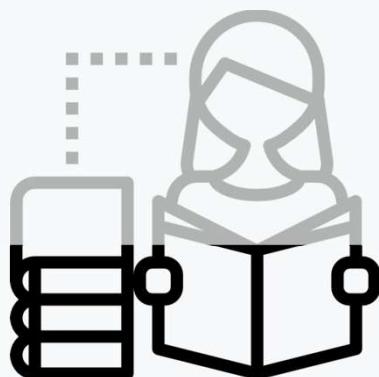
TEST DATA



4. Neural Network 실습

DATA 나누기 적용

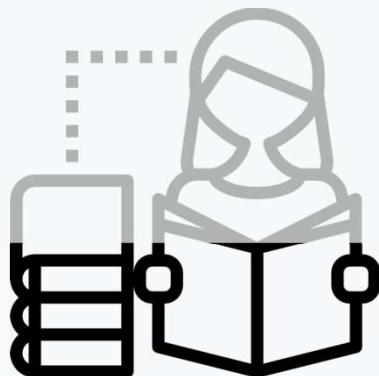
보스턴 집값 예측 모델에 적용하기!



4. Neural Network 실습

DATA 나누기 적용+Normalization

지역 집 값 예측 모델에 적용하기!



practice : P_02_07_house_price_of_area_prediction_data_div_with_normal.py

4. Neural Network 실습

DATA 나누기 + Normalization 적용 코드 리뷰

```
11 ## 데이터 읽어오기.## 데이터 읽어오기.  
12 raw_df = pd.read_csv("../dataset/house_price_of_unit_area.csv")  
13 print(raw_df.info())  
14 print(raw_df.head())  
15 dataset=raw_df.copy()  
16  
17 ## data 불교드 확인  
18 sns.pairplot(dataset[["house price", "bedrooms", "bathrooms", "sqft_living", "sqft_lot", "floors", "waterfront", "view", "condition", "grade", "price"]])  
19 plt.show()  
20  
21 ## 데이터 열 별로 min, max, mean, std 구하기.  
22 dataset_stats = dataset.describe()  
23 dataset_stats.pop("house price of unit area")  
24 dataset_stats = dataset_stats.transpose()  
25 label_data=dataset.pop("house price of unit area")
```

DATA NORMALIZATION을 위한 파라미터 구하기

```
50 loss=tf.keras.losses.mse  
51 optimizer=tf.keras.optimizers.SGD(lr=0.002)  
52 ## regression이므로 평가 지표는 MSE가 된다.  
53 model.compile(loss=loss,  
54                 optimizer=optimizer,  
55                 metrics=[tf.keras.metrics.mean_squared_error])  
56  
57 history=model.fit(X_train, Y_train, epochs=1000, batch_size=100, validation_data=(X_valid,Y_valid))
```

학습하기

학습 데이터 넣기

검증 데이터 넣기

DATA NORMALIZATION

```
27 ## data normalization  
28 def min_max_norm(x):  
29     return (x - dataset_stats['min']) / (dataset_stats['max'] - dataset_stats['min'])  
30  
31 def standard_norm(x):  
32     return (x - dataset_stats['mean']) / dataset_stats['std']  
33  
34 normed_train_data = standard_norm(dataset)
```

DATA를 TRAIN, VALIDATION, TEST로 나누기

```
36 # 전체 데이터에서 학습 데이터와 테스트 데이터를 나누기.  
37 X_train1, X_test, Y_train1, Y_test = train_test_split(normed_train_data, label_data, test_size=0.1)  
38 X_train, X_valid, Y_train, Y_valid = train_test_split(X_train1, Y_train1, test_size=0.1)
```

모델 만들기

```
40 # 모델의 설정  
41 input_layer = tf.keras.layers.Input(shape=(5,))  
42 x = tf.keras.layers.Dense(100, activation='sigmoid')(input_layer)  
43 x= tf.keras.layers.Dense(150, activation='sigmoid')(x)  
44 x= tf.keras.layers.Dense(100, activation='sigmoid')(x)  
45 Out_Layer= tf.keras.layers.Dense(1, activation=None)(x)  
46  
47 model = tf.keras.Model(inputs=[input_layer], outputs=[Out_Layer])  
48 model.summary()
```

평가할 때 테스트 데이터

```
print("\n Test rmse: %.4f" % (model.evaluate(normed_test_data, Y_test)[1]))
```

10샘플 데이터를 넣어서 예측값을 출력하여 정답값과 비교

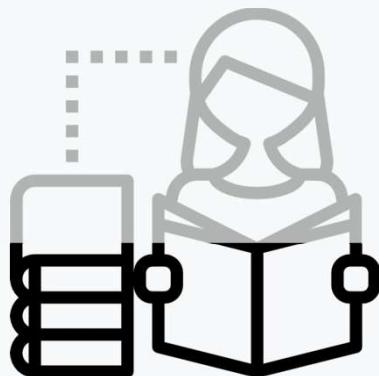
```
for i in range(10):  
    input_test_data=np.expand_dims(normed_test_data.values[i][:], axis=0)  
    print("true : ", Y_test.values[i], "prediction: ", model.predict(input_test_data))
```

값 예측할 때 테스트 데이터

4. Neural Network 실습

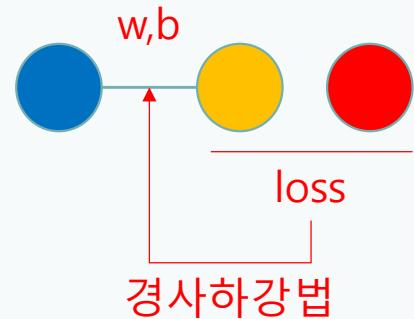
DATA 나누기 적용+Normalization

보스턴 집값 예측 모델에 적용하기!

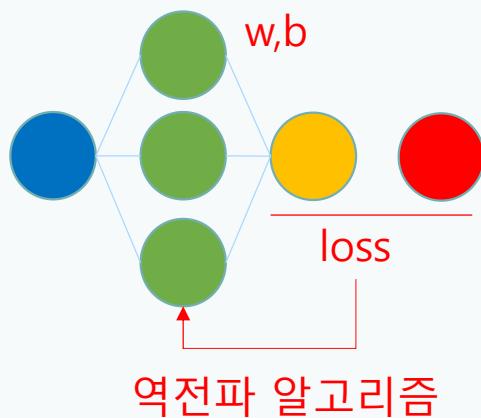


5. Summary

perceptron



Neural Network



Loss

- MSE : Regression
- Cross Entropy : Logistic Regression(binary classification)

Data

- 현실과 유사한 형태, 분포도를 가진 데이터 구축이 필요
- 데이터 구축 시 학습/검증/테스트 데이터로 나누어 개발
- 데이터에서 normalization을 통해 성능 향상 할 수도 있음.

Neural Network

- Input Layer : Data input
- Hidden Layer : Data representation
- Output Layer : Output (즉, loss에 따라 task(출력)을 정함)

역전파 알고리즘

- 경사하강법 처럼 미분을 통해 Δ_w , Δ_b 의 값을 구하는데 chain rule을 통해서 계산

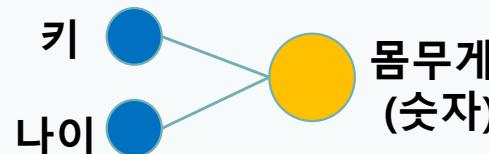
5. Summary

1. Linear Regression



$$\mathcal{L}_{mse} = \frac{1}{n} \sum_{i=1}^n (H(x_i) - y_i)^2$$

2. Multi-variable Linear Regression



$$\mathcal{L}_{mse} = \frac{1}{n} \sum_{i=1}^n (H(x_i) - y_i)^2$$

3. Logistic Regression(Classification)

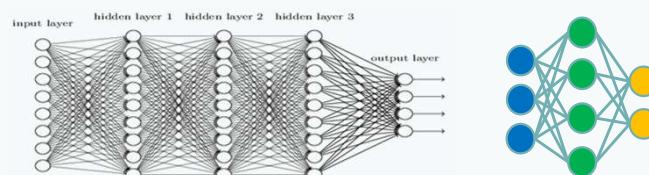


$$Cost(h_\theta(x), y) = \begin{cases} -\log(h_\theta(x)) & \text{if } y = 1 \\ -\log(1 - h_\theta(x)) & \text{if } y = 0 \end{cases}$$

4. Softmax Classifier



5. Neural Network (Deep Learning)



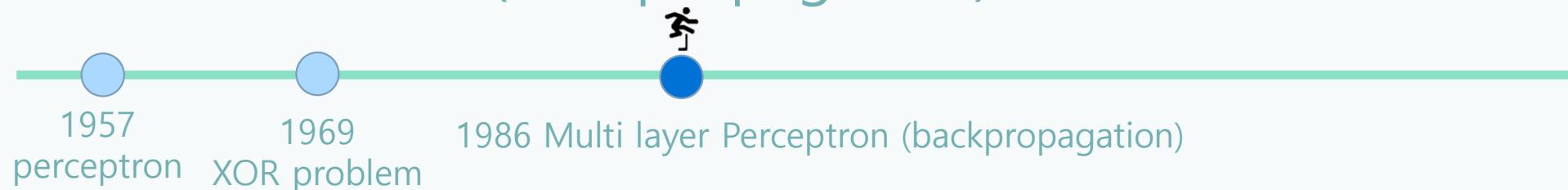
오늘 하루 고생 하셨습니다.
Q & A

참 고 자 료

- cs231n 강의
- 모두의 딥러닝 시즌 2
- 밑바닥 부터 시작하는 딥러닝 1, 2

Appendix. BACKPROPAGATION

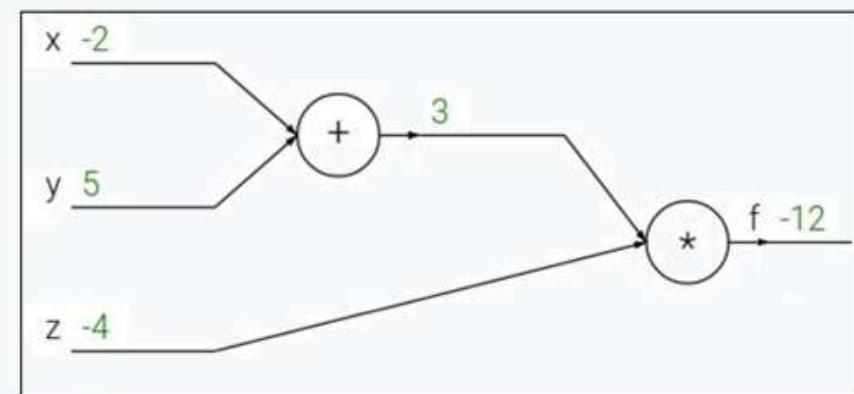
- 역전파 알고리즘(Backpropagation)



Backpropagation: a simple example

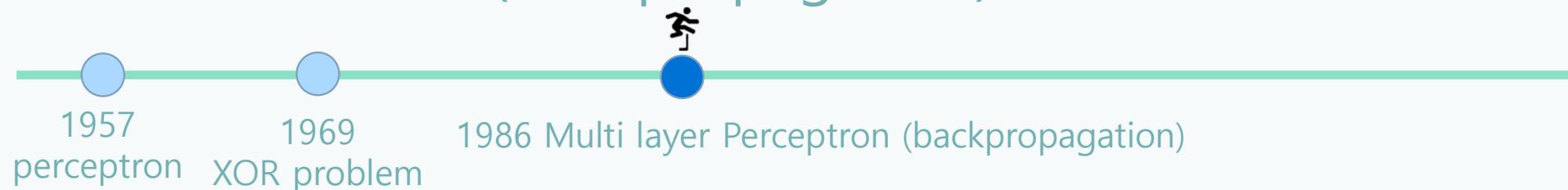
$$f(x, y, z) = (x + y)z$$

e.g. $x = -2$, $y = 5$, $z = -4$



Appendix. BACKPROPAGATION

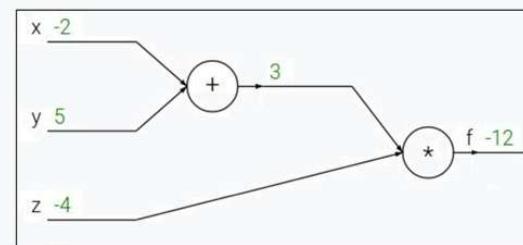
- 역전파 알고리즘(Backpropagation)



Backpropagation: a simple example

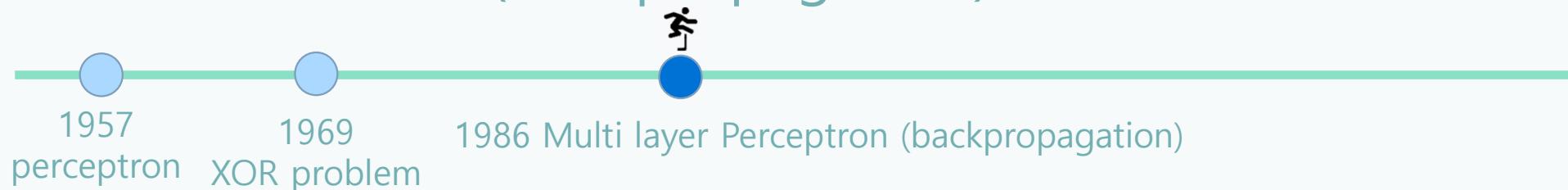
$$f(x, y, z) = (x + y)z$$

e.g. $x = -2, y = 5, z = -4$



Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



Backpropagation: a simple example

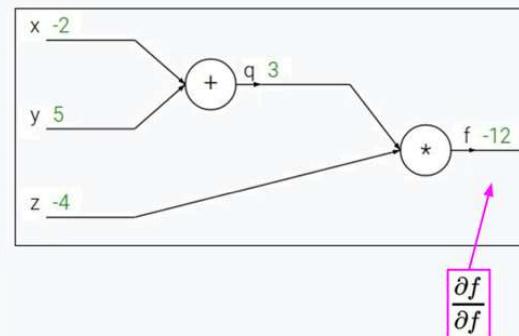
$$f(x, y, z) = (x + y)z$$

e.g. $x = -2, y = 5, z = -4$

$$q = x + y \quad \frac{\partial q}{\partial x} = 1, \frac{\partial q}{\partial y} = 1$$

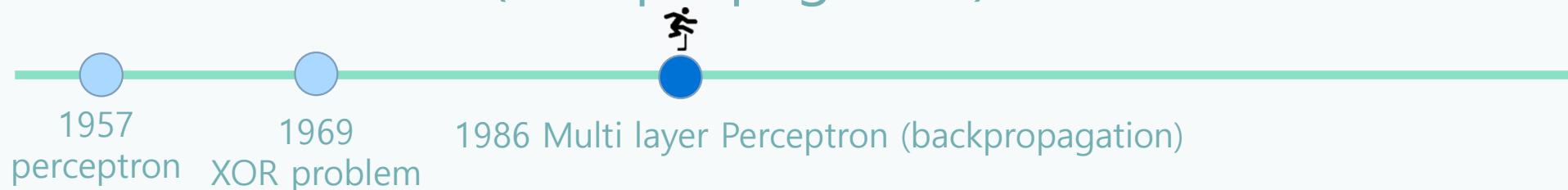
$$f = qz \quad \frac{\partial f}{\partial q} = z, \frac{\partial f}{\partial z} = q$$

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$



Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



Backpropagation: a simple example

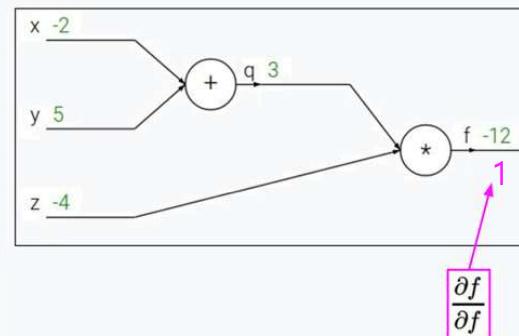
$$f(x, y, z) = (x + y)z$$

e.g. $x = -2, y = 5, z = -4$

$$q = x + y \quad \frac{\partial q}{\partial x} = 1, \frac{\partial q}{\partial y} = 1$$

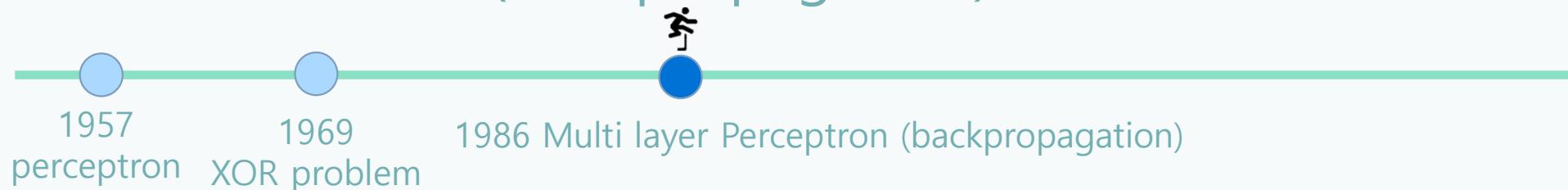
$$f = qz \quad \frac{\partial f}{\partial q} = z, \frac{\partial f}{\partial z} = q$$

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$



Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



Backpropagation: a simple example

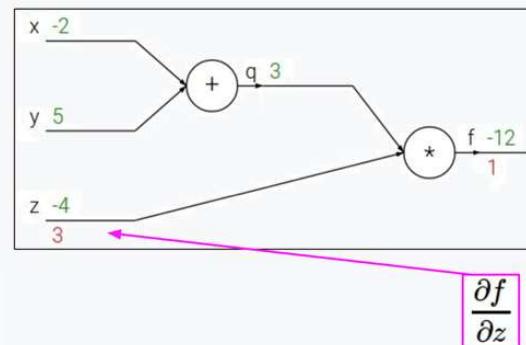
$$f(x, y, z) = (x + y)z$$

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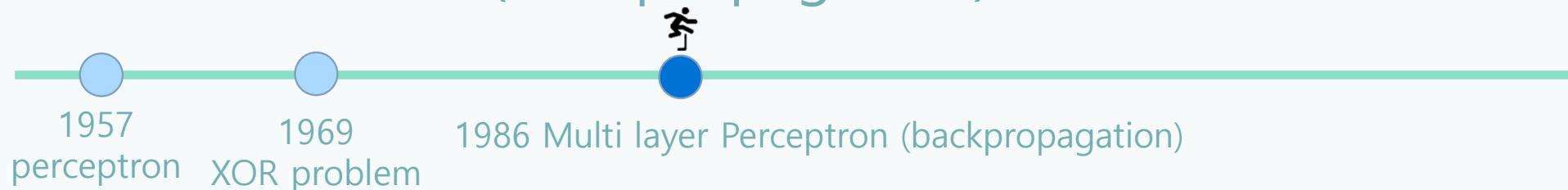
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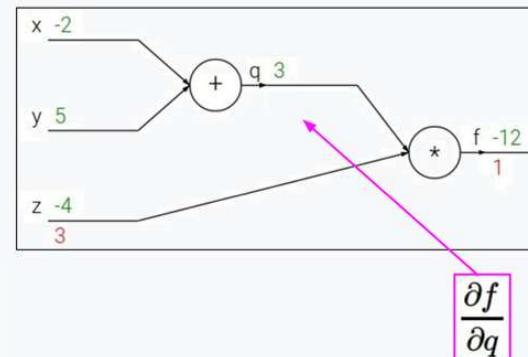
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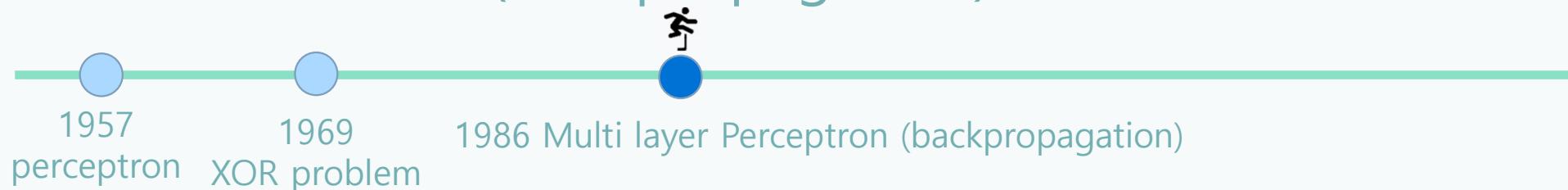
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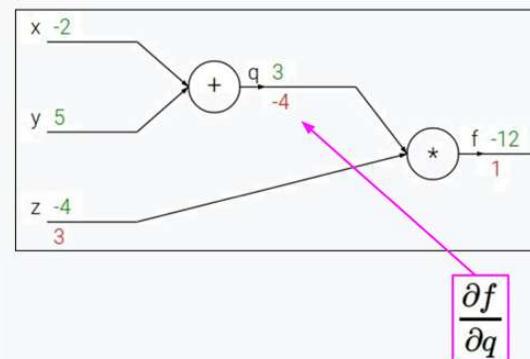
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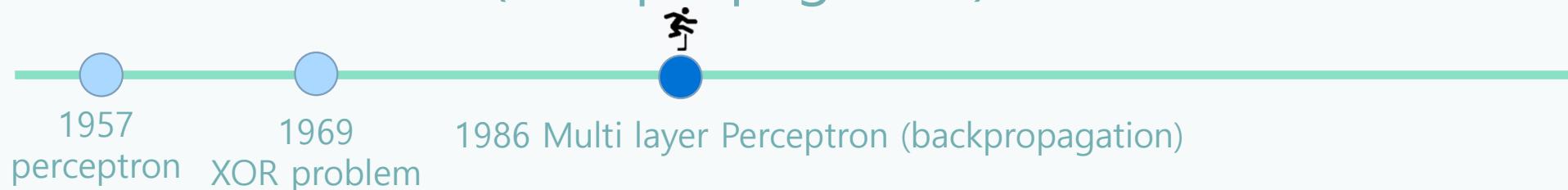
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Appendix. BACKPROPAGATION

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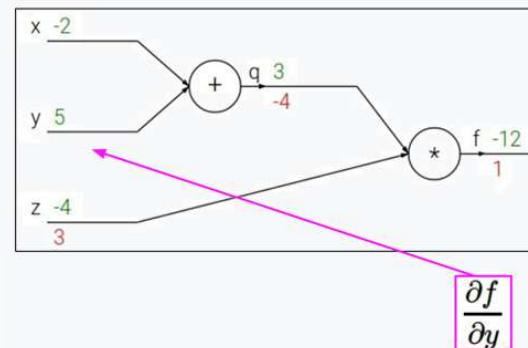
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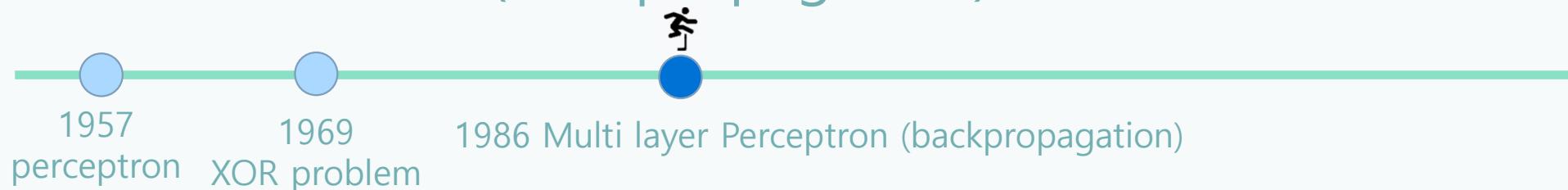
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Appendix. BACKPROPAGATION

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Backpropagation: a simple example

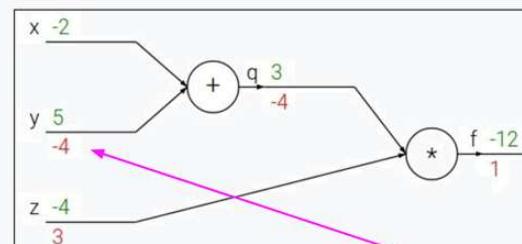
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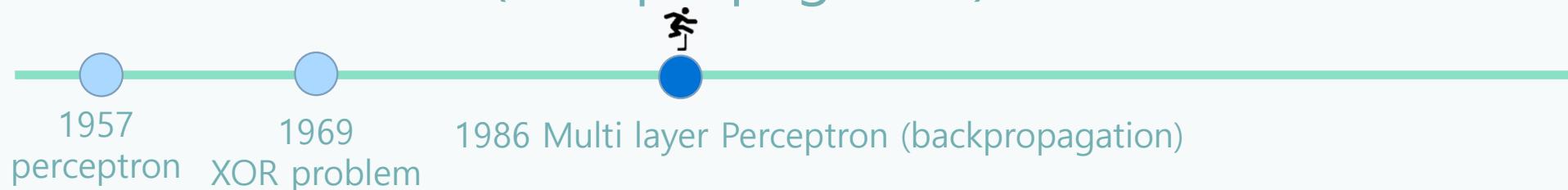
Chain rule:

$$\frac{\partial f}{\partial y} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial y}$$

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Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



Backpropagation: a simple example

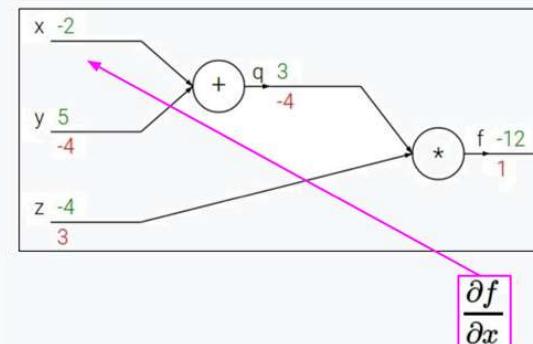
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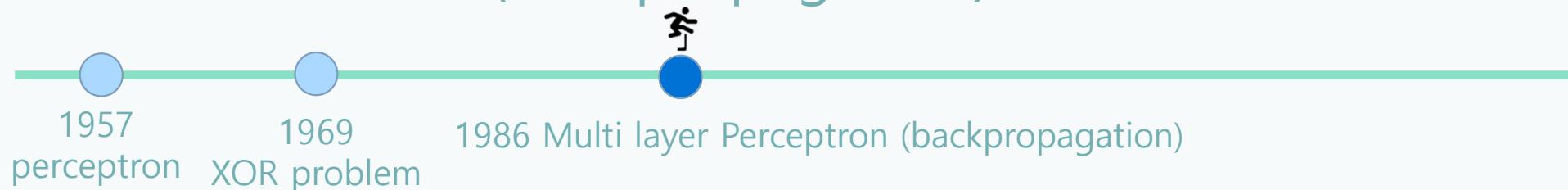
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Appendix. BACKPROPAGATION

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Backpropagation: a simple example

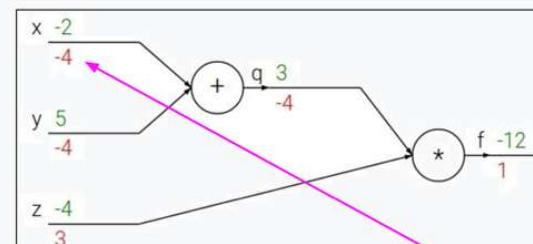
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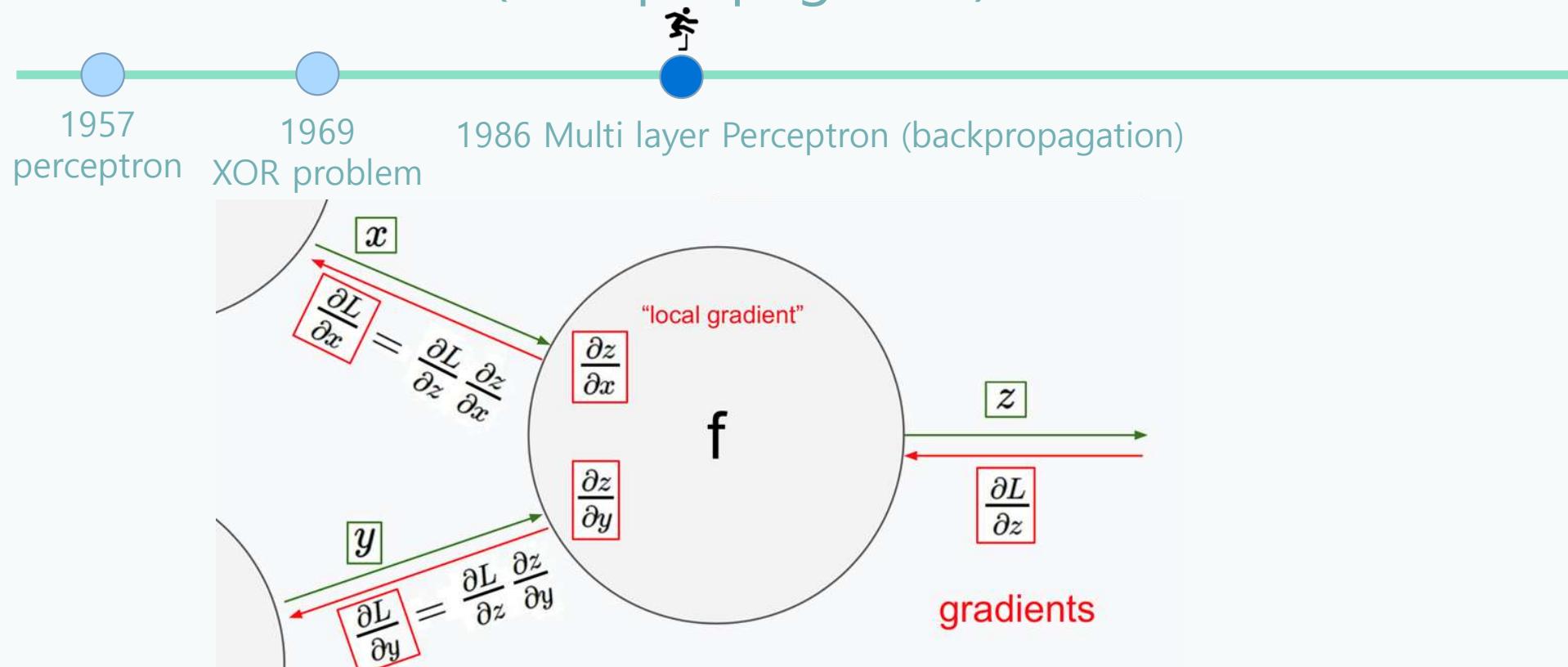
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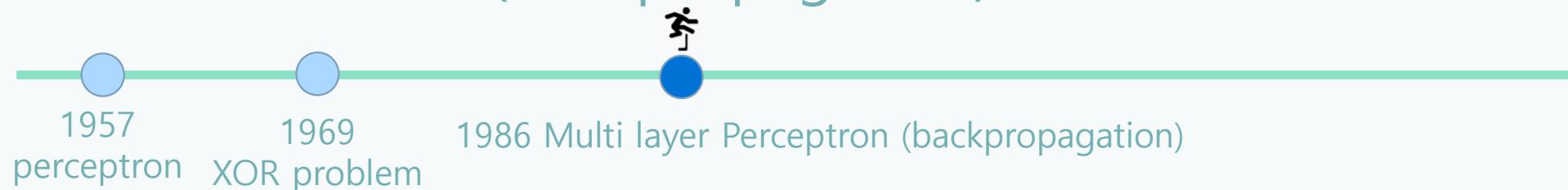
Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



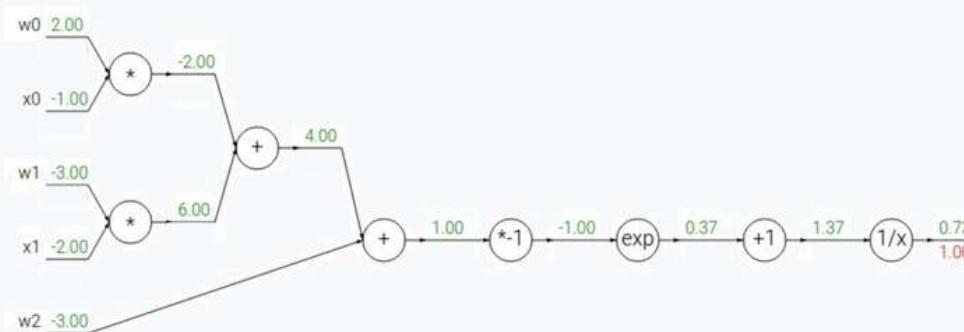
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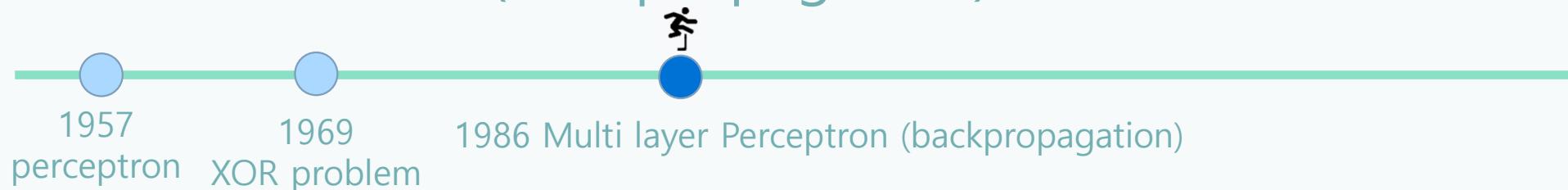
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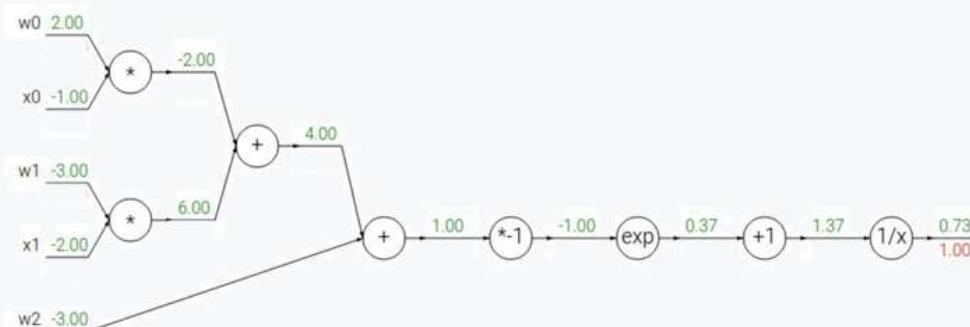
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- 역전파 알고리즘(Backpropagation)



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$$f(w, x) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + w_2)}}$$



$$f(x) = e^x$$

→

$$\frac{df}{dx} = e^x$$

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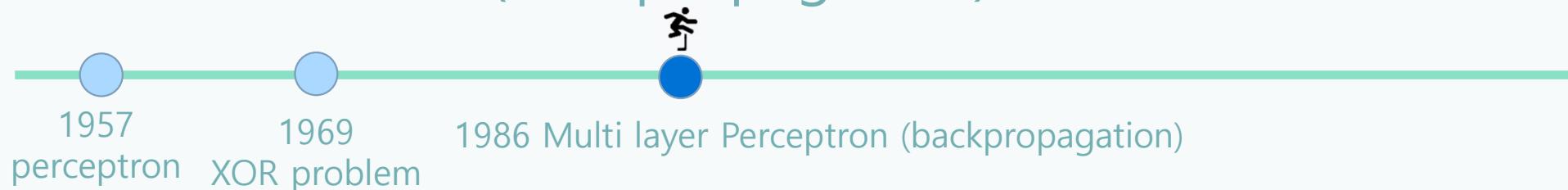
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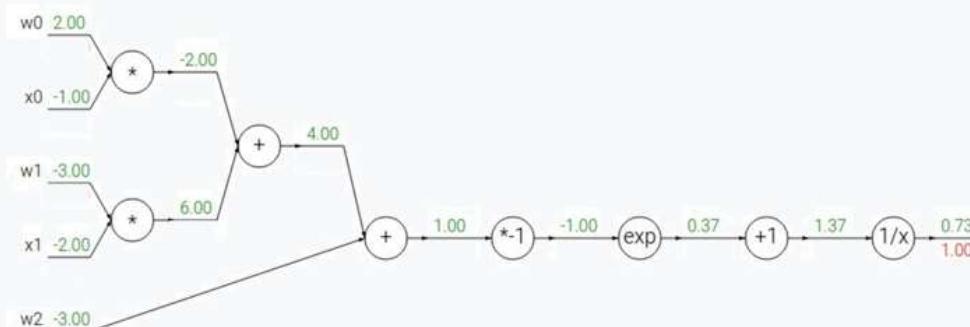
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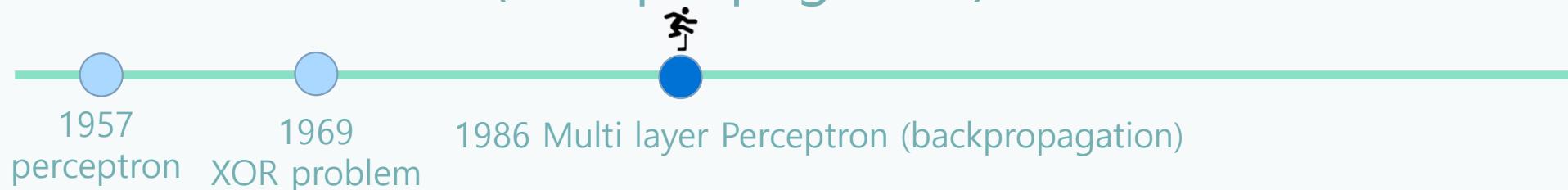
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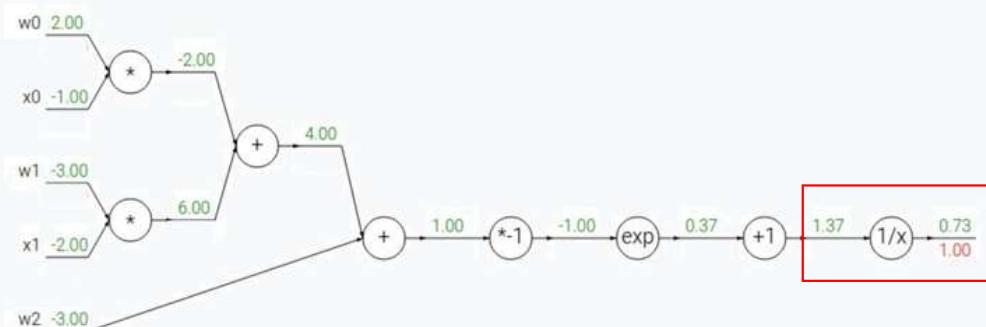
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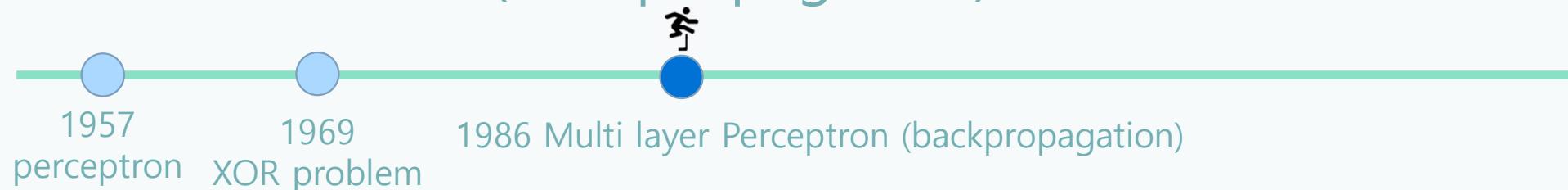
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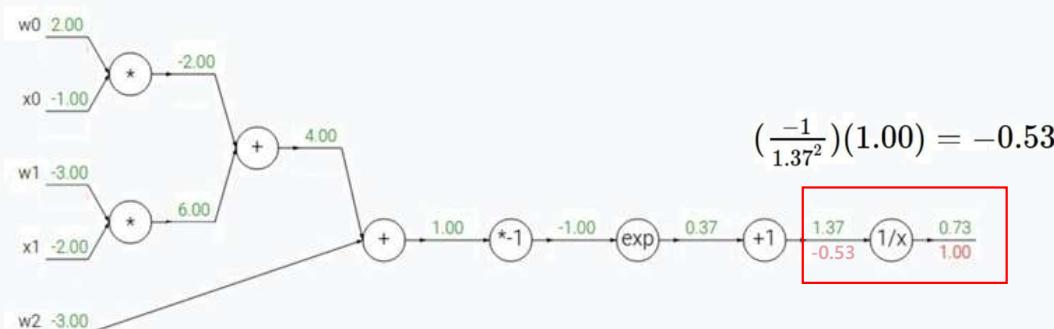
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Appendix. BACKPROPAGATION

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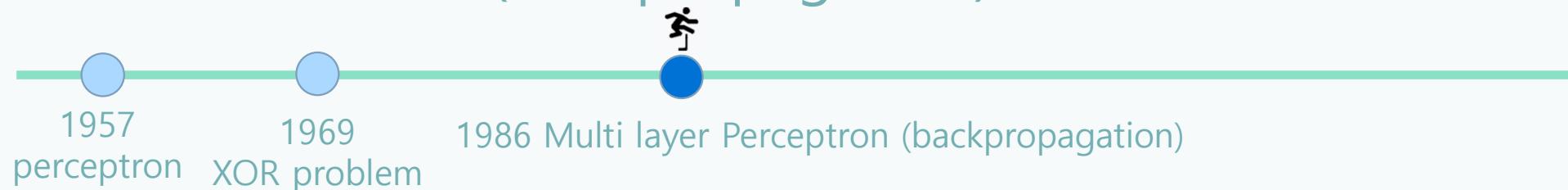
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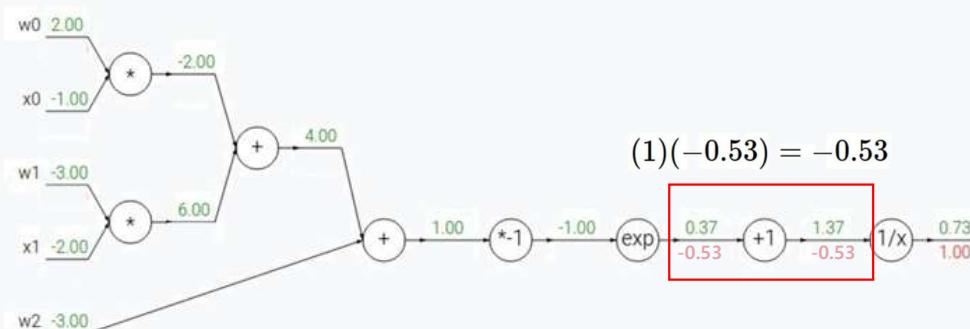
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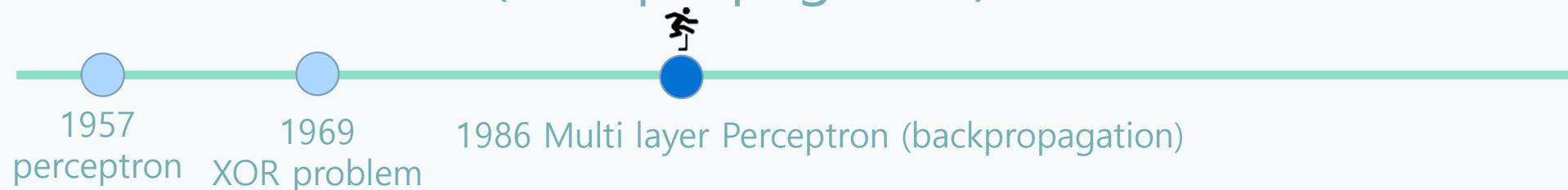
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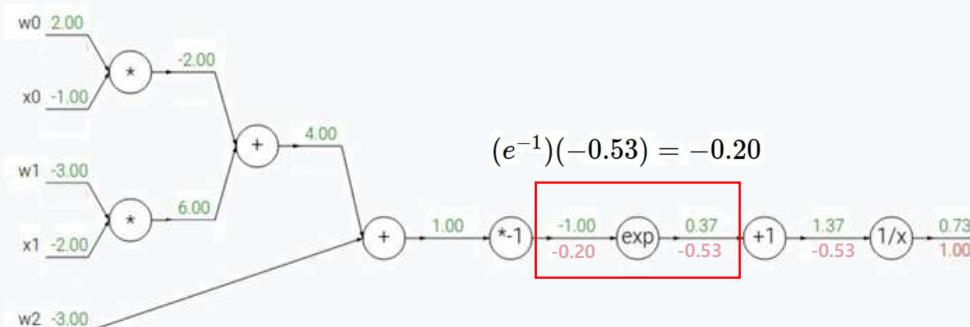
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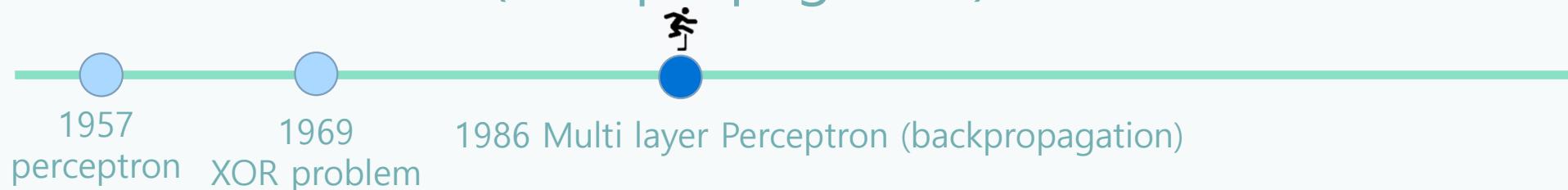
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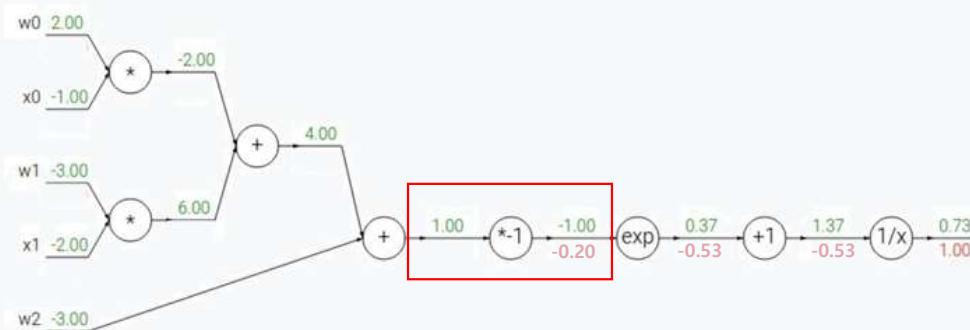
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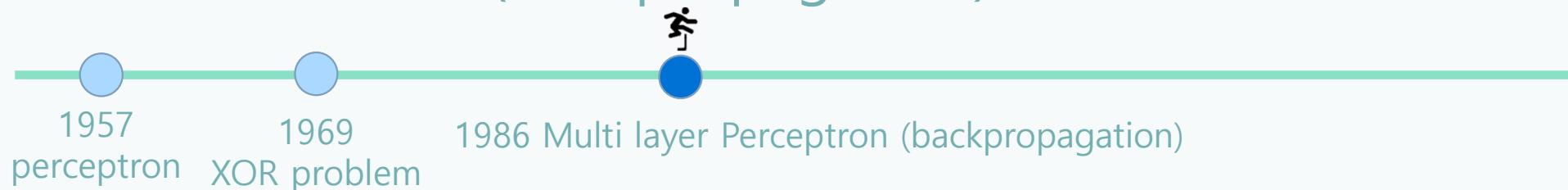
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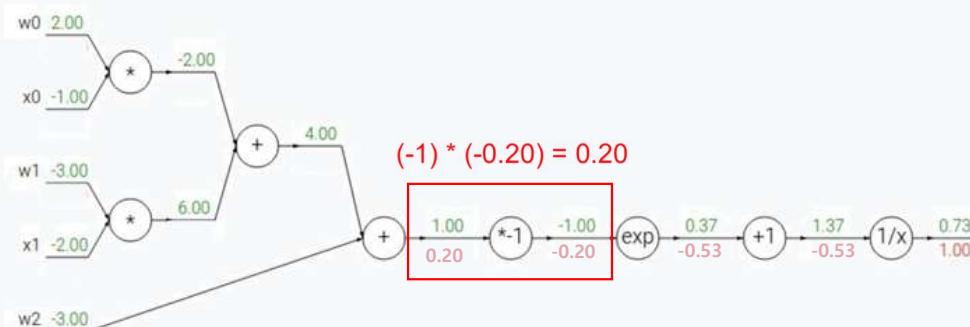
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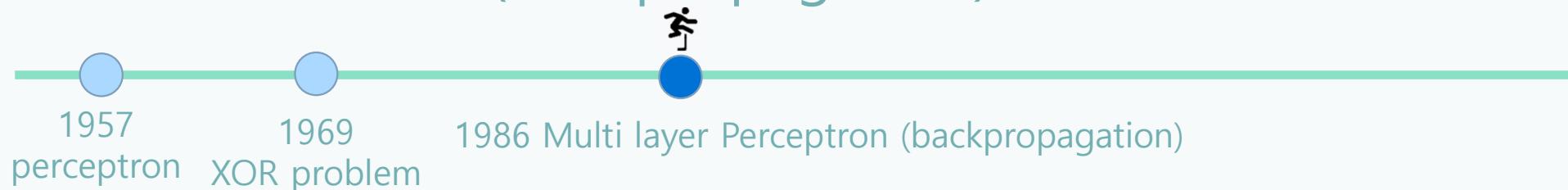
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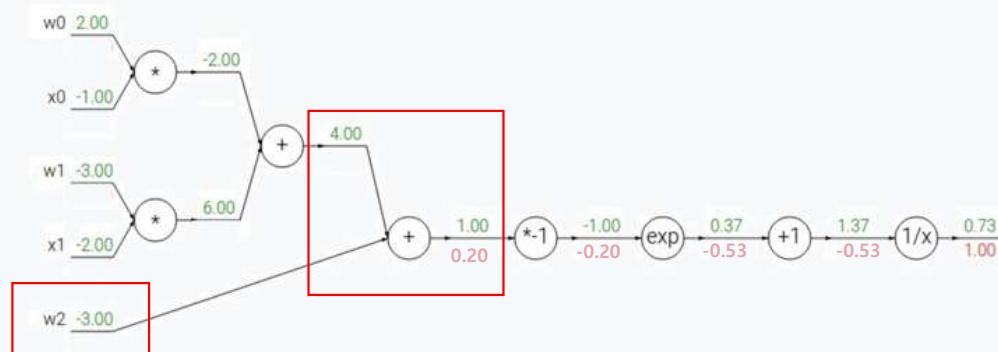
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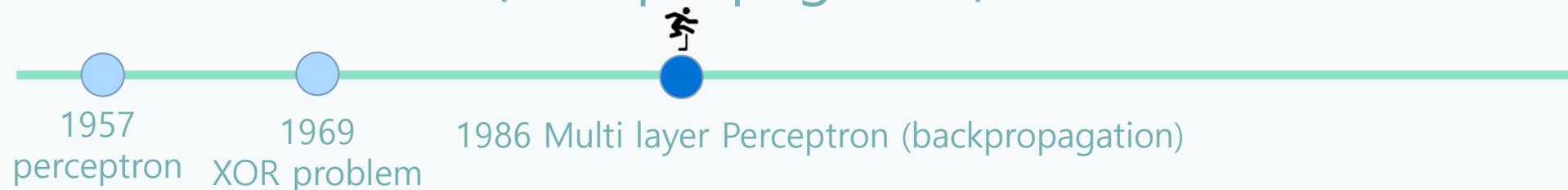
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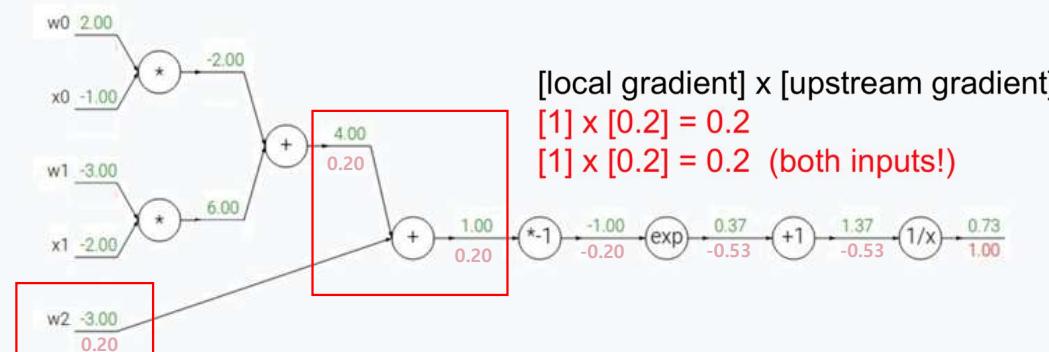
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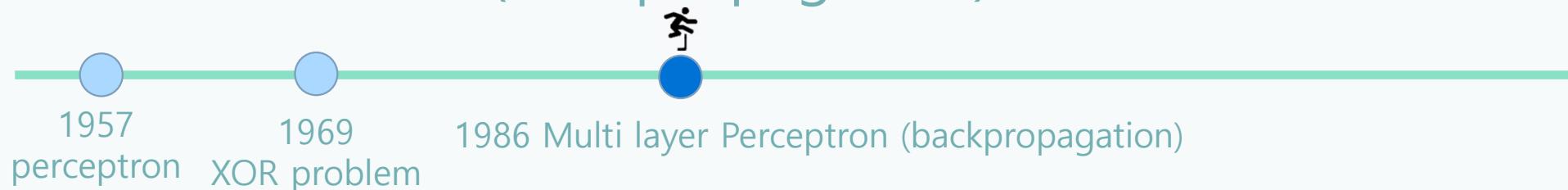
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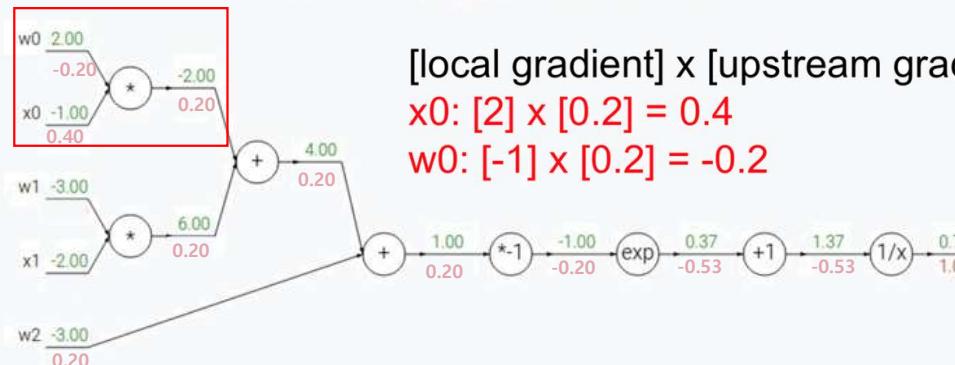
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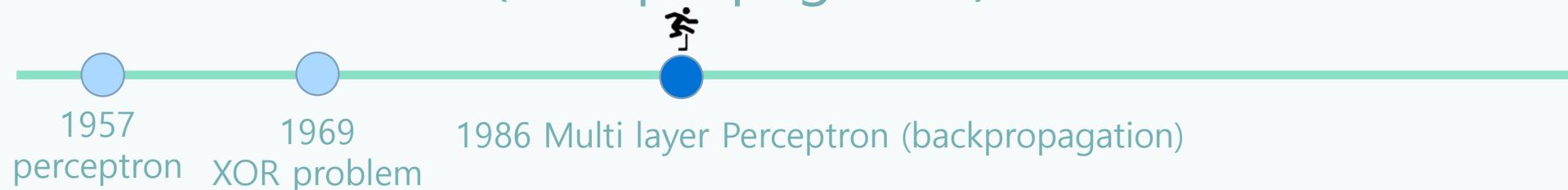
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Appendix. BACKPROPAGATION

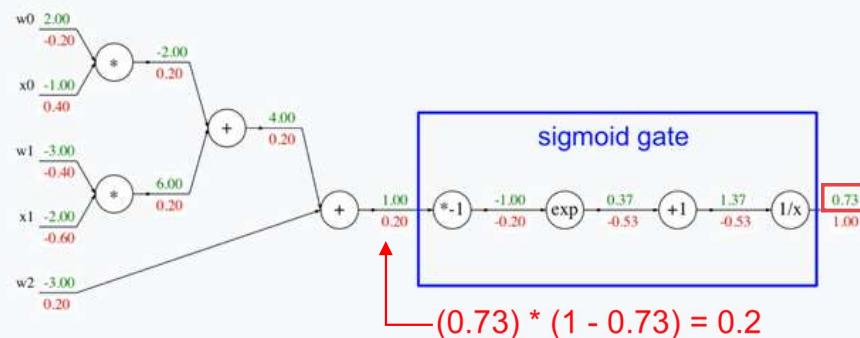
• 역전파 알고리즘(Backpropagation)



$$f(w, x) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + w_2)}}$$

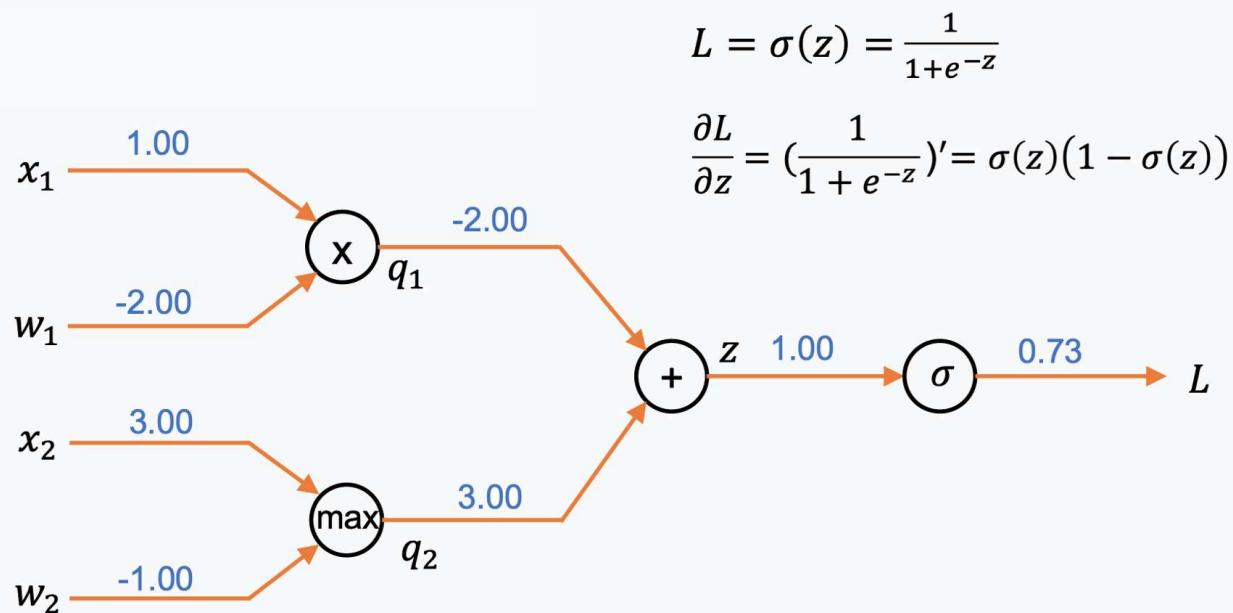
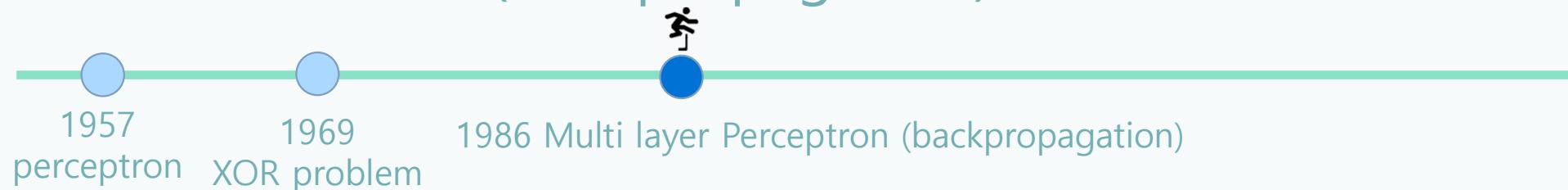
$$\sigma(x) = \frac{1}{1 + e^{-x}}$$
 sigmoid function

$$\frac{d\sigma(x)}{dx} = \frac{e^{-x}}{(1 + e^{-x})^2} = \left(\frac{1 + e^{-x} - 1}{1 + e^{-x}} \right) \left(\frac{1}{1 + e^{-x}} \right) = (1 - \sigma(x)) \sigma(x)$$



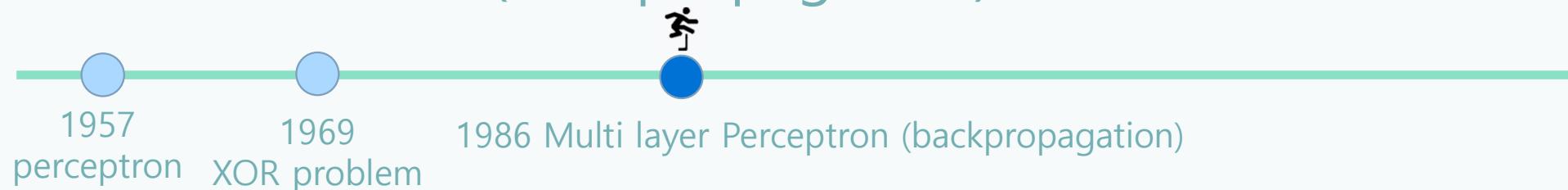
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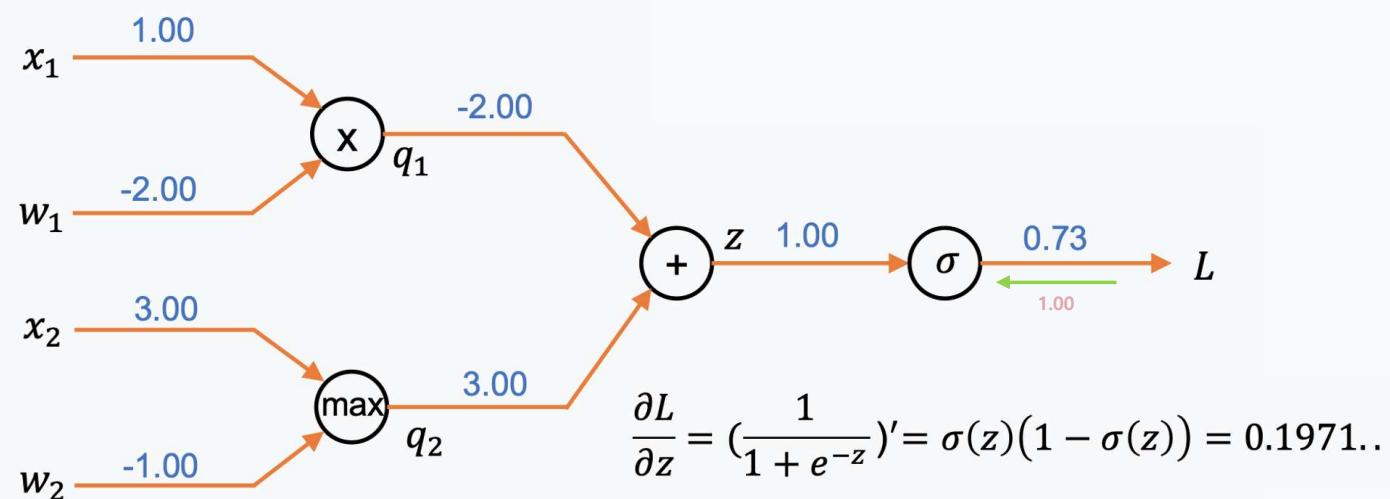


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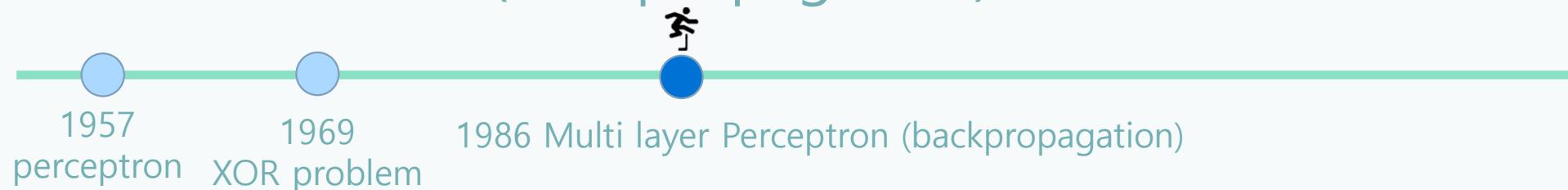


$$L = \sigma(z) = \frac{1}{1+e^{-z}}$$

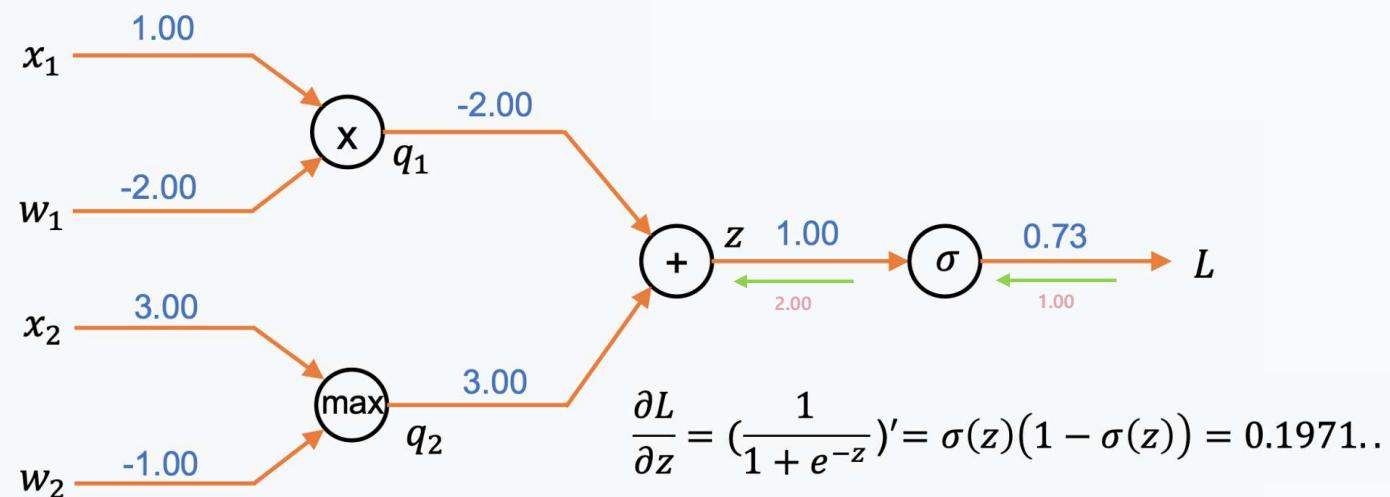


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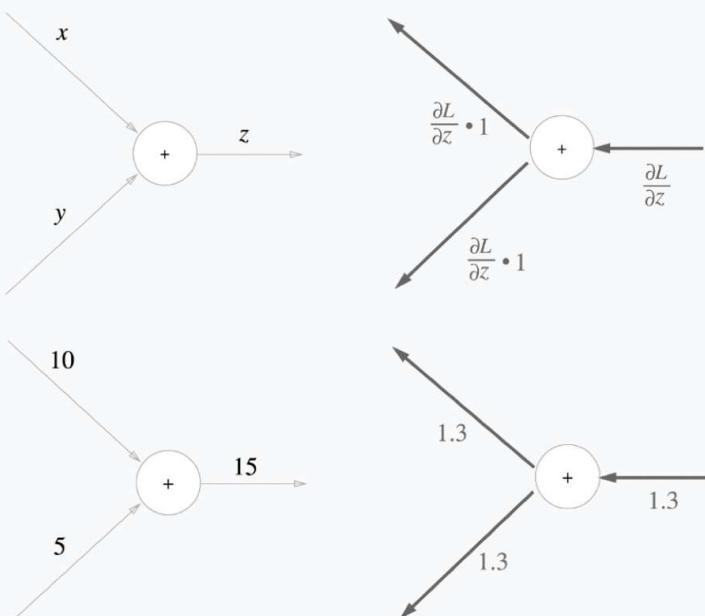
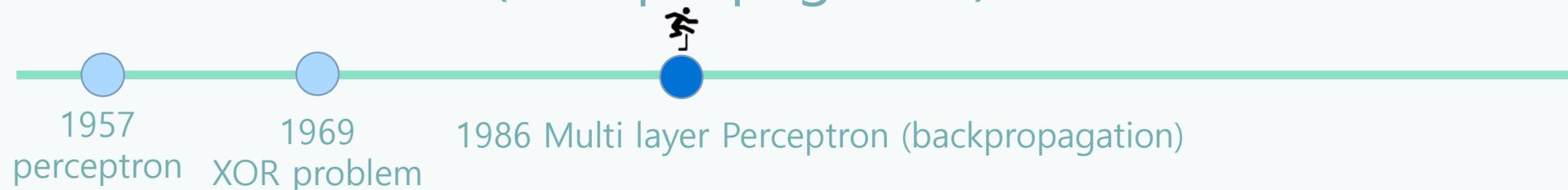


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Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)

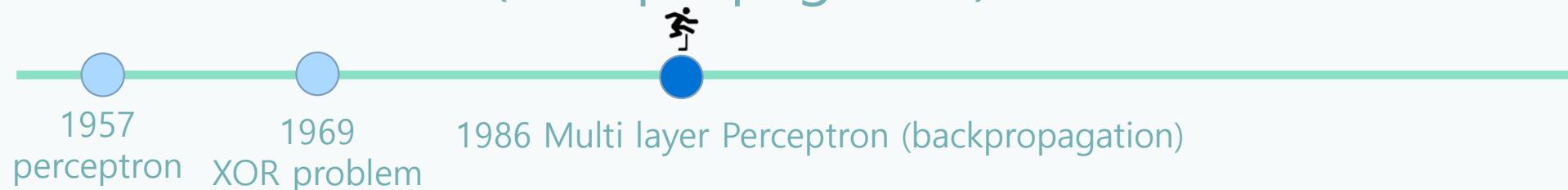


$$z = x + y \Rightarrow \begin{cases} \frac{\partial z}{\partial x} = 1 \\ \frac{\partial z}{\partial y} = 1 \end{cases}$$

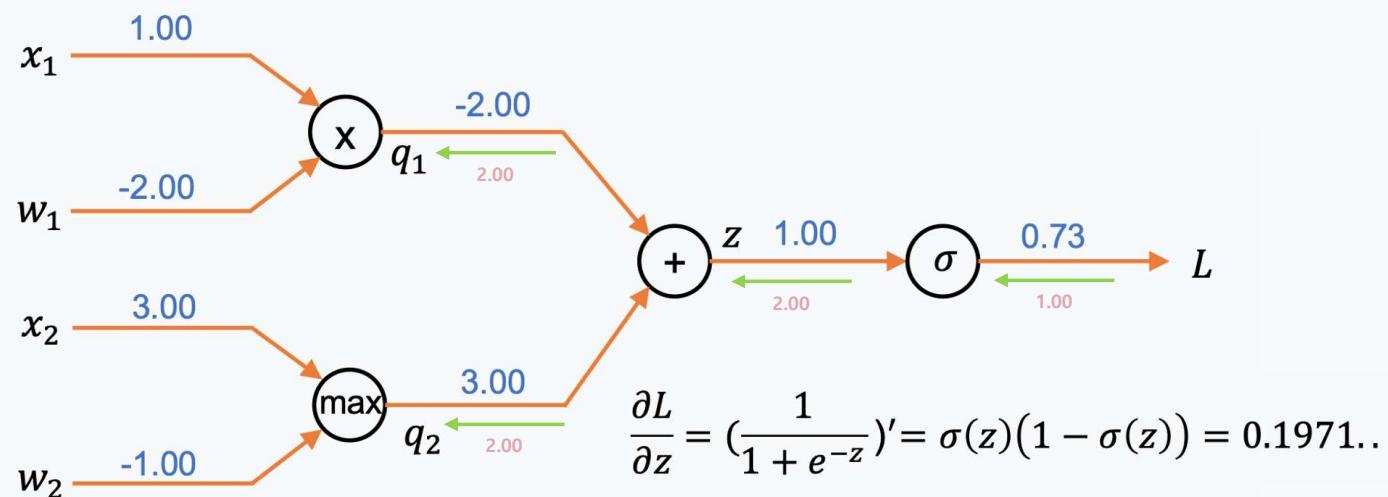
gradient distributor

Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)

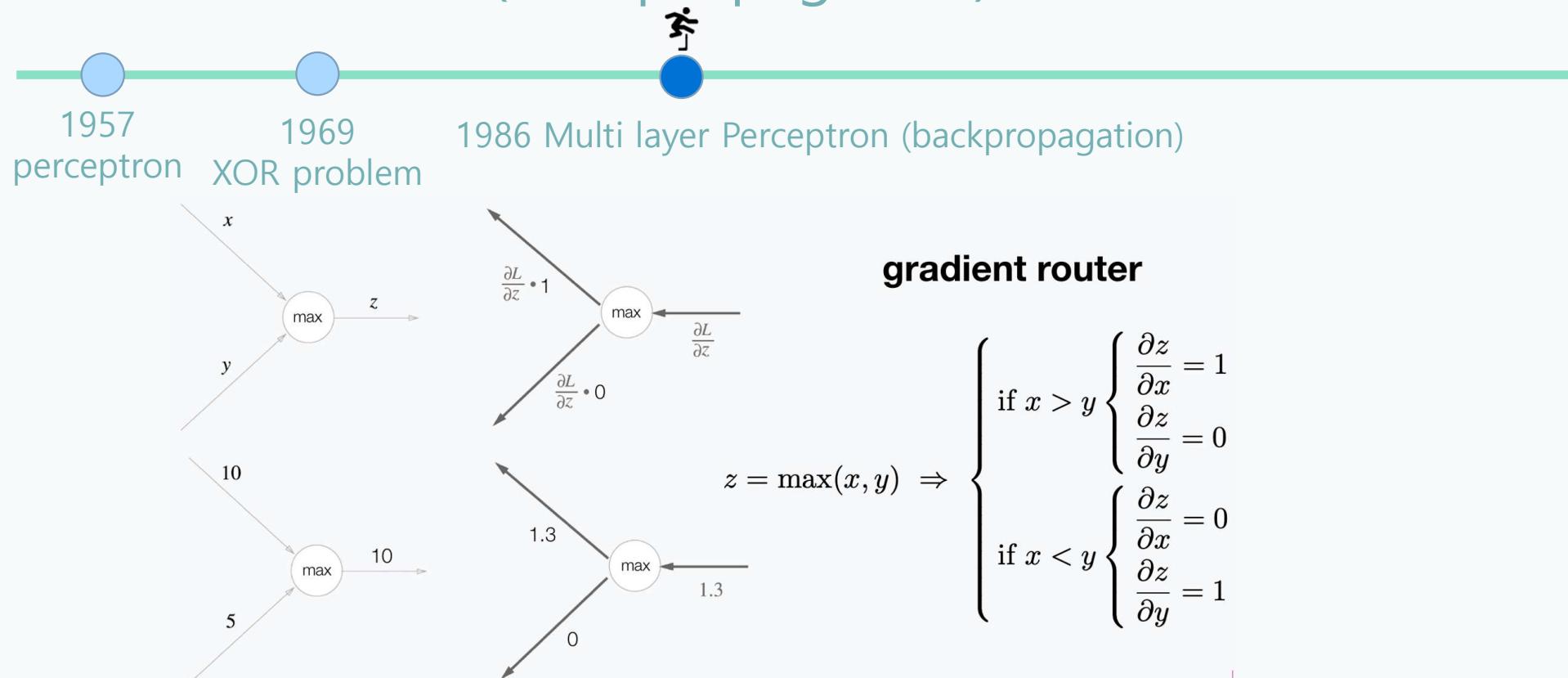


$$L = \sigma(z) = \frac{1}{1+e^{-z}}$$



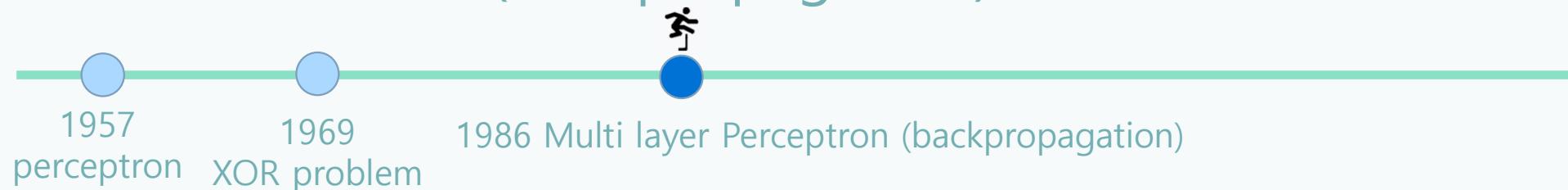
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- 역전파 알고리즘(Backpropagation)

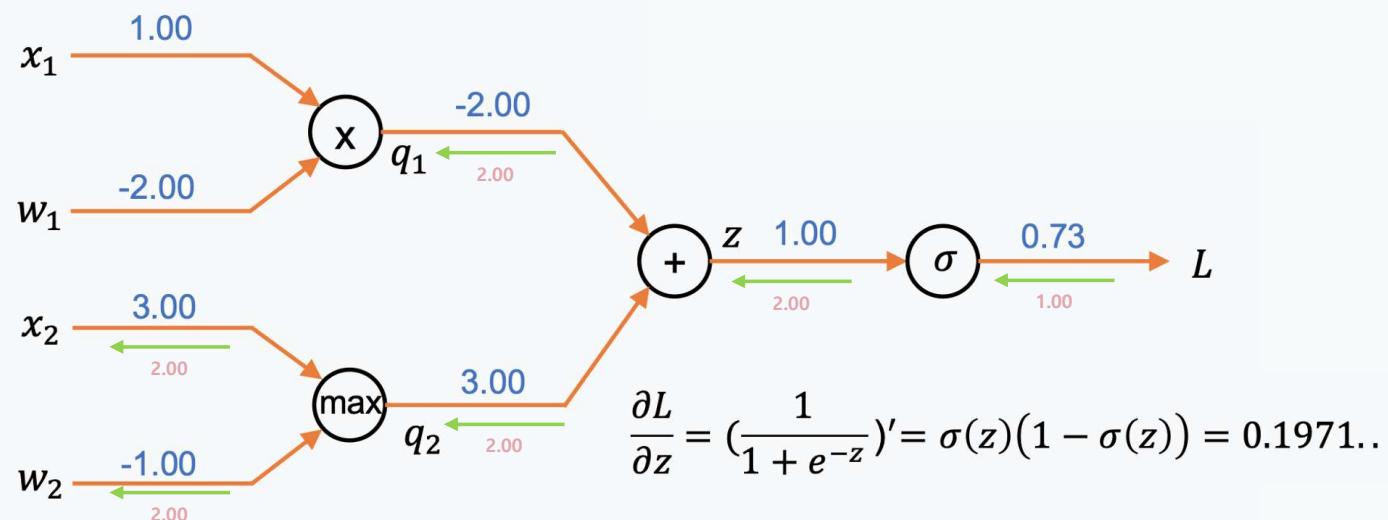


Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)

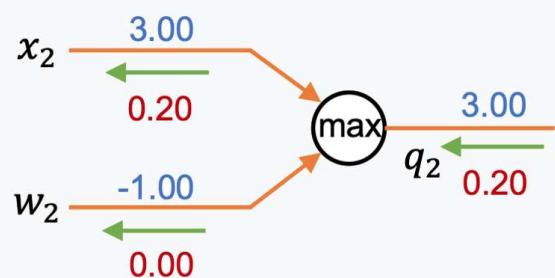
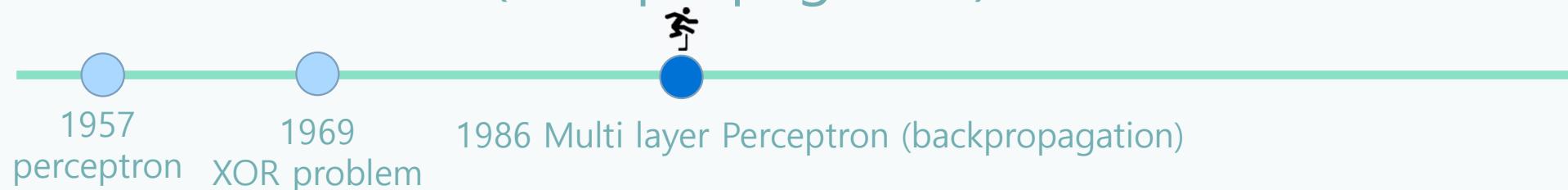


$$L = \sigma(z) = \frac{1}{1+e^{-z}}$$



Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$\frac{\partial q_2}{\partial x_2} = \mathbf{1}(x_2 > w_2)$$

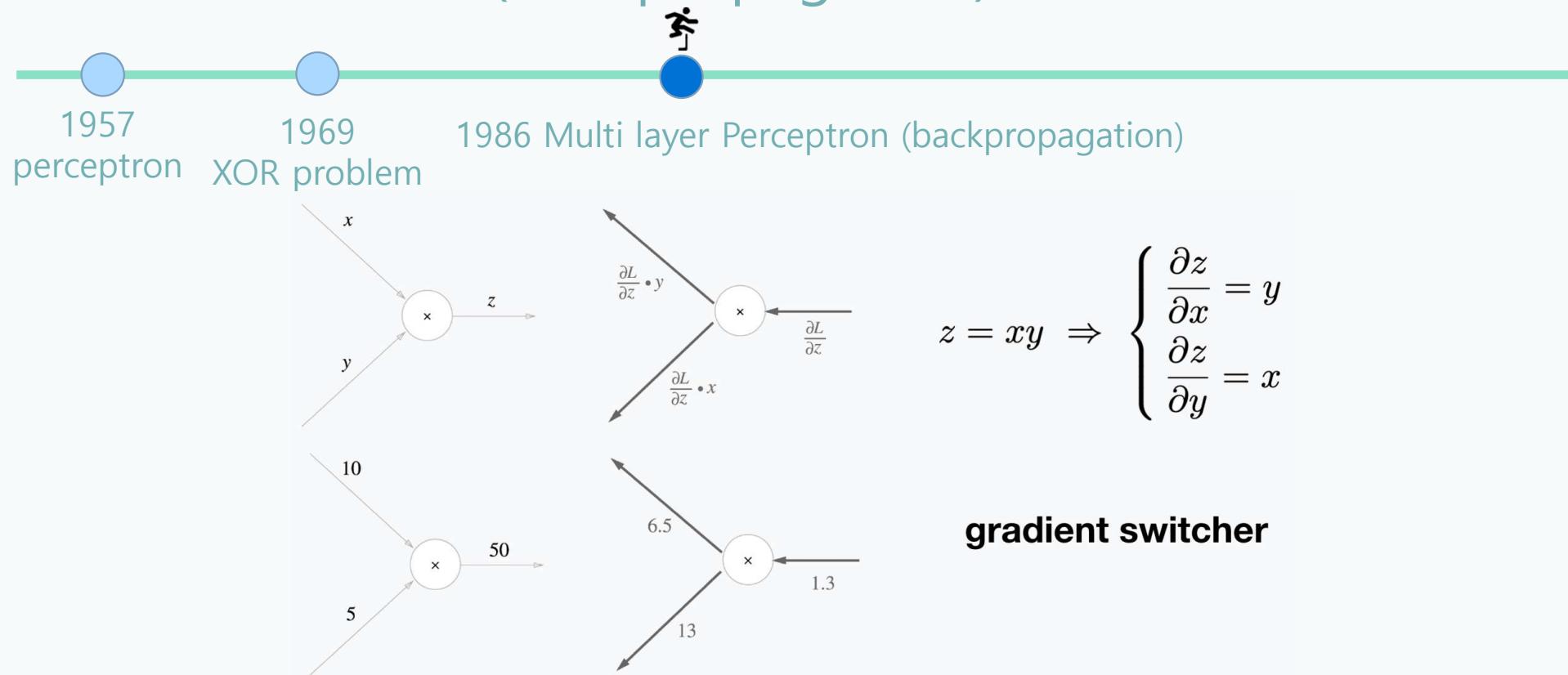
$$\frac{\partial L}{\partial x_2} = \frac{\partial L}{\partial q_2} \cdot \frac{\partial q_2}{\partial x_2} = 0.20 * 1.00 = 0.20$$

$$\frac{\partial q_2}{\partial w_2} = \mathbf{1}(w_2 > x_2)$$

$$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial q_2} \cdot \frac{\partial q_2}{\partial w_2} = 0.20 * 0.00 = 0.00$$

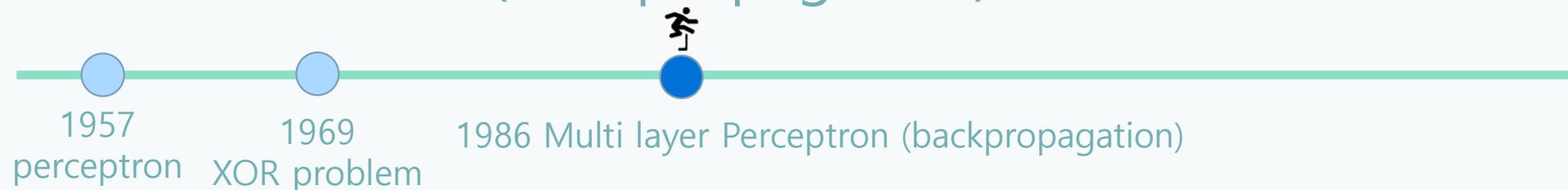
Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)

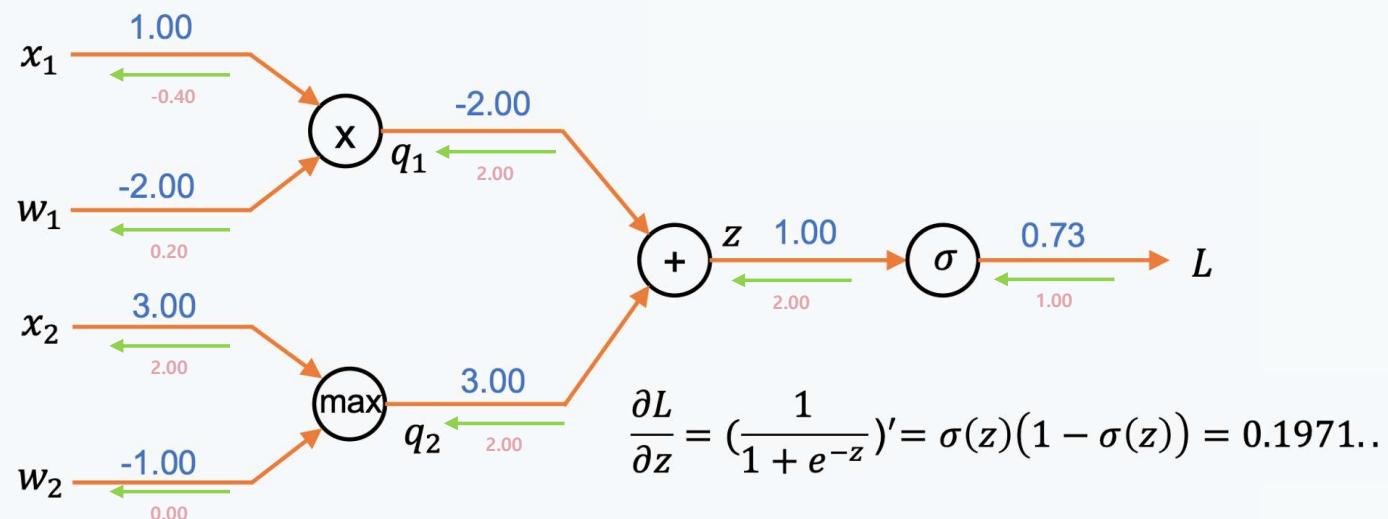


Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)

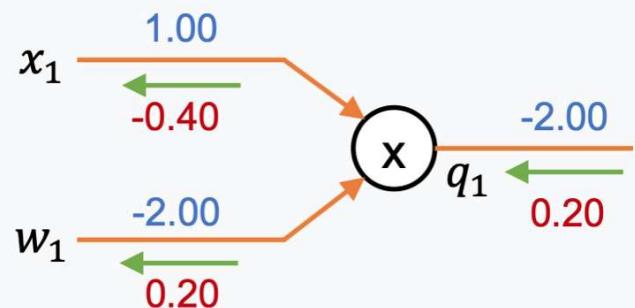
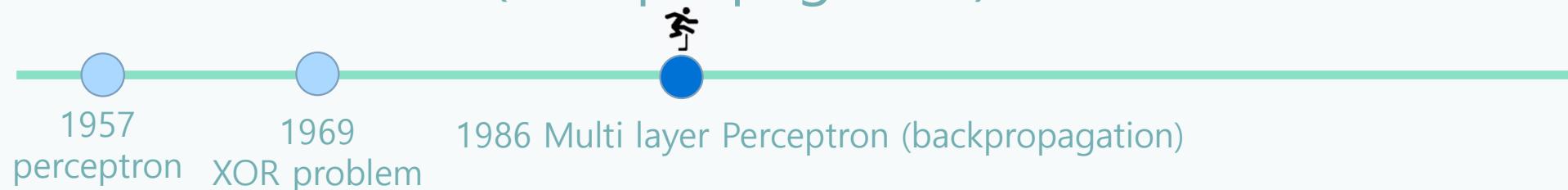


$$L = \sigma(z) = \frac{1}{1+e^{-z}}$$



Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$\frac{\partial q_1}{\partial x_1} = w_1$$

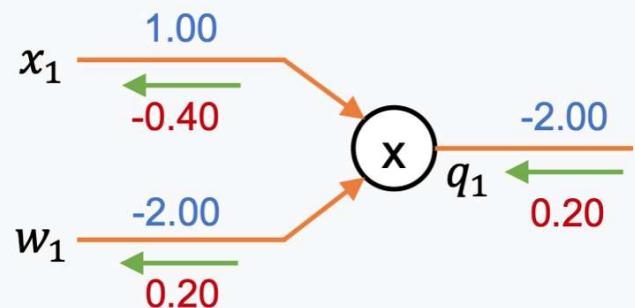
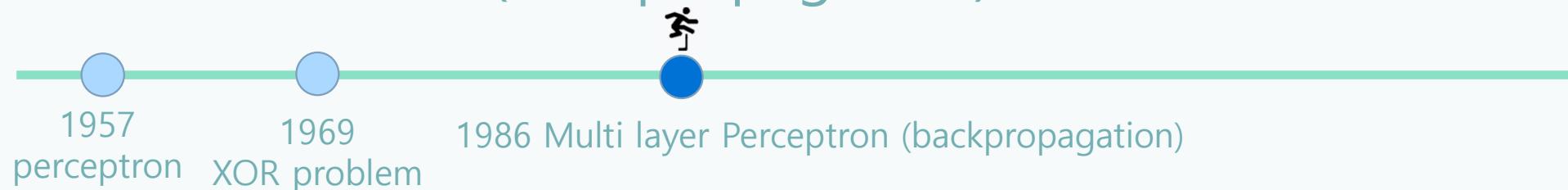
$$\frac{\partial L}{\partial x_1} = \frac{\partial L}{\partial q_1} \cdot \frac{\partial q_1}{\partial x_1} = 0.20 * (-2.00) = -0.40$$

$$\frac{\partial q_1}{\partial w_1} = x_1$$

$$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial q_1} \cdot \frac{\partial q_1}{\partial w_1} = 0.20 * 1.00 = 0.20$$

Appendix. BACKPROPAGATION

- 역전파 알고리즘(Backpropagation)



$$\frac{\partial q_1}{\partial x_1} = w_1$$

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$$\frac{\partial q_1}{\partial w_1} = x_1$$

$$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial q_1} \cdot \frac{\partial q_1}{\partial w_1} = 0.20 * 1.00 = 0.20$$