

**CONTEXT**

context0

**SETS**

pid\_t       //   *set of applications*

**END**

**CONTEXT****context1****EXTENDS****context0****SETS**

```
app_knobs_disc_t    // set of application discrete knobs
app_knobs_cont_t    // set of application continuous knobs
app_mons_disc_t     // set of application discrete monitors
app_mons_cont_t     // set of application continuous monitors
```

**END**

**CONTEXT**`context2`**EXTENDS**`context1`**CONSTANTS**`MIN_INFINITY``MAX_INFINITY`**AXIOMS**`axm1 : MIN_INFINITY  $\in$   $\mathbb{Z}$` `axm2 : MAX_INFINITY  $\in$   $\mathbb{Z}$` **END**

**MACHINE**

machine0

**SEES**

context0

**EVENTS****INITIALISATION**   ≐**STATUS**

ordinary

**BEGIN**

skip

**END****PRIME\_API\_APP\_RTM**   ≐**STATUS**

ordinary

**ANY**

proc\_id

**WHERE**

grd1 : proc\_id ∈ pid\_t

**THEN**

skip

**END****PRIME\_API\_DEV\_RTM**   ≐**STATUS**

ordinary

**BEGIN**

skip

**END****END**

**MACHINE**

```
machine1      // refining PRIME_API_APP_RTM
```

**REFINES**

```
machine0
```

**SEES**

```
context1
```

**VARIABLES**

```
app_sockets      // set of registered applications
app_knobs_disc    // set of registered application discrete knobs
app_knobs_cont    // set of registered application continuous knobs
app_mons_disc     // set of registered application discrete monitors
app_mons_cont     // set of registered application continuous monitors
```

**INVARIANTS**

```
inv1  : app_sockets  $\subseteq$  pid_t
inv2  : app_knobs_disc  $\in$  app_sockets  $\leftrightarrow$  app_knobs_disc_t
inv3  : app_knobs_cont  $\in$  app_sockets  $\leftrightarrow$  app_knobs_cont_t
inv4  : app_mons_disc  $\in$  app_sockets  $\leftrightarrow$  app_mons_disc_t
inv5  : app_mons_cont  $\in$  app_sockets  $\leftrightarrow$  app_mons_cont_t
```

**EVENTS**

```
INITIALISATION  $\triangleq$ 
```

```
  extended
```

```
STATUS
```

```
  ordinary
```

```
BEGIN
```

```
  act1 : app_sockets :=  $\emptyset$ 
  act2 : app_knobs_disc :=  $\emptyset$ 
  act3 : app_knobs_cont :=  $\emptyset$ 
  act4 : app_mons_disc :=  $\emptyset$ 
  act5 : app_mons_cont :=  $\emptyset$ 
```

```
END
```

```
PRIME_API_APP_REG  $\triangleq$ 
```

```
STATUS
```

```
  ordinary
```

```
REFINES
```

```
  PRIME_API_APP_RTM
```

```
ANY
```

```
  proc_id      // application id
```

```
WHERE
```

```
  grd1 : proc_id  $\in$  pid_t  $\wedge$  proc_id  $\notin$  app_sockets
```

```
THEN
```

```
  act1 : app_sockets := app_sockets  $\cup$  {proc_id}
```

```
END
```

```
PRIME_API_APP_KNOB_DISC_manage  $\triangleq$ 
```

```
STATUS
```

```
  ordinary
```

```
ANY
```

```
  proc_id
```

```
  knob
```

```
  idd      // app knob id
```

```
WHERE
```

```
  grd1 : proc_id  $\in$  pid_t  $\wedge$  proc_id  $\in$  app_sockets
```

```
  grd2 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\notin$  app_knobs_disc
```

```
THEN
```

```
  act1 : app_knobs_disc := app_knobs_disc  $\cup$  {proc_id  $\mapsto$  idd}
```

```
END
```

PRIME\_API\_APP\_KNOB\_CONT\_manage  $\triangleq$

STATUS

ordinary

ANY

proc\_id

knob

idd

WHERE

grd1 :  $\text{proc\_id} \in \text{pid\_t} \wedge \text{proc\_id} \in \text{app\_sockets}$

grd2 :  $\text{knob} \in \text{app\_knobs\_cont\_t} \wedge \text{proc\_id} \mapsto \text{idd} \notin \text{app\_knobs\_cont}$

THEN

act1 :  $\text{app\_knobs\_cont} := \text{app\_knobs\_cont} \cup \{\text{proc\_id} \mapsto \text{idd}\}$

END

PRIME\_API\_APP\_MON\_DISC\_manage  $\triangleq$

STATUS

ordinary

ANY

proc\_id

mon

idd

WHERE

grd1 :  $\text{proc\_id} \in \text{pid\_t} \wedge \text{proc\_id} \in \text{app\_sockets}$

grd2 :  $\text{mon} \in \text{app\_mons\_disc\_t} \wedge \text{proc\_id} \mapsto \text{idd} \notin \text{app\_mons\_disc}$

THEN

act1 :  $\text{app\_mons\_disc} := \text{app\_mons\_disc} \cup \{\text{proc\_id} \mapsto \text{idd}\}$

END

PRIME\_API\_APP\_MON\_CONT\_manage  $\triangleq$

STATUS

ordinary

ANY

proc\_id

mon //

idd

WHERE

grd1 :  $\text{proc\_id} \in \text{pid\_t} \wedge \text{proc\_id} \in \text{app\_sockets}$

grd2 :  $\text{mon} \in \text{app\_mons\_cont\_t} \wedge \text{proc\_id} \mapsto \text{idd} \notin \text{app\_mons\_cont}$

THEN

act1 :  $\text{app\_mons\_cont} := \text{app\_mons\_cont} \cup \{\text{proc\_id} \mapsto \text{idd}\}$

END

PRIME\_API\_APP\_DEREG  $\triangleq$

STATUS

ordinary

ANY

proc\_id

WHERE

grd1 :  $\text{proc\_id} \in \text{pid\_t} \wedge \text{proc\_id} \in \text{app\_sockets}$

grd2 :  $\text{ran}(\text{app\_knobs\_disc}) \subseteq \text{app\_knobs\_disc\_t} \wedge \text{app\_knobs\_disc}[\{\text{proc\_id}\}] = \emptyset$

grd3 :  $\text{ran}(\text{app\_knobs\_cont}) \subseteq \text{app\_knobs\_cont\_t} \wedge \text{app\_knobs\_cont}[\{\text{proc\_id}\}] = \emptyset$

grd4 :  $\text{ran}(\text{app\_mons\_disc}) \subseteq \text{app\_mons\_disc\_t} \wedge \text{app\_mons\_disc}[\{\text{proc\_id}\}] = \emptyset$

grd5 :  $\text{ran}(\text{app\_mons\_cont}) \subseteq \text{app\_mons\_cont\_t} \wedge \text{app\_mons\_cont}[\{\text{proc\_id}\}] = \emptyset$

THEN

act1 :  $\text{app\_sockets} := \text{app\_sockets} \setminus \{\text{proc\_id}\}$

act2 :  $\text{app\_knobs\_disc} := \{\text{proc\_id}\} \triangleleft \text{app\_knobs\_disc}$

act3 :  $\text{app\_knobs\_cont} := \{\text{proc\_id}\} \triangleleft \text{app\_knobs\_cont}$

act4 :  $\text{app\_mons\_disc} := \{\text{proc\_id}\} \triangleleft \text{app\_mons\_disc}$

act5 :  $\text{app\_mons\_cont} := \{\text{proc\_id}\} \triangleleft \text{app\_mons\_cont}$

END

```

PRIME_API_DEV_RTM  ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_DEV_RTM
BEGIN
  skip
END

PRIME_API_APP_KNOB_DISC_DEREG  ≐
STATUS
  ordinary
ANY
  knob
  proc_id
  idd
WHERE
  grd1 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc
THEN
  act1 : app_knobs_disc := app_knobs_disc \ {proc_id ↦ idd}
END

PRIME_API_APP_KNOB_CONT_DEREG  ≐
STATUS
  ordinary
ANY
  proc_id
  knob
  idd
WHERE
  grd1 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont
THEN
  act1 : app_knobs_cont := app_knobs_cont \ {proc_id ↦ idd}
END

PRIME_API_APP_MON_DISC_DEREG  ≐
STATUS
  ordinary
ANY
  proc_id
  mon
  idd
WHERE
  grd1 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc
THEN
  act1 : app_mons_disc := app_mons_disc \ {proc_id ↦ idd}
END

PRIME_API_APP_MON_CONT_DEREG  ≐
STATUS
  ordinary
ANY
  proc_id
  mon
  idd
WHERE
  grd1 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont
THEN

```

```
act1 : app_mons_cont := app_mons_cont \ {proc_id ↦ idd}  
END
```

```
END
```



**MACHINE**

```
machine2      // refining PRIME_API_APP_KNOB_DISC_manage and PRIME_API_APP_KNOB_CONT_manage
```

**REFINES**

```
machine1
```

**SEES**

```
context1
```

**VARIABLES**

```
app_sockets      // set of registered applications
app_knobs_disc   // set of registered application discrete knobs
app_knobs_cont   // set of registered application continuous knobs
app_mons_disc    // set of registered application discrete monitors
app_mons_cont    // set of registered application continuous monitors
app_knobs_disc_min
app_knobs_cont_min
app_knobs_disc_max
app_knobs_cont_max
app_knobs_disc_value
app_knobs_cont_value
```

**INVARIANTS**

```
inv1 : app_knobs_disc_min ∈ app_knobs_disc → ℤ
inv2 : app_knobs_cont_min ∈ app_knobs_cont → ℤ
inv3 : app_knobs_disc_max ∈ app_knobs_disc → ℤ
inv4 : app_knobs_cont_max ∈ app_knobs_cont → ℤ
inv5 : app_knobs_disc_value ∈ app_knobs_disc → ℤ
inv6 : app_knobs_cont_value ∈ app_knobs_cont → ℤ
```

**EVENTS**

```
INITIALISATION ≐
```

```
extended
```

```
STATUS
```

```
ordinary
```

```
BEGIN
```

```
act1 : app_sockets := ∅
act2 : app_knobs_disc := ∅
act3 : app_knobs_cont := ∅
act4 : app_mons_disc := ∅
act5 : app_mons_cont := ∅
act6 : app_knobs_disc_min := ∅
act7 : app_knobs_cont_min := ∅
act8 : app_knobs_disc_max := ∅
act9 : app_knobs_cont_max := ∅
act10 : app_knobs_disc_value := ∅
act11 : app_knobs_cont_value := ∅
```

```
END
```

```
PRIME_API_APP_REG ≐
```

```
extended
```

```
STATUS
```

```
ordinary
```

```
REFINES
```

```
PRIME_API_APP_REG
```

```
ANY
```

```
proc_id      // application id
```

```
WHERE
```

```
grd1 : proc_id ∈ pid_t ∧ proc_id ∉ app_sockets
```

```
THEN
```

```
act1 : app_sockets := app_sockets ∪ {proc_id}
```

```
END
```

```
PRIME_API_APP_KNOB_DISC_REG ≐
```

```
STATUS
```

```
ordinary
```

```
REFINES
```

```

PRIME_API_APP_KNOB_DISC_manage
ANY
  proc_id
  knob
  idd      //  app knob id
  minn
  maxx
WHERE
  grd1 :   proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2 :   knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∉ app_knobs_disc
  grd3 :   knob ∈ app_knobs_disc_t ∧ minn < maxx
THEN
  act1 :   app_knobs_disc := app_knobs_disc ∪ {proc_id ↦ idd}
  act2 :   app_knobs_disc_min := app_knobs_disc_min ∪ { (proc_id ↦ idd) ↦ minn }
  act3 :   app_knobs_disc_max := app_knobs_disc_max ∪ { (proc_id ↦ idd) ↦ maxx }
  act4 :   app_knobs_disc_value(proc_id ↦ idd) := minn
END

PRIME_API_APP_KNOB_CONT_REG  ≐
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_CONT_manage
ANY
  proc_id
  knob
  idd
  minn
  maxx
WHERE
  grd1 :   proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2 :   knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∉ app_knobs_cont
  grd3 :   knob ∈ app_knobs_cont_t ∧ minn < maxx
THEN
  act1 :   app_knobs_cont := app_knobs_cont ∪ {proc_id ↦ idd}
  act2 :   app_knobs_cont_min := app_knobs_cont_min ∪ { (proc_id ↦ idd) ↦ minn }
  act3 :   app_knobs_cont_max := app_knobs_cont_max ∪ { (proc_id ↦ idd) ↦ maxx }
  act4 :   app_knobs_cont_value(proc_id ↦ idd) := minn
END

PRIME_API_APP_KNOB_DISC_MIN  ≐
STATUS
  ordinary
ANY
  proc_id
  knob
  idd
  minn
  maxx
  val
WHERE
  grd1 :   knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc
  grd2 :   knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc ∧ maxx = app_knobs_disc_max
            (proc_id ↦ idd) ∧ minn < maxx
  grd3 :   knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc ∧ val = app_knobs_disc_value
            (proc_id ↦ idd) ∧ minn ≤ val
THEN
  act1 :   app_knobs_disc_min(proc_id ↦ idd) := minn
END

PRIME_API_APP_KNOB_CONT_MIN  ≐
STATUS
  ordinary
ANY
  proc_id

```

```

knob
idd
minn
maxx
val
WHERE
  grd1 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont
  grd2 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ maxx = app_knobs_cont_max
         (proc_id ↦ idd) ∧ minn < maxx
  grd3 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ val = app_knobs_cont_value
         (proc_id ↦ idd) ∧ minn ≤ val
THEN
  act1 : app_knobs_cont_min(proc_id ↦ idd) := minn
END

PRIME_API_APP_KNOB_DISC_MAX ≐
STATUS
  ordinary
ANY
  proc_id      //
  knob
  idd
  minn
  maxx
  val
WHERE
  grd1 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc
  grd2 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc ∧ minn = app_knobs_disc_min
         (proc_id ↦ idd) ∧ maxx > minn
  grd3 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc ∧ val = app_knobs_disc_value
         (proc_id ↦ idd) ∧ maxx ≥ val
THEN
  act1 : app_knobs_disc_max(proc_id ↦ idd) := maxx
END

PRIME_API_APP_KNOB_CONT_MAX ≐
STATUS
  ordinary
ANY
  proc_id
  knob
  idd
  minn
  maxx
  val
WHERE
  grd1 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont
  grd2 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ minn = app_knobs_cont_min
         (proc_id ↦ idd) ∧ maxx > minn
  grd3 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ val = app_knobs_cont_value
         (proc_id ↦ idd) ∧ maxx ≥ val
THEN
  act1 : app_knobs_cont_max(proc_id ↦ idd) := maxx
END

PRIME_API_APP_KNOB_DISC_GET ≐      // get value
STATUS
  ordinary
ANY
  proc_id
  knob
  idd
  minn
  maxx
  val

```

```

WHERE
  grd1 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ id ∈ app_knobs_disc
  grd2 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ id ∈ app_knobs_disc ∧ minn = app_knobs_disc_min
         (proc_id ↦ id) ∧ minn ≤ val
  grd3 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ id ∈ app_knobs_disc ∧ maxx = app_knobs_disc_max
         (proc_id ↦ id) ∧ maxx ≥ val
THEN
  act1 : app_knobs_disc_value(proc_id ↦ id) := val
END

PRIME_API_APP_KNOB_CONT_GET ≐          // get value
STATUS
  ordinary
ANY
  proc_id
  knob
  id
  minn
  maxx
  val
WHERE
  grd1 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ id ∈ app_knobs_cont
  grd2 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ id ∈ app_knobs_cont ∧ minn = app_knobs_cont_min
         (proc_id ↦ id) ∧ minn ≤ val
  grd3 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ id ∈ app_knobs_cont ∧ maxx = app_knobs_cont_max
         (proc_id ↦ id) ∧ maxx ≥ val
THEN
  act1 : app_knobs_cont_value(proc_id ↦ id) := val
END

PRIME_API_APP_KNOB_DISC_DEREG ≐
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_DISC_DEREG
ANY
  proc_id
  knob
  id
WHERE
  grd1 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ id ∈ app_knobs_disc
THEN
  act1 : app_knobs_disc := app_knobs_disc \ {proc_id ↦ id}
  act2 : app_knobs_disc_min := {proc_id ↦ id} ≪ app_knobs_disc_min
  act3 : app_knobs_disc_max := {proc_id ↦ id} ≪ app_knobs_disc_max
  act4 : app_knobs_disc_value := {proc_id ↦ id} ≪ app_knobs_disc_value
END

PRIME_API_APP_KNOB_CONT_DEREG ≐
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_CONT_DEREG
ANY
  proc_id
  knob
  id
WHERE
  grd1 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ id ∈ app_knobs_cont
THEN
  act1 : app_knobs_cont := app_knobs_cont \ {proc_id ↦ id}
  act2 : app_knobs_cont_min := {proc_id ↦ id} ≪ app_knobs_cont_min
  act3 : app_knobs_cont_max := {proc_id ↦ id} ≪ app_knobs_cont_max
  act4 : app_knobs_cont_value := {proc_id ↦ id} ≪ app_knobs_cont_value
END

```

```

PRIME_API_APP_MON_DISC_manage  ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_MON_DISC_manage
ANY
  proc_id
  mon
  idd
WHERE
  grd1  :  proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2  :  mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∉ app_mons_disc
THEN
  act1  :  app_mons_disc := app_mons_disc ∪ {proc_id ↦ idd}
END

PRIME_API_APP_MON_CONT_manage  ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_MON_CONT_manage
ANY
  proc_id
  mon    //
  idd
WHERE
  grd1  :  proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2  :  mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∉ app_mons_cont
THEN
  act1  :  app_mons_cont := app_mons_cont ∪ {proc_id ↦ idd}
END

PRIME_API_APP_DEREG  ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_DEREG
ANY
  proc_id
WHERE
  grd1  :  proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2  :  ran(app_knobs_disc) ⊆ app_knobs_disc_t ∧ app_knobs_disc[{proc_id}] = ∅
  grd3  :  ran(app_knobs_cont) ⊆ app_knobs_cont_t ∧ app_knobs_cont[{proc_id}] = ∅
  grd4  :  ran(app_mons_disc) ⊆ app_mons_disc_t ∧ app_mons_disc[{proc_id}] = ∅
  grd5  :  ran(app_mons_cont) ⊆ app_mons_cont_t ∧ app_mons_cont[{proc_id}] = ∅
THEN
  act1  :  app_sockets := app_sockets \ {proc_id}
  act2  :  app_knobs_disc := {proc_id} ⋈ app_knobs_disc
  act3  :  app_knobs_cont := {proc_id} ⋈ app_knobs_cont
  act4  :  app_mons_disc := {proc_id} ⋈ app_mons_disc
  act5  :  app_mons_cont := {proc_id} ⋈ app_mons_cont
END

PRIME_API_DEV_RTM  ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_DEV_RTM
BEGIN
  skip

```

END

PRIME\_API\_APP\_MON\_DISC\_DEREG  $\triangleq$

STATUS

ordinary

REFINES

PRIME\_API\_APP\_MON\_DISC\_DEREG

ANY

proc\_id        //

mon

idd

WHERE

grd1 : mon  $\in$  app\_mons\_disc\_t  $\wedge$  proc\_id  $\mapsto$  idd  $\in$  app\_mons\_disc

THEN

act1 : app\_mons\_disc := app\_mons\_disc \ {proc\_id  $\mapsto$  idd}

END

PRIME\_API\_APP\_MON\_CONT\_DEREG  $\triangleq$

STATUS

ordinary

REFINES

PRIME\_API\_APP\_MON\_CONT\_DEREG

ANY

proc\_id

mon

idd

WHERE

grd1 : mon  $\in$  app\_mons\_cont\_t  $\wedge$  proc\_id  $\mapsto$  idd  $\in$  app\_mons\_cont

THEN

act1 : app\_mons\_cont := app\_mons\_cont \ {proc\_id  $\mapsto$  idd}

END

END

**MACHINE**

```
machine3      // refining PRIME_API_APP_MON_DISC_manage and PRIME_API_APP_MON_CONT_manage
```

**REFINES**

```
machine2
```

**SEES**

```
context2
```

**VARIABLES**

```
app_sockets      // set of registered applications
app_knobs_disc   // set of registered application discrete knobs
app_knobs_cont   // set of registered application continuous knobs
app_mons_disc    // set of registered application discrete monitors
app_mons_cont    // set of registered application continuous monitors
app_knobs_disc_min
app_knobs_cont_min
app_knobs_disc_max
app_knobs_cont_max
app_knobs_disc_value
app_knobs_cont_value
app_mons_disc_min
app_mons_cont_min
app_mons_disc_max
app_mons_cont_max
app_mons_disc_weight
app_mons_cont_weight
app_mons_disc_value
app_mons_cont_value
```

**INVARIANTS**

```
inv1 : app_mons_disc_min ∈ app_mons_disc → ℤ
inv2 : app_mons_cont_min ∈ app_mons_cont → ℤ
inv3 : app_mons_disc_max ∈ app_mons_disc → ℤ
inv4 : app_mons_cont_max ∈ app_mons_cont → ℤ
inv8 : app_mons_disc_weight ∈ app_mons_disc → ℤ
inv7 : app_mons_cont_weight ∈ app_mons_cont → ℤ
inv5 : app_mons_disc_value ∈ app_mons_disc → ℤ
inv6 : app_mons_cont_value ∈ app_mons_cont → ℤ
```

**EVENTS**

```
INITIALISATION ≐
```

```
extended
```

```
STATUS
```

```
ordinary
```

```
BEGIN
```

```
act1 : app_sockets := ∅
act2 : app_knobs_disc := ∅
act3 : app_knobs_cont := ∅
act4 : app_mons_disc := ∅
act5 : app_mons_cont := ∅
act6 : app_knobs_disc_min := ∅
act7 : app_knobs_cont_min := ∅
act8 : app_knobs_disc_max := ∅
act9 : app_knobs_cont_max := ∅
act10 : app_knobs_disc_value := ∅
act11 : app_knobs_cont_value := ∅
act12 : app_mons_disc_min := ∅
act13 : app_mons_cont_min := ∅
act14 : app_mons_disc_max := ∅
act15 : app_mons_cont_max := ∅
act19 : app_mons_disc_weight := ∅
act18 : app_mons_cont_weight := ∅
act16 : app_mons_disc_value := ∅
act17 : app_mons_cont_value := ∅
```

```
END
```

```

PRIME_API_APP_REG    ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_REG
ANY
  proc_id          // application id
WHERE
  grd1 : proc_id ∈ pid_t ∧ proc_id ∉ app_sockets
THEN
  act1 : app_sockets = app_sockets ∪ {proc_id}
END

PRIME_API_APP_KNOB_DISC_REG    ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_DISC_REG
ANY
  proc_id
  knob
  idd      // app knob id
  minn
  maxx
WHERE
  grd1 : proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∉ app_knobs_disc
  grd3 : knob ∈ app_knobs_disc_t ∧ minn < maxx
THEN
  act1 : app_knobs_disc = app_knobs_disc ∪ {proc_id ↦ idd}
  act2 : app_knobs_disc_min = app_knobs_disc_min ∪ { (proc_id ↦ idd) ↦ minn }
  act3 : app_knobs_disc_max = app_knobs_disc_max ∪ { (proc_id ↦ idd) ↦ maxx }
  act4 : app_knobs_disc_value(proc_id ↦ idd) = minn
END

PRIME_API_APP_KNOB_CONT_REG    ≐
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_CONT_REG
ANY
  proc_id
  knob
  idd
  minn
  maxx
WHERE
  grd1 : proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∉ app_knobs_cont
  grd3 : knob ∈ app_knobs_cont_t ∧ minn < maxx
THEN
  act1 : app_knobs_cont = app_knobs_cont ∪ {proc_id ↦ idd}
  act2 : app_knobs_cont_min = app_knobs_cont_min ∪ { (proc_id ↦ idd) ↦ minn }
  act3 : app_knobs_cont_max = app_knobs_cont_max ∪ { (proc_id ↦ idd) ↦ maxx }
  act4 : app_knobs_cont_value(proc_id ↦ idd) = minn
END

PRIME_API_APP_KNOB_DISC_MIN    ≐
  extended
STATUS
  ordinary
REFINES

```



```

PRIME_API_APP_KNOB_DISC_MIN
ANY
  proc_id
  knob
  idd
  minn
  maxx
  val
WHERE
  grd1 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_disc
  grd2 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_disc  $\wedge$  maxx = app_knobs_disc_max
    (proc_id  $\mapsto$  idd)  $\wedge$  minn < maxx
  grd3 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_disc  $\wedge$  val = app_knobs_disc_value
    (proc_id  $\mapsto$  idd)  $\wedge$  minn  $\leq$  val
THEN
  act1 : app_knobs_disc_min(proc_id  $\mapsto$  idd)  $:=$  minn
END

PRIME_API_APP_KNOB_CONT_MIN  $\triangleq$ 
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_CONT_MIN
ANY
  proc_id
  knob
  idd
  minn
  maxx
  val
WHERE
  grd1 : knob  $\in$  app_knobs_cont_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_cont
  grd2 : knob  $\in$  app_knobs_cont_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_cont  $\wedge$  maxx = app_knobs_cont_max
    (proc_id  $\mapsto$  idd)  $\wedge$  minn < maxx
  grd3 : knob  $\in$  app_knobs_cont_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_cont  $\wedge$  val = app_knobs_cont_value
    (proc_id  $\mapsto$  idd)  $\wedge$  minn  $\leq$  val
THEN
  act1 : app_knobs_cont_min(proc_id  $\mapsto$  idd)  $:=$  minn
END

PRIME_API_APP_KNOB_DISC_MAX  $\triangleq$ 
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_DISC_MAX
ANY
  proc_id //
  knob
  idd
  minn
  maxx
  val
WHERE
  grd1 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_disc
  grd2 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_disc  $\wedge$  minn = app_knobs_disc_min
    (proc_id  $\mapsto$  idd)  $\wedge$  maxx > minn
  grd3 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_disc  $\wedge$  val = app_knobs_disc_value
    (proc_id  $\mapsto$  idd)  $\wedge$  maxx  $\geq$  val
THEN
  act1 : app_knobs_disc_max(proc_id  $\mapsto$  idd)  $:=$  maxx
END

PRIME_API_APP_KNOB_CONT_MAX  $\triangleq$ 

```

```

    extended
STATUS
    ordinary
REFINES
    PRIME_API_APP_KNOB_CONT_MAX
ANY
    proc_id
    knob
    idd
    minn
    maxx
    val
WHERE
    grd1 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont
    grd2 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ minn = app_knobs_cont_min
            (proc_id ↦ idd) ∧ maxx > minn
    grd3 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ val = app_knobs_cont_value
            (proc_id ↦ idd) ∧ maxx ≥ val
THEN
    act1 : app_knobs_cont_max(proc_id ↦ idd) := maxx
END

PRIME_API_APP_KNOB_DISC_GET ≐          // get value
    extended
STATUS
    ordinary
REFINES
    PRIME_API_APP_KNOB_DISC_GET
ANY
    proc_id
    knob
    idd
    minn
    maxx
    val
WHERE
    grd1 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc
    grd2 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc ∧ minn = app_knobs_disc_min
            (proc_id ↦ idd) ∧ minn ≤ val
    grd3 : knob ∈ app_knobs_disc_t ∧ proc_id ↦ idd ∈ app_knobs_disc ∧ maxx = app_knobs_disc_max
            (proc_id ↦ idd) ∧ maxx ≥ val
THEN
    act1 : app_knobs_disc_value(proc_id ↦ idd) := val
END

PRIME_API_APP_KNOB_CONT_GET ≐          // get value
    extended
STATUS
    ordinary
REFINES
    PRIME_API_APP_KNOB_CONT_GET
ANY
    proc_id
    knob
    idd
    minn
    maxx
    val
WHERE
    grd1 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont
    grd2 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ minn = app_knobs_cont_min
            (proc_id ↦ idd) ∧ minn ≤ val
    grd3 : knob ∈ app_knobs_cont_t ∧ proc_id ↦ idd ∈ app_knobs_cont ∧ maxx = app_knobs_cont_max
            (proc_id ↦ idd) ∧ maxx ≥ val
THEN

```

```

    act1 : app_knobs_cont_value
           (proc_id  $\mapsto$  idd) := val
END

PRIME_API_APP_KNOB_DISC_DEREG  $\triangleq$ 
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_DISC_DEREG
ANY
  proc_id
  knob
  idd
WHERE
  grd1 : knob  $\in$  app_knobs_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_disc
THEN
  act1 : app_knobs_disc := app_knobs_disc \ {proc_id  $\mapsto$  idd}
  act2 : app_knobs_disc_min := {proc_id  $\mapsto$  idd}  $\triangleleft$  app_knobs_disc_min
  act3 : app_knobs_disc_max := {proc_id  $\mapsto$  idd}  $\triangleleft$  app_knobs_disc_max
  act4 : app_knobs_disc_value := {proc_id  $\mapsto$  idd}  $\triangleleft$  app_knobs_disc_value
END

PRIME_API_APP_KNOB_CONT_DEREG  $\triangleq$ 
  extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_KNOB_CONT_DEREG
ANY
  proc_id
  knob
  idd
WHERE
  grd1 : knob  $\in$  app_knobs_cont_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_knobs_cont
THEN
  act1 : app_knobs_cont := app_knobs_cont \ {proc_id  $\mapsto$  idd}
  act2 : app_knobs_cont_min := {proc_id  $\mapsto$  idd}  $\triangleleft$  app_knobs_cont_min
  act3 : app_knobs_cont_max := {proc_id  $\mapsto$  idd}  $\triangleleft$  app_knobs_cont_max
  act4 : app_knobs_cont_value := {proc_id  $\mapsto$  idd}  $\triangleleft$  app_knobs_cont_value
END

PRIME_API_APP_MON_DISC_REG  $\triangleq$ 
STATUS
  ordinary
REFINES
  PRIME_API_APP_MON_DISC_manage
ANY
  proc_id
  mon
  idd // app knob id
  minn
  maxx
WHERE
  grd1 : proc_id  $\in$  pid_t  $\wedge$  proc_id  $\in$  app_sockets
  grd2 : mon  $\in$  app_mons_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\notin$  app_mons_disc
  grd3 : mon  $\in$  app_mons_disc_t  $\wedge$  proc_id  $\mapsto$  idd  $\in$  app_mons_disc  $\wedge$  minn < maxx
THEN
  act1 : app_mons_disc := app_mons_disc  $\cup$  {proc_id  $\mapsto$  idd}
  act2 : app_mons_disc_min := app_mons_disc_min  $\cup$  { (proc_id  $\mapsto$  idd)  $\mapsto$  minn }
  act3 : app_mons_disc_max := app_mons_disc_max  $\cup$  { (proc_id  $\mapsto$  idd)  $\mapsto$  maxx }
END

PRIME_API_APP_MON_CONT_REG  $\triangleq$ 
STATUS

```

```

ordinary
REFINES
PRIME_API_APP_MON_CONT_manage
ANY
proc_id
mon      //
idd
minn
maxx
WHERE
grd1  :  proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
grd2  :  mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∉ app_mons_cont
grd3  :  mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ minn < maxx
THEN
act1  :  app_mons_cont := app_mons_cont ∪ {proc_id ↦ idd}
act2  :  app_mons_cont_min := app_mons_cont_min ∪ { (proc_id ↦ idd) ↦ minn }
act3  :  app_mons_cont_max := app_mons_cont_max ∪ { (proc_id ↦ idd) ↦ maxx }
END

PRIME_API_APP_MON_DISC_MIN  ≐
STATUS
ordinary
ANY
proc_id
mon
idd
minn
maxx
val
WHERE
grd1  :  mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc
grd2  :  mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc ∧ maxx = app_mons_disc_max
        (proc_id ↦ idd) ∧ minn < maxx
grd3  :  mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc ∧ val = app_mons_disc_value
        (proc_id ↦ idd) ∧ minn ≤ val
THEN
act1  :  app_mons_disc_min(proc_id ↦ idd) := minn
END

PRIME_API_APP_MON_CONT_MIN  ≐
STATUS
ordinary
ANY
proc_id
mon
idd
minn
maxx
val
WHERE
grd1  :  mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont
grd2  :  mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ maxx = app_mons_cont_max
        (proc_id ↦ idd) ∧ minn < maxx
grd3  :  mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ val = app_mons_cont_value
        (proc_id ↦ idd) ∧ minn ≤ val
THEN
act1  :  app_mons_cont_min(proc_id ↦ idd) := minn
END

PRIME_API_APP_MON_DISC_MAX  ≐
STATUS
ordinary
ANY
proc_id
mon

```

```

idd
minn
maxx
val
WHERE
  grd1 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc
  grd2 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc ∧ minn = app_mons_disc_min
        (proc_id ↦ idd) ∧ maxx > minn
  grd3 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc ∧ val = app_mons_disc_value
        (proc_id ↦ idd) ∧ maxx ≥ val
THEN
  act1 : app_mons_disc_max(proc_id ↦ idd) := maxx
END

```

**PRIME\_API\_APP\_MON\_CONT\_MAX** ≐

**STATUS**

**ordinary**

**ANY**

```

proc_id
mon
idd
minn
maxx
val

```

**WHERE**

```

  grd1 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont
  grd2 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ minn = app_mons_cont_min
        (proc_id ↦ idd) ∧ maxx > minn
  grd3 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ val = app_mons_cont_value
        (proc_id ↦ idd) ∧ maxx ≥ val

```

**THEN**

```

  act1 : app_mons_cont_max(proc_id ↦ idd) := maxx

```

**END**

**PRIME\_API\_APP\_MON\_DISC\_WEIGHT** ≐

**STATUS**

**ordinary**

**ANY**

```

proc_id
mon
idd
minn
maxx
weight

```

**WHERE**

```

  grd1 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc
  mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc ∧ minn = app_mons_disc_min
  grd2 : (proc_id ↦ idd) ∧ maxx = app_mons_disc_max
        (proc_id ↦ idd) ∧ minn = MIN_INFINITY ∧ maxx = MAX_INFINITY ∧ weight ≠ 0

```

**THEN**

```

  act1 : app_mons_disc_weight(proc_id ↦ idd) := weight

```

**END**

**PRIME\_API\_APP\_MON\_CONT\_WEIGHT** ≐

**STATUS**

**ordinary**

**ANY**

```

proc_id
mon
idd
minn
maxx
weight

```

**WHERE**

```

  grd1 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont

```

```

    grd2 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ minn = app_mons_cont_min
          (proc_id ↦ idd) ∧ maxx = app_mons_cont_max
          (proc_id ↦ idd) ∧ minn = MIN_INFINITY ∧ maxx = MAX_INFINITY ∧ weight ≠ 0
  THEN
    act1 : app_mons_cont_weight(proc_id ↦ idd) := weight
  END

```

**PRIME\_API\_APP\_MON\_DISC\_SET**  $\triangleq$

**STATUS**

ordinary

**ANY**

```

proc_id
mon
idd
minn
maxx
val

```

**WHERE**

```

    grd1 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc
    grd2 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc ∧ minn = app_mons_disc_min
          (proc_id ↦ idd) ∧ minn ≤ val
    grd3 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc ∧ maxx = app_mons_disc_max
          (proc_id ↦ idd) ∧ maxx ≥ val

```

**THEN**

```

    act1 : app_mons_disc_value(proc_id ↦ idd) := val

```

**END**

**PRIME\_API\_APP\_MON\_CONT\_SET**  $\triangleq$

**STATUS**

ordinary

**ANY**

```

proc_id
mon
idd
minn
maxx
val

```

**WHERE**

```

    grd1 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont
    grd2 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ minn = app_mons_cont_min
          (proc_id ↦ idd) ∧ minn ≤ val
    grd3 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont ∧ maxx = app_mons_cont_max
          (proc_id ↦ idd) ∧ maxx ≥ val

```

**THEN**

```

    act1 : app_mons_cont_value(proc_id ↦ idd) := val

```

**END**

**PRIME\_API\_APP\_MON\_DISC\_DEREG**  $\triangleq$

**STATUS**

ordinary

**REFINES**

PRIME\_API\_APP\_MON\_DISC\_DEREG

**ANY**

```

proc_id
mon
idd

```

**WHERE**

```

    grd1 : mon ∈ app_mons_disc_t ∧ proc_id ↦ idd ∈ app_mons_disc

```

**THEN**

```

    act1 : app_mons_disc := app_mons_disc \ {proc_id ↦ idd}
    act2 : app_mons_disc_min := {proc_id ↦ idd} ≺ app_mons_disc_min
    act3 : app_mons_disc_max := {proc_id ↦ idd} ≺ app_mons_disc_max
    act4 : app_mons_disc_weight := {proc_id ↦ idd} ≺ app_mons_disc_weight
    act5 : app_mons_disc_value := {proc_id ↦ idd} ≺ app_mons_disc_value

```

**END**

```

PRIME_API_APP_MON_CONT_DEREG  ≐
STATUS
  ordinary
REFINES
  PRIME_API_APP_MON_CONT_DEREG
ANY
  proc_id
  mon
  idd
WHERE
  grd1 : mon ∈ app_mons_cont_t ∧ proc_id ↦ idd ∈ app_mons_cont
THEN
  act1 : app_mons_cont := app_mons_cont \ {proc_id ↦ idd}
  act2 : app_mons_cont_min := {proc_id ↦ idd} ≪ app_mons_cont_min
  act3 : app_mons_cont_max := {proc_id ↦ idd} ≪ app_mons_cont_max
  act4 : app_mons_cont_weight := {proc_id ↦ idd} ≪ app_mons_cont_weight
  act5 : app_mons_cont_value := {proc_id ↦ idd} ≪ app_mons_cont_value
END

PRIME_API_APP_DEREG  ≐
extended
STATUS
  ordinary
REFINES
  PRIME_API_APP_DEREG
ANY
  proc_id
WHERE
  grd1 : proc_id ∈ pid_t ∧ proc_id ∈ app_sockets
  grd2 : ran(app_knobs_disc) ⊆ app_knobs_disc_t ∧ app_knobs_disc[{proc_id}] = ∅
  grd3 : ran(app_knobs_cont) ⊆ app_knobs_cont_t ∧ app_knobs_cont[{proc_id}] = ∅
  grd4 : ran(app_mons_disc) ⊆ app_mons_disc_t ∧ app_mons_disc[{proc_id}] = ∅
  grd5 : ran(app_mons_cont) ⊆ app_mons_cont_t ∧ app_mons_cont[{proc_id}] = ∅
THEN
  act1 : app_sockets := app_sockets \ {proc_id}
  act2 : app_knobs_disc := {proc_id} ≪ app_knobs_disc
  act3 : app_knobs_cont := {proc_id} ≪ app_knobs_cont
  act4 : app_mons_disc := {proc_id} ≪ app_mons_disc
  act5 : app_mons_cont := {proc_id} ≪ app_mons_cont
END

PRIME_API_DEV_RTM  ≐
extended
STATUS
  ordinary
REFINES
  PRIME_API_DEV_RTM
BEGIN
  skip
END

```

END