

## Tarefa Básica

$$\textcircled{1} \begin{cases} ax+4y=1 \\ x+2y=b \end{cases} \quad D = \begin{vmatrix} a & 4 \\ 1 & 2 \end{vmatrix} = 2a-4$$

4                  2a

$$a=2=0$$

$$b = \frac{1}{2} = 0$$

$$Dx = \begin{vmatrix} 1 & 4 \\ b & 2 \end{vmatrix} = 2-4b$$

4b                  2

$$\frac{Dx}{D} = \frac{2a-4}{2-4b} = \frac{0}{0}$$

$$D \neq 0 \rightarrow \text{SPD}$$

$$D = 0 \rightarrow \text{SPI ou SI}$$

↓

$$Dx=0$$

$$Dy=0$$

↓

$$Dx \neq 0$$

$$Dy \neq 0$$

$$\textcircled{2} \begin{cases} x+ky=1 \\ kx+y=1-k \end{cases} \quad \begin{matrix} -k \\ \rightarrow \end{matrix} \begin{pmatrix} 1 & k & : & 1 \\ k & 1 & : & 1-k \end{pmatrix} \quad \begin{pmatrix} 0 & -k^2+1 & : & -2k+1 \end{pmatrix}$$

$k=-1 \quad y = \frac{-2k+1}{0} \quad y = \frac{-2k+1}{(-k^2+1)}$

↑                                  ↑

SI                                   $k \neq 1 \text{ ou } k \neq -1$

SPD

$$\textcircled{3} \begin{cases} x+2y+cz=1 \\ y+z=2 \\ 3x+2y+2z=-1 \end{cases}$$

$$a) A = \begin{vmatrix} 1 & 2 & c & | & 1 & 2 \\ 0 & 1 & 1 & | & 0 & 1 \\ 3 & 2 & 2 & | & 3 & 2 \end{vmatrix}$$

$3c+2+0$

$2+6+c$

$\det = 8-3c-2$

$\det = 6-3c$

$$b) 6-3c \neq 0$$

$$\frac{6}{-3} = c \quad -3 \rightarrow -2=c$$

$$\begin{aligned}
 & 0 + 0 + (-12k) = -12k \\
 & \textcircled{4} \begin{cases} x - y = k \\ 12x + ky + z = 1 \\ 36x + kz = 2 \end{cases} \quad D = \begin{vmatrix} 1 & -1 & 0 & 1 & -1 \\ 12 & -k & 1 & 12 & -k \\ 36 & 0 & k & 36 & 0 \end{vmatrix} = \det = k^2 - 36 - 12k \\
 & \quad \quad \quad -x^2 + (-36) + 0 = -x^2 - 36
 \end{aligned}$$

$$D \neq 0 \leadsto -k^2 - 36 - 12k \cdot (-1)$$

$$k^2 + 12k + 36$$

$$\begin{array}{c}
 \uparrow \quad \uparrow \\
 S \quad P
 \end{array}$$

$$6 \cdot 6 = 36 \rightarrow 6 + 6 = 12$$

$$6 + 6 = 12$$

$$6 \cdot 6 = 36$$

$$k \neq 6$$

## Parte 2 - Tarifa Básica

$$\textcircled{1} \begin{bmatrix} 1 & 7 \\ 7 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \end{bmatrix} = k \cdot \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\begin{cases} x + 7y = kx \\ 7x + y = ky \end{cases}$$

$$D = \begin{vmatrix} 1 & 7 \\ 7 & 1 \end{vmatrix} = 1 - 49 = -48$$

$$D_x = \begin{vmatrix} k & 7 \\ k & 1 \end{vmatrix} = k - 7k = -6k$$

$$\begin{matrix} -7 & (1 & 7 : k) \\ \hookrightarrow & (7 & 1 : k) \end{matrix} \quad \begin{pmatrix} 1 & 0 & -48 : -6k \end{pmatrix}$$

$$\hookrightarrow z = -48 = 6k$$

$$D \neq 0 \rightarrow -48 \neq 6k$$

$$-48 = k$$

$$\frac{-48}{-6} \rightarrow 8 = k$$

$$\textcircled{2} \begin{cases} 3x + 4y - z = 0 \\ 2x - y + 3z = 0 \\ x + y = 0 \end{cases}$$

$$D = \begin{vmatrix} 3 & 4 & -1 \\ 2 & -1 & 3 \\ 1 & 1 & 0 \end{vmatrix} \begin{vmatrix} 3 & 4 \\ 2 & -1 \\ 1 & 1 \end{vmatrix} \quad \begin{matrix} 1+9+0=10 \\ \det=10-10=0 \\ 0+12+(-2)=10 \end{matrix}$$

$$D_x = \begin{vmatrix} 0 & 4 & -1 \\ 0 & -1 & 3 \\ 0 & 1 & 0 \end{vmatrix} \begin{vmatrix} 0 & 4 \\ 0 & -1 \\ 0 & 1 \end{vmatrix} \quad \begin{matrix} 0+0+0=0 \\ \det_x=0 \\ 0+0+0=0 \end{matrix}$$

$$D_y = \begin{vmatrix} 3 & 0 & -1 \\ 2 & 0 & 3 \\ 1 & 0 & 0 \end{vmatrix} \begin{vmatrix} 3 & 0 \\ 2 & 0 \\ 1 & 0 \end{vmatrix} \quad \begin{matrix} 0+0+0=0 \\ \det_y=0 \\ 0+0+0=0 \end{matrix}$$



$$0+0+0=0$$

$$Dg = \begin{vmatrix} 3 & 4 & 0 & 3 & 4 \\ 2 & -1 & 0 & 2 & -1 \\ 1 & 1 & 0 & 1 & 1 \end{vmatrix} \det g = 0$$

$$0+0+0=0$$

$$x = \frac{Dx}{D} = \frac{0}{0} \quad y = \frac{Dy}{D} = \frac{0}{0} \quad z = \frac{Dz}{D} = \frac{0}{0}$$

SPI

$$\textcircled{3} \begin{cases} x+y+z=0 \\ kx+3y+4z=0 \\ x+ky+3z=0 \end{cases}$$

$$D = \begin{vmatrix} 1 & 1 & 1 & 1 & 1 \\ k & 3 & 4 & k & 3 \\ 1 & k & 3 & 1 & k \end{vmatrix} \begin{matrix} 3+k+3k=3+7k \\ 13+k^2-3+7k \\ k^2+7k+10=0 \end{matrix}$$

$$9+4+k^2=13+k^2$$

$$2+5=7$$

$$2 \cdot 5 = 10$$

Soma de k

$$2+5=7$$

$$\textcircled{4} \begin{cases} x+kz=0 \\ kx+y=0 \\ x+ky=0 \end{cases} \begin{matrix} Dx=0 \\ Dy=0 \\ Dz=0 \end{matrix} \begin{cases} 1 & 0 & k=0 \\ k & 1 & 0=0 \\ 1 & k & 0=0 \end{cases}$$

$$D = \begin{vmatrix} 1 & 0 & k & 1 & 0 \\ k & 1 & 0 & k & 1 \\ 1 & k & 0 & 1 & k \end{vmatrix} \begin{matrix} k+0+0=k \\ k^3-k \\ 0+0+k^3=k^3 \end{matrix}$$

$$k^3-k$$

$$k(k-1)(k+1)=0$$

$$k \neq 0, k \neq 1, k \neq -1$$

$$k = -1, k = 0, k = 1$$

$$V = \{k \in \mathbb{R} / k \neq 0, k \neq 1, k \neq -1\}$$

$$\textcircled{5} \begin{cases} -x + 2y - 3 = 0 \\ 3x - y + 3 = 0 \\ 2x - 4y + 6 = 0 \end{cases}$$

$$D = \begin{vmatrix} -1 & 2 & -3 \\ 3 & -1 & 3 \\ 2 & -4 & 6 \end{vmatrix} \begin{vmatrix} -1 & 2 \\ 3 & -1 \end{vmatrix} = 54 - 18 = 36$$

$$6 + 12 + 36 = 54$$

$$-6 + (-12) + 36 = 18$$

$$D \neq 0 \rightarrow 36$$