- 1. Text 12.2 Modified. Suppose that the $m \times n$ matrix Q has orthonormal columns.
 - a) Why do you immediately know that $m \ge n$ and hence Q is tall or square?
 - b) Show that $\hat{x} = Q^T b$ is the vector that minimizes $J(x) = ||Qx b||^2$. Do this by setting up the normal equations directly.
- 2. Supplemental 12.6 Hint: Your matrix A will be 6×4 and will have a lot of 0's and 1's.
- **3.** Suppose we want to compute the coefficients of the quadratic $p(t) = c_1 + c_2t + c_3t^2$ that is the least squares fit to the following (t, y) data points: (0, 0), (1, 8), (3, 8), (4, 20).
 - 1. Formulate the problem in the form of Ac = b. That is, find the matrix A and the vector b. You don't need to solve this system.
 - 2. Now formulate the normal equation $A^tAc = A^tb$ that you would use to find these best-fit coefficients. Again, do not solve the system. (But don't worry, there is a Julia problem that tackles this!)
- **4.** Text: problem 12.4. Hint: you will find that the square roots of the weights are important. For part (b), remember that the columns of C are linearly independent if and only if the only solution of Cx = 0 is x = 0.