Name:

1. Consider the vector-valued function

$$\mathbf{r}(t) = t^3 \mathbf{i} + e^{2t} \mathbf{j} + \cos(2t) \mathbf{k}$$

Compute $\mathbf{r}'(t)$

2. The function in the problem 1 desribes the position of a particle as a function of time. The i and j directions are horizontal and the k direction is vertical. List 3 different times when the particle is moving only in a horizontal direction.

Vertical component of velocity: -2sin(26)This varishes at t=0, $\pi/2$, $\pi/3$.

3. A vector-valued function has derivative

$$\mathbf{r}'(t) = te^{t^2}\mathbf{i} + \sin(3t)\mathbf{j}.$$

We are given the additional data $\mathbf{r}(0) = 2\mathbf{j}$. Determine $\mathbf{r}(t)$.

$$\vec{r}(\ell) = \int \{e^{\ell^2} \hat{c} + \int sm(2\ell) \hat{c} + \hat{c} \}$$

$$= \frac{1}{2} e^{\ell^2} \hat{c} - \frac{1}{3} \cos(3\ell) \hat{c} + \hat{c}$$

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$$= \frac{1}{2} \hat{c} - \frac{1}{3} \hat{c} + \hat{c} \Rightarrow \hat{c} = -\frac{1}{2} \hat{c} + \frac{7}{3} \hat{c}$$

$$\vec{r}(\ell) = \frac{1}{3} \left(e^{\ell^2} - 1 \right) \hat{c} + \left(\frac{7}{3} - \frac{1}{3} \cos(3\ell) \right) \hat{c}$$

4. Find an equation for the tangent line of the curve $\mathbf{r}(t) = e^{2t}\mathbf{i} + e^{t}\mathbf{j}$.

$$\vec{r}(0) = \hat{c} + \hat{c}$$

$$\vec{r}'(t) = 2te^{2t}\hat{c} + e^{t}\hat{c}$$

$$\vec{r}'(0) = 2\hat{c} + \hat{c}$$