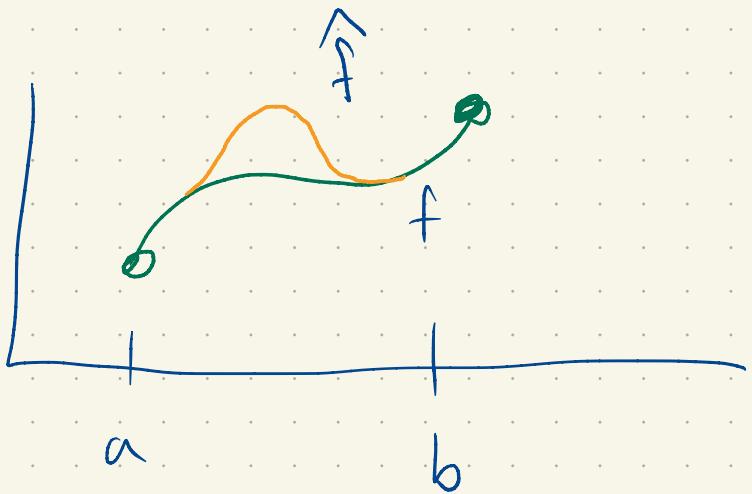


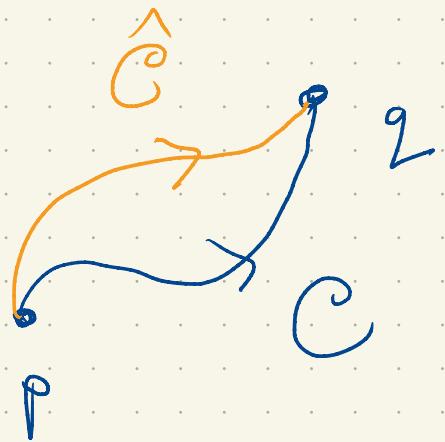
$$\iint_S \vec{\nabla} \times \vec{E} \cdot \hat{n} dS = \oint_C \vec{E} \cdot d\vec{r}$$



$$\int_a^b f'(x) dx = f(b) - f(a)$$

$$\int_a^b \hat{f}'(x) dx = \hat{f}(b) - \hat{f}(a)$$

$$= f(b) - f(a)$$

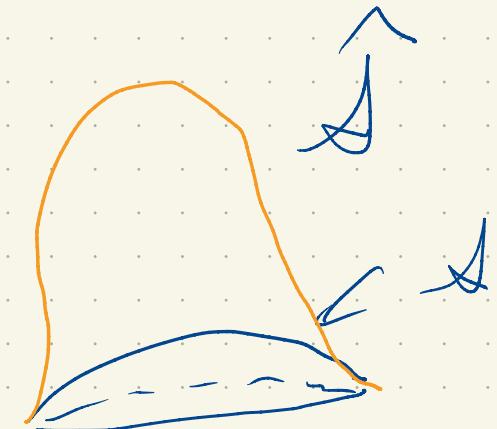


$$\int_C \vec{\nabla} f \cdot d\vec{r} = f(z) - f(p)$$

FTLI

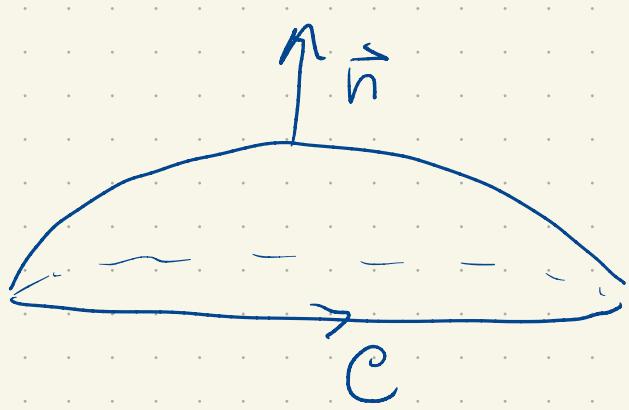
$$\int_C \vec{\nabla} f \cdot d\vec{r} \text{ vs } \int_{\hat{C}} \vec{\nabla} f \cdot d\vec{r}$$

=



$$\iint_S (\vec{\nabla}_x \vec{z}) \cdot \vec{n} dS = \int_C \vec{z} \cdot d\vec{r}$$

$$\iint_S (\vec{\nabla}_x \vec{z}) \cdot \vec{n} dS \text{ vs } \iint_S (\vec{\nabla}_x \vec{z}) \cdot \vec{n} dS$$



$$x^2 + y^2 + z^2 = 4$$

$$z \geq \sqrt{3}$$

$$z = \sqrt{3}$$

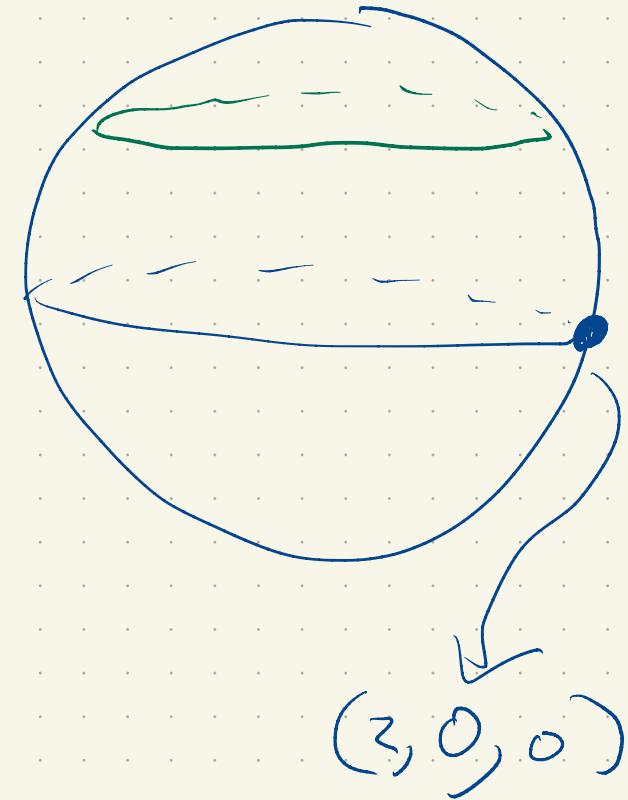
$$x^2 + y^2 \leq 1$$

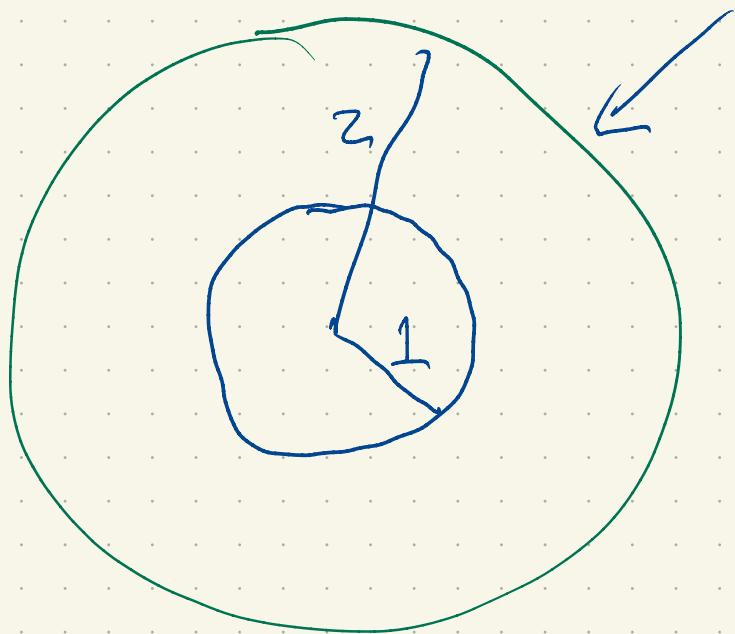
$$\vec{F} = \langle xz, yz + x, xy \rangle$$

$$\iint_{\text{surf}} (\vec{\nabla} \times \vec{F}) \cdot \vec{n} \, dS = \oint_{C \text{ loop}} \vec{F} \cdot d\vec{r}$$

$$\vec{r}(u, v) = \langle u, v, \sqrt{4 - u^2 - v^2} \rangle$$

$$z = \pm \sqrt{4 - x^2 - y^2}$$





$$u^2 + v^2 \leq 1$$

$$\vec{r}_u$$

$$\vec{r}_v$$

$$\vec{r}_u \times \vec{r}_v = \left\langle \frac{u}{\sqrt{1-u^2-v^2}}, \frac{v}{\sqrt{1-u^2-v^2}}, 1 \right\rangle$$

↑  
points perp. to surface

$$\vec{\nabla}_x \vec{F} = \langle x-y, x-y, 1 \rangle$$

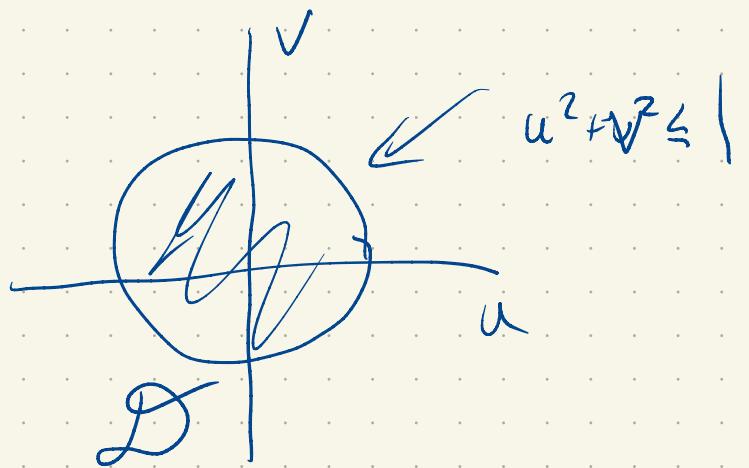
$$(\vec{\nabla}_x \vec{F})(\vec{r}(u, v)) = \langle u-v, u-v, 1 \rangle$$

$$\iint_S (\vec{\nabla}_x \vec{F}) \cdot \vec{n} \, dS = \iint_D (\vec{\nabla}_x \vec{F})(\vec{r}(u, v)) \cdot (\vec{r}_u \times \vec{r}_v) \, du \, dv$$

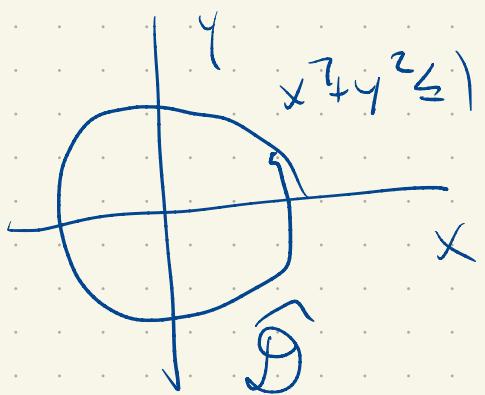
↑ region of  $u$ 's vs  $v$ 's that  
describes vector  $\vec{S}$

$$u^2 + v^2 \leq 1$$

$$= \pi$$

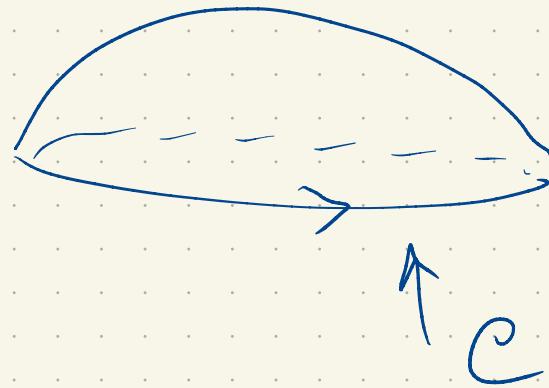


$$\iint_D u^2 dA(u, v)$$



$$\iint_{\hat{D}} x dA(x, y)$$

$$\int_C \vec{F} \cdot d\vec{r}$$



$$x^2 + y^2 = 1$$

$$z = \sqrt{3}$$

$$\vec{\sigma}(t) = \langle \cos(t), \sin(t), \sqrt{3} \rangle$$

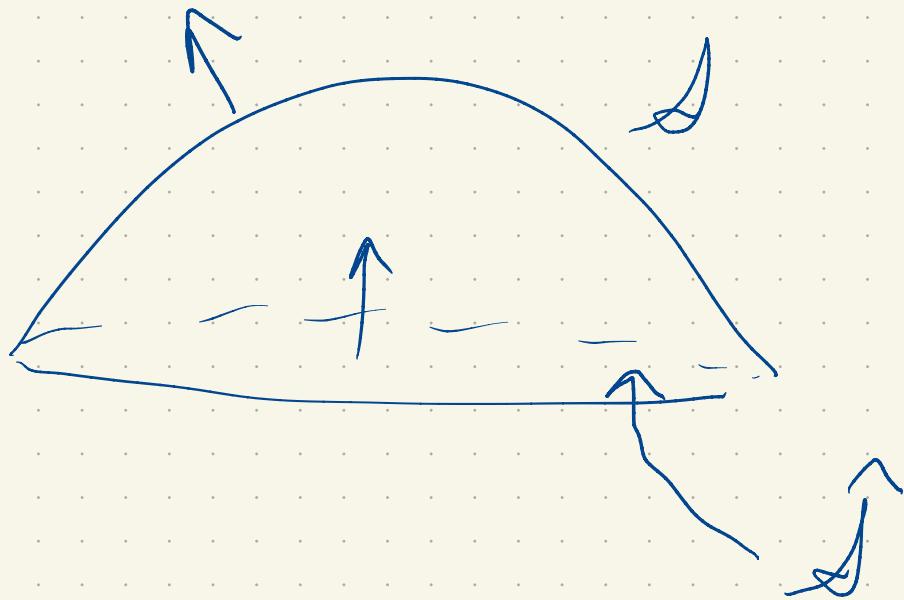
$$0 \leq t \leq 2\pi$$

$$\vec{F} = \langle xz, yz+x, xy \rangle$$

$$\vec{F}(\vec{\sigma}(t)) = \langle \sqrt{3}\cos(t), \sqrt{3}\sin(t) + \cos(t), \cos(t)\sin(t) \rangle$$

$$\vec{\sigma}'(t) = \langle -\sin(t), \cos(t), 0 \rangle$$

$$\int_C \vec{F} \cdot d\vec{r} = \int_0^{2\pi} \underbrace{\vec{F}(\vec{\sigma}(t)) \cdot \vec{\sigma}'(t)}_{\vec{F}(\vec{\sigma}(t)) \cdot \langle -\sin(t), \cos(t), 0 \rangle} dt = \pi$$



$$\iint_S (\vec{\nabla} \times \vec{F}) \cdot \vec{n} dS = \pi$$

$$\iint_S (\vec{\nabla} \times \vec{F}) \cdot \vec{n} dS = -\pi$$

$$\vec{r}(u, v) = \langle u, v, \sqrt{3} \rangle$$

$$\vec{\nabla} \times \vec{F} = \langle x-y, x-y, 1 \rangle$$

$$\vec{r}_u = \langle 1, 0, 0 \rangle$$

$$\vec{\nabla} \times \vec{F}(\vec{r}(u, v)) = \langle u-v, u-v, 1 \rangle$$

$$\vec{r}_v = \langle 0, 1, 0 \rangle$$

$$\vec{\nabla} \times \vec{F}(\vec{r}(u, v)) \cdot (\vec{r}_u \times \vec{r}_v) = 1$$

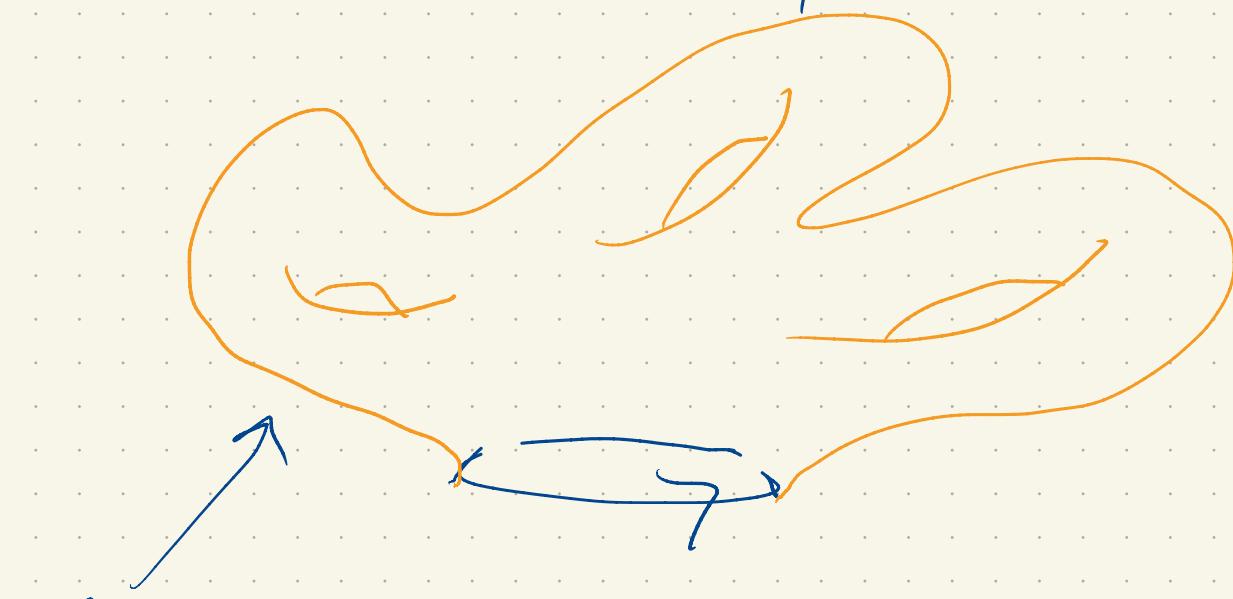
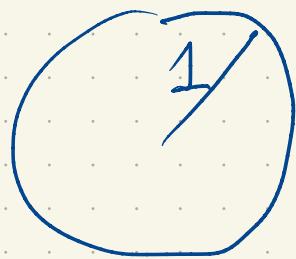
$$\vec{r}_u \times \vec{r}_v = \langle 0, 0, 1 \rangle$$

$$u^2 + v^2 \leq 1$$

$$\iint_D (\vec{\nabla} \times \vec{F}) \cdot \vec{n} dS = \iint_D 1 du dv = \pi$$

D

$$u^2 + v^2 \leq 1$$



$$\iint (\vec{\nabla} \times \vec{F}) \cdot \vec{n} dS = \pi$$

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$$\int_C \mathbf{F} \cdot d\mathbf{r}$$