

# Matrice

## MATEMATIKA ZA EKONOMISTE 1

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FOI, Varaždin

# Sadržaj

prvi zadatak

drugi zadatak

treći zadatak

četvrti zadatak

peti zadatak

šesti zadatak

sedmi zadatak

osmi zadatak

deveti zadatak

deseti zadatak

**prvi zadatak**

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## Zadatak 1

Napišite matricu  $A = [a_{ij}]$  tipa  $(3, 4)$  ako je

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

## Rješenje

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$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix}$$

## Rješenje

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$$a_{11} =$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$



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$$a_{11} = \log_2(1 + 1)$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

## Rješenje

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} & & & \\ & & & \\ & & & \end{bmatrix}$$

$$a_{11} = \log_2(1 + 1) = \log_2 2$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

## Rješenje

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$$a_{11} = \log_2(1 + 1) = \log_2 2 = 1$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

## Rješenje

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 \\ \\ \end{bmatrix}$$

$$a_{11} = \log_2(1 + 1) = \log_2 2 = 1$$

$$a_{12} =$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

## Rješenje

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$$a_{11} = \log_2(1 + 1) = \log_2 2 = 1$$

$$a_{12} = \log_2(1 + 2) = \log_2 3$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

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## Rješenje

$$\log_a a^x = x$$

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$$a_{13} = \log_2(1 + 3) = \log_2 4$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

Rješenje  $\log_2 4 =$

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$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i + j), & \text{ako je } i \leq j \end{cases}$$

## Rješenje

$$\log_2 4 = \log_2 2^2$$

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 & \log_2 3 & & \end{bmatrix}$$

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**Rješenje**  $\log_2 4 = \log_2 2^2 = 2$

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$$a_{11} = \log_2 (1 + 1) = \log_2 2 = 1$$

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$$a_{11} = \log_2 (1 + 1) = \log_2 2 = 1$$

$$a_{12} = \log_2 (1 + 2) = \log_2 3$$

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$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2 (i + j), & \text{ako je } i \leq j \end{cases}$$

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$$a_{21} =$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2 (i + j), & \text{ako je } i \leq j \end{cases}$$

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$$a_{21} = \cos \frac{2\pi}{2}$$

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$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2 (i + j), & \text{ako je } i \leq j \end{cases}$$

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$$a_{11} = \log_2 (1 + 1) = \log_2 2 = 1$$

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$$a_{14} = \log_2 (1 + 4) = \log_2 5$$

$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi = -1$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2 (i + j), & \text{ako je } i \leq j \end{cases}$$

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$$a_{14} = \log_2 (1 + 4) = \log_2 5$$

$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi = -1$$

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$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2 (i + j), & \text{ako je } i \leq j \end{cases}$$

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$$a_{14} = \log_2 (1 + 4) = \log_2 5$$

$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi = -1$$

$$a_{22} = \log_2 (2 + 2) = \log_2 4$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2 (i + j), & \text{ako je } i \leq j \end{cases}$$

## Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

$$\log_a a^x = x$$

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$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2 (i + j), & \text{ako je } i \leq j \end{cases}$$



Rješenje

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$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i+j), & \text{ako je } i \leq j \end{cases} \quad a_{23} =$$

$$a_{14} = \log_2(1+4) = \log_2 5$$

$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi = -1$$

$$a_{22} = \log_2(2+2) = \log_2 4 = 2$$

Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

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$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i+j), & \text{ako je } i \leq j \end{cases}$$

$$a_{23} = \log_2(2+3)$$

$$a_{14} = \log_2(1+4) = \log_2 5$$

$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi = -1$$

$$a_{22} = \log_2(2+2) = \log_2 4 = 2$$

Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 & \log_2 3 & 2 & \log_2 5 \\ -1 & 2 & \log_2 5 & \end{bmatrix}$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i+j), & \text{ako je } i \leq j \end{cases}$$

$$a_{23} = \log_2(2+3) = \log_2 5$$

$$a_{14} = \log_2(1+4) = \log_2 5$$

$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi = -1$$

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Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 & \log_2 3 & 2 & \log_2 5 \\ -1 & 2 & \log_2 5 & \end{bmatrix}$$

$$a_{ij} = \begin{cases} \cos \frac{i\pi}{2}, & \text{ako je } i > j \\ \log_2(i+j), & \text{ako je } i \leq j \end{cases}$$

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$$a_{24} =$$

$$a_{14} = \log_2(1+4) = \log_2 5$$

$$a_{21} = \cos \frac{2\pi}{2} = \cos \pi = -1$$

$$a_{22} = \log_2(2+2) = \log_2 4 = 2$$

Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 & \log_2 3 & 2 & \log_2 5 \\ -1 & 2 & \log_2 5 & \end{bmatrix}$$

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Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

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Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

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Rješenje

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Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

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**Rješenje**

$$\log_2 4 = \log_2 2^2 = 2$$

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# Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

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$$a_{22} = \log_2(2+2) = \log_2 4 = 2$$

$$a_{34} =$$



# Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 & \log_2 3 & 2 & \log_2 5 \\ -1 & 2 & \log_2 5 & \log_2 6 \\ 0 & 0 & \log_2 6 & \end{bmatrix}$$

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$$a_{22} = \log_2(2+2) = \log_2 4 = 2$$

$$a_{34} = \log_2(3+4)$$

# Rješenje

$$\log_2 4 = \log_2 2^2 = 2$$

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 & \log_2 3 & 2 & \log_2 5 \\ -1 & 2 & \log_2 5 & \log_2 6 \\ 0 & 0 & \log_2 6 & \log_2 7 \end{bmatrix}$$

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$$a_{22} = \log_2(2+2) = \log_2 4 = 2$$

$$a_{34} = \log_2(3+4) = \log_2 7$$

**Rješenje**

$$\log_2 4 = \log_2 2^2 = 2$$

$$\log_a a^x = x$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \end{bmatrix} = \begin{bmatrix} 1 & \log_2 3 & 2 & \log_2 5 \\ -1 & 2 & \log_2 5 & \log_2 6 \\ 0 & 0 & \log_2 6 & \log_2 7 \end{bmatrix}$$

$$a_{11} = \log_2 (1 + 1) = \log_2 2 = 1$$

$$a_{23} = \log_2 (2 + 3) = \log_2 5$$

$$a_{12} = \log_2 (1 + 2) = \log_2 3$$

$$a_{24} = \log_2 (2 + 4) = \log_2 6$$

$$a_{13} = \log_2 (1 + 3) = \log_2 4 = 2$$

$$a_{31} = \cos \frac{3\pi}{2} = 0$$

$$a_{14} = \log_2 (1 + 4) = \log_2 5$$

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$$a_{22} = \log_2 (2 + 2) = \log_2 4 = 2$$

$$a_{34} = \log_2 (3 + 4) = \log_2 7$$

## **drugi zadatak**

---

## Zadatak 2

*Dopunite matricu*

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

*tako da bude*

- a) *simetrična,*
- b) *antisimetrična.*

## Zadatak 2

*Dopunite matricu*

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

*tako da bude*

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## Rješenje

## Zadatak 2

*Dopunite matricu*

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

*tako da bude*

- a) *simetrična,*
- b) *antisimetrična.*

## Rješenje

a)  $a_{ij} = a_{ji}$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

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a)  $a_{ij} = a_{ji}$

$$\begin{bmatrix} & -1 & \\ e & 3 & \end{bmatrix}$$



## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

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- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$

$$\begin{bmatrix} & -1 & \\ -1 & & \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$

$$\begin{bmatrix} & -1 & e \\ -1 & & \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$

$$\begin{bmatrix} & -1 & e \\ -1 & & 3 \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

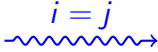
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} & -1 & e \\ -1 & & 3 \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

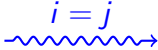
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & & 3 \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

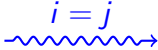
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

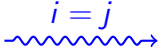
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix}$$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji} \xrightarrow{i=j} a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$



## Zadatak 2

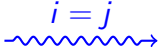
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji}$

## Zadatak 2

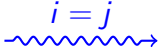
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji}$

$$\begin{bmatrix} & -1 & \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$   $\xrightarrow{i=j}$   $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji}$

$$\begin{bmatrix} & -1 & \\ 1 & & \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

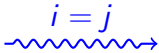
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji}$

$$\begin{bmatrix} & -1 & -e \\ 1 & & \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

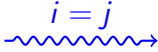
Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji}$    $a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji}$

$$\begin{bmatrix} & -1 & -e \\ 1 & & -3 \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji} \xrightarrow{i=j} a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji} \xrightarrow{i=j} a_{ii} = -a_{ii}$

$$\begin{bmatrix} & -1 & -e \\ 1 & & -3 \\ e & 3 & \end{bmatrix}$$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji} \xrightarrow{i=j} a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji} \xrightarrow{i=j} a_{ii} = -a_{ii}$

$$\begin{bmatrix} & -1 & -e \\ 1 & & -3 \\ e & 3 & \end{bmatrix} \quad 2a_{ii} = 0$$

## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

a) *simetrična*,

b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji} \xrightarrow{i=j} a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji} \xrightarrow{i=j} a_{ii} = -a_{ii}$

$$\begin{bmatrix} & -1 & -e \\ 1 & & -3 \\ e & 3 & \end{bmatrix} \quad \begin{aligned} 2a_{ii} &= 0 \\ a_{ii} &= 0 \end{aligned}$$



## Zadatak 2

Dopunite matricu

$$\begin{bmatrix} \cdot & -1 & \cdot \\ \cdot & \cdot & \cdot \\ e & 3 & \cdot \end{bmatrix}$$

tako da bude

- a) *simetrična*,
- b) *antisimetrična*.

## Rješenje

a)  $a_{ij} = a_{ji} \xrightarrow{i=j} a_{ii} = a_{ii}$

$$\begin{bmatrix} a & -1 & e \\ -1 & b & 3 \\ e & 3 & c \end{bmatrix} \quad a, b, c \in \mathbb{R}$$

b)  $a_{ij} = -a_{ji} \xrightarrow{i=j} a_{ii} = -a_{ii}$

$$\begin{bmatrix} 0 & -1 & -e \\ 1 & 0 & -3 \\ e & 3 & 0 \end{bmatrix} \quad \begin{aligned} 2a_{ii} &= 0 \\ a_{ii} &= 0 \end{aligned}$$

## treći zadatak

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### Zadatak 3

Odredite  $a, b \in \mathbb{R}$  tako da matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

bude

- a) gornje trokutasta,
- b) donje trokutasta.

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$a - b = 0$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$a - b = 0$$

$$a - 1 = 0$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$a - b = 0$$

$$a - 1 = 0$$

$$b - 1 = 0$$



a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \rightsquigarrow a = 1$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A =$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$



a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$a = 0$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$a = 0$$

$$b = 0$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$a = 0$$

$$b = 0$$

$$a + b = 0$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a = 0 \\ b = 0 \\ a + b = 0 \end{array} \right\}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a = 0 \\ b = 0 \\ a + b = 0 \end{array} \right\} \rightsquigarrow a = 0$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a = 0 \\ b = 0 \\ a + b = 0 \end{array} \right\} \begin{array}{l} \rightsquigarrow a = 0 \\ \rightsquigarrow b = 0 \\ \end{array}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a = 0 \\ b = 0 \\ a + b = 0 \end{array} \right\} \begin{array}{l} \rightsquigarrow a = 0 \\ \rightsquigarrow b = 0 \\ 0 + 0 = 0 \end{array}$$

a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a = 0 \\ b = 0 \\ a + b = 0 \end{array} \right\} \begin{array}{l} \rightsquigarrow a = 0 \\ \rightsquigarrow b = 0 \\ 0 + 0 = 0 \end{array}$$

$$A =$$



a) gornje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a - b = 0 \\ a - 1 = 0 \\ b - 1 = 0 \end{array} \right\} \begin{array}{l} 1 - 1 = 0 \\ \rightsquigarrow a = 1 \\ \rightsquigarrow b = 1 \end{array}$$

$$A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

b) donje trokutasta matrica

$$A = \begin{bmatrix} a^2 + 4b^2 & a & b \\ a - b & a^2 & a + b \\ a - 1 & b - 1 & b^2 \end{bmatrix}$$

$$\left. \begin{array}{l} a = 0 \\ b = 0 \\ a + b = 0 \end{array} \right\} \begin{array}{l} \rightsquigarrow a = 0 \\ \rightsquigarrow b = 0 \\ 0 + 0 = 0 \end{array}$$

$$A = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ -1 & -1 & 0 \end{bmatrix}$$

## čtvrti zadatak

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## Zadatak 4

Odredite  $a, b \in \mathbb{R}$  tako da matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

bude

- a) *gornje trokutasta,*
- b) *simetrična.*

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$a^2 - 9 = 0$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$a^2 - 9 = 0$$

$$a^2 + b = 0$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$a^2 - 9 = 0$$

$$a^2 + b = 0$$

$$b + 9 = 0$$



## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\}$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \rightsquigarrow b = -9$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \\ \text{~~~~~} \rightarrow b = -9 \end{array}$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow b = -9 \end{array}$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow b = -9 \end{array} \right\}$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow b = -9 \end{array} \right\} \text{~~~~~} \rightarrow a^2 = 9$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow b = -9 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 = 9 \\ a_1 = 3 \end{array}$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow b = -9 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 = 9 \\ a_1 = 3 \\ a_2 = -3 \end{array}$$



## Rješenje

a) gornje trokutasta matrica

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$$\left. \begin{array}{l} a^2 - 9 = 0 \\ a^2 + b = 0 \\ b + 9 = 0 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow a^2 - 9 = 0 \\ \text{~~~~~} \rightarrow b = -9 \end{array} \right\} \begin{array}{l} \text{~~~~~} \rightarrow a^2 = 9 \\ a_1 = 3 \\ a_2 = -3 \end{array}$$

$$a = 3$$

$$b = -9$$

## Rješenje

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$$a = 3$$

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$$B_1 =$$

## Rješenje

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## Rješenje

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$$a = -3$$

$$b = -9$$

$$B_2 =$$

## Rješenje

a) gornje trokutasta matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

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$$a = 3$$

$$b = -9$$

$$B_1 = \begin{bmatrix} 1 & 3 & -9 \\ 0 & 3 & 3 \\ 0 & 0 & 2 \end{bmatrix}$$

$$a = -3$$

$$b = -9$$

$$B_2 = \begin{bmatrix} 1 & -3 & -9 \\ 0 & 3 & -3 \\ 0 & 0 & 2 \end{bmatrix}$$

b) simetrična matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

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$$a^2 - 9 = a$$

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b) simetrična matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = a \\ a^2 + b = b \\ b + 9 = a \end{array} \right\}$$

b) simetrična matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = a \\ a^2 + b = b \\ b + 9 = a \end{array} \right\} \rightsquigarrow a^2 = 0$$

b) simetrična matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = a \\ a^2 + b = b \\ b + 9 = a \end{array} \right\} \begin{array}{l} \text{~~~~~} \\ \text{~~~~~} \\ \text{~~~~~} \end{array} \begin{array}{l} \text{~~~~~} \\ \text{~~~~~} \\ \text{~~~~~} \end{array} \begin{array}{l} a^2 = 0 \\ a = 0 \end{array}$$



b) simetrična matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

$$\left. \begin{array}{l} a^2 - 9 = a \\ a^2 + b = b \\ b + 9 = a \end{array} \right\} \begin{array}{l} \text{~~~~~} \\ \text{~~~~~} \\ \text{~~~~~} \end{array} \rightsquigarrow \begin{array}{l} a^2 = 0 \\ \boxed{a = 0} \end{array}$$

b) simetrična matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

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b) simetrična matrica

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nema rješenja

b) simetrična matrica

$$B = \begin{bmatrix} 1 & a & b \\ a^2 - 9 & 3 & a \\ a^2 + b & b + 9 & 2 \end{bmatrix}$$

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nema rješenja

Ne postoje  $a, b \in \mathbb{R}$  za koje bi matrica  $B$  bila simetrična matrica.

**peti zadatak**

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## Zadatak 5

*Zadane su matrice*

$$A = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \quad i \quad B = \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}.$$

*Odredite:*

- a)  $A^T$ ,
- b)  $BA$ ,
- c)  $AB$ .

## Zadatak 5

Zadane su matrice

$$A = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \quad i \quad B = \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}.$$

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**Rješenje**

## Zadatak 5

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Odredite:

- a)  $A^T$ ,
- b)  $BA$ ,
- c)  $AB$ .

### Rješenje

a)

$$A^T =$$



## Zadatak 5

Zadane su matrice

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Odredite:

- a)  $A^T$ ,
- b)  $BA$ ,
- c)  $AB$ .

### Rješenje

a)

$$A^T = \begin{bmatrix} & \\ & \\ & \end{bmatrix}$$

## Zadatak 5

Zadane su matrice

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Odredite:

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## Zadatak 5

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Zadane su matrice

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### Rješenje

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## Zadatak 5

Zadane su matrice

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Odredite:

- a)  $A^T$ ,
- b)  $BA$ ,
- c)  $AB$ .

### Rješenje

a)

$$A^T = \begin{bmatrix} 1 & 0 & 5 \\ 2 & -3 & 4 \end{bmatrix}$$

b)  $BA$

(2, 4)

## Zadatak 5

Zadane su matrice

$$A = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \quad i \quad B = \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}.$$

Odredite:

- a)  $A^T$ ,
- b)  $BA$ ,
- c)  $AB$ .

### Rješenje

a)

$$A^T = \begin{bmatrix} 1 & 0 & 5 \\ 2 & -3 & 4 \end{bmatrix}$$

b)  $BA$

$(2, 4) (3, 2)$

## Zadatak 5

Zadane su matrice

$$A = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \quad i \quad B = \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}.$$

Odredite:

- a)  $A^T$ ,
- b)  $BA$ ,
- c)  $AB$ .

### Rješenje

a)

$$A^T = \begin{bmatrix} 1 & 0 & 5 \\ 2 & -3 & 4 \end{bmatrix}$$

b)  $BA$

$(2, 4) (3, 2)$



## Zadatak 5

Zadane su matrice

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Odredite:

- a)  $A^T$ ,
- b)  $BA$ ,
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### Rješenje

a)

$$A^T = \begin{bmatrix} 1 & 0 & 5 \\ 2 & -3 & 4 \end{bmatrix}$$

b)  $BA$

$$(2, 4) (3, 2)$$

$\neq$

## Zadatak 5

Zadane su matrice

$$A = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \quad i \quad B = \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}.$$

Odredite:

- a)  $A^T$ ,
- b)  $BA$ ,
- c)  $AB$ .

### Rješenje

a)

$$A^T = \begin{bmatrix} 1 & 0 & 5 \\ 2 & -3 & 4 \end{bmatrix}$$

b)  $BA$  ← nije definirano

$(2, 4) (3, 2)$   
 $\neq$

c)

$$AB =$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix}$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix}.$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}$$

c)

$$(3,2) \quad AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}$$

$(3, 2) (2, 4)$



c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}$$

$(3, 2) (2, 4)$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix}$$

$(3, \boxed{2}) (2, 4)$   
 $\quad \quad \quad \underline{\quad}$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} \end{bmatrix}$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ & & & \\ & & & \\ & & & \end{bmatrix}$$

$(3, \boxed{2}) (2, 4)$   
 $=$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \end{bmatrix}$$

$(3, \boxed{2}) (2, 4)$   
 $\quad \quad \quad =$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, \boxed{2}) (2, 4)$   
 $\quad \quad \quad =$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
 $=$

$$AB = \begin{bmatrix} & & & \\ & & & \\ & & & \end{bmatrix}$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
=

$$AB = \begin{bmatrix} & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} =$$



c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} =$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} =$$



c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

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$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & -4 & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & -4 & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} =$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

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$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} =$$



c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ & & & \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} = (0, -3) \cdot (1, 8)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ & & & \\ & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

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$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} = (0, -3) \cdot (1, 8) = 0 \cdot 1 + (-3) \cdot 8$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} = (0, -3) \cdot (1, 8) = 0 \cdot 1 + (-3) \cdot 8 = -24$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} = (0, -3) \cdot (1, 8) = 0 \cdot 1 + (-3) \cdot 8 = -24$$

$$c_{22} =$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

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$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} = (0, -3) \cdot (1, 8) = 0 \cdot 1 + (-3) \cdot 8 = -24$$

$$c_{22} = (0, -3) \cdot (0, 4)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

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$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} = (0, -3) \cdot (1, 8) = 0 \cdot 1 + (-3) \cdot 8 = -24$$

$$c_{22} = (0, -3) \cdot (0, 4) = 0 \cdot 0 + (-3) \cdot 4$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & & \end{bmatrix}$$

$$c_{11} = (1, 2) \cdot (1, 8) = 1 \cdot 1 + 2 \cdot 8 = 17$$

$$c_{12} = (1, 2) \cdot (0, 4) = 1 \cdot 0 + 2 \cdot 4 = 8$$

$$c_{13} = (1, 2) \cdot (-2, -1) = 1 \cdot (-2) + 2 \cdot (-1) = -4$$

$$c_{14} = (1, 2) \cdot (5, 3) = 1 \cdot 5 + 2 \cdot 3 = 11$$

$$c_{21} = (0, -3) \cdot (1, 8) = 0 \cdot 1 + (-3) \cdot 8 = -24$$

$$c_{22} = (0, -3) \cdot (0, 4) = 0 \cdot 0 + (-3) \cdot 4 = -12$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & & \end{bmatrix}$$

$$c_{23} =$$



c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & & \\ & & & \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & & \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & \\ & & & \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

$$c_{24} =$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & \\ & & & \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

$$c_{24} = (0, -3) \cdot (5, 3)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

$$c_{24} = (0, -3) \cdot (5, 3) = 0 \cdot 5 + (-3) \cdot 3$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & -9 \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

$$c_{24} = (0, -3) \cdot (5, 3) = 0 \cdot 5 + (-3) \cdot 3 = -9$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & -9 \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

$$c_{24} = (0, -3) \cdot (5, 3) = 0 \cdot 5 + (-3) \cdot 3 = -9$$

$$c_{31} =$$



c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & -9 \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

$$c_{24} = (0, -3) \cdot (5, 3) = 0 \cdot 5 + (-3) \cdot 3 = -9$$

$$c_{31} = (5, 4) \cdot (1, 8)$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) (2, 4)$   
 $=$

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & -9 \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

$$c_{24} = (0, -3) \cdot (5, 3) = 0 \cdot 5 + (-3) \cdot 3 = -9$$

$$c_{31} = (5, 4) \cdot (1, 8) = 5 \cdot 1 + 4 \cdot 8$$

c)

$$AB = \begin{bmatrix} 1 & 2 \\ 0 & -3 \\ 5 & 4 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & -2 & 5 \\ 8 & 4 & -1 & 3 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & c_{14} \\ c_{21} & c_{22} & c_{23} & c_{24} \\ c_{31} & c_{32} & c_{33} & c_{34} \end{bmatrix}$$

$(3, 2) \cdot (2, 4)$   
=

$$AB = \begin{bmatrix} 17 & 8 & -4 & 11 \\ -24 & -12 & 3 & -9 \\ 37 & & & \end{bmatrix}$$

$$c_{23} = (0, -3) \cdot (-2, -1) = 0 \cdot (-2) + (-3) \cdot (-1) = 3$$

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c)

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(3, 2) (2, 4)

=

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## šesti zadatak

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## Zadatak 6

Odredite matricu  $3AB - 7BA$  ako je

$$A = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \quad i \quad B = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix}.$$

## Zadatak 6

Odredite matricu  $3AB - 7BA$  ako je

$$A = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \quad i \quad B = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix}.$$

## Rješenje



$$3AB - 7BA \neq -4AB$$

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## Rješenje



Hm?! Zašto?

$$3AB - 7BA \neq -4AB$$

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## Rješenje



Jož, pa množenje matrica  
nije komutativna operacija.

$$3AB - 7BA \neq -4AB$$

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$$AB =$$

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$$(3,3) \quad AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix}$$

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$(3,3) (3,3)$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix}$$

$(3, 3)$   $(3, 3)$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix}$$

$(3,3)(3,3)$   
 $=$

$$\begin{array}{c}
 (3,3)(3,3) \\
 \underline{\quad}
 \end{array}
 AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$\begin{array}{c}
 (3,3)(3,3) \\
 \underline{\quad}
 \end{array}
 AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ & & \\ & & \end{bmatrix}$$

$$\begin{array}{c}
 (3,3)(3,3) \\
 \boxed{\phantom{3}} \\
 =
 \end{array}
 AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \end{bmatrix}$$



$$\begin{array}{c}
 (3,3)(3,3) \\
 \boxed{\phantom{3}} \\
 =
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$(3,3)(3,3)$   
 $=$

$$AB = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

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$(3,3)(3,3)$   
 $=$

$$AB = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} =$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ \boxed{-5} & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3)$   $(3, 3)$   
 $=$

$$AB = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5)$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ \boxed{-5} & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3)$   $(3, 3)$   
 $=$

$$AB = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5)$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ \boxed{-5} & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3)$   $(3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} =$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3)$   $(3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 \\ \\ \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3)$$



$$AB = \begin{matrix} (3, \boxed{3}, 3) \\ \underline{\quad} \end{matrix} \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 \\ \\ \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3$$

$$AB = \begin{matrix} (3, \boxed{3}, 3) \\ \underline{\quad} \end{matrix} \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 & 10 & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & \boxed{-4} \\ 2 & 1 & \boxed{0} \\ -5 & 3 & \boxed{2} \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(\underline{3}, \underline{3})(\underline{3}, \underline{3})$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} =$$

$$AB = \begin{bmatrix} \boxed{3} & \boxed{1} & \boxed{-4} \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & \boxed{-4} \\ 2 & 1 & \boxed{0} \\ -5 & 3 & \boxed{2} \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(\underline{\underline{3}}, \underline{\underline{3}})(\underline{\underline{3}}, \underline{\underline{3}})$   
 $\underline{\underline{=}}$

$$AB = \begin{bmatrix} 31 & 10 & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2)$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & \boxed{-4} \\ 2 & 1 & \boxed{0} \\ -5 & 3 & \boxed{2} \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, \boxed{3}, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2$$

$$AB = \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & \boxed{-4} \\ 2 & 1 & \boxed{0} \\ -5 & 3 & \boxed{2} \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(\underline{3}, \underline{3})(\underline{3}, \underline{3})$   
 $\underline{=}$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} =$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} = (-4, 6, -2) \cdot (3, 2, -5)$$



$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ & & \\ & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} = (-4, 6, -2) \cdot (3, 2, -5) = -4 \cdot 3 + 6 \cdot 2 + (-2) \cdot (-5)$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} = (-4, 6, -2) \cdot (3, 2, -5) = -4 \cdot 3 + 6 \cdot 2 + (-2) \cdot (-5) = 10$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} = (-4, 6, -2) \cdot (3, 2, -5) = -4 \cdot 3 + 6 \cdot 2 + (-2) \cdot (-5) = 10$$

$$c_{22} =$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} = (-4, 6, -2) \cdot (3, 2, -5) = -4 \cdot 3 + 6 \cdot 2 + (-2) \cdot (-5) = 10$$

$$c_{22} = (-4, 6, -2) \cdot (7, 1, 3)$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} = (-4, 6, -2) \cdot (3, 2, -5) = -4 \cdot 3 + 6 \cdot 2 + (-2) \cdot (-5) = 10$$

$$c_{22} = (-4, 6, -2) \cdot (7, 1, 3) = -4 \cdot 7 + 6 \cdot 1 + (-2) \cdot 3$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & \end{bmatrix}$$

$$c_{11} = (3, 1, -4) \cdot (3, 2, -5) = 3 \cdot 3 + 1 \cdot 2 + (-4) \cdot (-5) = 31$$

$$c_{12} = (3, 1, -4) \cdot (7, 1, 3) = 3 \cdot 7 + 1 \cdot 1 + (-4) \cdot 3 = 10$$

$$c_{13} = (3, 1, -4) \cdot (-4, 0, 2) = 3 \cdot (-4) + 1 \cdot 0 + (-4) \cdot 2 = -20$$

$$c_{21} = (-4, 6, -2) \cdot (3, 2, -5) = -4 \cdot 3 + 6 \cdot 2 + (-2) \cdot (-5) = 10$$

$$c_{22} = (-4, 6, -2) \cdot (7, 1, 3) = -4 \cdot 7 + 6 \cdot 1 + (-2) \cdot 3 = -28$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3,3)(3,3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & \end{bmatrix}$$

$$c_{23} =$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2)$$



$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3)$   $(3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} =$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ (3, 3) \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

=

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5)$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5)$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & & \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ (3, 3) (3, 3) \quad \boxed{5 \quad 8 \quad 5} \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} =$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ (3, 3) (3, 3) \quad \boxed{5 \quad 8 \quad 5} \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3)$$



$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ (3, 3) (3, 3) \quad \boxed{5 \quad 8 \quad 5} \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3) = 5 \cdot 7 + 8 \cdot 1 + 5 \cdot 3$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ (3, 3) (3, 3) \quad \boxed{5 \quad 8 \quad 5} \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{7} & -4 \\ 2 & 1 & 0 \\ -5 & \boxed{3} & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3) = 5 \cdot 7 + 8 \cdot 1 + 5 \cdot 3 = 58$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ (3,3)(3,3) \quad \boxed{5} & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & \boxed{-4} \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3) = 5 \cdot 7 + 8 \cdot 1 + 5 \cdot 3 = 58$$

$$c_{33} =$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3) = 5 \cdot 7 + 8 \cdot 1 + 5 \cdot 3 = 58$$

$$c_{33} = (5, 8, 5) \cdot (-4, 0, 2)$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3) = 5 \cdot 7 + 8 \cdot 1 + 5 \cdot 3 = 58$$

$$c_{33} = (5, 8, 5) \cdot (-4, 0, 2) = 5 \cdot (-4) + 8 \cdot 0 + 5 \cdot 2$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3) = 5 \cdot 7 + 8 \cdot 1 + 5 \cdot 3 = 58$$

$$c_{33} = (5, 8, 5) \cdot (-4, 0, 2) = 5 \cdot (-4) + 8 \cdot 0 + 5 \cdot 2 = -10$$

$$AB = \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$AB = \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix}$$

$$c_{23} = (-4, 6, -2) \cdot (-4, 0, 2) = -4 \cdot (-4) + 6 \cdot 0 + (-2) \cdot 2 = 12$$

$$c_{31} = (5, 8, 5) \cdot (3, 2, -5) = 5 \cdot 3 + 8 \cdot 2 + 5 \cdot (-5) = 6$$

$$c_{32} = (5, 8, 5) \cdot (7, 1, 3) = 5 \cdot 7 + 8 \cdot 1 + 5 \cdot 3 = 58$$

$$c_{33} = (5, 8, 5) \cdot (-4, 0, 2) = 5 \cdot (-4) + 8 \cdot 0 + 5 \cdot 2 = -10$$

$$BA =$$



$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix}$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix}.$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix}$$

$$(3,3) \quad BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix}$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix}$$

$(3,3) (3,3)$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $\underline{\quad}$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$(3, 3)$   $(3, 3)$



$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ & & \\ & & \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $\underline{\quad}$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$BA = \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ \boxed{5} & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3})(\boxed{3}, 3)$   
 $=$

$$BA = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5)$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5$$

$$BA = \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & 1 & -4 \\ -4 & 6 & -2 \\ \boxed{5} & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$



$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8)$$

$$BA = \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{1} & -4 \\ -4 & \boxed{6} & -2 \\ 5 & \boxed{8} & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8$$

$$BA = \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & \boxed{1} & -4 \\ -4 & \boxed{6} & -2 \\ 5 & \boxed{8} & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5)$$

$$BA = \begin{bmatrix} \boxed{3} & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & \boxed{-4} \\ -4 & 6 & \boxed{-2} \\ 5 & 8 & \boxed{5} \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3})(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$



$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} = (2, 1, 0) \cdot (3, -4, 5)$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ & & \\ & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} = (2, 1, 0) \cdot (3, -4, 5) = 2 \cdot 3 + 1 \cdot (-4) + 0 \cdot 5$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} = (2, 1, 0) \cdot (3, -4, 5) = 2 \cdot 3 + 1 \cdot (-4) + 0 \cdot 5 = 2$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} = (2, 1, 0) \cdot (3, -4, 5) = 2 \cdot 3 + 1 \cdot (-4) + 0 \cdot 5 = 2$$

$$d_{22} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} = (2, 1, 0) \cdot (3, -4, 5) = 2 \cdot 3 + 1 \cdot (-4) + 0 \cdot 5 = 2$$

$$d_{22} = (2, 1, 0) \cdot (1, 6, 8)$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} = (2, 1, 0) \cdot (3, -4, 5) = 2 \cdot 3 + 1 \cdot (-4) + 0 \cdot 5 = 2$$

$$d_{22} = (2, 1, 0) \cdot (1, 6, 8) = 2 \cdot 1 + 1 \cdot 6 + 0 \cdot 8$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & \end{bmatrix}$$

$$d_{11} = (3, 7, -4) \cdot (3, -4, 5) = 3 \cdot 3 + 7 \cdot (-4) + (-4) \cdot 5 = -39$$

$$d_{12} = (3, 7, -4) \cdot (1, 6, 8) = 3 \cdot 1 + 7 \cdot 6 + (-4) \cdot 8 = 13$$

$$d_{13} = (3, 7, -4) \cdot (-4, -2, 5) = 3 \cdot (-4) + 7 \cdot (-2) + (-4) \cdot 5 = -46$$

$$d_{21} = (2, 1, 0) \cdot (3, -4, 5) = 2 \cdot 3 + 1 \cdot (-4) + 0 \cdot 5 = 2$$

$$d_{22} = (2, 1, 0) \cdot (1, 6, 8) = 2 \cdot 1 + 1 \cdot 6 + 0 \cdot 8 = 8$$



$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3}) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & \end{bmatrix}$$

$$d_{23} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5)$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)$   $(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -39 & 13 & -46 \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, \boxed{3}, \boxed{3})$   
 $\quad \quad \quad \underline{\quad}$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5)$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$



$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
        

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8)$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8) = -5 \cdot 1 + 3 \cdot 6 + 2 \cdot 8$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
        

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8) = -5 \cdot 1 + 3 \cdot 6 + 2 \cdot 8 = 29$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3) (3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8) = -5 \cdot 1 + 3 \cdot 6 + 2 \cdot 8 = 29$$

$$d_{33} =$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8) = -5 \cdot 1 + 3 \cdot 6 + 2 \cdot 8 = 29$$

$$d_{33} = (-5, 3, 2) \cdot (-4, -2, 5)$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
 $=$

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8) = -5 \cdot 1 + 3 \cdot 6 + 2 \cdot 8 = 29$$

$$d_{33} = (-5, 3, 2) \cdot (-4, -2, 5) = -5 \cdot (-4) + 3 \cdot (-2) + 2 \cdot 5$$

$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$(3, 3)(3, 3)$   
        

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8) = -5 \cdot 1 + 3 \cdot 6 + 2 \cdot 8 = 29$$

$$d_{33} = (-5, 3, 2) \cdot (-4, -2, 5) = -5 \cdot (-4) + 3 \cdot (-2) + 2 \cdot 5 = 24$$



$$BA = \begin{bmatrix} 3 & 7 & -4 \\ 2 & 1 & 0 \\ -5 & 3 & 2 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 & -4 \\ -4 & 6 & -2 \\ 5 & 8 & 5 \end{bmatrix} = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{21} & d_{22} & d_{23} \\ d_{31} & d_{32} & d_{33} \end{bmatrix}$$

(3, 3) (3, 3)

=

$$BA = \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix}$$

$$d_{23} = (2, 1, 0) \cdot (-4, -2, 5) = 2 \cdot (-4) + 1 \cdot (-2) + 0 \cdot 5 = -10$$

$$d_{31} = (-5, 3, 2) \cdot (3, -4, 5) = -5 \cdot 3 + 3 \cdot (-4) + 2 \cdot 5 = -17$$

$$d_{32} = (-5, 3, 2) \cdot (1, 6, 8) = -5 \cdot 1 + 3 \cdot 6 + 2 \cdot 8 = 29$$

$$d_{33} = (-5, 3, 2) \cdot (-4, -2, 5) = -5 \cdot (-4) + 3 \cdot (-2) + 2 \cdot 5 = 24$$

$$3AB - 7BA =$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} -$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ & & \end{bmatrix}$$



$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} -$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ & & \\ & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$



$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & & \\ & & \\ & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & & \\ & & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & 262 \\ & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & 262 \\ 16 & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & 262 \\ 16 & -140 & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & 262 \\ 16 & -140 & 106 \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & 262 \\ 16 & -140 & 106 \\ 137 & & \end{bmatrix}$$

$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & 262 \\ 16 & -140 & 106 \\ 137 & -29 & \end{bmatrix}$$



$$3AB - 7BA = 3 \cdot \begin{bmatrix} 31 & 10 & -20 \\ 10 & -28 & 12 \\ 6 & 58 & -10 \end{bmatrix} - 7 \cdot \begin{bmatrix} -39 & 13 & -46 \\ 2 & 8 & -10 \\ -17 & 29 & 24 \end{bmatrix} =$$

$$= \begin{bmatrix} 93 & 30 & -60 \\ 30 & -84 & 36 \\ 18 & 174 & -30 \end{bmatrix} - \begin{bmatrix} -273 & 91 & -322 \\ 14 & 56 & -70 \\ -119 & 203 & 168 \end{bmatrix} =$$

$$= \begin{bmatrix} 366 & -61 & 262 \\ 16 & -140 & 106 \\ 137 & -29 & -198 \end{bmatrix}$$

**sedmi zadatak**

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## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) =$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 =$$



## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

(2, 2)

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

(2, 2) (2, 2)

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

(2, 2) (2, 2)

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

$(2, 2)$   $(2, 2)$

$=$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$$

$(2, 2) \quad (2, 2)$   
=



## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(3, -2) \cdot (3, -1) =$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$$

$(2, 2) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(3, -2) \cdot (3, -1) = 3 \cdot 3 + (-2) \cdot (-1)$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} \boxed{3} & \boxed{-2} \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & -2 \\ \boxed{-1} & 5 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$$

$(2, \boxed{2}) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(3, -2) \cdot (3, -1) = 3 \cdot 3 + (-2) \cdot (-1) = 11$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} \boxed{3} & \boxed{-2} \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & -2 \\ \boxed{-1} & 5 \end{bmatrix} = \begin{bmatrix} 11 & \\ & \end{bmatrix}$$

$(2, \boxed{2}) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(3, -2) \cdot (-2, 5) =$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & \\ & \end{bmatrix}$$

$(2, 2) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(3, -2) \cdot (-2, 5) = 3 \cdot (-2) + (-2) \cdot 5$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & \\ & \end{bmatrix}$$

$(2, 2) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(3, -2) \cdot (-2, 5) = 3 \cdot (-2) + (-2) \cdot 5 = -16$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ 2 & 2 \end{bmatrix}$$

*(Note: In the original image, the calculation for the bottom row of the matrix multiplication is shown as  $(2, 2)(2, 2)$  with a blue equals sign below it.)*

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(-1, 5) \cdot (3, -1) =$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ 2 & 2 \end{bmatrix}$$

$(2, 2)$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(-1, 5) \cdot (3, -1) = -1 \cdot 3 + 5 \cdot (-1)$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ 1 & 23 \end{bmatrix}$$



## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(-1, 5) \cdot (3, -1) = -1 \cdot 3 + 5 \cdot (-1) = -8$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 19 \end{bmatrix}$$

$(2, 2) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(-1, 5) \cdot (-2, 5) =$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 19 \end{bmatrix}$$

$(2, 2) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(-1, 5) \cdot (-2, 5) = -1 \cdot (-2) + 5 \cdot 5$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 19 \end{bmatrix}$$

$(2, 2) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

$$(-1, 5) \cdot (-2, 5) = -1 \cdot (-2) + 5 \cdot 5 = 27$$

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2, 2) (2, 2)$   
=

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2, 2) (2, 2)$

$=$

$$A^3 =$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2, 2) (2, 2)$

$=$

$$A^3 = A^2 \cdot A$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

(2,2) (2,2)

=

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

(2,2) (2,2)

=

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$



## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

$(2,2)$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$=$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

$(2,2) (2,2)$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2)$   $(2,2)$

$=$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

$(2,2)$   $(2,2)$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$$

$(2,2)$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$$

$(2,2) (2,2)$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2, 2) (2, 2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$$

$(2, 2) (2, 2)$

$$(11, -16) \cdot (3, -1) =$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2, 2) (2, 2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$$

$(2, 2) (2, 2)$

$$(11, -16) \cdot (3, -1) = 11 \cdot 3 + (-16) \cdot (-1)$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2, 2) (2, 2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & \dots \\ \dots & \dots \end{bmatrix}$$

$(2, 2) (2, 2)$

$$(11, -16) \cdot (3, -1) = 11 \cdot 3 + (-16) \cdot (-1) = 49$$



## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2, 2) (2, 2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -38 \\ -11 & 119 \end{bmatrix}$$

$(2, 2) (2, 2)$

$$(11, -16) \cdot (-2, 5) =$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -38 \\ -11 & 119 \end{bmatrix}$$

$(2,2) (2,2)$

$$(11, -16) \cdot (-2, 5) = 11 \cdot (-2) + (-16) \cdot 5$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -102 \\ \dots & \dots \end{bmatrix}$$

$(2,2) (2,2)$

$$(11, -16) \cdot (-2, 5) = 11 \cdot (-2) + (-16) \cdot 5 = -102$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

$$A^2 = A \cdot A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -102 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$(-8, 27) \cdot (3, -1) =$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

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$$f(A) = A^3 + 2A^2 + 3I$$

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$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -102 \\ -8 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$(-8, 27) \cdot (3, -1) = -8 \cdot 3 + 27 \cdot (-1)$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

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$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -102 \\ -51 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$(-8, 27) \cdot (3, -1) = -8 \cdot 3 + 27 \cdot (-1) = -51$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

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$$f(A) = A^3 + 2A^2 + 3I$$

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$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -102 \\ -51 & 27 \end{bmatrix}$$

$(2,2) (2,2)$

$$(-8, 27) \cdot (-2, 5) =$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

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## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

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$(2,2) (2,2)$

$$(-8, 27) \cdot (-2, 5) = -8 \cdot (-2) + 27 \cdot 5$$



## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

$$f(A) = A^3 + 2A^2 + 3I$$

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$(2,2) (2,2)$

$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix}$$

$(2,2) (2,2)$

$$(-8, 27) \cdot (-2, 5) = -8 \cdot (-2) + 27 \cdot 5 = 151$$

## Zadatak 7

Zadana je matrica  $A = \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix}$  i polinom  $f(x) = x^3 + 2x^2 + 3$ .

Odredite  $f(A)$ .

## Rješenje

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$$A^3 = A^2 \cdot A = \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} \cdot \begin{bmatrix} 3 & -2 \\ -1 & 5 \end{bmatrix} = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix}$$

$(2,2)$

$$f(A) = A^3 + 2A^2 + 3I$$

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$$f(A) =$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix}$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix}$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

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$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} +$$

$$f(A) = A^3 + 2A^2 + 3I$$

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$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + \begin{bmatrix} 22 & -32 \\ -16 & 54 \end{bmatrix}$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

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$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + \begin{bmatrix} 22 & -32 \\ -16 & 54 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} & \\ & \end{bmatrix}$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + \begin{bmatrix} 22 & -32 \\ -16 & 54 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 74 & \\ & \end{bmatrix}$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + \begin{bmatrix} 22 & -32 \\ -16 & 54 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 74 & -134 \\ -51 & 151 \end{bmatrix}$$



$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + \begin{bmatrix} 22 & -32 \\ -16 & 54 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 74 & -134 \\ -67 & \end{bmatrix}$$

$$f(A) = A^3 + 2A^2 + 3I$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + 2 \cdot \begin{bmatrix} 11 & -16 \\ -8 & 27 \end{bmatrix} + 3 \cdot \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 49 & -102 \\ -51 & 151 \end{bmatrix} + \begin{bmatrix} 22 & -32 \\ -16 & 54 \end{bmatrix} + \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$$

$$f(A) = \begin{bmatrix} 74 & -134 \\ -67 & 208 \end{bmatrix}$$



Može li se  $A^n$  izračunati  
za svaku matricu  $A$  pri  
čemu je  $n \in \mathbb{N}$ ?





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$$A \cdot A$$





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$(m, n)$





Može li se  $A^n$  izračunati  
za svaku matricu  $A$  pri  
čemu je  $n \in \mathbb{N}$ ?

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$$(m, n) (m, n)$$





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za svaku matricu  $A$  pri  
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Može li se  $A^n$  izračunati  
za svaku matricu  $A$  pri  
čemu je  $n \in \mathbb{N}$ ?

$$\begin{array}{c} A \cdot A \\ (m, \boxed{n}) (m, n) \\ n = m \end{array}$$







Može li se  $A^n$  izračunati  
za svaku matricu  $A$  pri  
čemu je  $n \in \mathbb{N}$ ?

Potencirati se mogu  
samo kvadratne matrice.

$$\begin{array}{c} A \cdot A \\ (m, \boxed{n}) (m, n) \\ n = m \end{array}$$



**osmi zadatak**

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## Zadatak 8

*Izračunajte*

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

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## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} =$$

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} =$$

(2, 3)

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} =$$

(2, 3) (3, 1)

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} =$$

$(2, \boxed{3})(3, 1)$

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} =$$

$(2, \boxed{3})(3, 1)$

$=$



## Zadatak 8

Izračunajte

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## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} \phantom{0} \\ \phantom{0} \end{bmatrix}$$

$$(2, \boxed{3})(3, 1)$$

=

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} \phantom{0} \\ \phantom{0} \end{bmatrix}$$

$$(2, \boxed{3})(\boxed{3}, 1)$$

=

$$(2, -2, 0) \cdot (2, 1, 3) =$$

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} \phantom{0} \\ \phantom{0} \end{bmatrix}$$

$$(2, 3)(3, 1)$$

=

$$(2, -2, 0) \cdot (2, 1, 3) = 2 \cdot 2 + (-2) \cdot 1 + 0 \cdot 3$$

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \end{bmatrix}$$

$$(2, 3)(3, 1)$$

=

$$(2, -2, 0) \cdot (2, 1, 3) = 2 \cdot 2 + (-2) \cdot 1 + 0 \cdot 3 = 2$$

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ \end{bmatrix}$$

$$(2, \boxed{3})(3, 1)$$

=

$$(2, -2, 0) \cdot (2, 1, 3) = 2 \cdot 2 + (-2) \cdot 1 + 0 \cdot 3 = 2$$

$$(1, -2, 1) \cdot (2, 1, 3) =$$

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ \end{bmatrix}$$

$$(2, \boxed{3})(3, 1)$$

=

$$(2, -2, 0) \cdot (2, 1, 3) = 2 \cdot 2 + (-2) \cdot 1 + 0 \cdot 3 = 2$$

$$(1, -2, 1) \cdot (2, 1, 3) = 1 \cdot 2 + (-2) \cdot 1 + 1 \cdot 3$$

## Zadatak 8

Izračunajte

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}.$$

## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$(2, \boxed{3})(\boxed{3}, 1)$$

=

$$(2, -2, 0) \cdot (2, 1, 3) = 2 \cdot 2 + (-2) \cdot 1 + 0 \cdot 3 = 2$$

$$(1, -2, 1) \cdot (2, 1, 3) = 1 \cdot 2 + (-2) \cdot 1 + 1 \cdot 3 = 3$$

## Zadatak 8

Izračunajte

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## Rješenje

$$\begin{bmatrix} 2 & -2 & 0 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$(2, \boxed{3})(3, 1)$$

=

$$(2, -2, 0) \cdot (2, 1, 3) = 2 \cdot 2 + (-2) \cdot 1 + 0 \cdot 3 = 2$$

$$(1, -2, 1) \cdot (2, 1, 3) = 1 \cdot 2 + (-2) \cdot 1 + 1 \cdot 3 = 3$$



**deveti zadatak**

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## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

## Rješenje

$$AB =$$

## Zadatak 9

Izračunajte  $AB$  ako je

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## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix}$$

## Zadatak 9

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$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix}.$$

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## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}$$

## Zadatak 9

$$k(AB) = (kA)B = A(kB)$$

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} =$$



## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5}$$

## Zadatak 9

Izračunajte  $AB$  ako je

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$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix}$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

(2, 2)

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$(2, 2) (2, 3)$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$(2, 2)(2, 3)$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\overset{=}{(2,2)(2,3)}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} =$$



## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\overset{=}{(2,2)(2,3)}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5}$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\overset{=}{(2,2)(2,3)}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} \phantom{0} & \phantom{0} & \phantom{0} \\ \phantom{0} & \phantom{0} & \phantom{0} \end{bmatrix}$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\overset{=}{(2,2)(2,3)}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} \phantom{0} & \phantom{0} & \phantom{0} \\ \phantom{0} & \phantom{0} & \phantom{0} \end{bmatrix}$$

$$(2,3) \cdot (1,3) =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\overset{=}{(2,2)(2,3)}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} \phantom{00} & \phantom{00} & \phantom{00} \\ \phantom{00} & \phantom{00} & \phantom{00} \end{bmatrix}$$

$$(2,3) \cdot (1,3) = 2 \cdot 1 + 3 \cdot 3$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\overset{=}{(2,2)(2,3)}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & & \\ & & \\ & & \end{bmatrix}$$

$$(2,3) \cdot (1,3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$= (2, 2) (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & & \\ & & \\ & & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(2, 3) \cdot (0, 6) =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) \end{matrix} (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & & \\ & & \\ & & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) (2, 3) \end{matrix}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$



## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) (2, 3) \end{matrix}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & \\ & & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(2, 3) \cdot (4, 8) =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} & = \\ (2, 2) & (2, 3) \end{matrix}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & \\ & & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} & = \\ (2, 2) & (2, 3) \end{matrix}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) (2, 3) \end{matrix}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11 \quad (1, 5) \cdot (1, 3) =$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) \end{matrix} (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11 \quad (1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) \end{matrix} (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) (2, 3) \end{matrix}$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(1, 5) \cdot (0, 6) =$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) \end{matrix} (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(1, 5) \cdot (0, 6) = 1 \cdot 0 + 5 \cdot 6 = 30$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$



## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) \end{matrix} (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & 30 & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(1, 5) \cdot (0, 6) = 1 \cdot 0 + 5 \cdot 6 = 30$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$= (2, 2)(2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & 30 & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(1, 5) \cdot (0, 6) = 1 \cdot 0 + 5 \cdot 6 = 30$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

$$(1, 5) \cdot (4, 8) =$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$\begin{matrix} = \\ (2, 2) \end{matrix} (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & 30 & \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(1, 5) \cdot (0, 6) = 1 \cdot 0 + 5 \cdot 6 = 30$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

$$(1, 5) \cdot (4, 8) = 1 \cdot 4 + 5 \cdot 8$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$= (2, 2) (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & 30 & 44 \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(1, 5) \cdot (0, 6) = 1 \cdot 0 + 5 \cdot 6 = 30$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

$$(1, 5) \cdot (4, 8) = 1 \cdot 4 + 5 \cdot 8 = 44$$

## Zadatak 9

Izračunajte  $AB$  ako je

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \quad i \quad B = \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix}.$$

$$k(AB) = (kA)B = A(kB)$$

kvaziasocijativnost

## Rješenje

$$= (2, 2) (2, 3)$$

$$AB = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \cdot \frac{9}{5} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 1 & 0 & 4 \\ 3 & 6 & 8 \end{bmatrix} = \frac{9}{5} \begin{bmatrix} 11 & 18 & 32 \\ 16 & 30 & 44 \end{bmatrix}$$

$$(2, 3) \cdot (1, 3) = 2 \cdot 1 + 3 \cdot 3 = 11$$

$$(1, 5) \cdot (1, 3) = 1 \cdot 1 + 5 \cdot 3 = 16$$

$$(2, 3) \cdot (0, 6) = 2 \cdot 0 + 3 \cdot 6 = 18$$

$$(1, 5) \cdot (0, 6) = 1 \cdot 0 + 5 \cdot 6 = 30$$

$$(2, 3) \cdot (4, 8) = 2 \cdot 4 + 3 \cdot 8 = 32$$

$$(1, 5) \cdot (4, 8) = 1 \cdot 4 + 5 \cdot 8 = 44$$

**deseti zadatak**

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## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY =$$



## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix}$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$$

(1, 3)

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$$

$(1, 3) (3, 1)$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$$

$(1, 3)(3, 1)$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} \quad \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) =$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} \quad \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4$$



## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX =$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix}$$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix}$$

$(3, 1)$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix}$$

$(3, 1)(1, 3)$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix}$$

$(3, 1)(1, 3)$

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$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=



## Zadatak 10

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$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} \\ \\ \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

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$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & & \\ & & \\ & & \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & 6 & -17 \\ 0 & 0 & 0 \\ 4 & -8 & -20 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
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$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & 6 & -15 \\ 0 & 0 & 0 \\ 4 & -8 & -20 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

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$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

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$(3, 1)(1, 3)$   
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$(3, 1)(1, 3)$   
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## Zadatak 10

Izračunajte  $XY + YX$  ako je

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$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & 6 & -15 \\ 0 & 0 & 0 \\ 4 & 8 & -20 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

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$(1, 3)(3, 1)$   
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$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

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$(3, 1)(1, 3)$   
=



## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & 6 & -15 \\ 0 & 0 & 0 \\ 4 & 8 & -20 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & 6 & -15 \\ 0 & 0 & 0 \\ 4 & 8 & -20 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & 6 & -15 \\ 0 & 0 & 0 \\ 4 & 8 & -20 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

- $XY + YX$

## Zadatak 10

Izračunajte  $XY + YX$  ako je

$$X = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \quad i \quad Y = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}.$$

## Rješenje

$$XY = \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} = \begin{bmatrix} -17 \end{bmatrix}$$

$(1, 3)(3, 1)$   
=

$$(1, 2, -5) \cdot (3, 0, 4) = 1 \cdot 3 + 2 \cdot 0 + (-5) \cdot 4 = -17$$

$$YX = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} \begin{bmatrix} 1 & 2 & -5 \end{bmatrix} = \begin{bmatrix} 3 & 6 & -15 \\ 0 & 0 & 0 \\ 4 & 8 & -20 \end{bmatrix}$$

$(3, 1)(1, 3)$   
=

- $XY + YX$  nije definirano jer matrice  $XY$  i  $YX$  nisu istog tipa.