

Seminari 6

MATEMATIKA ZA EKONOMISTE 2

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Sadržaj

Parcijalne derivacije – oznake

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četvrti zadatak

Parcijalne derivacije drugog reda – oznake

peti zadatak

šesti zadatak

sedmi zadatak

osmi zadatak

deveti zadatak

deseti zadatak

Parcijalne derivacije – oznake

Oznake

- Funkcija dvije varijable: $z = z(x, y)$
- Parcijalna derivacija po varijabli x

$$z_x \qquad z'_x \qquad \frac{\partial z}{\partial x}$$

- Parcijalna derivacija po varijabli y

$$z_y \qquad z'_y \qquad \frac{\partial z}{\partial y}$$

prvi zadatak

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x =$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x +$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y =$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

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b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0$

Zadatak 1

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a) $f_x = 2x + 0 = 2x$

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Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y$

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Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

$$(cu)'(x) = c \cdot u'(x)$$

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x =$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

$$(cu)'(x) = c \cdot u'(x)$$

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

$$(cu)'(x) = c \cdot u'(x)$$

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x +$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

$$(cu)'(x) = c \cdot u'(x)$$

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

$$(cu)'(x) = c \cdot u'(x)$$

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y +$

Zadatak 1

$$(x^n)' = nx^{n-1}$$

Odredite parcijalne derivacije sljedećih funkcija:

$$(cu)'(x) = c \cdot u'(x)$$

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0$

Zadatak 1

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$$(cu)'(x) = c \cdot u'(x)$$

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

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Rješenje

a) $f_x = 2x + 0 = 2x$

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Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$g_y = 0$

Zadatak 1

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Rješenje

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$f_y = 0 + 2y = 2y$

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Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$g_y = 0 + x$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

c) $z = \frac{y}{x}$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$g_y = 0 + x + \frac{1}{2\sqrt{y}}$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

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Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

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Zadatak 1

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a) $f(x, y) = x^2 + y^2$

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$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

c) $z = \frac{y}{x}$

$z = yx^{-1}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

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Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

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$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x =$

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$$(cu)'(x) = c \cdot u'(x)$$

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Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x = y$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

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$z = yx^{-1}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x = y \cdot$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

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$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x = y \cdot (-x^{-2})$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

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c) $z = \frac{y}{x}$

$z = yx^{-1}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x = y \cdot (-x^{-2}) = -\frac{y}{x^2}$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

c) $z = \frac{y}{x}$

$z = yx^{-1}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x = y \cdot (-x^{-2}) = -\frac{y}{x^2}$

$z_y =$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

c) $z = \frac{y}{x}$

$z = yx^{-1}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

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Zadatak 1

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Rješenje

a) $f_x = 2x + 0 = 2x$

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Zadatak 1

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a) $f(x, y) = x^2 + y^2$

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$z = yx^{-1}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x = y \cdot (-x^{-2}) = -\frac{y}{x^2}$

$$z_y = x^{-1} \cdot 1$$

Zadatak 1

Odredite parcijalne derivacije sljedećih funkcija:

a) $f(x, y) = x^2 + y^2$

b) $g(x, y) = 3x^2 + xy + \sqrt{y}$

c) $z = \frac{y}{x}$

$z = yx^{-1}$

$$(x^n)' = nx^{n-1}$$

$$(cu)'(x) = c \cdot u'(x)$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Rješenje

a) $f_x = 2x + 0 = 2x$

$f_y = 0 + 2y = 2y$

b) $g_x = 6x + y + 0 = 6x + y$

$$g_y = 0 + x + \frac{1}{2\sqrt{y}} = x + \frac{1}{2\sqrt{y}}$$

c) $z_x = y \cdot (-x^{-2}) = -\frac{y}{x^2}$

$$z_y = x^{-1} \cdot 1 = \frac{1}{x}$$

drugi zadatak

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x =$

$$(cu)'(x) = c \cdot u'(x)$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y$

$$(cu)'(x) = c \cdot u'(x)$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y \cdot$

$$(cu)'(x) = c \cdot u'(x)$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y \cdot 1$

$$(cu)'(x) = c \cdot u'(x)$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y \cdot 1 = e^y$

$$(cu)'(x) = c \cdot u'(x)$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y \cdot 1 = e^y$

$z_y =$

$$(cu)'(x) = c \cdot u'(x)$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y \cdot 1 = e^y$

$z_y = x$

$$(cu)'(x) = c \cdot u'(x)$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y \cdot 1 = e^y$

$z_y = x \cdot$

$$(cu)'(x) = c \cdot u'(x)$$

$$(e^x)' = e^x$$

Zadatak 2

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

a) $z_x = e^y \cdot 1 = e^y$

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$z_y = x \cdot e^y = xe^y$

$$(cu)'(x) = c \cdot u'(x)$$

b) $z_x = 0 +$

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$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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c) $u_x = \frac{2}{(x + y)^2}$

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b) $z_x = 0 + \frac{1}{2\sqrt{x}} = \frac{1}{2\sqrt{x}}$

$z_y = 1 \cdot e^y + y \cdot e^y + 0 = (1 + y)e^y$

c) $u_x = \frac{2 \cdot (x + y) - (2x - y) \cdot 1}{(x + y)^2} = \frac{3y}{(x + y)^2}$

$$(e^x)' = e^x$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Zadatak 2

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

Odredite parcijalne derivacije sljedećih funkcija:

a) $z = xe^y$

b) $z = ye^y + \sqrt{x}$

c) $u(x, y) = \frac{2x - y}{x + y}$

Rješenje

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

a) $z_x = e^y \cdot 1 = e^y$

$z_y = x \cdot e^y = xe^y$

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$$(e^x)' = e^x$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$u_y =$

Zadatak 2

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$u_y =$ _____

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$u_y = \frac{-1 \cdot (x + y)^2 - (2x - y) \cdot 2(x + y)}{(x + y)^4} = \frac{-(x + y) - 2(2x - y)}{(x + y)^3} = \frac{-x - y - 4x + 2y}{(x + y)^3} = \frac{-5x + y}{(x + y)^3}$

$$(e^x)' = e^x$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

Zadatak 2

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

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$$u_y = \frac{-1 \cdot (x + y) - (2x - y) \cdot 1}{(x + y)^2} = \frac{-2x - 2y}{(x + y)^2}$$

$$(e^x)' = e^x$$

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Zadatak 2

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

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$$(e^x)' = e^x$$

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treći zadatak

Zadatak 3

Odredite parcijalne derivacije sljedećih funkcija:

a) $z(x, y) = (x + 2y)e^{x^2+y^3}$

c) $z = 2^{\sin \frac{y}{x}}$

b) $z = \frac{x}{\sqrt{x^2 + y^2}}$

d) $z = x^y$

Rješenje

a) $z_x =$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

a) $z_x = (x + 2y)'_x$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

a) $z_x = (x + 2y)'_x \cdot$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

a) $z_x = (x + 2y)'_x \cdot e^{x^2+y^3}$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

a) $z_x = (x + 2y)'_x \cdot e^{x^2+y^3} +$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

$$\text{a)} \quad z_x = (x + 2y)'_x \cdot e^{x^2+y^3} + (x + 2y)$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

a)
$$z_x = (x + 2y)'_x \cdot e^{x^2+y^3} + (x + 2y) \cdot$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

$$\text{a)} \quad z_x = (x + 2y)'_x \cdot e^{x^2+y^3} + (x + 2y) \cdot (e^{x^2+y^3})'_x$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

$$\begin{aligned} \text{a)} \quad z_x &= (x + 2y)'_x \cdot e^{x^2+y^3} + (x + 2y) \cdot (e^{x^2+y^3})'_x = \\ &= 1 \end{aligned}$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

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Rješenje

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$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

$$z = (x + 2y)e^{x^2+y^3}$$

Rješenje

$$(e^x)' = e^x$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$\begin{aligned} \text{a)} \quad z_x &= (x + 2y)'_x \cdot e^{x^2+y^3} + (x + 2y) \cdot (e^{x^2+y^3})'_x = \\ &= 1 \cdot e^{x^2+y^3} + (x + 2y) \end{aligned}$$

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Rješenje

$$(e^x)' = e^x$$

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$\begin{aligned} \text{a)} \quad z_x &= (x + 2y)'_x \cdot e^{x^2+y^3} + (x + 2y) \cdot (e^{x^2+y^3})'_x = \\ &= 1 \cdot e^{x^2+y^3} + (x + 2y)e^{x^2+y^3} \cdot (x^2 + y^3)'_x = \\ &= e^{x^2+y^3} + (x + 2y)e^{x^2+y^3} . \end{aligned}$$

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$$(e^x)' = e^x$$

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$$= \underline{\hspace{10cm}}$$

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$$\begin{aligned} \text{b)} \quad z_x &= \frac{(x)'_x \cdot \sqrt{x^2 + y^2} - x \cdot (\sqrt{x^2 + y^2})'_x}{\sqrt{x^2 + y^2}^2} = \\ &= \frac{1 \cdot \sqrt{x^2 + y^2}}{x^2 + y^2} \end{aligned}$$

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$$\begin{aligned} & 1 \cdot \sqrt{x^2 + y^2} - x \cdot \\ &= \frac{\quad}{x^2 + y^2} \end{aligned}$$

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$$= \underline{\hspace{2cm}}$$

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$$= \frac{\sqrt{x^2 + y^2} - \frac{x^2}{\sqrt{x^2 + y^2}}}{(x^2 + y^2)\sqrt{x^2 + y^2}}$$

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$$= \frac{x^2 + y^2 - x^2}{(x^2 + y^2)\sqrt{x^2 + y^2}} = \frac{y^2}{(x^2 + y^2)\sqrt{x^2 + y^2}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$= \frac{x^2 + y^2 - x^2}{(x^2 + y^2)\sqrt{x^2 + y^2}} = \frac{1}{(x^2 + y^2)^{\frac{3}{2}}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y =$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \underline{\hspace{10cm}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{\quad}{\sqrt{x^2 + y^2}^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y}{\sqrt{x^2 + y^2}^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} -}{\sqrt{x^2 + y^2}^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x}{\sqrt{x^2 + y^2}^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x \cdot \sqrt{x^2 + y^2}'}{\sqrt{x^2 + y^2}^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

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$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x \cdot (\sqrt{x^2 + y^2})'_y}{\sqrt{x^2 + y^2}^2} =$$

$$= \underline{\hspace{10cm}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x \cdot (\sqrt{x^2 + y^2})'_y}{\sqrt{x^2 + y^2}^2} =$$

$$= \frac{\quad}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x \cdot (\sqrt{x^2 + y^2})'_y}{\sqrt{x^2 + y^2}^2} =$$

0

$$= \frac{0}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x \cdot (\sqrt{x^2 + y^2})'_y}{\sqrt{x^2 + y^2}^2} =$$

0.

$$= \frac{\quad}{x^2 + y^2}$$

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$$\frac{0 \cdot \sqrt{x^2 + y^2}}{x^2 + y^2}$$

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$$0 \cdot \sqrt{x^2 + y^2} -$$

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$$\frac{0 \cdot \sqrt{x^2 + y^2} - x}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x \cdot (\sqrt{x^2 + y^2})'_y}{\sqrt{x^2 + y^2}^2} =$$

$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$0 \cdot \sqrt{x^2 + y^2} - x \cdot$$

$$= \frac{\quad}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}}}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}} \cdot (x^2 + y^2)'_y}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}} \cdot (x^2 + y^2)'_y}{x^2 + y^2} =$$

$$= \underline{\hspace{2cm}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}} \cdot (x^2 + y^2)'_y}{x^2 + y^2} =$$

$$= \frac{-x}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}} \cdot (x^2 + y^2)'_y}{x^2 + y^2} =$$

$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}}}{x^2 + y^2}$$

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$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2}$$

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$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \underline{\hspace{2cm}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}} \cdot (x^2 + y^2)'_y}{x^2 + y^2} =$$

$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \frac{-x}{x^2 + y^2}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \frac{-xy}{\sqrt{x^2 + y^2} \cdot (x^2 + y^2)}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \frac{-xy}{\sqrt{x^2 + y^2} \cdot (x^2 + y^2)} =$$

$$= \underline{\hspace{2cm}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

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$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \frac{-xy}{\sqrt{x^2 + y^2} \cdot (x^2 + y^2)} =$$

$$= \frac{-xy}{(x^2 + y^2)\sqrt{x^2 + y^2}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

$$z = \frac{x}{\sqrt{x^2 + y^2}}$$

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$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}} \cdot (x^2 + y^2)'_y}{x^2 + y^2} =$$

$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \frac{-xy}{\sqrt{x^2 + y^2} \cdot (x^2 + y^2)} =$$

$$= \frac{-xy}{(x^2 + y^2)\sqrt{x^2 + y^2}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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$$(\sqrt{x})' = \frac{1}{2\sqrt{x}}$$

$$= \frac{0 \cdot \sqrt{x^2 + y^2} - x \cdot \frac{1}{2\sqrt{x^2 + y^2}} \cdot (x^2 + y^2)'_y}{x^2 + y^2} =$$

$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \frac{-xy}{\sqrt{x^2 + y^2} \cdot (x^2 + y^2)} =$$

$$= \frac{-xy}{(x^2 + y^2)\sqrt{x^2 + y^2}} = \frac{-xy}{(x^2 + y^2)^{3/2}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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$$z_y = \frac{(x)'_y \cdot \sqrt{x^2 + y^2} - x \cdot (\sqrt{x^2 + y^2})'_y}{\sqrt{x^2 + y^2}^2} =$$

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$$= \frac{-\frac{x}{2\sqrt{x^2 + y^2}} \cdot 2y}{x^2 + y^2} = \frac{-xy}{\sqrt{x^2 + y^2} \cdot (x^2 + y^2)} =$$

$$= \frac{-xy}{(x^2 + y^2)\sqrt{x^2 + y^2}} = \frac{-xy}{(x^2 + y^2)^{\frac{3}{2}}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(\sqrt{\text{nešto}})' = \frac{1}{2\sqrt{\text{nešto}}} \cdot (\text{nešto})'$$

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$$= \frac{-xy}{(x^2 + y^2)\sqrt{x^2 + y^2}} = \frac{-xy}{(x^2 + y^2)^{\frac{3}{2}}}$$

$$\left(\frac{u}{v}\right)'(x) = \frac{u'(x) \cdot v(x) - u(x) \cdot v'(x)}{v(x)^2}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

c) $z_x =$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

c) $z_x = 2^{\sin \frac{y}{x}} \ln 2$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

c) $z_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$\text{c)} \quad z_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$\text{c)} \quad z_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\text{c)} \quad z_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\text{c) } z_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\text{c) } z_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x}.$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\text{c) } z_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z_y =$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z_y = 2^{\sin \frac{y}{x}} \ln 2$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

c)

$$\begin{aligned} z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

c)

$$\begin{aligned} z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

c)

$$\begin{aligned} z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

c)

$$\begin{aligned} z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

c)

$$\begin{aligned} z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

c)

$$\begin{aligned} z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} = \frac{1}{x} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

c)

$$\begin{aligned} z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \\ z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} = \frac{1}{x} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(x^n)' = nx^{n-1}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$\begin{aligned} z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} = \frac{1}{x} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z = x^y$$

$$\text{d)} \quad z_x$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(x^n)' = nx^{n-1}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c) } z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$\begin{aligned} z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} = \frac{1}{x} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z = x^y$$

$$\text{d) } z_x = yx^{y-1}$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(x^n)' = nx^{n-1}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c)} \quad z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$\begin{aligned} z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} = \frac{1}{x} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z = x^y$$

$$\text{d)} \quad z_x = yx^{y-1}$$

$$z_y =$$

$$(a^x)' = a^x \ln a$$

$$(a^{\text{nešto}})' = a^{\text{nešto}} \ln a \cdot (\text{nešto})'$$

$$z = 2^{\sin \frac{y}{x}}$$

$$(x^n)' = nx^{n-1}$$

$$(\sin x)' = \cos x$$

$$(\sin(\text{nešto}))' = \cos(\text{nešto}) \cdot (\text{nešto})'$$

$$\begin{aligned} \text{c) } z_x &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_x = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_x = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{-y}{x^2} = -\frac{y}{x^2} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$\begin{aligned} z_y &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \left(\sin \frac{y}{x} \right)'_y = 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \left(\frac{y}{x} \right)'_y = \\ &= 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \cdot \frac{1}{x} = \frac{1}{x} \cdot 2^{\sin \frac{y}{x}} \ln 2 \cdot \cos \frac{y}{x} \end{aligned}$$

$$z = x^y$$

$$\text{d) } z_x = yx^{y-1}$$

$$z_y = x^y \ln x$$

čtvrti zadatak

Zadatak 4

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x =$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz}.$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y =$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 -$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

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u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz}.$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

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u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z =$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$(\ln x)' = \frac{1}{x}$$

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

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Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z -$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$(\ln x)' = \frac{1}{x}$$

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

$$(\ln x)' = \frac{1}{x}$$

u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

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u točki $(0, 2, 1)$.

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Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z + 0$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

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$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z + 0 = e^{2xz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$(\ln x)' = \frac{1}{x}$$

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Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

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$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z + 0 = e^{2xz} \cdot$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

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u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z + 0 = e^{2xz} \cdot 2x$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

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Izračunajte vrijednosti parcijalnih derivacija funkcije

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u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z + 0 = e^{2xz} \cdot 2x - \frac{1}{yz}$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

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u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

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$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z + 0 = e^{2xz} \cdot 2x - \frac{1}{yz} \cdot$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

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u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

$$f_x = e^{2xz} \cdot (2xz)'_x - 0 + 0 = e^{2xz} \cdot 2z = 2ze^{2xz}$$

$$f_y = 0 - \frac{1}{yz} \cdot (yz)'_y + 0 = -\frac{1}{yz} \cdot z = -\frac{1}{y}$$

$$f_z = e^{2xz} \cdot (2xz)'_z - \frac{1}{yz} \cdot (yz)'_z + 0 = e^{2xz} \cdot 2x - \frac{1}{yz} \cdot y$$

Zadatak 4

$$(e^{\text{nešto}})' = e^{\text{nešto}} \cdot (\text{nešto})'$$

$$(e^x)' = e^x$$

Izračunajte vrijednosti parcijalnih derivacija funkcije

$$f(x, y, z) = e^{2xz} - \ln(yz) + 1$$

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u točki $(0, 2, 1)$.

$$(\ln(\text{nešto}))' = \frac{1}{\text{nešto}} \cdot (\text{nešto})'$$

Rješenje

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Zadatak 4

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Parcijalne derivacije drugog reda – oznake

Parcijalne derivacije drugog reda – oznake

- Funkcija dvije varijable: $z = z(x, y)$

z_{xx}	z'_{xx}	$\frac{\partial^2 z}{\partial x^2}$
z_{xy}	z'_{xy}	$\frac{\partial^2 z}{\partial x \partial y}$
z_{yx}	z'_{yx}	$\frac{\partial^2 z}{\partial y \partial x}$
z_{yy}	z'_{yy}	$\frac{\partial^2 z}{\partial y^2}$

peti zadatak

Zadatak 5

Odredite parcijalne derivacije drugog reda funkcije $z(x, y) = y^2 \cdot 2^x$.

Zadatak 5

Odredite parcijalne derivacije drugog reda funkcije $z(x, y) = y^2 \cdot 2^x$.

Rješenje

$$z_x =$$

$$(a^x)' = a^x \ln a$$

$$(x^n)' = nx^{n-1}$$

Zadatak 5

Odredite parcijalne derivacije drugog reda funkcije $z(x, y) = y^2 \cdot 2^x$.

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$$z_x = y^2 \cdot 2^x \ln 2$$

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Rješenje

$$(a^x)' = a^x \ln a$$

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$$z_y =$$

Zadatak 5

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$$(a^x)' = a^x \ln a$$

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$$z_y = 2^x \cdot 2y$$

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$$z_y = 2^x \cdot 2y = y \cdot 2^{x+1}$$

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$$z_{xy} = (z_x)_y = 2^x \ln 2 \cdot 2y = y \cdot 2^{x+1} \ln 2$$

Zadatak 5

Odredite parcijalne derivacije drugog reda funkcije $z(x, y) = y^2 \cdot 2^x$.

Rješenje

$$(a^x)' = a^x \ln a$$

$$(x^n)' = nx^{n-1}$$

$$z_x = y^2 \cdot 2^x \ln 2$$

$$z_y = 2^x \cdot 2y = y \cdot 2^{x+1}$$

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Zadatak 5

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$$z_{yy} =$$

Zadatak 5

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$$z_{yy} = (z_y)_y = 2^{x+1}.$$

Zadatak 5

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$$z_{yx} = (z_y)_x = y \cdot 2^{x+1} \ln 2 \cdot (x+1)'_x = y \cdot 2^{x+1} \ln 2$$

$$z_{yy} = (z_y)_y = 2^{x+1} \cdot 1$$

Zadatak 5

Odredite parcijalne derivacije drugog reda funkcije $z(x, y) = y^2 \cdot 2^x$.

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Zadatak 5

Odredite parcijalne derivacije drugog reda funkcije $z(x, y) = y^2 \cdot 2^x$.

Rješenje

$$(a^x)' = a^x \ln a$$

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$$z_{yy} = (z_y)_y = 2^{x+1} \cdot 1 = 2^{x+1}$$

šesti zadatak

Zadatak 6

Zadana je funkcija $f(x, y, z) = z \cdot y^x$. Odredite $\frac{\partial^3 f}{\partial x \partial y \partial z}$.

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Rješenje

$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

Zadatak 6

Zadana je funkcija $f(x, y, z) = z \cdot y^x$. Odredite $\frac{\partial^3 f}{\partial x \partial y \partial z}$.

Rješenje

$$f_x =$$

$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

Zadatak 6

Zadana je funkcija $f(x, y, z) = z \cdot y^x$. Odredite $\frac{\partial^3 f}{\partial x \partial y \partial z}$.

Rješenje

$$f_x = z \cdot$$

$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

$$(a^x)' = a^x \ln a$$

Zadatak 6

Zadana je funkcija $f(x, y, z) = z \cdot y^x$. Odredite $\frac{\partial^3 f}{\partial x \partial y \partial z}$.

Rješenje

$$f_x = z \cdot y^x \ln y$$

$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

$$(a^x)' = a^x \ln a$$

Zadatak 6

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Rješenje

$$f_x = z \cdot y^x \ln y = zy^x \ln y$$

$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

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$$f_x = z \cdot y^x \ln y = zy^x \ln y$$

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$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

$$(a^x)' = a^x \ln a$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

Zadatak 6

Zadana je funkcija $f(x, y, z) = z \cdot y^x$. Odredite $\frac{\partial^3 f}{\partial x \partial y \partial z}$.

Rješenje

$$f_x = z \cdot y^x \ln y = zy^x \ln y$$

$$f_{xy} = (f_x)_y$$

$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

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Rješenje

$$f_x = z \cdot y^x \ln y = zy^x \ln y$$

$$f_{xy} = (f_x)_y = z$$

$$\frac{\partial^3 f}{\partial x \partial y \partial z} \rightarrow f_{xyz}$$

$$(a^x)' = a^x \ln a$$

$$(x^n)' = nx^{n-1}$$

$$(uv)'(x) = u'(x) \cdot v(x) + u(x) \cdot v'(x)$$

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Zadatak 6

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$$(a^x)' = a^x \ln a$$

$$(x^n)' = nx^{n-1}$$

$$(\ln x)' = \frac{1}{x}$$

sedmi zadatak

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

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Rješenje

$$f_x =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$f_x = 3x^2 - 3$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$f_x = 3x^2 - 3$$

$$f_y =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$f_x = 3x^2 - 3$$

$$f_y = -2y + 12$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \\ f_y = -2y + 12 & -2y + 12 = 0 \end{array}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \\ f_y = -2y + 12 & -2y + 12 = 0 \end{array}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \end{array}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke:

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

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Stacionarne točke: $\overset{x_1}{1}, \overset{y}{6}, (\overset{x_2}{-1}, \overset{y}{6})$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{1}, \overset{y}{6}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{1}, \overset{y}{6}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{1}, \overset{y}{6}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{1}, \overset{y}{6}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{1}, \overset{y}{6}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

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Stacionarne točke: $\overset{x_1}{1}, \overset{y}{6}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, 6)}, \overset{x_2}{(-1, 6)}$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, 6)}, \overset{x_2}{(-1, 6)}$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

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Stacionarne točke: $\overset{x_1}{(1, 6)}, \overset{x_2}{(-1, 6)}$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(1, 6) =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$\overset{x}{H}(\overset{y}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$\overset{x}{H}(\overset{y}{1}, 6) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, 6)}, \overset{x_2}{(-1, 6)}$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, 6)}, \overset{x_2}{(-1, 6)}$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(-1, 6) =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} -6 & 0 \\ 0 & -2 \end{vmatrix}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} -6 & 0 \\ 0 & -2 \end{vmatrix} = 12$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} -6 & 0 \\ 0 & -2 \end{vmatrix} = 12 > 0$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, 6)}, \overset{x_2}{(-1, 6)}$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} \overset{<0}{-6} & 0 \\ 0 & -2 \end{vmatrix} = 12 > 0$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2 \qquad H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} \overset{<0}{-6} & 0 \\ 0 & -2 \end{vmatrix} = 12 > 0 \longrightarrow \text{točka lokalnog maksimuma}$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} \overset{<0}{-6} & 0 \\ 0 & -2 \end{vmatrix} = 12 > 0 \longrightarrow \text{točka lokalnog maksimuma}$$

$$f(-1, 6) =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2 \qquad H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \longrightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} \overset{<0}{-6} & 0 \\ 0 & -2 \end{vmatrix} = 12 > 0 \longrightarrow \text{točka lokalnog maksimuma}$$

$$f(\overset{x}{-1}, \overset{y}{6}) =$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \rightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} \overset{<0}{-6} & 0 \\ 0 & -2 \end{vmatrix} = 12 > 0 \rightarrow \text{točka lokalnog maksimuma}$$

$$f(\overset{x}{-1}, \overset{y}{6}) = 80 - 6^2 + (-1)^3 + 12 \cdot 6 - 3 \cdot (-1)$$

Zadatak 7

Odredite lokalne ekstreme funkcije $f(x, y) = 80 - y^2 + x^3 + 12y - 3x$.

Rješenje

$$\begin{array}{l|l} f_x = 3x^2 - 3 & 3x^2 - 3 = 0 \rightarrow x^2 = 1 \rightarrow x_1 = 1, x_2 = -1 \\ f_y = -2y + 12 & -2y + 12 = 0 \rightarrow y = 6 \end{array}$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y}{6})}, (\overset{x_2}{-1}, \overset{y}{6})$

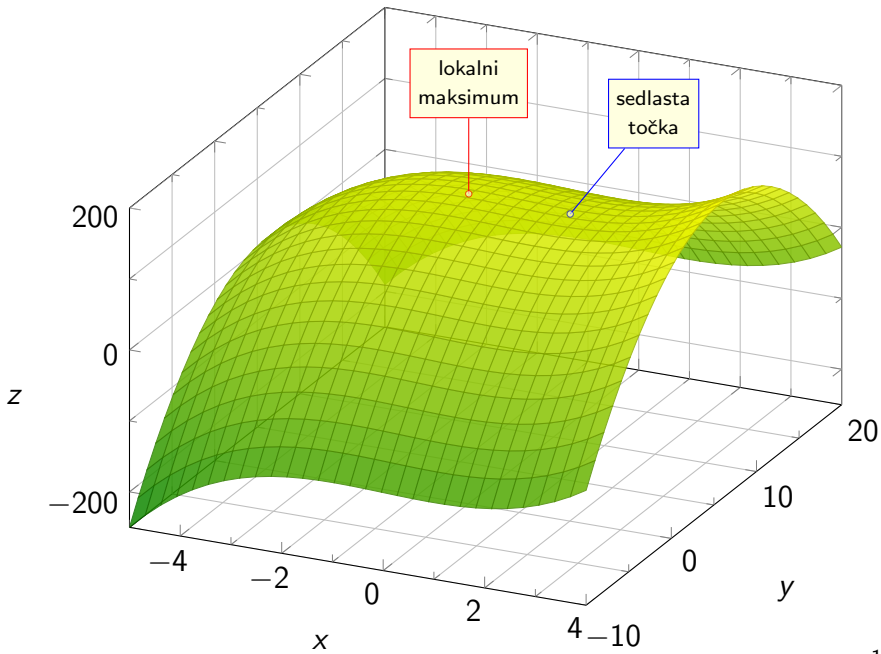
$$f_{xx} = 6x, \quad f_{xy} = 0, \quad f_{yy} = -2$$

$$H(x, y) = \begin{vmatrix} f_{xx} & f_{xy} \\ f_{xy} & f_{yy} \end{vmatrix} = \begin{vmatrix} 6x & 0 \\ 0 & -2 \end{vmatrix}$$

$$H(\overset{x}{1}, \overset{y}{6}) = \begin{vmatrix} 6 & 0 \\ 0 & -2 \end{vmatrix} = -12 < 0 \rightarrow \text{sedlasta točka}$$

$$H(\overset{x}{-1}, \overset{y}{6}) = \begin{vmatrix} \overset{<0}{-6} & 0 \\ 0 & -2 \end{vmatrix} = 12 > 0 \rightarrow \text{točka lokalnog maksimuma}$$

$$f(\overset{x}{-1}, \overset{y}{6}) = 80 - 6^2 + (-1)^3 + 12 \cdot 6 - 3 \cdot (-1) = 118 \quad 13/24$$



osmi zadatak

Zadatak 8

Odredite lokalne ekstreme funkcije

$$z(x, y) = \frac{8}{x} + \frac{x}{y} + y.$$

Zadatak 8

Odredite lokalne ekstreme funkcije

$$z(x, y) = \frac{8}{x} + \frac{x}{y} + y.$$

Rješenje

- $x \neq 0, y \neq 0$

Zadatak 8

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$$z(x, y) = \frac{8}{x} + \frac{x}{y} + y.$$

Rješenje

$$z(x, y) = 8x^{-1} + xy^{-1} + y$$

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Rješenje

$$z(x, y) = 8x^{-1} + xy^{-1} + y$$

- $x \neq 0, y \neq 0$

$$z_x =$$

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Rješenje

$$z(x, y) = 8x^{-1} + xy^{-1} + y$$

- $x \neq 0, y \neq 0$

$$z_x = -8x^{-2}$$

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Zadatak 8

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$$z(x, y) = \frac{8}{x} + \frac{x}{y} + y.$$

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$$z_x = -8x^{-2} + y^{-1}$$

$$z_y =$$

Zadatak 8

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$$z(x, y) = \frac{8}{x} + \frac{x}{y} + y.$$

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$$z(x, y) = \frac{8}{x} + \frac{x}{y} + y.$$

Rješenje

$$z(x, y) = 8x^{-1} + xy^{-1} + y$$

- $x \neq 0, y \neq 0$

$$z_x = -8x^{-2} + y^{-1}$$

$$-8x^{-2} + y^{-1} = 0$$

$$z_y = -xy^{-2} + 1$$

$$-xy^{-2} + 1 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

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$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$x^2y$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y}{x^2y}$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y +}{x^2y}$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y}$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

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$$-8x^{-2} + y^{-1} = 0$$

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$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$y^2$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x}{y^2}$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

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$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x +}{y^2}$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2}$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

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$$\frac{-8y + x^2}{x^2y} = 0$$

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$$\frac{-8y + x^2}{x^2y} = 0$$

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$$-8y + x^2 = 0$$

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$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$


$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

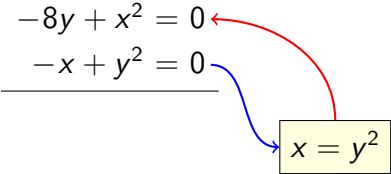
$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8x^{-2} + y^{-1} = 0$$

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$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

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$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

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$$-8x^{-2} + y^{-1} = 0$$

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$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$

$$y = 0$$

$$y^3 - 8 = 0$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$

$$\cancel{y = 0}$$

$$y^3 - 8 = 0$$

nije u domeni

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$


$$\underline{y = 0}$$

nije u domeni

$$y^3 - 8 = 0$$

$$y = 2$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$


$$\cancel{y = 0}$$

nije u domeni

$$y^3 - 8 = 0$$

$$y = 2$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$


$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$


$$y = 0$$

nije u domeni

$$y^3 - 8 = 0$$

$$y = 2$$

$$-8x^{-2} + y^{-1} = 0$$

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$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

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$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$

$$\cancel{y = 0}$$

nije u domeni

$$y^3 - 8 = 0$$

$$y = 2$$

$$x = 4$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$

$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$

~~$$y = 0$$~~

nije u domeni

$$y^3 - 8 = 0$$

$$y = 2$$

$$x = 4$$

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$

$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$

$$x = 4$$

~~$$y = 0$$~~

nije u domeni

$$y^3 - 8 = 0$$

$$y = 2$$

Stacionarna točka:

$$-8x^{-2} + y^{-1} = 0$$

$$-xy^{-2} + 1 = 0$$

$$-\frac{8}{x^2} + \frac{1}{y} = 0$$

$$-\frac{x}{y^2} + 1 = 0$$

$$\frac{-8y + x^2}{x^2y} = 0$$

$$\frac{-x + y^2}{y^2} = 0$$

$$-8y + x^2 = 0$$

$$-x + y^2 = 0$$

$$x = y^2$$

$$-8y + (y^2)^2 = 0$$

$$-8y + y^4 = 0$$

$$y(y^3 - 8) = 0$$

~~$$y = 0$$~~

nije u domeni

$$y^3 - 8 = 0$$

$$y = 2$$

$$x = 4$$

Stacionarna točka: (4, 2)

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} =$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8.$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} =$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} =$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot (-2)y^{-3}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot (-2)y^{-3} = \frac{2x}{y^3}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot (-2)y^{-3} = \frac{2x}{y^3}$$

$$H(x, y) = \begin{vmatrix} \frac{16}{x^3} & -\frac{1}{y^2} \\ -\frac{1}{y^2} & \frac{2x}{y^3} \end{vmatrix}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot (-2)y^{-3} = \frac{2x}{y^3}$$

$$H(x, y) = \begin{vmatrix} \frac{16}{x^3} & -\frac{1}{y^2} \\ -\frac{1}{y^2} & \frac{2x}{y^3} \end{vmatrix}$$

$$H(4, 2) =$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot (-2)y^{-3} = \frac{2x}{y^3}$$

$$H(x, y) = \begin{vmatrix} \frac{16}{x^3} & -\frac{1}{y^2} \\ -\frac{1}{y^2} & \frac{2x}{y^3} \end{vmatrix}$$

$$H(\overset{x}{4}, \overset{y}{2}) =$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot (-2)y^{-3} = \frac{2x}{y^3}$$

$$H(x, y) = \begin{vmatrix} \frac{16}{x^3} & -\frac{1}{y^2} \\ -\frac{1}{y^2} & \frac{2x}{y^3} \end{vmatrix}$$

$$H(\overset{x}{4}, \overset{y}{2}) = \begin{vmatrix} \frac{1}{4} & -\frac{1}{4} \\ -\frac{1}{4} & 1 \end{vmatrix}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

$$z_{yy} = -x \cdot (-2)y^{-3} = \frac{2x}{y^3}$$

$$H(x, y) = \begin{vmatrix} \frac{16}{x^3} & -\frac{1}{y^2} \\ -\frac{1}{y^2} & \frac{2x}{y^3} \end{vmatrix}$$

$$H(\overset{x}{4}, \overset{y}{2}) = \begin{vmatrix} \frac{1}{4} & -\frac{1}{4} \\ -\frac{1}{4} & 1 \end{vmatrix} = \frac{1}{4} - \frac{1}{16}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

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$$H(\overset{x}{4}, \overset{y}{2}) = \begin{vmatrix} \overset{0}{\left(\frac{1}{4}\right)} & -\frac{1}{4} \\ -\frac{1}{4} & 1 \end{vmatrix} = \frac{1}{4} - \frac{1}{16} = \frac{3}{16} > 0$$

$$z_x = -8x^{-2} + y^{-1}$$

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$$H(x, y) = \begin{vmatrix} \frac{16}{x^3} & -\frac{1}{y^2} \\ -\frac{1}{y^2} & \frac{2x}{y^3} \end{vmatrix}$$

$$H(4, 2) = \begin{vmatrix} \frac{1}{4} & -\frac{1}{4} \\ -\frac{1}{4} & 1 \end{vmatrix} = \frac{1}{4} - \frac{1}{16} = \frac{3}{16} > 0 \longrightarrow \text{točka lokalnog minimuma}$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

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$$H(x, y) = \begin{vmatrix} \frac{16}{x^3} & -\frac{1}{y^2} \\ -\frac{1}{y^2} & \frac{2x}{y^3} \end{vmatrix}$$

$$H(4, 2) = \begin{vmatrix} \frac{1}{4} & -\frac{1}{4} \\ -\frac{1}{4} & 1 \end{vmatrix} = \frac{1}{4} - \frac{1}{16} = \frac{3}{16} > 0 \longrightarrow \text{točka lokalnog minimuma}$$

$$z(4, 2) =$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

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$$z(4, 2) =$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

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$$z(4, 2) = \frac{8}{4} + \frac{4}{2} + 2$$

$$z_x = -8x^{-2} + y^{-1}$$

$$z_y = -xy^{-2} + 1$$

$$z = \frac{8}{x} + \frac{x}{y} + y$$

$$z_{xx} = -8 \cdot (-2)x^{-3} = \frac{16}{x^3}$$

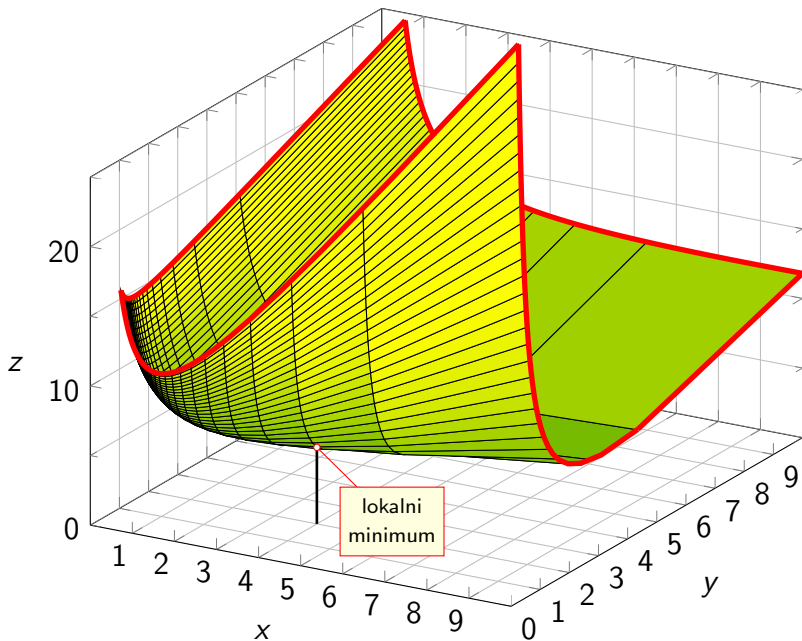
$$z_{xy} = -1 \cdot y^{-2} = -\frac{1}{y^2}$$

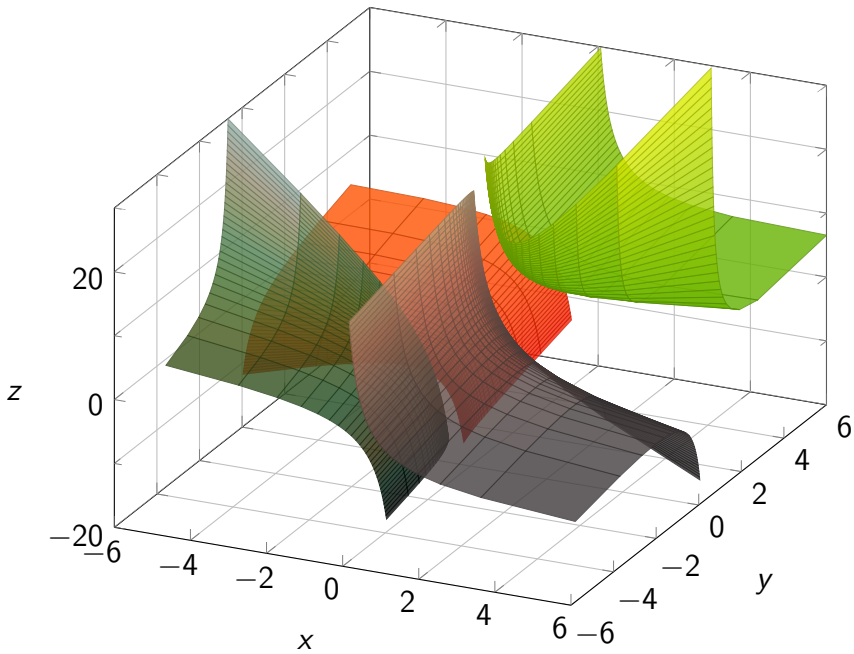
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$$z(4, 2) = \frac{8}{4} + \frac{4}{2} + 2 = 6$$





deveti zadatak

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje

$$x + y = 4$$

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje

$$x + y = 4 \implies y = 4 - x$$

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Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje

$$x + y = 4 \implies$$


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$$z(x, 4 - x) =$$

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje


$$x + y = 4 \implies \boxed{y = 4 - x}$$


$$z(x, 4 - x) = e^{x \cdot (4 - x)}$$

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje


$$x + y = 4 \implies y = 4 - x$$



$$z(x, 4 - x) = e^{x \cdot (4 - x)} = e^{4x - x^2}$$

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje


$$x + y = 4 \implies \boxed{y = 4 - x}$$


$$z(x, 4 - x) = e^{x \cdot (4 - x)} = e^{4x - x^2} \longrightarrow f(x) = e^{4x - x^2}$$


Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

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$$x + y = 4 \implies \boxed{y = 4 - x}$$



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Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje

$$x + y = 4 \implies \boxed{y = 4 - x}$$



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$$z(x, 4 - x) = e^{x \cdot (4 - x)} = e^{4x - x^2} \longrightarrow f(x) = e^{4x - x^2}$$

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Zadatak 9

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$$(4 - 2x)e^{4x - x^2} = 0$$


$$4 - 2x = 0$$

$$x = 2$$

Zadatak 9

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Zadatak 9

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Rješenje

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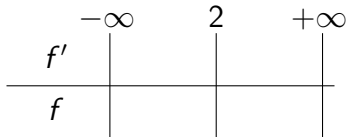
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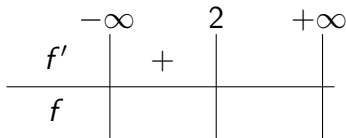
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Rješenje

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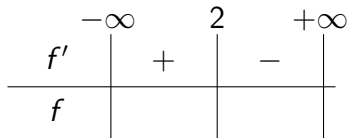
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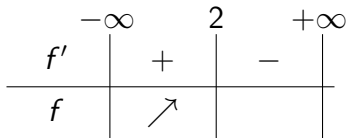
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	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

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globalni maksimum

$$(4 - 2x)e^{4x - x^2} = 0$$

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	$-\infty$		2		$+\infty$
f'		+		-	
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globalni maksimum

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	$-\infty$		2		$+\infty$
f'		+		-	
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$$y = 4 - x$$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

Zadatak 9

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globalni maksimum

$$(4 - 2x)e^{4x - x^2} = 0$$

$$4 - 2x = 0$$

$$\boxed{x = 2}$$

$$y = 4 - x = 4 - 2 = 2$$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

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globalni maksimum

$$(4 - 2x)e^{4x - x^2} = 0$$

$$4 - 2x = 0$$

$$x = 2$$

$$y = 4 - x = 4 - 2 = 2 \quad y = 2$$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

Zadatak 9

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$$x + y = 4 \implies y = 4 - x$$

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globalni maksimum

$$(4 - 2x)e^{4x - x^2} = 0$$

$$4 - 2x = 0$$

$$x = 2$$

$$y = 4 - x = 4 - 2 = 2$$

$$y = 2$$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

stacionarna točka:

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

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$$x + y = 4 \implies y = 4 - x$$

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$$(4 - 2x)e^{4x - x^2} = 0$$

$$4 - 2x = 0$$

$$x = 2$$

$$y = 4 - x = 4 - 2 = 2$$

$$y = 2$$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

stacionarna točka: $(\overset{x}{2}, \overset{y}{2})$

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje

$$x + y = 4 \implies \boxed{y = 4 - x}$$

$$z(x, 4 - x) = e^{x \cdot (4 - x)} = e^{4x - x^2} \longrightarrow f(x) = e^{4x - x^2}$$

$$f'(x) = e^{4x - x^2} \cdot (4x - x^2)' = (4 - 2x)e^{4x - x^2}$$

$$f(2) = e^4$$

globalni maksimum

$$(4 - 2x)e^{4x - x^2} = 0$$

$$4 - 2x = 0$$

$$\boxed{x = 2}$$

$$y = 4 - x = 4 - 2 = 2$$

$$\boxed{y = 2}$$

stacionarna točka: $\overset{x}{2}, \overset{y}{2}$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

Funkcija z postiže globalni maksimum uz uvjet $x + y = 4$ u točki $(2, 2)$

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje

$$x + y = 4 \implies y = 4 - x$$

$$z(x, 4 - x) = e^{x \cdot (4 - x)} = e^{4x - x^2} \longrightarrow f(x) = e^{4x - x^2}$$

$$f'(x) = e^{4x - x^2} \cdot (4x - x^2)' = (4 - 2x)e^{4x - x^2}$$

$$f(2) = e^4$$

globalni maksimum

$$(4 - 2x)e^{4x - x^2} = 0$$

$$4 - 2x = 0$$

$$x = 2$$

$$y = 4 - x = 4 - 2 = 2$$

$$y = 2$$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

stacionarna točka: $(2, 2)$

Funkcija z postiže globalni maksimum uz uvjet $x + y = 4$ u točki $(2, 2)$ i taj maksimum je jednak

Zadatak 9

Odredite ekstreme funkcije $z(x, y) = e^{xy}$ uz uvjet $x + y = 4$.

Rješenje

$$x + y = 4 \implies \boxed{y = 4 - x}$$

$$z(x, 4 - x) = e^{x \cdot (4 - x)} = e^{4x - x^2} \longrightarrow f(x) = e^{4x - x^2}$$

$$f'(x) = e^{4x - x^2} \cdot (4x - x^2)' = (4 - 2x)e^{4x - x^2}$$

$$f(2) = e^4$$

globalni maksimum

$$(4 - 2x)e^{4x - x^2} = 0$$

$$4 - 2x = 0$$

$$\boxed{x = 2}$$

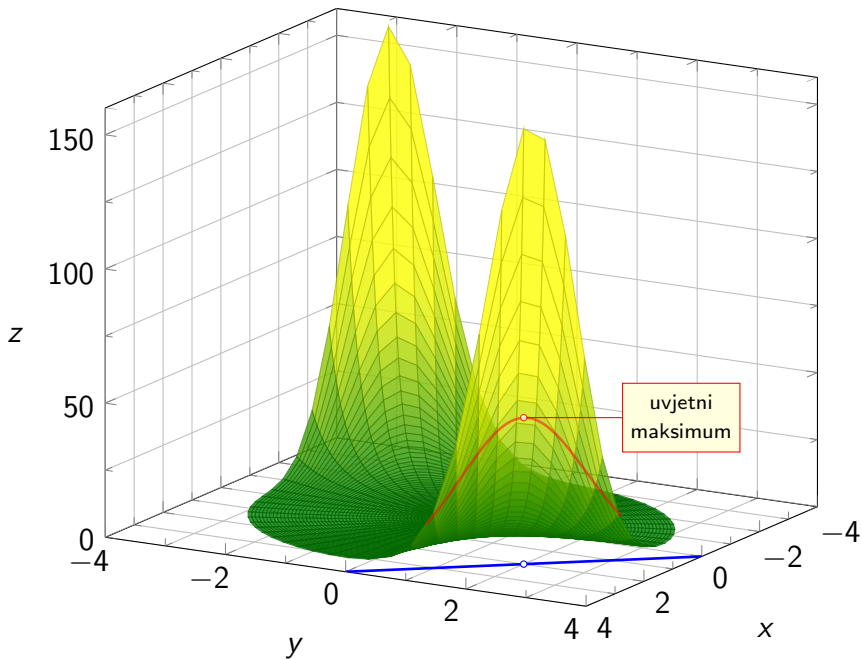
$$y = 4 - x = 4 - 2 = 2$$

$$\boxed{y = 2}$$

stacionarna točka: $\overset{x}{2} \overset{y}{2}$

	$-\infty$		2		$+\infty$
f'		+		-	
f		\nearrow		\searrow	

Funkcija z postiže globalni maksimum uz uvjet $x + y = 4$ u točki $(2, 2)$ i taj maksimum je jednak $z(2, 2) = e^4$.



deseti zadatak

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

- Lagrangeova funkcija

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

- Lagrangeova funkcija

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

funkcija

- Lagrangeova funkcija

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

- Lagrangeova funkcija

funkcija

uvjet

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

- Lagrangeova funkcija

funkcija

uvjet

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

- Lagrangeova funkcija

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

- Parcijalne derivacije Lagrangeove funkcije

$$L_x =$$

funkcija

uvjet

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

funkcija

- Lagrangeova funkcija

uvjet

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

- Parcijalne derivacije Lagrangeove funkcije

$$L_x = -1 + 2\lambda x$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

- Lagrangeova funkcija

funkcija

uvjet

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

- Parcijalne derivacije Lagrangeove funkcije

$$L_x = -1 + 2\lambda x$$

$$L_y =$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

funkcija

- Lagrangeova funkcija

uvjet

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

- Parcijalne derivacije Lagrangeove funkcije

$$L_x = -1 + 2\lambda x$$

$$L_y = -1 + 2\lambda y$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

funkcija

- Lagrangeova funkcija

uvjet

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

- Parcijalne derivacije Lagrangeove funkcije

$$L_x = -1 + 2\lambda x$$

$$L_y = -1 + 2\lambda y$$

$$L_\lambda =$$

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

- Lagrangeova funkcija

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

- Parcijalne derivacije Lagrangeove funkcije

$$L_x = -1 + 2\lambda x$$

$$L_y = -1 + 2\lambda y$$

$$L_\lambda = x^2 + y^2 - 2$$

funkcija

uvjet

Zadatak 10

Odredite ekstreme funkcije $f(x, y) = -x - y$ uz uvjet $x^2 + y^2 = 2$.

Rješenje

$$x^2 + y^2 = 2 \longrightarrow x^2 + y^2 - 2 = 0$$

funkcija

- Lagrangeova funkcija

uvjet

$$L(x, y, \lambda) = \text{funkcija} + \lambda \cdot \text{uvjet}$$

$$L(x, y, \lambda) = -x - y + \lambda(x^2 + y^2 - 2)$$

- Parcijalne derivacije Lagrangeove funkcije

$$L_x = -1 + 2\lambda x$$

$$-1 + 2\lambda x = 0$$

$$L_y = -1 + 2\lambda y$$

$$-1 + 2\lambda y = 0$$

$$L_\lambda = x^2 + y^2 - 2$$

$$x^2 + y^2 - 2 = 0$$

$$-1 + 2\lambda x = 0$$

$$-1 + 2\lambda y = 0$$

$$x^2 + y^2 - 2 = 0$$

$$-1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1$$

$$-1 + 2\lambda y = 0$$

$$\underline{x^2 + y^2 - 2 = 0}$$

$$-1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x}$$

$$-1 + 2\lambda y = 0$$

$$\underline{x^2 + y^2 - 2 = 0}$$

$$-1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x}$$

$$-1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1$$

$$\underline{x^2 + y^2 - 2 = 0}$$

$$-1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x}$$

$$-1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y}$$

$$x^2 + y^2 - 2 = 0$$

$$\begin{array}{l}
 -1 + 2\lambda x = 0 \quad \longrightarrow \quad 2\lambda x = 1 \quad \xrightarrow{\quad} \quad \lambda = \frac{1}{2x} \\
 -1 + 2\lambda y = 0 \quad \longrightarrow \quad 2\lambda y = 1 \quad \xrightarrow{\quad} \quad \lambda = \frac{1}{2y} \\
 \hline x^2 + y^2 - 2 = 0
 \end{array}
 \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \\ x^2 + y^2 - 2 = 0 \end{array}} \right\} \implies \frac{1}{2x} = \frac{1}{2y}$$

$$\begin{array}{l}
 -1 + 2\lambda x = 0 \quad \longrightarrow \quad 2\lambda x = 1 \quad \xrightarrow{\quad} \quad \lambda = \frac{1}{2x} \\
 -1 + 2\lambda y = 0 \quad \longrightarrow \quad 2\lambda y = 1 \quad \xrightarrow{\quad} \quad \lambda = \frac{1}{2y} \\
 \hline x^2 + y^2 - 2 = 0
 \end{array}
 \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \\ x^2 + y^2 - 2 = 0 \end{array}} \right\} \implies \begin{array}{l} \frac{1}{2x} = \frac{1}{2y} \\ x = y \end{array}$$

$$\begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \\ \underline{x^2 + y^2 - 2 = 0} \end{array} \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \end{array}} \right\} \implies \frac{1}{2x} = \frac{1}{2y} \implies \boxed{x = y}$$

$$\begin{array}{l}
 -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\
 -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y}
 \end{array}
 \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \end{array}} \right\} \implies \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

 $x^2 + y^2 - 2 = 0$

$$\begin{array}{l}
 -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\
 -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y}
 \end{array}
 \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \end{array}} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

$$x^2 + y^2 - 2 = 0$$

$$x^2 + x^2 - 2 = 0$$

$$\begin{array}{lcl}
 -1 + 2\lambda x = 0 & \longrightarrow & 2\lambda x = 1 \\
 -1 + 2\lambda y = 0 & \longrightarrow & 2\lambda y = 1
 \end{array}
 \left. \begin{array}{l} \longrightarrow \lambda = \frac{1}{2x} \\ \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

$$\begin{aligned}
 x^2 + y^2 - 2 &= 0 \\
 x^2 + x^2 - 2 &= 0 \\
 2x^2 &= 2
 \end{aligned}$$

$$\begin{array}{l}
 -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\
 -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y}
 \end{array}
 \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \end{array}} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

$$x^2 + y^2 - 2 = 0$$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$\begin{array}{l}
 -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\
 -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y}
 \end{array}
 \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \end{array}} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

$$x^2 + y^2 - 2 = 0$$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$\begin{array}{l}
 -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\
 -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y}
 \end{array}
 \left. \vphantom{\begin{array}{l} -1 + 2\lambda x = 0 \\ -1 + 2\lambda y = 0 \end{array}} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

$$x^2 + y^2 - 2 = 0$$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke:

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y}$$

$x = y$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y_1}{1})}, (\overset{x_2}{-1}, \overset{y_2}{-1})$

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y} \Rightarrow \boxed{x = y}$$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y_1}{1})}, (\overset{x_2}{-1}, \overset{y_2}{-1})$

$$\boxed{f(x, y) = -x - y}$$

- Neprekidna funkcija na kompaktnom skupu (konkretno, omeđenoj krivulji) postiže globalni minimum i globalni maksimum.

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y} \Rightarrow \boxed{x = y}$$

$x^2 + y^2 - 2 = 0$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y_1}{1})}, (\overset{x_2}{-1}, \overset{y_2}{-1})$

$$\boxed{f(x, y) = -x - y}$$

- Neprekidna funkcija na kompaktnom skupu (konkretno, omeđenoj krivulji) postiže globalni minimum i globalni maksimum.

$$f(1, 1) =$$

$$\left. \begin{array}{ll} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y} \Rightarrow \boxed{x = y}$$

$x^2 + y^2 - 2 = 0$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y_1}{1})}, (\overset{x_2}{-1}, \overset{y_2}{-1})$

$$\boxed{f(x, y) = -x - y}$$

- Neprekidna funkcija na kompaktnom skupu (konkretno, omeđenoj krivulji) postiže globalni minimum i globalni maksimum.

$$f(1, 1) = -1 - 1 = -2$$

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y} \Rightarrow \boxed{x = y}$$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, 1)}, \overset{x_2}{(-1, -1)}$

$$\boxed{f(x, y) = -x - y}$$

- Neprekidna funkcija na kompaktnom skupu (konkretno, omeđenoj krivulji) postiže globalni minimum i globalni maksimum.

$$f(1, 1) = -1 - 1 = -2$$

$$f(-1, -1) =$$

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y} \Rightarrow \boxed{x = y}$$

$x^2 + y^2 - 2 = 0$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y_1}{1})}, (\overset{x_2}{-1}, \overset{y_2}{-1})$

$$\boxed{f(x, y) = -x - y}$$

- Neprekidna funkcija na kompaktnom skupu (konkretno, omeđenoj krivulji) postiže globalni minimum i globalni maksimum.

$$f(1, 1) = -1 - 1 = -2$$

$$f(-1, -1) = -(-1) - (-1) = 2$$

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y} \Rightarrow \boxed{x = y}$$

$x^2 + y^2 - 2 = 0$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y_1}{1})}, (\overset{x_2}{-1}, \overset{y_2}{-1})$

$$\boxed{f(x, y) = -x - y}$$

- Neprekidna funkcija na kompaktnom skupu (konkretno, omeđenoj krivulji) postiže globalni minimum i globalni maksimum.

$$f(1, 1) = -1 - 1 = -2 \longleftarrow \boxed{\text{minimum}}$$

$$f(-1, -1) = -(-1) - (-1) = 2$$

$$\left. \begin{array}{l} -1 + 2\lambda x = 0 \longrightarrow 2\lambda x = 1 \longrightarrow \lambda = \frac{1}{2x} \\ -1 + 2\lambda y = 0 \longrightarrow 2\lambda y = 1 \longrightarrow \lambda = \frac{1}{2y} \end{array} \right\} \Rightarrow \frac{1}{2x} = \frac{1}{2y} \Rightarrow \boxed{x = y}$$

$x^2 + y^2 - 2 = 0$

$$x^2 + x^2 - 2 = 0$$

$$2x^2 = 2$$

$$x^2 = 1$$

$$x_1 = 1, \quad x_2 = -1$$

$$y_1 = 1, \quad y_2 = -1$$

Stacionarne točke: $\overset{x_1}{(1, \overset{y_1}{1})}, (\overset{x_2}{-1}, \overset{y_2}{-1})$

$$\boxed{f(x, y) = -x - y}$$

- Neprekidna funkcija na kompaktnom skupu (konkretno, omeđenoj krivulji) postiže globalni minimum i globalni maksimum.

$$f(1, 1) = -1 - 1 = -2 \longleftarrow \boxed{\text{minimum}}$$

$$f(-1, -1) = -(-1) - (-1) = 2 \longleftarrow \boxed{\text{maksimum}}$$

