## Fibonacci Heaps



## Glossary

Here are some terms that are used when discussing Fibonacci heaps:

- degree the number of children a node has
- root list a circular, doubly-linked list holding the root nodes of the subheaps
- child list a circular, doubly-linked list holding the children of a node in a subheap
- rootify turn a degree array into a root list (in log n time)
- union merge the root lists of two Fibonacci heaps creating a new heap (and destroying the original heaps)
- **consolidation** the process of linking individual subheaps having the same degree into a subheap with one degree larger the ultimate goal of consolidation is a root list with no two heaps having the same degree consolidation works via the *degree array*
- linking joining two subheaps together by making one of the subheaps a child of the other the heap with the larger valued root (for a min heap) becomes the child
- degree array an array with size on the order of the log of the number of nodes in the Fibonacci heap. The array slot with index 0 is a place to hold a subheap of degree zero. The slot with index 1 is a place of hold a subheap of degree one, and so on it is used by the consolidation operation to keep track of which subheaps have which degree

Note that the term *rootify* is not found in other Fibonacci heap descriptions.

## Fibonacci heap operations

A Fibonacci heap has the following properties:

operation	time bound (amortized)
insert	constant
$\operatorname{findMin}$	constant
extractMin	$\log$
union	constant
decreaseKey	constant
delete	$\log$

Next: Inserting into a Fibonacci heap