

CPRE 281: HW 02 Dr. Smith

1) a. & (ampersand)

b. |

c. ^

d. ~

2) • structural Verilog - by specifying the module's internal structure.

- specifies how components are interconnected.

- behavioral Verilog - by describing its behavior in a program-like manner.

- specifies how a particular design should respond to a given set of inputs.

The largest difference is how structural uses set components while behavioral uses assign to describe the behavior of the module.

3)

- structural:

```
module problem3(x1, x2, x3, f);
```

```
    input x1, x2, x3;
```

```
    output f;
```

```
    wire k, g, h;
```

```
    not(k, x3);
```

```
    or(h, x2, k);
```

```
    or(g, x1, x2);
```

```
    and(f, g, h);
```

```
endmodule;
```


• behavioral:

```
module problem3(x1,x2,x3,f);
```

```
input x1,x2,x3;
```

```
output f;
```

```
assign f = (~x3 | x2) & (x1 | x2);
```

```
endmodule
```

4)

• structural:

```
module problem4(a,b,c,f);
```

```
input a,b,c,f;
```

```
output f;
```

```
not(l,a);
```

```
not(m,c);
```

```
and(g,l,b,c);
```

```
and(h,l,b,m);
```

```
and(k,a,c);
```

```
or(f,g,h,k);
```

```
endmodule
```

• behavioral:

```
module problem3(a,b,c,f);
```

```
input a,b,c;
```

```
output f;
```

```
assign f = (~a & b & c) | (~a & b & ~c)
```

```
| (a & c);
```

```
endmodule
```

5) a) $\bar{A} + A = 1$

b) $\bar{A}B + A\bar{B} = \bar{A}B + A\bar{B}$

c) $\bar{A}\bar{B}\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C$

$= \bar{A}\bar{B}\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C$

d) $\bar{A}\bar{B}\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C + A\bar{B}C$

$= 7$

$$\begin{aligned}
 & \overline{A}BC + \overline{A}BC + A\overline{B}C + A\overline{B}C + A\overline{B}C \\
 \Rightarrow & \overline{A}C(\overline{B}+B) + A\overline{C}(\overline{B}+B) + A\overline{B}C \\
 \Rightarrow & \overline{A}C + A\overline{C} + A\overline{B}C \\
 \Rightarrow & \overline{A}C + C(\overline{A} + A \cdot \overline{B}) \quad \text{--- } x + x \cdot y = x + y
 \end{aligned}$$

$$d) \Rightarrow (\overline{A}C) + (C\overline{A}) + (C\overline{B})$$

$$\begin{aligned}
 e) & \overline{A}\overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}\overline{C}D + \overline{A}\overline{B}C\overline{D} + \overline{A}\overline{B}CD + \overline{A}B\overline{C}\overline{D} \\
 & + \overline{A}B\overline{C}D + \overline{A}BC\overline{D} + \overline{A}BCD + A\overline{B}\overline{C}\overline{D} + A\overline{B}\overline{C}D + A\overline{B}C\overline{D} + A\overline{B}CD \\
 & + AB\overline{C}\overline{D} + AB\overline{C}D + ABC\overline{D} + ABCD
 \end{aligned}$$

$$\begin{aligned}
 \Rightarrow & \overline{A}\overline{B}\overline{C}(\overline{D}+D) + \overline{B}\overline{C}\overline{D}(\overline{A}+A) + \overline{A}\overline{B}C(\overline{D}+D) \\
 & + \overline{A}B\overline{C}\overline{D} + \overline{A}\overline{B}C(\overline{D}+D) + \overline{A}BC(\overline{D}+D)
 \end{aligned}$$

$$\Rightarrow \overline{A}\overline{B}\overline{C} + \overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}C + \overline{A}BC\overline{D} + \overline{A}\overline{B}C + \overline{A}BC$$

$$\Rightarrow \overline{A}C(\overline{B}+B) + C\overline{D}(\overline{B}+A \cdot B) + \overline{A}C(\overline{B}+B)$$

$$\Rightarrow \overline{A}C + \overline{A}C + C\overline{D}(\overline{B}+B \cdot A)$$

$$\Rightarrow C\overline{D}(\overline{B}+B \cdot A) \quad \begin{matrix} B \cdot \overline{B} + A = BA \\ x + x \cdot y = x + y \end{matrix}$$

$$\Rightarrow \overline{C}A + \overline{C}\overline{A} + C\overline{D}(\overline{B}+A) \quad \begin{matrix} x \cdot y + x \cdot \overline{y} = x \end{matrix}$$

$$\Rightarrow \overline{C} + C\overline{D}(\overline{B}+A)$$

$$\Rightarrow (\overline{C} + C\overline{D})(\overline{B}+A) \quad \begin{matrix} x + xy = x + y \end{matrix}$$

$$\Rightarrow \overline{C} + \overline{D}(\overline{B}+A) \Rightarrow \overline{C} + \overline{D}\overline{B} + \overline{D}A$$

6)

A	B	C	D	f
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$$\Rightarrow \overline{A}BCD + A\overline{B}CD + AB\overline{C}D + ABC\overline{D} + ABCD$$

$$\Rightarrow BCD(\overline{A}+A) + A\overline{B}CD + AB\overline{C}D + ABC\overline{D}$$

$$\Rightarrow BCD + A\overline{B}CD + AB\overline{C}D + ABC\overline{D}$$

$$\Rightarrow CD(B + \overline{B} \cdot A) + A\overline{B}CD + ABC\overline{D}$$

$$\Rightarrow CD(B+A) + A\overline{B}CD + ABC\overline{D}$$

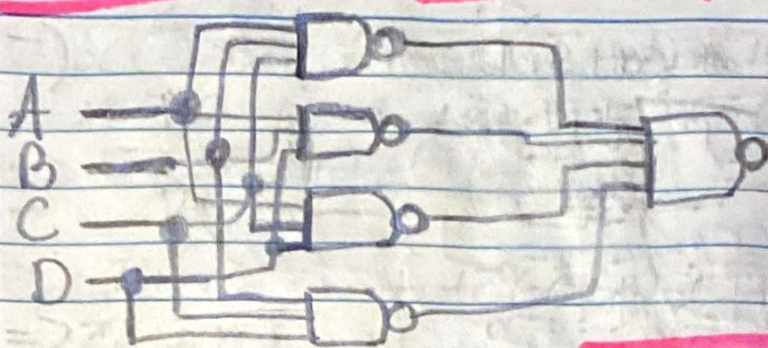
$$\Rightarrow BCD + ACD + A\overline{B}CD + ABC\overline{D}$$

$$\Rightarrow BD(C + \overline{C} \cdot A) + AC(D + \overline{D} \cdot B)$$

$$\Rightarrow BD(C+A) + AC(D+B)$$

$$\Rightarrow BCD + ABD + ACD + ABC$$

$$\Rightarrow ABC + ABD + ACD + BCD$$



7)

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

$$f(A, B, C, D) = \sum m(3, 5, 6, 7, 9, 10, 11, 12, 13, 14)$$

$$\Rightarrow \bar{A}\bar{B}CD + \bar{A}B\bar{C}D + \bar{A}BC\bar{D} + \bar{A}BCD + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD + A\bar{B}C\bar{D}$$

$$+ A\bar{B}CD + A\bar{B}C\bar{D}$$

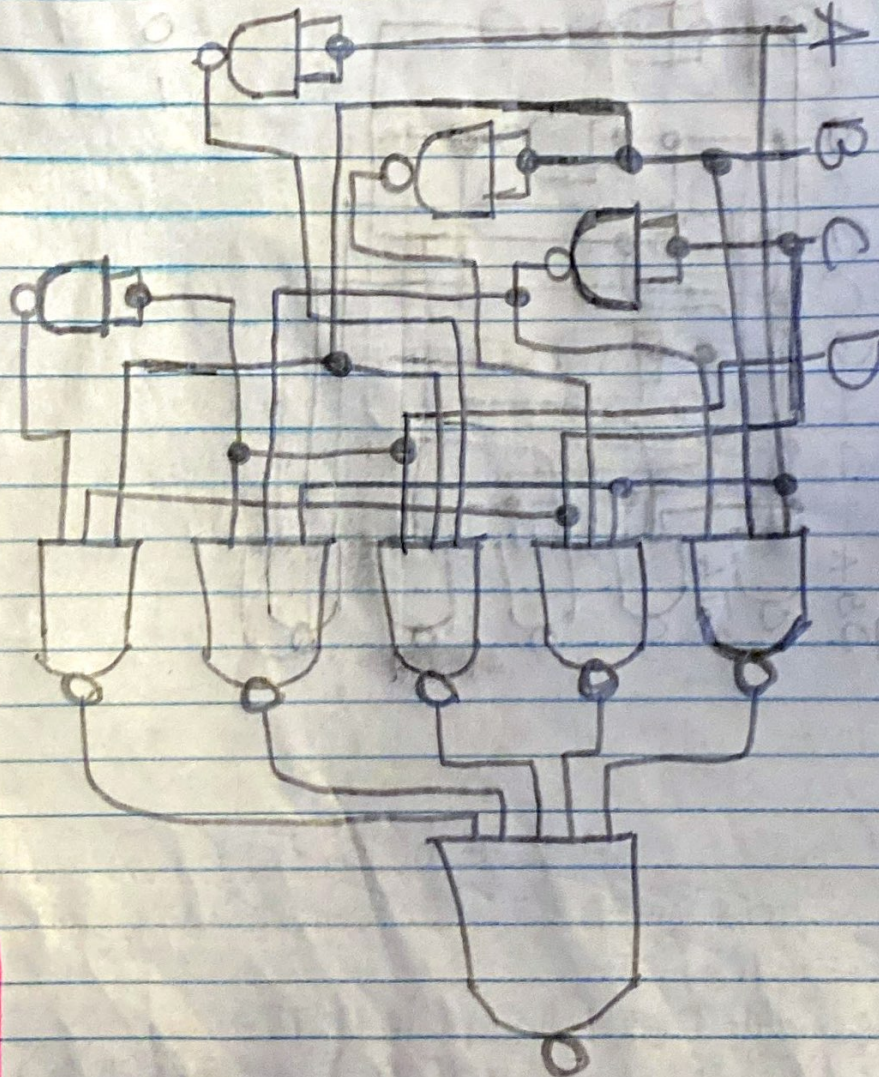
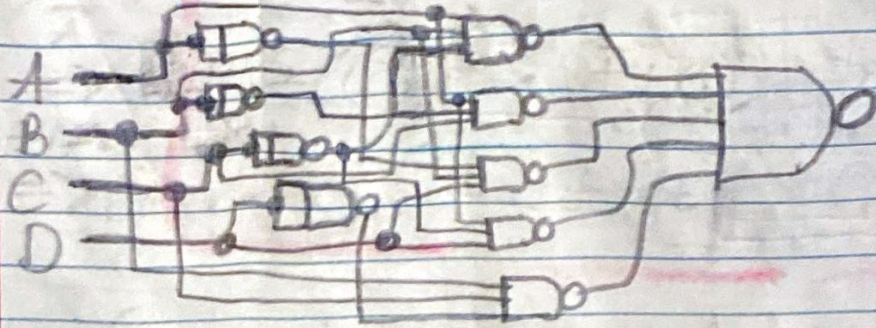
$$\circ 13, 12 + 7, 5 + 13, 9 + 11, 10 + 6, 14$$

$$\Rightarrow \bar{A}\bar{B}C(\bar{D}+D) + \bar{A}B\bar{C}(D+\bar{C}) + A\bar{B}C(D+\bar{B}) + A\bar{B}C(\bar{D}+D)$$

$$+ \bar{B}CD(\bar{A}+A)$$

$$\Rightarrow \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}C + \bar{B}CD$$

$$\Rightarrow ABC\bar{C} + \bar{A}BC + \bar{A}BD + A\bar{C}D + BCD$$



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