

CPRE 261: HW 02 Dr. Frank

1) a. & (AND)

b. |

c. ^

d. ~

2) • structural Verilog - by specifying the module's internal structure.

- specifies how components are interconnected.

- behavioral Verilog - by describing its behavior in a program-like manner.

- specifies how a particular design should respond to a given set of inputs.

3) The largest difference is how structural uses set components while behavioral uses assign to describe the behavior of the module.

3) structural:

```
module problem3(x1, x2, x3, f);
```

```
    input x1, x2, x3;
```

```
    output f;
```

```
    wire k, g, h;
```

```
    not(k, x3);
```

```
    or(g, x2, k);
```

```
    or(f, g, h);
```

```
endmodule;
```

• behavioral:

module problem3(x_1, x_2, x_3, f);

input x_1, x_2, x_3 ;

output f ;

assign $f = (\sim x_3 \mid x_2) \& (x_1 \mid x_2)$;

endmodule

4)

• structural:

module problem4(t, B, C, f);

input t, B, C, f ;

output f ;

not(l, t);

not(m, C);

and(g, l, B, C);

and(h, l, B, m);

and(k, t, C);

or(t, g, h, k);

endmodule

• behavioral:

module problem3(t, B, C, f);

input t, B, C ;

output f ;

assign $f = (\sim t \& B \& C) \mid (\sim t \& B \& \sim C)$

$\mid (t \& C)$;

endmodule

5) a) $\bar{A} + A \Rightarrow 1$

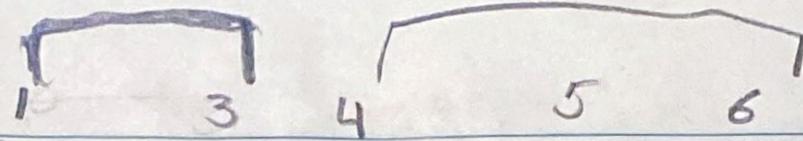
b) $\bar{A}B + A\bar{B} \Rightarrow \bar{A}B + AB$

c) $\bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}C + ABC$

$\Rightarrow \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}C + ABC$

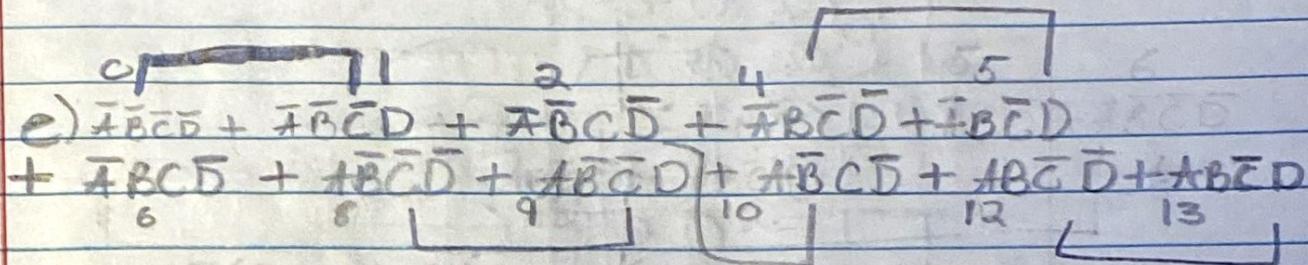
d) $\bar{A}\bar{B}C + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C + ABC$

\Rightarrow



$$\begin{aligned}
 & \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}\bar{B}\bar{C} + A\bar{B}C + A\bar{B}\bar{C} \\
 \Rightarrow & \bar{A}C(\bar{B}+B) + \bar{A}\bar{C}(\bar{B}+B) + A\bar{B}C \\
 \Rightarrow & \bar{A}C + \bar{A}\bar{C} + A\bar{B}C \\
 \Rightarrow & \bar{A}\bar{C} + C(\bar{A} + \bar{A} \cdot \bar{B}) \\
 & \quad \times \quad \times \quad \therefore \quad = \bar{A} + \bar{B}
 \end{aligned}$$

(d) $\Rightarrow (\bar{A}\bar{C}) + (\bar{A}\bar{C}) + (\bar{C}\bar{B})$



$$\begin{aligned}
 & \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} \\
 & + \bar{A}B\bar{C}D + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D \\
 \Rightarrow & \bar{A}\bar{B}\bar{C}(\bar{D}+D) + \bar{B}C\bar{D}(\bar{A}+A) + \bar{A}\bar{B}\bar{C}(\bar{D}+D) \\
 & + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}(\bar{D}+D) + \bar{A}\bar{B}\bar{C}(\bar{D}+D) \\
 \Rightarrow & \bar{A}\bar{B}\bar{C} + \bar{B}C\bar{D} + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}\bar{C}
 \end{aligned}$$

$$\Rightarrow \bar{A}\bar{C}(\bar{B}+B) + \bar{C}\bar{D}(\bar{B}+A \cdot B) + \bar{A}\bar{C}(\bar{B}+B)$$

$$\Rightarrow \bar{A}\bar{C} + \bar{A}\bar{C} + \bar{C}\bar{D}(\bar{B}+B \cdot \bar{A})$$

$$\Rightarrow \bar{C}\bar{D}(\bar{B}+B \cdot \bar{A}) \quad B \cdot \bar{B} + \bar{A} = \bar{B}A \\
 \quad \times \quad \times \quad \therefore \quad = x+y$$

$$\Rightarrow \bar{C}\bar{A} + \bar{C}\bar{A} + \bar{C}\bar{D}(\bar{B}+\bar{A})$$

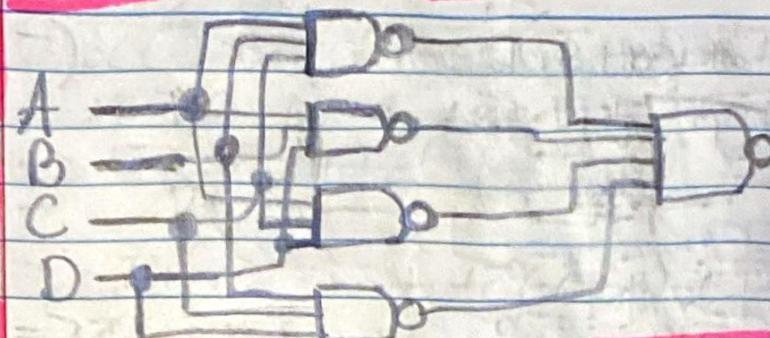
$$\Rightarrow \bar{C} + \bar{C}\bar{D}(\bar{B}+\bar{A})$$

$$\Rightarrow (\bar{C} + \bar{C}\bar{D})(\bar{B}+\bar{A}) \quad \times \quad \times \quad \therefore \quad = x+y$$

$$\Rightarrow \bar{C} + \bar{D}(\bar{B}+\bar{A}) \Rightarrow \bar{C} + \bar{D}\bar{B} + \bar{D}\bar{A}$$

6)	A	B	C	D	T
	0	0	0	0	0
	0	0	0	1	0
	0	0	1	0	0
	0	0	1	1	0
	0	1	0	0	0
	0	1	0	1	0
	0	1	1	0	0
	0	1	1	1	1
	1	0	0	0	0
	1	0	0	1	0
	1	0	1	0	0
	1	0	1	1	1
	1	1	0	0	0
	1	1	0	1	1
	1	1	1	0	1
	1	1	1	1	1

$$\begin{aligned}
 \Rightarrow & \bar{A}BCD + A\bar{B}CD + AB\bar{C}D \\
 & + ABC\bar{D} + A\bar{B}C\bar{D} \\
 \Rightarrow & BCD(\bar{A} + A) + A\bar{B}CD + AB\bar{C}D + \underline{ABC\bar{D}} \\
 \Rightarrow & BCD + A\bar{B}CD + A\bar{B}C\bar{D} + ABC\bar{D} \\
 \Rightarrow & CD(B + \bar{B} \cdot A) + A\bar{B}CD + ABC\bar{D} \\
 \Rightarrow & CD(B + A) + A\bar{B}CD + ABC\bar{D} \\
 \Rightarrow & \underline{BCD + ACD} + \underline{A\bar{B}CD} + \underline{ABC\bar{D}} \\
 \Rightarrow & BD(C + \bar{C} \cdot A) + AC(D + \bar{D} \cdot B) \\
 \Rightarrow & BD(C + A) + AC(D + B) \\
 \Rightarrow & BCD + ABD + ACD + ABC \\
 \Rightarrow & ABC + ABD + ACD + BCD
 \end{aligned}$$



A	B	C	D	f
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

$$f(A, B, C, D) = \sum m(3, 5, 6, 7, 9, 10, 11, 12, 13, 14)$$

$$\Rightarrow \bar{A}\bar{B}CD + A\bar{B}CD + \bar{A}B\bar{C}D + \bar{A}BCD + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}CD + A\bar{B}CD + \bar{A}\bar{B}\bar{C}\bar{D}$$
 ~~$\bar{A}\bar{B}\bar{C}D + \bar{A}B\bar{C}\bar{D}$~~

$$\circ 13, 12 + 7, 5 + 13, 9 + 11, 10 + 6, 14$$

$$\Rightarrow \bar{A}\bar{B}(\bar{D} + D) + \bar{A}D(\bar{C} + C) + A\bar{C}D(\bar{B} + B) + A\bar{B}C(\bar{D} + D) + BCD(\bar{A} + A)$$

$$\Rightarrow A\bar{B} + \bar{A}BD + A\bar{C}D + A\bar{B}C + BCD$$

$$\begin{array}{ccccccc}
 & \times & \times & + & \times & + \\
 \Rightarrow A\bar{B}\bar{C} + A\bar{B}C + \bar{A}BD + \bar{A}\bar{C}D + BCD
 \end{array}$$

