

Don Mill

2/16/22 Bonus Activity

1) a) $B + \overline{A}B = A \Rightarrow \overline{A} + B = A$ (T)

b) (T)

c) (F)

d) (F)

e) (F)

f) (T)

g) (T)

h) (F)

i) (F)

j) (F)

$\overline{A} \cdot B$

$A - 0 \quad 0 - 0 \quad B + A = A + B$

$B - 0 \quad \overline{A} \cdot B = \overline{A} + B$

$A - 0$

$B - 0$

$(2 \cdot 3 + 2 \cdot 1) + 6 - 13$

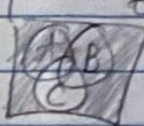
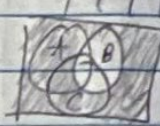
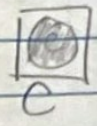
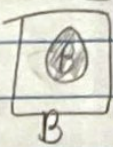
$8 + 8 = 16 - 13 = 3$

	00	01	11	01
0	0	0	0	0
1	0	0	1	0

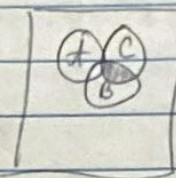
$\Rightarrow C \cdot b \cdot a + b$

32168421
 $111111 = 63$

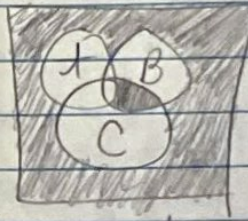
2)



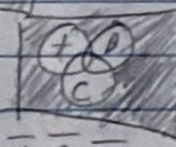
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=>



=>



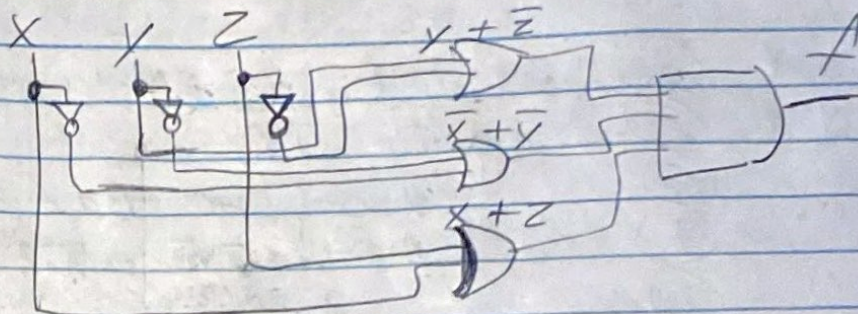
3)

	x	y	z	$x \oplus y$	$x \oplus z$	
0	0	0	0	0	0	0
1	0	0	1	0	1	1
2	0	1	0	1	0	2
3	0	1	1	1	1	3
4	1	0	0	1	1	4
5	1	0	1	1	0	5
6	1	1	0	0	1	6
7	1	1	1	0	0	7

$\Rightarrow y + \overline{z} \cdot \overline{x} + \overline{y} \cdot x + z$

$$Y + \bar{Z} \cdot \bar{X} + \bar{Y} \cdot X + Z$$

c)



4) a) $2 \cdot 6^2 + 5 \cdot 6^1 + 2 \cdot 6^0$
 $\Rightarrow 72 + 30 + 2 = 104$

Q	R
104	0
52	0
26	0
13	1
6	0
3	1
1	1
0	

$$\Rightarrow 96 + 8 = 104$$

$$\Rightarrow \begin{matrix} 64 & 32 & 16 & 8 & 4 & 2 & 1 \\ 1 & 1 & 0 & 1 & 0 & 0 & 0 \end{matrix}$$

\Rightarrow

$$640 + 32 + 12 = 684$$

$$\begin{matrix} 512 & 256 & 128 & 64 & 32 & 16 & 8 & 4 & 2 & 1 \end{matrix}$$

$$\Rightarrow \begin{matrix} 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 \end{matrix}$$

b)

Q	R
684	0
342	0
171	1
85	1
42	0
21	1
10	0
5	1
2	0
1	1
0	

$$16 \cdot 16 = 256 \cdot 16 \quad \begin{array}{r} 2560 \\ + 1536 \\ \hline 4096 \end{array} \Rightarrow 4096 \cdot 10 = 40,960$$

c) 3210
AADF

$$10 \cdot 16^3 + 10 \cdot 16^2 + 13 \cdot 16 + 15$$

$$40,960 + 2560 + 208 + 15 \Rightarrow$$

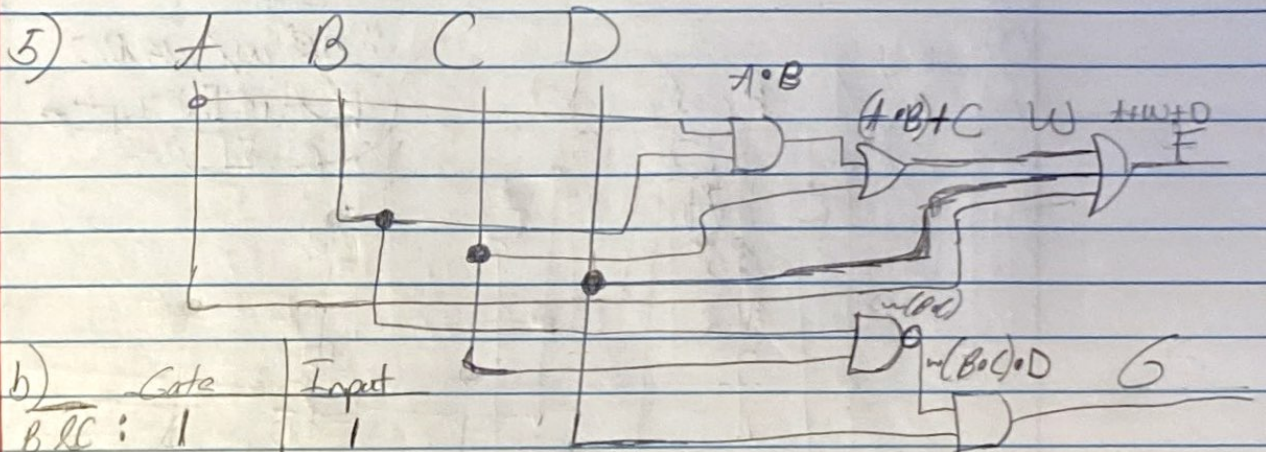
$$\begin{array}{r} 40960 \\ + 2560 \\ + 223 \\ \hline 43743 \end{array}$$

I did all this w/out calculator, but getting this into octal w/out a calculator would be horrible

Q	R
43743	7
5467	3
683	3
85	5
10	2
1	1

$\Rightarrow 1253378$

d) 256128012166421
100011001 $\Rightarrow 256 + 16 + 8 + 1$
 $= 281$



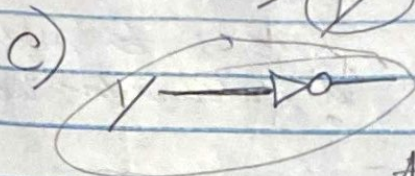
b)

Gate	Input
B.C.C	1
A.B	2
(A.B)+C	3
F	3
B.C	2
B.C.D	2

$$= 6 + 13 = 19$$

6) a) $f(x,y) = x\bar{y} \cdot \bar{y} \cdot \bar{x} + y$

b) $\Rightarrow x \cdot (\bar{y} \cdot \bar{y}) \cdot \bar{x} + y$
 $\Rightarrow x \cdot \bar{y} \cdot \bar{x} + y$
 $\Rightarrow x \cdot \bar{x} \cdot \bar{y} + y$
 $\Rightarrow \bar{y} + y$
 $\Rightarrow 1$

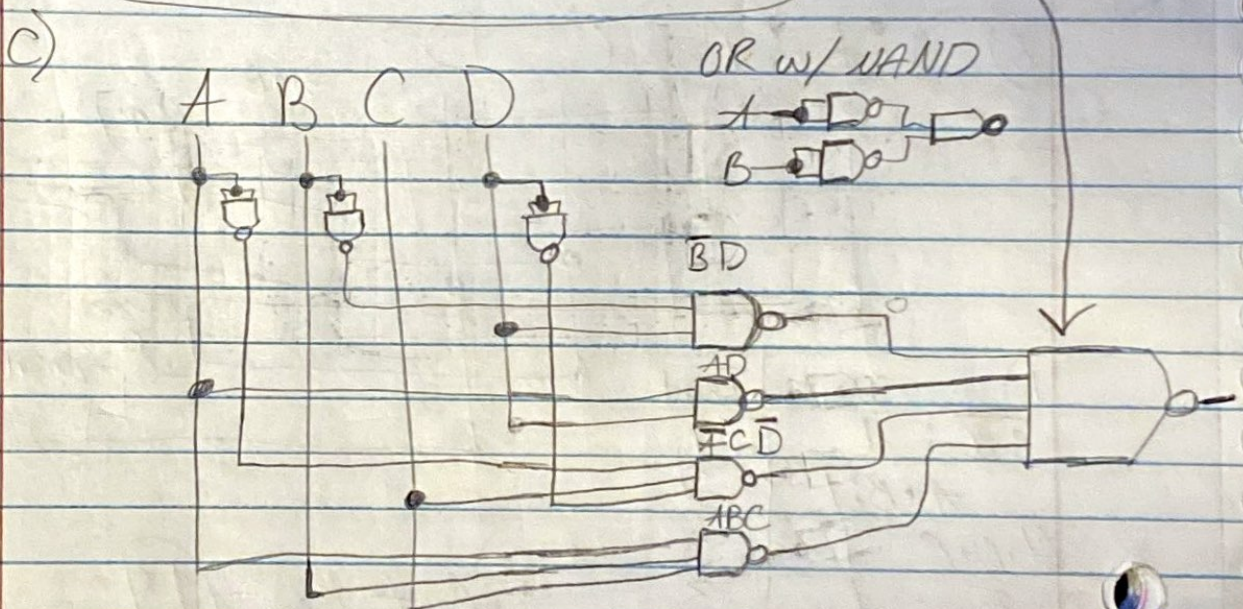


7) a)

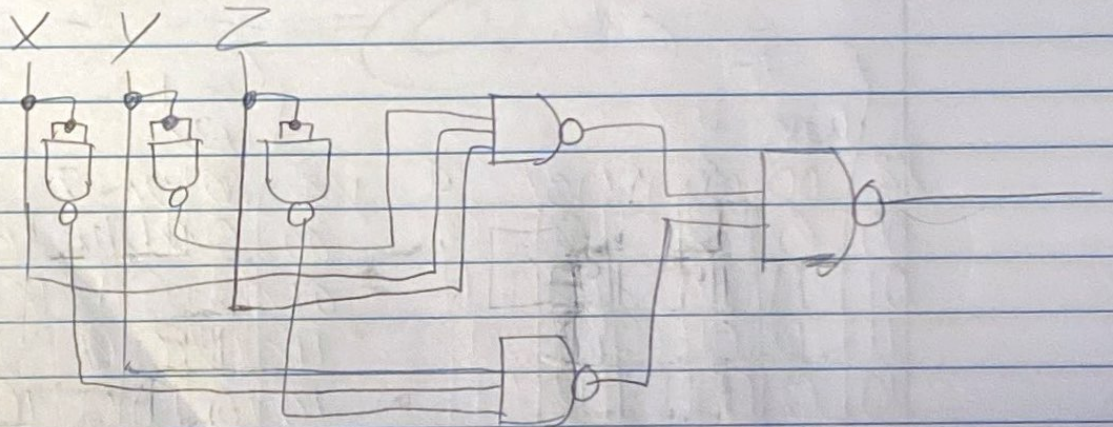
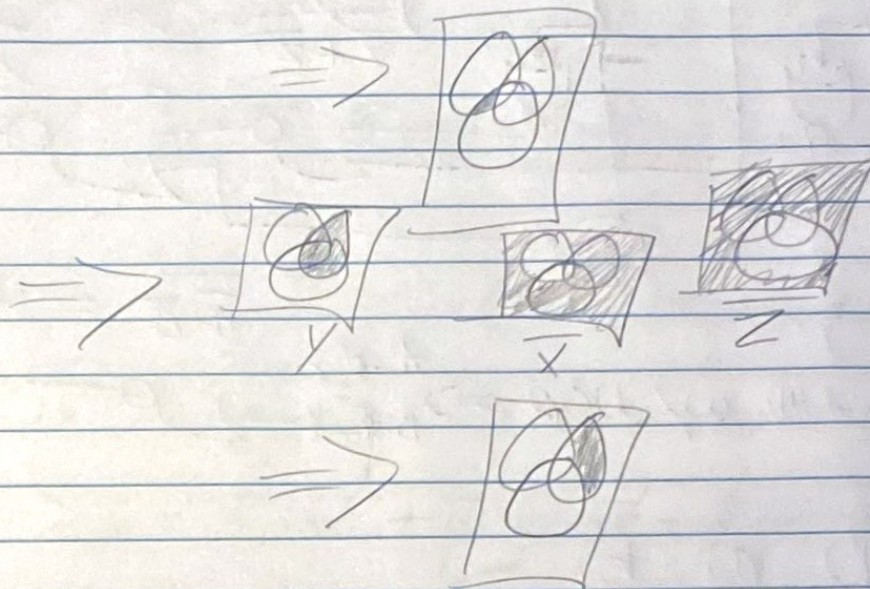
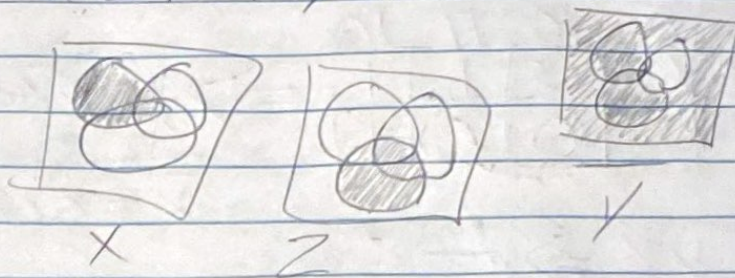
AB \ CD	00	01	11	10
00	0	0	0	0
01	1	0	1	1
11	1	0	1	1
10	1	1	1	0

ABD $\bar{A}\bar{C}\bar{D}$ $\bar{A}\bar{B}\bar{D}$ $\bar{A}\bar{B}\bar{D}$ $\bar{B}\bar{C}\bar{D}$
 1 1 1 0 1 0 0 0 1 1 0 1 1 1 0

b) $\Rightarrow \bar{B}D + AD + \bar{A}\bar{C}\bar{D} + ABC$



8) a) $X \cdot Z \cdot \bar{Y} + Y \cdot \bar{X} \cdot \bar{Z}$

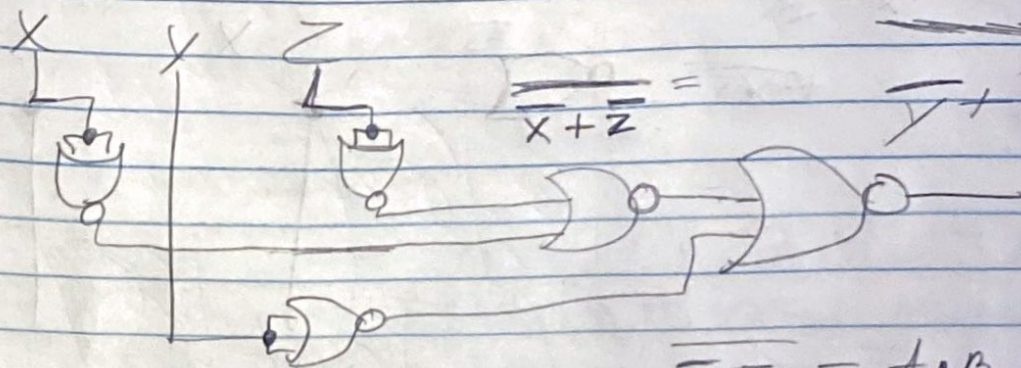


b)

	xy				
z	00	01	11	10	
0	0	0	1	1	
1	0	0	0	1	

$$\Rightarrow y \cdot \bar{x} \bar{z}$$

$$\overline{y + x \cdot z} \Rightarrow \overline{y} \cdot \overline{x + z}$$



$$\overline{A+B} = A \cdot B$$

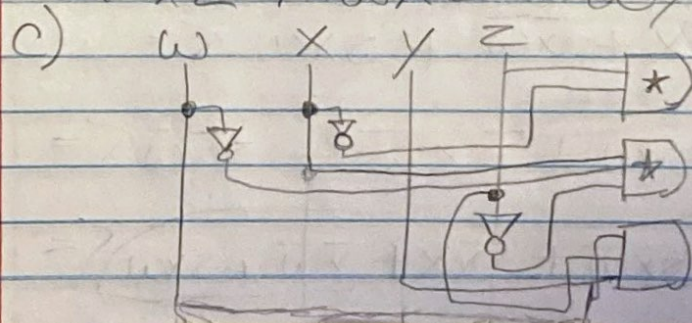
AND w/ NOR \Rightarrow

g) a) b)

F	wx				
z	00	01	11	10	
00	0	1	0	0	
01	1	d	0	1	
11	1	0	0	d	
10	0	d	0	1	

G	wx				
yz	00	01	11	10	
00	0	1	d	d	
01	d	0	0	1	
11	1	0	1	1	
10	0	1	d	0	

$$\Rightarrow \bar{x}z + \bar{w}x\bar{z} + w y z$$



$$10) \overline{xy}(\overline{z} + (z(\overline{w} + w)) + (\overline{y+z}) \cdot (\overline{y+yz}) \cdot (\overline{wx}) \\ + wxy + yxz \cdot (\overline{z+z\overline{y}}) \quad x \quad y$$

$$\Rightarrow \overline{x} + \overline{y}(\overline{z} + (z(\overline{w} + w))) + (\overline{y} \cdot \overline{z}) + (\overline{y} \cdot \overline{yz}) + (\overline{w} + \overline{x}) \\ + wxy + yxz \cdot (\overline{z} \cdot \overline{zy})$$

$$\Rightarrow \overline{x} + \overline{y} + (\overline{y} \cdot \overline{z}) + (\overline{y} \cdot \overline{yz}) + (\overline{w} + \overline{x}) + wxy + yxz \cdot y$$

$$\Rightarrow \overline{x} + \overline{y} + \overline{yz} + (\overline{y} \cdot \overline{y} + \overline{z}) + (\overline{w} + \overline{x}) + wxy + yxz \cdot y$$

$$\Rightarrow \overline{x} + \overline{y} + (\overline{y} \cdot \overline{z} + \overline{z}) + (\overline{w} + \overline{x}) + wxy + yxz \cdot y$$

$$\Rightarrow \overline{x} + \overline{y} + \overline{z} + \overline{w} + \overline{x} + wxy + yxz \cdot y$$

$$\Rightarrow \overline{y} + \overline{x} + \overline{w} + \overline{x} + wxy + yxz \cdot y$$

$$\Rightarrow \overline{y} \cdot y = 0$$