

Implementation of a Self-Organizing Map

Damien DELPY

ENSEIRB-MATMECA

November 1, 2023

Overview

Algorithm

Bibliography

OVERVIEW

What is a SOM ?

Definition

It is a neural network of just one layer : the output layer.

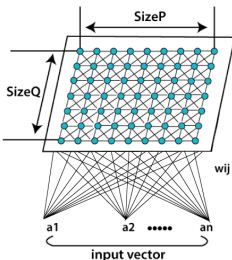


Figure: SOM Architecture (see 2 of Bibliography).

Wikipedia

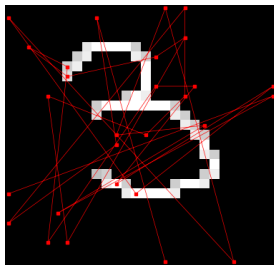
A self-organizing map (SOM) is used to produce a low-dimensional (typically two-dimensional) representation of a higher dimensional data set, while preserving the topological structure of the data.

Motivation

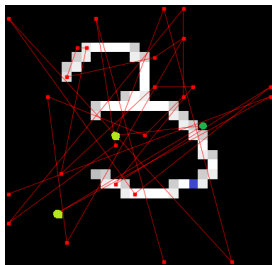
The Self-Organizing Maps permit to :

- ▶ Analyse and visualise the data. It represents complex data on a map of only two or three dimensions (see Convergence slide).
- ▶ Detect patterns from the data. Clustering (see K-means slide).
- ▶ Improve a deep neuronal network by sorting the data at the beginning.

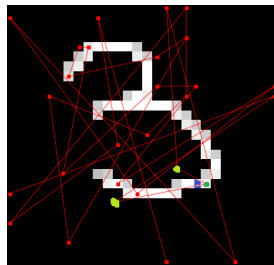
Example



Step 1



Step 2



Step 3

1. Initialize the weight vectors (randomly or not) in red.
2. **Competition** : Select a data vector(blue), then chose the closest weight vector(green) to it.
3. **Adaptation** : Update the winner and its neighbors (all green ones).
4. repeat the process till reach max_iteration

Similarities with the Perceptron

Perceptron

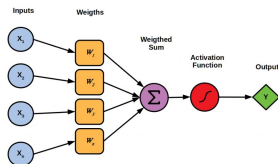


Figure: Diagram of a Perceptron.

It is also a one-layer neuronal network. However, this one is used to separate two different classes. The output is actually a binary one.

This is a supervised learning algorithm.

SOM

The SOM can gather vectors due to their similarities.

The SOM is an **unsupervised learning algorithm**.

Similarities with K-means algorithm

K-means algorithm is an unsupervised learning technique that can automatically gather data by creating **clusters**, which are subsets of data elements that share common characteristics.

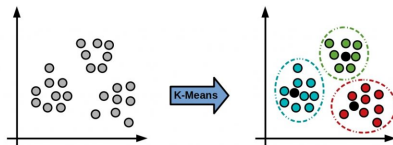


Figure: Process of K-means algorithm

The user must define the number of clusters **K**. However, The SOM does not require this, it guesses the right amount of clusters.

Convergence

The convergence of the SOM algorithm is not guaranteed (1). There are actually 2 errors that can appear.



Figure: Dimension Error.

It happens when the number of neurons does not fit with the data.

The ideal number of neurons is $5\sqrt{N}$ where N is the number of data vectors.

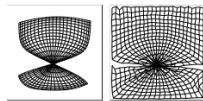


Figure: Topological Error.

It happens when a node is created. It looks like a butterfly.

ALGORITHM

Cooperation

To prevent from discontinuous adaptation by only modifying the winner neuron, all of its neighbors are also modified.

The number of neighbors depends on the topology.

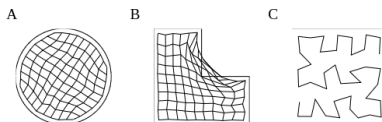


Figure: Different topologies possible. A : circular topology; B : rectangular topology; C : linear topology

Here, the grid is the neural network.

Each node of the grid is a neuron.

On the linear topology, each neuron has a maximum number of 2 neighbors.

On the rectangular topology, each neuron has a maximum number of 8 neighbors.

Adaptation

Here is the update of the weight vectors of the winner neuron and its neighbors.

it is at the instant t :

$$w_k(t+1) = w_k(t) + \alpha \cdot h_{kj}(t) \cdot (X_j - w_k(t))$$

- ▶ X_j is the input vector
- ▶ $w_k(t)$ is the weight vector of the neuron k at the instant t
- ▶ α is the **learning rate**
- ▶ h_{kj} is the **neighborhood** function which smooths the update of the neighbors depending on their proximity with the winner and the iteration t . (see 1 of Bibliography)

We can chose the **Gaussian** function :

$$h_{jk} = \exp\left(\frac{-\|w_{winner} - w_k\|^2}{2\sigma^2}\right)$$

σ is the standard deviation of the Gaussian function (2). It could a function which decreases with t .

Algorithm

BIBLIOGRAPHY

1. Self-Organizing Maps - Teuvo Kohonen (2001)
2. <https://www.baeldung.com/cs/som-algorithm>
3. http://www.pspc.unige.it/~drivsc/Papers/VanHulle_Springer.pdf