## Implementation of a Self-Organizing Map

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# **OVERVIEW**

### What is a SOM?

#### Definition

It is a neural network of just one layer: the output layer.

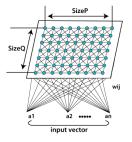


Figure: SOM Architecture (see 2 of Bibliography).

#### Wikipedia

A self-organizing map (SOM) is used to produce a low-dimensional (typically two-dimensional) representation of a higher dimensional data set, while preserving the topological structure of the data.

#### Motivation

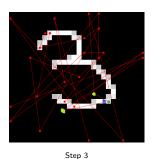
#### The Self-Organizing Maps permit to :

- Analyse and visualise the data. It represents complex data on a map of only two or three dimensions (see Convergence slide).
- Detect patterns from the data. Clustering (see K-means slide).
- Improve a deep neuronal network by sorting the data at the beginning.

### Example







- Step 1
- 1 Step 2
- Initialize the weight vectors (randomly or not) in red.
- $2. \quad \textbf{Competition}: \ \mathsf{Select} \ \mathsf{a} \ \mathsf{data} \ \mathsf{vector}(\mathsf{blue}), \ \mathsf{then} \ \mathsf{chose} \ \mathsf{the} \ \mathsf{closest} \ \mathsf{weight} \ \mathsf{vector}(\mathsf{green}) \ \mathsf{to} \ \mathsf{it}.$
- 3. Adaptation: Update the winner and its neighbors (all green ones).
- 4. repeat the process till reach max\_iteration

### Similarities with the Perceptron

### Perceptron

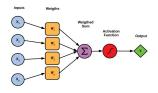


Figure: Diagram of a Perceptron.

It is also a one-layer neuronal network. However, this one is used to separate two different classes. The output is actually a binary one.

This is a supervised learning algorithm.

#### **SOM**

The SOM can gather vectors due to their similarities.

The SOM is an unsupervised learning algorithm.



### Similarities with K-means algorithm

K-means algorithm is an unsupervised learning technique that can automatically gather data by creating clusters, which are subsets of data elements that share common characteristics.

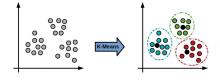


Figure: Process of K-means algorithm

The user must define the number of clusters K. However, The SOM does not require this, it guesses the right amount of clusters.

## Convergence

The convergence of the SOM algorithm is not guaranteed (1). There are actually 2 errors that can appear.



Figure: Dimension Error.

It happens when the number of neurons does not fit with the data.

The ideal number of neurons is  $5\sqrt{N}$  where N is the number of data vectors.

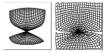


Figure: Topological Error.
It happens when a node is created

It happens when a node is created. It looks like a butterfly.

## **ALGORITHM**

#### Different Phases

#### Initialisation

The weights  $m_i$  or  $w_i$  of neuron connections are randomly initialized.

### Competition

Chose randomly an input vector  $X_j$ .

Search for the neuron with the closest weight vector from  $X_i$ .

To realise it, a distance is needed.

All distances can work, let is choose the Euclidean distance.

The identity of the winner neuron is :

$$k = \arg_i \min \|X_i - w_i\|$$

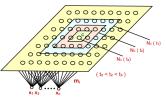
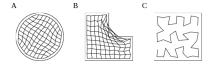


Figure 1. The structure of SOM Network

### Cooperation

To prevent from discontinous adaptation by only modifying the winner neuron, all of its neighbors are also modified.

The number of neighbors depends on the topology.



 $\label{eq:Figure:Different topologies possible. A: circular topology; B: rectangular topology; C: linear topology$ 

Here, the grid is the neural network.

Each node of the grid is a neuron.

On the linear topology, each neuron has a maximum number of 2 neighbors.

On the rectangular topology, each neuron has a maximum number of 8 neighbors.

### Adaptation

Here is the update of the weight vectors of the winner neuron and its neighbors.

it is at the instant t:

$$w_k(t + 1) = w_k(t) + \alpha . h_{kj}(t) . (X_j - w_k(t))$$

- X<sub>j</sub> is the input vector
- w<sub>k</sub>(t) is the weight vector of the neuron k at the instant t
- $\triangleright$   $\alpha$  is the learning rate
- h<sub>kj</sub> is the neighborhood function which smooths the update of the neighbors depending on their proximity
  with the winner and the iteration t. (see 1 of Bibliography)

We can chose the Gaussian function :

$$h_{jk} = \exp(\frac{-\|w_{winner} - w_k\|^2}{2\sigma^2})$$

 $\sigma$  is the standard deviation of the Gaussian function (2). It could be a function which decreases with t.

### Algorithm

#### Algorithm 1 Self-Organizing Map Algorithm

Require: input data X; maximum number of iterations IMAX; the neighborhood function h; lattice dimensions kxl

Ensure: the weight vectors W

1: Randomly initialize weight vectors  $w_i$ 

2: for  $t \leftarrow 1$  to IMAX do

3:

4: for sample in X do

5: competition

6: Find the neuron closest to the sample

cooperation and adaptation

7: Find this neuron and its neighbors

8: end for

9: end for

10: return W



# **BIBLIOGRAPHY**

- 1. Self-Organizing Maps Teuvo Kohonen (2001)
- 2. https://www.baeldung.com/cs/som-algorithm
- 3. http://www.pspc.unige.it/ drivsco/Papers/VanHulle\_Springer.pdf