

Flipping a bitboard **vertical** reverses all eight bytes - it performs a little- big-endian conversion or vice versa. A scalar square may be flipped vertically by xor 56.

❗ **✖** It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (<http://blog.wikispaces.com>)

```
sq' = sq ^ 56;
```

The obvious approach with 21 operations, note that the shifts by 56 don't need masks:

```
/**
 * Flip a bitboard vertically about the centre ranks.
 * Rank 1 is mapped to rank 8 and vice versa.
 * @param x any bitboard
 * @return bitboard x flipped vertically
 */
U64 flipVertical(U64 x) {
    return ( (x << 56) ) |
           ( (x << 40) & C64(0x00ff000000000000) ) |
           ( (x << 24) & C64(0x0000ff0000000000) ) |
           ( (x << 8) & C64(0x000000ff00000000) ) |
           ( (x >> 8) & C64(0x00000000ff000000) ) |
           ( (x >> 24) & C64(0x0000000000ff0000) ) |
           ( (x >> 40) & C64(0x000000000000ff00) ) |
           ( (x >> 56) );
}
```

The **parallel prefix**-approach takes 13 operations, to swap bytes, words and double-words in a **SWAR-wise** manner, performing three **delta swaps**:

```
/**
 * Flip a bitboard vertically about the centre ranks.
 * Rank 1 is mapped to rank 8 and vice versa.
 * @param x any bitboard
 * @return bitboard x flipped vertically
 */
U64 flipVertical(U64 x) {
    const U64 k1 = C64(0x00FF00FF00FF00FF);
    const U64 k2 = C64(0x0000FFFF0000FFFF);
    x = ((x >> 8) & k1) | ((x & k1) << 8);
    x = ((x >> 16) & k2) | ((x & k2) << 16);
    x = (x >> 32) | (x << 32);
    return x;
}
```

Using the **x86-64 _byteswap_uint64** or bswap64 intrinsics only takes one processor instruction in 64-bit mode.

```
/**
 * Flip a bitboard vertically about the centre ranks.
 * Rank 1 is mapped to rank 8 and vice versa.
 * @param x any bitboard
 * @return bitboard x flipped vertically
 */
U64 flipVertical(U64 x) {
    return _byteswap_uint64(x);
}
```

Horizontal

```
. 1 1 1|1 . . . . . 1 1 1 .
. 1 . . 1 . . . . 1 . . . 1 .
. 1 . . 1 . . . . 1 . . . 1 .
. 1 . . 1 . . . . 1 . . . 1 .
. 1 1 1 . . . . . 1 1 1 .
. 1 . 1 . . . . . 1 . 1 .
. 1 . . 1 . . . . 1 . . 1 .
. 1 . . 1 . . . . 1 . . 1 .
```

Horizontal mirroring reverses the bits of each byte. A scalar square may be mirrored horizontally by xor 7.

```
sq' = sq ^ 7;
```

The **parallel prefix**-algorithm swaps bits, bit-duos and **nibbles** in a **SWAR-wise** manner, performing three **delta swaps**, 15 operations:

```
/**
 * Mirror a bitboard horizontally about the center files.
 * File a is mapped to file h and vice versa.
 * @param x any bitboard
 * @return bitboard x mirrored horizontally
 */
U64 mirrorHorizontal (U64 x) {
    const U64 k1 = C64(0x5555555555555555);
    const U64 k2 = C64(0x3333333333333333);
    const U64 k4 = C64(0x0f0f0f0f0f0f0f0f);
    x = ((x >> 1) & k1) | ((x & k1) << 1);
    x = ((x >> 2) & k2) | ((x & k2) << 2);
    x = ((x >> 4) & k4) | ((x & k4) << 4);
    return x;
}
```

Replacing bitwise 'or' of disjoint sets by 'add' and shift left by appropriate multiply - taking advantage of x86 lea instruction for multiplication with 2 and 4:

```
/**
 * Mirror a bitboard horizontally about the center files.
 * File a is mapped to file h and vice versa.
 * @param x any bitboard
 * @return bitboard x mirrored horizontally
 */
U64 mirrorHorizontal (U64 x) {
    const U64 k1 = C64(0x5555555555555555);
    const U64 k2 = C64(0x3333333333333333);
    const U64 k4 = C64(0x0f0f0f0f0f0f0f0f);
    x = ((x >> 1) & k1) + 2*(x & k1);
    x = ((x >> 2) & k2) + 4*(x & k2);
    x = ((x >> 4) & k4) + 16*(x & k4);
}
```

❗ **x** It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (<http://blog.wikispaces.com>)

```

***
* Mirror a bitboard horizontally about the center files.
* File a is mapped to file h and vice versa.
* @param x any bitboard
* @return bitboard x mirrored horizontally
*/
U64 mirrorHorizontal (U64 x) {
    const U64 k1 = C64(0x5555555555555555);
    const U64 k2 = C64(0x3333333333333333);
    const U64 k4 = C64(0x0f0f0f0f0f0f0f0f);
    x ^= k4 & (x ^ rotateLeft(x, 8));
    x ^= k2 & (x ^ rotateLeft(x, 4));
    x ^= k1 & (x ^ rotateLeft(x, 2));
    return rotateRight(x, 7);
}

```

In [Knuth's *The Art of Computer Programming*](#) , Volume 4, Fascicle 1: Bitwise tricks & techniques, page 9, Knuth interprets the *magic masks* as 2-[adic](#) fractions ^[4] :

How the masks look on a chess board:

```

/**
 * Flip, mirror or reverse a bitboard
 * @param x any bitboard
 * @param flip the bitboard
 * @param mirror the bitboard
 * @return bitboard x flipped, mirrored or reversed
 */
U64 flipMirrorOrReverse(U64 x, bool flip, bool mirror)
{
    for (U32 i = 3*(1-mirror); i < 3*(1+flip); i++) {
        int s( 1 << i);
        U64 f( C64( 1) << s);
        U64 k( C64(-1) / (f+1) );
        x = ((x >> s) & k) + f*(x & k);
    }
    return x;
}

```

```
mirror:    for (U32 i = 0; i < 3; i++)
flip:      for (U32 i = 3; i < 6; i++)
reverse := mirror && flip
           for (U32 i = 0; i < 6; i++)
```

... and therefor following values for $i = 0 \dots 5$:

```
s(0) 1
f(0) 2
k(0) 0x5555555555555555 = 0xffffffffffffffff / (2+1)

s(1) 2
f(1) 4
k(1) 0x3333333333333333 = 0xffffffffffffffff / (4+1)

s(2) 4
f(2) 16
k(2) 0x0f0f0f0f0f0f0f0f = 0xffffffffffffffff / (16+1)

s(3) 8
f(3) 256
k(3) 0x0ff0ff0ff0ff0ff = 0xffffffffffffffff / (256+1)

s(4) 16
f(4) 65536
k(4) 0x000fffff000fffff = 0xffffffffffffffff / (65536+1)

s(5) 32
f(5) 4294967296
k(5) 0x00000000ffffffff = 0xffffffffffffffff / (4294967296+1)
```

Diagonal It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (<http://blog.wikispaces.com>)
Flip about the Diagonal

```
. 1 1 1 1 . . /      . . . . . . . .
. 1 . . . 1 . .      . . . . . . . .
. 1 . . . 1 . .      1 . . . . 1 1 .
. 1 . . 1 . . .      . 1 . . 1 . . 1
. 1 1 1 . . . .      . . 1 1 . . . 1
. 1 . 1 . . . .      . . . 1 . . . 1
. 1 . . 1 . . .      1 1 1 1 1 1 1 1
/ 1 . . . 1 . .      . . . . . . . .
```

A scalar square needs to swap rank and file.

```
sq' = ((sq >> 3) | (sq << 3)) & 63;
sq' = (sq * 0x20800000) >>> 26; // unsigned 32-bit shift, zeros no sign bits from left
```

Performing three [delta swaps](#):

```
/**
 * Flip a bitboard about the diagonal a1-h8.
 * Square h1 is mapped to a8 and vice versa.
 * @param x any bitboard
 * @return bitboard x flipped about diagonal a1-h8
 */
U64 flipDiagA1H8(U64 x) {
    U64 t;
    const U64 k1 = C64(0x5500550055005500);
    const U64 k2 = C64(0x3333000033330000);
    const U64 k4 = C64(0x0f0f0f0f00000000);
    t = k4 & (x ^ (x << 28));
    x ^= t ^ (t >> 28);
    t = k2 & (x ^ (x << 14));
    x ^= t ^ (t >> 14);
    t = k1 & (x ^ (x << 7));
    x ^= t ^ (t >> 7);
    return x;
}
```

How the masks look on a chess board:

k1	k2	k4
0x5500550055005500	0x3333000033330000	0xf0f0f0f000000000
1 . . . 1 . . .	1 1 . . 1 1 . .	1 1 1 1
.	1 1 . . 1 1 . .	1 1 1 1
1 . . . 1	1 1 1 1
.	1 1 1 1
1 . . . 1 . . .	1 1 . . 1 1
.	1 1 . . 1 1
1 . . . 1
.

Anti-Diagonal
Flip about the Anti-Diagonal

```
\ 1 1 1 1 . . .      . . . . . . . .
. 1 . . . 1 . .      1 1 1 1 1 1 1 1
. 1 . . . 1 . .      1 . . . 1 . . .
. 1 . . 1 . . .      1 . . . 1 1 . .
. 1 1 1 . . . .      1 . . 1 . . 1 .
. 1 . 1 . . . .      . 1 1 . . . . 1
. 1 . . 1 . . .      . . . . . . . .
. 1 . . . 1 . \      . . . . . . . .
```

Flip about the [Anti-Diagonal](#) results in the bit-reversal of flip about the Diagonal.
Thus, a scalar square needs not only swap rank and file, but also xor 63.

```
sq' = (((sq >> 3) | (sq << 3)) & 63) ^ 63;
sq' = ((sq * 0x20800000) >>> 26) ^ 63; // unsigned 32-bit shift
```

Performing three [delta swaps](#):

```
/**
 * Flip a bitboard about the antidiagonal a8-h1.
 * Square a1 is mapped to h8 and vice versa.
 * @param x any bitboard
 * @return bitboard x flipped about antidiagonal a8-h1
 */
U64 flipDiagA8H1(U64 x) {
    U64 t;
    const U64 k1 = C64(0xaa00aa00aa00aa00);
    const U64 k2 = C64(0xcccc0000cccc0000);
    const U64 k4 = C64(0xf0f0f0f00f0f0f0f);
    t = x ^ (x << 36);
    x ^= k4 & (t ^ (x >> 36));
    t = k2 & (x ^ (x << 18));
    x ^= t ^ (t >> 18);
    t = k1 & (x ^ (x << 9));
    x ^= t ^ (t >> 9);
    return x;
}
```

How the masks look on a chess board:

k1	k2	k4
0xAAAA00AA00AA00	0xCCCC0000CCCC0000	0xf0f0f0f00f0f0f0f
. 1 . . 1 . . 1	. . 1 1 . . 1 1 1 1 1 1
. 1 1 . . 1 1 1 1 1 1
. 1 . . 1 . . 1 1 1 1 1
. 1 1 1 1
. 1 . . 1 . . 1	. . 1 1 . . 1 1	1 1 1 1
. 1 1 . . 1 1	1 1 1 1

```
. 1 . 1 . 1 . 1 . . . . . . . . . . 1 1 1 1 . . . . .
. . . . . . . . . . . . . . . . . . . . 1 1 1 1 . . . . .
```

✖ It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (<http://blog.wikispaces.com>)

Rotating

This is about

- [Rotation by 180 degrees](#)
- [Rotation by 90 degrees Clockwise](#)
- [Rotation by 90 degrees Anti-Clockwise](#)

Rotation can be deduced from flipping and mirroring in various ways.

	mirrorHorizontal	flipDiagAIH8	flipDiagA8H1
. 1 1 1 1 1 1 1 1
. 1 . . . 1 1 . . . 1	1 1 1 1 1 1 1 1 1
. 1 . . . 1 1 . . . 1	1 1 1	1 . . . 1
. 1 . . . 1 1 . . . 1 1 . . . 1 . . . 1 .	1 . . . 1 1
. 1 1 1 1 1 1 1 1 1 . .	1 . . . 1 . . . 1 .
. 1 . 1 1 . . . 1 1 1 . .	. 1 1 1 .
. 1 . . 1 1 . . . 1 . . .	1 1 1 1 1 1 1 1 1
. 1 . . . 1 1 1
flipVertical	rotate180	rotate90clockwise	rotate90antiClockwise
. 1 . . . 1 1 . . . 1
. 1 . . 1 1 . . . 1	1 1 1 1 1 1 1 1 1
. 1 . 1 1 . . . 1 1 1 . .	. 1 1 1 .
. 1 1 1 1 1 1 1 1 1 . .	1 . . . 1 . . . 1 .
. 1 . . 1 1 1 1 . . . 1 . . . 1 .	1 . . . 1 1
. 1 . . . 1 1 . . . 1 . . .	1 1 1	1 . . . 1
. 1 . . . 1 1 1	1 1 1 1 1 1 1 1 1
. 1 1 1 1 1 1 1 1

By 180 degrees - Bit-Reversal

```
. 1 1 1 1 . . . . . . . 1 . . . 1 .
. 1 . . . 1 . . . . . . 1 . . . 1 .
. 1 . . . 1 . . . . . . 1 . . 1 .
. 1 . . 1 . . . . . . . 1 1 1 .
. 1 1 1 . . . . . . . . 1 . . 1 .
. 1 . 1 . . . . . . . . 1 . . 1 .
. 1 . . 1 . . . . . . . 1 . . . 1 .
. 1 . . . 1 . . . . . . 1 1 1 1 .
```

Rotating by 180 degrees reverses all bits in a bitboard. A scalar square may be reversed by xor 63:

```
sq' = sq ^ 63; // 63 - sq;
```

Deduced from [flipping vertically](#), and [mirroring horizontally](#). Both operation may be applied in different orders.

```
/**
 * Rotate a bitboard by 180 degrees.
 * Square a1 is mapped to h8, and a8 is mapped to h1.
 * @param x any bitboard
 * @return bitboard x rotated 180 degrees
 */
U64 rotate180 (U64 x) {
    return mirrorHorizontal (flipVertical (x) );
}
```

The resulting code applies six [delta swaps](#):

```
/**
 * Rotate a bitboard by 180 degrees.
 * Square a1 is mapped to h8, and a8 is mapped to h1.
 * @param x any bitboard
 * @return bitboard x rotated 180 degrees
 */
U64 rotate180 (U64 x) {
    const U64 h1 = C64 (0x5555555555555555);
    const U64 h2 = C64 (0x3333333333333333);
    const U64 h4 = C64 (0x0F0F0F0F0F0F0F0F);
    const U64 v1 = C64 (0x00FF00FF00FF00FF);
    const U64 v2 = C64 (0x0000FFFF0000FFFF);
    x = ((x >> 1) & h1) | ((x & h1) << 1);
    x = ((x >> 2) & h2) | ((x & h2) << 2);
    x = ((x >> 4) & h4) | ((x & h4) << 4);
    x = ((x >> 8) & v1) | ((x & v1) << 8);
    x = ((x >> 16) & v2) | ((x & v2) << 16);
    x = ( x >> 32) | ( x << 32);
    return x;
}
```

By 90 degrees Clockwise

```
. 1 1 1 1 . . . . . . . . . .
. 1 . . . 1 . . . . . 1 1 1 1 1 1 1
. 1 . . . 1 . . . . . . 1 . . . 1
. 1 . . 1 . . . . . . . 1 1 . . . 1
. 1 1 1 . . . . . . 1 . . . 1 . . 1
. 1 . 1 . . . . . . 1 . . . . 1 1 .
. 1 . . 1 . . . . . . . . . . . .
. 1 . . . 1 . . . . . . . . . . .
```

A scalar square swaps rank and file plus xor 56:

```
sq' = (((sq >> 3) | (sq << 3)) & 63) ^ 56;
sq' = ((sq * 0x20800000) >>> 26) ^ 56; // unsigned 32-bit shift
```

Deduced from [flipping vertically](#), and [flipping along the antidiagonal](#).

```
/**
 * Rotate a bitboard by 90 degrees clockwise.
```

```
* @param x any bitboard
* @return bitboard x rotated 90 degrees clockwise
```

```
U64 rotate90clockwise (U64 x) {
    return flipVertical (flipDiagA1H8 (x) );
}
```

Note that

```
flipVertical (flipDiagA1H8 (x) ) == flipDiagA8H1 (flipVertical (x) )
```

By 90 degrees Anti-Clockwise

```
. 1 1 1 1 . . . . . . . . . .
. 1 . . . 1 . . . . . . . . . .
. 1 . . . 1 . . . 1 1 . . . . 1
. 1 . . 1 . . . . 1 . . 1 . 1 .
. 1 1 1 . . . . . 1 . . . 1 1 . .
. 1 . 1 . . . . . 1 . . . 1 . . .
. 1 . . 1 . . . . 1 1 1 1 1 1 1
. 1 . . . 1 . . . . . . . . . .
. 1 . . . 1 . . . . . . . . . .
```

A scalar square swaps rank and file plus xor 7:

```
sq' = (((sq >> 3) | (sq << 3)) & 63) ^ 7;
sq' = ((sq * 0x20800000) >>> 26) ^ 7; // unsigned 32-bit shift
```

Deduced from [flipping vertically](#) and [flipping along the diagonal](#).

```
/**
 * Rotate a bitboard by 90 degrees anticlockwise.
 * @param x any bitboard
 * @return bitboard x rotated 90 degrees anticlockwise
 */
U64 rotate90anticlockwise (U64 x) {
    return flipDiagA1H8 (flipVertical (x) );
}
```

Note that

```
flipDiagA1H8 (flipVertical (x) ) == flipVertical (flipDiagA8H1 (x) )
```

Pseudo-Rotation by 45 degrees

The chess-board is four-fold symmetry - thus there is no real 45 degree rotation in the mathematical sense. Anyway we may map [diagonals](#) and [anti-diagonals](#) to [ranks](#), similar to [rotated bitboards](#).

Clockwise

The 15 [diagonals](#) are enumerated by (file - rank) - [nibble](#) wise [two's complement](#) F == (16) -1, 9 == (16) -7. Two shorter diagonals are file-aligned packed into one rank each. Note that the three lower bits are equal in each rank and bit three (the sign-bit inside a signed nibble) indicates a "negative" diagonal north the main diagonal.

```
9 A B C D E F 0 9 1 1 1 1 1 1 1
A B C D E F 0 1 A A 2 2 2 2 2 2
B C D E F 0 1 2 B B 3 3 3 3 3 3
C D E F 0 1 2 3 C C C C 4 4 4 4
D E F 0 1 2 3 4 D D D D 5 5 5 5
E F 0 1 2 3 4 5 E E E E 6 6 6 6
F 0 1 2 3 4 5 6 F F F F 7 7 7 7
0 1 2 3 4 5 6 7 0 0 0 0 0 0 0 0
```

We need to rotate the A-H files vertically by 0 to 7 ranks - done parallel prefix wise. One square is therefor mapped by:

```
sq' = (sq + 8*(sq&7)) & 63;
```

The main-diagonal is rotated clockwise to the first rank - thus 45 degrees.

On using xor, see [bits from two sources by a mask](#). See [rotate](#) for the intrinsic routines.

```
/**
 * Pseudo rotate a bitboard 45 degree clockwise.
 * Main Diagonal is mapped to 1st rank
 * @param x any bitboard
 * @return bitboard x rotated
 */
U64 pseudoRotate45clockwise (U64 x) {
    const U64 k1 = C64(0xAAAAAAAAAAAAAAAA);
    const U64 k2 = C64(0xCCCCCCCCCCCCCCCC);
    const U64 k4 = C64(0xF0F0F0F0F0F0F0F0);
    x ^= k1 & (x ^ rotateRight(x, 8));
    x ^= k2 & (x ^ rotateRight(x, 16));
    x ^= k4 & (x ^ rotateRight(x, 32));
    return x;
}
```

Another pseudo rotation scheme was introduced by [Robert Hyatt's rotated bitboards](#) approach. While the 45 degree rotation looks more natural at the first glance, the calculations of this mapping is more complicated.

normal chess board bitmap	45 clockwise	45 clockwise crafty
A8 B8 C8 D8 E8 F8 G8 H8		C7 D8 A6 B7 C8 A7 B8 A8
A7 B7 C7 D7 E7 F7 G7 H7	A8	F8 A4 B5 C6 D7 E8 A5 B6
A6 B6 C6 D6 E6 F6 G6 H6	A7 B8	E6 F7 G8 A3 B4 C5 D6 E7
A5 B5 C5 D5 E5 F5 G5 H5	A6 B7 C8	E5 F6 G7 H8 A2 B3 C4 D5
A4 B4 C4 D4 E4 F4 G4 H4	A5 B6 C7 D8	E4 F5 G6 H7 A1 B2 C3 D4
A3 B3 C3 D3 E3 F3 G3 H3	A4 B5 C6 D7 E8	D2 E3 F4 G5 H6 B1 C2 D3
A2 B2 C2 D2 E2 F2 G2 H2	A3 B4 C5 D6 E7 F8	G3 H4 D1 E2 F3 G4 H5 C1
A1 B1 C1 D1 E1 F1 G1 H1	A2 B3 C4 D5 E6 F7 G8	H1 G1 H2 F1 G2 H3 E1 F2
	A1 B2 C3 D4 E5 F6 G7 H8	
A8 B1 C2 D3 E4 F5 G6 H7	B1 C2 D3 E4 F5 G6 H7	A8 B1 C2 D3 E4 F5 G6 H7
A7 B8 C1 D2 E3 F4 G5 H6	C1 D2 E3 F4 G5 H6	A7 B8 C1 D2 E3 F4 G5 H6
A6 B7 C8 D1 E2 F3 G4 H5	D1 E2 F3 G4 H5	A6 B7 C8 D1 E2 F3 G4 H5
A5 B6 C7 D8 E1 F2 G3 H4	E1 F2 G3 H4	A5 B6 C7 D8 E1 F2 G3 H4

A4 B5 C6 D7 E8 F1 G2 H3	F1 G2 H3	A4 B5 C6 D7 E8 F1 G2 H3
A3 B4 C5 D6 E7 F8 G1 H2	G1 H2	A3 B4 C5 D6 E7 F8 G1 H2
<p> A4 B5 C6 D7 E8 F1 G2 H3 A3 B4 C5 D6 E7 F8 G1 H2 A2 B3 C4 D5 E6 F7 G8 H1 A1 B2 C3 D4 E5 F6 G7 H8 </p>		
45 clockwise		45 clockwise

A parallel prefix solution to map the normal occupancy to the visual rotated approach is left to the ambitious reader.

Anti-Clockwise

We enumerate the 15 [anti-diagonals](#) by 7 ^ (file + rank), a [nibble](#) wise [two's complement](#) F == -1.

0	F	E	D	C	B	A	9	1	1	1	1	1	1	9
1	0	F	E	D	C	B	A	2	2	2	2	2	A	A
2	1	0	F	E	D	C	B	3	3	3	3	B	B	B
3	2	1	0	F	E	D	C	4	4	4	4	C	C	C
4	3	2	1	0	F	E	D	5	5	D	D	D	D	D
5	4	3	2	1	0	F	E	6	E	E	E	E	E	E
6	5	4	3	2	1	0	F	7	F	F	F	F	F	F
7	6	5	4	3	2	1	0	0	0	0	0	0	0	0

We need to rotate the A-H files vertically by 7 to 0 ranks - done parallel prefix wise.
One square is therefor mapped by:

```
sq' = (sq + 8*((sq&7)^7)) & 63;
```

The main anti-diagonal is rotated anti-clockwise to the first rank - thus 45 degrees. The shorter anti-diagonals are pairwise and properly file aligned packed into further ranks.

On using xor see [bits from two sources by a mask](#). See [rotate](#) for the intrinsic routines.

```

/**
 * Pseudo rotate a bitboard 45 degree anti clockwise.
 * Main AntiDiagonal is mapped to 1st rank
 * @param x any bitboard
 * @return bitboard x rotated
 */
U64 pseudoRotate45antiClockwise (U64 x) {
    const U64 k1 = C64(0x5555555555555555);
    const U64 k2 = C64(0x3333333333333333);
    const U64 k4 = C64(0x0f0f0f0f0f0f0f0f);
    x ^= k1 & (x ^ rotateRight(x, 8));
    x ^= k2 & (x ^ rotateRight(x, 16));
    x ^= k4 & (x ^ rotateRight(x, 32));
    return x;
}
```

Rank, File and Diagonal

Those subsets may be flipped or mirrored in a more efficient way by multiplication-techniques with disjoint intermediate sums and no internal overflows. Unlike the whole board techniques, multiplication doesn't swap bits, but maps file to a rank or vice versa in different steps, which can not be combined in one step. Main application is to map file- or diagonal occupancies to ranks, to dense the line-occupancy to consecutive bits, further elaborated in [Occupancy of any Line](#) or [Kindergarten Bitboards](#).

Flip about the Anti-Diagonal

Flipping about the anti-diagonal multiplies with the main-diagonal. Note that the set bits in the main-diagonal have a distance of 9 (2^0, 2^9,2^18,....,2^54, 2^63). We can therefor safely multiply it with a rank-pattern with 8 consecutive neighboring bits without overflows.

File to a Rank

Multiplying the masked A-file with the main-diagonal, maps the file-bits to the 8th rank, similar to a flip about the anti-diagonal A8-H1. Shifting down to the 1st rank, leaves the bits like a 90-degree anti clockwise rotation.

masked bits			mapped to 8th rank	
bits on A-file	* main-diagonal	=	with garbage	-> 1st rank
A 1		A B C D E F G H
B 1 .		B C D E F G H
C 1 . .		C D E F G H
D 1 . . .		D E F G H . . .	>>
E 1	=	E F G H	56
F 1		F G H
G 1		G H
H	1		H	A B C D E F G H

Rank to File

Multiplying the masked 1st rank with the main-diagonal, maps the rank-bits to the H-file, similar to a flip about the anti-diagonal A8-H1. Shifting the H-file to the A-file plus mask acts like a 90-degree clockwise rotation.

masked bits			mapped to H-file	
bits on 1st rank	* main-diagonal	=	with garbage	-> masked A-file
. A 1		C D E F G H . A	A
. B 1 .		D E F G H . A B	B
. C 1 . .		E F G H . A B C	>> C
. D 1 . . .		F G H . A B C D	7 D
. E	. . . 1	=	G H . A B C D E	& E
. F	. . 1		H . A B C D E F	A F
. G	. 1 A B C D E F G	G
A B C D E F G H	1		A B C D E F G H	H


Flip about the Diagonal

Flipping about the Diagonal is a bit more tricky. Since the Anti-Diagonal pattern as factor has the set bits with distance of 7 only (2^0,2^7, 2^14,...,2^49, 2^56) with possible overflows, if multiplied with rank pattern of eight neighboring bits. Thus it can only be used to flip the H-file about the diagonal.

File to a Rank

Multiplying the masked H-file with the 7-bit right shifted (board left shifted) anti-diagonal, maps the file-bits to the 8th rank, similar to a flip about the diagonal A1-H8. Shifting it down to the 1st rank, leaves the bits like flip about the diagonal. Shifting down to the 1st rank, leaves the bits like a 90-degree clockwise rotation.

masked bits	Shifted		mapped to 8th rank	
bits on H-file	* anti-diagonal	=	with garbage	-> 1st rank
. A		H G F E D C B A
. B	. 1 H G F E D C B
. C	. . 1 H G F E D C

. D . . . 1 H G F E D >>
 E * 1 = H G F E 56
 •  It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (<http://blog.wikispaces.com>)
 G 1 H G
 / H 1 1 H H G F E D C B A

That is straight forward multiplication of a masked diagonal or anti-diagonal with the A-file. To mask the garbage off, we further shift down by 7 ranks.

```

masked diagonal * A-file          mapped
                                  to 8th rank    -> 1st rank
. . . . . H      1 . . . . . A B C D E F G H . . . . .
. . . . . G      1 . . . . . A B C D E F G . . . . .
. . . . . F      1 . . . . . A B C D E F . . . . . >>
. . . . . E      1 . . . . . A B C D E . . . . . 56
. . . . . D      * 1 . . . . . = A B C D . . . . .
. . . . . C      1 . . . . . A B C . . . . .
. . . . . B      1 . . . . . A B . . . . .
A . . . . .      1 . . . . . A . . . . . A B C D E F G H

```

This is about bit-reversal of a byte.

```
rank1mirrored = (((rank1 * 0x80200802) & 0x0884422110) * 0x0101010101010101) >> 56;
```

```

rank1          * 0x80200802          flipped
. . . . .      . . . . .      . . . . .
. . . . .      . . . . .      . . . . .
. . . . .      . . . . .      . . . . .
. . . . .      . . . . .      B C D E F G H .
. . . . .      * . . . . . 1 = D E F G H . . A
. . . . .      . . . . . 1 . F G H . . A B C
. . . . .      . . . 1 . . . H . . A B C D E
A B C D E F G H . 1 . . . . . . A B C D E F G

flipped        & 0x0884422110        reversedOnFiles
. . . . .      . . . . .      . . . . .
. . . . .      . . . . .      . . . . .
. . . . .      . . . . .      . . . . .
B C D E F G H . . . . 1 . . . . . E . . . .
D E F G H . . A & . . 1 . . . 1 = . . F . . . A
F G H . . A B C . 1 . . . 1 . . G . . . B .
H . . A B C D E . 1 . . . 1 . . H . . . C . .
. A B C D E F G . . . . 1 . . . . . D . . .

reversedOnFiles * A-file              reversedOn8      reversed
. . . . .      1 . . . . .      H G F E D C B A      . . . . .
. . . . .      1 . . . . .      H G F E D C B A      . . . . .
. . . . .      1 . . . . .      H G F E D C B A      . . . . .
. . . E . . .      1 . . . . .      H G F E D C B A      >> . . . . .
. . F . . . A * 1 . . . . . = H G F . D C B A 56 . . . . .
. G . . . B .      1 . . . . .      H G . . D C B .      . . . . .
H . . . C . .      1 . . . . .      H . . . D C . .      . . . . .
. . . . D . .      1 . . . . .      . . . . D . . .      H G F E D C B A

```

```
rank1mirrored = ( (rank1 * 0x0802 & 0x22110)
                  |(rank1 * 0x8020 & 0x88440) )
                  * 0x10101000 >> 24;
```

```
rank1mirrored = reverseByteLookup256[rank1];
```

- [BMI2.PEXT instruction](#)
- [Color Flipping](#)
- [Diagonal Mirroring](#)
- [Horizontal Mirroring](#)
- [Kindergarten Bitboards](#)
- [Occupancy of any Line](#)
- [Vertical Flipping](#)
- [XOP VPPERM instruction](#)

- [Christopher Strachey \(1961\)](#). *Bitwise operations*. [Communications of the ACM](#), Vol. 4, No. 3 ^[5]
- [Henry S. Warren, Jr. \(2002, 2012\)](#). *Hacker's Delight*. Addison-Wesley.
- [Donald Knuth \(2009\)](#). *The Art of Computer Programming* , Volume 4, Fascicle 1: Bitwise tricks & techniques, as [Pre-Fascicle 1a postscript](#)

- [Reflection of a bitboard](#) by Harm Geert Muller, CCC, April 22, 2016

- [Bit Gather Via Multiplication](#) by [Vlad Petric](#), [Dr. Petric's Technical Blog](#) , September 17, 2013 ^[6]

- [Flip from Wikipedia](#)
- [Flip \(mathematics\) from Wikipedia](#)
- [Flip](#) from [iCoachMath](#)
- [Flip, Slide, Turn - Alphabet Geometry](#) from [misterteacher.com](#)

- [Mirror from Wikipedia](#)
- [Mirroring \(psychology\) from Wikipedia](#)
- [Reflection \(mathematics\) from Wikipedia](#)

- [Reflection \(physics\) from Wikipedia](#)
 - [Reflection symmetry from Wikipedia](#)
 - [Why do Mirrors Reverse Left and Right?](#)
- It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (<http://blog.wikispaces.com>)

Rotation

- [Rotation from Wikipedia](#)
- [Rotation \(mathematics\) from Wikipedia](#)
- [Rotation matrix from Wikipedia](#)
- [Rotation formalisms in three dimensions - Wikipedia](#)
- [Rotation](#) from [iCoachMath](#)
- [Oliver Vornberger's](#) German [lecture](#) on Graphic Rotation:
 - [2D Rotation](#)
 - [3D Rotation](#)

Reflection

- [Reflection \(mathematics\) from Wikipedia](#)
- [Reflection \(physics\) from Wikipedia](#)
- [Reflection symmetry from Wikipedia](#)

Smoke 'n' Mirrors

- [Lee Ritenour](#), [Mike Stern](#), [Simon Phillips](#), [John Beasley](#) , [Melvin Davis](#) - Smoke 'n' Mirrors ^[1] [Blue Note Tokyo](#) , 2011, [YouTube](#) Video ^[2]



References





1. [^] [Figurative Paintings](#) by [Barbara Mittman](#)
2. [^] [byteswap_uint64](#) Visual C++ Developer Center - Run-Time Library Reference
3. [^] [rotl, rotr, rotr64, rotr64](#) Visual C++ Developer Center - Run-Time Library Reference
4. [^] [Donald Knuth \(2009\). The Art of Computer Programming , Volume 4, Fascicle 1: Bitwise tricks & techniques, as Pre-Fascicle 1a postscript](#)
5. [^] [reverse.c](#) from [C code for most of the programs that appear in HD](#) by [Henry S. Warren, Jr.](#)
6. [^] [Demystifying the Magic Multiplier?](#)
7. [^] [Smoke and mirrors \(disambiguation\)](#)
8. [^] [Shorter front view version with interviews](#)






What links here?

Page	Date Edited
Aleks Peshkov	Jan 13, 2016
Algorithms	May 5, 2017
Anti-Diagonals	Sep 2, 2012
Big-endian	Jan 25, 2015
Bit-Twiddling	Nov 6, 2017
Bitboard Serialization	Dec 24, 2014
Bitboards	Nov 14, 2017
Chessboard	May 10, 2017
Christopher Strachey	May 8, 2017
Color Flipping	May 17, 2017
Crafty	Jan 28, 2018
Diagonal Mirroring	Jun 29, 2013
Diagonals	Jan 16, 2013
Direction	Oct 6, 2016
Efficient Generation of Sliding Piece Attacks	Nov 5, 2016
Endianness	Jan 25, 2015
Flipping Mirroring and Rotating	Oct 14, 2016
General Setwise Operations	Feb 25, 2018
Gk	Oct 9, 2017
Horizontal Mirroring	Jun 29, 2013
Hyperbola Quintessence	Mar 25, 2017
KBNK Endgame	Nov 26, 2016
Kindergarten Bitboards	Aug 1, 2017
Kurt	Apr 20, 2014
Little-endian	Jan 25, 2015
Occupancy	Sep 19, 2016
Occupancy of any Line	Sep 16, 2016
Parallel Prefix Algorithms	Jun 22, 2016
Population Count	Sep 3, 2017
Reverse Bitboards	Aug 29, 2015
Rotated Bitboards	Mar 7, 2017
Rotated Indices	Oct 9, 2017
Ryan Mack	Jan 18, 2011
SIMD and SWAR Techniques	Jun 27, 2017
Squares	Feb 15, 2015
SSSE3	Aug 8, 2017
Vertical Flipping	Oct 10, 2013

Page	Date Edited
Vladimir ✖ It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (http://blog.wikispaces.com)	Oct 25, 2013
Wing	Oct 26, 2017
XOP	Aug 8, 2017

[Up one Level](#)


(https://www.wikispaces.com/user/view/workingonchess) 	Idea to avoid rotating workingonchess (https://www.wikispaces.com/user/view/workingonchess) Jan 23, 2012	▼
<p>Hello,</p> <p>It's seems too easy to be true, but I have an idea to avoid rotating and calculate good moves for sliding pieces. We could put a mask to a sliding piece, this mask will be retrieved with the piece position. Applying this mask (with most 0 a few 1) on the entire chessboard with all pieces, we retrieve 64*64 possibilities. Putting this new bitboard into a hashmap we could retrieve all the moves for the current piece.</p> <p>As example, we got a rook at c3 square. We put the bitboard with only one 1 at c3 to an hashmap. This hashmap will give a bitboard with four rectangles of 0 and two lines of 1. The lines will be c8 to c1 and a3 to h3. We can now do an AND for all pieces of the chessboard. We will retrieve a bitboard with a almost only 0 and some 0 on the two lines. Now we can put the result into another hashmap which will bring the final moves for the rook. There will be 64*64 items into this hashmap. We could do the same for bishop, and add theses two techniques to compute queen moves. Using this we do not need to rotate bitmap. Where is the problem with this method ? Sorry for bad english and thanks beforehand.</p> <p>Bretwa</p>		
	(https://www.wikispaces.com/user/view/Gerdsenberg) Gerdsenberg (https://www.wikispaces.com/user/view/Gerdsenberg) Jan 23, 2012	
<p>Hi Bretwa, this page "Flipping Mirroring and Rotating" has nothing to do with move generation. Intersection of occupancy with the one or two lines to lookup attack sets is topic of Sliding Piece Attacks (/Sliding%20Piece%20Attacks), specially the none rotated lookup techniques Kindergarten Bitboards (/Kindergarten%20Bitboards), Hashing Dictionaries (/Hashing%20Dictionaries), Congruent Modulo Bitboards (/Congruent%20Modulo%20Bitboards) and Magic Bitboards (/Magic%20Bitboards).</p> <p>Gerd</p>		
	(https://www.wikispaces.com/user/view/workingonchess) workingonchess (https://www.wikispaces.com/user/view/workingonchess) Jan 25, 2012	
<p>Hi Gerd,</p> <p>Sorry for that, I have believed it was the right place to deal with rotating efficiency because this article deals with rotating bitboard. Actually the method I have given already exists and is fully described here http://code.google.com/p/shatranjpy/downloads/detail?name=avoiding-rotations-final.pdf&can=2&q= (<a "="" href="http://code.google.com/p/shatranjpy/downloads/detail?name=avoiding-rotations-final.pdf&can=2&q=">http://code.google.com/p/shatranjpy/downloads/detail?name=avoiding-rotations-final.pdf&can=2&q=). Probably it could be a good idea to compare on this wiki the good and worse ideas about chess programming in order to give a conspicuous level on what works effectively and what is not.</p> <p>Bretwa</p>		
	(https://www.wikispaces.com/user/view/Gerdsenberg) Gerdsenberg (https://www.wikispaces.com/user/view/Gerdsenberg) Jan 25, 2012	
<p>Hi Bretwa,</p> <p>No problem, I was even a bit wrong since this page also covers in its second part <i>Rank, File and Diagonal</i> the basics of kindergarten bitboard index calculation. Sam Tannous (/Sam%20Tannous) approach and paper is mentioned in Hashing Dictionaries (/Hashing%20Dictionaries). At least in compiled C/C++ a none rotated "and/mul/shift" perfect hashing function ala kindergarten or magic lookups seems hard to beat.</p> <p>Gerd</p>		

(https://www.wikispaces.com/user/view/AGN1964) 	45, 135 degree rotations AGN1964 (https://www.wikispaces.com/user/view/AGN1964) Aug 31, 2011	▼
<p>This wiki and this bitboard rotation page contain some amazing ideas and a lot of low level code that I could not recreate myself. Kudos to all involved.</p> <p>I am using the Pseudo-Rotation by 45 degrees routine to convert a bitboard to a "horizontal" representation, where I can do some fast processing. Once complete, I need to rotate back to the original position. Due to the different diagonal packing mechanism: pseudoRotate45antiClockwise(pseudoRotate45clockwise(x) != x Of course, I'll need the undoPseudoRotate45antiClockwise() next, too. I am not good enough with binary math to figure out my own undoPseudoRotate45clockwise() function. I've searched, looked at the references, look at What Links Here, but I can only see the two forward rotation functions. Can anyone point me to the two undo functions I need? Or give a link to tools that might help me devise my own? Thanks.</p>		
	(https://www.wikispaces.com/user/view/Gerdsenberg) Gerdsenberg (https://www.wikispaces.com/user/view/Gerdsenberg) Aug 31, 2011	
<p>Using the same routines with rotateLeft inside should do the trick, I guess.</p> <p>Gerd</p>		
	(https://www.wikispaces.com/user/view/AGN1964) AGN1964 (https://www.wikispaces.com/user/view/AGN1964) Sep 2, 2011	
<p>After 5 mins of testing, I'm sure you are correct. I am surprised the answer was so simple!</p> <p>Thanks very much.</p>		
	(https://www.wikispaces.com/user/view/Gerdsenberg) Gerdsenberg (https://www.wikispaces.com/user/view/Gerdsenberg) Sep 2, 2011	
<p>You are welcome!</p> <p>Curious about your fast processing of the "horizontal" representation, with such a prologue and epilogue to map and re-map the bits. Isn't it cheaper to perform the processing directly in the "diagonal" world?</p>		
	(https://www.wikispaces.com/user/view/AGN1964) AGN1964 (https://www.wikispaces.com/user/view/AGN1964) Sep 2, 2011	
<p>I am re-writing my Othello program, for the fourth time; the original is over 30 years old now. This is the first version using bitboards. This particular question came up during move generation. Using 2 8-bit integers, representing black and white positions in one row, I have precalculated all the legal moves and stored them in an array; it's quite small [256][256][2]. Move list generation (for a single row) is now a quick look up. For a full board, I need to or the results from all possible rows together, i.e.</p>		

✖ It's time for us to say farewell... Regretfully, we've made the tough decision to close Wikispaces. Find out why, and what will happen, here (http://blog.wikispaces.com)

from all ranks, files and diagonals. The 8 ranks can be extracted from the bitboards easily, and making the result bit board is simple, too. Then I flip the board along the diagonal, to swap ranks and files and repeat the process. I just flip the result to put the bits back in the correct position. Finally I do something similar for the 45 and 135 diagonals; extracting the diagonals is slightly harder since two diagonals are packed into each rank. Currently, this is 80 times faster than a naive 2D indexing approach. I probably could extract the 8-bit row integers directly. But while I am using an 8-bit number for the look up, I think I will always need something equivalent to the rotation, masking and shifting to get the bits in need. Perhaps it could be done more efficiently than currently, where 64-bit rotation is a separate operation from 8-bit extraction, but I think that would be a small gain. I think I would need to abandon my look-up table if I stay in the "diagonal world"; perhaps there are efficient algorithms in that space. As I become more experienced with the bitboards, I might re-examine this. Thanks for the help and the interest.

[Hilfe](#) · [Über](#) · [Preisliste](#) · [Privatsphäre](#) · [Bedingungen](#) · [Unterstützung](#) · [Höherstufen](#)

Contributions to <https://chessprogramming.wikispaces.com/> are licensed under a [Creative Commons Attribution Share-Alike 3.0 License](#). 

Portions not contributed by visitors are Copyright 2018 Tangient LLC

[TES](#): The largest network of teachers in the world