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KATEDRA INFORMATYKI

PRACA DYPLOMOWA MAGISTERSKA

Angielski tytuł pracy

A tutaj jej polski tytuł

Autor:
Kierunek studiów:
Opiekun pracy:

Jan Kowalski
Informatyka
dr hab. inż. Zbigniew Iksiński, prof. AGH

Kraków, 2016

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.....

SKŁADAM SZCZEGÓLNE PODZIĘKOWANIA MOJEMU
PROMOTOROWI, DR HAB. INŻ. ?????,
PROFESOROWI NADZWYCZAJNEMU AGH ZA
ŻYCZLIWOŚĆ, CENNE UWAGI MERYTORYCZNE,
WSZECHESTRONNĄ POMOC ORAZ POŚWIĘCONY
CZAS.

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Chapter 1

Preface

1.1 Motivation

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1.2 Content of this work

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The chapter 2 provides the requirements for the project, and as well formulates the sample problem of shallow water simulation. The chapter 3 outlines the tools and methods necessary for approaching the problems. In the chapter 4 I thoroughly document the software I developed to accomplish the research goals. I discuss the obtained results in the chapter 5 and sum up the thesis in chapter 6.

1.3 State of the art

1.3.1 Technology 1

A lot of bibliography citations here...

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1.3.2 Technology 2

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1.4 Main thesis of this work

The main thesis of this work may be expressed as follows:

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Chapter 2

Problem formulation

Describe what each section contains...

2.1 Issues to be addressed in this work

2.1.1 (e.g.) Algorithmic challenges

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2.1.2 (e.g.) Parallelization challenges

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2.2 Functional requirements

1. Core functionalities

(a) ...

(b) ...

(c) ...

2. Adaptation strategies

(a) ...

(b) ...

3. Visualization and profiling

(a) ...

(b) ...

(c) ...

(d) ...

2.3 Non-functional requirements

1. Performance and complexity

(a) ...

(b) ...

(c) ...

2. Development requirements

(a) ...

(b) ...

Chapter 3

Solution methodology

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3.1 Method 1

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tellus, aliquet aliquam, luctus a, egestas a, turpis. Mauris lacinia lorem sit amet ipsum. Nunc quis urna dictum turpis accumsan semper.

3.2 Method 2

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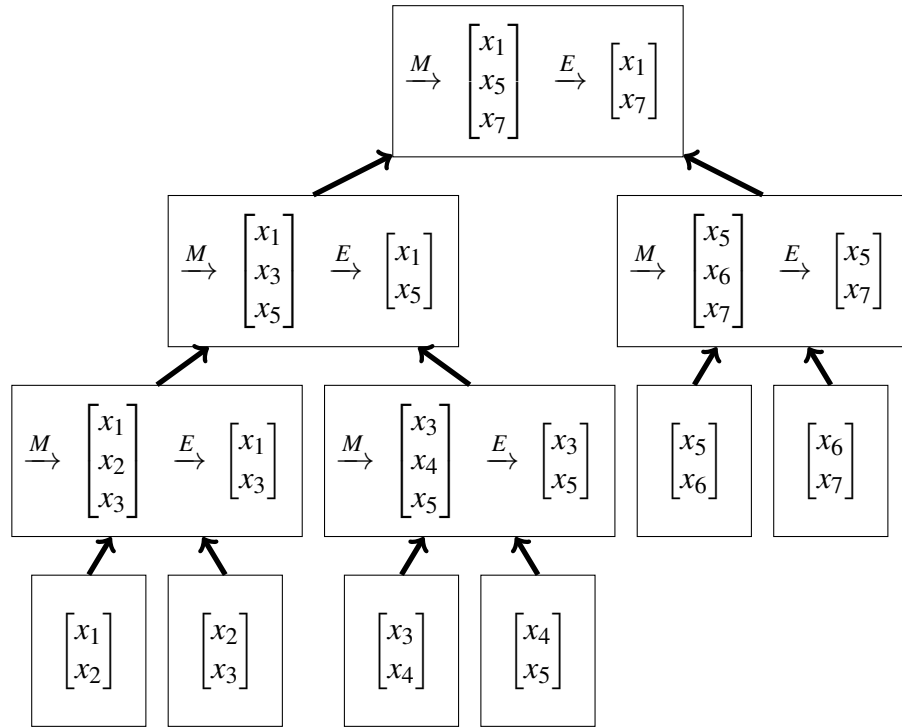
3.3 Method 3

Some nice matrices...

$$A = \begin{bmatrix} 1 & & & & & & \\ 1 & -2 & 1 & & & & \\ & 1 & -2 & 1 & & & \\ & & 1 & -2 & 1 & & \\ & & & 1 & -2 & 1 & \\ & & & & 1 & -2 & 1 \\ & & & & & 1 & \\ & & & & & & 1 \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 0 \end{bmatrix} \quad (3.1)$$

Some nice diagrams...

Figure 3.1: Elimination tree for multifrontal solver



Some nice algorithms...

Algorithm 1 One iteration of the double-grid algorithm

```
Compute the solution  $\mathcal{U}^C$  on the coarse mesh
Split each element of the coarse mesh, thus obtaining the fine mesh
Compute the solution  $\mathcal{U}^F$  on the fine mesh
for each coarse mesh element  $\varepsilon_i$  do
   $\triangleright \rho_i$  is the relative error
   $\rho_i \leftarrow \left| \frac{\mathcal{U}_i^F - \mathcal{U}_i^C}{\mathcal{U}_i^F} \right|$ 
end for
 $\rho_{max} \leftarrow \max_i(\rho_i)$ 
for each element  $\varepsilon_i$  do
  if  $\rho_i > \tau \cdot \rho_{max}$  then
    adapt the  $\varepsilon_i$  element (split into two halves)
  end if
end for
```

Some nice figures...

Figure 3.2: Steps 1-5 of the double-grid h-adaptation strategy, quadratic B-splines



(a) Step 1. A solution is delivered on coarse (4 elements) and fine grid (8 elements). Red line marks the coarse-grid solution, green line — the fine-grid solution and black line — the exact (analytic) solution.



(b) Step 2. Since the maximal error multiplied by τ (here set to 20%) were lower than the error on any element, the algorithm halved all four elements after step 1.

Figure 3.2



(c) Step 3. The extreme left and right elements did not get refined after the step 2.



(d) Step 4

Chapter 4

Project documentation

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4.1 Some clever stuff

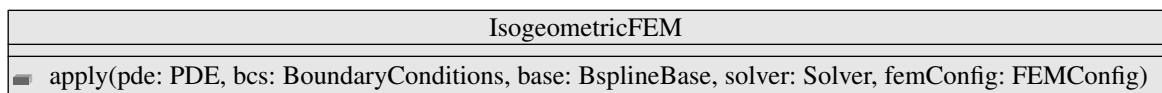
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4.2 API components overview

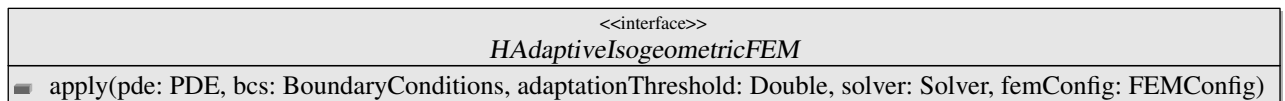
Nice UML no. 1...

Figure 4.1: IsogeometricFEM class



Nice UML no. 2...

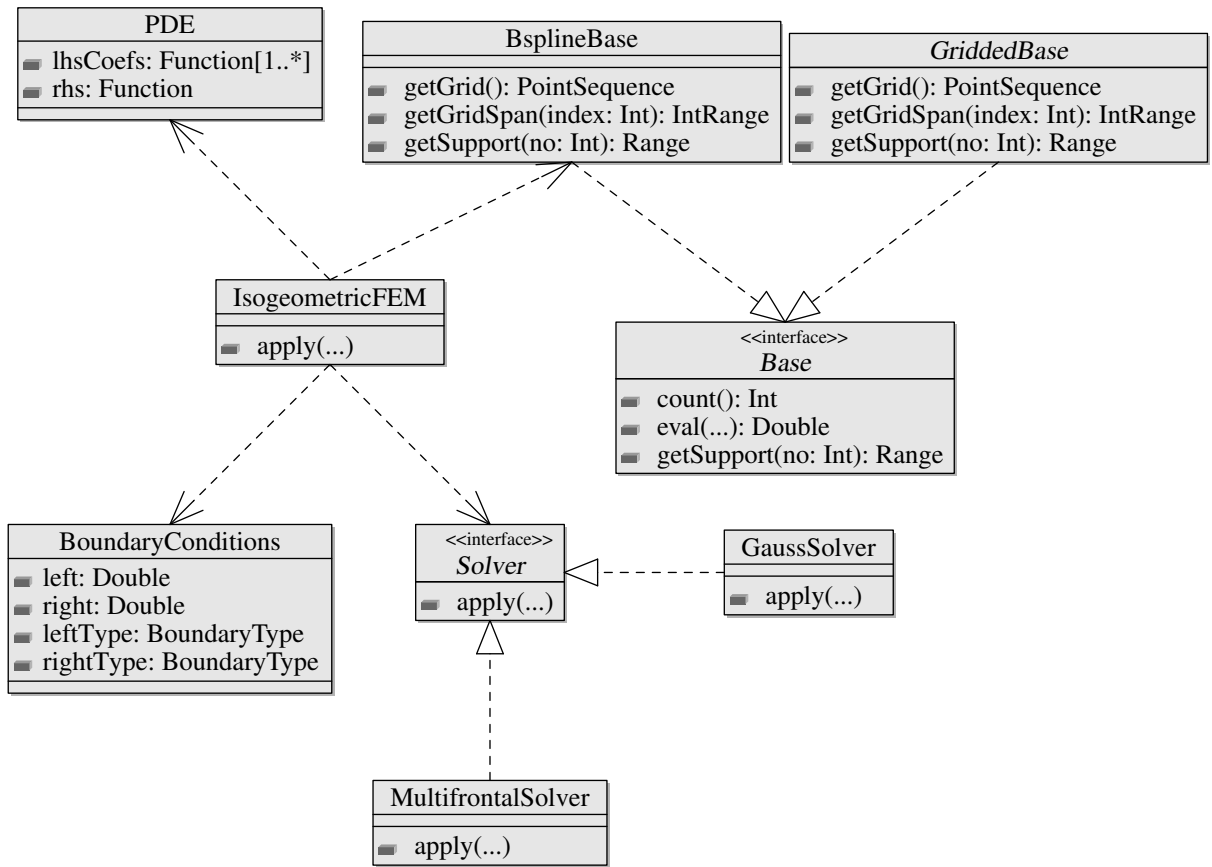
Figure 4.2: HAdaptiveIsogeometricFEM interface



4.3 Detailed API specification and class diagrams

And another large UML...

Figure 4.3: The overall class diagram



Chapter 5

Evaluation of the results

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5.1 e.g. Convergence analysis

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5.2 e.g. Complexity analysis

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5.3 e.g. Flood simulation results

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Chapter 6

Conclusions and future works

6.1 Achieved goals and observations

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6.2 Areas for development

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List of Algorithms

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Bibliography

- [1] Babuška I., Guo B.: The hp-version of the finite element method, Part I: The basic approximation results. In: *Computational Mechanics*, pp. 21–41, 1986.
- [2] Babuška I., Guo B.: The hp-version of the finite element method, Part II: General results and applications. In: *Computational Mechanics*, pp. 203–220, 1986.
- [3] Cottrell J., Hughes T.J.R., Bazilevs Y.: *Isogeometric Analysis: Toward Integration of CAD and FEA*. Wiley Publishing, 1st ed., 2009. ISBN 0470748737, 9780470748732.
- [4] Demkowicz L.: *Computing with hp adaptive finite element methods. Part I. Elliptic and Maxwell problems with applications*. Taylor & Francis, CRC Press, 2006.
- [5] Krawezik G., Poole G.: Accelerating the ANSYS Direct Sparse Solver with GPUs. In: *Symposium on Application Accelerators in High Performance Computing, SAAHPC*. 2009.
- [6] Lucas R.F., Wagenbreth G., Davis D.M., Grimes R.: Multifrontal Computations on GPUs and Their Multi-core Hosts. In: *VECPAR, Lecture Notes in Computer Science*, vol. 6449, pp. 71–82. Springer, 2010.
- [7] Woźniak M., Kuźnik K., Paszyński M., Calo V., Pardo D.: Computational cost estimates for parallel shared memory isogeometric multi-frontal solvers. In: *Computers and Mathematics with Applications*, vol. 67(10), pp. 1864–1883, 2014.
- [8] Yu C.D., Wang W., Pierce D.: A CPU-GPU Hybrid Approach for the Unsymmetric Multifrontal Method. In: *Parallel Comput.*, vol. 37(12), pp. 759–770, 2011.