

fn sample_geometric_buffer

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This document proves soundness of `sample_geometric_buffer` in `mod.rs` at commit `f5bb719` (outdated¹).

1 Hoare Triple

Preconditions

None

Pseudocode

```
1 def sample_geometric_buffer(buffer_len: usize, constant_time: bool) -> Optional[uint]:
2
3     if constant_time:
4         buf = bytearray(buffer_len)
5         fill_bytes(buf) # mutates in-place
6         ret = None
7         for i in range(buffer_len):
8             # find first nonzero event
9             if buf[i] > 0:
10                # compute index of first nonzero bit buffer
11                cand = 8 * i + buf[i].leading_zeros()
12                ret = cand if ret is None else min(ret, cand)
13        return ret
14    else:
15        for i in range(buffer_len):
16            buf = bytearray(1)
17            fill_bytes(buf) # mutates in-place
18            if buf[0] > 0:
19                return 8 * i + buf[0].leading_zeros()
20
21    return None
```

Postcondition

For any setting of the input arguments, `sample_geometric_buffer` either raises an exception if there is insufficient system entropy, or returns `sample` where `sample` is drawn from a discrete distribution.

`sample` is either `geo` where `geo` is a sample from the $Geometric(p = 0.5)$ distribution, and is less than $buffer_len * 8$, or `None` with probability $2^{-buffer_len * 8}$.

Proof. `sample_geometric_buffer` uses `fill_bytes` as a subroutine to generate a buffer of `buffer_len` bytes. For each bit b in the buffer it follows that $\Pr[b = 1] = \frac{1}{2}$ and $\Pr[b = 0] = \frac{1}{2}$. If there is some bit in the

¹See new changes with `git diff f5bb719..ab34e69 rust/src/traits/samplers/geometric/mod.rs`

buffer equal to 1, the position of the *first* such bit is a zero-indexed draw from the Geometric distribution $Geom(p)$ with $p = 0.5$, by definition of a Geometric random variable. If the buffer is zero, the function returns **None**. □