

DAS2021-Group-19

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1 Introduction

1.1 Background Information

Dataset 19 comes from the Dallas animal shelter. You will have access to the following variables, recorded by animal admission:

- **Animal_type** – The type of animal admitted to the shelter
- **Month** – Month the animal was admitted, recorded numerically with January=1
- **Year** – Year the animal was admitted to the shelter.
- **Intake_type** – Reason for the animal being admitted to the shelter
- **Outcome_type** – Final outcome for the admitted animal
- **Chip_Status** – Did the animal have a microchip with owner information?
- **Time_at_Shelter** – Days spent at the shelter between being admitted and the final outcome.

1.2 Question of Interest

Imagine you have been asked by the shelter management to investigate the following questions of interest:

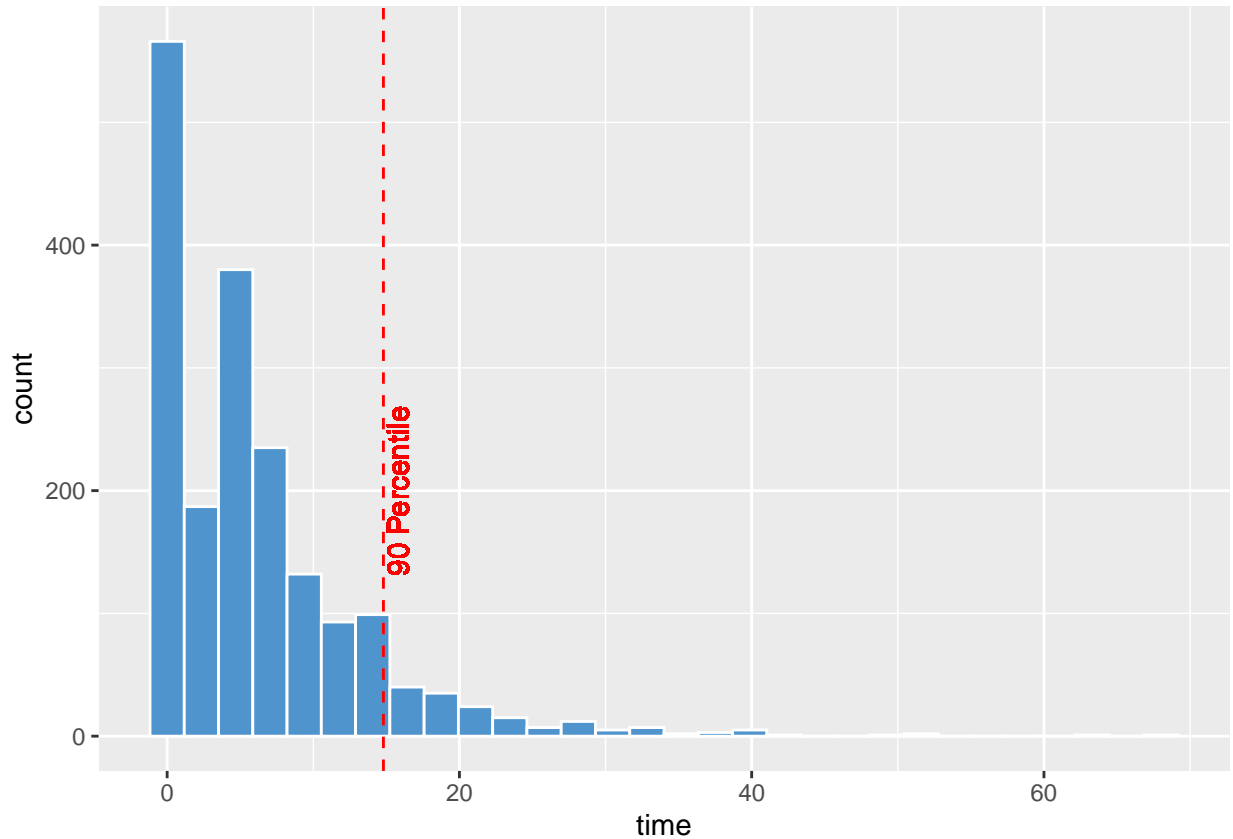
- Which factors influence the number of days an animal spends in the shelter before their final outcome is decided?

You should conduct an analysis to answer your question using a Generalised Linear Model (GLM). Following your analyses, you should then summarise your results in the form of a presentation.

2 Exploratory Data Analysis

2.1 Tidying Data

```
Rows: 1,853
Columns: 7
$ animal_type    <chr> "CAT", "DOG", "DOG", "DOG", "DOG", "CAT", "DOG", "CAT"~
$ month          <int> 11, 12, 5, 8, 10, 5, 12, 10, 4, 4, 6, 6, 6, 6, 5, 9, 3~
$ year           <int> 2016, 2016, 2017, 2017, 2016, 2017, 2016, 2016, 2017, ~
$ intake_type    <chr> "STRAY", "OWNER SURRENDER", "OWNER SURRENDER", "STRAY"~
$ outcome_type   <chr> "ADOPTION", "ADOPTION", "EUTHANIZED", "RETURNED TO OWN~
$ chip_status    <chr> "SCAN NO CHIP", "SCAN NO CHIP", "SCAN CHIP", "SCAN NO ~
$ time_at_shelter <int> 21, 2, 2, 0, 0, 0, 1, 6, 5, 21, 7, 0, 22, 8, 4, 10, 2,~
```



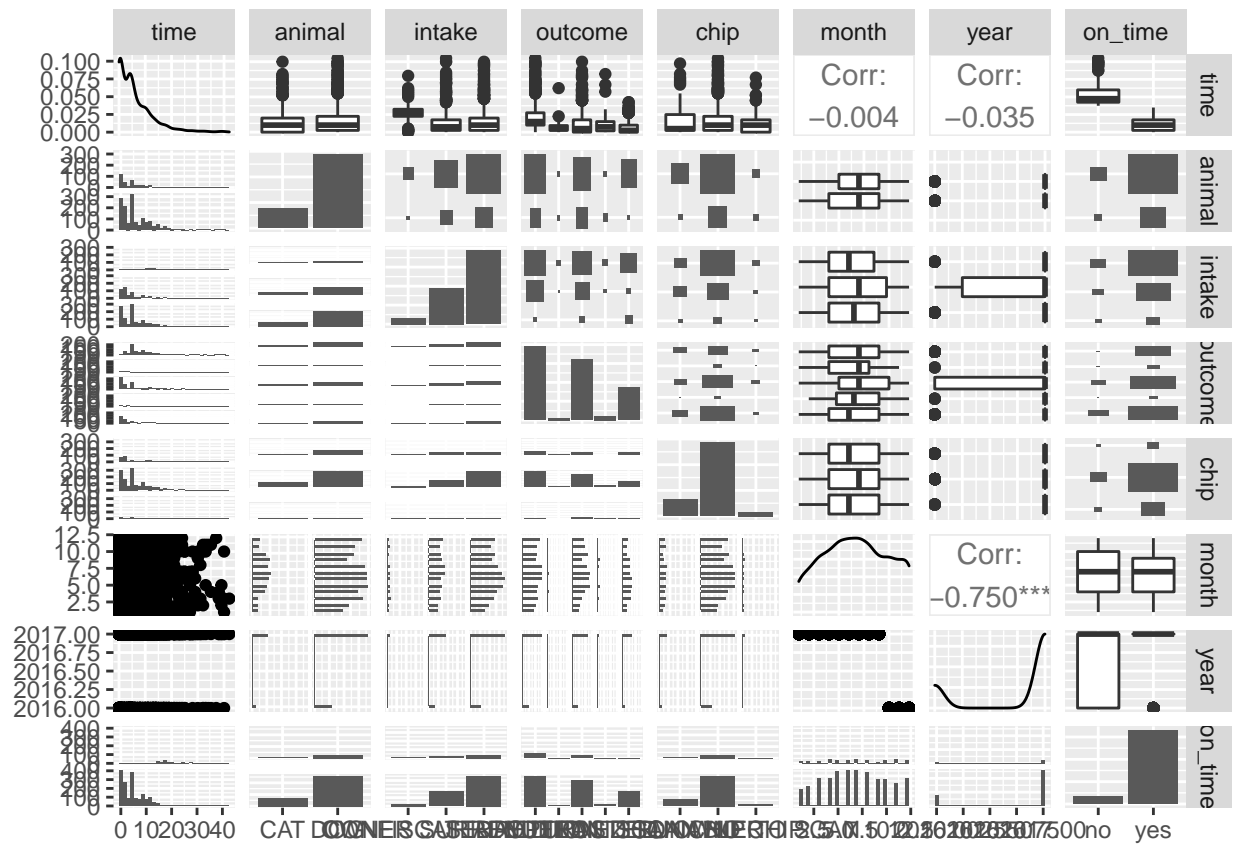
	mean	s.d	min	Q1	med	Q3	max
1	6.132758	7.130583	0	1	4	9	68

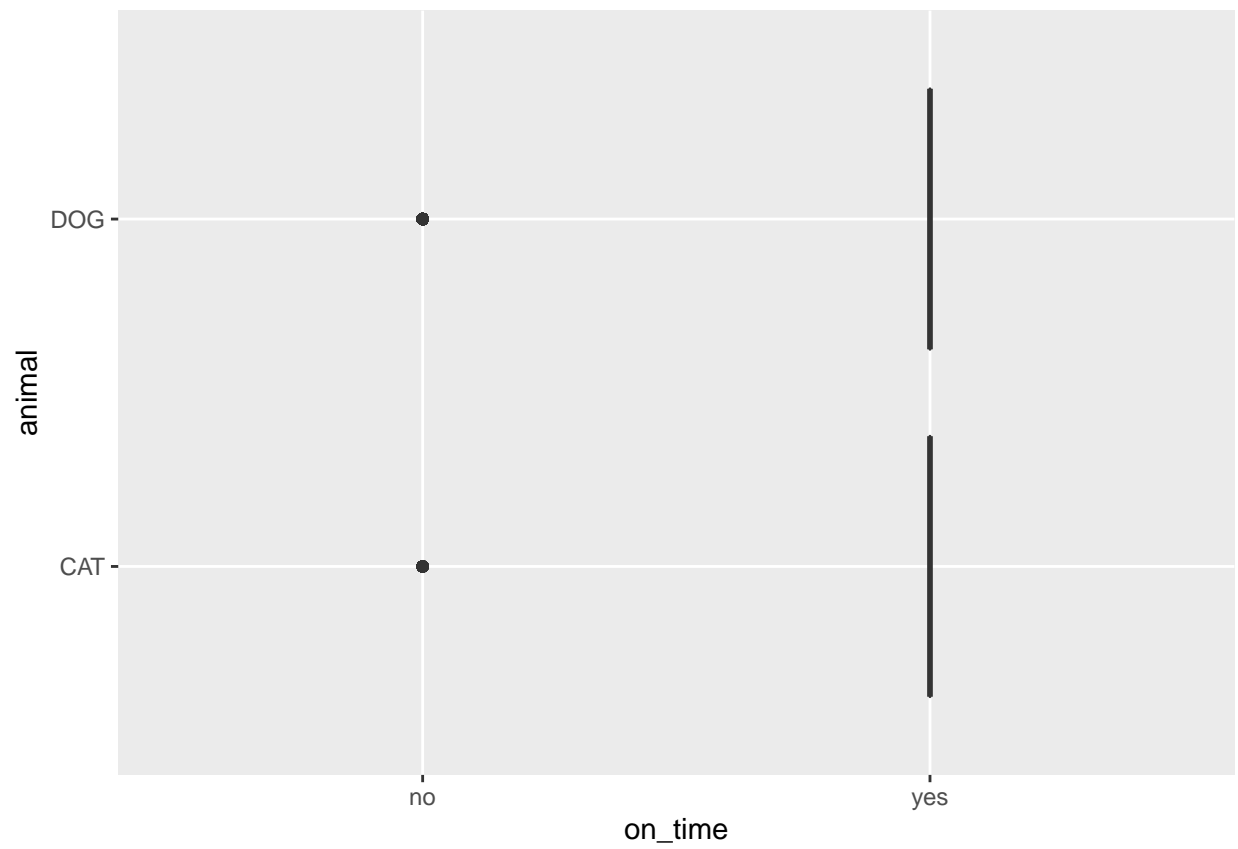
The time spent in the shelter is skewed - most animals (90%) stay no longer than two weeks and very few after three. The majority seem leave the shelter within one week. We could speculate that there are factors (possibly categorical variables) that contribute to the time at the shelter being shorter, and therefore if these factors do not occur then the animal stays longer.

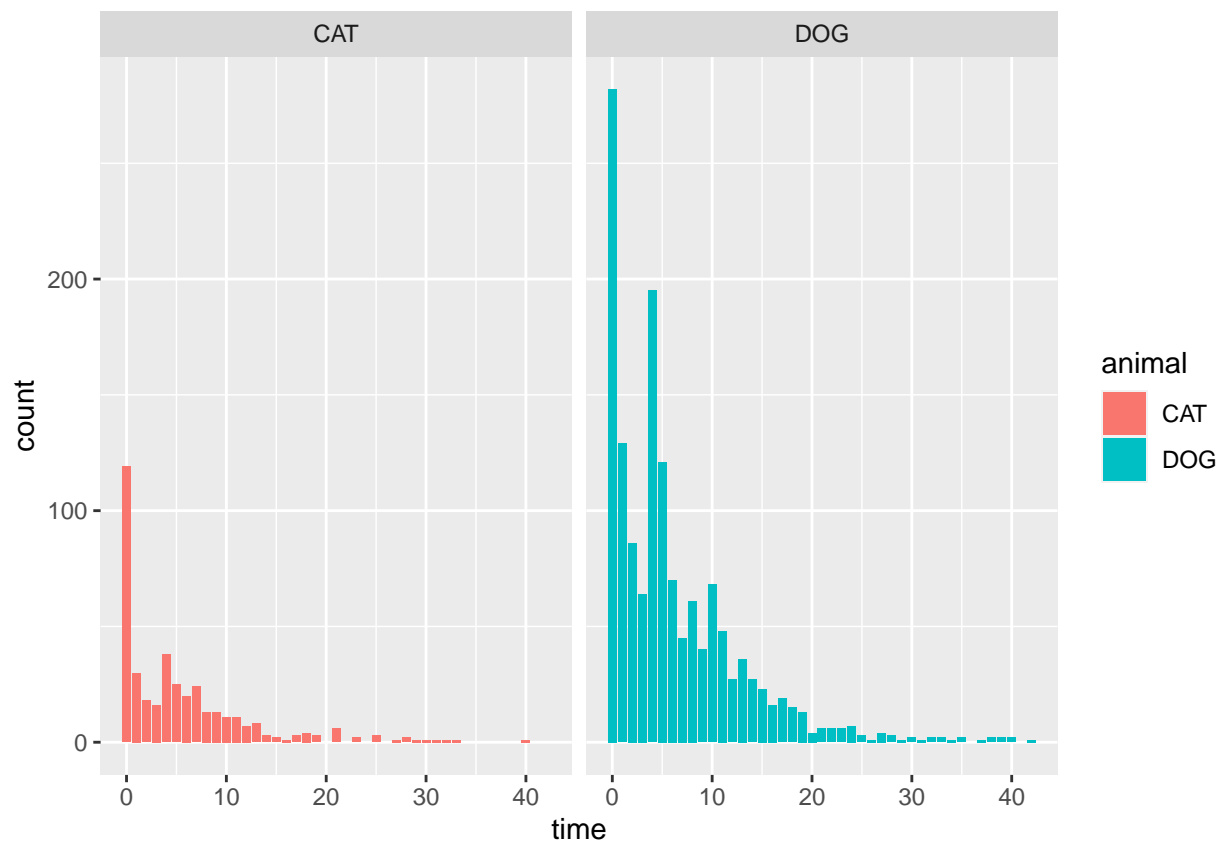
We see that 90% of animals' outcome is decided by 14.8 days at the shelter - this could be our research: what makes animals stay beyond 14 days?

If we consider staying longer than 14 days as a failure, then we can reduce our problem to a binary GLM.

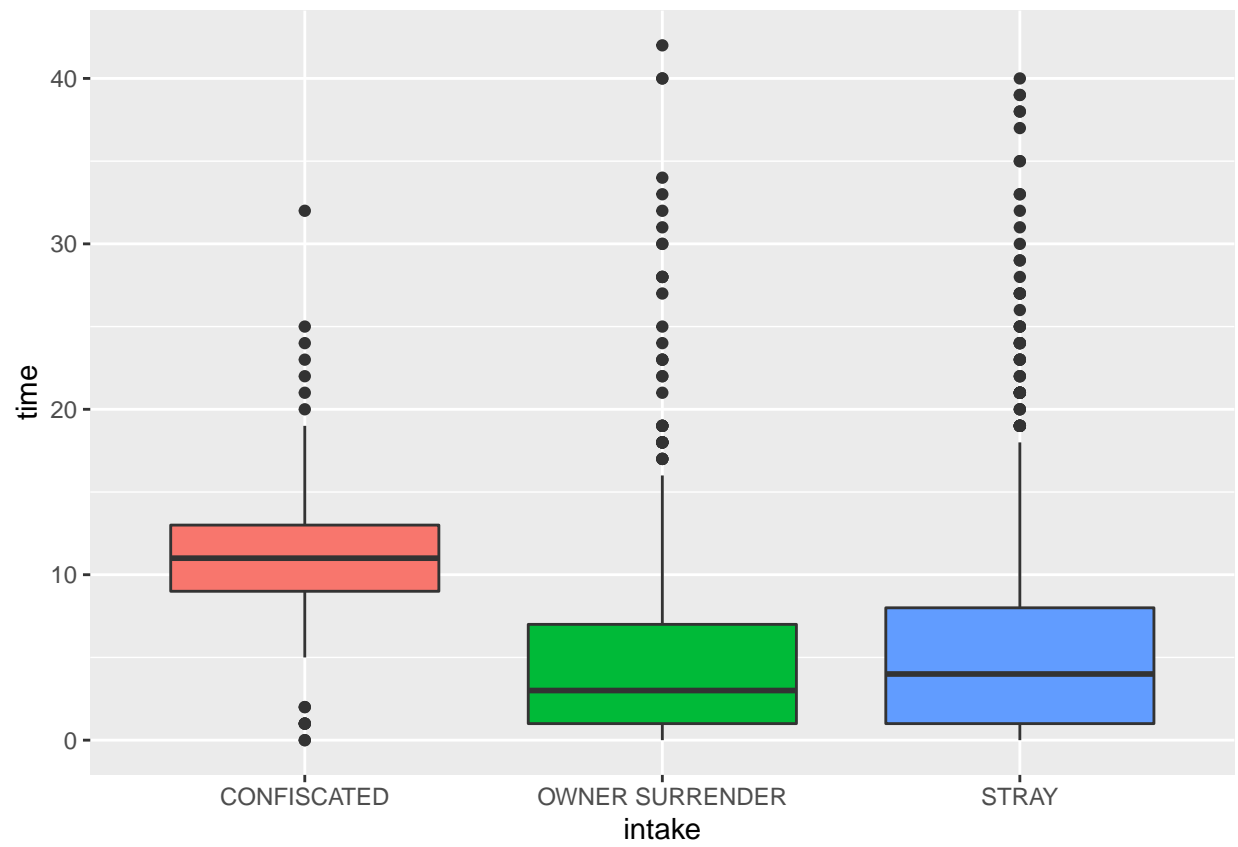
There are only two birds in the data and 13 wildlife. Therefore the impact these animal types will have on the other animal types will be minimal as they do not even contribute to 0.01% of the data, so they can be removed.

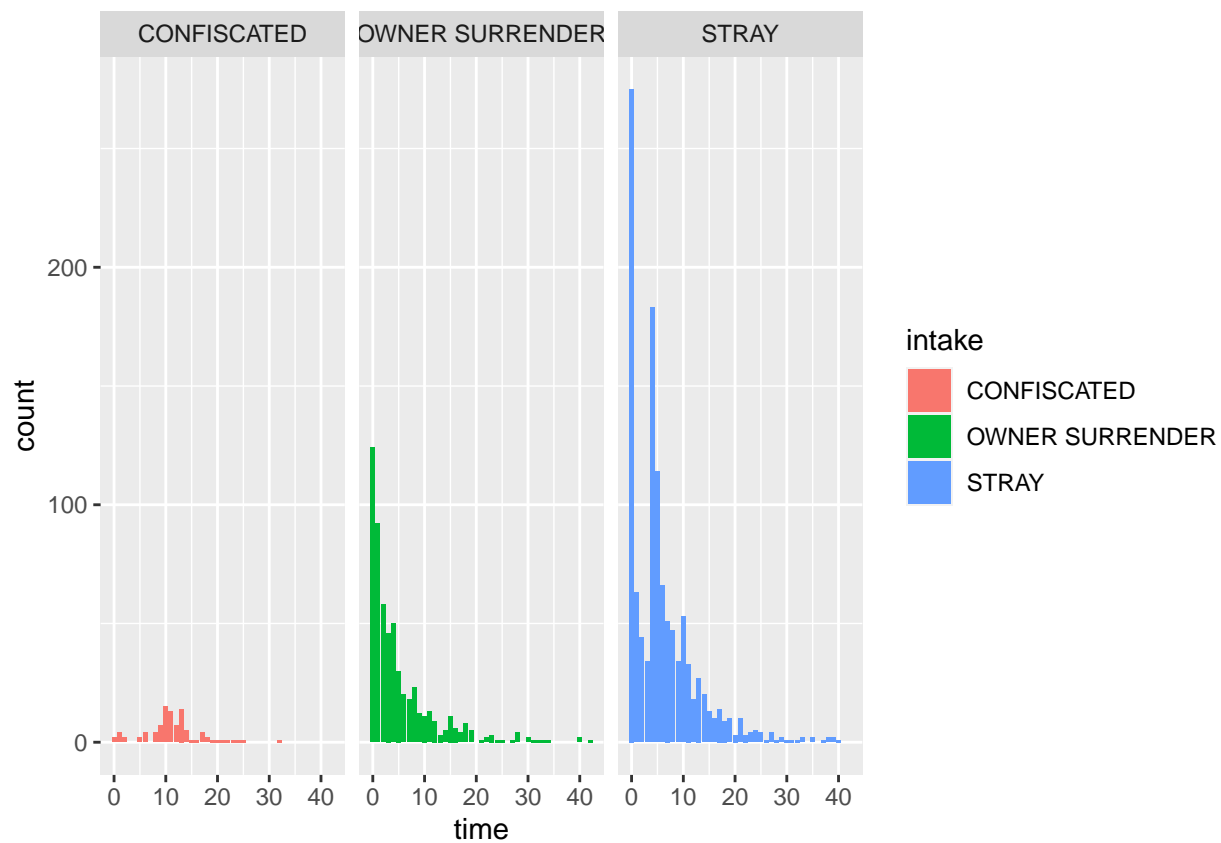




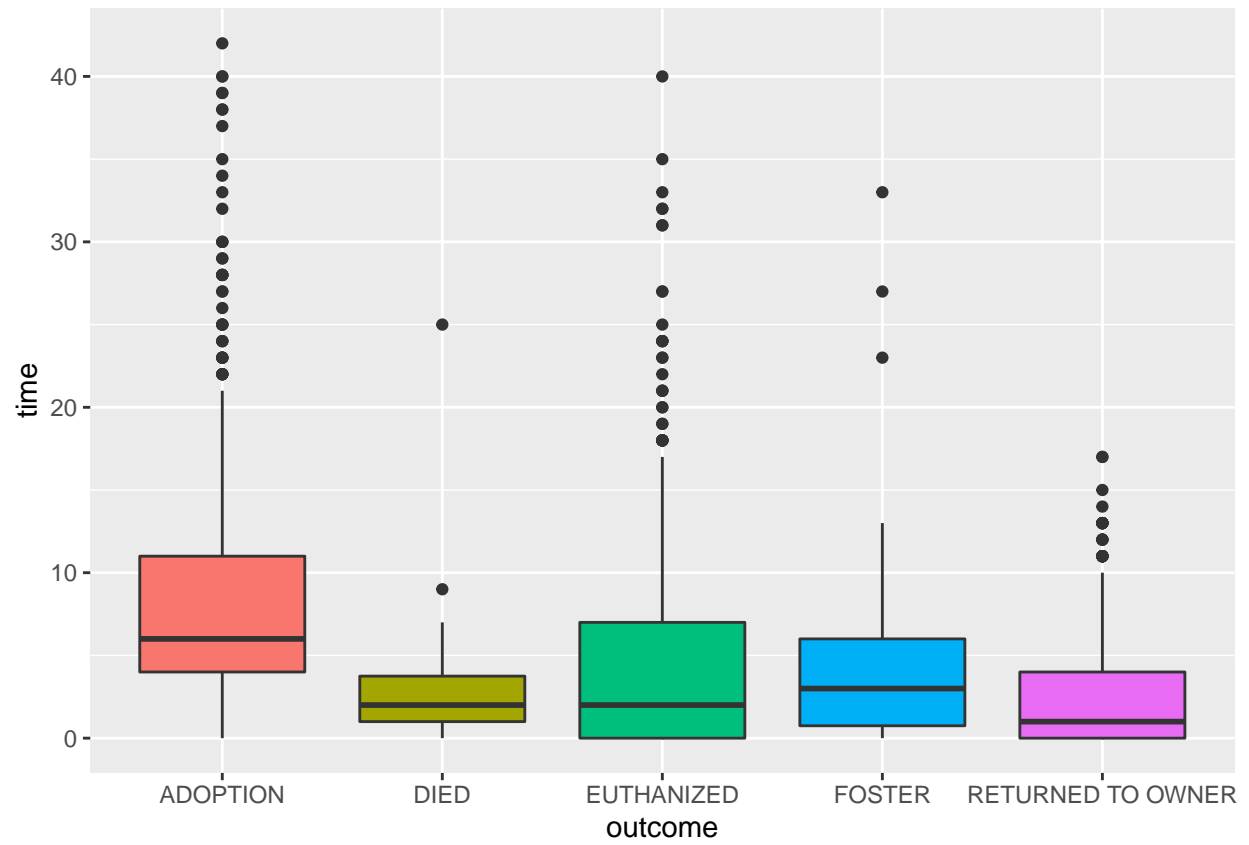


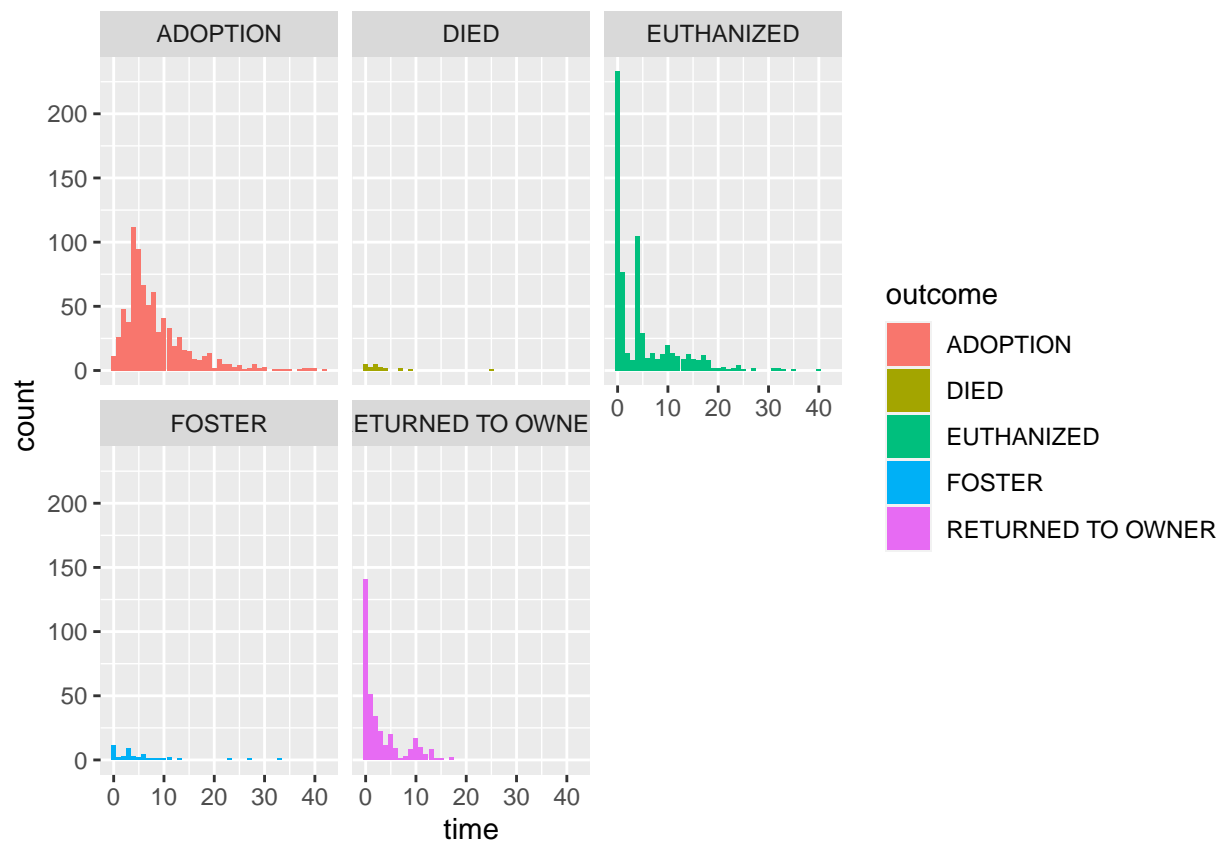
It would seem that there is a slight difference in how long dogs and cats spend at the shelter by looking at the histograms, but from the boxplots we can see that both animals have very similar distributions: the medians are in similar places, their ranges are the similar, both have long tails (skewed right) and lots of outliers. It could be possible that this variable will be omitted from the final model.



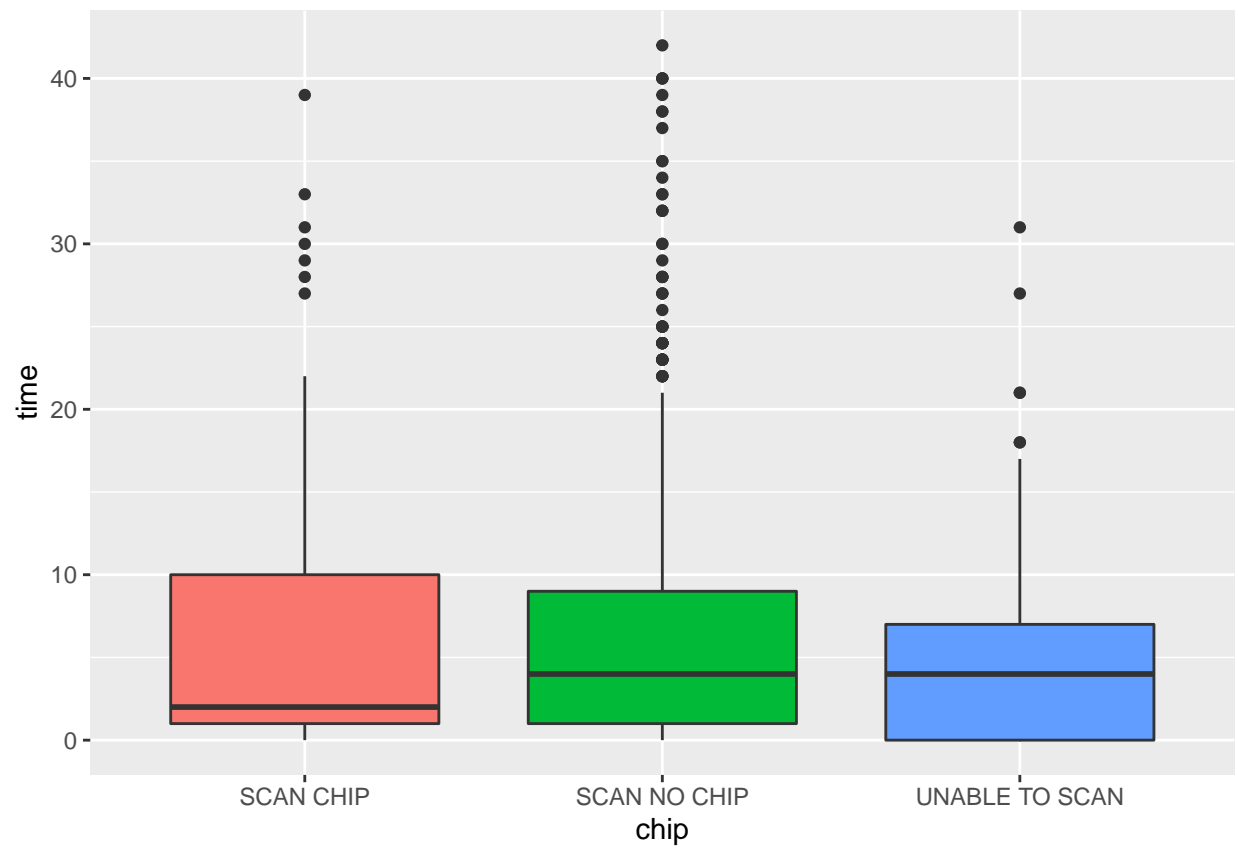


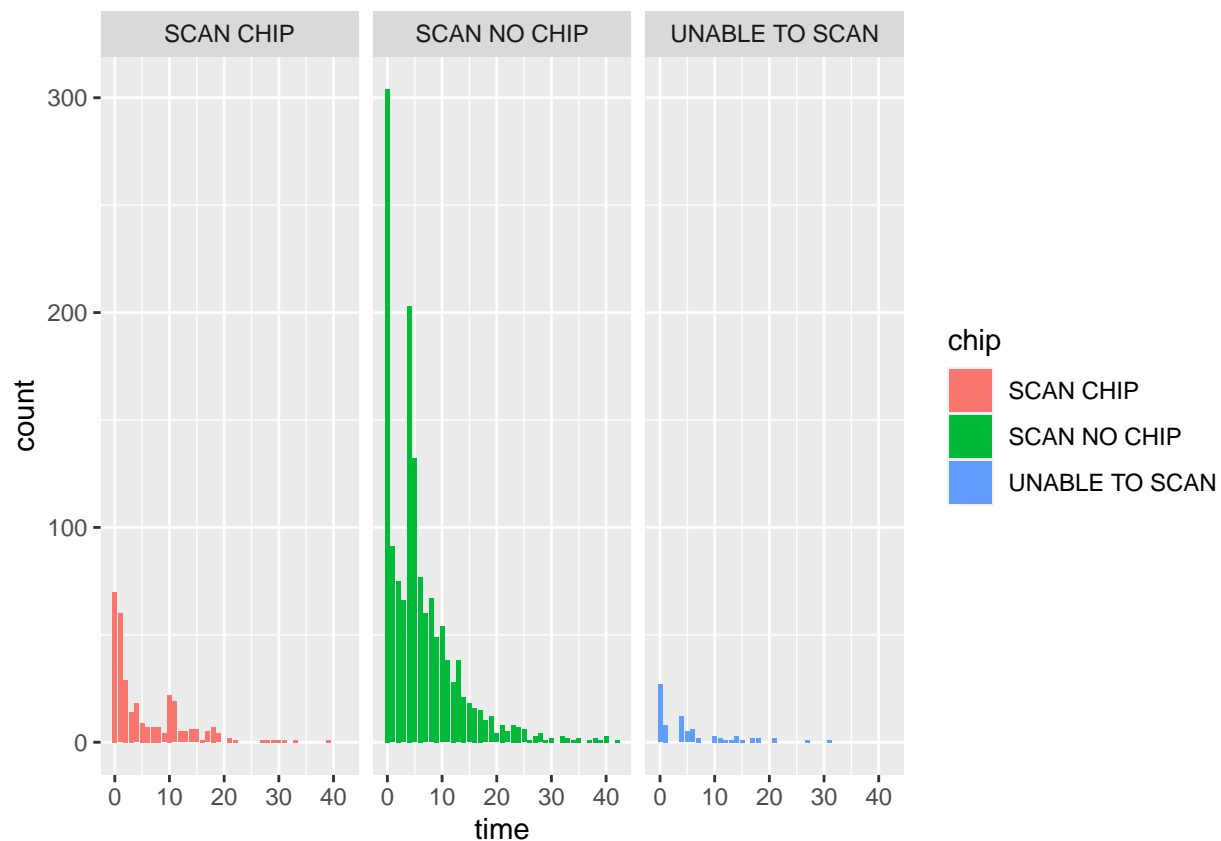
Confiscated animals seems to stay longer at the shelter than those animals that are surrendered by their owner or found as strays. There is a clear separation of one group from the other two. Strays seem to stay slightly longer than animals that are surrendered.



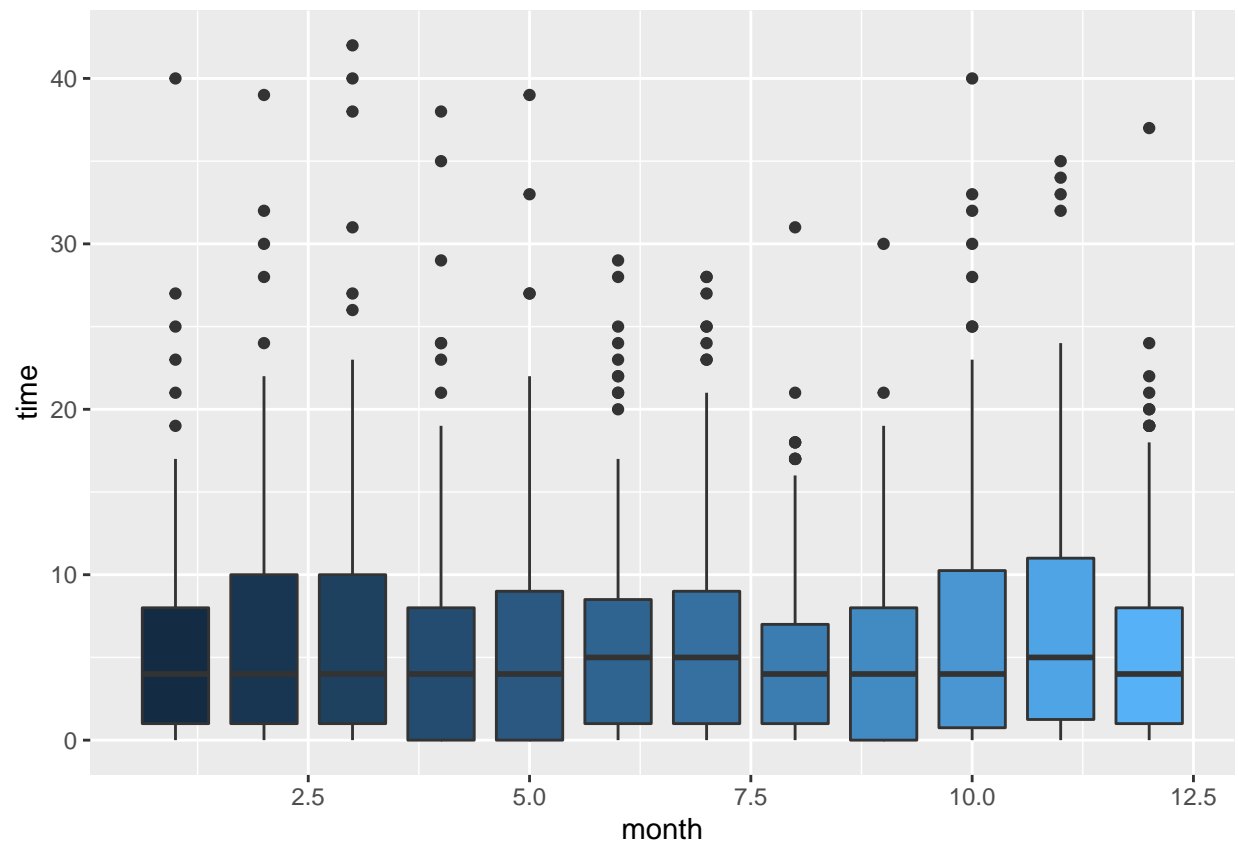


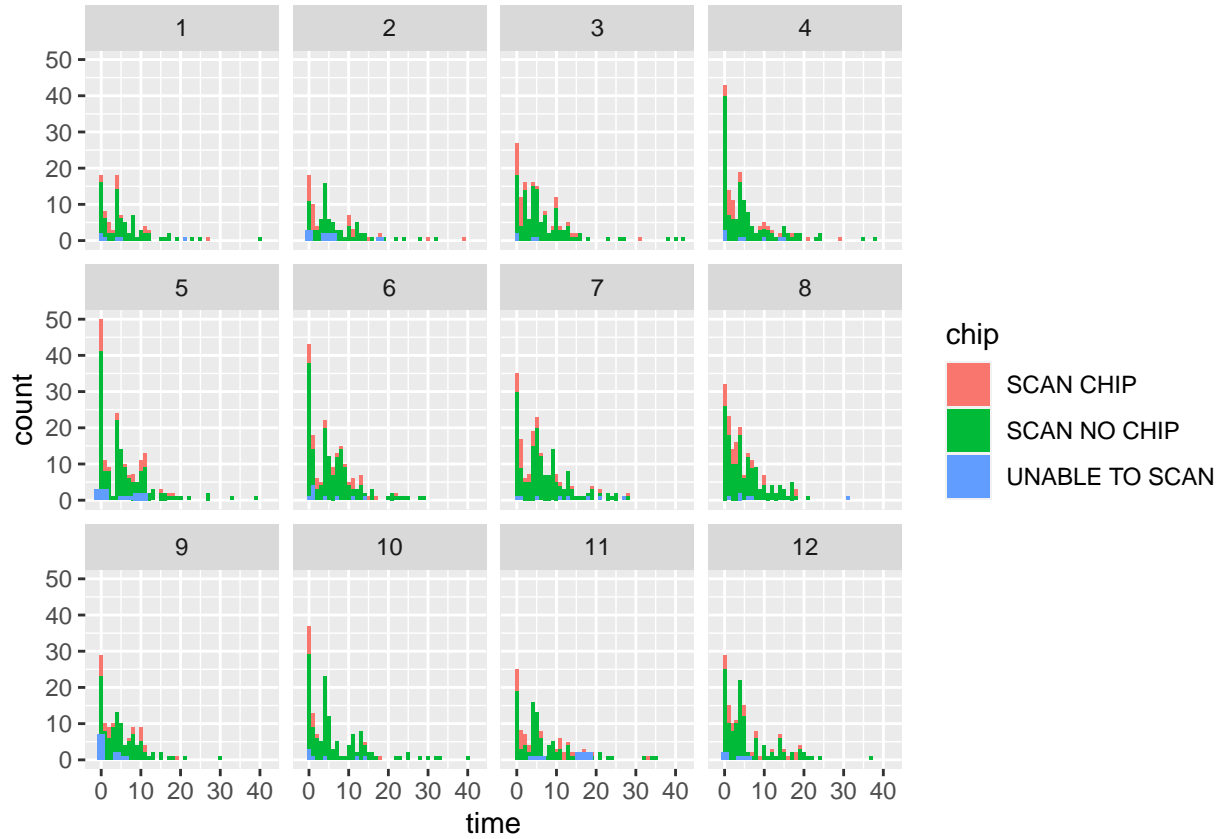
There is some variation across outcome - animals returned to owner or euthanized tend to spend short times at the shelter. Those that are adopted tend to be at the shelter for a slightly longer time and the distribution of this subgroup is more normally distributed. There is less data for died and fostered to make an assumption.



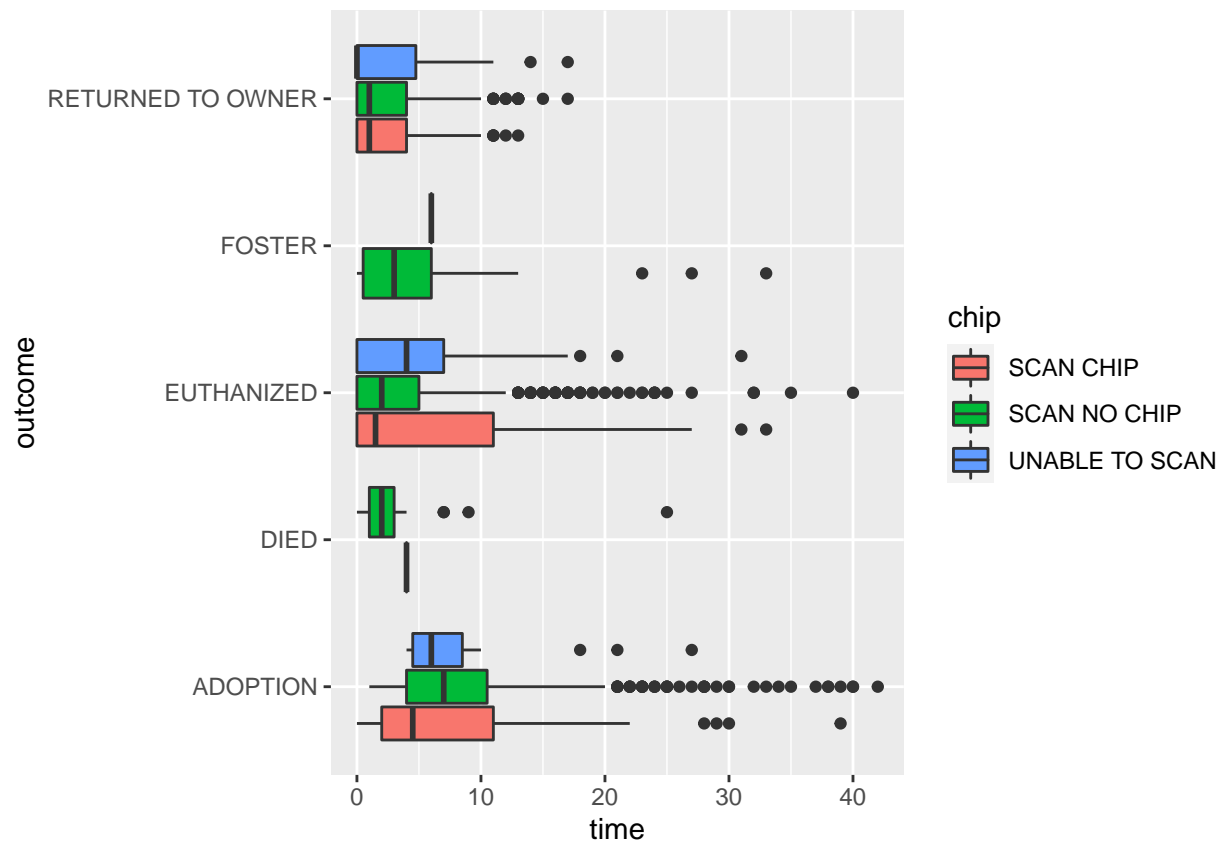


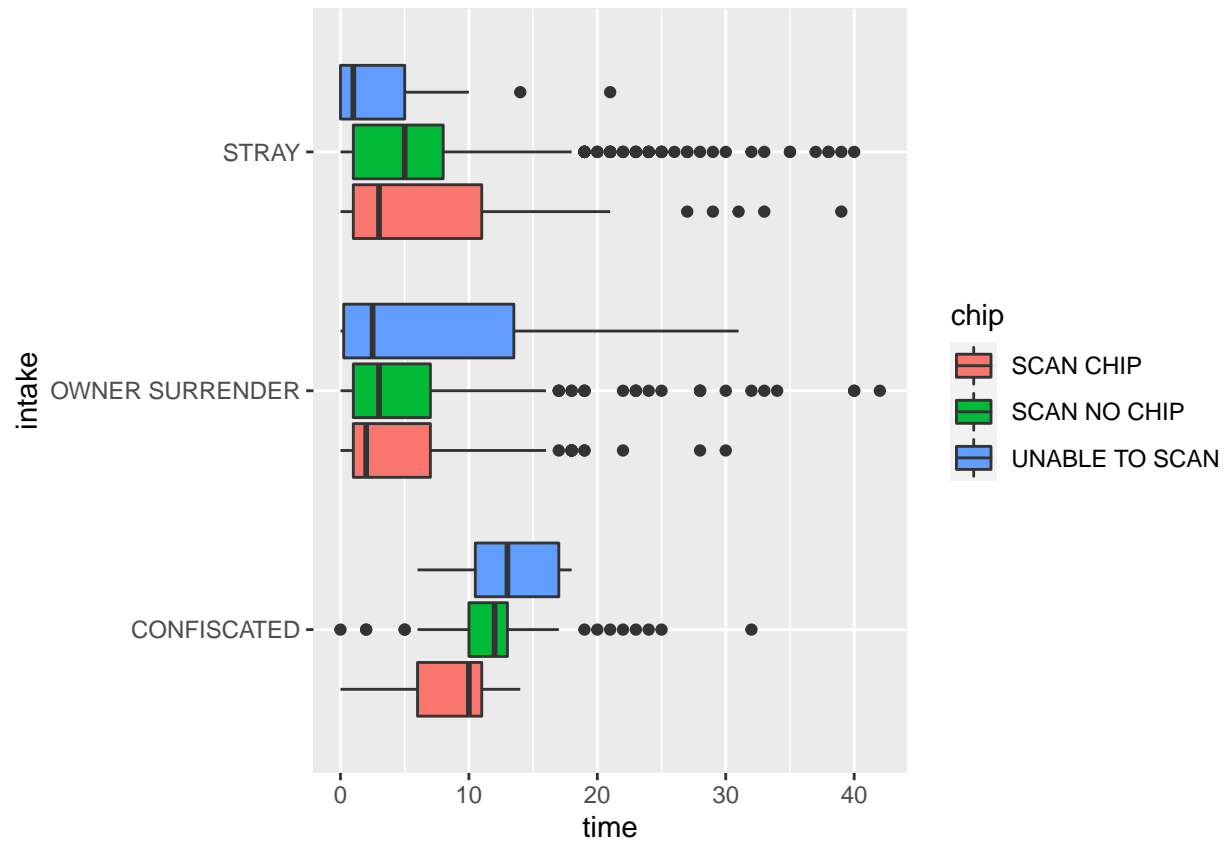
Again all the data is skewed to the right, meaning most types stay for a short period of time. However, it would seem that animals with a chip is a lot more skewed than those that are not. We could speculate that these animals are rescued early and if not then held onto for longer, thus this variable could be a good predictor if combined with outcome perhaps.

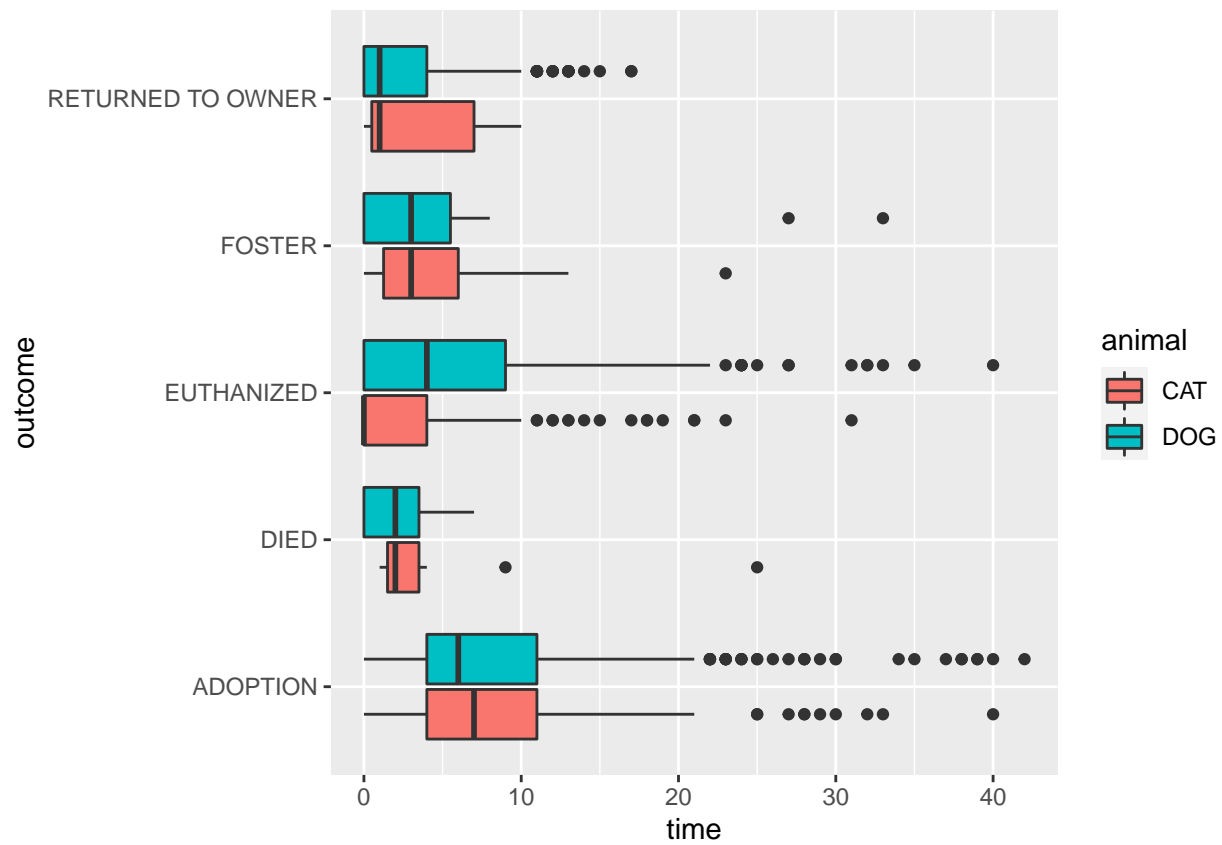


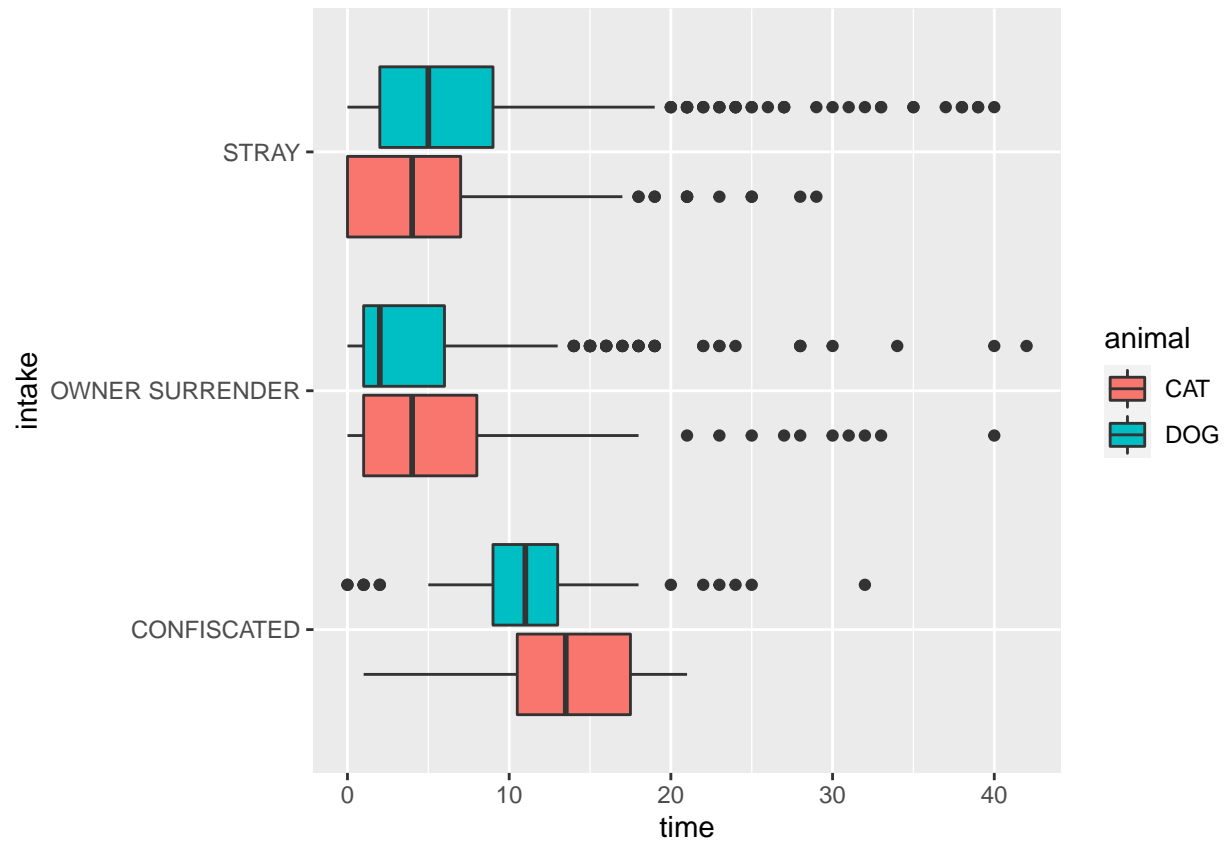


The distributions for month seem to all be similar. We do not envisage that this variable will have an impact on the time variable. Similarly the variable year, which only has 2 levels, may not be a good predictor of time. that means we could potentially have 4 categorical variables explaining one continuous variable - **possible loglinear model**.

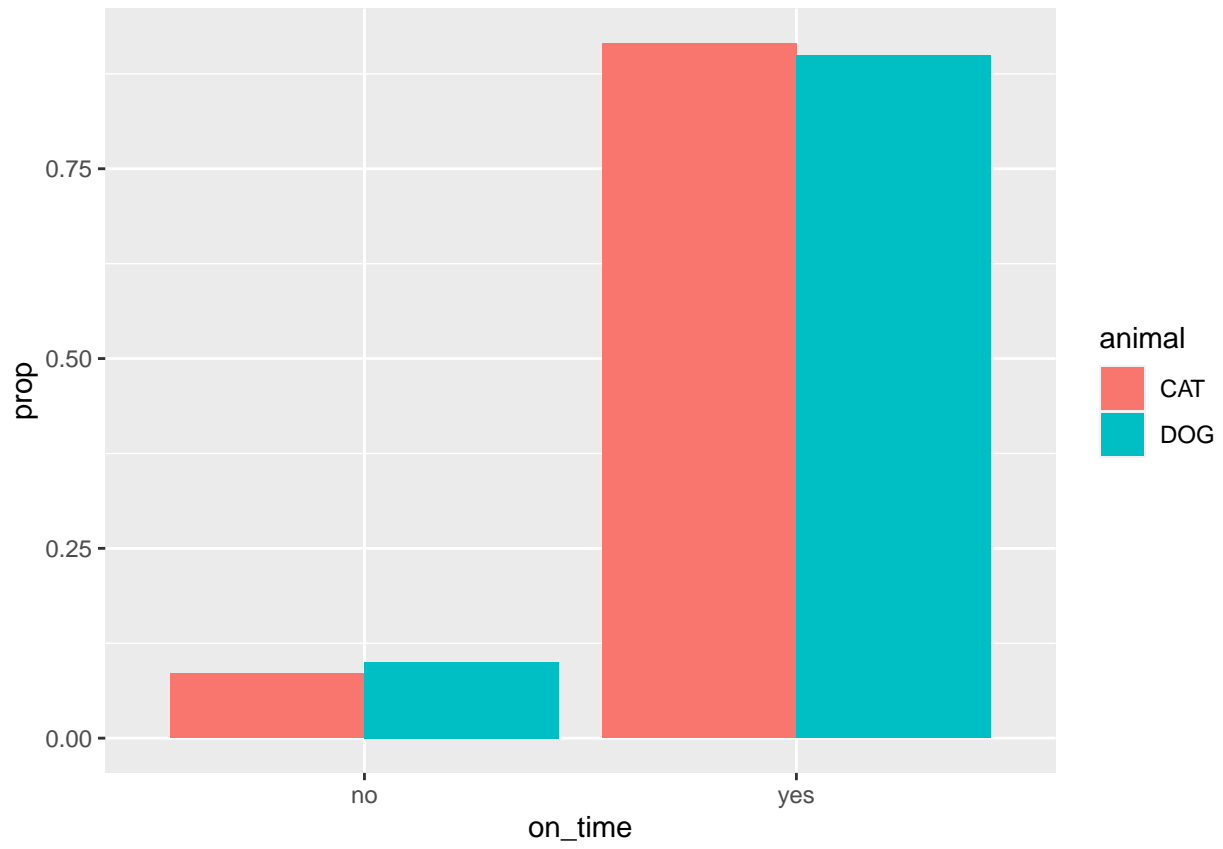


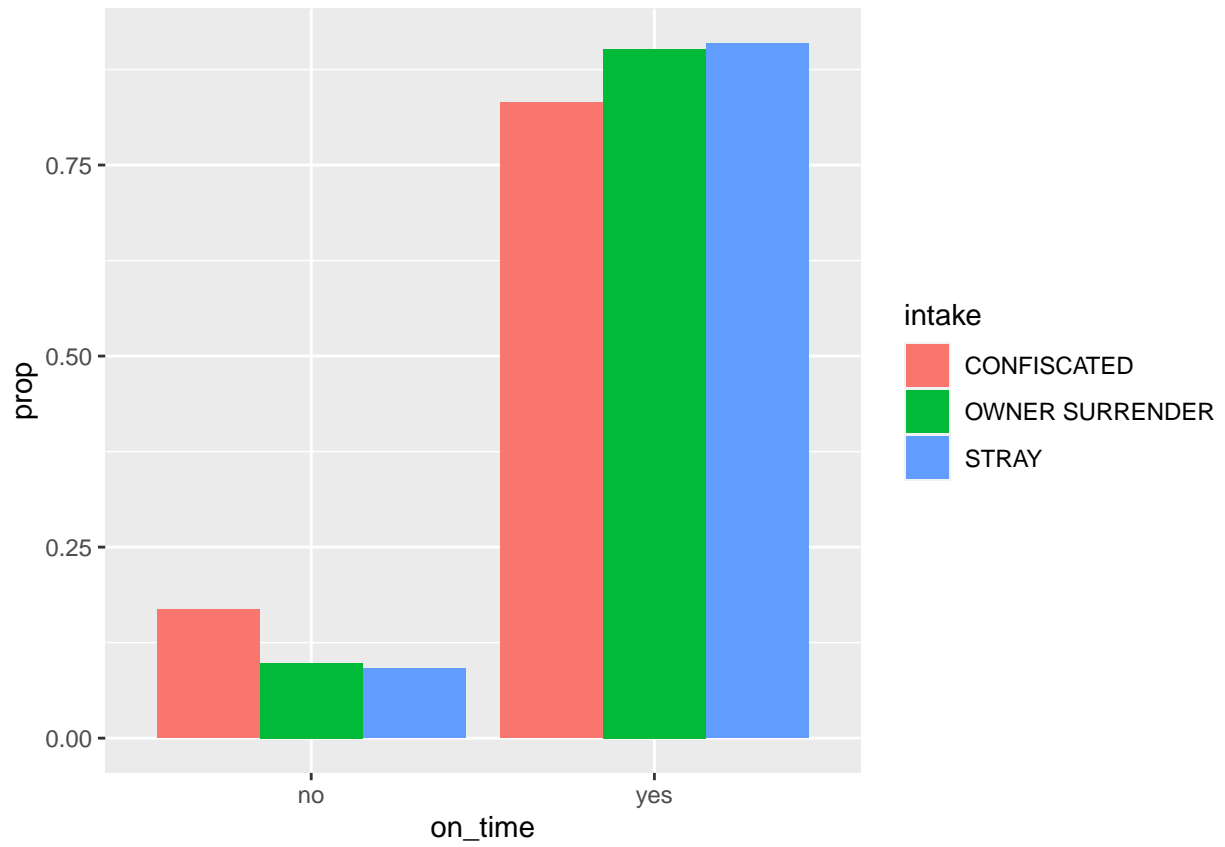


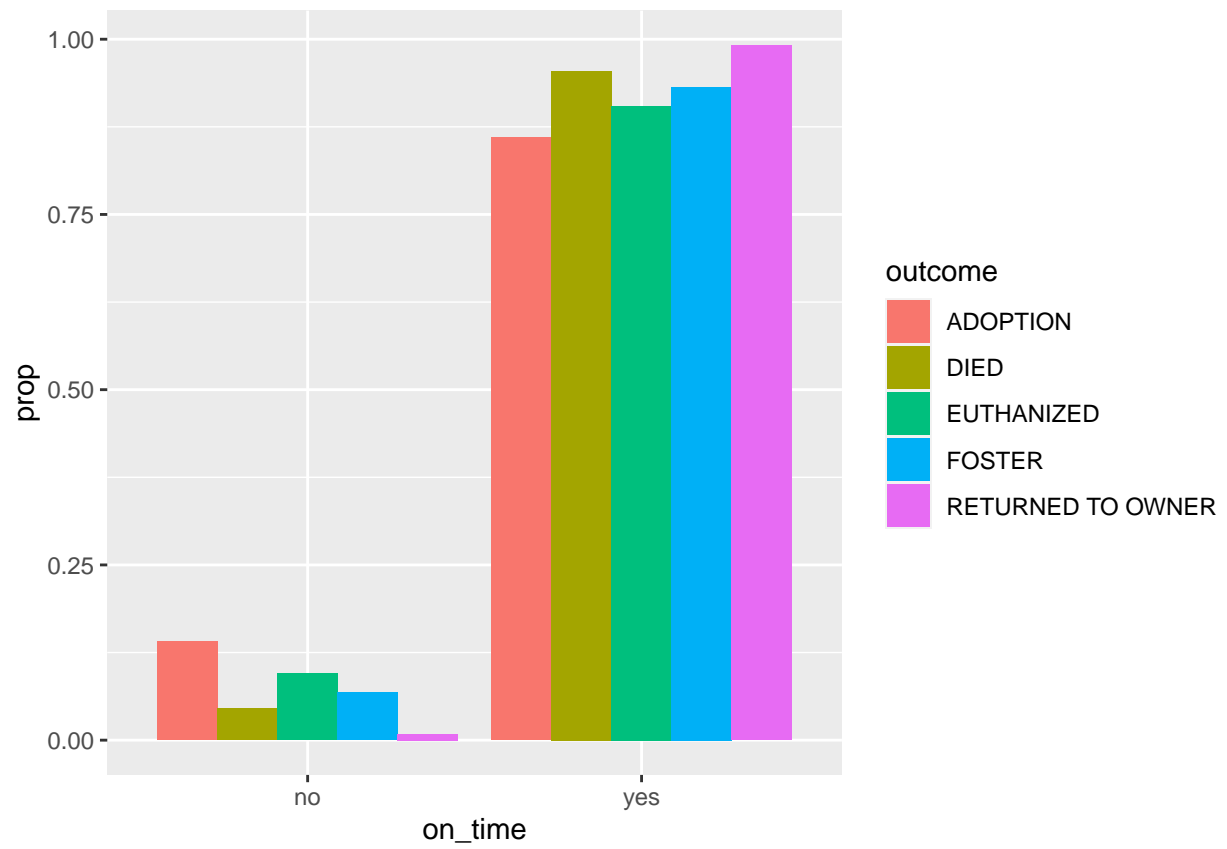


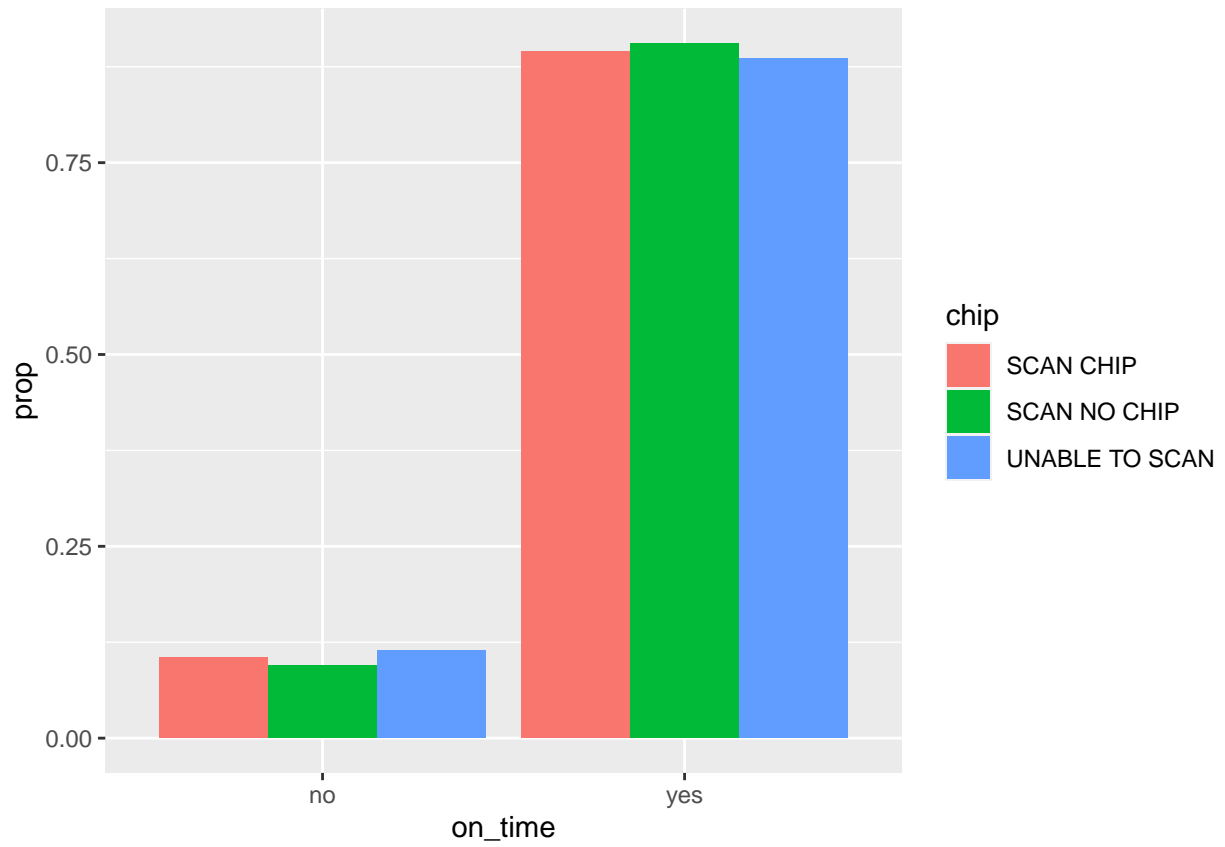


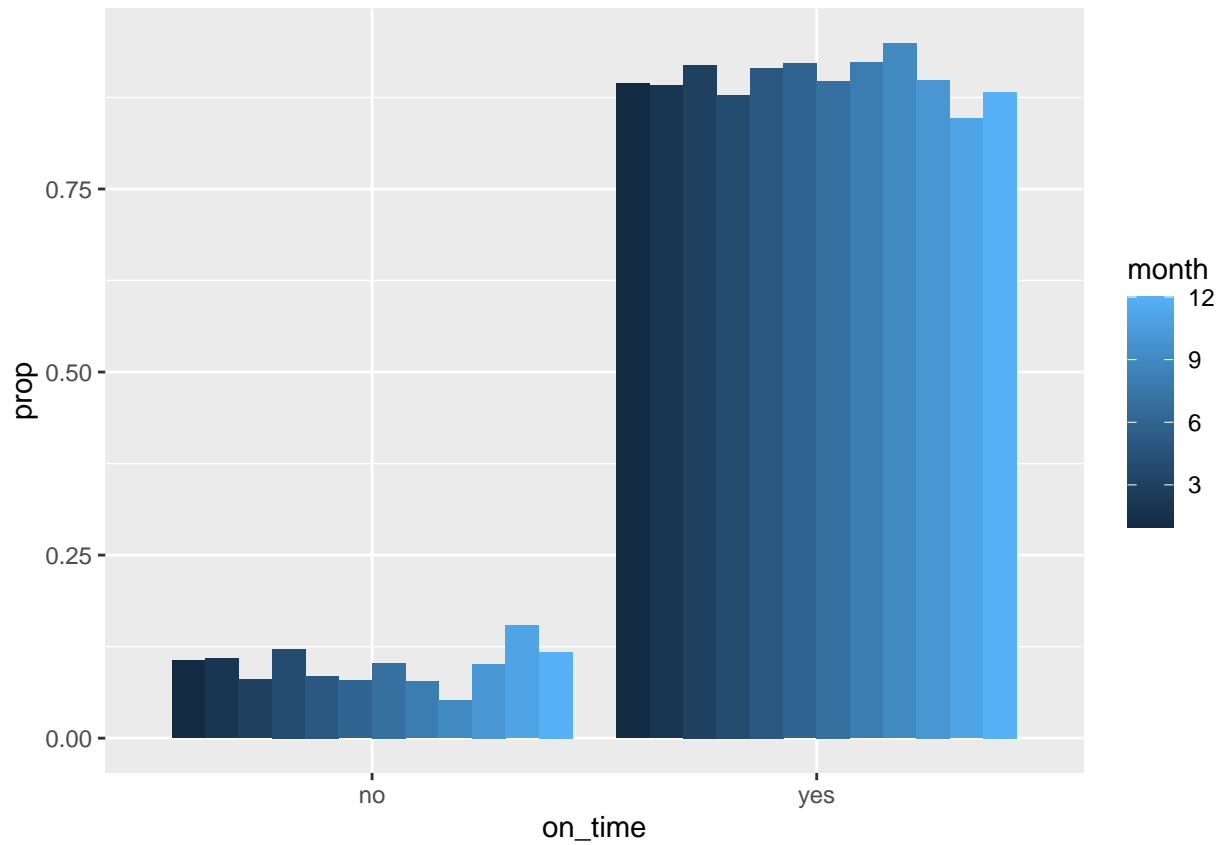
Looking at the above plots, we see some change in distributions across different combinations of categories.







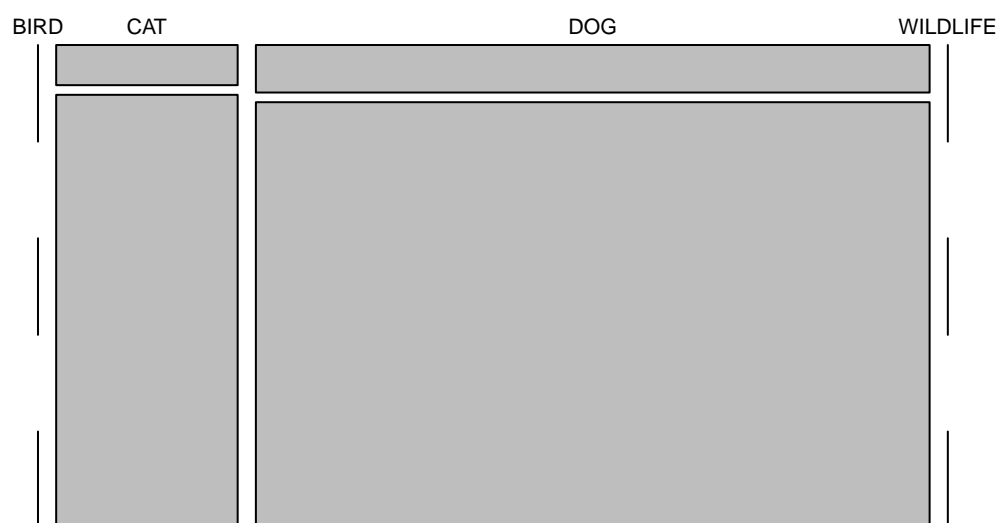




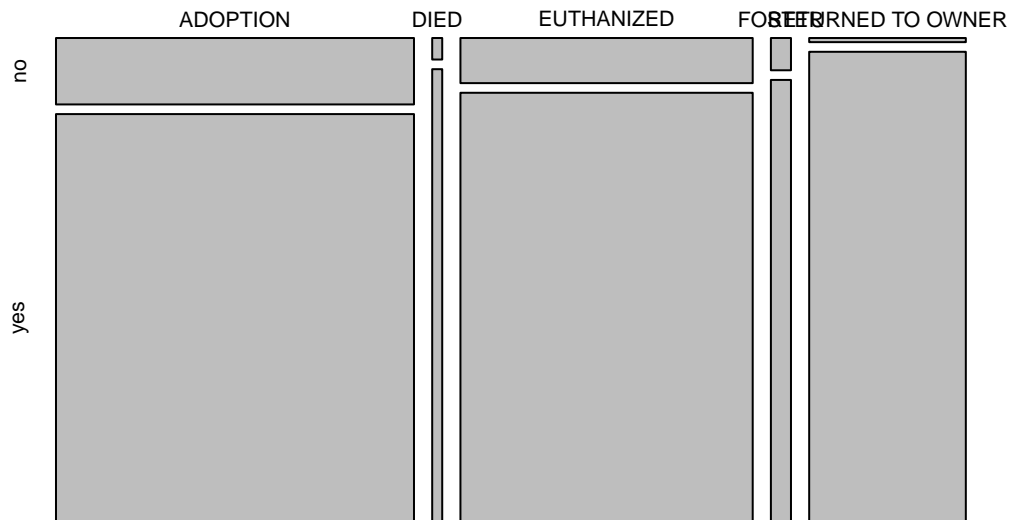
There does not seem to be much difference in proportions between the two types of animals. There is some difference in proportion between confiscated and the other levels of intake. There is some differences from one group to another in the variable outcome. There does not seem to be much differences in proportions for chip. For month, the proportions seem fairly even - cannot see any trend that could relate to seasonal activity.

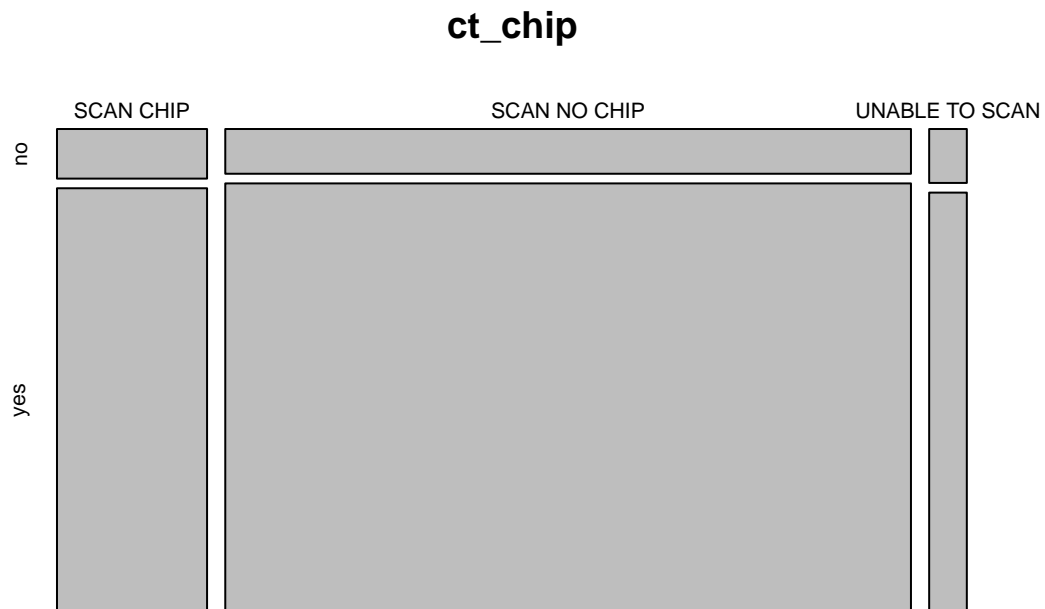
ct_int

CONFISCATED		OWNER SURRENDER	STRAY
no			
yes			

ct_anml

ct_outcome





Very little difference in proportions for yes/no across different levels of each categorical explanatory - maybe do not go for log-odds model.

3 Formal Data Analysis

3.1 Binomial models for on_time

Observations	1833
Dependent variable	on_time
Type	Generalized linear model
Family	binomial
Link	logit

$\chi^2(9)$	92.20
Pseudo-R ² (Cragg-Uhler)	0.10
Pseudo-R ² (McFadden)	0.08
AIC	1096.09
BIC	1151.23

BINOMIAL MODEL: From the exploratory analysis, it seemed fitting to try models based on intake and/or outcome, and then build up from there. Having fitted some models, model1 seems to be the best, which is simply intake as the only explanatory variable for the log-odds.

	Est.	S.E.	z val.	p
(Intercept)	0.24	0.45	0.54	0.59
animalDOG	-0.31	0.21	-1.44	0.15
intakeOWNER SURRENDER	1.69	0.35	4.80	0.00
intakeSTRAY	1.39	0.33	4.18	0.00
outcomeDIED	1.13	1.03	1.09	0.27
outcomeEUTHANIZED	0.53	0.18	2.99	0.00
outcomeFOSTER	0.59	0.62	0.96	0.34
outcomeRETURNED TO OWNER	3.51	0.61	5.77	0.00
chipSCAN NO CHIP	0.44	0.23	1.93	0.05
chipUNABLE TO SCAN	-0.02	0.44	-0.05	0.96

Standard errors: MLE

Observations	1833
Dependent variable	on_time
Type	Generalized linear model
Family	binomial
Link	logit

$\chi^2(4)$	65.23
Pseudo-R ² (Cragg-Uhler)	0.07
Pseudo-R ² (McFadden)	0.06
AIC	1113.07
BIC	1140.63

	Est.	S.E.	z val.	p
(Intercept)	1.81	0.10	17.63	0.00
outcomeDIED	1.23	1.03	1.20	0.23
outcomeEUTHANIZED	0.44	0.17	2.58	0.01
outcomeFOSTER	0.80	0.61	1.32	0.19
outcomeRETURNED TO OWNER	2.92	0.59	4.95	0.00

Standard errors: MLE

Observations	1833
Dependent variable	on_time
Type	Generalized linear model
Family	binomial
Link	logit

$\chi^2(2)$	5.18
Pseudo-R ² (Cragg-Uhler)	0.01
Pseudo-R ² (McFadden)	0.00
AIC	1169.11
BIC	1185.65

3.2 Poisson models for time

Call:

	Est.	S.E.	z val.	p
(Intercept)	1.60	0.27	5.82	0.00
intakeOWNER SURRENDER	0.62	0.31	2.01	0.04
intakeSTRAY	0.71	0.29	2.42	0.02

Standard errors: MLE

Observations	1833
Dependent variable	on_time
Type	Generalized linear model
Family	binomial
Link	logit

$\chi^2(6)$	84.96
Pseudo-R ² (Cragg-Uhler)	0.10
Pseudo-R ² (McFadden)	0.07
AIC	1097.33
BIC	1135.93

	Est.	S.E.	z val.	p
(Intercept)	0.32	0.33	0.97	0.33
outcomeDIED	1.25	1.03	1.21	0.23
outcomeEUTHANIZED	0.53	0.17	3.07	0.00
outcomeFOSTER	0.79	0.61	1.31	0.19
outcomeRETURNED TO OWNER	3.34	0.60	5.52	0.00
intakeOWNER SURRENDER	1.65	0.35	4.78	0.00
intakeSTRAY	1.45	0.33	4.41	0.00

Standard errors: MLE

Observations	1833
Dependent variable	on_time
Type	Generalized linear model
Family	binomial
Link	logit

$\chi^2(4)$	5.42
Pseudo-R ² (Cragg-Uhler)	0.01
Pseudo-R ² (McFadden)	0.00
AIC	1172.88
BIC	1200.45

	Est.	S.E.	z val.	p
(Intercept)	1.55	0.32	4.86	0.00
chipSCAN NO CHIP	0.08	0.21	0.37	0.71
chipUNABLE TO SCAN	-0.05	0.40	-0.13	0.89
intakeOWNER SURRENDER	0.61	0.31	1.98	0.05
intakeSTRAY	0.69	0.29	2.34	0.02

Standard errors: MLE

Observations	1833
Dependent variable	on_time
Type	Generalized linear model
Family	binomial
Link	logit

$\chi^2(3)$	5.77
Pseudo-R ² (Cragg-Uhler)	0.01
Pseudo-R ² (McFadden)	0.00
AIC	1170.52
BIC	1192.58

	Est.	S.E.	z val.	p
(Intercept)	1.74	0.33	5.24	0.00
animalDOG	-0.15	0.20	-0.76	0.45
intakeOWNER SURRENDER	0.60	0.31	1.94	0.05
intakeSTRAY	0.69	0.29	2.35	0.02

Standard errors: MLE

```
glm(formula = time ~ intake + animal + chip + outcome, family = poisson(),
     data = shelter)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-5.0878	-2.0942	-0.8433	0.5840	9.8204

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	3.25588	0.04922	66.151	< 2e-16 ***
intakeOWNER SURRENDER	-1.40129	0.03806	-36.820	< 2e-16 ***
intakeSTRAY	-1.01833	0.03393	-30.013	< 2e-16 ***
animalDOG	0.15174	0.02523	6.015	1.80e-09 ***
chipSCAN NO CHIP	-0.14071	0.02783	-5.056	4.28e-07 ***
chipUNABLE TO SCAN	-0.10393	0.05517	-1.884	0.0596 .
outcomeDIED	-0.87212	0.11426	-7.633	2.29e-14 ***
outcomeEUTHANIZED	-0.64037	0.02225	-28.775	< 2e-16 ***
outcomeFOSTER	-0.39698	0.06786	-5.850	4.92e-09 ***
outcomeRETURNED TO OWNER	-1.46341	0.03663	-39.953	< 2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 12201.6 on 1832 degrees of freedom
Residual deviance: 9378.3 on 1823 degrees of freedom
AIC: 14517

Number of Fisher Scoring iterations: 6

	2.5 %	97.5 %
(Intercept)	3.1590085	3.35194721

```

intakeOWNER SURRENDER    -1.4755537 -1.32635806
intakeSTRAY              -1.0843667 -0.95135276
animalDOG                0.1025139  0.20141301
chipSCAN NO CHIP        -0.1950108 -0.08591295
chipUNABLE TO SCAN      -0.2131352  0.00317712
outcomeDIED              -1.1044422 -0.65595751
outcomeEUTHANIZED        -0.6840986 -0.59686078
outcomeFOSTER            -0.5326087 -0.26647242
outcomeRETURNED TO OWNER -1.5357062 -1.39211393

```

Call:

```
glm(formula = time ~ intake + outcome, family = poisson(), data = shelter)
```

Deviance Residuals:

```

      Min       1Q   Median       3Q      Max
-5.0660  -2.0874  -0.9047   0.5466   9.9237

```

Coefficients:

```

              Estimate Std. Error z value Pr(>|z|)
(Intercept)      3.26169    0.03392  96.147 < 2e-16 ***
intakeOWNER SURRENDER -1.38194    0.03731 -37.042 < 2e-16 ***
intakeSTRAY       -1.03047    0.03372 -30.561 < 2e-16 ***
outcomeDIED       -0.92431    0.11401  -8.107 5.18e-16 ***
outcomeEUTHANIZED -0.65207    0.02207 -29.551 < 2e-16 ***
outcomeFOSTER     -0.48740    0.06674  -7.303 2.81e-13 ***
outcomeRETURNED TO OWNER -1.40548    0.03578 -39.284 < 2e-16 ***
---

```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

```

Null deviance: 12201.6 on 1832 degrees of freedom
Residual deviance: 9448.5 on 1826 degrees of freedom
AIC: 14581

```

Number of Fisher Scoring iterations: 6

```

              2.5 %    97.5 %
(Intercept)      3.1946881  3.3276782
intakeOWNER SURRENDER -1.4547129 -1.3084578
intakeSTRAY       -1.0960888 -0.9639035
outcomeDIED       -1.1561811 -0.7086556
outcomeEUTHANIZED -0.6954363 -0.6089368
outcomeFOSTER     -0.6209137 -0.3591875
outcomeRETURNED TO OWNER -1.4761247 -1.3358652

```

[1] FALSE

[1] FALSE

POISSON MODEL: looking at model6, using it has a very high pearson residual which is higher than the chi-squared statistic meaning it is probably suffering from overdispersion. To deal with this could be to introduce a dispersion parameter and have a quasi-poisson model OR we go for a negative binomial model.

```
Call:
glm(formula = time ~ intake + outcome, family = poisson(), data = shelter)
```

Deviance Residuals:

	Min	1Q	Median	3Q	Max
	-5.0660	-2.0874	-0.9047	0.5466	9.9237

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	3.26169	0.08524	38.265	< 2e-16 ***
intakeOWNER SURRENDER	-1.38194	0.09374	-14.742	< 2e-16 ***
intakeSTRAY	-1.03047	0.08472	-12.163	< 2e-16 ***
outcomeDIED	-0.92431	0.28647	-3.227	0.00125 **
outcomeEUTHANIZED	-0.65207	0.05544	-11.761	< 2e-16 ***
outcomeFOSTER	-0.48740	0.16769	-2.907	0.00365 **
outcomeRETURNED TO OWNER	-1.40548	0.08990	-15.634	< 2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 6.313406)

Null deviance: 12201.6 on 1832 degrees of freedom
Residual deviance: 9448.5 on 1826 degrees of freedom
AIC: 14581

Number of Fisher Scoring iterations: 6

Single term deletions

Model:

	Df	Deviance	AIC	F value	Pr(>F)
<none>		9448.5	14581		
intake	2	10587.1	15715	110.03	< 2.2e-16 ***
outcome	4	11750.8	16875	111.24	< 2.2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Coefficients still significant (by F-tests) but deviance still above chi-squared.

Call:

```
glm.nb(formula = time ~ intake + outcome + chip + animal, data = shelter,
       init.theta = 1.114925073, link = log)
```

Deviance Residuals:

	Min	1Q	Median	3Q	Max
	-2.1487	-1.0149	-0.3325	0.2207	3.6358

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	3.48306	0.14330	24.306	< 2e-16 ***

intakeOWNER SURRENDER	-1.62161	0.11844	-13.692	< 2e-16 ***
intakeSTRAY	-1.25740	0.11014	-11.416	< 2e-16 ***
outcomeDIED	-0.86714	0.23541	-3.684	0.00023 ***
outcomeEUTHANIZED	-0.71229	0.05612	-12.691	< 2e-16 ***
outcomeFOSTER	-0.43965	0.16496	-2.665	0.00769 **
outcomeRETURNED TO OWNER	-1.61127	0.07887	-20.430	< 2e-16 ***
chipSCAN NO CHIP	-0.12566	0.07004	-1.794	0.07279 .
chipUNABLE TO SCAN	-0.07656	0.13781	-0.556	0.57852
animalDOG	0.17273	0.06356	2.718	0.00658 **

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for Negative Binomial(1.1149) family taken to be 1)

Null deviance: 2660.0 on 1832 degrees of freedom
 Residual deviance: 2156.3 on 1823 degrees of freedom
 AIC: 10079

Number of Fisher Scoring iterations: 1

Theta: 1.1149
 Std. Err.: 0.0507

2 x log-likelihood: -10057.4320

Call:

glm.nb(formula = time ~ intake + outcome, data = shelter, init.theta = 1.103703043,
 link = log)

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.1038	-0.9345	-0.4035	0.2407	3.3850

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	3.51491	0.11394	30.849	< 2e-16 ***
intakeOWNER SURRENDER	-1.62341	0.11796	-13.762	< 2e-16 ***
intakeSTRAY	-1.26185	0.11024	-11.446	< 2e-16 ***
outcomeDIED	-0.95171	0.23616	-4.030	5.58e-05 ***
outcomeEUTHANIZED	-0.70648	0.05586	-12.647	< 2e-16 ***
outcomeFOSTER	-0.52936	0.16266	-3.254	0.00114 **
outcomeRETURNED TO OWNER	-1.55583	0.07675	-20.273	< 2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for Negative Binomial(1.1037) family taken to be 1)

Null deviance: 2642.4 on 1832 degrees of freedom
 Residual deviance: 2154.8 on 1826 degrees of freedom
 AIC: 10085

Number of Fisher Scoring iterations: 1

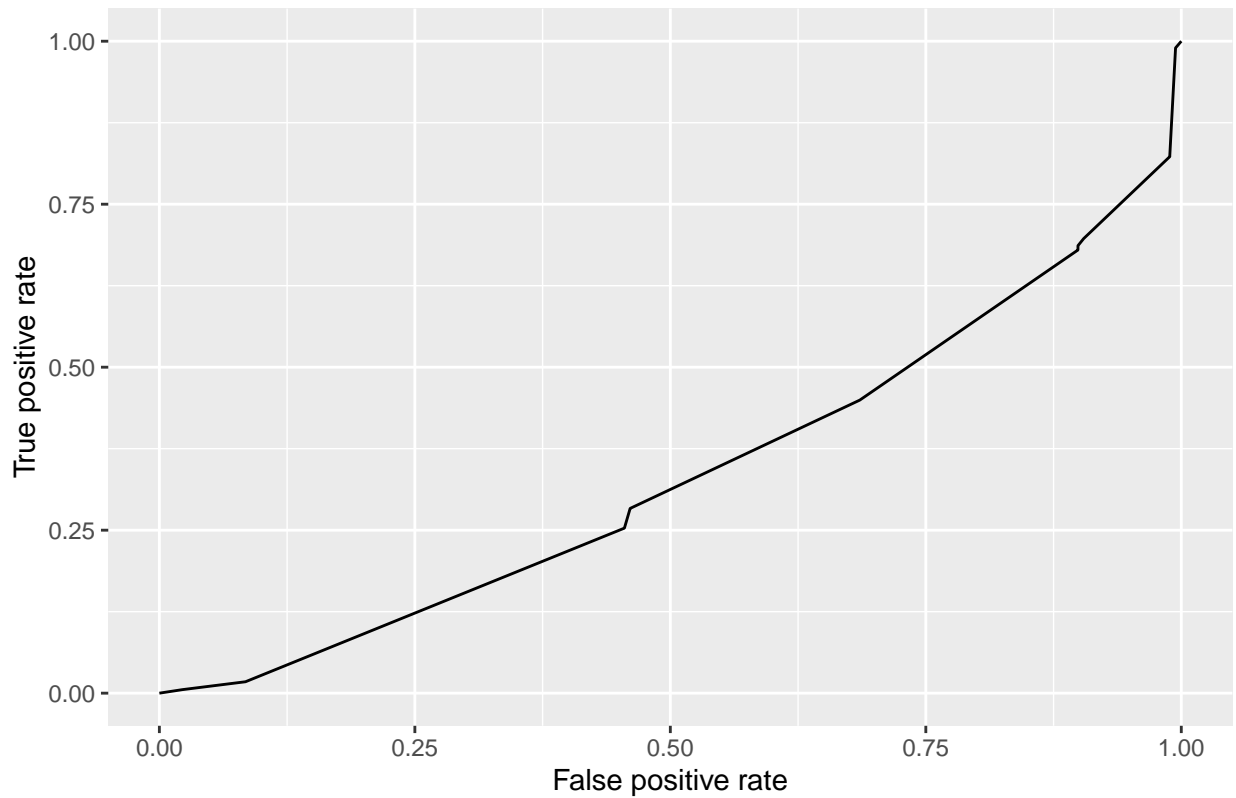
Theta: 1.1037
Std. Err.: 0.0500

2 x log-likelihood: -10069.4000

(Intercept)	intakeOWNER SURRENDER	intakeSTRAY
33.6128993	0.1972248	0.2831305
outcomeDIED	outcomeEUTHANIZED	outcomeFOSTER
0.3860798	0.4933791	0.5889826
outcomeRETURNED TO OWNER		
0.2110144		

	2.5 %	97.5 %
(Intercept)	26.8856526	42.0234173
intakeOWNER SURRENDER	0.1565133	0.2485260
intakeSTRAY	0.2281128	0.3514178
outcomeDIED	0.2430290	0.6133324
outcomeEUTHANIZED	0.4422130	0.5504654
outcomeFOSTER	0.4282019	0.8101330
outcomeRETURNED TO OWNER	0.1815460	0.2452663

Area under the curve: 0.334



$$\widehat{on\ time} = 33.613 + 0.197 \cdot I_{Surrender}(i) + 0.283 \cdot I_{Stray}(i) + 0.386 \cdot I_{Died}(j) + 0.493 \cdot I_{Euthanized}(j) + 0.0589 \cdot I_{Foster}(j)$$

$$I_{Surrender}(i) = \begin{cases} 1 & \text{if Position of } i\text{th observation is Surrender,} \\ 0 & \text{Otherwise.} \end{cases}$$

$$I_{\text{Stray}}(i) = \begin{cases} 1 & \text{if Position of } i\text{th observation is Stray,} \\ 0 & \text{Otherwise.} \end{cases}$$

$$I_{\text{Died}}(j) = \begin{cases} 1 & \text{if Position of } j\text{th observation is Died,} \\ 0 & \text{Otherwise.} \end{cases}$$

$$I_{\text{Euthanized}}(j) = \begin{cases} 1 & \text{if Position of } j\text{th observation is Euthanized,} \\ 0 & \text{Otherwise.} \end{cases}$$

$$I_{\text{Foster}}(j) = \begin{cases} 1 & \text{if Position of } j\text{th observation is Foster,} \\ 0 & \text{Otherwise.} \end{cases}$$

$$I_{\text{Returned}}(j) = \begin{cases} 1 & \text{if Position of } j\text{th observation is Returned,} \\ 0 & \text{Otherwise.} \end{cases}$$

Conclusions {#sec:Conc}