

BACHELOR THESIS

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$\begin{array}{c} \textbf{Semantics and transformations of HTN} \\ \textbf{models} \end{array}$

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Abstract: Hierarchical task network (HTN) is an approach to planning where compound tasks are decomposed into subtasks that can be either decomposed or executed right away. HTN is an extension of classical planning analogously as context-free languages extend regular languages. The goal of the thesis is split into two parts: describe, compare, and analyze various semantics and propose transformations of HTN models that do not lose any characteristics about the model. A significant piece of the thesis aims at handling empty methods which are usually not defined properly. The biggest challenges of HTN transformations lie in the proper management of constraints.

Keywords: hierarchical planning, hierarchical task networks, semantics, transformations

Název práce: Sémantiky a transformace HTN modelů

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Abstrakt: Hierarchická síť úloh (HTN) je způsob plánování obsahující složené úlohy, které lze dekomponovat na podúlohy, které mohou být opět dekomponovány nebo přímo vykonány. HTN je rozšíření klasického plánování podobně jako bezkontextové jazyky rozšiřují regulární jazyky. Tato práce má dva cíle. Prvním je popsat, porovnat a analyzovat různé sémantiky. Druhým je navrhnout transformace HTN modelů, které by neztrácely žádné informace a vlastnosti modelů. Značná část této práce se zabývá vyřešením problémů prázdných metod, které většinou nejsou moc dobře zpracovány. Největší výzva HTN transformací je správná správa plánovacích omezujících podmínek.

Klíčová slova: hierarchické plánování, hierarchické sítě úloh, sémantika, transformace

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Introduction

Anyone with internet access must have noticed the rapid development of artificial intelligence (AI). What used to be science fiction in the past (not that many years ago) is now becoming more and more relevant. Some people are fascinated and others are terrified by the capabilities of modern AI technologies, ranging from large language models (LLM) to generative video makers with precise details.

We can have lengthy and deeply philosophical discussions on the definition and meaning of intelligence. Every living being has some kind of intelligence. Humans, animals, insects, and even trees have some level of intelligence (someone might use the word consciousness). We may not conclude on the final form of this definition, but surely we will all agree that a substantial part of intelligence is decision-making and planning. From the variety of all possible actions, we choose one that is the most suitable and optimal for the current situation. In situations where we want to attain a complex goal, we need to use our intelligence and create a plan, i.e., a sequence of valid actions that will change the current state of the world to the desired one.

This thesis concerns the Hierarchical Task Network (HTN) which is the way most people think about problems and ways of solving them. Having some abstract and high-level tasks, we may decompose these tasks into subtasks that may be later again decomposed or executed right away. A high-level task is accomplished when all of its subtasks are accomplished. HTN can express different planning domains more compactly and intuitively than classical planning, which will be discussed in this thesis as well.

Motivation

The theory of classical and hierarchical planning is closely related to the theory of Automata and Grammars [1] [2] [3] [4]. For this reason, we can utilize concepts, knowledge, and well-known structures from the theory of Automata and Grammars and apply them to the field of planning. Planning and especially hierarchical planning is widely used in AI and other similar fields of informatics.

If we want to improve AI, then we need to improve planning, which is part of the concept of intelligence, as we discussed earlier. If we want to improve some theoretical knowledge, then we need to do theoretical research in that field. Hence, this bachelor's thesis was created, to at least somehow help the international community of researchers in this particular field. It is important to remember the saying, "Rome was not built in a day".

Goal

The goal of this thesis is a consequence of what was said in the **Motivation** section. We want to explore the theory of planning by taking advantage of the existing knowledge of Automata and Grammars. The title of this thesis consists of words **Semantics** and **Transformations** thus the scope of exploration is set

so. One of the subgoals is to assemble valuable information about the theory of planning that is spread throughout different publications and textbooks. In the semantics part, we want to describe and compare different formalisms and their characteristics. Moreover, we will introduce new semantics regarding hierarchical planning. In the transformations part, we want to find ways of modifying the hierarchical models without losing any properties of the models. For example, we might try to compile away some constraints and convert them into different constraints.

Structure

In chapters one and two, we will describe and define classical planning and HTN planning, respectively. There are many different ways of representing both planning models, however, we will outline only the most known representations. In the third chapter, we will characterize various semantics of HTN planning. That is, what is the meaning of HTN models, and how we should think about them. Finally, the fourth chapter shows some transformations, that might help achieve prerequisites for particular HTN planners, for example, to compile away unsupported features.

1 Classical Planning

Before we dive into HTN planning, it's essential to understand its predecessor, which is classical planning or, as it is called in some literature, STRIPS planning [5]. Classical planning is lightweight in the sense that it is easier to get into the theory of planning (independently on a representation of planning, which will be discussed in this chapter) and it is easier to describe domains of problems. The concept of classical planning is similar to the theory of Automata and Grammars (deterministic finite automaton (DFA), to be precise). There are different states of the world as well as actions that change one state to another. An action in classical planning can be viewed as a state transition function $\gamma: S \times A \to S$, where S and A denote the sets of all states and actions, respectively. If an action is applicable to a state then there will be a state transition, otherwise it will be undefined. The set of goal states, $S_g \subseteq S$, is analogous to a set of accepting states. The planning problem then can be reduced to a problem of searching paths in a directed graph.

Although this approach to classical planning is simple and straightforward, it has one crucial flaw which makes it unusable in practice. Imagine a planning domain that describes a warehouse. If we have five locations, three piles of containers per location, three robots, and one hundred containers, then there are 10^{277} states [6], which is much more than the number of atoms in the observable universe. And that is just a simple small domain with a small amount of objects. For this purpose, we need to use better ways of representing classical planning, which will be called state-transition system. We will briefly describe two possible representations: set-theoretic representation and classical representation.

In both representations, the idea is to use more compact ways of defining a state of the world and actions that change the state. Instead of having a set of all states S, we will have a finite set of proposition symbols $P = \{p_1, \ldots, p_n\}$ in set-theoretic representation and a first-order language \mathcal{L} in classical representation. Both, P and \mathcal{L} describe properties and features of the world. Each state is then defined by a set of properties, which are true in that state and every other property is false. This feature is called closed world assumption. Both of these representations have the same expressive power [6].

All of the following definitions are correspondent and equivalent to the definitions in the book Automated Planning: theory and practice (Chapter 2) [6].

1.1 Set-Theoretic Representation

Definition 1. Let $P = \{p_1, \ldots, p_n\}$ be a finite set of propositional symbols, which will model properties of a world. Then $\Sigma = (S, A, \gamma)$ is a planning domain on P. S, A, and γ denote the set of all states, set of all actions, and the state-transition function, respectively, such that:

• $S \subseteq 2^P$, each state $s \in S$ is described by propositions that hold in that state. Other propositional symbols $p \in P$, $p \notin s$ do not hold in a state s.

- Each action $a \in A$ is defined as a triple of sets describing the preconditions and changes to a current state. Action $a \in A$ will be denoted as $a = (pre(a), eff^-(a), eff^+(a)) \in 2^P \times 2^P \times 2^P$, where pre(a) stands for preconditions that must be true in a state to apply this action, meanwhile $eff^-(a)$ and $eff^+(a)$ describe changes to the state or, in other words, negative and positive $effects^1$. We require $eff^-(a) \cap eff^+(a) = \emptyset$ for every $a \in A$, because otherwise it does not make any sense. Having a state $s \in S$, an action $a \in A$ is applicable to state s, if and only if $pre(a) \subseteq s$ (it might be convenient to specify $pre^-(a)$ and $pre^+(a)$ to denote positive and negative preconditions).
- Having $s \in S$ and an action $a \in A$ that is applicable to state s, state-transition function γ is defined as follows: $\gamma(s,a) = (s eff^-(a)) \cup eff^+(a)$, otherwise it is undefined.
- S must have a property that for every s ∈ S and a ∈ A that is applicable to s, γ(s, a) ∈ S. This way we do not have to know all of the states in advance. All we need is a set of actions A and some initial state s₀ ∈ S, then we can find all reachable states using Breadth-First Search (BFS), Depth-First Search (DFS), or some other searching algorithms.

Definition 2. A planning problem is a triple $\mathcal{P} = (\Sigma, s_o, g)$, such that:

- $\Sigma = (S, A, \gamma)$ is a planning domain on P.
- $s_0 \in S$ is an initial state.
- $g \subseteq P$ is a set of goal proposition symbol, which must be true in the state after the final action of a plan. $S_g = \{s \in S | g \subseteq s\}$ is a set of goal states, i.e., states that satisfy the planning problem \mathcal{P} .

Because the set of $propositional\ symbol\ P$ is finite, sets of states, actions, and state-transition function are also finite.

Definition 3. A plan in a planning domain Σ is a finite sequence of actions $\pi = (a_1, \ldots, a_k)$, where $k \geq 0$ and $(\forall a \in \pi)a \in A$. The plan π is applicable to a state $s_0 \in S$, if and only if a sequence of states (s_0, \ldots, s_k) exist, such that: $(1 \leq i \leq k)$ pre $(a_i) \subseteq s_{i-1}$ and $s_i = \gamma(s_{i-1}, a_i) = ((s_{i-1} - eff^-(a_i)) \cup eff^+(a_i))$ is defined. Otherwise, the plan π is invalid.

In other words, a plan $\pi = (a_1, \ldots, a_k)$ is applicable to a state s_0 , if and only if a plan $\pi' = (a_2, \ldots, a_k)$ is applicable to a state $s_1 = \gamma(s_0, a_1) \in S$.

Having a plan $\pi = (a_1, ..., a_k)$ and a state $s \in S$, we will abuse the notation to let $\gamma(s, \pi)$ denote a state $s_k \in S$, where we get after applying the sequence of actions of a plan, i.e.,

$$\gamma(s, (a_1, \dots, a_k)) = \begin{cases} s, & \text{if } k = 0 \text{ (there are no actions)}, \\ \gamma(\gamma(s, a_1), (a_2, \dots, a_k)), & \text{if } k > 0, a_1 \text{ is applicable to } s, \\ undefined, & \text{otherwise.} \end{cases}$$

¹In some literature these sets are called: add list, delete list.

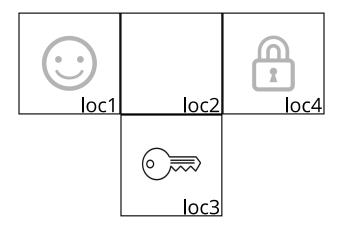


Figure 1.1 Initial state of a simple planning domain

Definition 4. A solution to a planning problem $\mathcal{P} = (\Sigma, s_o, g)$ is a plan $\pi = (a_1, \ldots, a_k)$ that is applicable to s_0 , which changes the initial state s_0 to a state that satisfies goal propositional symbols: $\gamma(s_0, \pi)$ is defined and $g \subseteq \gamma(s_0, \pi)$ (equivalent to $\gamma(s_0, \pi) \in S_q$).

For a planning problem there might be many solutions, moreover, there might be an infinite number of solutions if there are states that can be visited repeatedly, (e.g. we might have two adjacent locations in a domain, that can be visited cyclically without any constraints).

It is easy to see that for each planning problem \mathcal{P} with nonempty set of solutions (there exist a plan π such that π is a solution to a \mathcal{P}) there exist at least one minimal solution $\pi = (a_1, \ldots, a_k)$, i.e., there is no solution $\pi' = (a'_1, \ldots, a'_j)$ such that j < k. There might be many different minimal solutions but all of them share the same length.

Example 1. Imagine a simple planning domain (Figure 1.1) that can represent states in an uncomplicated maze-like game. We have four game locations, a player character, a key, and a locked door (illustrated by a loc4). The character can move freely between locations but if he wants to enter loc4, then he needs a key that can be picked at the loc3 (but cannot be discarded later on). Now we will define a planning problem $\mathcal{P} = (\Sigma, s_0, g)$ for this domain $\Sigma = (S, A, \gamma)$ more formally:

- $P = \{\text{at-loc1,at-loc2,at-loc3,at-loc4,key-picked}\},$
- $S = \{\{\text{at-loc1}\}, \{\text{at-loc2}\}, \{\text{at-loc3}\}, \{\text{at-loc1}, \text{key-picked}\}, \{\text{at-loc2}, \text{key-picked}\}, \{\text{at-loc3}, \text{key-picked}\}, \{\text{at-loc4}, \text{key-picked}\}\},$

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• A = \{\text{move12}, \text{move21}, \text{move23}, \text{move24}, \text{move42}, \text{pick}\}, \text{where} : \text{move12} = (\{\text{at-loc1}\}, \{\text{at-loc1}\}, \{\text{at-loc2}\}); \\ \text{move21} = (\{\text{at-loc2}\}, \{\text{at-loc2}\}, \{\text{at-loc1}\}); \\ \text{move23} = (\{\text{at-loc2}\}, \{\text{at-loc2}\}, \{\text{at-loc3}\}); \\ \text{move32} = (\{\text{at-loc3}\}, \{\text{at-loc3}\}, \{\text{at-loc2}\}); \\ \text{move24} = (\{\text{at-loc2}, \text{key-picked}\}, \{\text{at-loc2}\}, \{\text{at-loc4}\}); \\ \text{move42} = (\{\text{at-loc4}\}, \{\text{at-loc4}\}, \{\text{at-loc2}\}); \\ \text{pick} = (\{\text{at-loc3}\}, \{\}, \{\text{key-picked}\}), \\ \end{cases}
```

- γ as defined in Definition 1,
- $s_0 = \{\text{at-loc1}\}\ (\text{Figure 1.1}),$
- $q = \{\text{at-loc4}, \text{key-picked}\}.$

Example 1 shows us a complete description of a planning domain Σ and a planning problem \mathcal{P} . There is one and only minimal solution which is $\pi = (\text{move12}, \text{move23}, \text{pick}, \text{move32}, \text{move24})$. On the other hand, there is an infinite number of solutions. We might go to the loc3 and apply the action pick as many times as we desire, thus generating an infinite amount of solutions.

With knowledge of the particular domain, we can adjust the domain without losing any domain's specifics. For example, we might alter the set of the *goal proposition symbols* g to be $g = \{\text{at-loc4}\}$ because we know that it is impossible to enter loc4 without having a key picked up at the loc3.

The set of states S contains all reachable states from the initial state s_0 , other unreachable states might be added to the S but they are not needed. For example, the state {at-loc1,at-loc2} is contradictory because we cannot be at two locations simultaneously. Likewise states {}, {key-picked}, {at-loc4} are also meaningless.

The concept of the key in this domain is depicted as a propositional symbol key-picked. This simplification does not take into account the location of a key because it is not needed in this domain. Once the key is picked, it will be implicitly located at the same location as the character. Hence, the action pick is applicable more than once in a plan.

Example 2. Let's consider an extension of this domain by adding two new locations, and another key (Figure 1.2). Only this time we want to model a new constraint that allows at most one key to be held at a time. There are numerous ways of modeling this planning domain. For instance, we might introduce new propositional symbols: key1-picked, key2-picked, door1-opened, door2-opened. If we wanted to model the locations of keys, we would need to include many new propositional symbols of the form key1-at-loc1, key1-at-loc2, and so on. Also, we would need new actions that would consider the locations of a key and the character. New actions may look like this: pick-key1-at1 = ({at-loc1,key1-at-loc1},{key2-picked},{key1-picked}), move12-with-key1 = ({at-loc1,key1-at-loc1},{at-loc1,key1-at-loc2}) and so on. This enumeration of possible substates might result in an enormous set of propositional symbols and other related sets [6] (2.2.4 Properties of the Set-Theoretic Representation). An elaborate solution that fixes this problem is discussed in the following chapter.

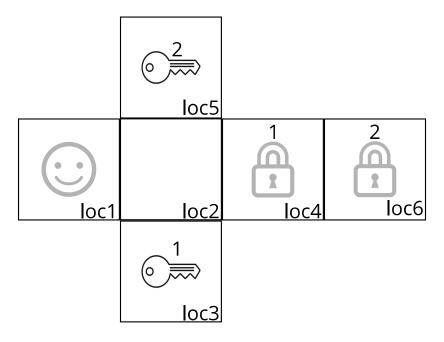


Figure 1.2 Extended planning domain of a maze-like game

1.2 Classical Representation

Classical representation of planning improves set-theoretic representation by introducing a first-order language \mathcal{L} that consists of a finite number of constant symbols (similar to a set of propositional symbols defined in Definition 1), predicate symbols, and other symbols for the representation of planning operators. We do not allow any functional symbols in \mathcal{L} because we are focused to model finite models where functions are not needed. A state in classical representation is defined as a set of grounded logical atoms of \mathcal{L} .

Example 3. Before we start with definitions, we will look at Figure 1.1 from the perspective of classical planning. We want to model the player, key, locations, and locked door. Thus, the set of constant symbols is {player,loc1,loc2,loc3,loc4, key1,nothing,door}. The constant symbol nothing represents that the player's inventory is empty. With this knowledge, we can represent the initial state of Figure 1.1 to be $s_0 = \{adjacent(loc1,loc2), adjacent(loc2,loc1), adjacent(loc2,loc3), adjacent(loc3,loc2), adjacent(loc2,loc4), adjacent(loc4,loc2), at(player,loc1), holds(player,nothing), locked(door)\}. Some logical atoms will remain the same throughout all possible states, e.g. adjacent(loc1,loc2), meanwhile other atoms like at(player,loc1) or holds(player,nothing) will change after the application of proper actions.$

Now we will define *planning operators* in *classical planning*. A grounded instance of an operator is an action that can be part of a *plan*.

Definition 5. A planning operator is a triple o = (name(o), precond(o), eff(o)), where:

- name(o) is of a form $n(x_1, \ldots, x_k)$, where n is a operator symbol and must be unique in \mathcal{L} and x_1, \ldots, x_k represent variable symbols that appear in an operator,
- precond(o) and eff(o) generalize preconditions and effects of set-theoretic representation. These sets contain positive and negative logical literals.

Let O denote a set of all planning operators as specified above.

In some literature, the usage of name(o) is not specified, rather the multiset of grounded operators (actions) is assumed. The essence of name(o) is in the planning phase. We might have multiple grounded instances of operators that might use the equivalent constant symbols. To help differentiate a planning operator from an instance of a planning operator, the name(o) might come in handy. name(o) refers unambiguously to one specific planning operator. We will omit the usage name(o) because the meaning will be obvious from the context.

Example 4. In this example, we will look at some possible planning operators that might be used in Figure 1.2 (we will use new predicate symbols that were not specified yet):

- move(player,location1,location2)

 precond: adjacent(location1,location2), at(player,location1), ¬locked(location2)

 effects: ¬at(player,location1), at(player, location2)
- pickup-key(player,key,location)

 precond: at(player,location), at(key,location), holds(player,nothing)

 effects: ¬holds(player,nothing), ¬at(key,location), holds(player,key)
- drop-key(player,key,location)

 precond: at(player,location), holds(player,key)

 effects: ¬holds(player,key), at(key,location), holds(player,nothing)
- open-door(player,location1,location2, key)

 precond: adjacent(location1,location2), locked(location2), at(player,location1), key-opens-door(key,location2), holds(player,key)

 effects: ¬locked(location2)

In the Example 4 predicate symbols adjacent(l1,l2) and key-opens-door(key,location) are describing static properties of a domain that will never change and thus, will never appear in effects of *planning operators*. On the other hand, predicate symbols like at(player/key,location), locked(location), or holds(player, key) will change and therefore will occur in effects of *planning operators*.

Definition 6. Let us be given a state $s \in S$ and an action (ground instance of a planning operator) a. If $precond^+(a) \subseteq s$ and $precond^-(a) \cap s = \emptyset$, where $precond^+(a)$ denotes a set of all positive atoms in precond(a) and $precond^-(a)$ denotes a set of all atoms whose negation is in precond(a), then a is applicable to s and $\gamma(s,a) = (s - eff^-(a)) \cup eff^+(a)$. $eff^-(a)$ and $eff^+(a)$ are analogous to $precond^-(a)$ and $precond^+(a)$, respectively.

Definition 7. Having a first-order language \mathcal{L} with a finite amount of constant and predicate symbols and no functional symbols, the classical planning domain in \mathcal{L} is a state-transition system $\Sigma = (S, A, \gamma)$ such that:

- $S \subset 2\{all \ ground \ atoms \ of \ \mathcal{L}\}$
- $A = \{all \ ground \ instances \ of \ operators \ in \ O\},$
- γ is analogous Definition 1,
- S is closed under γ in the same manner as in Definition 1.

Definition 8. A classical planning problem is corresponding to set-theoretic planning problem, it is defined as $\mathcal{P} = (\Sigma, s_0, g)$, where:

- $\Sigma = (S, A, \gamma)$ is a classical planning domain,
- $s_0 \in S$ is an initial state
- *g* is a set of literals.

2 Hierarchical Planning

Now that we have understood classical planning, we can move on to hierarchical planning or Hierarchical Task Network (HTN), to be precise. In HTN the goal alone is not to find an *applicable plan* that will meet all of the criteria of the *planning problem*. HTN focuses on accomplishing some set of tasks by decomposing them into sub-tasks with constraints like ordering and state conditions. A task is accomplished immediately upon all of his sub-tasks are accomplished. HTN is an extension of classical planning which gives us clues on how to find the proper *plan*.

As in classical planning, there are states of the world represented by the set of proposition symbols or logical atoms that are true in a state. We can apply actions to states if the preconditions of actions are satisfied (held in a state). These actions will be called primitive tasks in HTN. These tasks are executable right away and they change the current state to another one by applying negative and positive effects. In addition to primitive tasks there are non-primitive tasks. We will call them compound tasks. These tasks cannot be executed and applied to a state, rather they have to be decomposed into a set of sub-tasks (both primitive and compound) using decomposition methods. Having an initial task network, that is a set of tasks and a set of constraints, the goal is to decompose all tasks into primitive tasks and find an ordering of these tasks so that the constraints are not violated. After doing so, it is important to check that the resulting plan (a sequence of primitive tasks) is a valid plan and can be applied to an initial state.

All of the following definitions are correspondent and equivalent to the definitions in the book *Automated Planning: theory and practice (Chapter 11)* [6] and other publications [3] [4] [7] [8].

2.1 HTN Planning

Definition 9. A task network is a pair $\omega = (U, C)$, where U is a set of tasks (primitive and compound) and C is a set of constraints.

For a solution (plan) to be valid we need to satisfy all of the constraints listed in C. We identify four types of constraints:

- $t_i \prec t_j$ where $t_i, t_j \in U$: an ordering-constraint meaning that in every valid solution the last primitive task (action) in the solution to which t_i decomposes must precede the first primitive task (action) in the solution to which t_j decomposes,
- before (l, U'): before-constraint symbolizing that in every valid solution the literal l must hold in a state right before the application of a first action to which $U' \subseteq U$ decomposes,
- after(U', l): after-constraint is similar to before-constraint with the difference that the literal l must hold in a state right after the last action to which set U' decomposes,

• between (U', l, U''): between-constraint is saying that the literal l must hold in all states starting after the last action of U' and lasting until the state right before the application of a first action of U''.

We will say that the task network is primitive if and only if, all of the tasks are primitive. A task network having at least one compound task will be called non-primitive.

The most used state-constraint is a before-constraint which can be modeled in various HTN planners. The usage and application of this constraint is obvious. Before the beginning of a task, we want to hold some preconditions that are significant for that particular task. For example, a user needs to input all of the information before he can continue with the paying; a player needs to complete all of the quests before he can move on to the next stage, or a warehouse robot needs to have permission set before he can execute some real-life tasks. Analogous after-constraint has different use cases. We might use this constraint on the last task in the task network to signalize our intentions which are not modeled with the tasks themselves. For example, we want to deallocate resources of the process after the completion, or we want to give a player new abilities after the completion of many tasks that might interleave. This constraint can be used as a shortcut in difficult models where the person responsible for the modeling cannot enumerate and decide the ordering of tasks perfectly. The between-constraint represents an interval of states which hold some property. For example, we want a player to have a specific item in his inventory after the completion of one task and lasting until the other tasks, or an autonomous robot must hold a crate in all states meanwhile he moves from one location to another (possibly doing other unrelated things).

In accordance with the Definition 5, the more formal definition [2] [3] [6] of the $task\ network$ would contain some function $\alpha:U\to N$, which would map instances of primitive and compound tasks to the set of names of all tasks. This function would allow us to have multiple instances of the same task in the set of tasks U, each with a unique identifier. We will omit a function α because its context will always be clear.

Definition 10. A method is a triple m = (compound(m), subtasks(m), constraints(m)), where compound(m) is a compound task and (subtasks(m), constraints(m)) is a task network. constraints(m) operate only with the tasks in subtasks(m). Having a task network $\omega = (U, C)$, compound task $c \in U$, and an instance of method m from M such that compound(m) = c. Then m decomposes c into subtasks(m), creating a new task network $\omega' = (U', C')$ of a form:

$$\delta(\omega,c,m) = ((U - \{c\}) \cup subtasks(m), C' \cup constraints(m)),$$
 where C' is a modification of C :

• replace each ordering-constraint containing c with new ones containing subtasks(m), i.e., $\forall c' \in subtasks(m) : c \prec x$ is replaced with $c' \prec x$ and $x \prec c$ is replaced with $x \prec c'$,

• replace each before-, after-, between-constraint containing c with new ones containing subtasks(m). For example, we would replace before-constraint before (l, V) with before $(l, (V - \{c\}) \cup subtasks(m))$.

It is highly convenient to write planning *methods* as rewriting rules [7]:

$$T \to T_1, \ldots, T_k \quad [C].$$

This rewriting rule symbolizing a method is saying as follows: A method which decomposes the compound task T into sub-tasks T_1, \ldots, T_k under the constraints C.

Definition 10 works well for planning domains without empty methods (a method that decomposes compound task into the empty set of subtasks). Using an empty method creates undefined behavior because the decomposed compound task is removed from all constraints and thus it is unclear where the specified constraint should be checked. For this reason, we will later redefine method decomposition.

Definition 11. A (HTN) planning domain is a quadruple $\mathcal{D} = (\mathcal{L} / P, O, C, M)$, where \mathcal{L} / P and O are first-order language (set of propositional symbols) and a set of operators, respectively, as described in the section Classical Representation, C is a set of compound tasks and M represents a set of all methods.

Planning domain will be referred to as totally-ordered if all of the methods in M and the initial task network are totally-ordered (there is a total strict ordering of sub-tasks). Planning domains that are not totally-ordered will be referred to as partially-ordered.

A first-order language \mathcal{L} can be easily interchanged for a set of propositional symbols P due to the equivalent expressive power of set-theoretic representation and classical representation [6].

Definition 12. A (hierarchical) planning problem is a triple $\mathcal{P} = (s_0, \omega, \mathcal{D})$ that consists of initial state of the world s_0 , initial task network ω and a planning domain \mathcal{D} .

Definition 13. A solution to the planning problem \mathcal{P} is a plan $\pi = (a_1, \ldots, a_k)$. This sequence of actions is assembled from a primitive task network $\omega' = (U', C')$, $U' = \{a_i \mid 1 \leq i \leq k\}$, after the application of a sequence of methods from M to the initial task network ω . A solution π needs to be valid, i.e., $\gamma(s_0, \pi)$ is not undefined and also needs to satisfy all of the constraints in C'. That is:

- $a_i \prec a_j \implies i < j$,
- before $(l, V) \implies l \in s_{min\{i \mid a_i \in V\} 1}$ (if the literal l is negative then it must not be in a state, same applies for other constraints),
- $after(V, l) \implies l \in s_{max\{i \mid a_i \in V\}}$,
- between $(V', l, V'') \implies (\forall j, \max\{i \mid a_i \in V'\} \leq j < \min\{i \mid a_i \in V''\}: l \in s_i).$

By l we mean a ground instance of a literal l (in the case of set-theoretic representation it would be $p \in P$).

2.2 HTN and Context-free Grammars

With the knowledge acquired in the previous sections, we can try to map planning definitions and structures to the definitions and structures of the theory of Automata and Grammars. By doing so, we would be able to utilize already discovered knowledge and algorithms. Furthermore, it will allow us to prove different language classifications [3].

The simplest example is to map classical planning problem to the equivalent DFA, and vice versa. The mapped DFA generates all of the solutions, i.e., plans that are valid, applicable to the initial state s_0 and satisfy the goal g.

Theorem 1. For every classical planning problem $\mathcal{P} = (S, A, \gamma, s_0, g)$, where (S, A, γ) is a planning domain, there exists a DFA [1] $D = (Q, \Sigma, \delta, q_0, F)$ such that D generates all the solutions for \mathcal{P} .

Proof. The proof is straightforward. Having $\mathcal{P} = (S, A, \gamma, s_0, g)$, we can construct DFA $D = (S, A, \delta, s_0, S_g)$ where $S_g = \{s \in S | g \subseteq s\}$ and $\delta(s, a) = \gamma(s, a) = (s - \text{eff}^-(a)) \cup \text{eff}^+(a)$. We can easily see that every generated word (plan) $\pi \in L(A)$ is also a valid solution to the planning problem. Every solution is applicable to the $q_0 = s_0$ because transition function of D imitates planning state-transition function of \mathcal{P} . Every $\pi \in L(A)$ is a solution because the set of accept states is S_g .

Theorem 2. For every DFA $D = (Q, \Sigma, \delta, q_0, F)$ there exists a correspondent classical planning problem $\mathcal{P} = (S, A, \gamma, s_0, g)$ where the set of solutions of \mathcal{P} is equal to L(D).

Proof. Having DFA $D = (Q, \Sigma, \delta, q_0, F)$, we will construct planning problem \mathcal{P} with individual components defined as follows. Without loss of generality, we will rename states of Q. Each state $q \in Q$ will have a unique index $i: 0 \le i < |Q|$. q_0 is the *initial state* of D. Now we define $\mathcal{P} = (S, A, \gamma, s_0, g)$ with:

$$S = \{\{i\} | q_i \in Q - F\} \cup \{\{i, goal\} | q_i \in F\},\$$

$$A = \{\sigma = (\{i\}, \{i, goal\}, \{j\}) | \delta(q_i, \sigma) = q_j \text{ and } q_j \notin F\} \cup \{\sigma = (\{i\}, \{i\}, \{j, goal\}) | \delta(q_i, \sigma) = q_j \text{ and } q_j \in F\},\$$

$$\gamma(s, a) = (s - \text{eff}^-(a)) \cup \text{eff}^+(a),\$$

$$s_0 = \begin{cases} \{0\}, & \text{if } q_0 \notin F,\ \{0, \text{goal}\}, & \text{if } q_0 \in F,\ \end{cases}$$

$$g = \{goal\}.$$

Every generated word $\sigma_1 \dots \sigma_n \in L(D)$ corresponds to a single solution $\pi = (a_1, \dots, a_n)$. Each state of \mathcal{P} is represented by an index (propositional symbol) i which specifies the state $q_i \in Q$. If a state is an accepting state, then the planning state s has propositional symbol goal. This is forced by the positive and negative effects of actions.

Corollary. Classical planning is classified into the class of regular languages.

Now we will prove that *totally-ordered* HTN planning can be represented as a context-free (CF) grammar and vice versa. These claims are extremely useful and will be used in the following parts of this thesis. Similar proofs are presented in [3].

Theorem 3. For every CF grammar $G = (V_G, T_G, P_G, S_G)$ [1] there exists a correspondent totally ordered planning problem $\mathcal{P} = (s_0, \omega, \mathcal{D})$ with $\mathcal{D} = (P, O, C, M)$ such that the set of solutions of \mathcal{P} is equal to L(G).

Proof. Constructing planning problem \mathcal{P} is uncomplicated and intuitive because the structures are similar. All we need is to handle operators $o \in O$ so that the generated plans are applicable to the initial state s_0 . Having $G = (V_G, T_G, P_G, S_G)$ we construct $\mathcal{P} = (\{\}, (\{S_G\}, \{\}), \mathcal{D})$ with $\mathcal{D} = (\{\}, T_G, V_G, M)$. Methods are defined as follows:

$$M = \{T \to T_1, \dots, T_k \mid \{T_i \prec T_i \mid 1 \le i < j \le k\} \mid | (T, T_1 \dots T_k) \in P_G\}.$$

Using this construction, the planning problem \mathcal{P} can now generate the set of plans that equals L(G). One problem is that the generated plans might not be valid solutions. This can be handled conveniently if we use empty sets for the preconditions of all operators. Each $o \in O$ will be defined as $o = (\{\}, \{\}, \{\})$. The result of this modification is that every possible plan is now a valid solution if it can be decomposed from the initial task network.

Theorem 4. For every totally ordered planning problem $\mathcal{P} = (s_0, \omega, \mathcal{D})$ with $\mathcal{D} = (P, O, C, M)$ without before, after, between-constraints there exists a CF language L that is equal to the set of solutions of \mathcal{P} .

Proof. Let $\mathcal{P} = (s_0, \omega = (U, C), \mathcal{D} = (P, O, C, M))$ be a totally ordered planning problem in which constraints of each method consist only of ordering-constraints. We will construct CF grammar $G = (V_G, T_G, P_G, S_G)$ where $V_G = C, T_G = O$ and $S_G \in U$. We assume that the initial task network ω consists of one task, |U| = 1. If there are more tasks (that are totally ordered by constraints C), we will add one extra production rule to the P_G that rewrites the new starting symbol S'_G to the given state of $\omega = (U, C)$. The set of production rules is defined as follows:

$$P_G = \{(T, T_1 \dots T_k) \mid (T, \{T_1, \dots, T_k\}, \{T_i \prec T_j \mid 1 \le i < j \le k\}) \in M\}.$$

Grammar G generates all plans that can be generated with \mathcal{P} . Some of these plans might be valid solutions and some of them might not be applicable to the $initial\ state\ s_0$. In other words, L(G) is a superset of all possible solutions of \mathcal{P} . To solve this issue it is sufficient to use the fact that the intersection of a context-free language and a regular language is resulting into context-free language [1]. We can use Theorem 1 to build a DFA D that will generate all plans that are applicable to s_0 . The empty set of goal symbols $g = \emptyset$ will ensure that the language of D equals to all possible plans that are allowed by the planning $operators\ O$. Having everything prepared, we can construct a CF language $L = L(G) \cap L(D)$ which is equal to the set of solutions of \mathcal{P} .

Corollary. Totally-ordered HTN planning without state-constraints is classified into the class of context-free languages.

2.3 HTN Plan Verification

Hierarchical plan verification can be seen as a reversal process to the decomposition of a *initial task network* into a *plan* that is *applicable* to the *initial state* s_0 and satisfies all constraints. Given a *hierarchical planning domain* $\mathcal{D} = (P, O, C, M)$, *initial task network* ω , an *initial state* s_0 , and a *plan* π , we ask if it is possible to decompose the ω into π using \mathcal{D} . Depending on a hierarchical model or semantics specification, there might be some additional information and structures to the input of a plan verification problem. For example, we might analyse totally-ordered plan verification with *method* preconditions [4].

2.4 HTN Semantics with Goal Tasks

Up to now, we have only discussed HTN definitions based on the book Automated Planning: theory and practice [6]. This book does not consider goal tasks [2] which are very similar to the goals in classical planning (Definition 2). Goal tasks are attached to the compound tasks and define the set of propositional symbols (or logical atoms) that need to hold in a state after the execution of all primitive tasks to which the compound task decomposes. In the case of primitive task, the set of positive effects is logically equivalent to the goal task of that task.

Many formalisms for describing hierarchical planning exist, and each of them comes with different approaches to define and propose hierarchical planning problems. Each formalism allows diverse features that might come in handy during modeling or planning of the planning problems. For example, HDDL [9], allows to specify goal state which is equivalent to the set of goal predicate symbols defined in Definition 2. For a plan to be valid in HDDL, a sequence of task decompositions transforming the initial task network into the primitive task network must exist. Also, the primitive task network must satisfy all constraints, a linear ordering of primitive tasks (actions) must exist, and the state after the execution of the plan must hold propositional symbols defined in goal state. This is a great feature but the definition of a goal state is allowed only for the whole planning problem and not for the individual tasks. On the other hand, alternative formalism [2] grant the feature of goal tasks which is noticeably more flexible than HDDL's formalism.

Now we will present a way of using goal tasks in modeling and planning. The idea is to omit the negative effects of actions. This way, all actions will only append predicate symbols to the state (which is defined as an element of the set 2^P). In such a manner, the planning might remind us of monotone functions. The sequence of intermediate states (s_0, \ldots, s_k) , created by the plan $\pi = (a_1, \ldots, a_k)$, has a non-decreasing size of propositional symbols in a state. Thus, we can call this subclass of planning problems – monotone hierarchical planning.

With the knowledge from the previous paragraph, let's combine the concepts of goal tasks, monotone hierarchical planning, and totally-ordered planning domains. Assume a compound task T is decomposed into the subtasks T_1, \ldots, T_k (with the ordering $T_1 \prec \cdots \prec T_k$) with given goal tasks. Because of the totally-ordered domain and the monotone hierarchical planning, we can use the technique divide and conquer and try to find the decompositions of subtasks independently.

Furthermore, the subtask T_i might take into consideration *propositional symbols* contained in *goal tasks* of subtasks T_1, \ldots, T_{i-1} . These symbols can be viewed as granted because of the fact that there are no negative effects and all methods are totally-ordered.

3 HTN Semantics

So far we have only discussed the definitions of classical and hierarchical planning. In this chapter, we will consider various semantics for hierarchical planning. A large part of this chapter will compare and describe semantics concerning *empty methods* which are not defined properly within Definition 10. The main issue regarding *empty methods* is caused by the unclear and ambiguous modification of *task network's* constraints. It is uncertain how and when the modified constraints need to be checked. In the first part of this chapter, we will analyze existing approaches and propose new ways of handling *empty methods* concerning the HTN plan verification process. In the second part, we will introduce a new idea for modeling hierarchical planning problems without the negative effects of *primitive tasks*.

3.1 Empty Methods

The following section will describe different solutions of how to handle *empty* methods.

Example 5. To understand the importance of empty methods we will reuse Figure 1.2 as an example.

Suppose that the game's initial state is $s_0 = \{at\text{-}loc1, key2\text{-}at\text{-}loc5, key1\text{-}at\text{-}loc3, door1\text{-}locked, door2\text{-}locked, key1\text{-}picked}\}$. We will assume that multiple keys can be held at the same time, and, for some reason, the player has already picked up the key1 (for example he picked it up in the previous level). The initial task network is ($\{Get\text{-}to\text{-}loc6\}, \{\}\}$). An arrow \rightarrow symbolizes a decomposition.

$$(\{Go\text{-}to\text{-}loc6\}, \{\}) \rightarrow (\{Get\text{-}key1, Get\text{-}key2, Go\text{-}to\text{-}loc4, Go\text{-}to\text{-}loc6}\},$$

 $\{Get\text{-}key1 \prec Go\text{-}to\text{-}loc4, Get\text{-}key2 \prec Go\text{-}to\text{-}loc6, before(key1\text{-}picked, Get\text{-}key2}\})$

At this point it is very convenient to use an empty method that decomposes Get-key1 into nothing because we have already picked up the key.

Example 6. Suppose we have a simple task network $\omega = (\{t1, t2\}, \{t1 \prec t2, before(p, t2)\})$. In natural language, we would say that task (primitive or compound) t1 must precede task t2, and at the same time, before executing the first primitive task to which task t2 decomposes (in case of a primitive task, we mean the state before the application of the task t2) the propositional symbol p must hold in a state. Having an empty method m such that:

$$t2 \rightarrow \varepsilon$$
 [C], where $C = \emptyset$ and ε denotes no subtasks,

we can decompose t2 in task network ω . After the application of the empty method m, we are not able to tell with certainty the semantics of the result task network. By applying m, we erase the task t2 from the set of tasks in ω and we modify all of the constraints in C. The unclear result might look like this:

 $\omega' = (\{t1\}, \{t1 \prec ?, before(p,?)\})$ with ? symbolizing undefined behaviour. Thus, the following section will study different ways of representing HTN planning with the goal of resolving undefined behavior of empty methods. Usually, we will need some additional information about task network's decomposition process which will deal with unclear situations. Sometimes we will need to modify existing definitions from the previous chapters.

Another possible use case of *empty methods* concerns situations when the decomposed task is contained in *the method's* constraints set. Our definitions of decomposition do not allow this behavior, nonetheless, it might be beneficial for the architect of a planning domain. Suppose a task network containing a compound task Pick-up-item-X. With the extended method decomposition definition, we would be able to decompose this task into nothing while not saying explicitly where the state check should be made:

$$Pick$$
-up-item- $X \to \varepsilon$ [{before(X-in-inventory, Pick-up-item-X)}]

This extended definition also contains undefined behavior because it is unclear where the *state-constraint* needs to be checked. Transformations of HTN models with the extended decomposition definition can be found here [8].

3.1.1 No Empty Methods Model

The most effortless way to handle *empty methods* is to forbid them (every totalitarian dictator would approve). This way, each $method\ m \in M$ must have nonempty set of subtasks(m), i.e.:

$$T \to T_1, \dots, T_k \quad [C], \text{ where } k \ge 1.$$

The main benefit of this semantics is regarding the method decomposition in Definition 10. By forbidding the usage of empty methods we are not able to create fuzzy situations with unclear constraints. This way we do not need to adjust any definition and everything works as it should.

As it happens in life, forbidding something might help in some cases but, on the other hand, it closes doors for the flexibility and advantages of *empty methods*. Now, it is not possible to fulfill the task by doing nothing which might be very convenient in states that already hold all desired *propositional symbols*. In such states, the decomposition of certain *compound tasks* is meaningless and creates *plans* that are longer and more redundant than *plans* which would allow *empty methods*.

Succeeding models will allow different kinds of *empty methods*, usually by handling some workaround.

3.1.2 No-op Based Model (version 1)

Another possible way to resolve the issue with *empty methods* is the No-op model [7] [8]. The no-op model introduces a new symbol no-op() which is not

presented in the hierarchical planning domain. Formally, the no-op() symbol is just another primitive task with no preconditions and effects, i.e. $no\text{-}op() = (\{\}, \{\}, \{\})$. The semantics behind this symbol is hidden right in the name, "no operation", meaning that this action has no impact on the world that we model. It serves as a regular symbol during the planning phase concerning all of the ordering-constraints and before-, after-, between-constraint. After the checking of all available constraints, the no-op() symbol is deleted from the final plan as it was not part of the former planning problem.

Pros of the no-op model are easily seen. We have solved the issue of *empty methods* by introducing a new symbol no-op() and at the same time we did not need to allow regular *empty methods* which decompose a task into an empty set. The no-op model extends the previous model in Section 3.1.1.

Cons of this model lies in the HTN plan verification, reverse process to the hierarchical planning. The main problem is due to the fact that the no-op() symbols are not part of the input to the plan verification because they are removed after the check of all constraints in a primitive task network (consists only of primitive tasks). For this reason, the no-op model is inefficient for plan verification because it would be needed to guess the locations and number of no-op() symbols in the input plan, e.g.:

```
input: \pi = (task1, task2, task3) guess1: (task1, task2, task3) guess2: (task1, no-op(), task2, task3) guess3: (no-op(), task1, task2, task3, no-op()) guess4: (task1, no-op(), no-op(), no-op(), task2, task3)
```

The main problem with the no-op model is the inability to verify plan efficiently. In the no-op model, we erase no-op() symbols after the checking of all constraints. It is possible to avoid this problem by forcing the planner of $planning\ problem$ to include the no-op() symbol into his $planning\ domain$ and treat it as an $empty\ method$ (in some sense). With this practice, the planner will not need to erase no-op() symbols in the resulting plan which will make HTN plan verification much more efficient. The second version of the no-op model also extends Section 3.1.1 (No Empty Methods Model) as it does not allow real $empty\ methods$ in $planning\ problems$.

Even though we have solved the *empty methods* problem and HTN verification problem, we still have not used *empty methods*, but rather some illusion of them. In the coming models, we will try to integrate actual *empty methods*, however, more planning information will be required.

3.1.3 Constraint Graph Model

A similar yet not equivalent ideas can be viewed in the book Automated Planning: theory and practice (Chapter 11, STN Planning) [6].

The constraint graph model will be the first in the series of models that will allow actual usage of $empty\ methods$. For this purpose, we will redefine $task\ network$ and $method\ decomposition$. $Task\ network$ will be represented with a directed acyclic graph (DAG) displaying the evolution of the $initial\ task\ network$ into the $primitive\ task\ network$. $Method\ decomposition$ will append new directed edges to the $task\ network$ (graph). Each directed edge (u,v) determines the $compound\ task\ u$ and task ($primitive\ or\ compound$) v to which the $compound\ task\ u$ decomposes. Vertices will hold additional information about constraints. Now, let's put it all more formally.

Task network is a DAG G = (V, E) in which the set of vertices V portray primitive and compound tasks and arcs depict task decomposition done by methods. As we know, only *compound tasks* can be decomposed, which is why edges can emerge only from vertices with compound tasks. In this model, only the graph's leaves can be decomposed (which are compound tasks), otherwise, it would be possible to decompose a task multiple times, which is unwanted. Having a (nonempty) $method\ m = (compound(m), subtasks(m), constr(m))$ and a task network G with a leaf symbolizing a compound task compound (m), we can apply the method m to task network G. As a result, we get $G' = (V \cup subtasks(m), E \cup subtasks(m))$ $\{(compound(m), sub) \mid sub \in subtasks(m)\}\}$. The definition of task decomposition has one special case: unsurprisingly, an empty method. In this model, we do not want to follow practices of no-op models by forcing the planner to use a special symbol like no-op(). The desirable outcome is to support real empty methods, i.e. $T \to \varepsilon$ [C], $C = \emptyset$, meanwhile allowing the planner to check all types of constraints completely. To fulfill this requirement an empty method will also create a new special vertex denoted by \square . This vertex serves for the sake of constraints in the primitive task network. E.g. having a compound task comp and an empty method comp $\to \varepsilon$ [C] $C = \emptyset$, applying the method to the task comp would create a new vertex \square and a new directed edge $(comp, \square)$. The difference between this approach and no-op() model approach is that here the empty vertex does not have any impact on actual plan (sequence of primitive tasks). Thus, the planner does not need to integrate or use any new symbols in the solving phase of a planning problem.

Now, we should talk about the constraints and their semantics in this model. Constraints, as we know them from the previous models, have their meaning in the planning phase. Instead of having one single set with all constraints in the task network, each vertex in the graph will have its own set of constraints. Every task decomposition provided by a method creates new vertices in the graph with an empty set of constraints. If a method, $T \to T_1, \ldots, T_k$ [C] has a non-empty set of constraints then (when the application of a method takes place) they are passed to the set of constraints of a vertex which is being decomposed (in our example it is the vertex with compound task T). Before the decomposition, the set of constraints of T was empty. For this purpose, each vertex in the graph is a pair of vertex and the set of constraints linked to that task. Primitive tasks' set of constraints is always empty due to the inability to decompose.

The constraints can be checked only when the *task network* is *primitive* and *a plan* $\pi = (a_1, \ldots, a_k)$ is assembled. At this point, we can start with the bottom-up analysis of the graph to check all of the constraints in all of the vertices. Starting

from the leaves which have no constraints in their vertices, the information (task position) about the *primitive tasks* is propagated to the parent vertices which might have some constraints. If a *compound task* has constraints then the information about *primitive tasks* alongside total-ordering created by the *plan* π (not be confused with total-, partial-order *planning domains*) can easily serve for an efficient constraint checks. Now let's put it more formally and clearly.

A plan $\pi = (a_1, \ldots, a_k)$ (with the parallel states (s_0, \ldots, s_k)) is created from the primitive task network, i.e. all leaves of the graph are either empty vertices \square or vertices representing primitive tasks. The plan π is created only from the primitive tasks but before that, we need to find a total ordering of **all** leaves, including empty vertices \square . For that, each leaf is assigned a natural number ranging from 1 to the number of leaves. Having a leaf vertex v, its ordering can be viewed with the function order(v). Along the actual plan π we also need a preplan ϕ , that is a plan that also contains empty vertices in the proper places. ϕ is created with the order function. Having $\phi = (x_1, \ldots, x_l)$, we can create a parallel series of states (s_0, \ldots, s_l) such that $\gamma(s_{i-1}, x_i) = s_i$ if x_i is an action, and $s_{i-1} = s_i$ if x_i is an empty vertex. This preplan is then used to check constraints.

Let $m = T \to T_1, \ldots, T_k$ [C] be a method and $U, V \subseteq \{T_1, \ldots, T_k\}$. Then, the constraints defined earlier in Definition 10 are checked accordingly:

- $T_i \prec T_j$ in a valid solution plan, all primitive tasks and empty vertices in a sub-tree with a root vertex T_i must precede (using the function order) all primitive tasks and empty vertices in a sub-tree with a root vertex T_j ,
- $before(p, U) p \in s_{i-1}$, i is the minimal value of *primitive tasks* and empty vertices (using *order* function) in sub-trees with roots U,
- $after(U, p) p \in s_i$, i is the maximal value of *primitive tasks* and empty vertices (using *order* function) in sub-trees with roots U,
- between(U, p, V) p must hold in states that target after(U, p), before(p, V), and in all states in between.

On contrary to previous models and definitions, in this model the tasks and constraints are not erased nor modified from the *task network*, they are only appended. This practice does not create any inconsistent state, because, in the end, all of the constraints in all vertices must be satisfied for a *plan* to be valid.

A solution to the planning problem is a plan $\pi = (a_1, \ldots, a_k)$ that is applicable to the initial state. Moreover, all constraints must be satisfied for each vertex in the constraint graph. The scope of constraints located in a vertex has constraints only for the sub-tree of the given vertex. This feature is possible since the constraint graph is directed and acyclic.

The constraint graph model allows planners to create and verify plans without the demand of new symbols for the representation of *empty methods*. Since the constraints are appended to the model, rather than adjusted, it is possible to spot constraint collisions much earlier. The downside of this model is the graph itself which will need additional space for storing information.

By extending this model and the decomposition definition, it would be possible to use *state-constraints* targeting a decomposing task because the decomposed task is not removed from the graph. For example, $T \to \varepsilon$ $[C], C = \{before(p, T)\}$ would create a new empty vertex \Box , and later, during the phase of constraint checking, the check would be made in $s_{order(\Box)-1}$ (in the preplan ϕ).

3.1.4 Index-Based Model

In this subsection, we will inspect a model that will combine ideas of a task network defined in Definition 9 and a constraint satisfaction problem [7]. The core idea lies in two functions: start(t) and end(t) with t being a task (primitive or compound). These two functions indicate the beginning and the end of the task, or, in other words, the first and the last primitive task in plan to which the task decomposes. If the task is already primitive then start(t) = end(t), and at the same time, this value means the position of the primitive task in a valid plan. The image of functions start and end is $\mathbb{N} \cup \{n+0.5 \mid n \in \mathbb{N}_0\}$. The image of these functions is differentiated between natural numbers which express actions that actually do something (primitive tasks) and so-called half-indices which represent *empty methods*. The meaning behind half-indices is that the task that expresses no action or an *empty method* points to a specific place between tasks. This helps the planner to identify the location of empty methods and to check all constraints properly. The Index-based model is also allowing real empty methods for the cost of extra information that is needed during the planning phase. Like the constraint graph model, the index-based model does not modify the set of constraints, instead, it appends new constraints that need to be satisfied.

Task network, contrary to the constraint graph model, is a pair $\omega = (U, C)$ as in Definition 9. Tasks in U are the inputs to the index functions start and end. The actual indices of tasks are not known until the task network is primitive and a valid plan is found. Even though the task network definition is unchanged, the method decomposition differs in this model. Let us be given a method $m = T \rightarrow T_1, \ldots, T_k$ [Constr] and a task network $\omega = (V, C)$ with a compound task $T \in V$, the decomposition is as follows:

$$\delta(\omega, T, m) = ((V - \{T\}) \cup \{T_1, \dots, T_k\}, C \cup Constr \cup \{c\}).$$

As we can see, we only remove the task T from the set of tasks V in a task network but do not touch any of the existing constraints. New constraints are only added, never modified. For each task $t \in \{T_1, \ldots, T_k\}$ we create new variables start(t) and end(t).

Because we remove the decomposed task T, we need to set up and bind constraints between the removed task and its subtasks (if the method is not empty). That is done with the newly added constraint c in this way:

- $start(T) = min\{start(t')|t' \in \{T_1, \dots, T_k\}\},\$
- $end(T) = max\{end(t')|t' \in \{T_1, \dots, T_k\}\}.$

If the *method* is empty (no subtasks), then we add specific constraint start(T) = end(T) and reduce the image of these functions to half-indices, i.e. $\{0.5, 1.5, \dots\}$.

The meaning of this constraint is that the *empty tasks* (tasks that decompose to nothing via *empty methods*) lie in between tasks that do something (in special cases, before the first *primitive task* or after the last *primitive task* in a *plan*). There is also a possibility that the *primitive task network* would have no tasks at all, in this case, all tasks figuring in a planning phase would point to index 0.5 which indicates the state before the *application* of the first *primitive task* which is equal to the *initial state* in a *planning problem*.

The index-based model allows analogous constraints as Definition 9. Constraint checks are achieved via indices in the following way:

- $T_i \prec T_j$: $\lfloor end(T_i) \rfloor < \lceil start(T_j) \rceil$,
- before(p, U): $before(p, \lceil start(U) \rceil)$,
- after(U, p): $after(\lfloor end(U) \rfloor, p)$,
- between(U, p, V): $between(\lfloor end(U) \rfloor, p, \lceil start(V) \rceil)$,

where $start(U) = min\{start(t) \mid t \in U\}$ and $end(U) = max\{end(t) \mid t \in U\}$.

Let us be given a primitive task network $\omega = (U, C)$, a plan $\pi = (a_1, \ldots, a_k)$ (with the associated sequence of intermediate states (s_0, \ldots, s_k)) is the solution to the planning problem if the task network was decomposed from the initial task network using methods from the planning domain and all constraints in C are satisfied:

- $before(p, I \in \{1, ..., k\}): p \in s_{I-1},$
- $after(I \in \{1, ..., k\}, p): p \in s_I,$
- between(I, p, J): $(\forall f)$: $I \leq f < J$: $p \in s_f$.

Another constraints for the solution are:

- $(\forall t): 0.5 \leq start(t) \leq 0.5 + k$, where k is the length of a plan
- $(\forall t): 0.5 \le end(t) \le 0.5 + k$, where k is the length of a plan.

This way, we make sure that the images of functions *start*, *end* are not widespread more than needed.

All empty tasks are mapped to correct half-indices. At the same time the constraints semantics work properly. Multiple empty tasks can have the same values of start and end. Suppose a task t1 with function values start(t1) = end(t1) = 3.5 and a task t2 with identical function values. Due to ceiling ($\lceil \rceil$) and floor ($\lfloor \rfloor$) functions there is no collision in ordering-constraints: $t1 \prec t2$: $\lfloor 3.5 \rfloor < \lceil 3.5 \rceil$. State conditions are also checked correctly with the empty tasks. A task t1 with function values start(t1) = end(t1) = 3.5 is placed correctly between the third and fourth action. In this example, both $before(p, \{t1\})$ and $after(\{t1\}, p)$ are checked in the same state s_3 because $before(p, \lceil 3.5 \rceil)$: $s_{\lceil 3.5 \rceil - 1}$ and $after(\lfloor 3.5 \rfloor, p)$: $s_{\lfloor 3.5 \rfloor}$. This behavior makes perfect sense by cause of the fact that empty tasks do not change the state in any sense. Indeed, the state to be checked is after the last applied action in a plan before the empty task.

Moreover, every solution plan $\pi = (a_1, \ldots, a_k)$ regarding the constraints or a planning domain must satisfy these properties:

- for each task t: $start(t) \leq end(t)$,
 - that is obvious from the fact that the start values are minimized and end values are maximized,
- in totally-ordered domains each compound task T decomposed to nothing holds start(T) = end(T) (which is half-index),
 - task T is decomposed into nothing. That means, T is not decomposed into any of *actions* thus all of the subtasks of T, his "grand-subtasks" and so on must have only half-indices as values of start, end. With that, start(T), end(T) must have also half-indices,
 - suppose, that there is T such that $start(T) \neq end(T)$ (both half-indices), this would mean that there exist an action that is placed in between indices start(T) and end(T) but that contradicts with total-ordering and the fact that T is decomposed into nothing (this action would be decomposed from T),
- if two compound tasks t1, t2 with start(t2) < end(t1) < end(t2) (and t1 is not decomposed from t2) exist then the planning domain is not totally-ordered,
 - tasks in totally-ordered domains that are not decomposed from each other (independent tasks) have disjunctive intervals created with start, end. Two independent compound tasks might have identical values of start and end but only if they point to the half-index. This is the only possible interleaving.
 - this property is possible only in partially-ordered domains,
- no two compound tasks t1, t2 can have identical values of start or end functions (also start(t1) with end(t2)) if they both point to the full-index and t1 is not decomposed from t2 (and vice versa),
 - each action has an unique index (position in the plan). Having two independent compound tasks and an action, at most one of those tasks can have this action in their decomposition tree. Therefore, at most one of those tasks can use this index,
- if a compound task t1 has only one subtask t2 then start(t1) = start(t2) and end(t1) = end(t2) holds,
 - trivial,
- a half-index start/end(t) = k + 0.5, $k \in \mathbb{N}_0$ indicates that exactly k actions (primitive tasks) precede this empty task.
 - each action is associated with a unique full-index.

Many more properties could be found, these are just some of them.

Similarly to the previous model, this model would also allow *empty methods* with *state-constraints* targeting the decomposed task. This constraint would be added to *the task network* and treated as a normal constraint.

3.1.5 Increment-Based Model

For our last example of HTN semantics handling empty methods, we will look at a model with a special context. This time, we will only concern totally-ordered (TO) planning domains. Moreover, for simplicity, we will omit the between-constraint as it can be simulated with the before-constraint and after-constraints (will be shown in Algorithm 1). Totally-ordered domains have all methods totally-ordered, that is: for every method $(T \to T_1, \ldots, T_k [C]) \in M$: for every $T_i, T_j \in \{T_1, \ldots, T_k\}, i \neq j$: $T_i \prec T_j$ or $T_j \prec T_i$. This special subclass of planning domains is more strict about ordering than partially-ordered (PO) planning domains, nonetheless, it allows us to operate with methods and state-constraints beneficially.

Furthermore, in this model, we will introduce the first model transformation techniques but only in the sense of *task decomposition*. More to this topic will be presented in the following chapter.

The increment-based model tries to solve issues of *empty methods* caused by Definition 10 directly. The semantics of this model are somewhat special and differ from the previous semantics. In this model, not only the *method* selection matters but also the order of the *method* (especially *empty methods*).

The main problem with the Definition 10 is the task decomposition using an empty method. In this case, all constraints containing a decomposed task are removed, and new modified constraints should be added but because we do not have any subtasks, we cannot say with certainty the semantics of the result task network. To solve this problem, we need to deal with ordering-constraints and state-constraints.

Now we will redefine task decomposition that will allow usage of empty methods. As was said earlier, we are only concerned about totally-ordered planning domains. Having a method $m = T \to T_1, \ldots, T_k$ [Constr], $k \ge 0$, a task network $\omega = (U, C)$ with a compound task $T \in U$, the decomposition δ is defined followingly:

$$\delta(\omega, T, m) = ((U - \{T\}) \cup \{T_1, \dots, T_k\}, C' \cup Constr),$$

where C' is a modification of C:

- replace each ordering-constraint containing T with new ones containing $\{T_1, \ldots, T_k\}$, i.e., $\forall i \in \{1, \ldots, k\} : T \prec x$ is replaced with $T_i \prec x$ and $x \prec T$ is replaced with $x \prec T_i$. If k = 0, then we just remove all ordering-constraints containing T,
- replace each before-, after-constraint containing T with new ones containing $\{T_1, \ldots, T_k\}$. For example, we would replace before-constraint before (p, V) with $before(p, (V \{T\}) \cup \{T_1, \ldots, T_k\})$. If k = 0, then we have two distinct situations. Either we remove one of the tasks or the last task in the set. Now, let's break down different outcomes:
 - $before(p, V), T \in V, |V| > 1$: we only remove the task T and replace before(p, V) with $before(p, V \{T\})$,
 - before $(p, V), T \in V, |V| = 1$: we find strict total order on the set U (tasks of the task network ω) $T_i \prec T_j \prec \cdots \prec T_k$, and locate the index d of the decomposed task T. After that, we include a new constraint

before $(p, \{T_{d+1}\})$ into the set of constraints and remove the former constraint before (p, V). If T_{d+1} does not exist then we create a new constraint after $(\{T_{d-1}\}, p)$. If T_{d-1} also does not exist then T is the only task in ω , we can remove the task from the task network but the planner needs to check if the initial state s_0 contains required propositional symbol p,

- $after(V, p), T \in V, |V| > 1$: we only remove the task T and replace after(V, p) with $after(V \{T\}, p)$,
- $after(V,p), T \in V, |V| = 1$: we find strict total order on the set U $T_i \prec T_j \prec \cdots \prec T_k$, and locate the index d of the decomposed task T. After that, we include a new constraint $after(\{T_{d-1}\}, p)$ and remove the former after(V, p) constraint. If T_{d-1} does not exist, we include $before(p, \{T_{d+1}\})$. If T_{d+1} also does not exist then T is the only task in ω , we can remove the task from the task network but the planner needs to check if the tinitial tini

One might ask, why do state-constraints concern sets of tasks rather than just a single task? In the totally-ordered domains a single task is sufficient enough. The explanation is that there might be multiple orderings of the methods and each of the orderings might give a different result. This semantics acts differently from the previous models because here we prioritize primitive tasks to empty tasks. Different sequences of empty method decomposition shift the state to be checked based on the remaining tasks of a state-constraint. If there are no tasks left then we shift the constraint to the next (or previous) task. We can see, that with the different sequences of the task decomposition constraint might end up attached to different tasks.

Example 7. In this example, we will show how the order of methods might have different resulting task networks. Suppose, we have a task network $\omega = (\{T_1, T_2, T_3\}, \{T_1 \prec T_2 \prec T_3, before(p, \{T_1, T_3\})\})$ and two empty methods $m_1 = T_1 \rightarrow \varepsilon$ [{}], $m_2 = T_3 \rightarrow \varepsilon$ [{}].

```
If we start with m1: (\{T_1, T_2, T_3\}, \{T_1 \prec T_2 \prec T_3, before(p, \{T_1, T_3\})\}) \rightarrow (\{T_2, T_3\}, \{T_2 \prec T_3, before(p, \{T_3\})\}) \rightarrow (\{T_2\}, \{after(p, \{T_2\})\}).

If we start with m2: (\{T_1, T_2, T_3\}, \{T_1 \prec T_2 \prec T_3, before(p, \{T_1, T_3\})\}) \rightarrow (\{T_1, T_2\}, \{T_1 \prec T_2, before(p, \{T_1\})\}) \rightarrow (\{T_2\}, \{before(p, \{T_2\})\}).
```

It would be also possible to match previous models by allowing only a single task in *state-constraints*. This way, each *empty method* would shift the constraint to the adjacent task. This behavior is equivalent to the previous models.

Now, we will discuss constraint modification. First of all, we will look at the ordering-constraint. A compound task that is decomposed with an empty method is not relevant from the perspective of ordering as this task does not do anything. Hypothetically, between each two actions there is an infinite amount of virtual empty tasks, none of them is relevant to the task network or the resulting plan. For this reason, all ordering-constraints containing the decomposed empty task can be removed.

On the other hand, state-constraints cannot be removed from the task network because they are telling the planner that they need to be checked at some point in the planning phase. Having an empty method that decomposes a compound task T, all state-constrains containing T needs to be modified as this task will be deleted from the task network. With our model, we only remove the task from all constraints if the set of tasks in a particular constraint has more than one element. It could also be possible to modify all constraints right away but, for convenience, we have decided to do it this way. If the decomposed task is the last one then we have to modify all constraints holding T to prevent undefined behavior. Since the task is empty it will produce no actions, meaning that there will be no transition between states. The state before the compound task T is identical to the state after the T. For this reason, it is possible to easily modify all existing state-constraints containing T. The key for the constraint modification is the fact that the planning domain is totally-ordered. At any point of planning, we can construct a strict total ordering of the tasks and shift the constraints to the next or the previous task in the ordering.

With the increment-based model, we have finished our list of HTN semantics that solve the problem of *empty methods*. The first two semantics do not allow usage of real *empty methods* meanwhile the last three allow them. Different semantics might be beneficial in different situations, depending on the *planning domain*. Some future software for hierarchical planning might even combine various features from the semantics presented, but that is left for future work.

4 Transformations of HTN Models

After an enumeration of various definitions and semantics, we will finally start discussing the transformation of different HTN models. This chapter will exhibit varying transformations along divergent contexts and preconditions. For example, HTN models might be partially-ordered, totally-ordered, with or without *goal tasks*, having a different set of allowed *state-constraints*.

4.1 Normal Forms

The first section of this chapter is inspired by the Chomsky normal form (ChNF) [1]. A context-free grammar (CFG) is in ChNF if all of its production rules are of the form: $A \to BC$, $A \to a$, $S \to \varepsilon$ (in this case S cannot be on the right side of a production rule) where A, B, C are nonterminal symbols, a is a terminal symbol, S is a starting nonterminal symbol, and ε denotes an empty symbol. This "nice" form of CF grammar allows us to prove important theorems about CF languages more easily. Similarly, we want to have "nice" forms of planning domains without empty methods which might speed up algorithms for planning, or plan verification. Also, these forms are useful for proving HTN theorems [3] [4].

Definition 14. [3] A hierarchical planning problem $\mathcal{P} = (s_0, \omega, \mathcal{D})$ is said to be in $NF_{\geq 2}$ if all methods are of the form: $T \to T_1, \ldots, T_k$ [C], $k \geq 2$; $T \to a$ [C] where T, T_1, \ldots, T_k are compound tasks, and a is a primitive task (action).

Definition 15. A hierarchical planning problem $\mathcal{P} = (s_0, \omega, \mathcal{D})$ is said to be in HTN-ChNF if all of its methods are of the form: $T \to T_1, T_2$ [C]; $T \to a$ [C] where T, T_1, T_2 are compound tasks, and a is a primitive task.

In Definitions 14, 15 we exclude the possibility of having empty *plans* but this decision can be interchanged at any time. Moreover, these definitions do not allow *empty methods*.

Definition 16. We say that two planning problems \mathcal{P}' , \mathcal{P}'' are equivalent if the set of solutions of \mathcal{P}' is equal to the set of solutions of \mathcal{P}'' .

Definition 17. A method $T \to T_1, \ldots, T_k$ [C] has linear ordering-constraints C if subtasks can be split into disjunctive sets (set partition) $S_1, \ldots, S_k, k \ge 1$ such that all ordering-constraints between tasks are within the same set, and all tasks within one set S_i are linearly ordered (if any two tasks aren't comparable within a set directly then we apply a transitive closure). Tasks not contained in any of ordering-constraints are in sets of one element.

Definition 18. A hierarchical planning problem $\mathcal{P} = (s_0, \omega, \mathcal{D})$ is said to be in HTN-GNF [10] if it is TO and all of its methods are of the form: $T \to a, T_1, T_2, \ldots, T_i$ [C], $i \geq 0$; where T, T_i are compound tasks, and a is a primitive task.

Theorem 5. Every planning problem \mathcal{P} (partially-, totally-ordered) that does not generate an empty plan as a solution, without state-constraints (before, after, between) can be transformed into an equivalent planning problem in $NF_{\geq 2}$.

Proof. The proof follows the ideas of the transformation of CFG into ChNF [3]. First of all, we need to get rid of empty methods. For that, we need to find all nullable compound tasks. A compound task T is nullable if a method $T \to \varepsilon$ [$\{\}\}$] exists, or if there is a sequence of decomposition such that $T \to \cdots \to \varepsilon$ [C]. Nullable compound tasks can be found followingly: for each method $T \to \varepsilon$ [$\{\}\}$], T is nullable, and for each method $T \to T_1, \ldots, T_k$ [C], $k \ge 1$ where T_1, \ldots, T_k are nullable, T is also nullable (actions are never nullable). Having all nullable tasks, we can remove empty methods from the domain. After that, for each method $T \to T_1, \ldots, T_k$ [C] holding $i \ge 1$ nullable tasks as subtasks, we create 2^i new methods with/without nullable tasks, one special case is if i = k then we do not create a new empty method $T \to \varepsilon$ [C]. All ordering-constraints containing removed tasks are also removed in each new method.

The next step is to remove methods of a form $T \to T_1$ [{}] where T, T_1 are compound tasks. These methods will be called - unit methods. For that, we need to find all unit pairs. A unit pair (T_1, T_2) $T_1 \neq T_2$ is a pair of compound tasks such that T_2 can be decomposed from T_1 only with the usage of unit methods, i.e., $T_1 \to \cdots \to T_2$ [C]. After that, for each unit pair (T_1, T_2) and for each non-unit-method $T_2 \to T_i, \ldots, T_j$ [C₂], i < j, we create a new method: $T_1 \to T_i, \ldots, T_j$ [C₂], i < j (ordering-constraints are inherited from the second method). Doing so, we can delete all unit-methods from the planning problem without the modification of solutions.

For each action a we produce a new compound task T_a , a new method $T_a \to a$ [{}], and for each method $T \to T_1, \ldots, T_k$ [C] having a as a subtask we delete a from the subtasks and include T_a instead. All ordering-constraints having a are interchanged with ones containing T_a .

In this proof, we deleted all empty methods, unit methods, and modified methods so they have single action or compound tasks as subtasks. Thus, all methods left have a form: $T \to T_1, \ldots, T_k$ [C], $k \ge 2$; $T \to a$ [{}] where T, T_1, \ldots, T_k are compound tasks, and a is action. In every step, we did not create nor remove any potential solution.

Theorem 6. Every planning problem \mathcal{P} in $NF_{\geq 2}$, with all methods containing only linear ordering-constraints, without state-constraints (before, after, between) can be transformed into an equivalent planning problem in HTN-ChNF.

Proof. In this proof, we will need to divide the large *methods* into smaller ones. Because all tasks are linearly ordered within the divided sets we know that there cannot be "ordering cycles", also we know that at every time in every task set, there is the first task, with respect to *ordering-constraints*. A key feature of such constraints is that the tasks in sets are mutually independent because, from the definition, no *ordering-constraints* exist between tasks from different sets.

Let us have a method $T \to T_1, \ldots, T_k$ $[C], k \geq 3$, and a set partition of tasks $S_1, \ldots, S_k, k \geq 1$ by the Definition 17. Now, we will transform the input planning problem \mathcal{P} into the result HTN-ChNF planning problem in two steps. First, we will add new compound tasks S_1, \ldots, S_k (same names as set partitions) and k-2 C_i compound tasks to the planning problem. After that, we will add new methods:

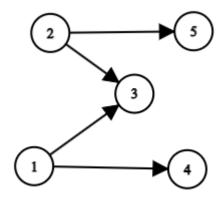


Figure 4.1 Unbinarizable graph

 $T \to S_1, C_1$ [{}]; $C_1 \to S_2, C_2$ [{}]; ...; $C_{k-2} \to S_{k-1}, S_k$ [{}]. Newly created methods have an empty set of constraints because, as was mentioned, tasks from different partitions do not have any ordering relations between them. Therefore, their subtasks can interleave without any restrictions.

One special case that might occur is if the set of subtasks is fully linearly ordered then there will be only one partition S_1 . This situation can be handled easily. We will start the process of binarization right away. Similarly to the previous process, we will create k-2 X_i compound tasks. After that, we will append new methods: $T \to T_1, X_1$ [$\{T_1 \prec X_1\}$]; $X_1 \to T_2, X_2$ [$\{T_2 \prec X_2\}$]; ...; $X_{k-2} \to T_{k-1}, T_k$ [$\{T_{k-1} \prec T_k\}$] where T_1 is the first element with respect to ordering-constraints, T_2 is the second element and so on.

In the case of multiple sets S_1, S_2, \ldots , we repeat the process above for each compound task S_i and for each partition S_i independently. Doing so, we can delete the former method. We iterate this process for all methods with at least 3 tasks as subtasks.

Example 8. If we want to binarize a planning domain then we can use different types of ordering-constraints. Method's subtasks are binarizable if they can be split into two disjunctive sets of subtasks such that all subtasks in one set precede all subtasks in the second set, or if all subtasks in the first set have none order-constraints with the second set of subtasks. A method is binarizable if this process of splitting into two sets can be done repeatedly until all sets have a single task as an element.

Using graphs (DAG) terminology where tasks are nodes and an arc (a,b) exists if an order-constraint $a \prec b$ exists, we can say that the graph can be split if it contains ≥ 2 components, or a vertex u exists such that in every topological sorting u has the same position. If such a vertex exists then we know that all vertices with a higher number must come after u and other vertices before. Thus we have 2 disjunctive sets of vertices and u can be added to either of these two sets. A graph is binarizable if this process can be repeated until only single vertex is left.

Figure 4.1 shows us the smallest DAG that is not binarizable. Now we understand the reason for our choice of the linear ordering-constraints in which we can always find the first or the last element.

Theorem 7. Theorem 5 transforms a planning problem \mathcal{P} with all methods having

linear ordering-constraints into a planning problem in $NF_{\geq 2}$ with all methods having linear ordering-constraints.

Proof. Theorem 5 includes two main parts: removing all empty methods and unit-methods. The elimination of unit-methods does not have any effect on ordering because we need at least two tasks for an ordering-constraint. We create new methods without nullable tasks which also deletes constraints containing these tasks. But because the ordering is linear even after the deletion of some elements (transitive closure from the definition) we do not create methods that are not linear ordering-constraints.

4.2 Totally-Ordered Transformations

Before we start with the transformation of totally-ordered planning problems we need to tidy up state-constraints. So far, state-constraints are defined on sets of subtasks, i.e., before(p,U), after(U,p), between(U,p,V) with U,V denoting subsets of subtasks, and p denotes a propositional symbol. TO planning problems allow us to remove unnecessary tasks from sets U,V leaving us with only one subtask. Hence, we abuse the notation to let before(p,T) denote $before(p,\{T\})$ with T being a method's subtask. Similarly, we will use this notation for after and between constraints.

Theorem 8. For each TO planning problem there is an equivalent planning problem with all state-constraints operating with tasks instead of sets of sets of tasks.

Proof. Let us have a method $T \to T_1, \ldots, T_k$ $[C], k \ge 1$, and a before $(p, U) \in C$. This constraint can be transformed to before (p, T) such that $T \in U$ and $(\forall F \in (U - \{T\})) : T \prec F$. This can be done analogously for each after(U, p) and between(U, p, V) constraint. If the result between(U, p, V) constraint is of a form between(T, p, F) and $F \prec T$ holds then this whole constraint can be removed from the set of constraints as there are none states to test this constraint. \square

Now, all *TO* domains will implicitly have only *state-constraints* described in Theorem 8.

In the following parts, we will try to convert general TO planning problems into ones of a HTN-ChNF. Initially, we will compile away between constraints because this type of state-constraint spans throughout states which is undesirable. This behavior complicates the conversion because the HTN-ChNF has at most two tasks as subtasks. In this case (HTN-ChNF), the between (T_1, p, T_2) constraint is saying that the check is made before the application of the first action to which T_2 decomposes, after the last action to which T_1 decomposes, and also all states in between are checked. This means that the test is made in a single state after the last action of T_1 . This can be easily transformed to a single before-after-constraint. Complications with between-constraints begin if we have at least three TO subtasks $T_1 \prec T_2 \prec T_3$ and a between (T_1, p, T_3) constraint. Having this, the check has to be made in (potentially) multiple states depending on a

decomposition tree of a compound task T_2 . Transformation of this feature becomes difficult if we do not want to lose any information about a planning domain.

In [7] [8] it is described how to get rid of between constraints from TO planning problems by adding a series of before constraints. This conversion is false as it does not concern all states between subtasks but only states before the first action to which potential compound tasks decompose. Compiling away between constraints is more complicated but not impossible. The Algorithm 1 below shows how to do it properly.

In the following Algorithm 1, we will create new compound tasks that are derived from the existing ones. Let us have a compound task T. A new compound task $T_{\{p,q\}}$ (same name but with a suffix) denotes that in every possible decomposition tree starting from $T_{\{p,q\}}$ all methods do not contain any between constraints, and every primitive task network derived from the $T_{\{p,q\}}$ holds propositional symbols $\{p,q\}$ in every state. These new compound task will be replaced in methods containing between constraints, and as a result, it will allow us to remove these constraints. Also, we will use the notation before (Q,T) with T being a task and $Q \subseteq P$ being a subset of propositional symbols. before (Q,T) is just an abbreviation for a before (q_1,T) , before (q_2,T) , ... where $q_i \in Q$.

Theorem 9. For each TO planning problem there is an equivalent planning problem without any between-constraint.

Proof. First of all, we will compile away between-constraints of the neighboring tasks, i.e., tasks $T_1 \prec T_2$ such that no task T_i exist with $T_1 \prec T_i$ and $T_i \prec T_2$. As was said before, these constraints can be interchanged to a single before-constraint (between $(T_1, p, T_2) = before(p, T_2)$). Between-constraints of a form between (T_i, p, T_i) or between (T_j, p, T_i) with $T_i \prec T_j$ are pointless and can be removed without any loss of information.

The idea of the Algorithm 1 is to remove between-constraints method by method with a procedure that might remind us of Depth-first search (DFS). Suppose a method M includes at least one between-constraint. In every valid solution of the planning problem \mathcal{P} that employs M during the planning phase, there must exist a consecutive sub-plan that is decomposed from the compound M and contains the propositional symbol specified in the constraint.

If we want to remove between(T, p, F) constraint then we must ensure that all decompositions (even those with cycles) of all *compound tasks* between T and F (with respect to TO) hold $propositional\ symbol\ p$.

An algorithm is split into two distinct parts: the while-loop (3) in the Main function and a recursive function SearchCompoundTask (23). The main cycle removes all between-constraints from a single method per iteration meanwhile not creating any new between-constraints. All compound tasks that are mentioned in between-constraints are substituted with new compound tasks that are stored in an auxiliary set NewCT (2). If a substituted compound task is already stored in NewCT then we do not have to recursively search this task with SearchCompoundTask function (17, 38). On the contrary, if the task is not searched then we need to create new methods so that tasks from other methods cannot be decomposed via methods designed for the substituted tasks (7, 33).

The recursive procedure SearchCompoundTask looks for all *methods* that decompose the input *compound tasks* and append constraints so that the *propositional*

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Algorithm 1 TO into TO without between-constraints
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1: procedure MAIN(TO planning problem: \mathcal{P} = (s_0, \omega, \mathcal{D}))
        NewCT \leftarrow \{\}
                                                             ▶ New Compound Tasks
 2:
        while \mathcal{D} contains a method m with a between-constraint do
 3:
           for each compound task CT in subtasks(m) that is part of \geq 1 between-
 4:
    constraints do
               PropSymbols \leftarrow \{p : between(T, p, F) \ and \ T \prec t \prec F\}
 5:
 6:
               if CT_{PropSymbols} not in NewCT then
                   find methods m' with CT = compound(m') and create new
 7:
    M = (CT_{PropSymbols}, subtasks(m'), constraints(m'))
               end if
 8:
               swap all occurrences of CT with CT_{PropSymbols} in a method m
 9:
           end for
10:
           for each task t in subtasks(m) do
11:
12:
               PropSymbols \leftarrow \{p : between(T, p, F) \ and \ T \prec t \prec F\}
                       \triangleright if PropSymbols = \emptyset then constraints are always satisfied
13:
               add before(PropSymbols, t), after(t, PropSymbols) to m
14:
           end for
15:
           remove all between-constraints from constraints(m)
16:
17:
           for each CT_{symbols} in subtasks(m) (CT_{symbols} not in NewCT) do
               NewCT \leftarrow NewCT \cup CT_{symbols}
18:
               SearchCompoundTask(CT_{sumbols})
19:
20:
           end for
        end while
21:
    end procedure
22:
   procedure SearchCompound Task( Compound task: CT_{InputSymbols})
        for each method m with CT_{InputSymbols} = compound(m) do
24:
           for each task t in subtasks(m) do
25:
               PropSymbols \leftarrow \{p : between(T, p, F) \ and \ T \prec t \prec F\}
26:
               add before(PropSymbols \cup InputSymbols, t) to m
27:
               add after(t, PropSymbols \cup InputSymbols) to m
28:
           end for
29:
30:
           for each compound task CT in subtasks(m) do
               PropSymbols \leftarrow \{p : between(K, p, L) \ and \ K \prec T \prec L\}
31:
32:
               if CT_{PropSymbols \cup InputSymbols} not in NewCT then
33:
                   find methods m' with CT = compound(m') and create new
    M = (CT_{PropSymbols \cup InputSymbols}, subtasks(m'), constraints(m'))
34:
               end if
               swap all occurrences of CT with CT_{PropSymbols \cup InputSymbols} in m
35:
36:
           end for
           remove all between-constraints from constraints(m)
37:
38:
           for each CT_{symbols} in subtasks(m) (CT_{symbols} not in NewCT) do
39:
               NewCT \leftarrow NewCT \cup CT_{symbols}
40:
               SearchCompoundTask(CT_{sumbols})
           end for
41:
        end for
42:
43: end procedure
```

symbols are checked in all states concerning the subtasks (27, 28). Also, the recursive procedure removes all between-constraints during the search (35), so they are not found in the main while-loop.

There is a finite number of propositional symbols, methods, compound tasks, and new compound tasks in NewCT. Therefore, the algorithm will not fall into an infinite cycle, and gradually all between-constraints will be removed. \Box

Theorem 10. For each TO planning problem that does not generate empty plan as a solution, there is an equivalent planning problem without empty methods.

Proof. First, we will remove all between-constraints with the Theorem 9.

Similarly to Theorem 5, we will need to find all $nullable\ tasks$ in $a\ planning\ problem$ and create new methods without these tasks. The difficult part is handling the before-, after-constraints which need to be checked eventually. $A\ nullable\ task$ may have many different series of decompositions that lead to an empty set of tasks. Each of these decompositions may have different constraints that need to be checked. For this purpose, we will use a function Nullifies(T) that accepts a $nullable\ compound\ task$ and returns a set of sets of $propositional\ symbols$. Each element of the function's output represents one possible way of how we can decompose this $compound\ task$ and which $propositional\ symbols$ need to be checked.

We will find all values of the function Nullifies in the following inductive manner. **Base:** for each $T \to \varepsilon$ [{}]: $Nullifies(T) = \{\{\}\}$. **Induction:** having $T \to T_1, \ldots, T_k$ [C], $k \ge 1$ with subtasks containing only nullable compound tasks we extend $Nullifies(T) = Nullifies(T) \cup \{\{\text{propositional symbols mentioned in } C\} \cup propSym_1 \cup \cdots \cup propSym_k\}$ where $propSym_i \in Nullifies(T_i)$. The induction part is repeated until there is a new unique combination of propositional symbols that is not mentioned in Sullifies(T) with some Sullifies(T) with some Sullifies(T) and some Sullifies(T) with some Sullifies(T) and Sullifies(T) with some Sullifies(T) with some Sullifies(T) and Sullifies(T) with some Sullifies(T) with some Sullifies(T) and Sullifies(T) with some Sullifies(T) and Sullifies(T) with some Sullifies(T) and Sullifies(T) with Sullifies(T) and Sullifies(T) with Sullifies(T) with Sullifies(T) and Sullifies(T) and Sullifies(T) with Sullifies(T) with Sullifies(T) and Sullifies(T) and Sullifies(T) and Sullifies(T) with Sullifies(T) and Sullifies(T) are Sullifies(T) and Sullifies(T) and Sullifies(T) are Sullifies(T) and Sullifies(T) and Sullifies(T) and Sullifies(T) are Sullifies(T) and Sullifies(T) and Sullifies(T) and Sullifies(T) and Sullifies(T) and Sullifies(T) are Sullifies(T) and Sullifies(T) and Sullifies(T) and Sullifies(T) are Sullifies(T) and Sullifies(T) and Sullifies(T) are Sullifies(T) and Sullifies(T) and Sullifies(T) and Sullifies(T) are Sullifi

It can be easily seen that T is nullable if and only if $Nullifies(T) \neq \emptyset$ (after we have found all values). The compound task in the initial task network is never nullable as stated in the theorem. This feature will be used in the second part of the $empty\ method$ elimination.

At this point, all *empty methods* can be removed from the *planning domain*. Now, for the final part, we will append new methods with/without nullable tasks to the planning problem, similarly to Theorem 5. Suppose a method contains i nullable tasks in subtasks. Without loss of generality, nullable tasks will be T_1, \ldots, T_i . There will be $(|Nullifies(T_1)| + 1) * \cdots * (|Nullifies(T_i)| + 1)$ new methods, some of them might be identical. For each such combination, we will create a new method without (some) nullable tasks. Ordering-constraints mentioning deleted tasks are removed from the set of constraints. If we want to remove a nullable task T_i then we need to find the closest task that is not removed from the method and shift state-constraints. If the non-removed task T_k holds k < j then we create a new constraint: $after(T_k, PropSymbols), PropSymbols \in Nullifies(T_i)$. On the other hand, if k > j then we append $before(PropSymbols, T_k)$ to the set of method's constraints. It might happen that all subtasks(M) of a method M are nullable, in this case, we do not create new empty method because compound(M)will be removed from methods that contain compound(M) as a subtask. As was stated before, initial task network is never nullable, thus we do not need to handle this awkward situation.

Theorem 11. For each TO planning problem there is an equivalent planning problem without any after-constraints.

Proof. TO planning problems allow us to shift any after-constraint to the succeeding task. So, an after-constraint is changed to before-constraint. This transformation is valid with only one exception. If the after-constraint targets the last task with respect to TO then an after-constraint cannot be shifted to the following task because such task does not exist in a set of method's subtasks. One might think that we can compile this feature away using the cooperation with other methods. Still, it can happen that the targeted task will be the last action in the solution which means that the check will be evaluated in a state after the execution of all actions in the plan. Therefore, in this case, we cannot shift an after-constraint so easily. What we can do is to create a new compound task T_{empty} with one empty method. Then, this task can be inserted at the end of a method and problematic after-constraints can be shifted to the T_{empty} .

Symmetrically, we can transform all before-constraints to the equivalent after-constraints. \Box

Theorem 12. For each TO planning problem that does not generate empty plan as a solution, there is an equivalent planning problem in HTN-ChNF.

Proof. The proof is akin to proofs of Theorems 5 6 with some extra steps to handle state-constraints. At the beginning, we will use Theorem 9 to remove all between-constraints. Afterwards, we will use Theorem 10 to remove all empty methods which does not create any new between-constraints. Now we need to handle unit methods. We will find all unit pairs which is identical to the proof to the Theorem 5. Analogous to the process of discarding empty methods unit pairs might have different decompositions which lead to different sets of constraints. As for *empty methods*, we will find all such combinations of *unit pairs* with sets of constraints with the help of an auxiliary function Nulifies(T, F)with (T, F) $T \neq F$ being an unit pair. Base: for each unit method $T \to F$ [C]: $Nullifies(T, F) = \{C\}$ (if there are multiple unit methods with identical compound tasks but with different constraints then each set of constraints is added separately). Induction: having a unit pair (T, F) and a unit method $F \rightarrow$ $H[C]: Nullifies(T, H) = Nullifies(T, H) \cup \{constr_t \cup constr_h \mid (\forall constr_t \in T)\}$ Nullifies(T,F)) and $(\forall constr_h \in Nullifies(F,H))$. Hence, for each unit pair (T, F) and for each non-unit method $F \to F_1, \ldots, F_k$ [C] we create new methods for each set of constraints in Nullifies(T, F). New method is of a form $T \to F_1, \ldots, F_k \ [C \cup newC]$ where newC are newly produced constraints from $newConstr \in Nullifies(T, F)$. $newC = \{before(p, F_1) \mid before(p, X) \in$ newConstr} \cup { $after(F_k, p) \mid after(X, p) \in newConstr$ }. After that, we can remove all unit methods.

For each method with multiple subtasks with at least one primitive task as a subtask, we substitute a primitive task a with a compound task T_a . All constraints targeting a are interchanged with constraints targeting T_a . We also create a new method $T_a \to a$ [{}]. Now, our planning problem is in NF $_{\geq 2}$. To finish the proof we need to divide long methods.

For each method $T \to T_1, \ldots, T_k$ [C], $k \ge 3$ we produce k-2 C_i compound tasks, and construct new methods $T \to T_1, C_1$ $[\{T_1 \prec C_1\} \cup \{\text{all state-constraints targeting } T_1\}], <math>C_1 \to T_2, C_2$ $[\{T_2 \prec C_2\} \cup \{\text{all state-constraints targeting } T_2\}],$

...,
$$C_{k-2} \to T_{k-1}, T_k$$
 [$\{T_{k-1} \prec T_k\} \cup \{\text{all state-constraints targeting } T_{k-1}, T_k\}$].

Theorem 13. For each TO planning problem in HTN-ChNF there is an equivalent planning problem in HTN-GNF.

Proof. We assume that the planning problem does not contain any between-constraints as they can be easily eliminated 4.2 in HTN-ChNF.

The proof follows the [11] with the addition of HTN specifics. Initially, we rename *compound tasks* to A_1, A_2, \ldots, A_n in some ascending order (and substitute these new tasks in constraints). The compound task in the initial task network is renamed to A_1 .

Our next goal is to modify methods such that $A_i \to A_j$, α $[C] \Longrightarrow i < j$, where A_j is the first $compound\ task$ with respect to ordering and α , is a set of $compound\ tasks$. For this, we will iterate over A_i starting from i=1 and proceeding to i=n. Having $A_i \to A_j$, α [C], we might have two scenarios that need adjustment:

- 1. If i > j then we generate new methods substituting A_j with subtasks(M) such that $compound(M) = A_j$ for $methods\ M$. Constraints of these new methods are unioned with the old one $(constraints(M) \cup C)$. After we generate new methods we can remove the unsuitable one.
- 2. (a) If i = j then we have encountered the incompatible left recursion. To remove that, we need to handle constraints targeting A_j . Now we need to find all methods with $compound(M) = A_i$ and separate them into two groups (with/without left recursion):

$$A_i \to A_i, \alpha_1 [C_{\alpha_1}] \mid \ldots \mid A_i, \alpha_m [C_{\alpha_m}],$$

$$A_i \to \beta_1 [C_{\beta_1}] \mid \ldots \mid \beta_p [C_{\beta_p}].$$

For each $A_i oup A_i$, α [C] we remove all after-constraints targeting A_i and append new before-constraints targeting the first task in α (same state in a plan). This can always be done as we have HTN-ChNF which contains two compound tasks in subtasks (if the first one is compound). To handle before-constraints targeting A_i , we need to find all possible outcomes of all recursions. We will construct a

$$\Omega = \{ \{ p \in P \mid before(p, A_i) \in C \} \mid (A_i \to A_i, \alpha [C]) \in M \} (|\Omega| = m).$$

In other words – a set of sets with *propositional symbols* where each element is a union of *propositional symbols* found in a before-constraints targeting the first task in a method with a left recursion of A_i .

With these two groups, we eliminate left recursion by introducing new compound tasks Z_Q^R with $R \subseteq Q \subseteq \{1, \ldots, |\Omega|\}$ (Q is a set of possible decompositions, R is a set of mandatory decompositions that have not been used yet) and a bijective function $f: \{1, \ldots, |\Omega|\} \to \Omega$

(s.t. $f(j) = \{ p \in P \mid before(p, A_i) \in C_{\alpha_j} \}$). We will substitute these methods with:

$$A_i \to \beta_i \ [C_{\beta_i}] \mid \beta_i, Z_Q^Q \ [C_{\beta_i} \cup \{before(f(Q), \beta_i) \mid Q \subseteq \{1, \dots, |\Omega|\}\} \cup \{\beta_i \prec Z_Q^Q\}],$$

$$Z_Q^R \to \alpha_{q \in Q \; (R = \emptyset)} \mid \alpha_{q \in Q}, Z_Q^R \mid \alpha_{r \in R}, Z_Q^{R - \{r\}}.$$

(b) Alternatively, we could remove left recursion differently with lesser number of methods. With this approach, it could be possible to create $task\ networks$ with more state-constraints than needed, but it will not change the set of possible solutions of the domain. As in the previous approach, we will construct Ω and f. New methods will look as follows:

$$A_i \to \beta_i [C_{\beta_i}] \mid \beta_i, Z_Q [C_{\beta_i} \cup \{before(f(Q), \beta_i) \mid Q \subseteq \{1, \dots, |\Omega|\}\} \cup \{\beta_i \prec Z_Q\}],$$

$$Z_Q \to \alpha_j, Z_Q (\{p \in P \mid before(p, A_i) \in C_{\alpha_j}\} \subseteq f(Q)),$$

$$Z_Q \to \alpha_j \ (\{p \in P \mid before(p, A_i) \in C_{\alpha_j}\} \subseteq f(Q)).$$

The next step is to make sure that $A_i \to pt$, α [C] with a primitive task pt holds for all methods with $compound(M) = A_i$. For this, we will start from i = n-1 and move on to i = 1. For each i we will find all unsuitable methods $A_i \to A_j$, α [C]. These methods will be substituted with subtasks(M) and constraint(M) as was done earlier in this proof.

The same procedure will be carried out to the new *methods*, where $compound(M) = \mathbb{Z}_Q^R$.

Conclusion

In summary, the main purpose of this thesis was to provide a brief introduction to the field of planning and to explore some aspects that can be used later in other types of related work. Starting from classical planning which can be expressed in different ways and lasting with hierarchical planning, HTN to be precise. The theory of HTN is not yet unified, therefore we can find different definitions and understandings about this topic in various publications.

One of the goals was to establish proper boundaries through combinations of definitions from varying sources. By doing so, we could describe, compare, and analyze HTN semantics with the subtle goal of handling empty methods that are not handled accurately in plenty of similar papers. Difficulties start to appear if we want to use constraints that are bound to states. In addition, new types of HTN semantics were introduced.

In the last chapter of the thesis, we tried to find transformations of HTN models that might be suitable within some context. Most transformations were inspired by the theory of Automata and Grammars, yet they need a significant amount of extension as HTN models allow partially-ordered domains and state-constraints.

We have shown a few transformations regarding (mostly) TO planning domains. These transformations can be used for plan validation and recognition. Future experiments with these normal forms may result in an increased speed of computation. In particular, GNF may be useful, as in every step of a plan validation, one primitive task / action is placed.

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List of Abbreviations

AI – Artificial Intelligence

BFS - Breadth-First Search

CFG - Context-free Grammar

ChNF – Chomsky Normal Form

DAG – Directed Acyclic Graph

DFA – Deterministic Finite Automaton

DFS – Depth-First Search

GNF – Greibach Normal Form

HDDL - An Extension to PDDL for Expressing Hierarchical Planning Problems

HTN – Hierarchical Task Network

LLM – Large Language Models

PO – Partially-ordered

TO-Totally-ordered

A Attachments

A.1 First Attachment

NAME

htn-transformator - a command-line program that demonstrates some of the transformations mentioned in this text.

SYNOPSIS

htn-transformator -i INPUTFILE [--between|--empty|--tocnf]
[-o OUTPUTFILE]

DESCRIPTION

htn-transformator is a utility designed to apply specific transformations to HTN planning domains.

OPTIONS

- -i INPUTFILE Specifies the input file containing the HTN data. This option is mandatory.
- **-between** Removes all between constraints from the input planning domain.
- **–empty** Removes all between constraints and empty methods from the input planning domain.
- -tocnf Transforms the input planning domain into the HTN-ChNF.
- **-o OUTPUTFILE** Specifies an optional output file to save the result. If this option is omitted, the output is displayed to stdout.