

# Bubble sort

DATA STRUCTURES AND ALGORITHMS IN PYTHON

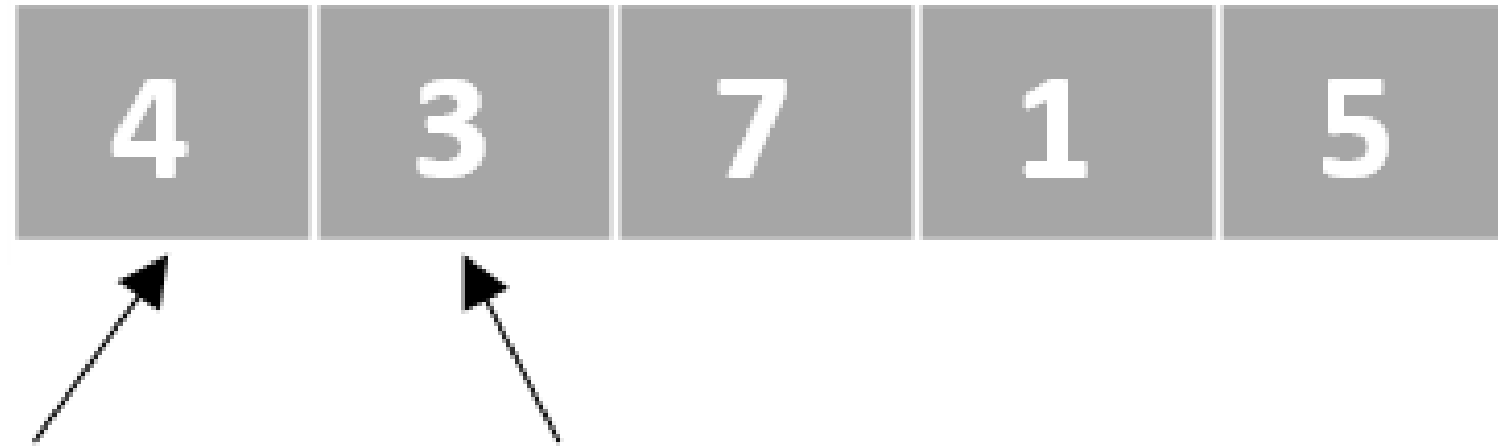


**Miriam Antona**  
Software engineer

# Sorting algorithms

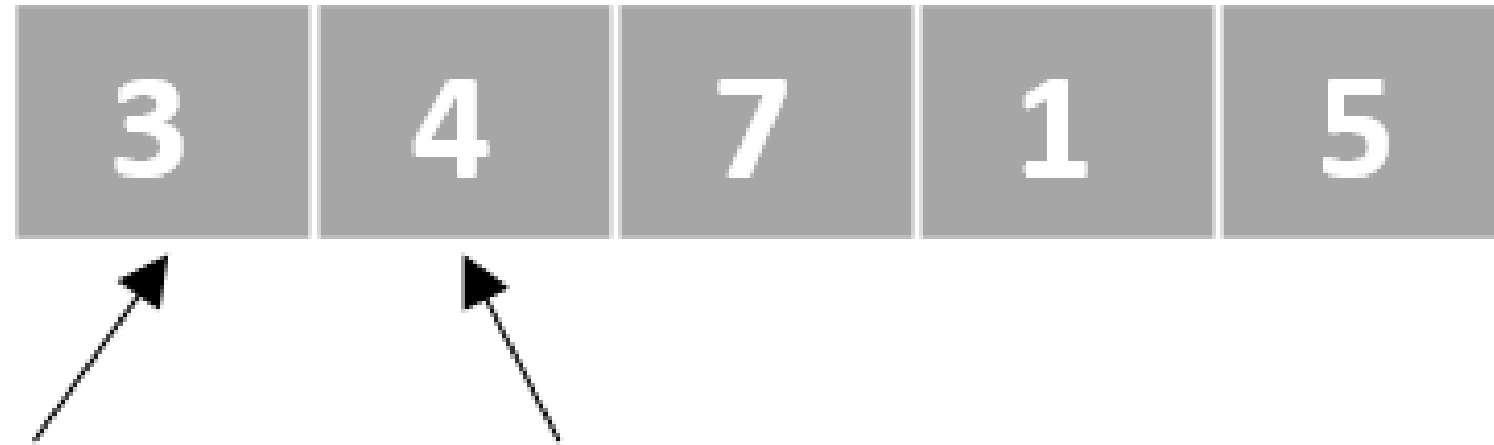
- Deeply studied
- Solve how to **sort** an **unsorted collection** in **ascending/descending** order
- Can **reduce complexity** of problems
- Some sorting algorithms:
  - bubble sort
  - selection sort
  - insertion sort
  - merge sort
  - quicksort

# Bubble sort



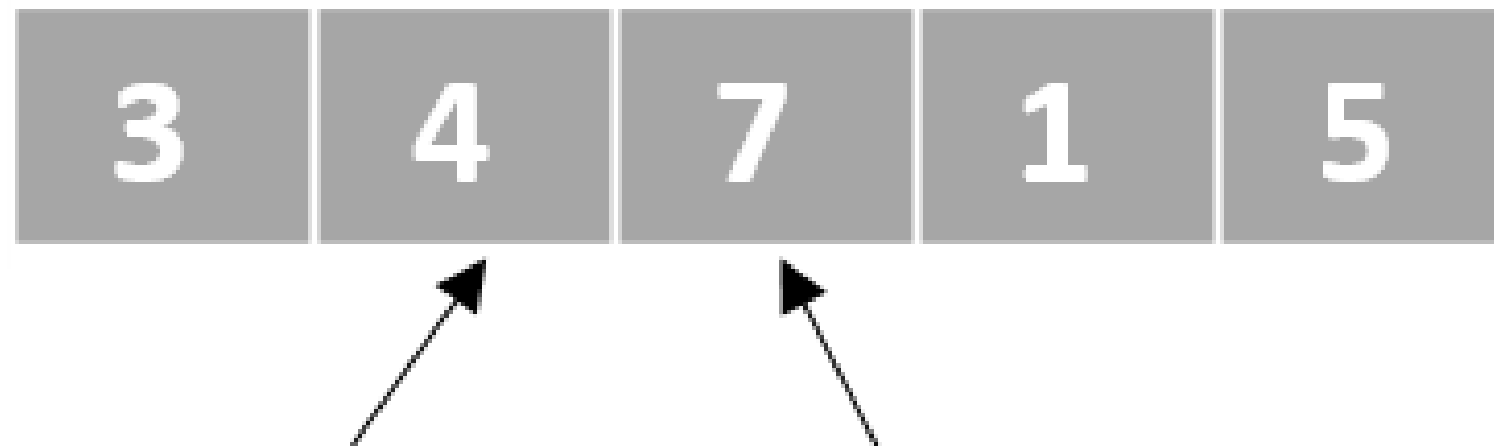
- First value greater than the second value

# Bubble sort



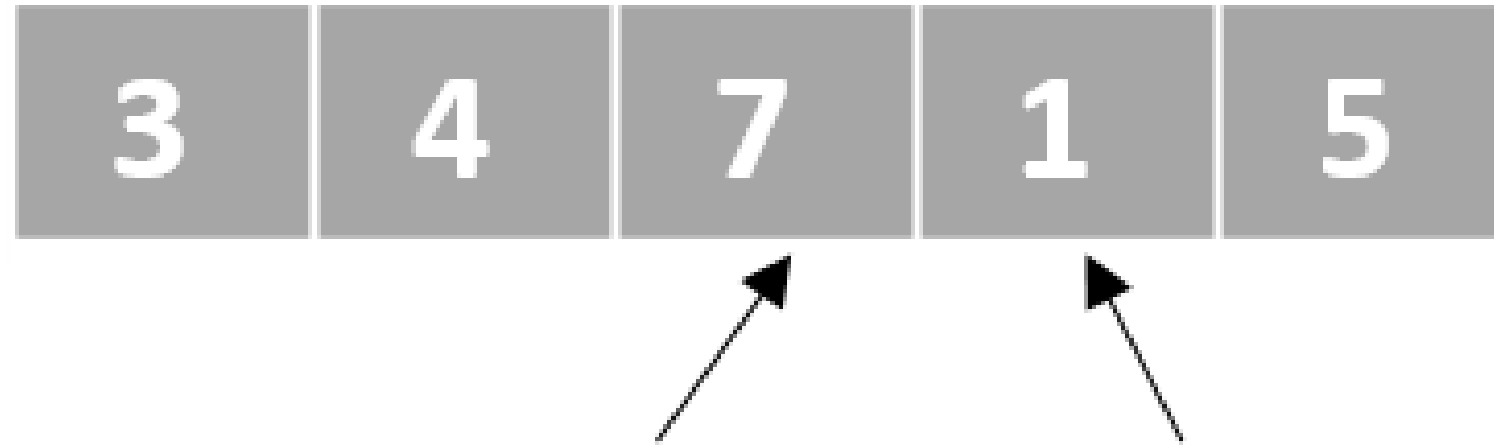
- First value greater than the second value
  - Swap them
- Second value greater than the first value
  - Nothing

# Bubble sort



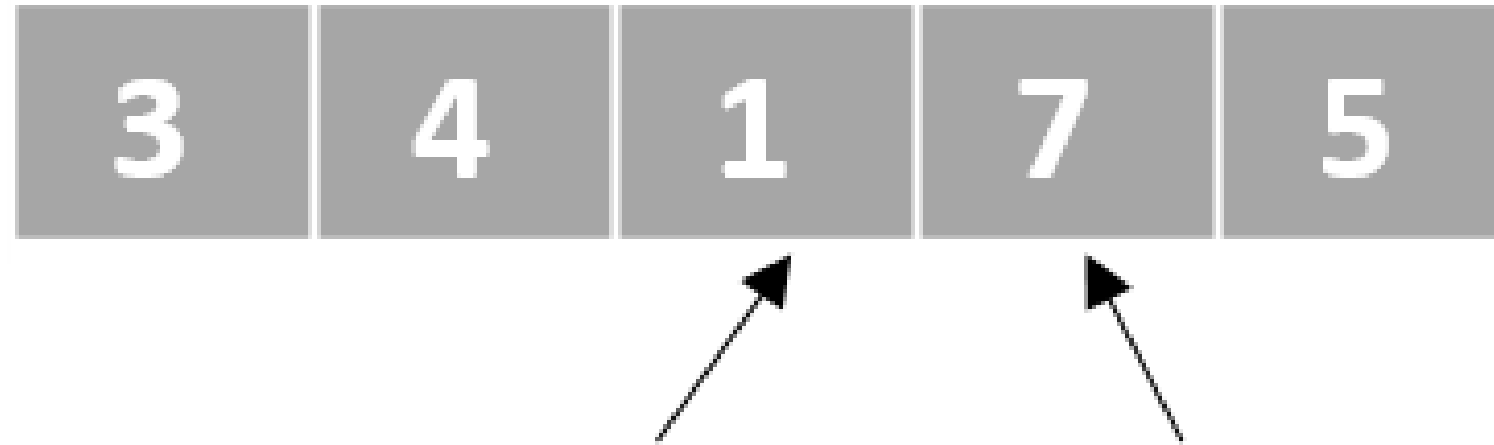
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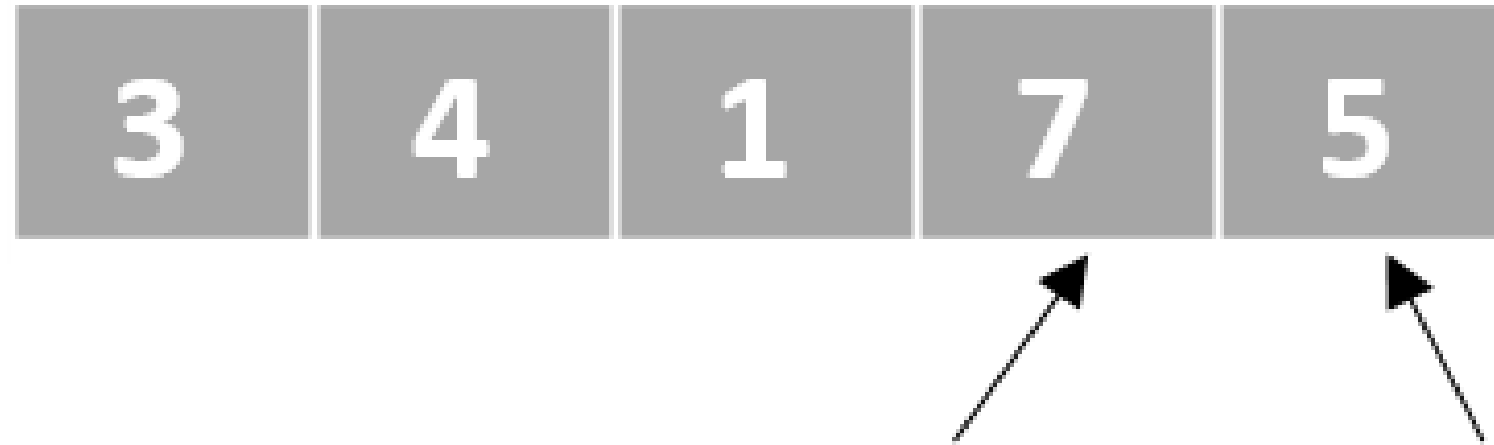
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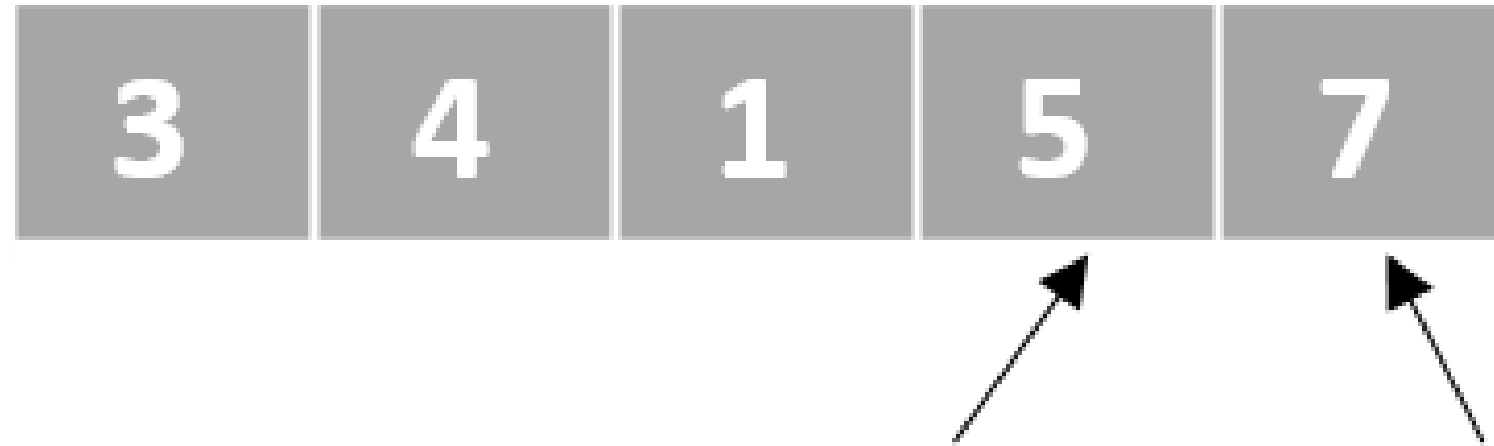
# Bubble sort



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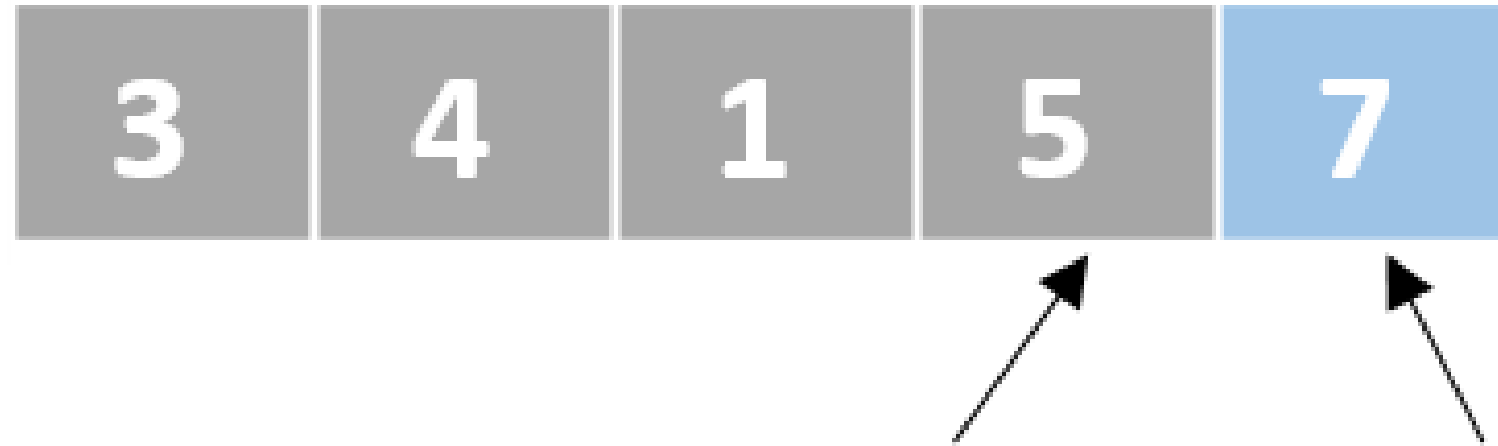


# Bubble sort



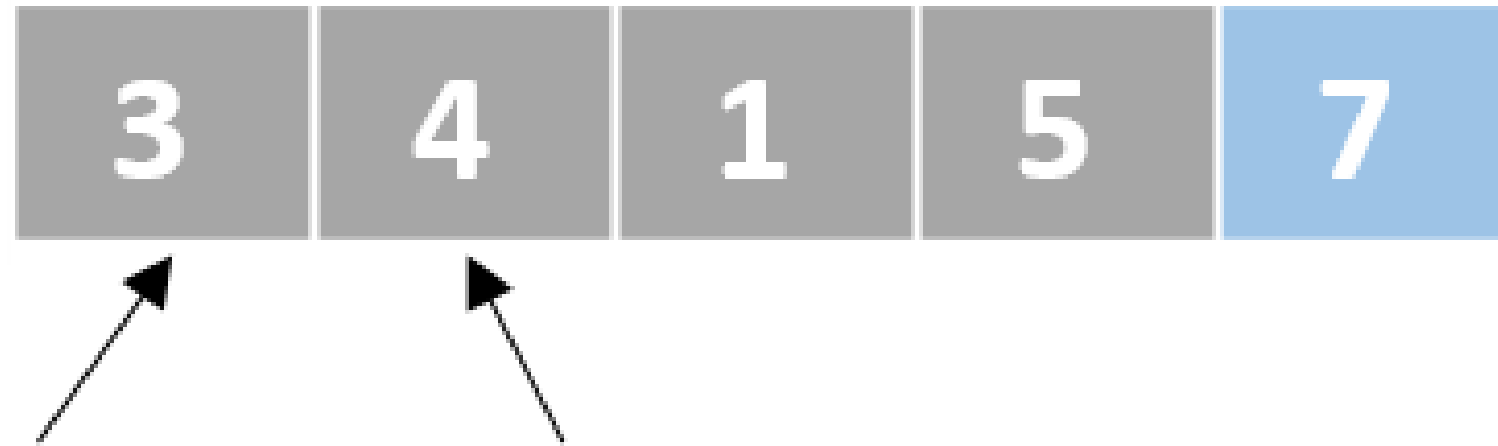
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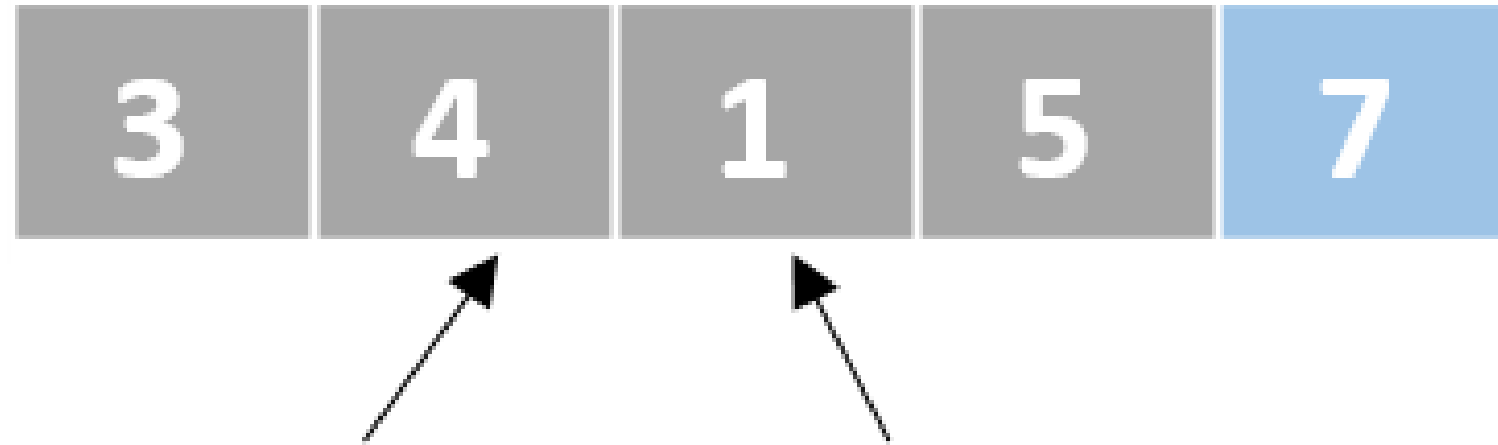
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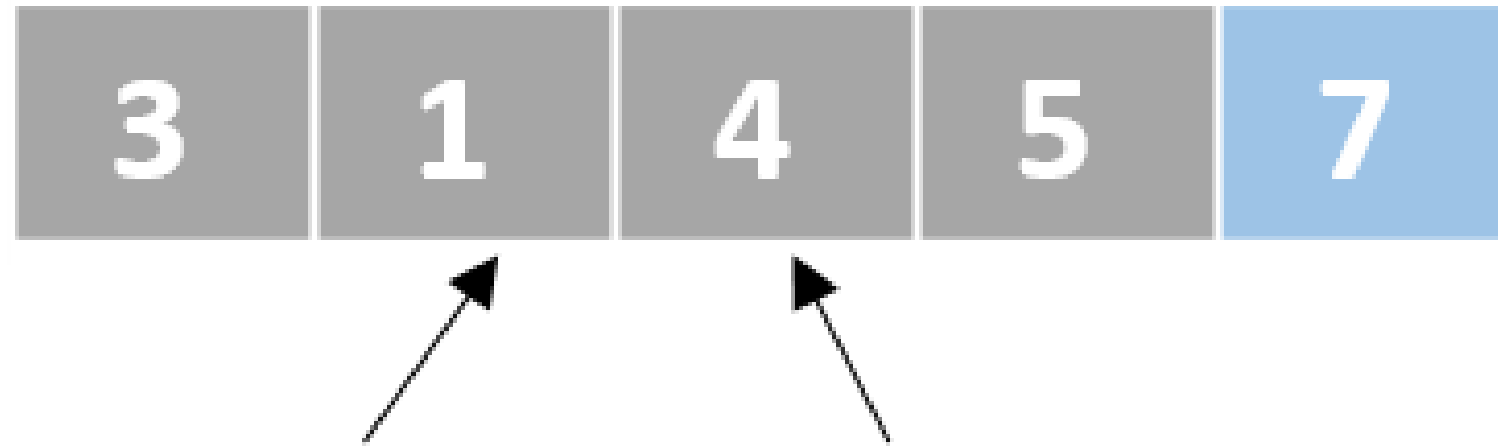
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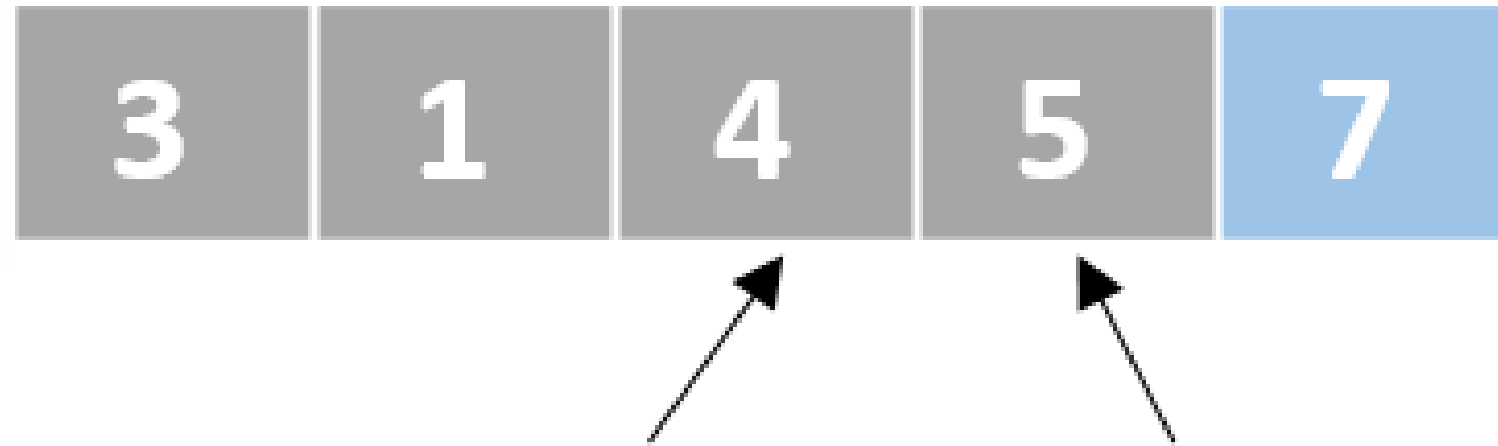
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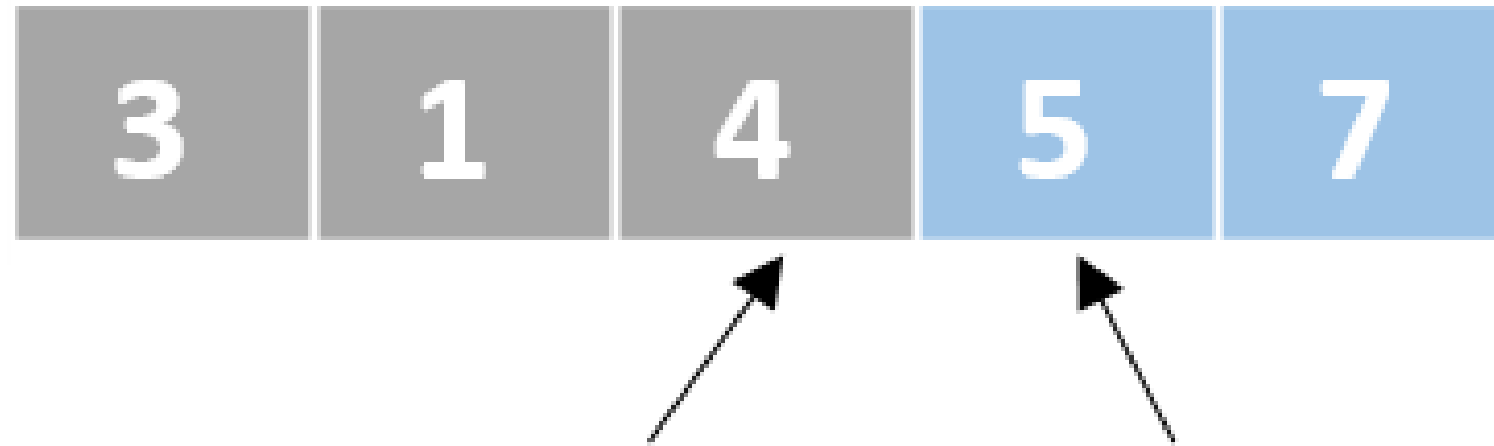
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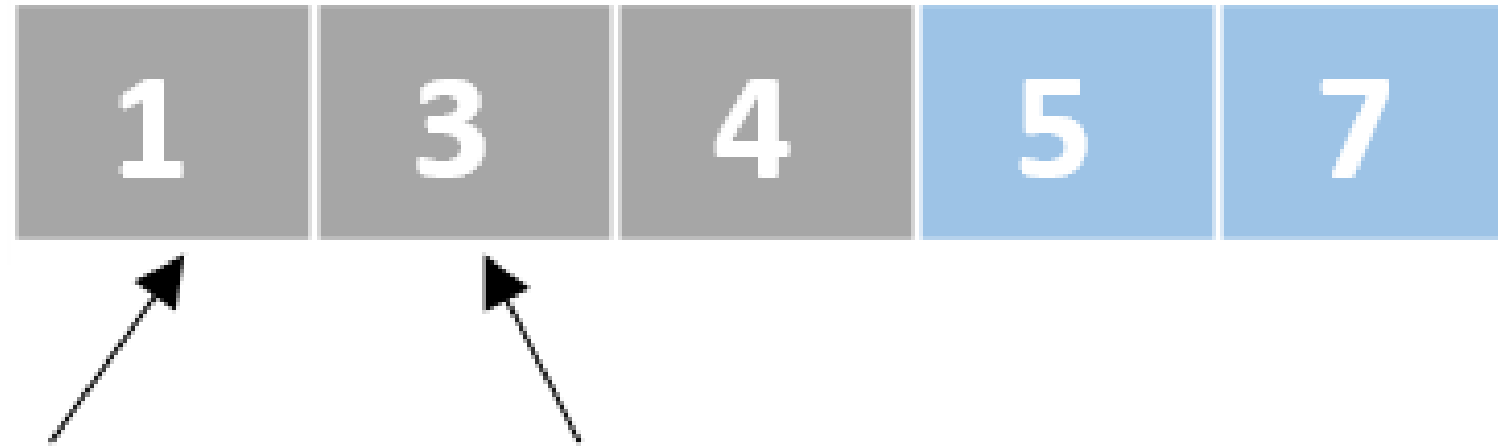
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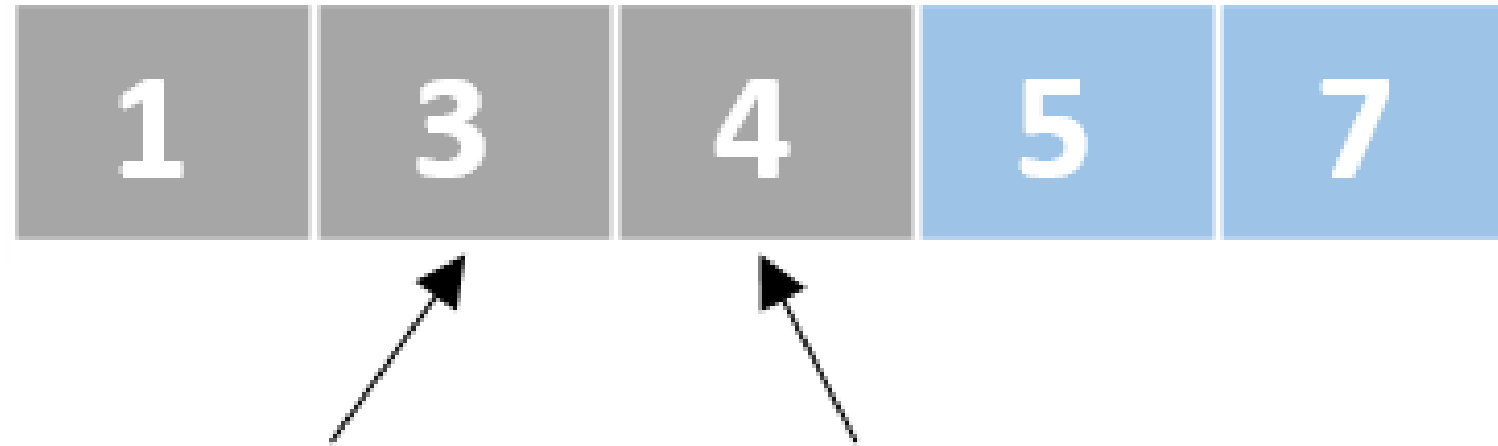


# Bubble sort



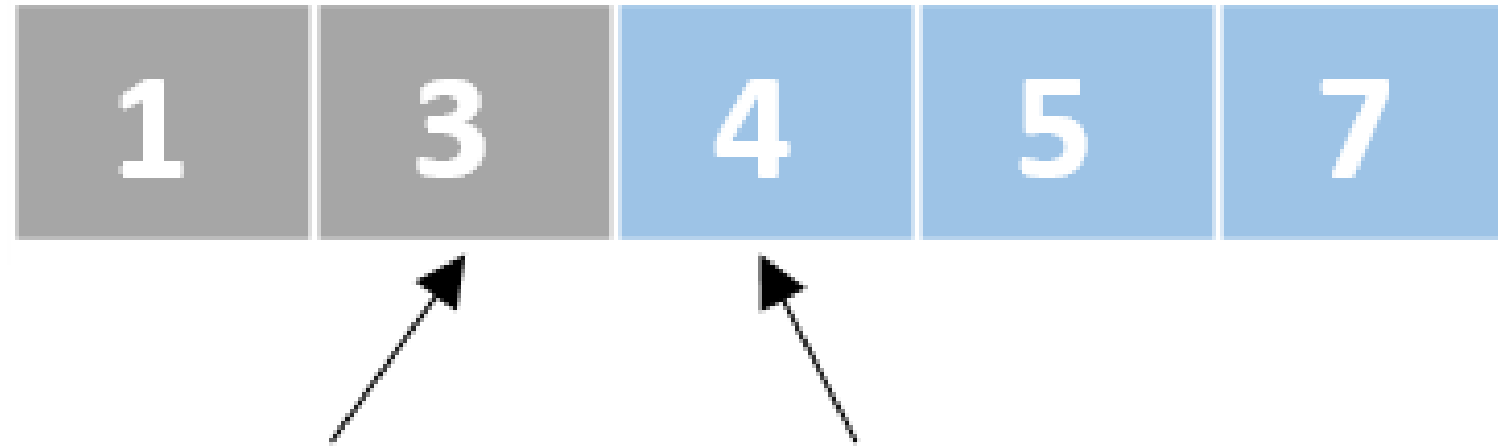
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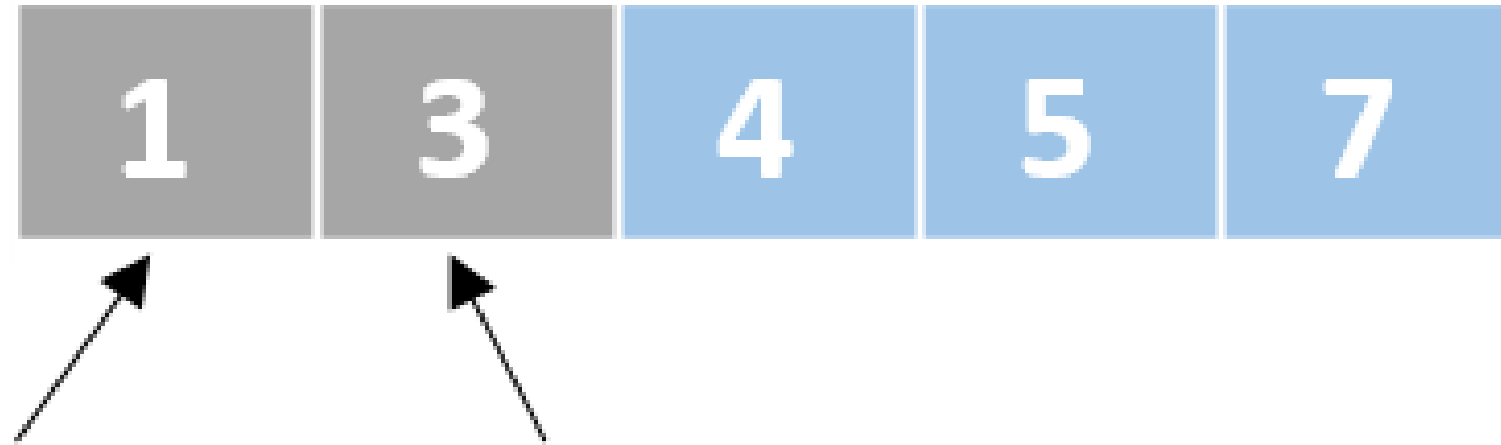
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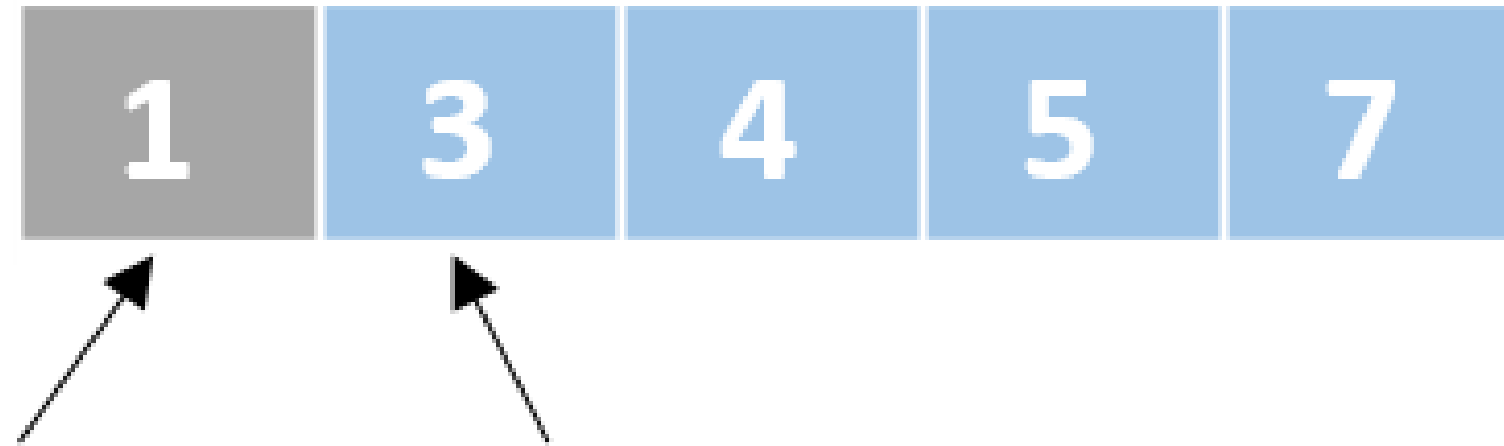
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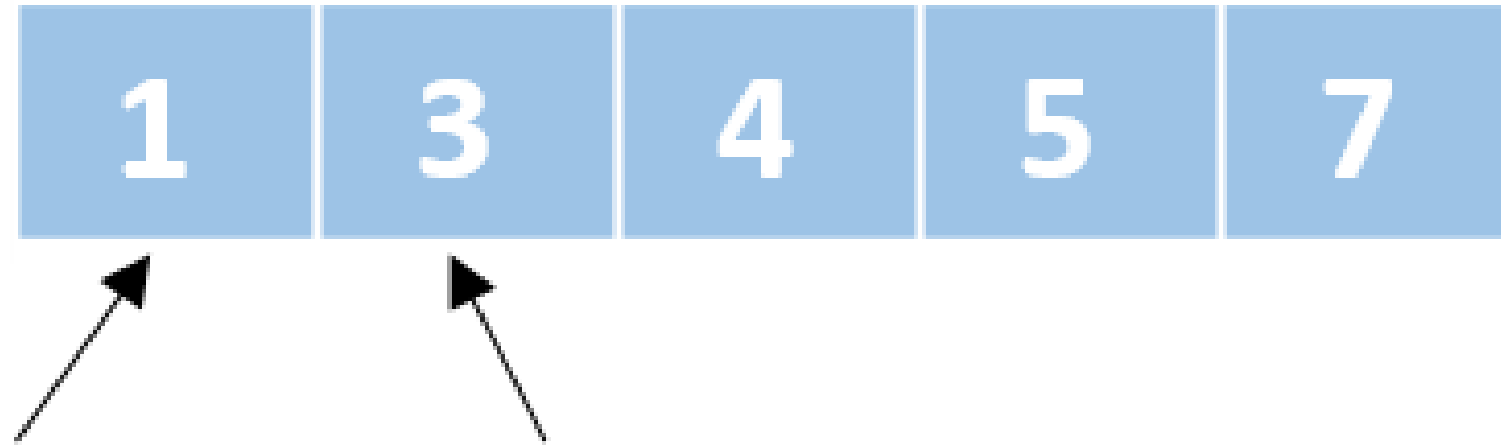
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# Bubble sort - implementation

```
def bubble_sort(my_list):  
    list_length = len(my_list)  
    for i in range(list_length-1):  
        for j in range(list_length-1-i):  
            if my_list[j] > my_list[j+1]:  
                my_list[j] , my_list[j+1] = my_list[j+1] , my_list[j]  
    return my_list
```

```
print(bubble_sort([4,3,7,1,5]))
```

```
[1, 3, 4, 5, 7]
```

# Bubble sort - implementation

```
def bubble_sort(my_list):  
    list_length = len(my_list)  
    is_sorted = False  
    while not is_sorted:  
        is_sorted = True  
        for i in range(list_length-1):  
            if my_list[i] > my_list[i+1]:  
                my_list[i] , my_list[i+1] = my_list[i+1] , my_list[i]  
                is_sorted = False  
        list_length -= 1  
    return my_list
```



# Bubble sort - complexity

- Worst case:  $O(n^2)$
- Best case - not improved version:  $\Omega(n^2)$
- Best case - improved version:  $\Omega(n)$
- Average case:  $\Theta(n^2)$
- Doesn't perform well with highly unsorted large lists
- Performs well:
  - large sorted/almost sorted lists
  - small lists

# Let's practice!

DATA STRUCTURES AND ALGORITHMS IN PYTHON

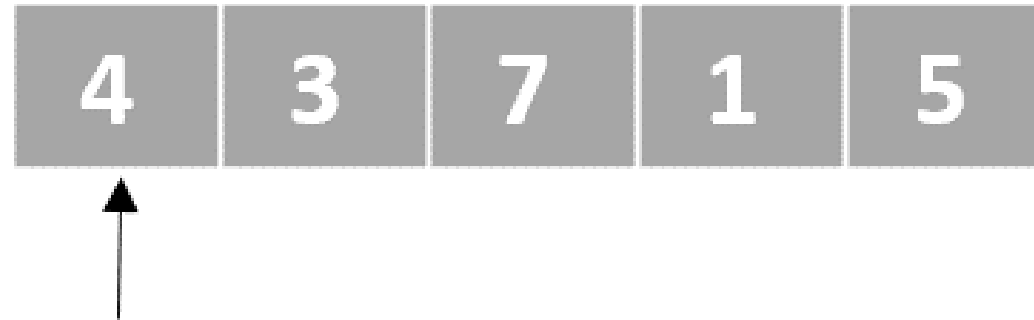
# Selection Sort and Insertion Sort

DATA STRUCTURES AND ALGORITHMS IN PYTHON



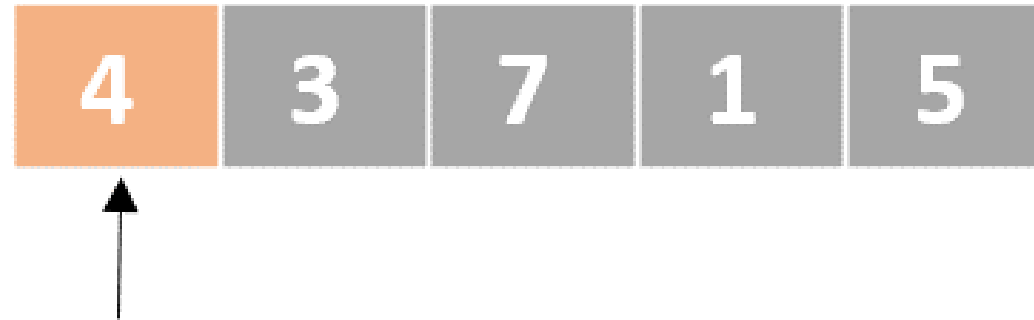
**Miriam Antona**  
Software engineer

# Selection sort



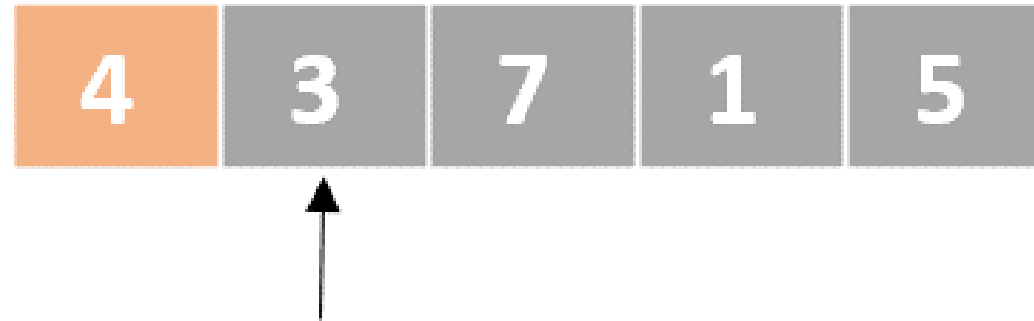
- Determine the lowest value

# Selection sort



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# Selection sort



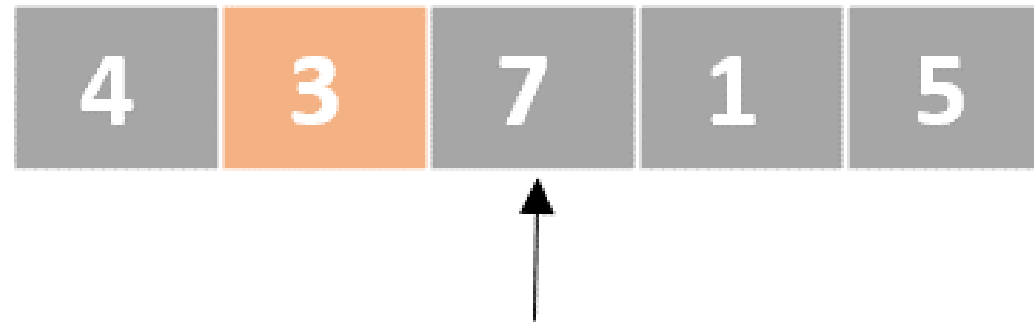
- Determine the lowest value

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- Determine the lowest value

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# Selection sort



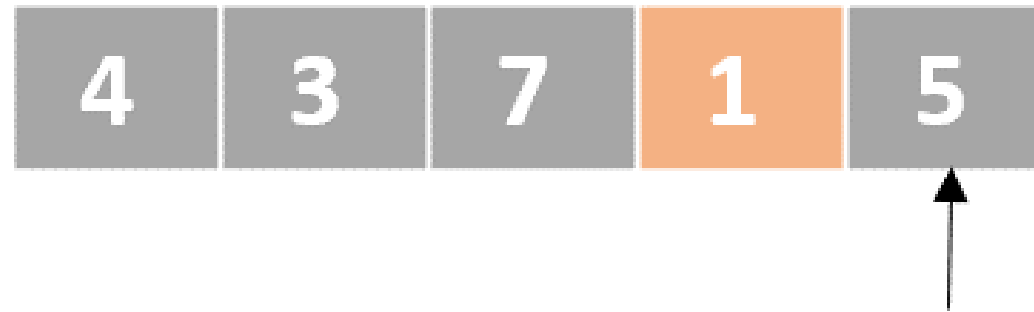
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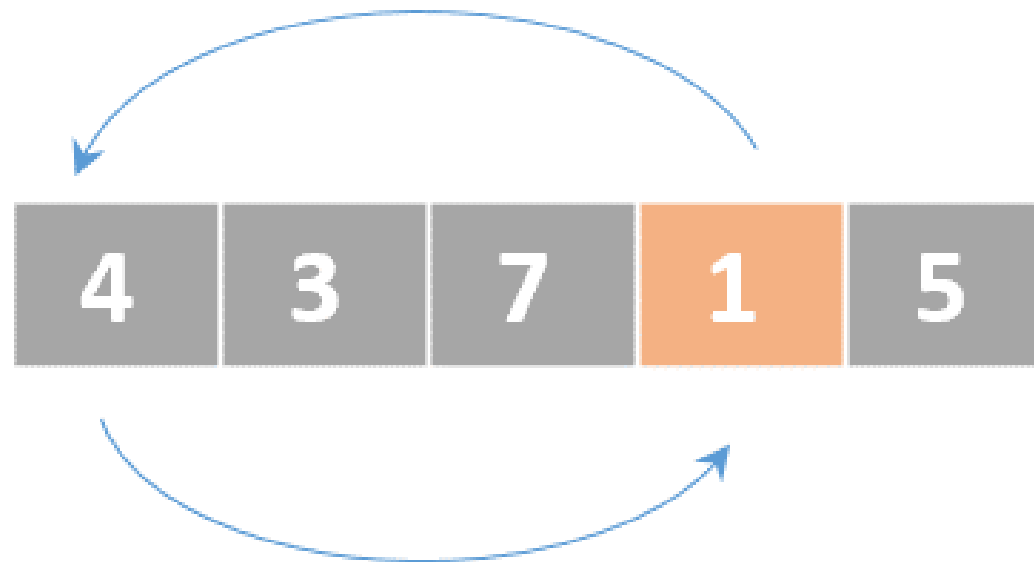
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# Selection sort



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# Selection sort



- Determine the lowest value
- Swap the lowest value with the first unordered element

# Selection sort



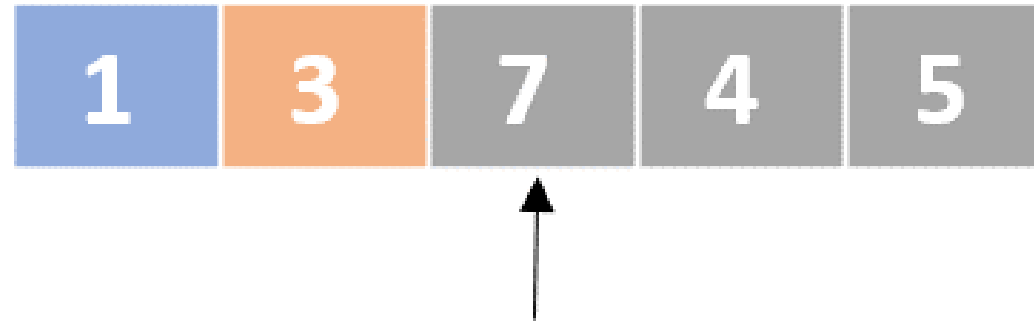
- Determine the lowest value
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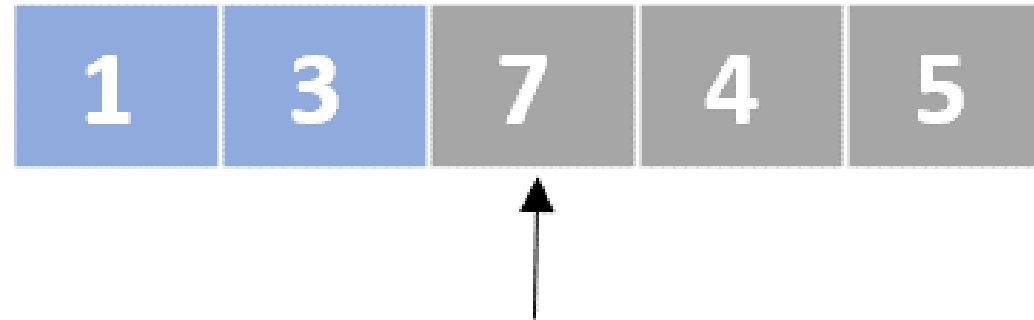


# Selection sort



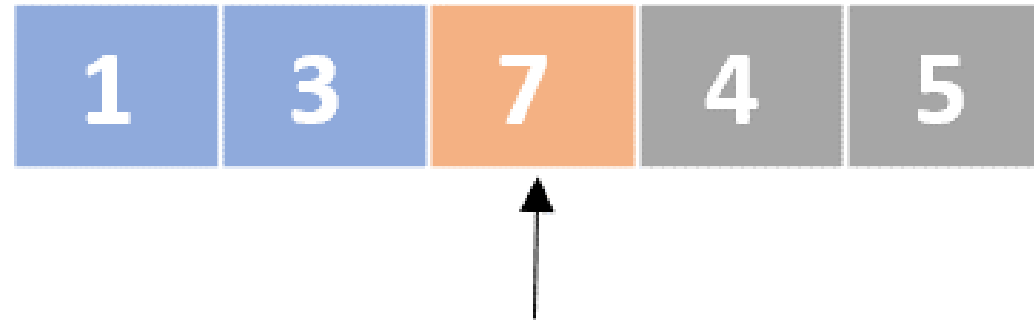
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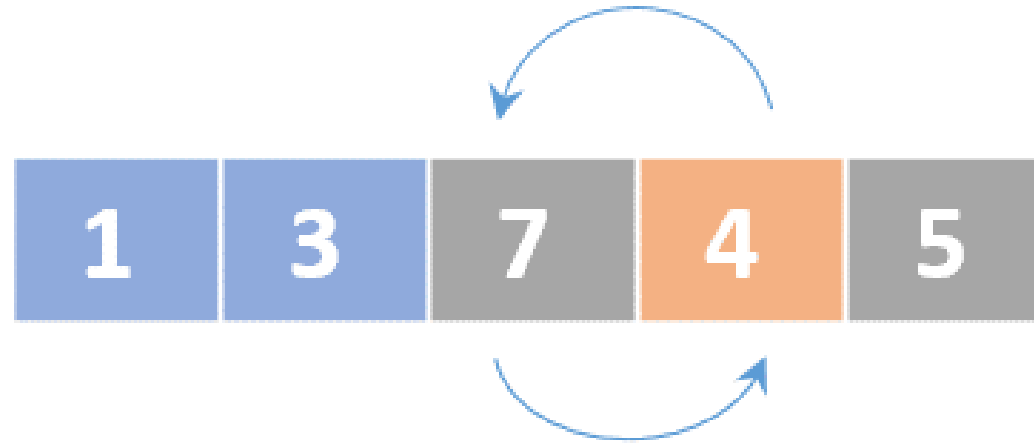
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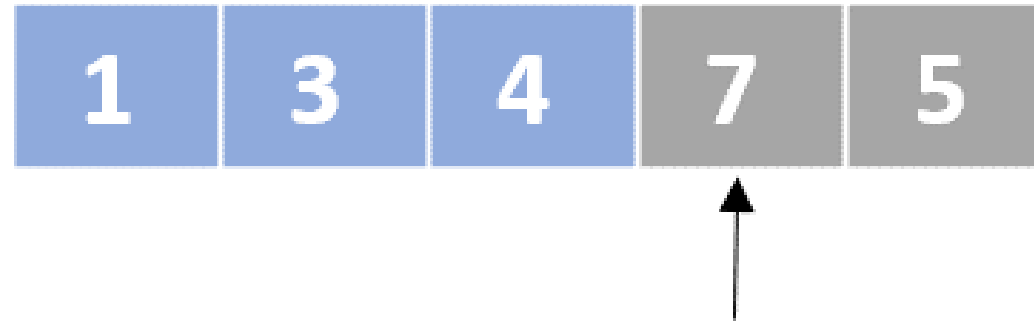
# Selection sort



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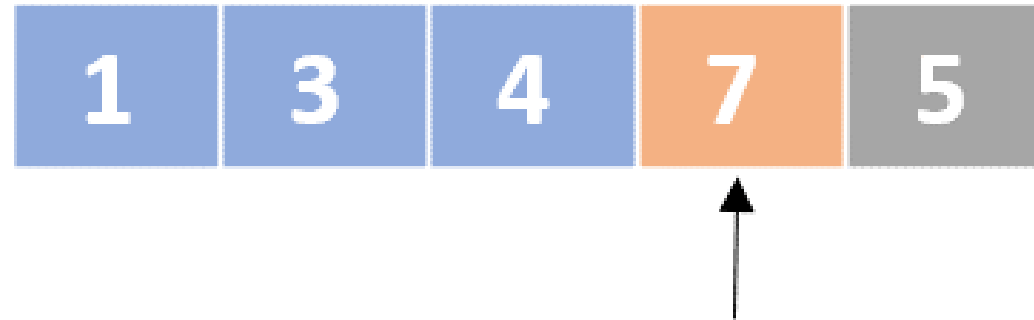


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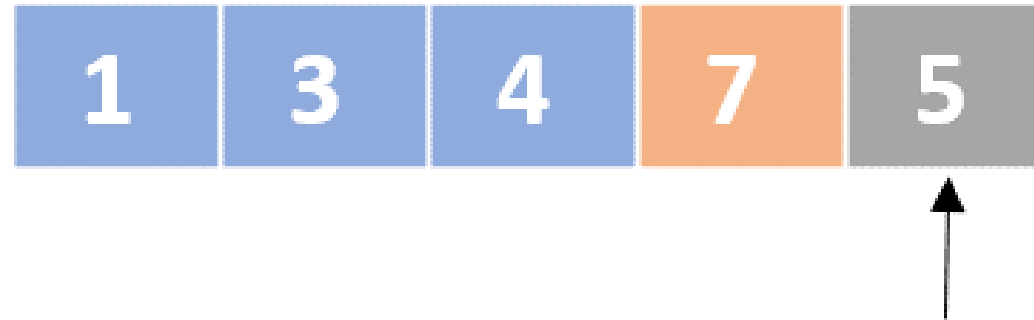
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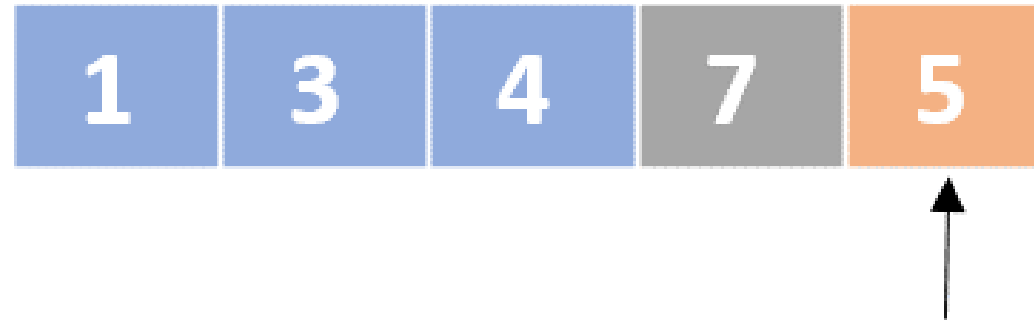
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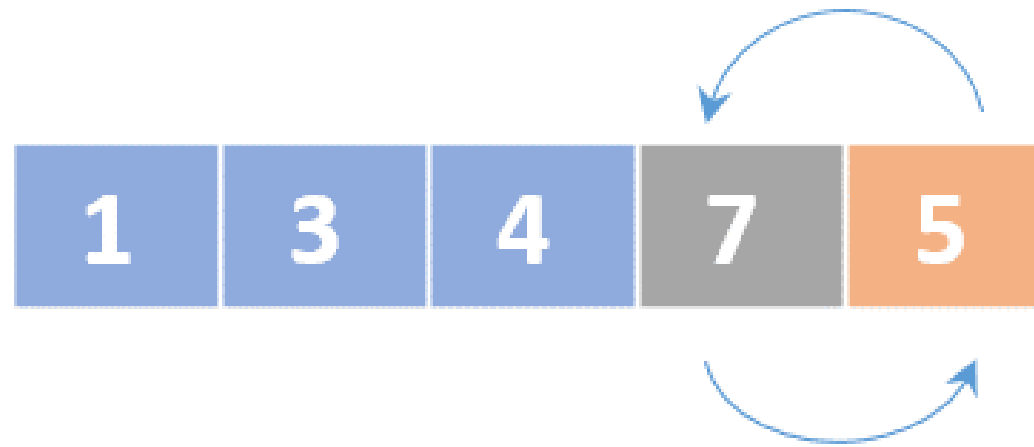
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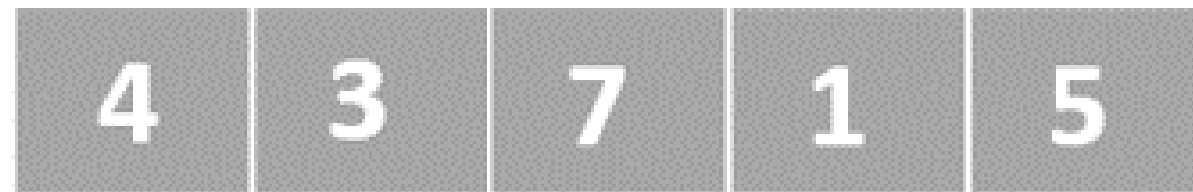
# Selection sort - implementation

```
def selection_sort(my_list):  
    list_length = len(my_list)  
    for i in range(list_length - 1):  
        lowest = my_list[i]  
        index = i  
        for j in range(i + 1, list_length):  
            if my_list[j] < lowest:  
                index = j  
                lowest = my_list[j]  
        my_list[i] , my_list[index] = my_list[index] , my_list[i]  
    return my_list
```

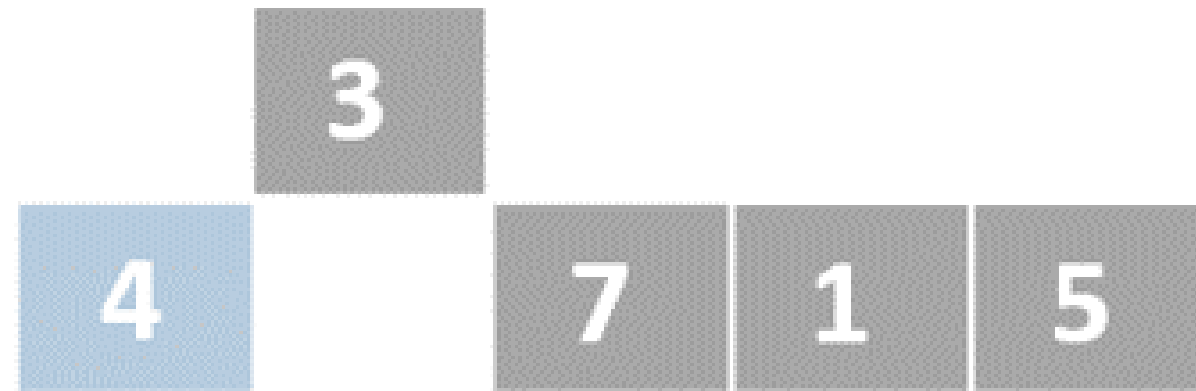
# Selection sort - complexity

- Worst case:  $O(n^2)$
- Average case:  $\Theta(n^2)$
- Best case:  $\Omega(n^2)$

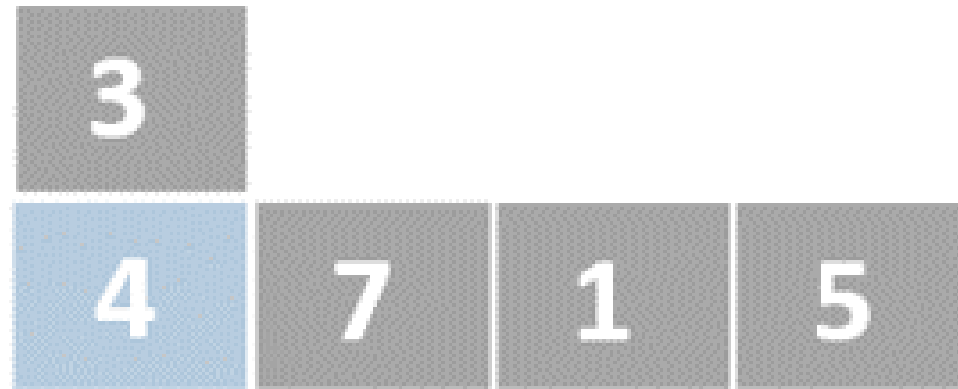
# Insertion sort



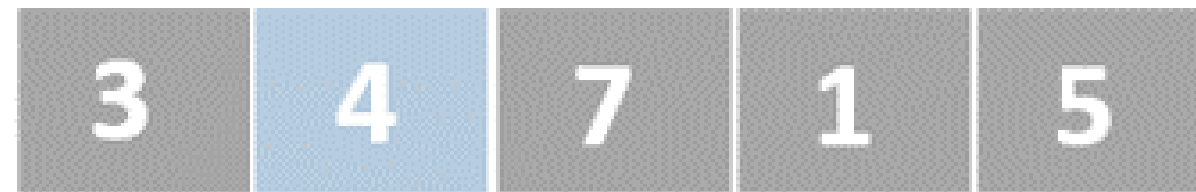
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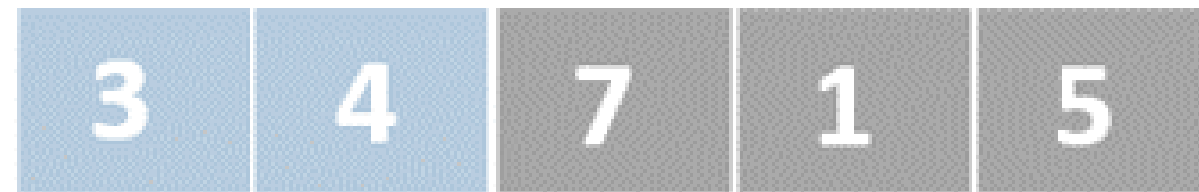
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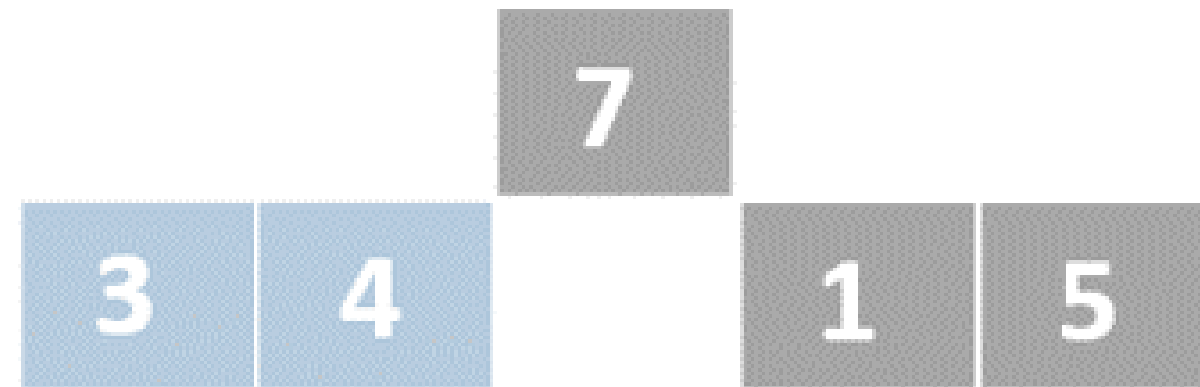
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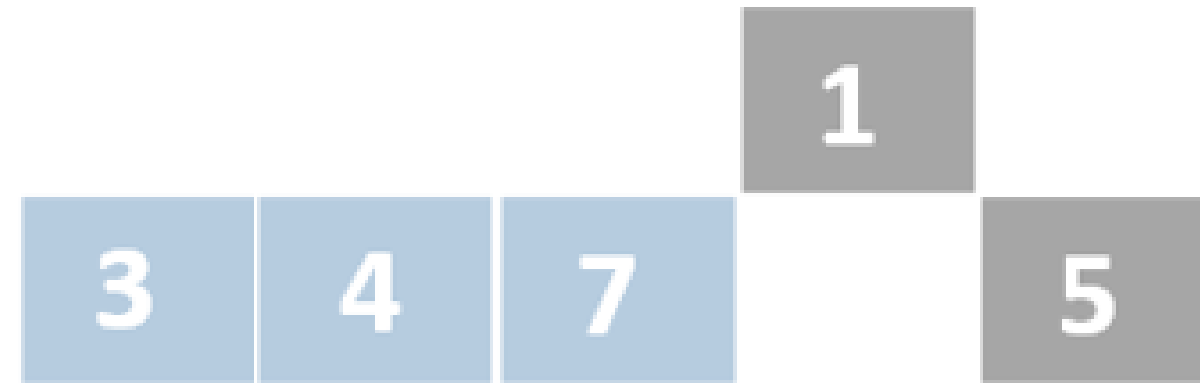




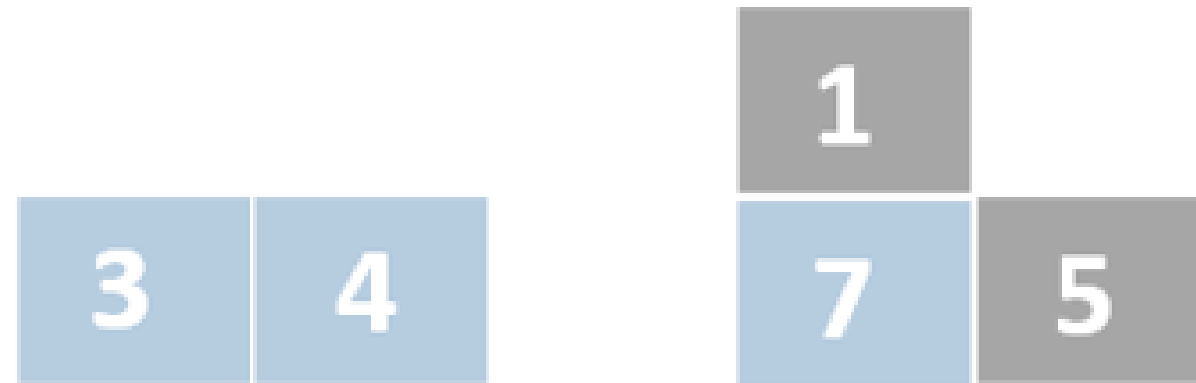
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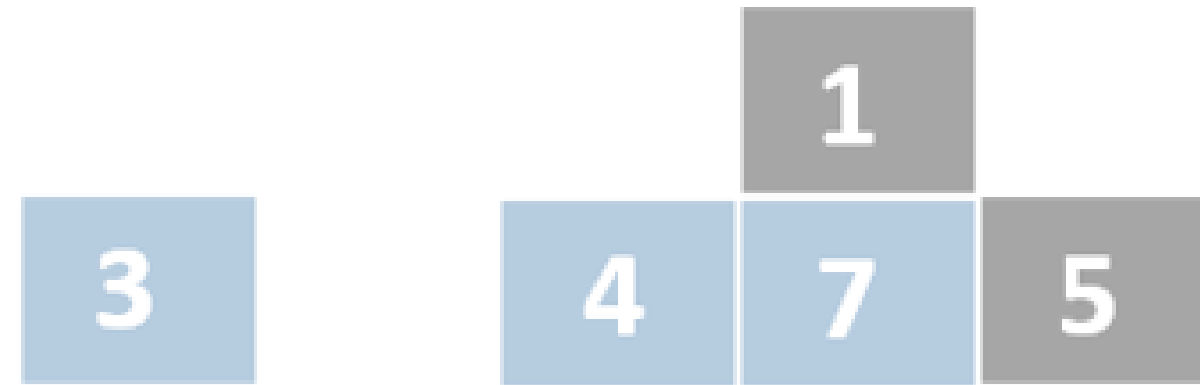
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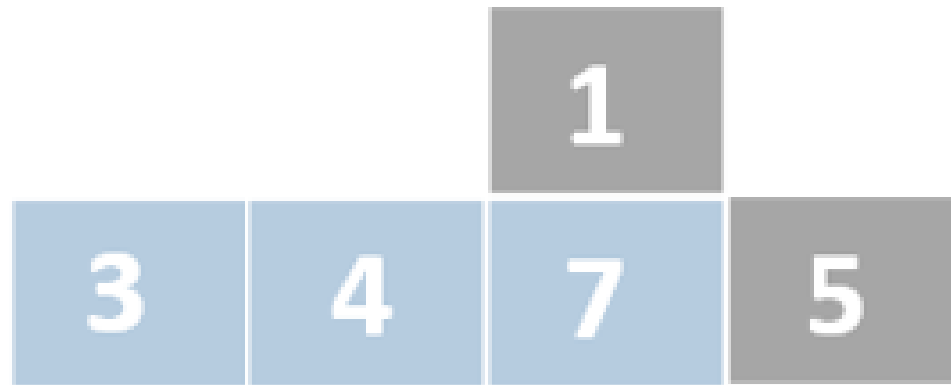
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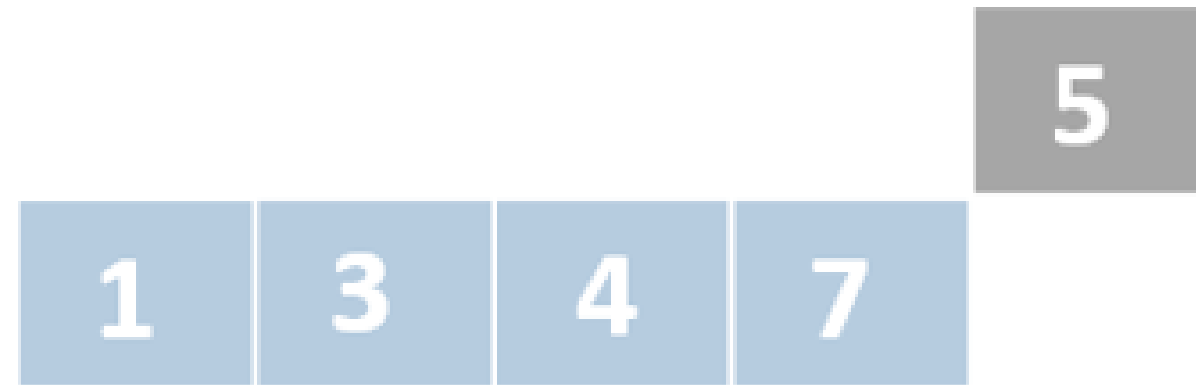
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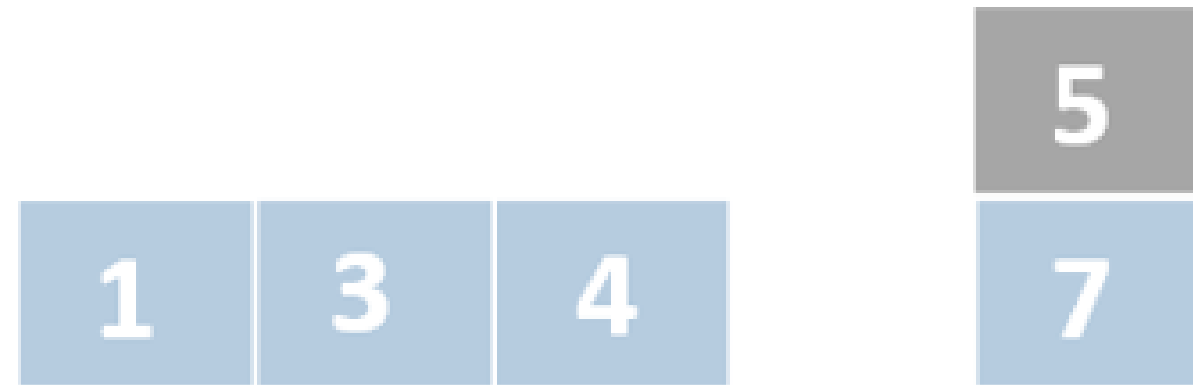


# Insertion sort





# Insertion sort



# Insertion sort



# Insertion sort - implementation

```
def insertion_sort(my_list):  
    for i in range(1, len(my_list)):  
        number_to_order = my_list[i]  
        j = i - 1  
        while j >= 0 and number_to_order < my_list[j]:  
            my_list[j + 1] = my_list[j]  
            j -= 1  
        my_list[j + 1] = number_to_order  
    return my_list
```

# Insertion sort - complexity

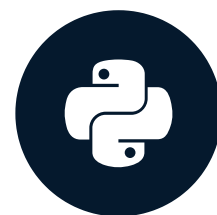
- Worst case:  $O(n^2)$
- Average case:  $\Theta(n^2)$
- Best case:  $\Omega(n)$

# Let's practice!

DATA STRUCTURES AND ALGORITHMS IN PYTHON

# Merge sort

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Software engineer

# Merge sort

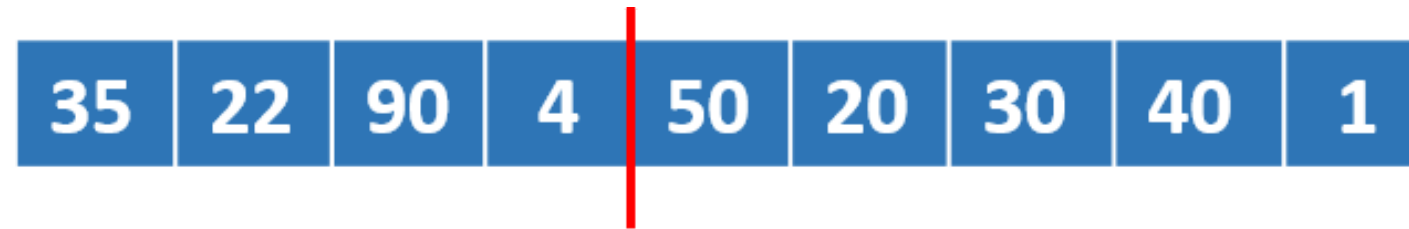
- Follows **divide and conquer**
  - **Divide**
    - divides the problem into smaller sub-problems
  - **Conquer**
    - sub-problems are solved recursively
  - **Combine**
    - solutions of sub-problems are combined to achieve the final solution

# Merge sort - in action

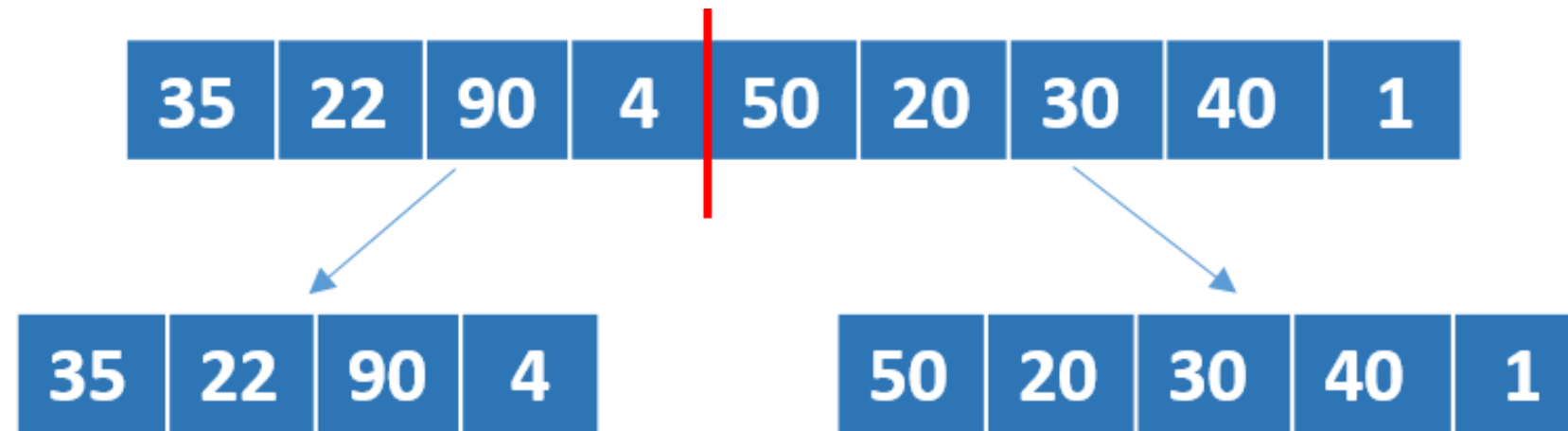
35	22	90	4	50	20	30	40	1
----	----	----	---	----	----	----	----	---



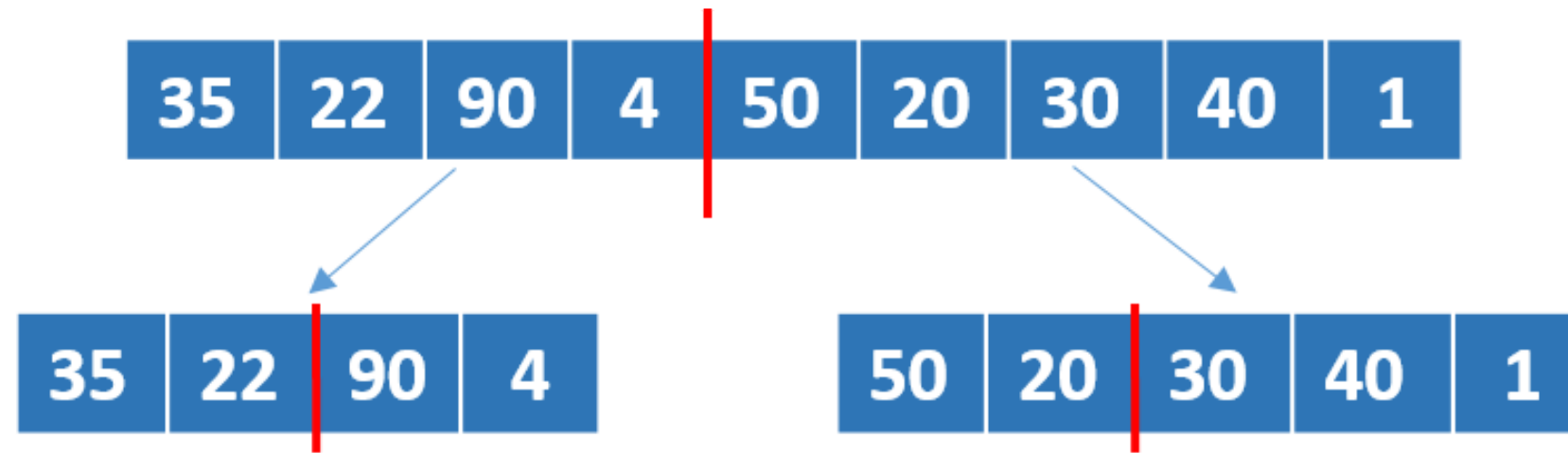
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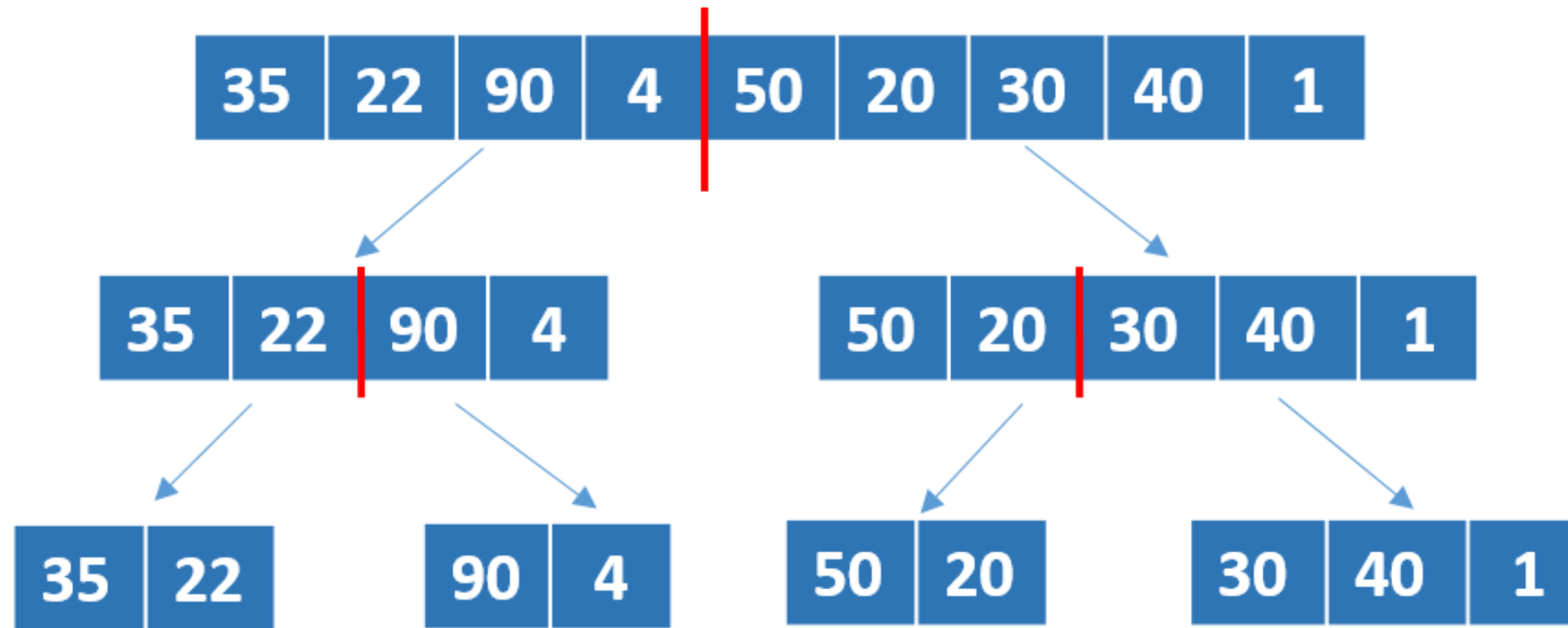
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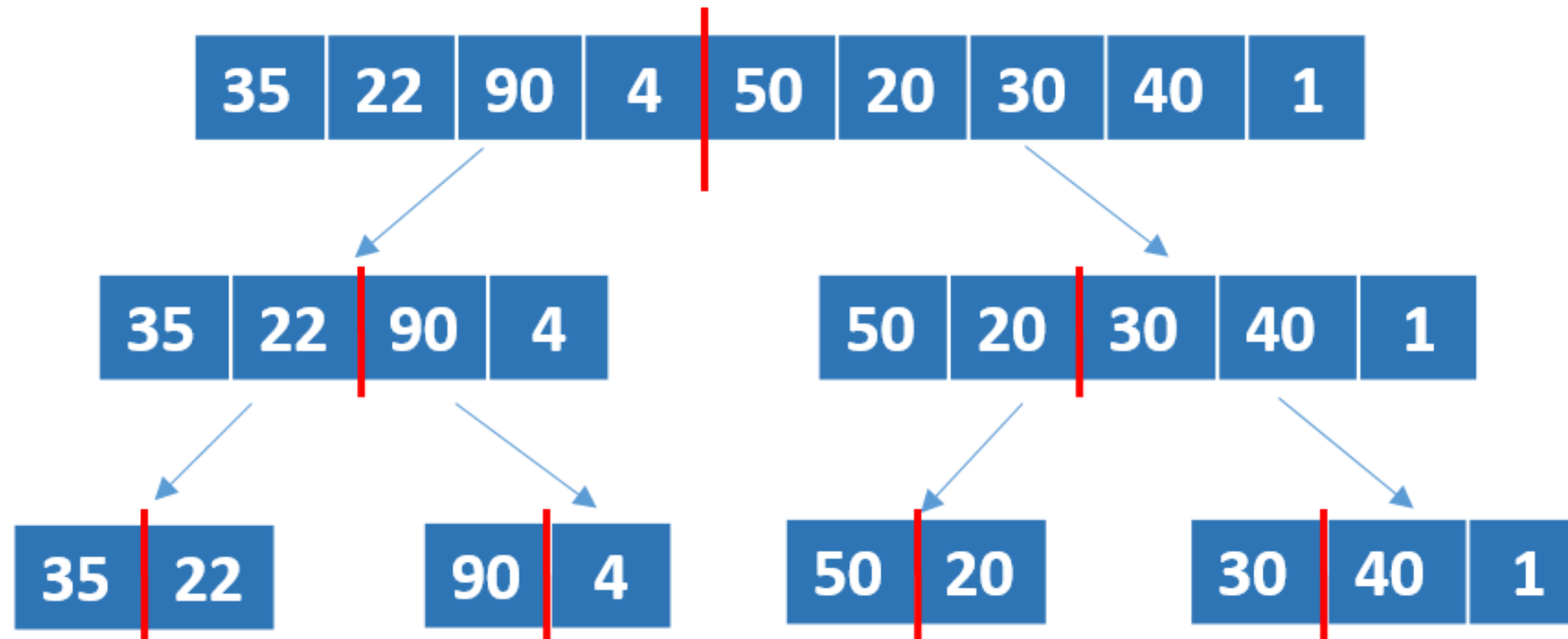
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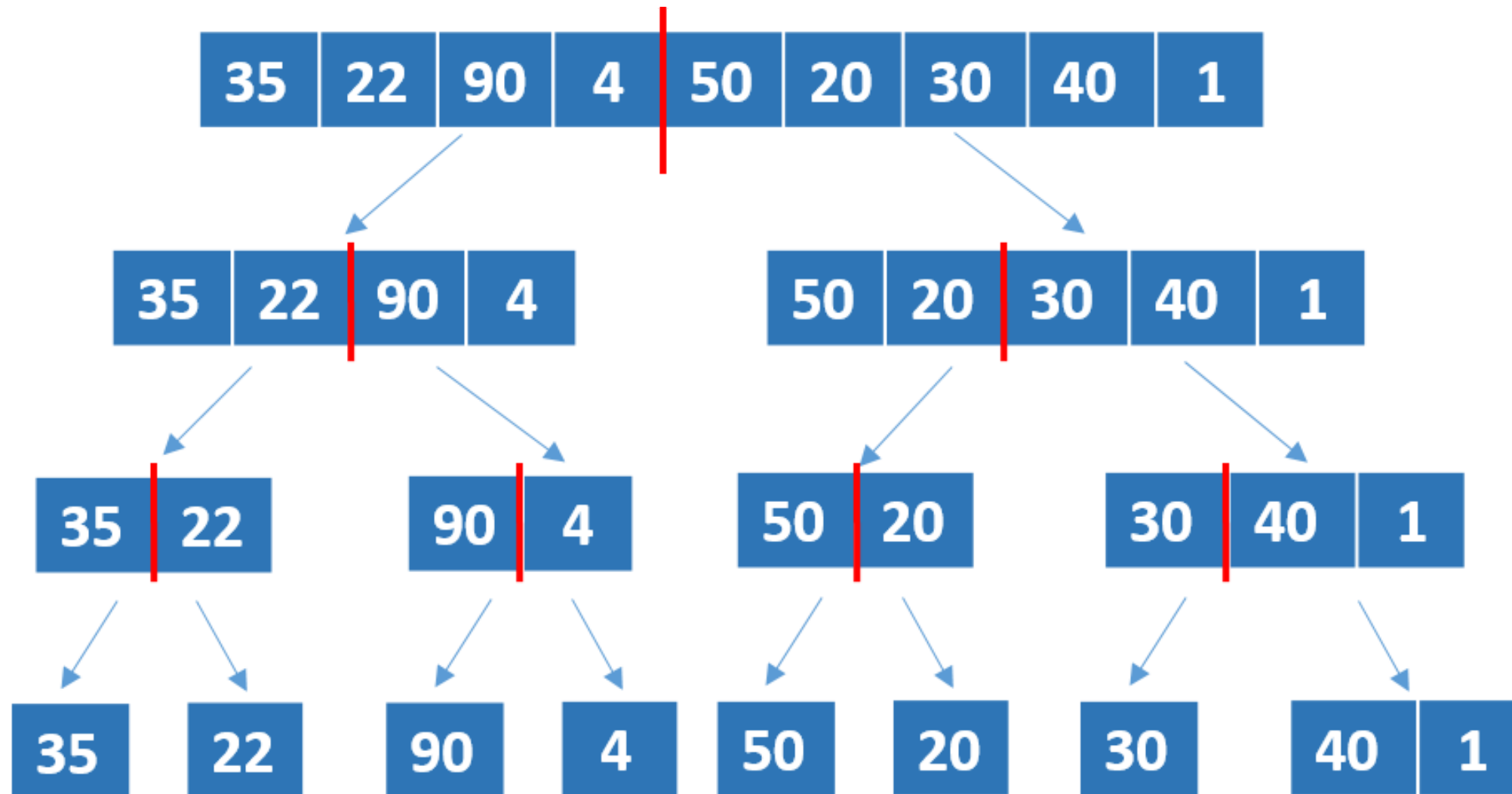
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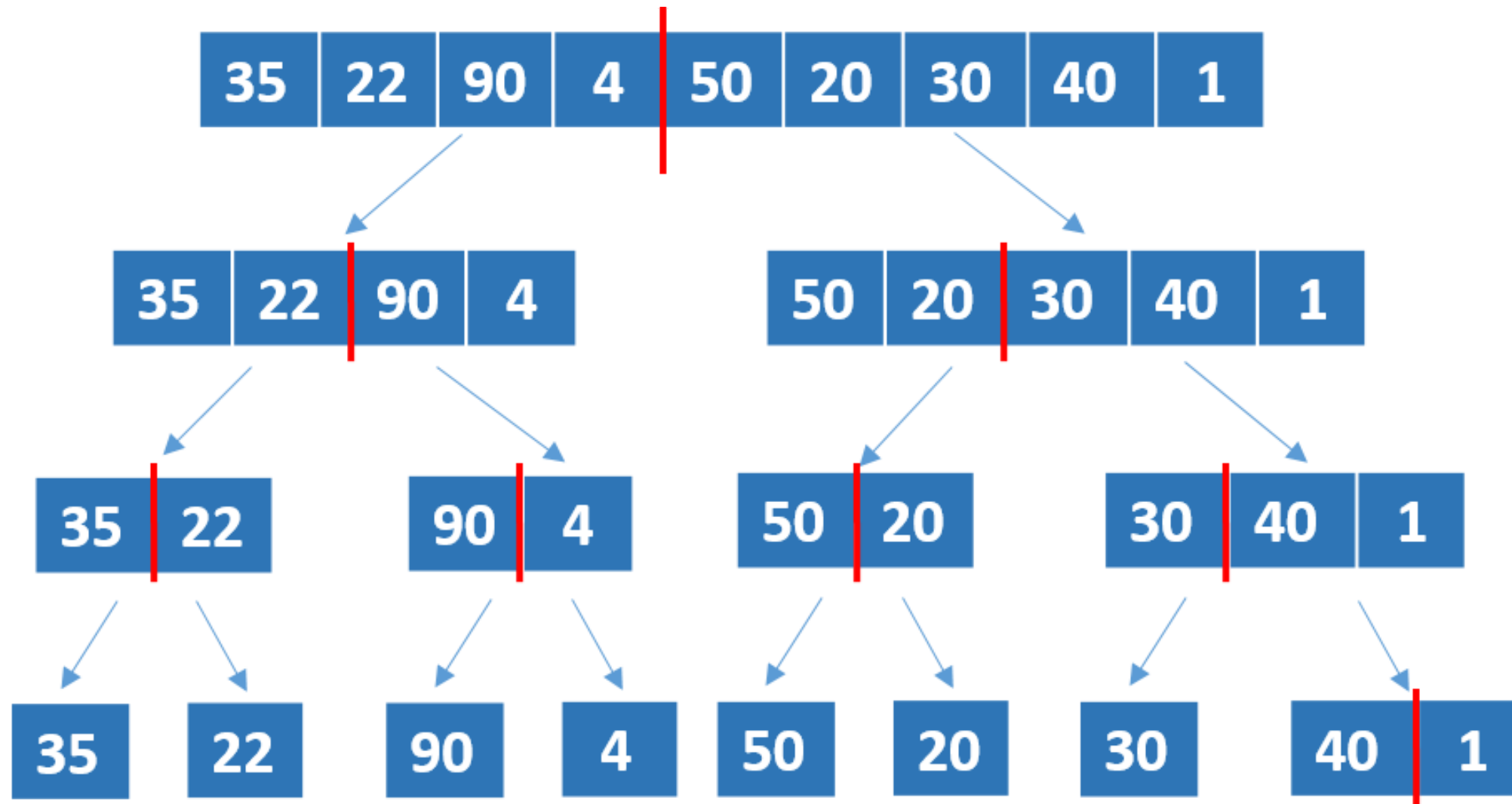
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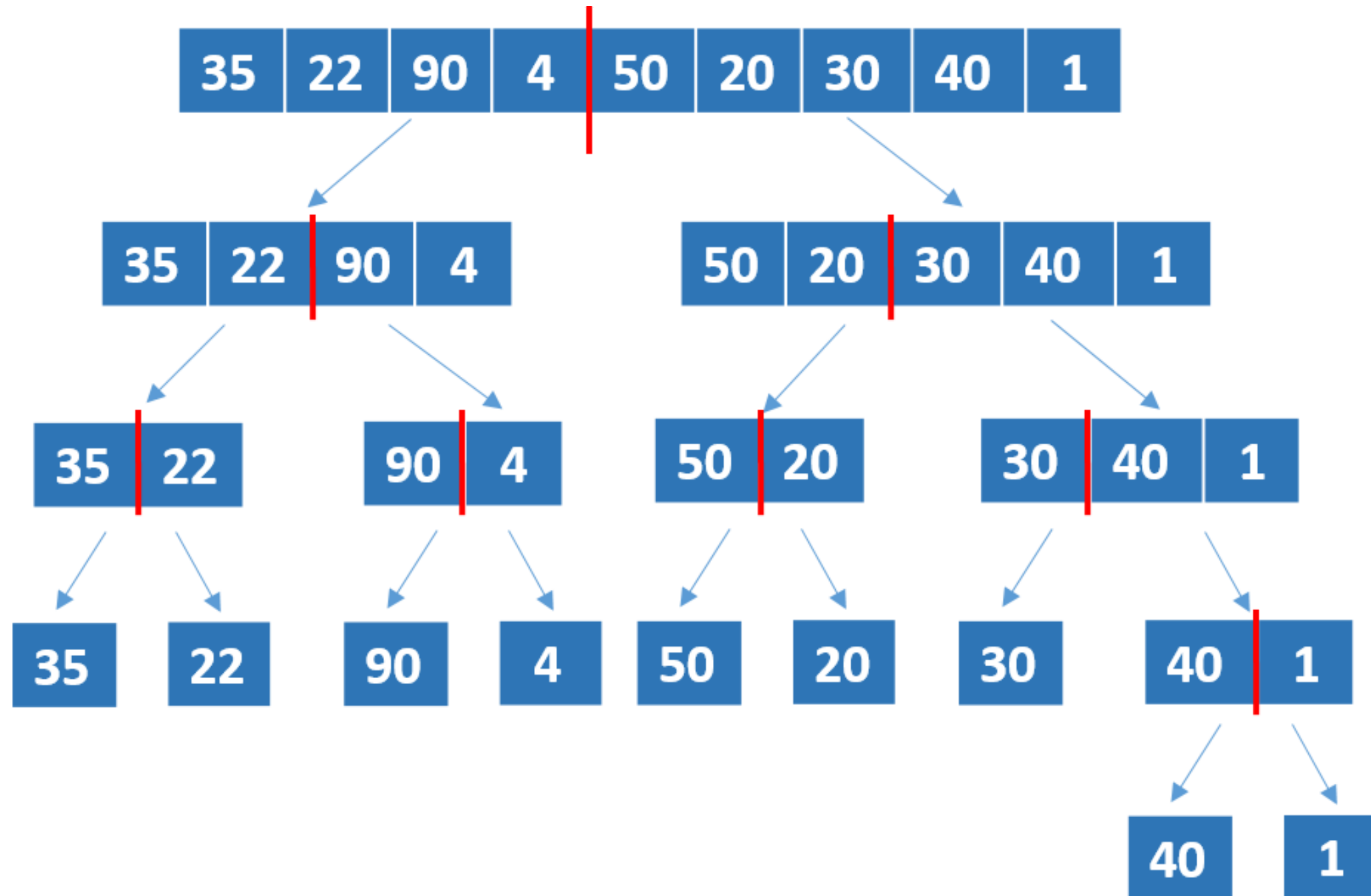
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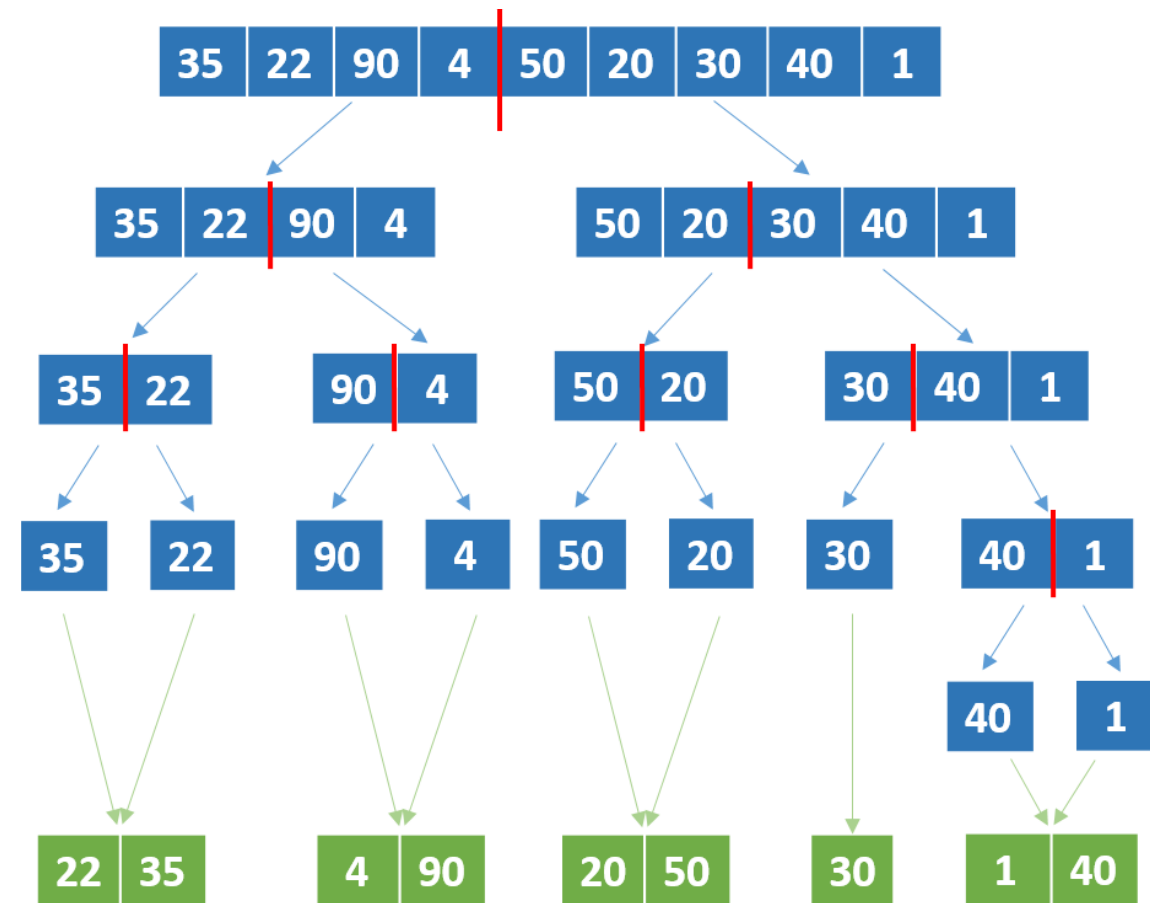


# Merge sort - in action

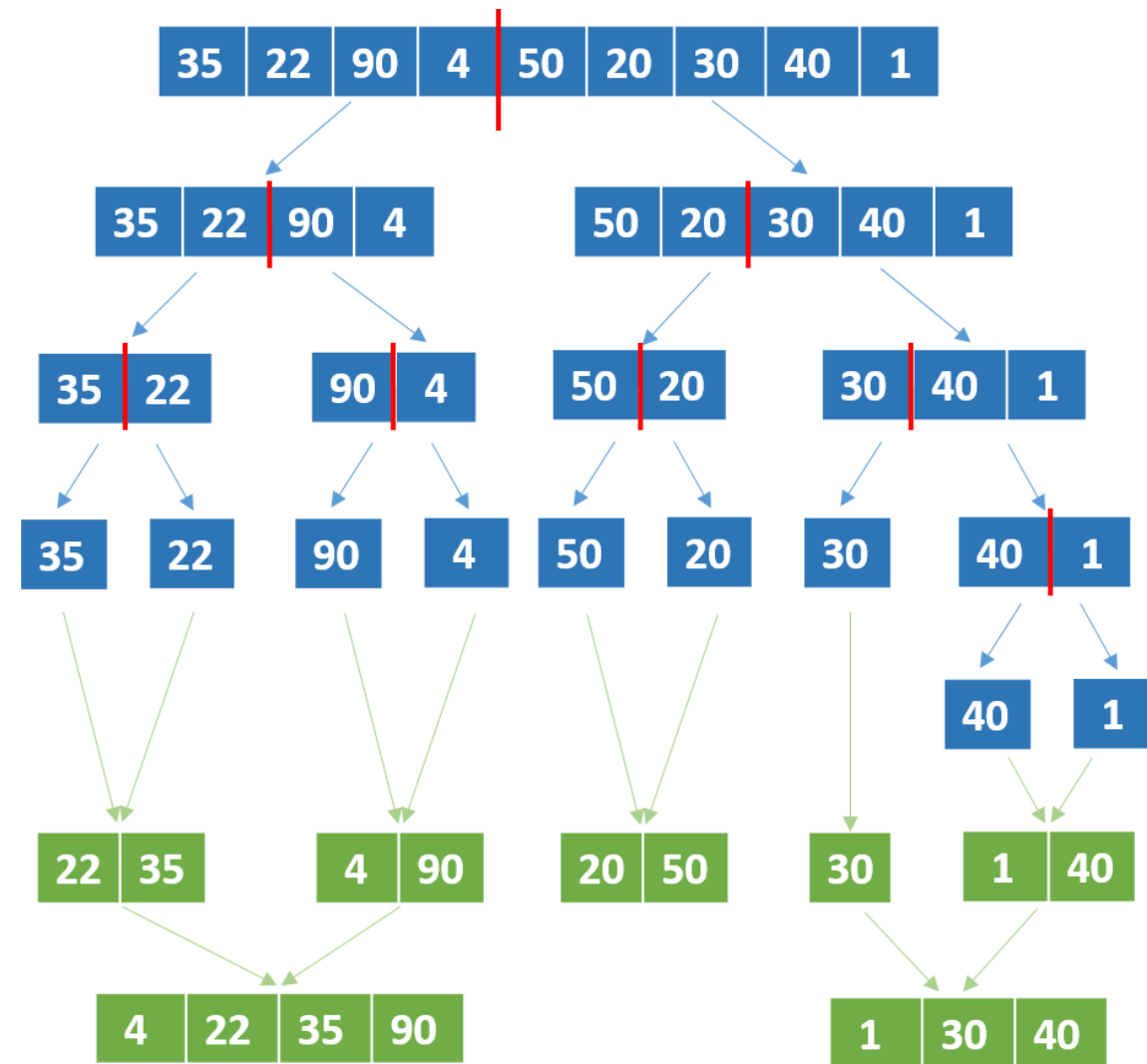




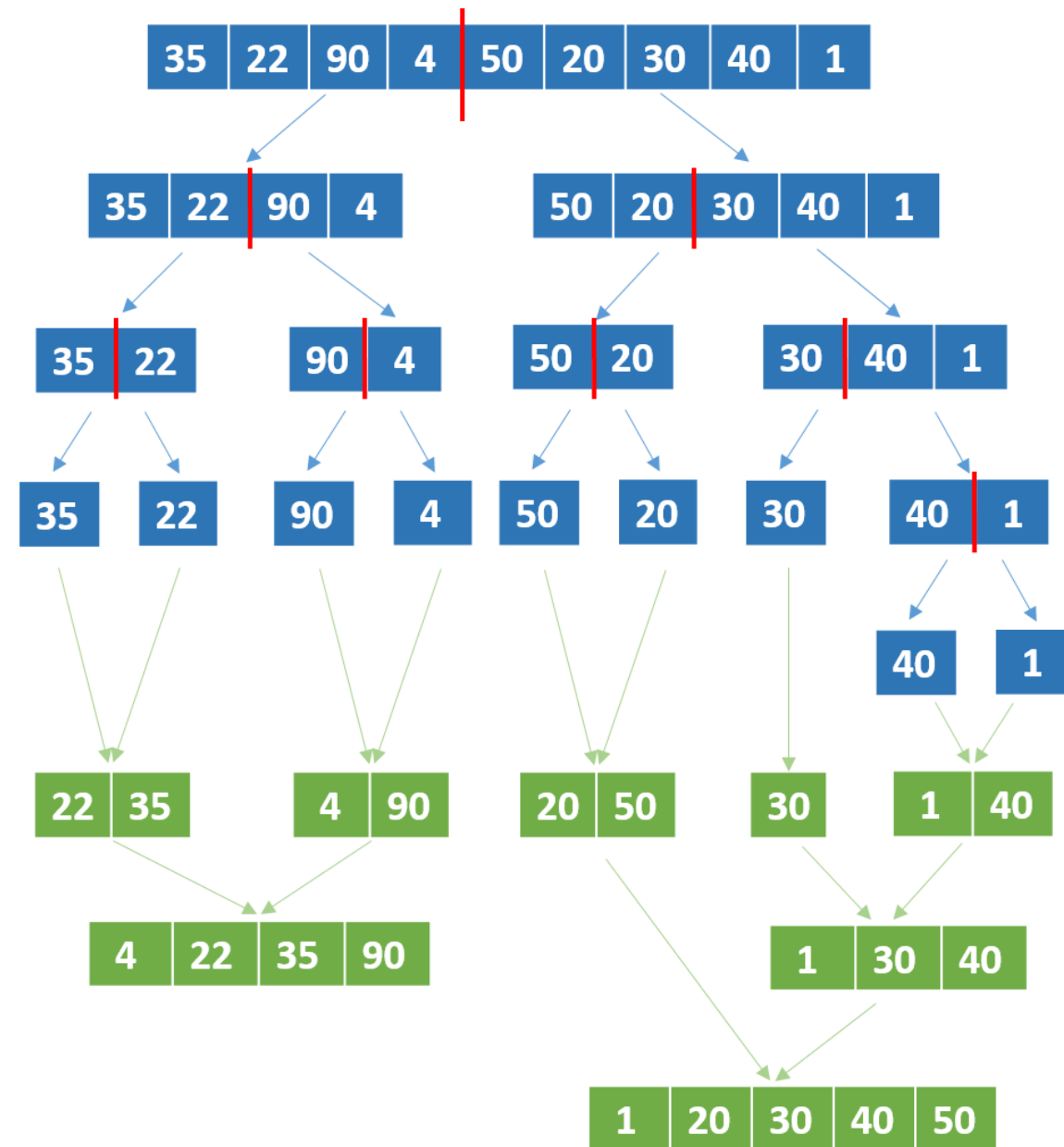
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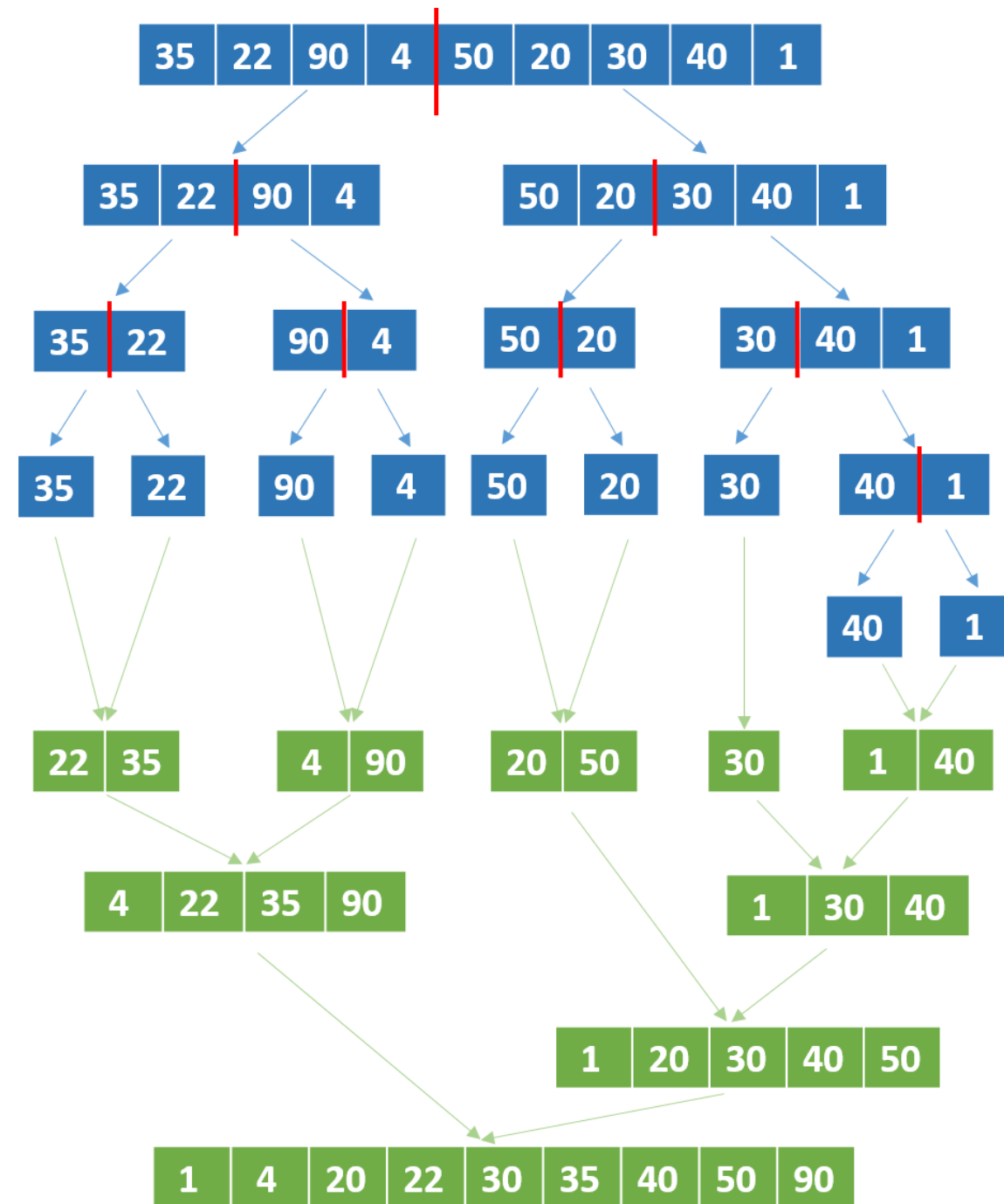
# Merge sort - in action



# Merge sort - in action



# Merge sort - in action



# Merge sort - implementation

```
def merge_sort(my_list):
    if len(my_list) > 1:
        mid = len(my_list)//2
        left_half = my_list[:mid]
        right_half = my_list[mid:]
        merge_sort(left_half)
        merge_sort(right_half)

    i = j = k = 0
    while i < len(left_half) and j < len(right_half):
        if left_half[i] < right_half[j]:
            my_list[k] = left_half[i]
            i += 1
        else:
            my_list[k] = right_half[j]
            j += 1
        k += 1
```

```
while i < len(left_half):
    my_list[k] = left_half[i]
    i += 1
    k += 1

while j < len(right_half):
    my_list[k] = right_half[j]
    j += 1
    k += 1
```

```
my_list = [35,22,90,4,50,20,30,40,1]
merge_sort(my_list)
print(my_list)
```

```
[1, 4, 20, 22, 30, 35, 40, 50, 90]
```

# Merge sort - complexity

- Worst case:  $O(n \log n)$ 
  - significant improvement over bubble sort, selection sort, and insertion sort
  - suitable for sorting large lists
- Average case:  $\Theta(n \log n)$
- Best case:  $\Omega(n \log n)$ 
  - other algorithms (e.g. bubble sort, insertion sort) have better best case complexity
- Space complexity:  $O(n)$ 
  - worst space complexity than other algorithms with  $O(1)$
- Other variants reduce this space complexity

# Let's practice!

DATA STRUCTURES AND ALGORITHMS IN PYTHON

# Quicksort

DATA STRUCTURES AND ALGORITHMS IN PYTHON



**Miriam Antona**  
Software engineer



# Quicksort

- Follows **divide and conquer** principle
- Implemented by many **programming languages**
- **Partition** technique
  - **Pivot**
  - items **smaller** than the pivot -> **left**
  - items **greater** than the pivot -> **right**
- Elements to the **left** will be sorted **recursively**
- Elements to the **right** will be sorted **recursively**

# Quicksort - in action



# Quicksort - in action



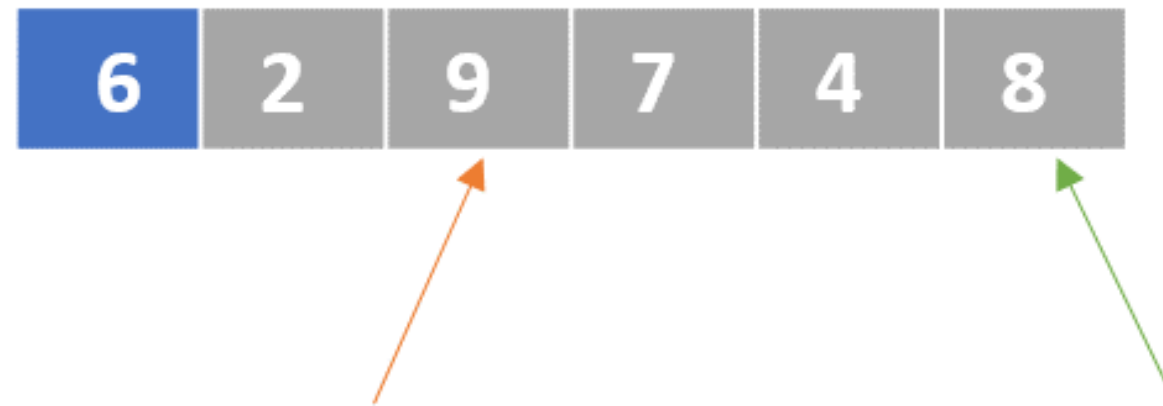
- Hoare's partition

# Quicksort - in action



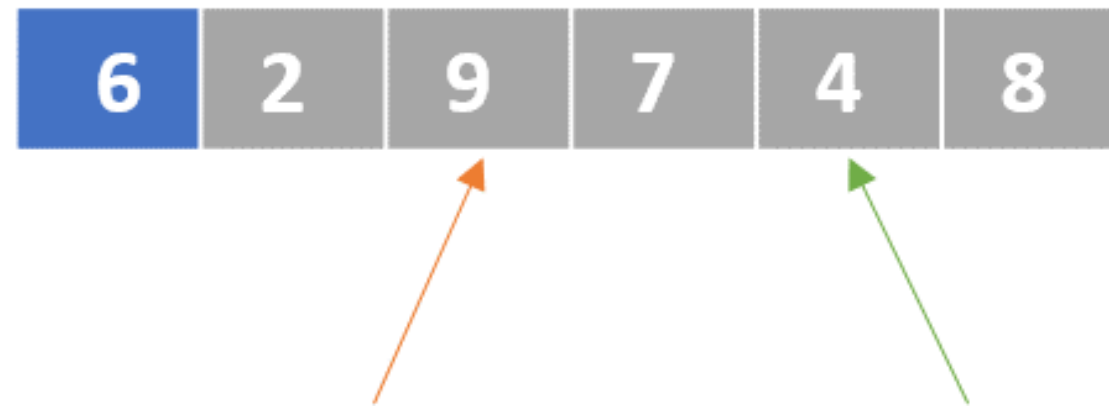
- Hoare's partition
  - Move **left** pointer until a value **greater** than pivot is found

# Quicksort - in action



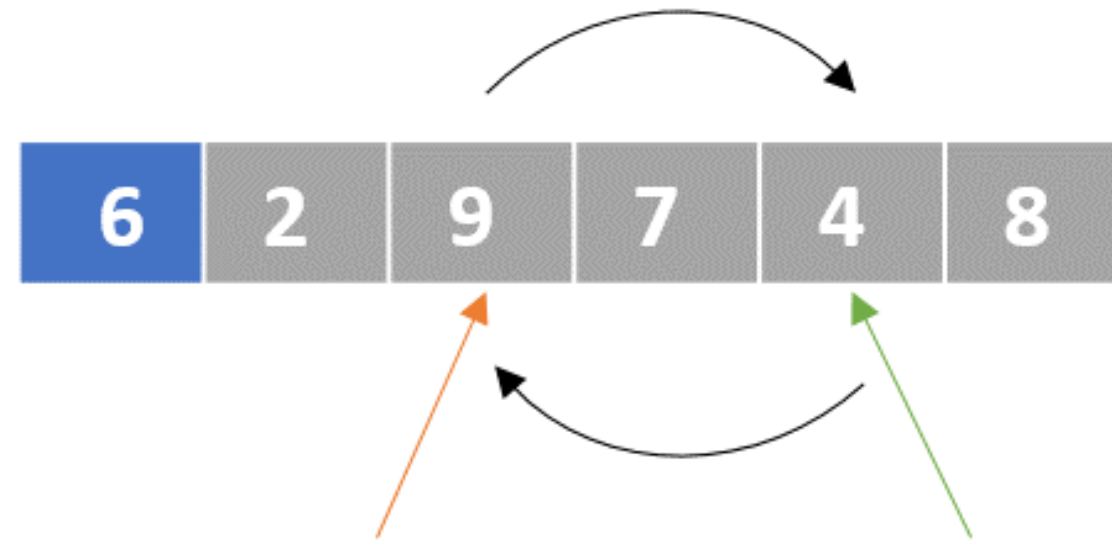
- Hoare's partition
  - Move **left** pointer until a value **greater** than pivot is found

# Quicksort - in action



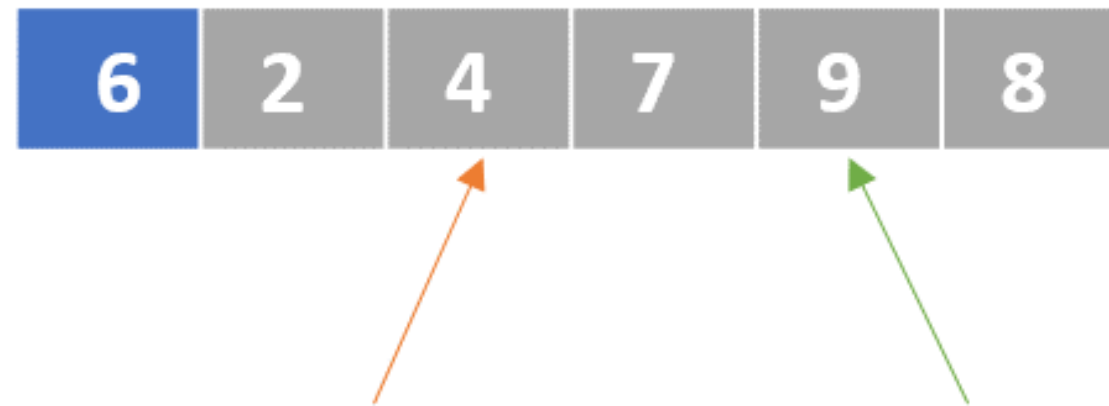
- Hoare's partition
  - Move **left** pointer until a value **greater** than pivot is found
  - Move **right** pointer until a value **lower** than pivot is found

# Quicksort - in action



- Hoare's partition
  - Move **left** pointer until a value **greater** than pivot is found
  - Move **right** pointer until a value **lower** than pivot is found

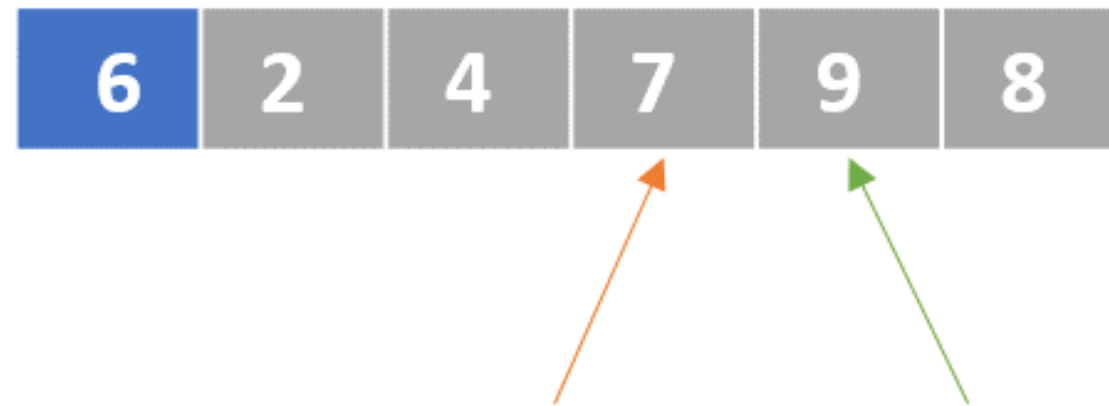
# Quicksort - in action



- Hoare's partition
  - Move **left** pointer until a value **greater** than pivot is found
  - Move **right** pointer until a value **lower** than pivot is found

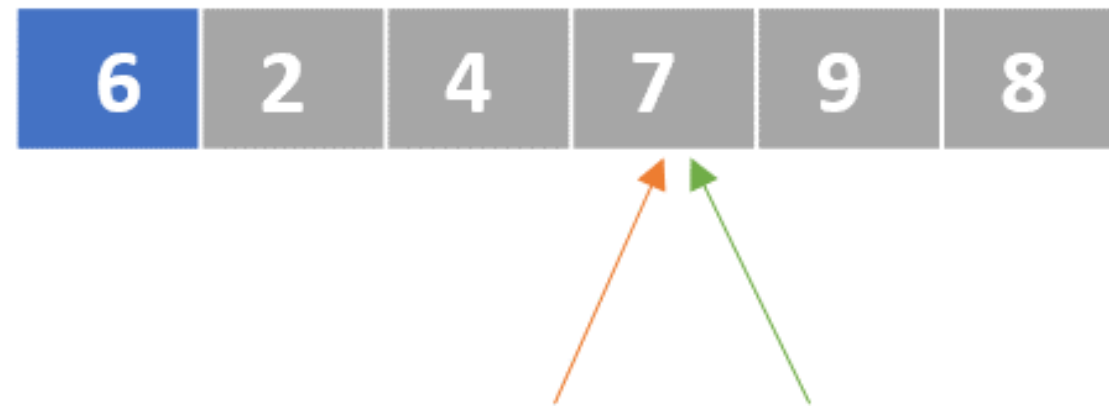


# Quicksort - in action



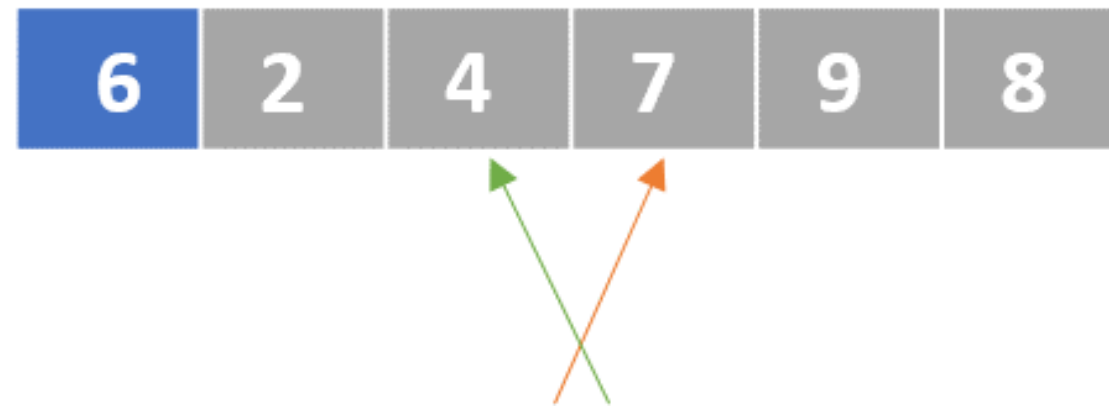
- Hoare's partition
  - Move **left** pointer until a value **greater** than pivot is found
  - Move **right** pointer until a value **lower** than pivot is found

# Quicksort - in action



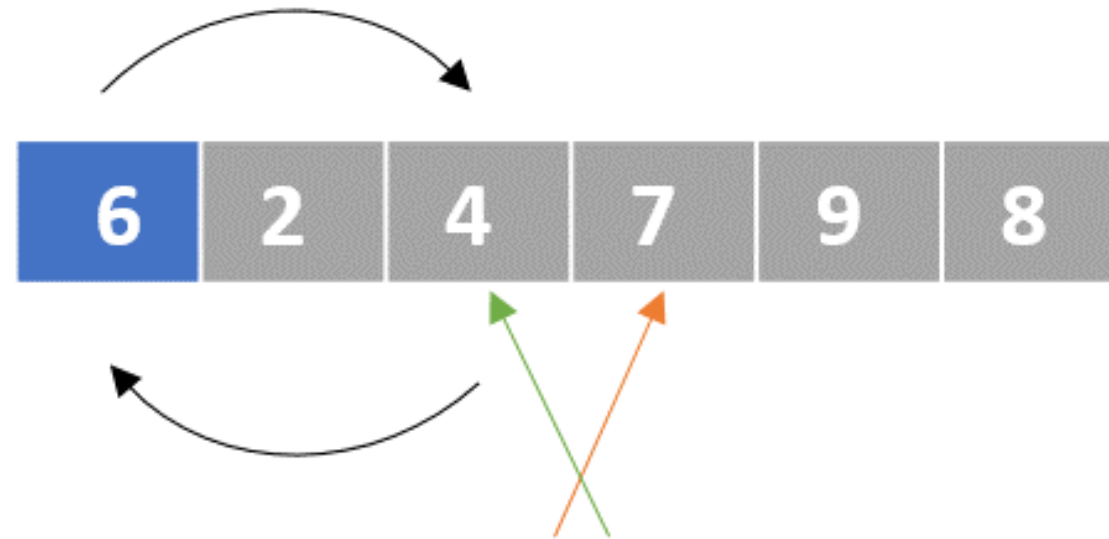
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# Quicksort - in action



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# Quicksort - in action



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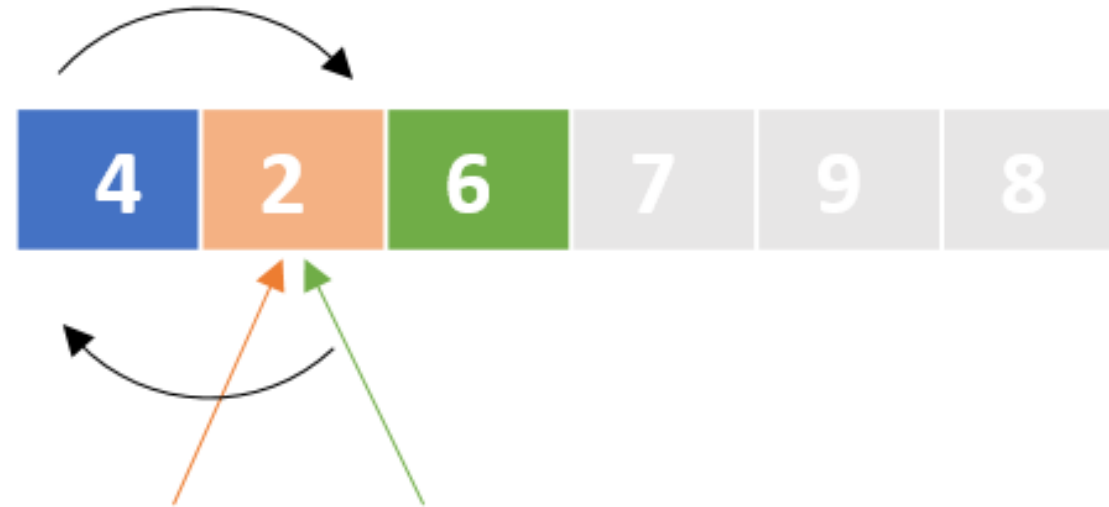
# Quicksort - in action



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  - Move **left** pointer until a value **greater** than pivot is found
  - Move **right** pointer until a value **lower** than pivot is found

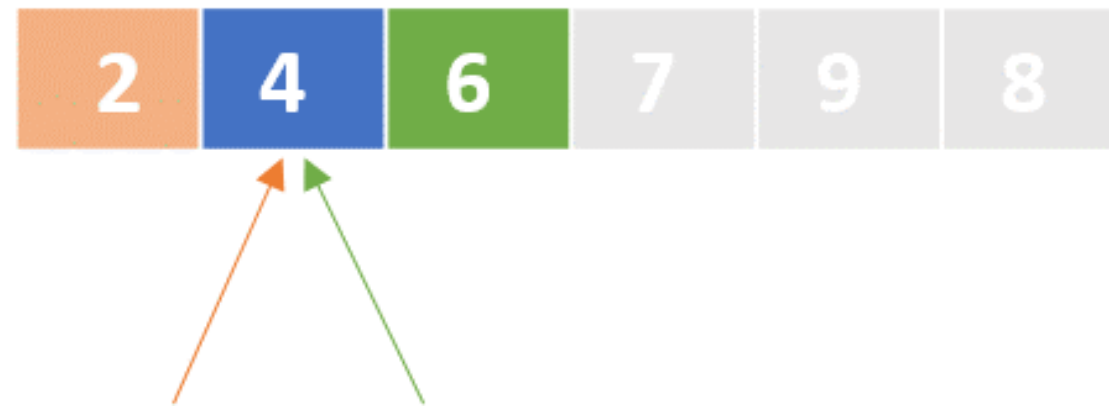


# Quicksort - in action



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  - Move **left** pointer until a value **greater** than pivot is found
  - Move **right** pointer until a value **lower** than pivot is found

# Quicksort - in action



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# Quicksort - in action



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# Quicksort - in action



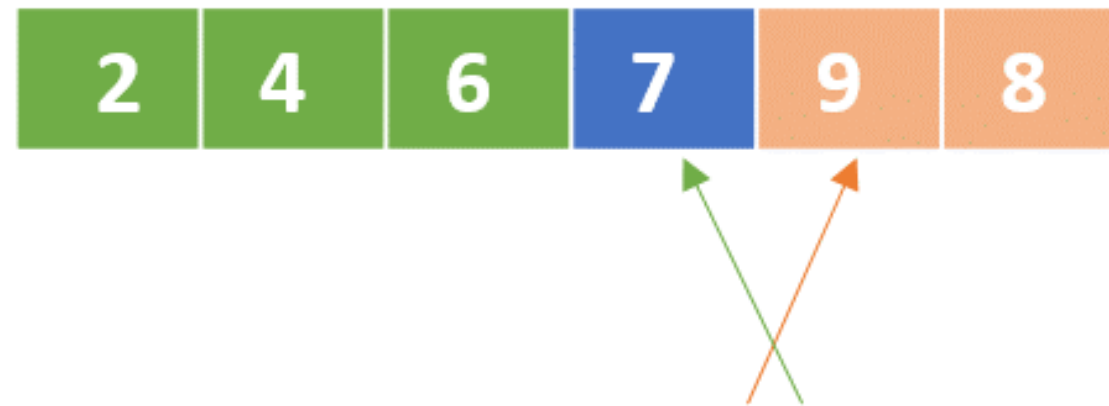
- Hoare's partition
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# Quicksort - in action



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# Quicksort - in action



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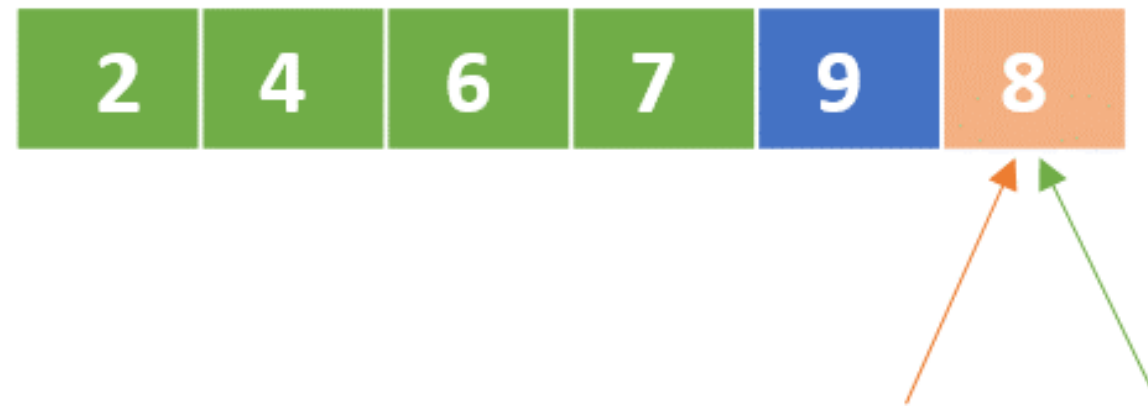


# Quicksort - in action



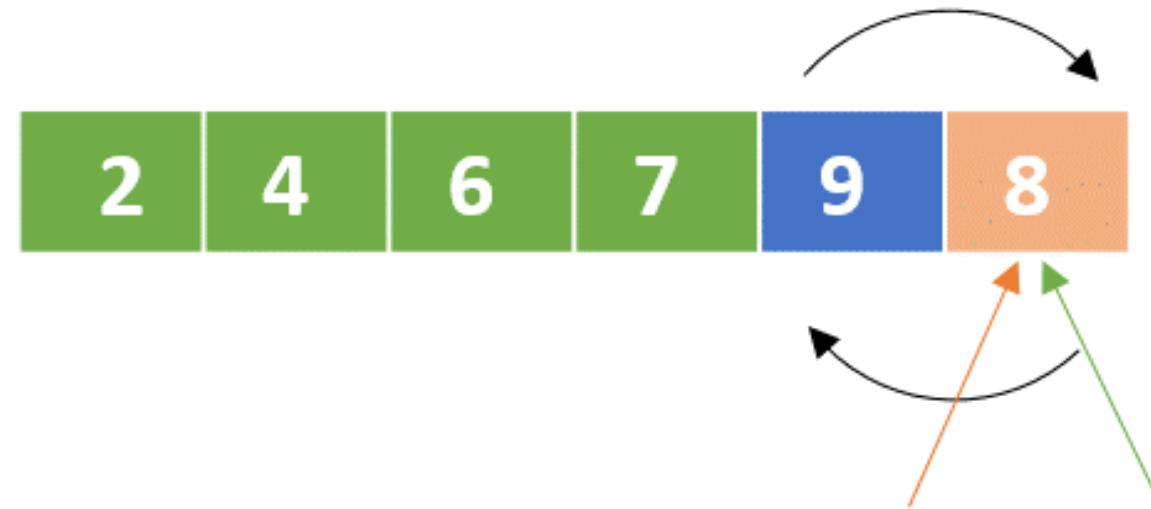
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# Quicksort - in action



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# Quicksort - in action



- Hoare's partition
  - Move **left** pointer until a value **greater** than pivot is found
  - Move **right** pointer until a value **lower** than pivot is found

# Quicksort - implementation

```
def quicksort(my_list, first_index, last_index):  
    if first_index < last_index:  
        partition_index = partition(my_list, first_index, last_index)  
        quicksort(my_list, first_index, partition_index)  
        quicksort(my_list, partition_index + 1, last_index)
```

# Quicksort - implementation

```
def partition(my_list, first_index, last_index):
    pivot = my_list[first_index]
    left_pointer = first_index + 1
    right_pointer = last_index
    while True:
        while my_list[left_pointer] < pivot and left_pointer < last_index:
            left_pointer += 1
        while my_list[right_pointer] > pivot and right_pointer >= first_index:
            right_pointer -= 1
        if left_pointer >= right_pointer:
            break
        my_list[left_pointer], my_list[right_pointer] = my_list[right_pointer], my_list[left_pointer]
    my_list[first_index], my_list[right_pointer] = my_list[right_pointer], my_list[first_index]
    return right_pointer
```

# Quicksort - implementation

```
my_list = [6, 2, 9, 7, 4, 8]
quicksort(my_list, 0, len(my_list) - 1)
print(my_list)
```

```
[2, 4, 6, 7, 8, 9]
```



# Quicksort - complexity

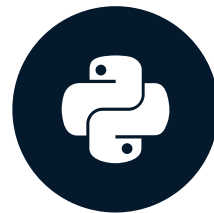
- Worst case:  $O(n^2)$
- Very efficient!
  - Average case:  $\Theta(n \log n)$
  - Best case:  $\Omega(n \log n)$
- Space complexity:  $O(n \log n)$

# Let's practice!

DATA STRUCTURES AND ALGORITHMS IN PYTHON

# Congratulations!

DATA STRUCTURES AND ALGORITHMS IN PYTHON



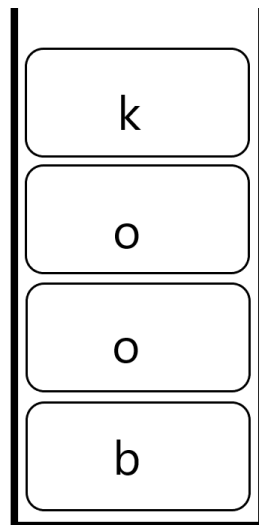
**Miriam Antona**  
Software engineer

# Chapter 1

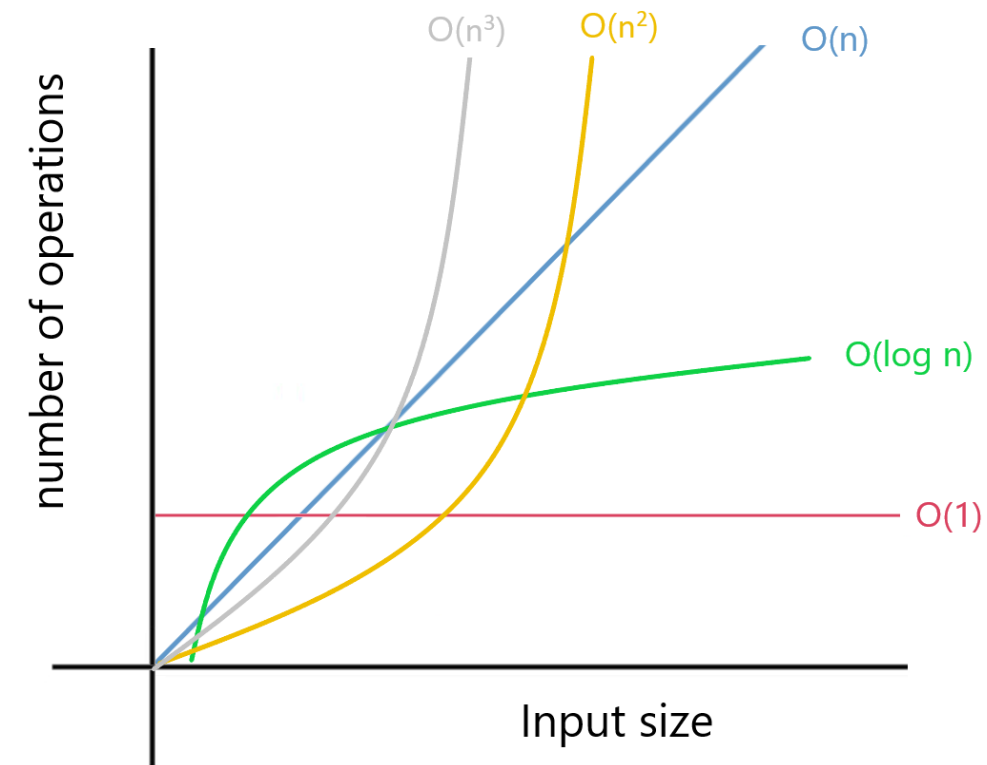
- What algorithms and data structures are
- Linked lists



- Stacks



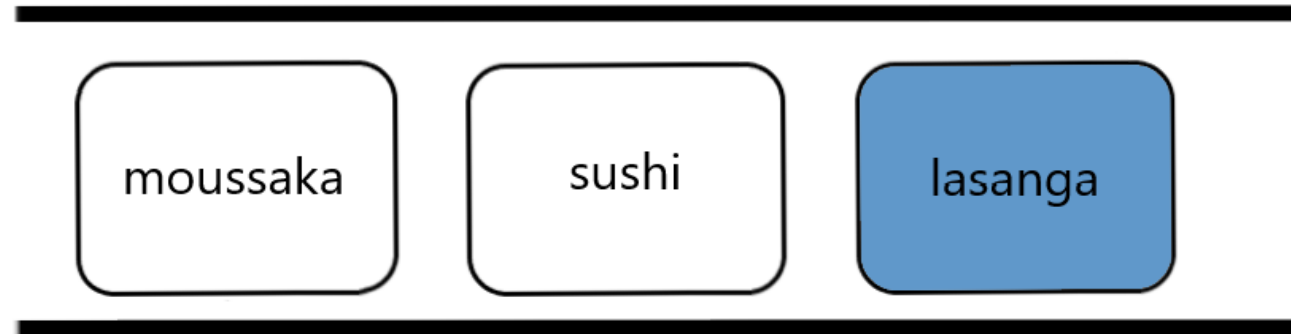
- Calculate time complexity using Big O Notation



# Chapter 2

- Queues

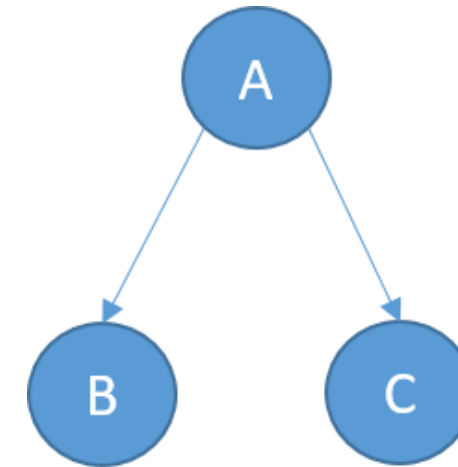
orders\_queue



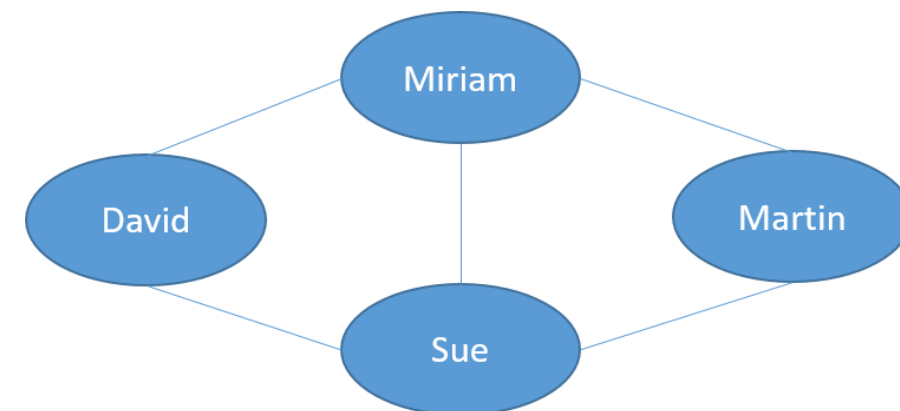
- Hash tables

```
my_menu = {  
    'lasagna': 14.75,  
    'moussaka': 21.15,  
    'sushi': 16.05  
}
```

- Trees



- Graphs

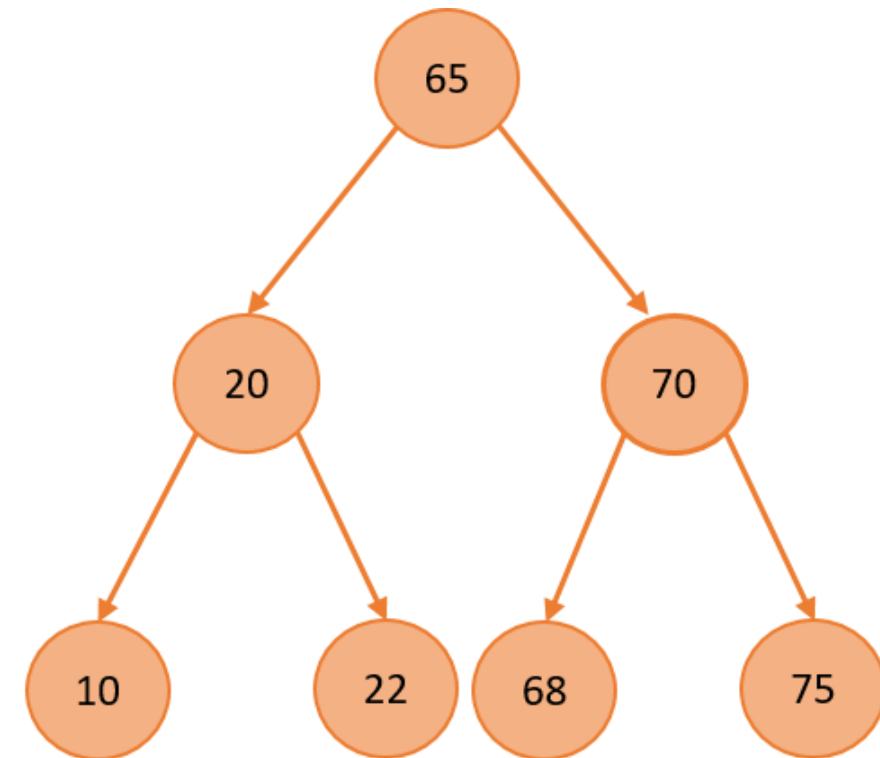


- Recursion

# Chapter 3

- Searching algorithms:
  - Linear search
  - Binary search
  - Depth first search
  - Breadth first search

- Binary search trees



# Chapter 4

- Sorting algorithms
  - Bubble sort
  - Selection sort
  - Insertion sort
  - Merge sort
  - Quicksort

# Thank you!

DATA STRUCTURES AND ALGORITHMS IN PYTHON