

# 1 Angles

let  $T'$  be the extriangle of  $T$ . Then

$$\begin{array}{rcl} A' & = & \frac{\pi-A}{2} \\ B' & = & \dots \end{array}$$

Note:  $T$  will be the orthic of  $T'$ .

let  $T''$  be the orthic of  $T$ . Then, assuming  $T$  is acute, and using the same logic:  $A = \frac{\pi-A''}{2}$  and:

$$\begin{array}{rcl} A'' & = & \pi - 2A \\ B'' & = & \dots \end{array}$$

or:

$$\begin{array}{rcl} \sin(A''/2) & = & \sin(\pi/2 - A) = \cos(A) \\ \sin(B''/2) & = & \cos(B) \\ \sin(C''/2) & = & \cos(C) \end{array}$$

So it appears  $T''$  should conserve the sum of sines of its half-angles.  
It remains to be proven this is also true for obtuse  $T$ .