

Release 10.1

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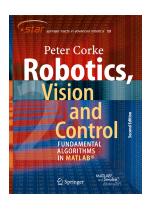
Toolbox home page http://www.petercorke.com/robot

Discussion group http://groups.google.com.au/group/robotics-tool-box

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http://www.petercorke.com

Preface



This, the tenth major release of the Toolbox, representing over twenty five years of continuous development and a substantial level of maturity. This version corresponds to the **second edition** of the book "*Robotics, Vision & Control, second edition*" published in June 2017 – RVC2.

This MATLAB® Toolbox has a rich collection of functions that are useful for the study and simulation of robots: arm-type robot manipulators and mobile robots. For robot manipulators, functions include kinematics, trajectory generation, dynamics and control. For mobile robots, functions include path planning, kinodynamic planning, localization, map building and simultaneous

localization and mapping (SLAM).

The Toolbox makes strong use of classes to represent robots and such things as sensors and maps. It includes Simulink® models to describe the evolution of arm or mobile robot state over time for a number of classical control strategies. The Toolbox also provides functions for manipulating and converting between datatypes such as vectors, rotation matrices, unit-quaternions, quaternions, homogeneous transformations and twists which are necessary to represent position and orientation in 2- and 3-dimensions.

The code is written in a straightforward manner which allows for easy understanding, perhaps at the expense of computational efficiency. If you feel strongly about computational efficiency then you can always rewrite the function to be more efficient, compile the M-file using the MATLAB compiler, or create a MEX version.

The bulk of this manual is auto-generated from the comments in the MATLAB code itself. For elaboration on the underlying principles, extensive illustrations and worked examples please consult "*Robotics*, *Vision & Control*, *second edition*" which provides a detailed discussion (720 pages, nearly 500 figures and over 1000 code examples) of how to use the Toolbox functions to solve many types of problems in robotics.

Functions by category

Contents

Chapter 1

Introduction

1.1 Changes in RTB 10

RTB 10 is largely backward compatible with RTB 9.

1.1.1 Incompatible changes

- The class Vehicle no longer represents an Ackerman/bicycle vehicle model. Vehicle is now an abstract superclass of Bicycle and Unicycle which represent car-like and differentially-steered vehicles respectively.
- The class LandmarkMap replaces PointMap.
- Robot-arm forward kinematics now returns an SE3 object rather than a 4 × 4 matrix.
- The Quaternion class used to represent both unit and non-unit quaternions which was untidy and confusing. They are now represented by two classes UnitQuaternion and Quaternion.
- The method to compute the arm-robot Jacobian in the end-effector frame has been renamed from jacobn to jacobe.
- The path planners, subclasses of Navigation, the method to find a path has been renamed from path to query.
- The Jacobian methods for the RangeBearingSensor class have been renamed to Hx, Hp, Hw, Gx,Gz.
- The function se2 has been replaced with the class SE2. On some platforms (Mac) this is the same file. Broadly similar in function, the former returns a 3×3 matrix, the latter returns an object.
- The function se3 has been replaced with the class SE3. On some platforms (Mac) this is the same file. Broadly similar in function, the former returns a 4×4 matrix, the latter returns an object.

RTB 9	RTB 10
Vehicle	Bicycle
Map	LandmarkMap
jacobn	jacobe
path	query
H_x	Hx
H_xf	Нр
H_w	Hw
G_x	Gx
G_z	Gz

Table 1.1: Function and method name changes

These changes are summarized in Table ??.

1.1.2 New features

- SerialLinkplot3d() renders realistic looking 3D models of robots. STL models from the package ARTE by Arturo Gil (https://arvc.umh.es/arte) are now included with RTB, by kind permission.
- ETS2 and ETS3 packages provide a gentle (non Denavit-Hartenberg) introduction to robot arm kinematics, see Chapter 7 for details.
- Distribution as an .mltbx format file.
- A comprehensive set of functions to handle rotations and transformations in 2D, these functions end with the suffix 2, eg. trans12, rot2, trot2 etc.
- Matrix exponentials are handled by trexp, trlog, trexp2 and trlog2.
- The class Twist represents a twist in 3D or 2D. Respectively, it is a 6-vector representation of the Lie algebra se(3), or a 3-vector representation of se(2).
- The method SerialLink.jointdynamics returns a vector of tf objects representing the dynamics of the joint actuators.
- The class Lattice is a kino-dynamic lattice path planner.
- The class PoseGraph solves graph relaxation problems and can be used for bundle adjustment and pose graph SLAM.
- The class Plucker represents a line using Plücker coordinates.
- \bullet The folder RST contains Live Scripts that demonstrate some capabilities of the MATLAB Robotics System Toolbox TM .
- The folder symbolic contains Live Scripts that demonstrate use of the MAT-LAB Symbolic Math ToolboxTM for deriving Jacobians used in EKF SLAM (vehicle and sensor), inverse kinematics for a 2-joint planar arm and solving for roll-pitch-yaw angles given a rotation matrix.
- All the robot models, prefixed by mdl_, now reside in the folder models.

- New robot models include Universal Robotics UR3, UR5 and UR10; and Kuka light weight robot arm.
- A new folder data now holds various data files as used by examples in RVC2: STL models, occupancy grids, Hershey font, Toro and G2O data files.

Since its inception RTB has used matrices¹ to represent rotations and transformations in 2D and 3D. A trajectory, or sequence, was represented by a 3-dimensional matrix, eg. $4 \times 4 \times N$. In RTB10 a set of classes have been introduced to represent orientation and pose in 2D and 3D: SO2, SE2, SO3, SE3 and UnitQuaternion. These classes are fairly polymorphic, that is, they share many methods and operators². All have a number of static methods that serve as constructors from particular representations. A trajectory is represented by a vector of these objects which makes code easier to read and understand. Overloaded operators are used so the classes behave in a similar way to native matrices³. The relationship between the classical Toolbox functions and the new classes are shown in Fig ??.

You can continue to use the classical functions. The new classes have methods with the names of classical functions to provide similar functionality. For instance

```
>> T = transl(1,2,3); % create a 4x4 matrix
>> trprint(T) % invoke the function trprint
>> T = SE3(1,2,3); % create an SE3 object
>> trprint(T) % invoke the method trprint
>> T.T % the equivalent 4x4 matrix
>> double(T) % the equivalent 4x4 matrix
>> T = SE3(1,2,3); % create a pure translation SE3 object
>> T2 = T*T; % the result is an SE3 object
>> T3 = trinterp(T, 5); % create a vector of five SE3 objects
>> T3(1) % the first element of the vector
>> T3*T % each element of T3 multiplies T, giving a vector of five SE3 objects
```

1.1.3 Enhancements

- Dependencies on the Machine Vision Toolbox for MATLAB (MVTB) have been removed. The fast dilation function used for path planning is now searched for in MVTB and the MATLAB Image Processing Toolbox (IPT) and defaults to a provided M-function.
- A major pass over all code and method/function/class documentation.
- Reworking and refactoring all the manipulator graphics, work in progress.
- An "app" is included: tripleangle which allows graphical experimentation with Euler and roll-pitch-yaw angles.
- A tidyup of all Simulink models. Red blocks now represent user settable parameters, and shaded boxes are used to group parts of the models.

¹Early versions of RTB, before 1999, used vectors to represent quaternions but that changed to an object once objects were added to the language.

²For example, you could substitute objects of class SO3 and UnitQuaternion with minimal code change.

³The capability is extended so that we can element-wise multiple two vectors of transforms, multiply one transform over a vector of transforms or a set of points.

Orientation		Pose		
Classic	New	Classic	New	
rot2	S02	trot2	SE2	
		trans12	SE2	
trplot2	.plot	trplot2	.plot	
rotx, roty, rotz	S03.Rx, S03.Ry, S03.Rz	trotx, troty, trotz	SE3.Rx, SE3.Ry, SE3.Rz	
		T = transl(v)	SE3(v)	
eul2r, rpy2r	S03.eul, S03.rpy	eul2tr, rpy2tr	SE3.eul, SE3.rpy	
angvec2r	SO3.angvec	angvec2tr	SE3.angvec	
oa2r	S03.oa	oa2tr	SE3.oa	
		v = transl(T)	.t, .transl	
tr2eul, tr2rpy	.toeul, .torpy	tr2eul, tr2rpy	.toeul, .torpy	
tr2angvec	.toangvec	tr2angvec	.toangvec	
trexp	SO3.exp	trexp	SE3.exp	
trlog	.log	trlog	.log	
trplot	.plot	trplot	.plot	

Functions starting with dot are methods on the new objects. You can use them in functional form toeul (R) or in dot form R.toeul() or R.toeul. It's a personal preference. The trailing parentheses are not required if no arguments are passed, but it is a useful convention and reminder that you that you are invoking a method not reading a property. The old function transl appears twice since it maps a vector to a matrix as well as the inverse.

	Output type										
Input type	t	Euler	RPY	$\theta_i v$	R	T	Twist vector	Twist	Unit- Quaternion	503	SE3
t (3-vector)						transl		Twist('T')			SE3()
Euler (3-vector)					eul2r	eul2tr			UnitQuater- nion.eul()	SO3.eul()	SE3.eul()
RPY (3-vector)					rpy2r	rpy2tr			UnitQuater- nion.rpy()	S03.rpy()	SE3.rpy()
θ, v (scalar + 3-vector)					angvec2r	angvec2tr			UnitQuater- nion.angvec()	SO3.angvec()	SE3.angvec()
R (3×3 matrix)		tr2eul	tr2rpy	tr2angvec		r2t	trlog		UnitQuater- nion()	SO3()	SE3()
T (4×4 matrix)	transl	tr2eul	tr2rpy	tr2angvec	t2r		trlog	Twist()	UnitQuater- nion()	SO3()	SE3()
Twist vector (3- or 6-vector)					trexp	trexp		Twist()		S03.exp()	SE3.exp()
Twist						.т	.s				.SE
Unit- Quaternion		.toeul	.torpy	.toangvec	.R	т.				.803	.SE3
SO3		.toeul	.torpy	.toangvec	.R	.т	.log		.UnitQuater- nion		.SE3
SE3	.t	.toeul	.torpy	.toangvec	.R	.т	.log	.Twist	.UnitQuater- nion	.S03	

Dark grey boxes are not possible conversions. Light grey boxes are possible conversions but the Toolbox has no direct conversion, you need to convert via an intermediate type. Red text indicates classical Robotics Toolbox functions that work with native MATLAB® vectors and matrices. Class.type() indicates a static factory method that constructs a Class object from input of that type. Functions shown starting with a dot are a method on the class corresponding to that row.

Figure 1.1: (top) new and classic methods for representing orientation and pose, (bottom) functions and methods to convert between representations. Reproduced from "Robotics, Vision & Control, second edition, 2017"

- RangeBearingSensor animation
- All the java code that supports the DHFactor functionality now lives in the folder java. The Makefile in there can be used to recompile the code. There are java version issues and the shipped class files are built to java 1.7 which allows operation

1.2 Changes in RTB 10.2

This release has a relatively small number of bug fixes compared to 10.1:

- Fixed bugs in jacobe and coriolis when using symbolic arguments.
- New robot models: UR3, UR5, UR10, LWR.
- Fixed bug for interp method of SE3 object.
- Fixed bug with detecting Optimisation Toolbox for ikcon and ikunc.
- Fixed bug in ikine_sym.
- Fixed various bugs related to plotting robots with prismatic joints.

1.3 How to obtain the Toolbox

The Robotics Toolbox is freely available from the Toolbox home page at

```
http://www.petercorke.com
```

The file is available in MATLABtoolbox format (.mltbx) or zip format (.zip).

1.3.1 From .mltbx file

Since MATLAB R2014b toolboxes can be packaged as, and installed from, files with the extension .mltbx. Download the most recent version of robot.mltbx or vision.mltbx to your computer. Using MATLAB navigate to the folder where you downloaded the file and double-click it (or right-click then select Install). The Toolbox will be installed within the local MATLAB file structure, and the paths will be appropriately configured for this, and future MATLAB sessions.

1.3.2 From .zip file

Download the most recent version of robot.zip or vision.zip to your computer. Use your favourite unarchiving tool to unzip the files that you downloaded. To add the Toolboxes to your MATLAB path execute the command

```
>> addpath RVCDIR ;
>> startup_rvc
```

where RVCDIR is the full pathname of the folder where the folder rvctools was created when you unzipped the Toolbox files. The script startup_rvc adds various subfolders to your path and displays the version of the Toolboxes. After installation the files for both Toolboxes reside in a top-level folder called rvctools and beneath this are a number of folders:

robot The Robotics Toolbox vision The Machine Vision Toolbox

common Utility functions common to the Robotics and Machine Vision Toolboxes

simulink Simulink blocks for robotics and vision, as well as examples

contrib Code written by third-parties

If you already have the Machine Vision Toolbox installed then download the zip file to the folder above the existing rvctools directory, and then unzip it. The files from this zip archive will properly interleave with the Machine Vision Toolbox files.

You need to setup the path every time you start MATLAB but you can automate this by setting up environment variables, editing your startup.m script, using pathtool and saving the path, or by pressing the "Update Toolbox Path Cache" button under MATLAB General preferences. You can check the path using the command path or pathtool.

A menu-driven demonstration can be invoked by

>> rtbdemo

1.3.3 MATLAB OnlineTM

The Toolbox works well with MATLAB OnlineTM which lets you access a MATLAB session from a web browser, tablet or even a phone. The key is to get the RTB files into the filesystem associated with your Online account. The easiest way to do this is to install MATLAB DriveTM from MATLAB File Exchange or using the Get Add-Ons option from the MATLAB GUI. This functions just like Google Drive or Dropbox, a local filesystem on your computer is synchronized with your MATLAB Online account. Copy the RTB files into the local MATLAB Drive cache and they will soon be synchronized, invoke startup_rvc to setup the paths and you are ready to simulate robots on your mobile device or in a web browser.

1.3.4 Simulink®

Simulink[®] is the block-diagram-based simulation environment for MATLAB. It provides a very convenient way to create and visualize complex dynamic systems, and is particularly applicable to robotics. RTB includes a library of blocks for use in constructing robot kinematic and dynamic models. The block library is opened by

>> roblocks

and a window like that shown in Figure ??(a) will be displayed. Double click a particular category and it will expand into a palette of blocks, like Figure ??(b), that can be dragged into your model.

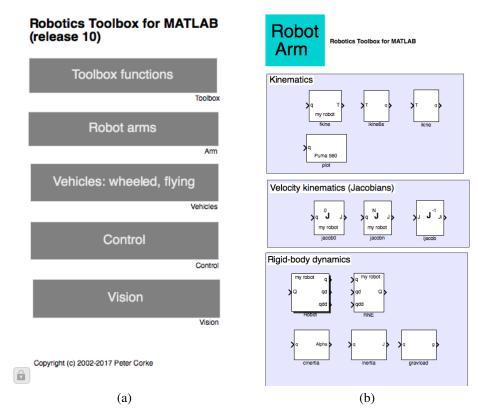


Figure 1.2: The Robotics Toolbox blockset.

Users with no previous Simulink experience are advised to read the relevant Mathworks manuals and experiment with the examples supplied. Experienced Simulink users should find the use of the Robotics blocks quite straightforward. Generally there is a one-to-one correspondence between Simulink blocks and Toolbox functions. Several demonstrations have been included with the Toolbox in order to illustrate common topics in robot control and demonstrate Toolbox Simulink usage. These could be considered as starting points for your own work, just select the model closest to what you want and start changing it. Details of the blocks can be found using the File/ShowBrowser option on the block library window.

Arm robots	
Robot	represents a robot, with generalized joint force input and joint co-
	ordinates, velocities and accelerations as outputs. The parameters
	are the robot object to be simulated and the initial joint angles. It
	is similar to the fdyn () function and represents the forward dy-
	namics of the robot.
rne	computes the inverse dynamics using the recursive Newton-Euler
	algorithm (function rne). Inputs are joint coordinates, velocities
	and accelerations and the output is the generalized joint force.
	The robot object is a parameter.

inertia computes the manipulator joint-space inertia matrix. The parameters are the robot object to be simulated and the initial joint angles. inertia computes the gravity load. The parameters are the robot object to be simulated and the initial joint angles. jacob0 outputs a manipulator Jacobian matrix, with respect to the world frame, based on the input joint coordinate vector. outputs the Jacobian matrix. The robot object is a parameter. jacobn outputs a manipulator Jacobian matrix, with respect to the endeffector frame, based on the input joint coordinate vector. outputs the Jacobian matrix. The robot object is a parameter. ijacob invers a Jacobian matrix. The robot object is a parameter. ijacob invers a Jacobian matrix. The robot object is a parameter. plot creates a graphical animation for the pose of the endeffector corresponding to the input joint coordinates. The robot object is a parameter. Mobile robots Bicycle is the kinematic model of a mobile robot that uses the bicycle model. The inputs are speed and steer angle and the outputs are position and orientation. is the kinematic model of a mobile robot that uses the unicycle, or differential steering, model. The inputs are speed and turn raate and the output is translational and angular position and velocity. Parameter is a quadrotor structure. N-rotor is the dynamic model of a N-rotor flyer. The inputs are rotor speeds and the output is translational and angular position and velocity. Parameter is a quadrotor structure. ControlMixer accepts thrust and torque commands and outputs rotor speeds for a quadrotor. Quadrotor plot parameter is a quadrotor structure. Trajectory jtraj outputs coordinates of a point following a quintic polynomial as a function of time, as well as its derivatives. Initial and final velocity are assumed to be zero. The parameters include the initial and final points as well as the overall motion time. outputs to ordinates of a point following an LSPB trajectory as a function of time. The parameters include the initi	cinertia	computes the manipulator Cartesian inertia matrix. The parameters are the robot object to be simulated and the initial joint an-
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and the output is translational and angular position and velocity. Parameter is a quadrotor structure. N-rotor is the dynamic model of a N-rotor flyer. The inputs are rotor speeds and the output is translational and angular position and velocity. Parameter is a quadrotor structure. ControlMixer accepts thrust and torque commands and outputs rotor speeds for a quadrotor. Quadrotor creates a graphical animation of the quadrotor in a new window. Parameter is a quadrotor structure. Trajectory jtraj outputs coordinates of a point following a quintic polynomial as a function of time, as well as its derivatives. Initial and final velocity are assumed to be zero. The parameters include the initial and final points as well as the overall motion time. lspb outputs coordinates of a point following an LSPB trajectory as a function of time. The parameters include the initial and final points as well as the overall motion time. circle outputs the xy-coordinates of a point around a circle. Parameters	Unicycle	is the kinematic model of a mobile robot that uses the unicycle, or differential steering, model. The inputs are speed and turn raate
is the dynamic model of a N-rotor flyer. The inputs are rotor speeds and the output is translational and angular position and velocity. Parameter is a quadrotor structure. ControlMixer accepts thrust and torque commands and outputs rotor speeds for a quadrotor. Quadrotor creates a graphical animation of the quadrotor in a new window. Parameter is a quadrotor structure. Trajectory jtraj outputs coordinates of a point following a quintic polynomial as a function of time, as well as its derivatives. Initial and final velocity are assumed to be zero. The parameters include the initial and final points as well as the overall motion time. outputs coordinates of a point following an LSPB trajectory as a function of time. The parameters include the initial and final points as well as the overall motion time. circle outputs the xy-coordinates of a point around a circle. Parameters	Quadrotor	and the output is translational and angular position and velocity.
ControlMixer accepts thrust and torque commands and outputs rotor speeds for a quadrotor. Quadrotor creates a graphical animation of the quadrotor in a new window. Parameter is a quadrotor structure. Trajectory jtraj outputs coordinates of a point following a quintic polynomial as a function of time, as well as its derivatives. Initial and final velocity are assumed to be zero. The parameters include the initial and final points as well as the overall motion time. outputs coordinates of a point following an LSPB trajectory as a function of time. The parameters include the initial and final points as well as the overall motion time. circle outputs the xy-coordinates of a point around a circle. Parameters	N-rotor	is the dynamic model of a N-rotor flyer. The inputs are rotor speeds and the output is translational and angular position and
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outputs coordinates of a point following an LSPB trajectory as a function of time. The parameters include the initial and final points as well as the overall motion time. circle outputs the xy-coordinates of a point around a circle. Parameters		locity are assumed to be zero. The parameters include the initial
outputs the xy-coordinates of a point around a circle. Parameters	lspb	outputs coordinates of a point following an LSPB trajectory as a function of time. The parameters include the initial and final
are the centre, radius and angular frequency.		noints as well as the overall motion time

Vision	
camera	input is a camera pose and the output is the coordinates of points projected on the image plane. Parameters are the camera object and the point positions.
camera2	input is a camera pose and point coordinate frame pose, and the output is the coordinates of points projected on the image plane. Parameters are the camera object and the point positions relative to the point frame.
image	input is image points and output is the point feature Jacobian.
Jacobian	Parameter is the camera object.
image	input is image points in spherical coordinates and output is the
Jacobian	point feature Jacobian. Parameter is a spherical camera object.
sphere	computes camera pose from image points. Parameter is the camera object.
Pose	computes camera pose from image points. Parameter is the cam-
estimation	era object.
Miscellaneous	-
Inverse	outputs the inverse of the input matrix.
Pre	outputs the input homogeneous transform pre-multiplied by the
multiply	constant parameter.
Post	outputs the input homogeneous transform post-multiplied by the
multiply	constant parameter.
inv Jac	inputs are a square Jacobian J and a spatial velocity v and outputs are J^{-1} and the condition number of J .
pinv Jac	inputs are a Jacobian J and a spatial velocity and outputs are J+ and the condition number of J.
tr2diff	outputs the difference between two homogeneous transformations as a 6-vector comprising the translational and rotational difference.
xyz2T	converts a translational vector to a homogeneous transformation matrix.
rpy2T	converts a vector of roll-pitch-yaw angles to a homogeneous transformation matrix.
eul2T	converts a vector of Euler angles to a homogeneous transformation matrix.
T2xyz	converts a homogeneous transformation matrix to a translational vector.
T2rpy	converts a homogeneous transformation matrix to a vector of roll-pitch-yaw angles.
T2eul	converts a homogeneous transformation matrix to a vector of Euler angles.
angdiff	computes the difference between two input angles modulo 2π .

A number of models are also provided:

D.1.4	
Robot manipulator arms	
sl_rrmc	Resolved-rate motion control
sl_rrmc2	Resolved-rate motion control (relative)
sl_ztorque	Robot collapsing under gravity
sl_jspace	Joint space control
sl_ctorque	Computed torque control
sl_fforward	Torque feedforward control
sl_opspace	Operational space control
sl_sea	Series-elastic actuator
vloop_test	Puma 560 velocity loop
ploop_test	Puma 560 position loop
Mobile ground robot	
sl braitenberg	Braitenberg vehicle moving to a source
sl_lanechange	Lane changing control
sl_drivepoint	Drive to a point
sl_driveline	Drive to a line
sl_drivepose	Drive to a pose
sl_pursuit	Drive along a path
Flying robot	
sl_quadrotor	Quadrotor control
— -	
sl_quadrotor_vs	Control visual servoing to a target

1.3.5 Notes on implementation and versions

The Simulink blocks are implemented in Simulink itself with calls to MATLAB code, or as Level-1 S-functions (a proscribed coding format which MATLAB functions to interface with the Simulink simulation engine).

Simulink allows signals to have matrix values but not (yet) object values. Transformations must be represented as matrices, as per the classic functions, not classes. Very old versions of Simulink (prior to version 4) could only handle scalar signals which limited its usefulness for robotics.

1.3.6 Documentation

This document robot.pdf is a comprehensive manual that describes all functions in the Toolbox. It is auto-generated from the comments in the MATLAB code and is fully hyperlinked: to external web sites, the table of content to functions, and the "See also" functions to each other.

1.4 Compatible MATLAB versions

The Toolbox has been tested under R2016b and R2017bPRE. Compatibility problems are increasingly likely the older your version of MATLAB is.

1.5 Use in teaching

This is definitely encouraged! You are free to put the PDF manual (robot.pdf or the web-based documentation html/*.html on a server for class use. If you plan to distribute paper copies of the PDF manual then every copy must include the first two pages (cover and licence).

Link to other resources such as MOOCs or the Robot Academy can be found at www.petercorke.com/moocs.

1.6 Use in research

If the Toolbox helps you in your endeavours then I'd appreciate you citing the Toolbox when you publish. The details are:

```
@book{Corke17a,
   Author = {Peter I. Corke},
   Note = {ISBN 978-3-319-54413-7},
   Edition = {Second},
   Publisher = {Springer},
   Title = {Robotics, Vision \& Control: Fundamental Algorithms in {MATLANY Year = {2017}}}
or
```

P.I. Corke, Robotics, Vision & Control: Fundamental Algorithms in MAT-LAB. Second edition. Springer, 2017. ISBN 978-3-319-54413-7.

which is also given in electronic form in the CITATION file.

1.7 Support

There is no support! This software is made freely available in the hope that you find it useful in solving whatever problems you have to hand. I am happy to correspond with people who have found genuine bugs or deficiencies but my response time can be long and I can't guarantee that I respond to your email.

I can guarantee that I will not respond to any requests for help with assignments or homework, no matter how urgent or important they might be to you. That's what your teachers, tutors, lecturers and professors are paid to do.

You might instead like to communicate with other users via the Google Group called "Robotics and Machine Vision Toolbox"

```
http://tiny.cc/rvcforum
```

which is a forum for discussion. You need to signup in order to post, and the signup process is moderated by me so allow a few days for this to happen. I need you to write a few words about why you want to join the list so I can distinguish you from a spammer or a web-bot.

1.8 Related software

1.8.1 Robotics System ToolboxTM

The Robotics System Toolbox TM (RST) from MathWorks is an official and supported product. System toolboxes (see also the Computer Vision System Toolbox) are aimed at developers of systems. RST has a growing set of functions for mobile robots, arm robots, ROS integration and pose representations but its design (classes and functions) and syntax is quite different to RTB. A number of examples illustrating the use of RST are given in the folder RST as Live Scripts (extension .mlx), but you need to have the Robotics System Toolbox TM installed in order to use it.

1.8.2 Octave

GNU Octave (www.octave.org) is an impressive piece of free software that implements a language that is close to, but not the same as, MATLAB. The Toolboxes will not work well with Octave, though with Octave 4 the incompatibilities are greatly reduced. An old version of the arm-robot functions described in Chap. 7–9 have been ported to Octave and this code is distributed in RVCDIR/robot/octave.

Many Toolbox functions work just fine under Octave. Three important classes (Quaternion, Link and SerialLink) will not work so modified versions of these classes is provided in the subdirectory called Octave. Copy all the directories from Octave to the main Robotics Toolbox directory. The Octave port is now quite dated and not recently tested – it is offered in the hope that you might find it useful.

1.8.3 Machine Vision toolbox

Machine Vision toolbox (MVTB) for MATLAB. This was described in an article

```
@article{Corke05d,
    Author = {P.I. Corke},
    Journal = {IEEE Robotics and Automation Magazine},
    Month = nov,
    Number = {4},
    Pages = {16-25},
    Title = {Machine Vision Toolbox},
    Volume = {12},
    Year = {2005}}
```

and provides a very wide range of useful computer vision functions and is used to illustrate principals in the Robotics, Vision & Control book. You can obtain this from http://www.petercorke.com/vision. More recent products such as MAT-LABImage Processing Toolbox and MATLABComputer Vision System Toolbox provide functionality that overlaps with MVTB.

1.9 Contributing to the Toolboxes

I am very happy to accept contributions for inclusion in future versions of the toolbox. You will, of course, be suitably acknowledged (see below).

1.10 Acknowledgements

I have corresponded with a great many people via email since the first release of this Toolbox. Some have identified bugs and shortcomings in the documentation, and even better, some have provided bug fixes and even new modules, thankyou. See the file CONTRIB for details.

Giorgio Grisetti and Gian Diego Tipaldi for the core of the pose graph solver. Arturo Gil for allowing me to ship the STL robot models from ARTE. Jörn Malzahn has donated a considerable amount of code, his Robot Symbolic Toolbox for MATLAB. Bryan Moutrie has contributed parts of his open-source package phiWARE to RTB, the remainder of that package can be found online. Other mentions to Gautam Sinha, Wynand Smart for models of industrial robot arm, Paul Pounds for the quadrotor and related models, Paul Newman for inspiring the mobile robot code, and Giorgio Grissetti for inspiring the pose graph code.

Chapter 2

Functions and classes