Best Practices in Latent Class Analysis using Free Open Source Software

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Abstract

Latent class analysis is a family of techniques for identifying groups in data based on a parametric model. Its examples include mixture models, latent class analysis (with continuous and/or ordinal indicators), and latent class (mixture) growth analysis. Despite the popularity of this technique, there is limited guidance with respect to best practices in estimating and reporting mixture models. Moreover, although user-friendly interfaces for advanced mixture modeling have long been available in commercial software packages, open source alternatives have remained somewhat inaccessible. This tutorial describes best practices for the estimation and reporting of latent class analysis, using free and open source software in R. To this end, this tutorial introduces new functionality for estimating and reporting mixture models in the `tidySEM` R-package whose backend relies on the `OpenMx` R-package.

Keywords: latent class analysis, mixture models, best practices, free open source software, tidySEM

Word count: 9001

Best Practices in Latent Class Analysis using Free Open Source Software

Latent class analysis (LCA) is an umbrella term that refers to a number of techniques for estimating unobserved group membership based on a parametric model of one or more observed indicators of group membership. The types of LCA have become quite popular across scientific fields, most notably finite Gaussian mixture modeling and latent profile analysis. Vermunt et al. (2004) defined LCA more generally as virtually any statistical model where "some of the parameters [...] differ across unobserved subgroups".

Despite its popularity, there is a lack of standards for estimating and reporting LCA. While Van De Schoot, Sijbrandij, Winter, Depaoli, and Vermunt (2017) developed reporting guidelines for a specific type of LCA known as latent growth models, general reporting guidelines for all LCA are still lacking. This complicates manuscript review and assessment of the quality of published studies, and introduces a risk of misapplications of the technique. The present paper seeks to address this gap in the literature by suggesting updated guidelines for estimation and reporting of LCA, based on current best practices. Importantly, in order to lower the barrier of entry and ensure reproducibility of all examples, this paper exclusively relies on free, open source software in R. Our goal is to make best-practices in LCA widely accessible.

Defining Latent Class Analysis

Latent class analysis is a group of methods for estimating unobserved groups based on a parametric model of observed indicators of group membership. The concept of LCA can be understood in different ways. A mixture model assumes that the study population is composed of K subpopulations or classes. It further assumes that the observed data are a mixture of data generated by class-specific models. The simplest univariate model is a normal distribution, which can be described with two parameters: the mean and the variance. Commonly, the same model is estimated across all classes, but with different

parameters for each class (i.e., class-specific means and variances). Mixture modeling then estimates both the parameters for each class, and the probability that an individual belongs to each class. This way, describing the whole sample with a single mean and variance is a special case where we assume the sample is homogeneous in function of these parameters.

As an illustrative example, imagine that a detective wants to know if it would be possible to use mixture modeling to identify the sex of a suspect, based on footprints found at the crime scene. To test the feasibility of this approach, the detective records the shoe sizes and sex of 100 volunteers. The resulting observed data look like this:

The distribution is evidently bimodal, which bodes well for the intended mixture model. In this case, the number of classes is known a-priori. When estimating a two-class mixture model, the detective observes that the model estimates the mean shoe size of the two groups are equal to 9.22 and 7.25, which is close to the true means of the two groups, namely 9.04 and 6.93. When tabulating estimated group membership against observed (known) group membership, it can be seen that women are classified with a high degree of accuracy, but men are not:

Table 1

Observed group membership by estimated class membership.

Observed	Class 1	Class 2
Man	28	21
Woman	0	51

LCA is like confirmatory factor analysis, except that the continuous latent variable is substituted with a categorical latent variable. Both assume that the indicators are related, and these relations can be represented by the underlying latent variable. One difference between the two techniques is that factor analysis can be considered as a way to group observed *variables* into latent constructs, and LCA groups *individuals* into classes.While factor analysis seeks to describe the relations between variables, LCA seeks to describe each
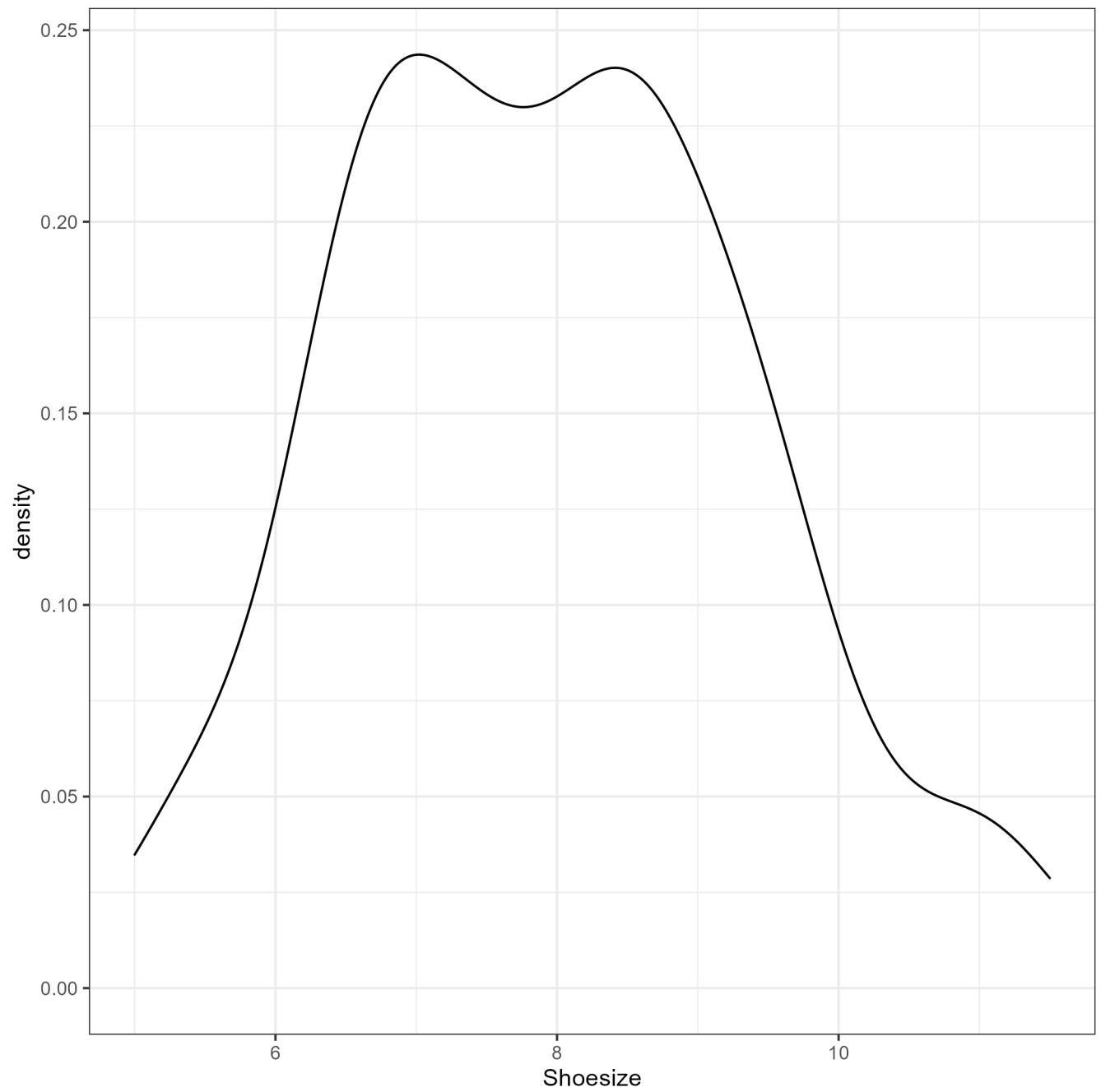
Figure 1. Kernel density plot of shoe sizes.

unobserved group and the differences between them. In line with this distinction, LCA (mixture models) is referred to as a "person-centered" technique, and factor analysis as a "variable-centered" technique (Masyn, 2013; Nylund-Gibson & Choi, 2018).

When the focus is on the model parameters in each group, LCA can be thought of as similar to a multi-group structural equation model. The main distinction is that group membership is not known a-priori, but is instead estimated – with measurement error – based on the data. Whereas in a multi-group model, the data are split by group and treated as independent samples, in LCA, all cases contribute to the estimation of all parameters in all groups. The relative contribution of each case to the parameters of each group is determined by that case's posterior probability of belonging to that group.

In factor analysis, the latent variable is continuous, so the relation between indicators is defined by the communalities between them, and the latent variable represents the error corrected approximation of the sample. While in LCA, the relation between indicators is define by how well they separate the classes, as a multinomial regression between indicators and latent variable (Masyn, 2013)

When the focus is on each individual's estimated class membership, LCA can be thought of as a type of clustering algorithm. In line with this perspective, LCA is sometimes described as "model-based clustering" (Hennig, Meila, Murtagh, & Rocci, 2015; Scrucca, Fop, Murphy, & Raftery, 2016). Many clustering algorithms apply some recursive splitting algorithm to the data. By contrast "model-based" clustering refers to the fact that LCA estimates cluster membership based on a parametric model. Specifically, the posterior class probability that an individual belongs to a latent class can be computed from the likelihood of that individual's observed data under given the class-specific model. For these differences, LCA is a clustering method, that corrects for (random) measurement error, while clustering algorithms do not correct for. This is something LCA has in common with factor analysis, as both model an underlying latent variable, which accounts for the communalities between

indicators and correcting for measurement error. 0

Finally, in the context of machine learning, LCA can be considered as an *unsupervised classification* problem (Figueiredo & Jain, 2002). The term *unsupervised* refers to the fact that the outcome variable – true class membership – is not known, and the term *classification* refers to the fact that the algorithm is predicting a categorical outcome – class membership.

A Taxonomy of Latent Class Analysis Methods

In this paper, we use the term latent class analysis to refer to a family of techniques that estimate latent class membership based on a parametric model of observed indicators. From a historical perspective, the term was initially conceived to refer to analyses with categorical, usually binary indicators (Vermunt et al., 2004). Nowadays, there are a number of related techniques, known by distinct names, that serve a similar purpose. The term "latent class analysis" seems most appropriate as an umbrella term for this broader class of models, as it only refers to the purpose of the analysis, and does not imply restrictions to the model used, or the level of measurement of the indicators. Given the abundance of terms in use for closely related classes of models, we will provide a rudimentary taxonomy of LCA methods.

A common type of LCA is the *finite Gaussian mixture model*; a univariate analysis where the observed distribution of a single variable is assumed to result from a mixture of a known number of normal (Gaussian) distributions. The parameters of a finite Gaussian mixture model are the means and variances of these underlying normal distributions. The analysis of shoe sizes presented earlier is a canonical example of this type of analysis. In the multivariate case, with more than one indicator variable, the parameters of a mixture model are the means, variances, and covariances between the indicators (which can be standardized to obtain correlations). These parameters can be estimated freely, or set to be constrained across classes (Collins & Lanza, 2009).

The technique known as *latent profile analysis (LPA)* is a special case of the mixture model, which assumes conditional independence of the indicators. Conditional independence means that, after class membership is accounted for, the covariances/correlations between indicators are assumed to be zero. This can be conceived of as a restricted mixture model with covariances fixed to zero. Stating that the covariances/correlations are accounted by the latent variable. In some cases, such constraints will be inappropriate; for instance when the cohesion between indicators is expected to differ between classes (Collins & Lanza, 2009). As an example, a LPA of ocean plastic particles found two classes of particles based on length and width: a class of smaller particles with a high correlation between length and width, meaning that these particles were approximately round or square in shape, and a class of larger particles with a low correlation between length and width, meaning that these particles were heterogenous in shape. From a theoretical perspective, this makes sense, because the smaller particles have been ground down to a more uniform shape by the elements.

It is also possible to estimate a mixture model based on latent indicators. This means that, within each class, one or more continuous latent variables are estimated based on the observed indicators. Categorical latent variable membership is then estimated based on these continuous latent variables. A common application of this approach is in longitudinal research, where the indicators reflect one construct assessed at different time points. Examples of this approach include *growth mixture models* (GMM) and *latent class growth analyses* (LCGA). These techniques estimate a latent growth model to describe grouped trajectories over time. The growth mixture model is a latent class model where the parameters that indicate class membership are the intercepts and variances, and typically covariances of the latent growth variables, e.g., a latent intercept and slope. This technique assumes that individuals within a class can have heterogenous trajectories. If the variance of the growth parameters is fixed to zero, it is known as a latent class growth analysis. This latter approach assumes that all individuals within a class share the same identical trajectory, and that any variance in the indicators not explained by the class-specific latent

trajectories is due to residual error variance.

The term latent class analysis originally referred to cases where the observed indicators were categorical (Collins & Lanza, 2009). Nowadays, it is more commonly used as an umbrella term. To prevent ambiguity, the special case where indicators are of binary or ordinal measurement level might be described as *latent class analysis with ordinal indicators*. Latent class models with ordinal indicators are parameterized differently from mixture models. One common parameterization assumes that each categorical variable reflects an underlying standard normal distribution. The parameters are "thresholds" that correspond to quantiles of a standard normal distribution (with $N(\mu = 0, \sigma = 1)$). These thresholds are estimated based on the proportion of individuals in each of the response categories of the indicator variable. For example, a binary indicator has a single threshold that distinguishes the two response categories. If responses are distributed 50/50, then the corresponding threshold would be $t_1 = 0.00$. If the responses are distributed 60/40, then the resulting threshold would be $t_1 = 0.25$.

This paper will primarily focus on mixture models and special cases thereof, although most of the suggested guidelines are applicable to all LCA methods.

Use Cases for Latent Class Analysis

There are several use cases for which LCA methods are suitable. One example is to test a theory that postulates the existence of a categorical latent variable. For example, *identity status theory* posits that, at any given point in time, adolescents reside in one of four identity statuses. Latent class analysis can be used to identify these four statuses based on observed indicators (e.g., self-reported identity exploration and commitment). If results indicate that the data are better described by a different number of classes, or that the four-class solution does not correspond to the predicted pattern of responses on the indicators, then the theory may be called into question.

Another use case is unsupervised learning: when the goal is to restore unobserved class membership based on observed indicators, or to classify individuals. For example, a mixture model can be used as a diagnostic aid when several clinical indicators can be used to distinguish between a fixed number of physical (Baughman, Bisgard, Lynn, & Meade, 2006), mental (Wu, Woody, Yang, Pan, & Blazer, 2011) health problems, or health outcomes after recovering from cancer (Hardy, Garnier-Villarreal, McCarthy, Anderson, & Reynolds, 2018). The example of shoe size is a rudimentary illustration of this type of application.

LCA can be used as a descriptive analysis where a researcher wishes to describe their sample and identify a few prototypes based on many variables. As an example, if a survey among all Dutch academics was carried out with the goal of bringing about a funding reform, LCA could be used to discover the types of publications that get funding.

With LCA, our goal could be to inductively identify the number of classes. For instance, if we believe that a variable represents a group, but don't know how many groups there are, LCA may be an appropriate technique to answer this question. For example, Hopfer, Tan, and Wylie (2014) studied substance use, sexual behavior, and mental health status of urban population in Winnipeg, Canada. The underlying assumption was that there were different risk profiles, but their number was not known. From a collection of indicators, LCA provided evidence that there are four distinct risk profiles in the Winnipeg area.

Another application of LCA is to classify individuals. In a peer harassment study, Giang and Graham (2008) used LCA to classify over 2,000 sixth grade students into aggressor and victim latent classes. The five-class solution comprised of classes of victims, aggressors, and socially adjusted students. For instance, it revealed that there were two types of victims: highly-victimized aggressive-victims and highly-aggressive aggressive-victims.

LCA is also appropriate when we wish to identify indicators that capture classes well. High quality indicators will be strongly related to the latent variable and will lead to good class separation. This relationship of high quality indicators to the latent variable is reflected

in very high or very low conditional response probabilities. For a simulation study exploring the effects of indicator quality on LCA, see Geiser and Wurpts (2014). Therefore, one could use conditional response probabilities for each item to assess its quality with regards to how well it helps separate the latent classes. From this, a theory about the selection of indicators could be informed.

An extension of LCA is that containing covariates which can be used to predict class membership. In this approach, we not only model the latent class variable based on indicators, but we also relate the class membership to other explanatory variables (Vermunt (2017)). An example of using covariates comes from Nozadi et al. (2016) who applied LCA to identify the probability of children's membership to an anxiety class. The authors tested several covariates including children's age, sex, and accuracy scores. Age and sex were not found to be related to the children's latent class membership, hence these covariates were excluded from the analysis. Accuracy scores, however, were related to probabilities of being in anxiety and attention-anxiety classes. Therefore this covariate was kept as a valuable predictor.

When our interest is the prediction of one or more outcomes, LCA can be used to construct latent classes as categorical predictors. Lanza, Tan, and Bray (2013) demonstrated how LCA can be used to classify adolescents into depression classes, and subsequently these classes can be used to predict smoking, grades, and delinquency. The study showed that the outcomes predicted by class membership can be binary (regular smoking), continuous (grades) or count (delinquency).

These mixture models can also be useful to evaluate quality of measurement across instrument. For example, employment status was collected across register and survey data, and there is disagreement between them. You could think that register data is without error, but it has been shown that is victim of measurement error as well. In this case mixture models was used to evaluate the underlying factor of "error corrected employment status",

by using two indicators of the same question and identify random and systamtic measurement error in either indicator (Pavlopoulos & Vermunt, 2015).

In addition to these applications, LCA can be used for dimensionality reduction as the resulting groups summarize response patterns on a large number of indicators. For example, MacGregor et al. (2021) investigated symptom profiles among injured U.S. military personnel. They used fifteen dichotomous items from the Post-Deployment Health Assessment survey as LCA indicators. Combinatorics informs us that fifteen dichotomous items have 2^{15} or $32,768$ unique symptom combinations. Perhaps for this reason, MacGregor et al. (2021) incorporated LCA as a method of dimensionality reduction. A five class solution was found to have the best fit according to both statistical criteria and clinical interpretability.

Finally, LCA can be used to deal with data which violate certain assumptions. As discussed in the shoe size example, LCA can deal with violations of normality. In fact, LCA assumes the population distribution is a non-normal mixture of K normal distributions, and it can discover the value of K, i.e. generate a K-class solution.

LCA and factor analysis share the approximation of an unobserved latent variable, the difference being if that variable is continuous of categorical. We encourage researchers to be agnostic about the **true** nature of the latent variable. And focus on the approach that fits the research question.

Best Practices

Best Practices in Estimation

The best practices in estimation, as outlined in Table **??**, are rooted in existing recommendations for best practices for estimating specific subtypes of LCA, including latent class growth analysis (Van De Schoot et al., 2017) and latent class analysis with ordinal

indicators (e.g., Nylund-Gibson & Choi, 2018). These were generalized to be relevant to all types of LCA, and updated to current best practices, as explained below.

#	Item
1.	Examining Observed Data
2.	Handling Missing Data
3.	Alternative Model Specifications
4.	Software
5.	Algorithm
6.	Class Enumeration
7.	Model Fit Indices
8.	Classification Diagnostics
9.	Interpreting Class Solutions
10.	Label switching

Examining Observed Data.   Examining observed data is essential for any analysis as it may reveal patterns and violations of assumptions that had not been considered prior to data collection. Special attention should be paid to level of measurement of the indicators. Finite Gaussian mixture models (including LPA) are only suitable for continuous variables. Indicators with an ordinal level of measurement are likely to violate the assumption of within-class normal distributions of mixture models (see Vermunt, 2011). Personal experience consulting on LCA methods and moderating the `tidyLPA` Google group suggest that the misapplication of mixture models to ordinal (e.g., Likert-type) indicators is the most common source of user error. Whereas it has been argued that some parametric methods are robust when scales with 7+ indicators are treated as continuous (e.g., Norman, 2010) or with 5+ categories (Rhemtulla, Brosseau-Liard, & Savalei, 2012), this certainly does not imply that all methods are. It is certainly unlikely that such ordinal variables can be treated as a *mixture* of multiple normal distributions. The problem becomes egregious when

the number of classes estimated equals or exceeds the number of categories; in this case, each class-specific mean could describe a single response category, and a class-specific variance component would be nonsensical. In sum, Likert-type scales are rarely suitable for Gaussian mixture modeling; latent class analysis with ordinal indicators is more appropriate.

Relatedly, a recent publication claimed that an assumption of mixture models is that observed indicators are normally distributed (Spurk, Hirschi, Wang, Valero, & Kauffeld, 2020). This is incorrect. When the number of classes is greater than one, Gaussian mixture models assume that the observed indicators are a mixture of multiple (multivariate) normal distributions. In our shoe size example, it can be seen that the population distribution is comprised of two normal distributions. When examined visually, the population distribution is evidently bimodal. The Shapiro-Wilk normality test ($W = 0.971$, $p < 0.05$) rejects the null hypothesis that the sample comes from a normally distributed population. Yet, this is a prototypical example of a mixed population distribution where LCA can discover latent groups. If the population distribution were instead normal, there would be no classes to extract as the whole population would belong to a single (homogeneous) class.

Extensive descriptive statistics (including the number of unique values, variance of categorical variables, and missingness; see next subsection) can be obtained using the function `tidySEM::descriptives(data)`. Note, however, that sample-level descriptive statistics are of limited value when the goal of a study is to identify subsamples using latent class analysis. Plots (density plots for continuous variables, and bar charts for categorical ones) may be more diagnostic. Note that density plots can also aid in the choice of the number of classes, as further explained in the section on visualization. Descriptive statistics and plots can be relegated to online supplements, provided that these are readily accessible (consider using a GitHub repository as a comprehensive public research archive, as explained in Van Lissa et al., 2021).

Handling Missing Data.   Previous work has emphasized the importance of examining the pattern of missing data and reporting how missingness was handled (Van De

Schoot et al., 2017). Three types of missingness have been distinguished in the literature (Enders, 2022; Rubin, 1976): Missing completely at random (MCAR), which means that missingness is random and unrelated to any observed or unobserved variables; missing at random (MAR), which means that missingness is contingent on the *observed* data (and can thus be accounted for); and finally missing not at random (MNAR), which means that missingness is related to unobserved factors. It is possible to conduct a so-called "MCAR" test, for example the non-parametric MCAR test (Jamshidian & Jalal, 2010). But note that the name "MCAR test" is somewhat misleading, as the null-hypothesis of this test is that the data are not MAR, and a significant test statistic indicates that missingness is related to the observed data (MAR). A non-significant test statistic does not distinguish between MCAR or MNAR. As Little's classic MCAR test relies on the comparison of variances across groups with different patterns of missing data, it assumes normality (Little, 1988). This assumption is tenuous in the context of LCA. A non-parametric MCAR test, as provided by Jamshidian and Jalal, may be more suitable (Jamshidian & Jalal, 2010). Unfortunately, this test was removed from the central R-repository CRAN due to lack of maintenance. For this tutorial, I have re-implemented it in the `mice` package as `mice::mcar()`, with a fast backend in C++ and new printing and plotting methods.

While we concur that investigating missingness is due diligence, it is important to emphasize that missingness is adequately handled by default in many software packages for LCA, such as Mplus, Latet GOLD, and `OpenMx` which is the backend of `tidySEM`. These packages use Full Information Maximum Likelihood (FIML) estimation, which makes use of all available information without imputing missing values. FIML is a best-practice solution for handling missing data; on par with multiple imputation when the estimation model includes the same variables as the imputation model (Lee & Shi, 2021). FIML estimation assumes that missingness is either MCAR or MAR. Thus, one would typically proceed with FIML, regardless of the outcome of an MCAR test. Although FIML does not, by default, handle missingness in exogenous variables – all indicator variables in LCA are endogenous,

so this is not a concern.

Multiple imputation is less suitable to LCA for two reasons. First, because LCA methods are often computationally expensive, and conducting them on multiple imputed datasets may be unfeasible. Second, because there is no straightforward way to integrate LCA results across multiple datasets. To conclude; our recommendation is to inspect missingness (e.g., using `mice::MCAR()`) and report the proportion of missingness per variable (e.g., using `tidySEM::descriptives()`), before proceeding with FIML. One minor concern is that the K-means algorithm, which `tidySEM` uses for determining starting values, is *not* robust to missing values. When it fails, `tidySEM` automatically switches to hierarchical clustering, unless the user specifies a different clustering algorithm or uses manual starting values.

Alternative Model Specifications. In order to aid researchers working with latent trajectory models, Van De Schoot et al. (2017) developed a protocol called Guidelines for Reporting on Latent Trajectory Studies (GRoLTS). Two of the GRoLTS guidelines (namely, 6a and 6b) refer to considering alternative model specifications. Both are discussing specific cases in latent trajectory model specification. The first is about whether the variance of the growth parameter is estimated freely or fixed, and the second is about whether conditional independence is assumed, as the researcher might also want to free-up the variance-covariance structure. In LCA, there are also many different ways to specify the model. Means, variances, and covariances between the indicators can either be constrained across classes, or estimated freely. Researchers using LCA should transparently report their chosen parametrization as well as discuss different parametrizations that were tested in the process.

Different types of latent class models have different parameters. For example, mixture models and latent profile analyses typically have class-specific means, variances, and covariances. Latent growth analyses have the same parameters, but with respect to the latent growth variables. Latent class analyses with ordinal indicators have thresholds. All of these parameters can be freely estimated, constrained to be equal across classes, or fixed to a

certain value (e.g., to zero). The total number of parameters thus scales with the number of estimated classes. Consequently, LCA methods have a potentially very high number of parameters. As any of these parameters could be misspecified, it is important to consider alternative model specifications. However, alternative model specifications may be approached differently depending on whether an analysis is data driven (exploratory), or theory driven (confirmatory). This distinction has remained underemphasized in prior writing.

Prior literature on LCA has emphasized its exploratory applications (Nylund, Asparouhov, & Muthén, 2007). In exploratory LCA, a large number of models are typically estimated in batch, with varying numbers of classes and model specifications. The "correct" model specification is then determined based on a combination of fit indices, significance tests, and interpretability. For latent profile analysis, the function `tidySEM::mx_profiles(classes, variances, covariances)` largely automates this process. The argument `classes` indicates which class solutions should be estimated (e.g., 1 through 6). The argument `variances` specifies whether variances should be `"equal"` or `"varying"` across classes. The argument `covariances` specifies whether covariances should be constrained to `"zero"`, `"equal"` or `"varying"` across classes. The means are free to vary across classes by default, although the more general function `tidySEM::mx_mixture()` could be used to circumvent this. After all models have been estimated, the function `tidySEM::table_fit()` can be used to obtain a model fit table suitable for determining the optimal model according to best practices. Note, however, that this table does not include the bootstrapped likelihood ratio test (BLRT) by default, because this test is very computationally expensive. It is recommended to use the function `tidySEM::BLRT()` to compare a shortlist of likely candidate models based on other fit indices. More on fit indices can be found in the Model Fit Indices subsection of this paper.

Confirmatory LCA typically requires less comprehensive alternative model specifications. For example, in the context of a preregistered analysis, the main models of

interest would have been specified a priori. Even in this case, the theoretical model could be compared to a few others to contextualize it.

Software. Many software packages are available for the estimation of LCA models. Some of these packages have limited functionality, or implement specific innovations. Other packages implement LCA in the context of a more flexible structural equation modeling framework. The most notable examples of the latter are the commercial programs Mplus and Latent GOLD, and the free open source R-package OpenMx. The commercial packages stand out because they offer relatively user-friendly interfaces and implement sensible defaults for complex analyses, including LCA methods. This lowers the threshold for applied researchers to adopt such methods. Commercial software also has several downsides, however. One such downside is that use of the software is restricted to those individuals and institutions who can afford a license. Another downside is that the source code, being proprietary, cannot be audited, debugged, or enhanced by third parties. This incurs the risk that mistakes in the source code may go unnoticed, and curbs progress as software developers cannot add new functionality.

Conversely, the free open source program OpenMx (Neale et al., 2016) is very flexible, but not very user-friendly. We directly address this limitation using the `tidySEM` R-package. New functionality in `tidySEM` seeks to lower the threshold for latent class analysis using `OpenMx`. It adheres to best practices in estimation and reporting, as described in this paper. The user interface is simple, making use of the model syntax of the widely used `lavaan` R-package (Rosseel, 2012). This syntax offers a human-readable way to specify latent variable models. Minor enhancements are made to simplify the specification of LCA.

Because of the limitations of the aforementioned tools, we set out to develop a free tool that provides sensible defaults and is easy to use, but provides the option to access and modify all of the model inputs (i.e., low barrier, high ceiling). `tidySEM` interfaces with existing tools, and is able to translate between what existing tools are capable of and what researchers and analysts carrying-out person-oriented analyses would like to specify.

Furthermore,`tidySEM` facilitates fully-reproducible analyses and contributes to open science.

Algorithm. LCA parameters and model fit statistics can be estimated in a variety of ways. The choice of the estimator depends on the presence of missing values, sample size, number of indicators, and available computational resources (Weller, Bowen, & Faubert, 2020). A commonly used technique is maximum likelihood (ML) estimation with the expectation-maximization (EM) algorithm as a local optimizer. Imagine we are estimating two parameters, e.g. the class-specific means μ_c on a continuous indicator (ignoring the variance for now). The EM algorithm will attempt to find a combination of values for these two parameters that maximizes the likelihood (LL) of all observed data. In practice, instead of maximizing LL, often $-2 * LL$ is minimized, as this offers computational advantages. We can think of this optimization problem as a three-dimensional landscape: The X and Y dimensions are determined by the class-specific means, so $X = \mu_1$ and $Y = \mu_2$ - and the Z-dimension is determined by $Z = -2 * LL$. The optimizer must find the deepest "valley" in this landscape, which reflects the combination of μ_1 and μ_2 that maximizes the likelihood of the data. The EM optimizer behaves somewhat like a marble dropped in this landscape. It is dropped at some random point in space, and will roll into the nearest valley. The problem is that, once EM rolls into a valley, it will settle on the bottom of that valley (this is known as "convergence"). It cannot climb out again. Thus, if their are multiple valleys, the risk is that the optimizer gets stuck in a shallower valley (a "local optimum"), and never discovers the deepest valley (the "global optimum", or best solution). One solution to this problem is to drop many marbles at random places, compare their final $-2 * LL$ values, choose the solution with the lowest $-2 * LL$, and make sure that several marbles replicated this solution. This is the "random starts" approach.

One problem with the random starts approach is that it is computationally expensive to run this many replications. Moreover, because the algorithm begins with random starting values, many of the marbles are likely to be very far away from a "good enough" solution. Two innovations may improve the estimation procedure. The first is that, instead of picking

random starting values, a "reasonable solution" may be used for the starting values. For example, if we assume that the different classes are likely to have different mean values on the indicators, then the K-means clustering algorithm can be used to determine these cluster centroids. We can compute the expected values of all model parameters by treating the K-means solution as a known class solution, and use these as starting values for a mixture model. One remaining concern is that this approach may result in starting values close to a local optimum, and that the EM algorithm will thus never find the global optimum. A second innovation addresses this concern. Instead of using EM, it is possible to use an optimizer that can climb out of a valley. Simulated annealing iteratively considers some "destination" in the landscape, and compares its likelihood to the current one. If the destination likelihood is higher, the estimator moves there. If the destination likelihood is *lower*, the estimator still moves there occasionally, based on probability. This latter property allows it to escape local optima, and find the global optimum.

By default, `tidySEM` derives starting values using K-means clustering, and identifies the global optimum solution using simulated annealing. Once a solution has been found, simulated annealing is followed up with a short run of the EM algorithm, as EM inherently produces an asymptotic covariance matrix for the parameters that can be used to compute standard errors. Note that these defaults can be manually overridden.

A recent paper suggested maximum likelihood with robust standard errors should be used when the observed indicators are not normally distributed (Spurk et al., 2020). This statement is incorrect, and may lead readers to believe that they must use commercial software, as robust maximum likelihood is currently only implemented in Mplus and LatentGOLD. As explained before, mixture modeling assumes that observed data are a mixture of (multivariate) normal distributions; thus, the observed indicators will likely not be normally distributed.

Class Enumeration.   As explained, LCA can be done in an exploratory or in a confirmatory fashion. In exploratory LCA, a sequence of models is fitted to the data with

each additional model estimating one more class than the previous model. These models are then compared and the best solution is selected as the final class solution. In some cases, prior theory can inform the researcher about the number of classes to expect. Even in such confirmatory LCA cases, it is nonetheless useful to know if the theoretical model is markedly better than those with differing numbers of classes. Therefore, it may always be useful to compare different class solutions.

From a sequence of models, the final class solution is chosen based on both theoretical and statistical criteria. Theory should drive the selection of indicator variables, inform the expectations and reflect on the findings. In addition to this, there are several statistical criteria to consider in model selection. These include but are not limited to likelihood ratio tests, information criteria, and the Bayes factor (Masyn, 2013; Weller et al., 2020).

Relative model fit can be examined using the likelihood ratio test. This is only appropriate when the two models we wish to compare are nested. The likelihood ratio test statistic is computed as the difference in maximum log-likelihoods of the two models, with the test degrees of freedom being the difference in the degrees of freedom of the two compared models. The test statistic follows the χ^2 distribution, and we want it to be non-significant in order to give support to the simpler model. The likelihood ratio test can only compare two nested models at a time (Lanza, Bray, & Collins, 2003).

Model Fit Indices. Fit indices typically used for determining the optimal number of classes include the Akaike Information Criterion (AIC) and the Bayesian Information Criterion (BIC). Both information criteria are based on the -2*log-likelihood (which is lower for better fitting models), and add a penalty for the number of parameters (thus incentivizing simpler models). This helps balance model fit and model complexity. The lower the value of an information criterion, the better the overall fit of the model.

The general objective of the Information Criteria (IC) is to evaluate the model's out-of-sample predictive accuracy, so adjusting for over fitting. Fit measures like R^2 evaluate

the in-sample predictive accuracy, meaning that they evaluate the models ability to predict the observed outcomes based on the same data that was use to build up the model. These metrics are positively bias, meaning that will present better model fit than it has in reality. While IC corrects for this positive bias by evaluating the models accuracy approximating the out-of-sample predictive accuracy, meaning that it is the ability to predict the outcome for observations that are not part of the training model. Ideally we would estimate the model a lot of time with less observations and predict their scores, but IC's approximate this by their different penalty metrics. For example R^2 will increase even if an added predictors are unnecessary, while IC's will show worst fit when a predictor (complexity) is unnecessary (McElreath, 2020)

The BIC applies a stronger penalty for model complexity that scales logarithmically with the sample size. The literature suggests the BIC may be the most appropriate information criterion to use for model comparison (Masyn, 2013; Nylund-Gibson & Choi, 2018). Both the AIC and the BIC are available in the `tidySEM` output.

Information criteria may occasionally contradict each other, so it is important to identify a suitable strategy to reconcile them. One option is to select a specific fit index before analyzing the data. Another option is to always prefer the most parsimonious model that has best fit according to any of the available fit indices. Yet another option is to incorporate information from multiple fit indices using the analytic hierarchy process (Akogul & Erisoglu, 2016). Finally, one might make an elbow plot and compare multiple information criteria (Nylund-Gibson & Choi, 2018).

Another common test of model fit is the likelihood ratio χ^2 goodness-of-fit test. However, this test is not implemented in `tidySEM`.

A disadvantage of the IC's is that we do not have standard errors for them, so we only have the absolute values without a measure of their variability. So, the difference between models IC can be very small. Still indicating that the model with the lower value is "better",

but if this difference is very small can considered them "functionally equal", and you should take into consideration the interpretability of the model.

LCA studies commonly report -2*log likelihood of the final class solution. This is a basic fit measure used to compute most information criteria. However, since log likelihood is not penalized for model complexity, it will continuously fall with the addition of more classes.

An alternative is using the bootstrapped likelihood ratio test which can be run using `tidySEM::BLRT()`. Currently, this test is computationally expensive and can be slow on most computers. A faster version of this test, namely an implementation of *the lazy bootstrap* (Kollenburg, Mulder, & Vermunt, 2018) to `tidySEM` is being developed.

Classification Diagnostics.   Best models will divide the sample into subgroups which are internally homogeneous and externally distinct. Classification diagnostics give us a way to assess the degree to which this is the case. They are separate from model fit indices as a model can fit the data well but show poor latent class separation (Masyn, 2013). Classification diagnostics should not be used for model selection, but they can be used to disqualify certain solutions because they are uninterpretable. Interpretability should always be a consideration when considering different class solutions (Nylund-Gibson & Choi, 2018).

Three important classification diagnostics provided by `tidySEM` are: (1) the *minimum* and *maximum* percentage of the sample assigned to a particular *class*, (2) the *range of the posterior class probabilities* by most likely class membership, and (3) *entropy.* All three are based on posterior class probabilities.

The posterior class probability is a measure of classification uncertainty which can be computed for each individual, or averaged for each latent class. When the posterior class probability is computed for each individual in the dataset, it represents each person's probability of belonging to each latent class. For each person, the highest posterior class probability is then determined and the individual is assigned to the corresponding class. We want each individual's posterior class probabilities to be high for one and low for the

remaining latent classes. This is considered a high classification accuracy and means that the classes are distinct. To obtain posterior class probabilities, run `tidySEM::class_prob()`. This function produces output comprised of several elements:

`$sum.posterior` is a summary table of the posterior class probabilities indicating what proportion of the data contributes to each class.

`$sum.mostlikely` is a summary table of the most likely class membership based on the highest posterior class probability. From this table, we compute the minimum and maximum percentage of the sample assigned to a particular class, , i.e. **n_min** (the smallest class proportion based on the posterior class probabilities) and **n_max** (the largest class proportion based on the posterior class probabilities). We are especially interested in **n_min** as if it is very small and comprised of few observations, the model for that group might not be locally identified. It may be impossible to calculate descriptive statistics for such a small class. Estimating LCA parameters on small subsamples might lead to bias in the results. Therefore, we advise caution when dealing with small classes.

`$mostlikely.class` is a table with rows representing the class the person was assigned to, and the columns indicating the average posterior probability. The diagonal represents the probability that observations in each class will be correctly classified. If any of the values on the diagonal of this table is low, we might consider not to interpret that solution. In `tidySEM` we use the diagonal to compute the range of the posterior class probabilities by most likely class membership which consists of the lowest class posterior probability (**prob_min**), and the highest posterior probability (**prob_max**). Both **prob_min** and **prob_max** can be used to disqualify certain class solutions, and are a convenient way to summarize class separation in LCA. We want both **prob_min** and **prob_max** to be high as that means that for all classes the people who were assigned to that class have a high probability of being there. **prob_min** is especially important as it can diagnose if there is a class with low posterior probabilities which could make one reconsider that class solution.

`$avg.mostlikely` contains the average posterior probabilities for each class, for the subset of observations with most likely class of 1:k, where k is the number of classes.

`$individual` is the individual posterior probability matrix, with dimensions n (number of cases in the data) x k (number of classes). Additionally it includes the `predicted` class in function of the highest predicted probability. Individual class probabilities and/or predicted class are often useful for researchers who wish to do follow up analyses.

Entropy is a summary measure of posterior class probabilities across classes and individuals. It ranges from 0 (model classification no better than random chance) to 1 (perfect classification). As a rule of thumb, values above .80 are deemed acceptable and those approaching 1 are considered ideal. An appropriate use of entropy is that it can disqualify certain solutions if class separability is too low. Entropy was not built for nor should it be used for model selection during class enumeration (Masyn, 2013).

n_min, **n_max**, **prob_min**, **prob_max**, and **entropy** and can be obtained using `tidySEM::table_fit()`.

Interpreting Class Solutions.   An important outcome of LCA are conditional item probabilities, also known as class-specific item probabilities (Masyn, 2013), conditional response, or conditional solution probabilities (Geiser, 2012). They indicate the probability of an item being endorsed given that the observation belongs to a particular latent class. Conditional item probabilities can be obtained using `tidySEM::table_prob()`. If a particular item is endorsed by two or more classes at markedly different rates, it is said to discriminate well between the classes and is consequently considered a good indicator. Classes are considered highly homogeneous with respect to an item when for a particular item there is a distinct difference in conditional item probabilities for two or more classes. For instance, if an item is endorsed below 30% for one class and above 70% for another class, the classes have high homogeneity with respect to this item (Masyn, 2013). Conditional item probabilities are the analogue of mean and standard deviation when the indicators are binary

or ordinal.

A problem which can occur is that of inadmissible solutions. With binary indicators, LCA is modelling a cross-table with all the predictors. The problem with such cross-tables is that they will often contain empty cells, i.e. combinations of responses that never occur together. This problem is reflected by extreme conditional item probabilities (as in exactly 0 or 1). Such boundary parameter estimates could indicate that the solution is invalid (Geiser, 2012). Boundary parameter estimates can also happen with continuous indicators. For instance, if we have a zero-inflated normal distribution and a two class solution, one class might have the mean of zero and its standard deviation cannot be determined since there is little variance. This too could be a sign of an invalid solution, warn that too many classes were extracted, or indicate a local optimum (Geiser, 2012).

Label Switching.   The final class solution will usually discover and enumerate several classes. The class ordering, however, is completely arbitrary. The class labeled as Class 1 in one solution may become Class 2 or Class 3 in another model, even when the only difference between the models is in their starting values. Label switching is something to be mindful of when comparing different LCA models (Masyn, 2013).

The order of clusters is nondeterministic when using K-means in `tidySEM`. Therefore label switching is still a consideration. A simple solution to this is setting a random seed number one line prior to fitting the model. We advise `tidySEM` users to always do so in order to circumvent label switching.

Class names should be chosen to accurately reflect group membership, as theoretically relevant names according to the interpretation of the class solutions. Overly simplified and generalized class names may prove misleading to both audiences and researches alike leading to what is known as a naming fallacy (Weller et al., 2020).

Best Practices in Reporting

Among studies using LCA, reporting practices vary significantly (Weller et al., 2020). Various authors have tried to improve and standardize ways of reporting LCA (e.g. Masyn, 2013; Weller et al., 2020), but more work is needed. Van Lissa et al. (2020) developed WORCS, a workflow for open reproducible code in science. WORCS consists of step-by-step guidelines for research projects based on the TOP-guidelines developed by Nosek et al. (2015). WORCS workflow can be easily implemented in R in form of an R package which facilitates preregistration, article drafting, version control, citation and formatting, among others (Van Lissa et al., 2020).

TOP-guidelines emphasize the use of comprehensive citation (including referencing the software used in the analysis), as well as code and data sharing wherever possible (Nosek et al., 2015). Van Lissa et al. (2020) suggest sharing synthetic data in case the original data cannot be shared, and provide functions to generate such synthetic data. Ideally, the entire research project is made reproducible so that others may download it and reproduce it with just one click; for guidance, see Van Lissa et al. (2020).

As the open science movement is gaining momentum, researchers are becoming increasingly aware how important it is that analyses can be reproduced and audited. In line with open science principles, one of the suggested reporting standards relates to reproducible code. In this context, it is important to note that user-friendly methods for estimating LCA models have predominantly been available in commercial software packages (e.g., *Mplus* and *Latent GOLD*). A potential downside of commercial software is that it restricts the ability to reproduce analyses to license holders, and prevents auditing research because the underlying source code is proprietary. To overcome these limitations, the present paper introduces new user-friendly functions in the `tidySEM` R-package that can be used to estimate a wide range of LCA models using the free, open-source R-package `OpenMx` as the backend. The reporting guidelines described in this paper are adopted in `tidySEM` by default. The `tidySEM`

R-package thus makes advanced mixture modeling based on best practices widely accessible, and facilitates the adoption of the estimation and reporting guidelines described in this paper.

Visualization. Plots can greatly improve the interpretability of LCA models. There are several stages where this is an important consideration.

First, in class enumeration, we want to compare several competing class solutions. This can be done by means of the AIC and BIC. Here, we suggest using an elbow plot with the $K - class\ solution$ on the X-axis, and information criteria value on the Y-axis. We show an implementation of such an elbow plot in our Tutorial subsection.

Second, once we have decided on the final class solution, we want to interpret the response patterns on the indicators for each latent class. While `tidySEM` can create a table showing the probability of each item's response endorsement (using `tidySEM::table_prob`), it may be easier to inspect these probabilities visually. For this reason, we created `ggplot2::plot_prob()`. The resulting shows response patterns on all indicators for each group. We give an example of this plot in the Tutorial subsection.

Tutorial

This is an example of an exploratory LCA using `tidySEM`.

Loading the Dataset

In this example, we use *data_mix_ordinal*, a simulated data for mixture modelling with ordinal indicators. This dataset is built-in to `tidySEM`. For more information about the dataset, type `?tidySEM::data_mix_ordinal` into the R console after loading the `tidySEM` using library().

We load the dataset and convert the indicators into ordered factors.

Exploring the Data

An important step to preceding any statistical analysis is data exploration. Here we use `tidySEM::descriptives()` to describe the dataset we are using.

As we can see, the output includes various descriptives of our dataset. Special attention should be paid to examining the pattern of missingness, as discussed in the *Handling missing data* section of this paper. In our example, we see that there are no missing values, hence we proceed with our analysis.

Conducting Latent Class Analysis

Before we fit a series of LCA models, we set a random seed using `set.seed()`. The seed number can be any digit. This is an important step as there is some inherent randomness in the LCA computations, and having the same seed number ensures that two separate researcher obtain exactly the same results when fitting LCA models.

Finally, we reach the step of fitting LCA models. To do so, we use `tidySEM::mx_lca()` which takes data and number of classes as inputs. Notice that the analysis will be done on all the variable in the data set, so you have to make sure it only includes the relevant variables. In our example, we want to fit 1 to 4 class solutions and compare their output. Depending on your computer's computational power, this might take a while.

Notice that the model was run 10 times for each K class solution. This because the functions runs a total of 10 **extra** times the model. This way we can choose the best fitting model across all the solutions. In this examples we see that all models converged without issues.

As `tidySEM::mx_lca()` was run for several models at the same time, the resulting object `res` is a `mixture_list` class where each K class solution is an object in the list, and each of them are `OpenMx` models (`MxModel`).

Class Enumeration

In class enumeration, we want to compare a sequence of LCA models fitted to the data. To aid the process, we create a model fit table using `tidySEM::table_fit()` with the results object as the input. As the output contains a lot of information on each of the four fitted models, we select a subset of helpful model fit indices and classification diagnostics.

Our selection of fit indices and classification diagnostics includes:

Table 2

Selection of Fit Indices and Classification Diagnostics

Selection	Description
Name	the K-class solution
LL	the -2*log-likelihood of each model
Parameters	Number of estimated parameters in each model
AIC	the Akaike Information Criterion value
BIC	the Bayesian Information Criterion value
prob_min	the lowest posterior class probability by most likely class membership
prob_max	the highest posterior class probability by most likely class membership
n_min	the lowest class proportion based on the posterior class probabilities
n_max	the highest class proportion based on the posterior class probabilities

We discussed several possible strategies to select the final class solution. Here, we apply our own.

To aid our interpretation of the results, we create an elbow plot showing the trends in information criteria across four models.

From the elbow plot, we see that AIC has a lower penalty for model complexity. However, we are more interested in the BIC values, which are similar for the one, two and

three-class solutions, but the four-class solution fits significantly worse. For this reason, we eliminate the four-class solution from the selection process.

Then we examine the model fit table. As expected, the -2*log likelihood falls successively with each added class. As previously stated, classification diagnostics should not be used for model selection, but they can be used to disqualify certain solutions because they are uninterpretable. We see that prob_min and n_min for the four-class solution is low, knowing that this solution also has a high BIC, we disqualify this solution.

Out of the remaining three solutions, we notice that entropy is the highest for the three-class solution, and it has a satisfactory prob_min and n_min. Based on this, we retain the three class solution in model selection. Note that entropy for the one-class solution will always equal to one, as it is 100% true that every case is in that class. Based on the low entropy of the two-class solution, we eliminate this model.

Finally, when comparing the one and three-class solutions, we inspect the information criteria. For BIC, the one-class solution fits better, but the difference is marginal. AIC tells us that the added complexity of having three classes still explains the data better than a one-class solution. Therefore, we select the three-class solution as our final-class solution.

Interpreting the Final Class Solution

To aid our understanding of the final class solution, we use `ggplot2::plot_prob()` with the results of the three-class model as the input. The resulting graph shows response patterns on all the indicators for each group.

If we want to know the probability of each response option's endorsement for each class, we can use `tidySEM::table_prob`. These are thresholds for ordinal dependent variables in the probability scale.

In the plot, we can see the distributions of the response probabilities on the indicators for each of the three classes. For instance, we see that in Class 1 the most common response

to u2 is 2, while in Class 2 and Class 3 this is 0. We can also see that response 1 is a rare response not forming the majority in any class. Class 2 distinguishes itself because the majority scores the response 0 category of u3 and u4, while in Class 1 and 2 this is not the case. Class 3 distinguishes itself because the most common response to u3 and u4 is 3.

We can also interpret the response patterns numerically. It is a matter of preferences on how to interpret these probabilities. Here is where you would **name** each class, such that each response pattern is theoretically meaningful.

Extracting Posterior Class Probabilities

Another step is to extract posterior class probabilities. This is done by the use of `tidySEM::class_prob` with the results of the final class solution as the input.

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