

# Rotation Homework Problems:

## p. 158: #39, 41, 44, 47, 53

Problems taken from the school's old textbook:

Giancoli, D. (1980). *Physics*, 2<sup>nd</sup> Ed. Englewood Cliffs, NJ: Prentice Hall.

---

39. A centrifuge rotor has a moment of inertia of  $4.00 \times 10^{-2} \text{ kg} \cdot \text{m}^2$ . How much energy is required to bring it from rest to 10,000 rpm?
41. When an object has symmetry, its moment of inertia often can be expressed as a simple formula. For instance, the moment of inertia for a hoop rotated about its center is  $mr^2$ . For a uniform disk rotating about its center, the moment of inertia is  $1/2mr^2$ . A uniform sphere rotated about its center is  $2/5mr^2$ . However as you know, most objects do not enjoy the benefit of symmetry. As a result, if we can even come up with a formula for their moments of inertia, the formulas might not be all that simple. Often, the moments of inertia for these objects are determined experimentally by applying a known torque to the object, measuring the angular acceleration it experiences, and calculating its moment of inertia using  $\Sigma \tau = I\alpha$ . If this calculated moment of inertia is set equal to  $mr^2$  (the basic formula for the simplest of objects – a point mass), the  $r$  that satisfies this equation is called the object's *radius of gyration*. With all of that explanation behind us now, we are finally ready for this problem. A merry-go-round has a mass of 1560 kg and a *radius of gyration* of 18.5 m. How much work is required to accelerate it from rest to a rotation rate of one revolution in 7.10 seconds? (Hint: Think about CLEE and how a change in KE relates to work).
44. A hollow cylinder (hoop) is rolling on a horizontal surface at a speed of 3.4 m/s when it reaches a  $20^\circ$  incline.
- How far up the surface of the incline will it go?
  - How long will it be on the incline before it arrives back at the bottom?
47. What is the angular momentum of a 200-g ball rotating on the end of a string in a circle of radius 1.00 m at an angular speed of 9.45 rad/s?
53. A 4.5-m-diameter merry-go-round is rotating freely with an angular velocity of 0.70 rad/s; its total moment of inertia is  $1750 \text{ kg} \cdot \text{m}^2$ .
- Four people standing on the ground, each of 65-kg mass, suddenly step onto the edge of the merry-go-round. What will be the angular velocity of the merry-go-round now?
  - What will be the angular velocity of the merry-go-round if the people were on it initially, and then jump off?

### ANSWERS:

39.  $2.19 \times 10^4 \text{ J}$   
41.  $2.09 \times 10^5 \text{ J}$   
44a. 3.45 m  
44b. 4.06 seconds  
47.  $1.89 \text{ (kg} \cdot \text{m}^2\text{)/s}$   
53a. 0.400 rad/sec  
53b. The angular velocity of the merry-go-round DOES NOT CHANGE when the passengers jump off. See the solutions book in the classroom for an expanded explanation.