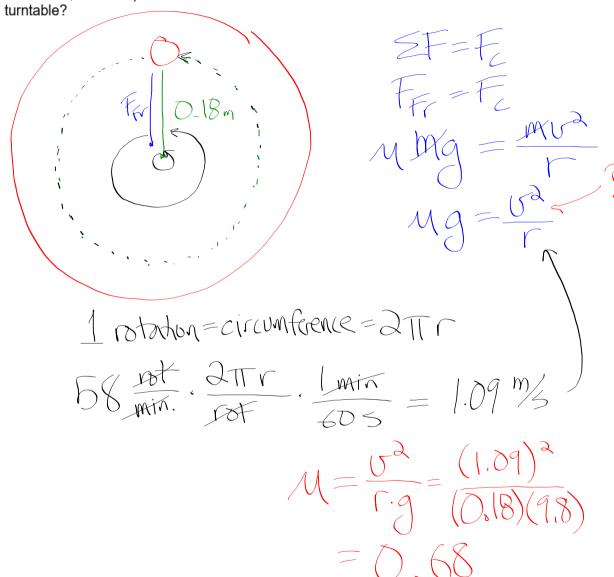
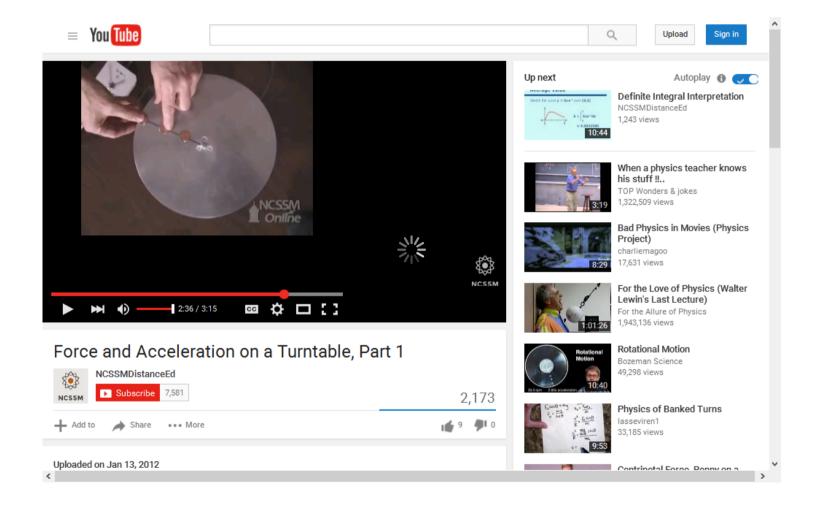
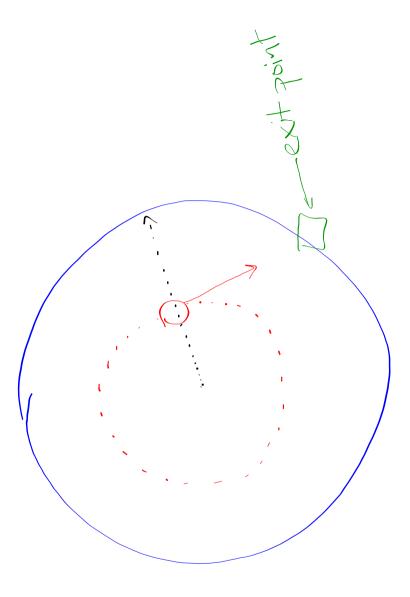
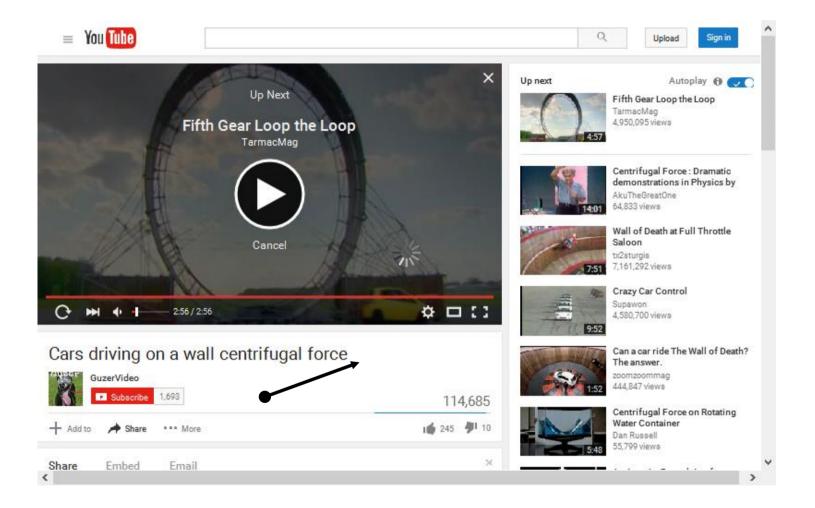
9. A coin is placed 18.0 cm from the axis of a rotating turntable of variable speed. When the speed of the turntable is slowly increased, the coin remains fixed on the turntable until a rate of 58 rpm (rotations-per-minute) is reached, at which point the coin slides off. What is the coefficient of static friction between the coin and the









#### **Uniform Circular Motion**

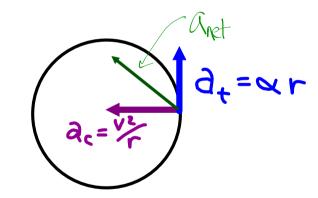
- Speed is constant
- The centripetal acceleration is the only acceleration
- a<sub>c</sub> is directed radially inward

Now for the case when circular motion is uniformly **accelerated**:

- Speed is changing
- There are two separate lineal accelerations

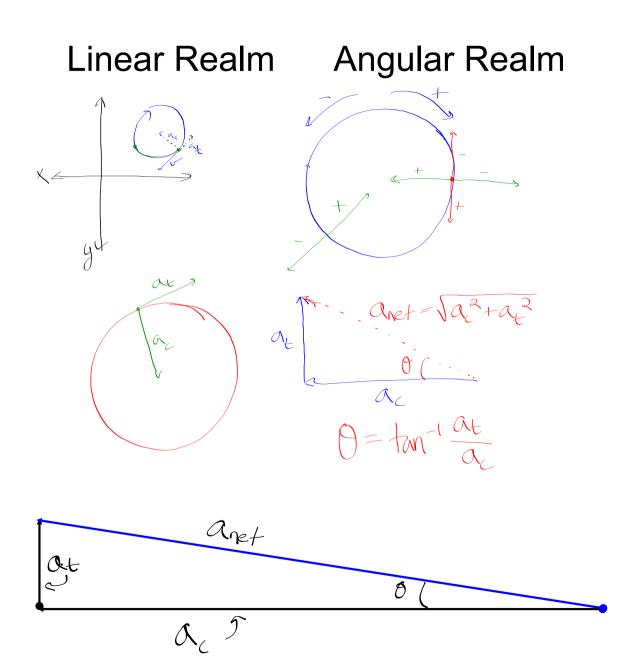
### **CENTRIPETAL ACCELERATION**(a<sub>c</sub>)

- Directed inward
- a<sub>c</sub> = v<sup>2</sup>/r
   Responsible for changing the direction



## TANGENTIAL ACCELERATION(a,)

- Directed in the direction of instantaneous travel
- a₁ = 
   ✓
- Responsible for increasing / decreasing the angular velocity



# Linear Quantities vs. Angular Quantities

Linear Displacement (meters)	Angular Displacement (radians)  (He ta)
Linear Velocity (m/sec)	Angular Velocity (radians/sec)
Linear Acceleration (m/s²)	Angular Acceleration (radians/s²)
a	$\sim$ $(alpha)$

When **linear** acceleration is constant:

$$X = X_0 + V_0 t + \frac{1}{2}at^2$$

$$V = V_0 + at$$

$$V = V_0^2 + 2a(x - X_0)$$

When angular acceleration is constant:

$$\Theta = \Theta_0 + \omega_0 t + 2 \propto t^2$$

$$\omega = \omega_0 + \alpha t \quad (\text{mdians})$$

$$\omega^2 = \omega_0^2 + 2 \times (\Theta - \Theta_0)$$

#### **Relating Linear Quantities to Angular Quantities**



If an object is rotating for a given amount of time ( $_{\delta}$ +), an angular displacement ( $_{\delta}$ +) and linear dislacement ( $_{\delta}$ 5) are realized.

$$\Delta \Theta = \frac{\Delta S}{r}$$

$$\frac{\Delta \Theta}{\Delta E} = \frac{\Delta S}{\Delta E(r)} \quad \text{(DIVIDE BOTH Sides BY } \Delta t \text{)}$$

$$W = \frac{V}{r}$$

If an object is also experiencing an angular acceleration (speeding up or slowing down) over some time period ( $_{\alpha}$ +), there will be changes in the angular speed ( $_{\alpha}\omega$ ) and the linear speed ( $_{\Delta}v$ -).

$$\Delta W = \frac{\Delta V}{r}$$

$$\frac{\Delta W}{\Delta t} = \frac{\Delta V}{\Delta t(r)}$$
 (Dividing Both Sides By  $\Delta t$ )

EXAMPLE 1: A typical compact disc records data starting at a radius of 25.0 mm and ending at a radius of 58.0 mm from its center. All disc players read information from the disc at a rate of 4500 mm/min.

- a) What is the initial angular velocity (in RPM) of the disc when it starts reading data?
- b) What is the angular velocity (in RPM) of the disc when it finishes reading data at the outside radius?
- c) If the CD plays continuously from the beginning to end, what is the angular acceleration (in rot/min²) assuming a play time of 75.0 minutes?
- d) What are a<sub>t</sub> and a<sub>c</sub> (in m/s<sup>2</sup>) at a point when the data is being read at a radius of 50.0 mm?

EXAMPLE 2: Nannosquilla decemspinosa is a small, legless crustacean living on the west coast of Panama. When stranded on the beach by high tide, it moves back to the water by doing sommersaults. If nannosquilla has a body length of 3.0 cm, takes this body length and curls it up as a wheel (having this circumference), rotates as a wheel at 70.0 RPM, and if it must travel 4.0 meters to return to the water, how long does it take it to get back into the water?

EXAMPLE 3: A wheel with a diameter of 19.0 centimeters starts from rest and reaches a speed of 40.0 RPM after rotating through 46 radians.

- a) Determine the wheel's constant angular acceleration.
- b) How long did the above process take?