

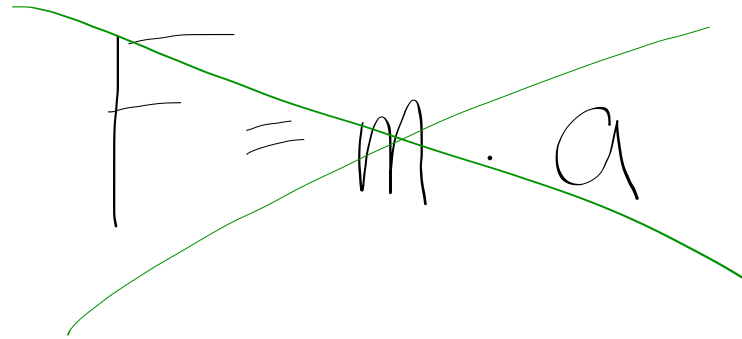
constant speed

$$\Sigma F = 0 \text{ (static)}$$

acceleration

$$\Sigma F \neq 0 \text{ (dynamic)}$$

What is the Mathematical Relationship between Force, Mass, and Acceleration?



A handwritten equation $F = m \cdot a$ is shown, crossed out with a large green 'X'. The 'F' is written with a vertical line and two horizontal bars. The '=' is written with two horizontal bars. The 'm' is written in a cursive style. The 'a' is written in a cursive style. The green 'X' is drawn with two intersecting lines.

For the textbook:

- $F = 100 \text{ N}$
- $m = 10 \text{ kg}$

$$F = ma; \quad a = F/m$$
$$a = \frac{100}{10} = 10 \text{ m/s}^2$$

$$8.04 \text{ m/s}^2?$$

For the dog:

- $F = 250 \text{ N}$
- $m = 25 \text{ kg}$

$$F = ma; \quad a = F/m$$
$$a = \frac{250}{25} = 10 \text{ m/s}^2$$

$$\sim 5 \text{ m/s}^2?$$

$$\sum \mathbf{F} = m \times a$$

$\sum \mathbf{F}$
sum of
all forces
(includes
direction)

m
mass of
an object
(or a combined
mass)

a
resulting
acceleration
(in direction
of overall force)

Dynamics (Newton's 2nd Law)

Objectives:

- Students will understand the mathematics and concepts behind Newton's 2nd Law
- Students will be able to use Newton's 2nd Law to solve problems
- Students will know what friction is, understand the difference between kinetic and static friction, and be able to use friction to solve problems

Steps For Solving Dynamics Problems:

1. Draw a picture / establish a reference frame.
2. Identify variables / check units.
3. Draw a FBD.
4. Resolve all forces into X and Y components.
5. $\sum F_x = ma_x$
6. $\sum F_y = ma_y$
7. Solve for unknowns.

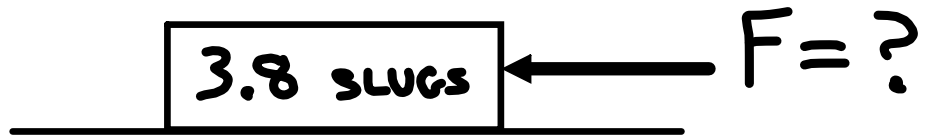
Note: A static situation (zero or constant velocity) is described by Newton's 2nd Law, just like a dynamic situation:

$$\begin{aligned}\sum F &= ma \\ (a = 0 \text{ for statics...}) \\ \sum F &= m(0) = 0\end{aligned}$$

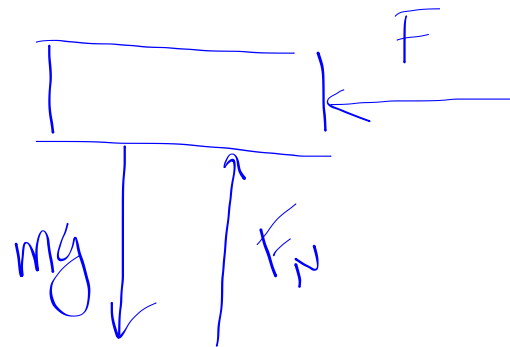
So really all we need to remember is $\boxed{\sum F = ma!}$

EXAMPLE 1:

← 5.9 ft/sec²

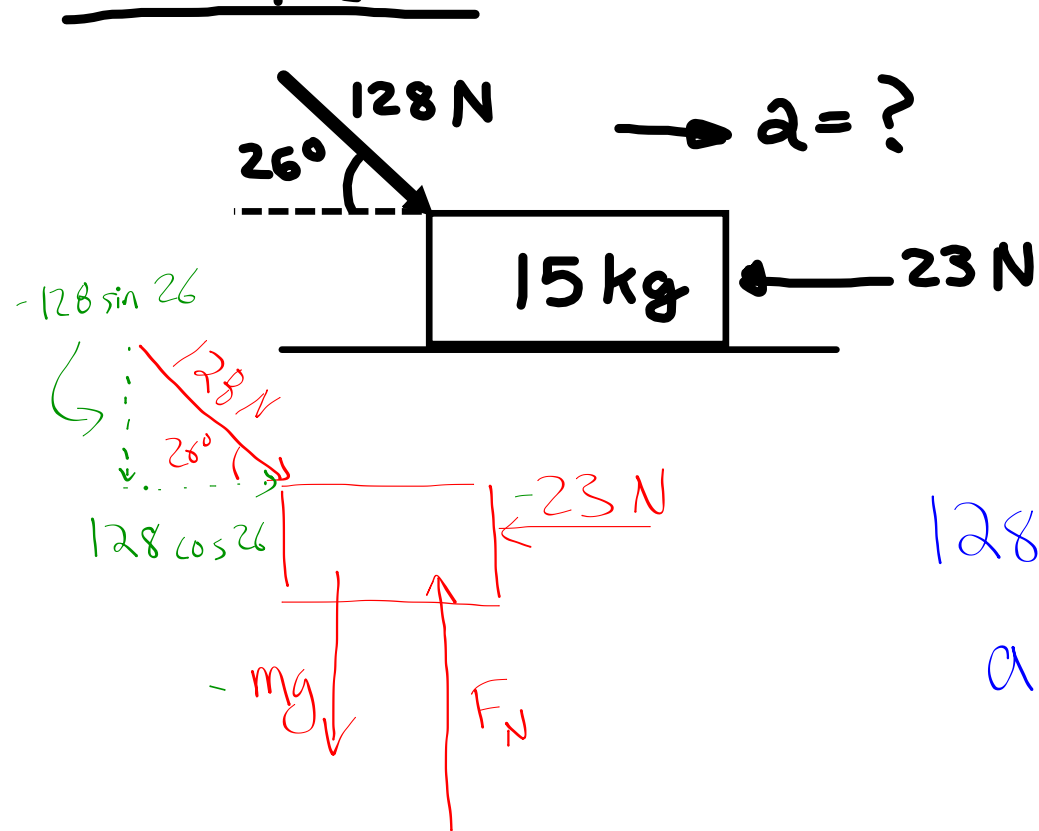


Assume there is no friction in any problem unless stated otherwise ...



$$\sum F_x = ma_x$$

$$F = (3.8)(5.9)$$

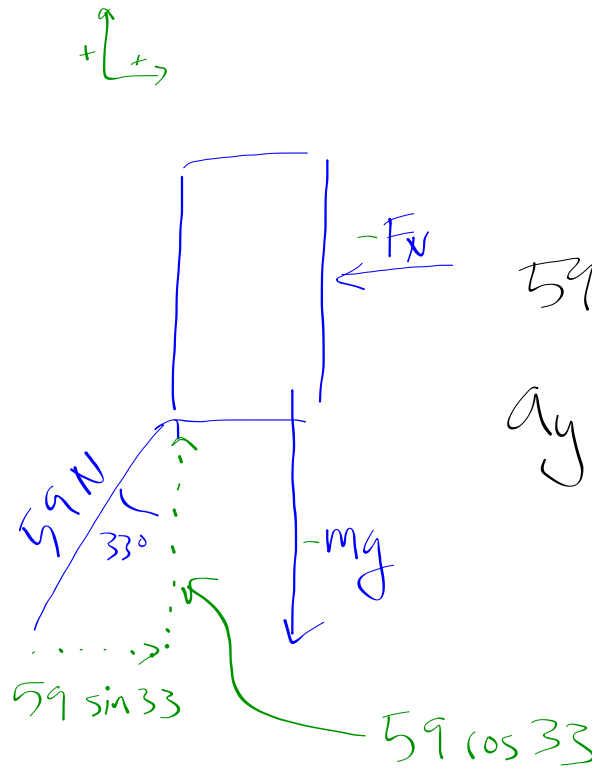
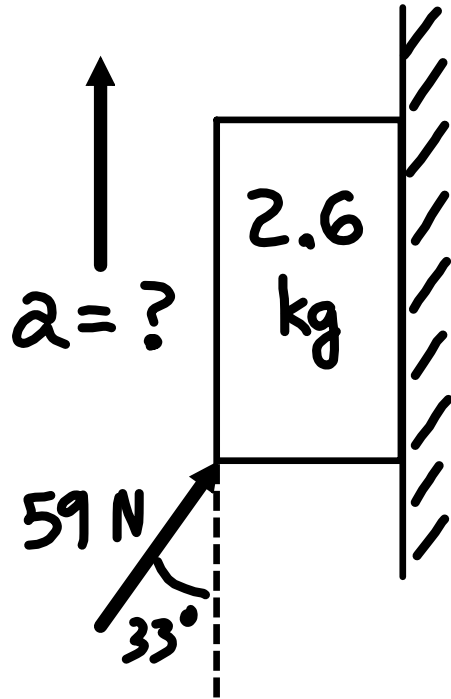
EXAMPLE 2:

$$\sum F_x = ma_x$$

$$128 \cos 26 + -23 = (15)a_x$$

$$a_x = \frac{128 \cos 26 + -23}{15}$$

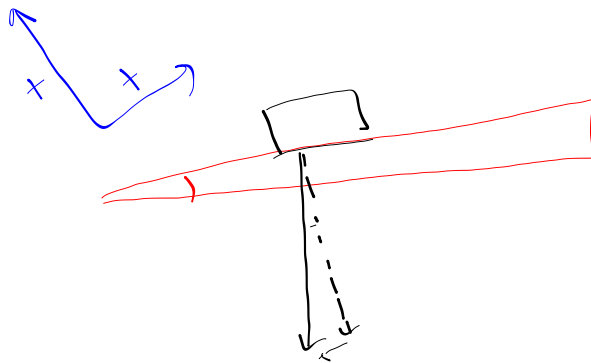
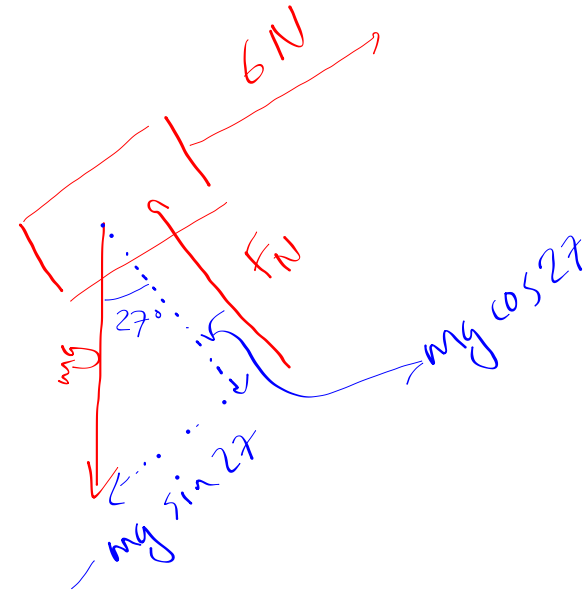
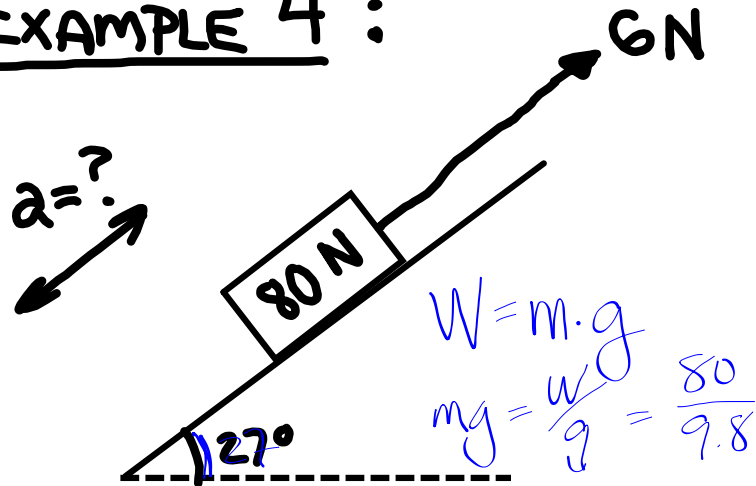
EXAMPLE 3 :



$$\sum F_y = ma_y$$

$$59 \cos 33 + -mg = 2.6a_y$$

$$a_y = \frac{59 \cos 33 - mg}{2.6}$$

EXAMPLE 4 :

$$\sum F_x = m a_x$$

$$-mg \sin 27 + 6 = \left(\frac{80}{9.8}\right) a_x$$

$$a_x = \frac{(-80 \sin 27 + 6) \cdot 9.8}{80}$$

$$a_x = -3.71 \text{ m/s}^2$$

Friction:

A force! It pushes or pulls just like any other force.

Exists between two surfaces in contact with one another.

Resists relative motion between the two surfaces.

Always opposite direction of motion (or potential motion - in absence of friction).

The force of friction can change:

- Static friction: *Friction force between objects that aren't sliding.*
- Kinetic friction: *Friction force between objects that are sliding.*

Friction = coefficient \times "clamping force"

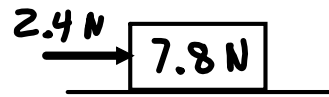
$$F_{fr} = \mu F_n$$

F_n = the force clamping the two surfaces together
(usually the normal - perpendicular - force)

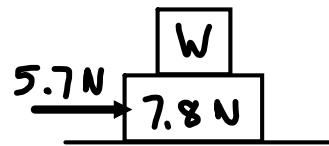
μ = the coefficient of friction

- > Unitless (reflects that the force of friction is related to the normal force)
- > Usually less than 1.0 (but not always)
- > Unique to any two surfaces
- > Two kinds:

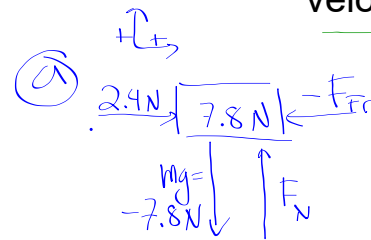
- μ_k : coefficient of kinetic friction
- μ_s (always greater than kinetic...): coefficient of static friction
(the maximum amount we multiply F_n) - tells us
the maximum amount of F_{static}

EXAMPLE 1

a) For the 7.8 N object to move across the surface by itself at constant speed, a 2.4 N force must be applied. What is the coefficient of kinetic friction? $a=0$



b) If the 2.4 N force must be increased to 5.7 N when an object with weight W is placed on the 7.8 N object, what is W? Assume the two blocks move at constant velocity. $a=0$



$$F_{fr} = \mu F_N$$

$$\sum F_x = 0$$

$$2.4 + -F_{fr} = 0$$

$$F_{fr} = 2.4 N$$

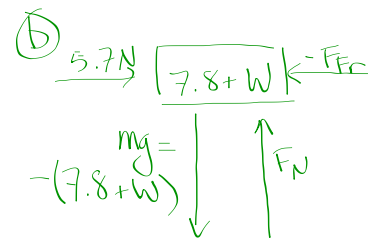
$$2.4 = \mu(7.8)$$

$$\mu = 0.31$$

$$\sum F_y = 0$$

$$-7.8 + F_N = 0$$

$$F_N = 7.8$$



$$\sum F_x = 0$$

$$5.7 + -F_{fr} = 0$$

$$F_{fr} = 5.7 N$$

$$F_{fr} = \mu F_N$$

$$5.7 = (0.31)(7.8 + W)$$

$$5.7 = 2.42 + 0.31 W$$

$$W = 10.58 N$$

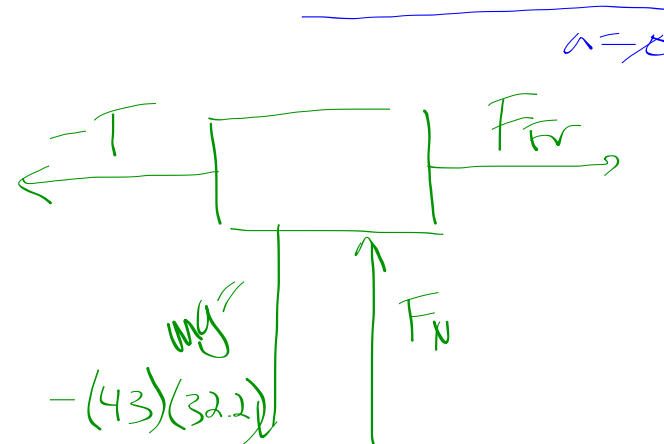
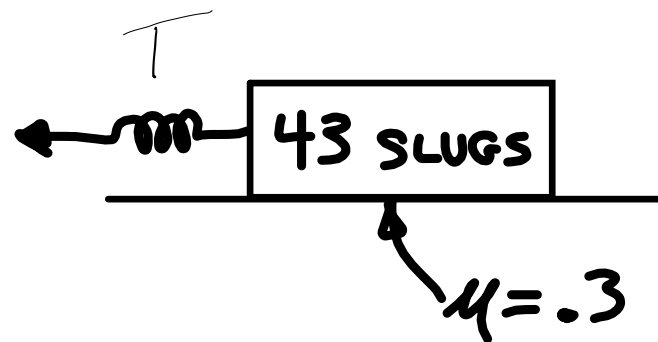
$$\sum F_y = 0$$

$$-(7.8 + W) + F_N = 0$$

$$F_N = 7.8 + W$$

EXAMPLE 2

What must the tension in the spring be in order to slide the mass along the surface at constant speed?



$$\Sigma F_x = 0$$

$$\Sigma F_y = 0$$

$$-T + F_{fr} = 0$$

$$F_{fr} = T$$

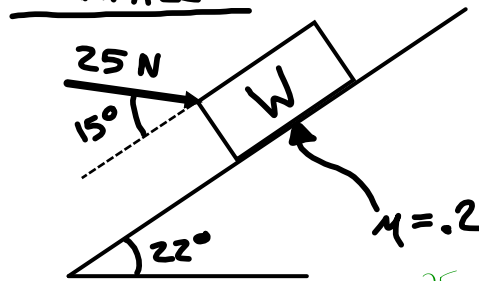
$$-(43)(32.2) + F_N = 0$$

$$F_N = 1384.6 \text{ lb}$$

$$F_{fr} = \mu F_N$$

$$T = (0.3)(1384.6)$$

$$\boxed{T = 415.2 \text{ lb}}$$

EXAMPLE 3

What is W if the object moves up the incline at constant speed? (W is a weight) $a = 0$

$$\sum F_x = 0$$

$$24.15 - W \sin 22 - F_{Fr} = 0$$

$$F_{Fr} = 24.15 - W \sin 22$$

$$\sum F_y = 0$$

$$F_N + (-6.47) + (-W \cos 22) = 0$$

$$F_N = 6.47 + W \cos 22$$

$$F_{Fr} = \mu F_N$$

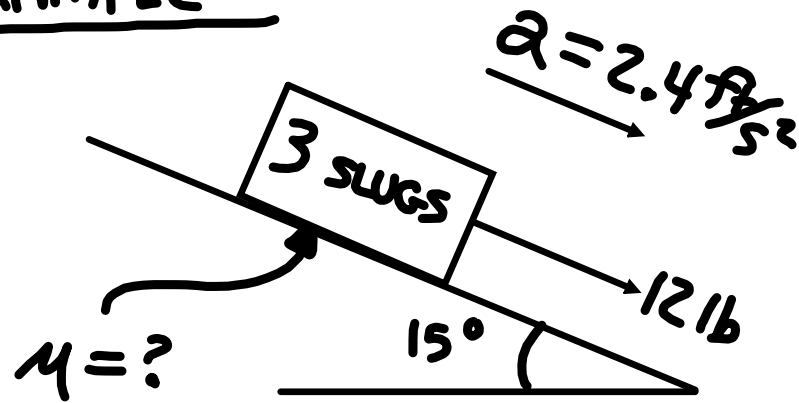
$$24.15 - W \sin 22 = (0.2)(6.47 + W \cos 22)$$

$$24.15 - W \sin 22 = 1.29 + (0.2)(W)(\cos 22)$$

$$W \sin 22 + (0.2)(W) \cos 22 = 22.86$$

$$W(\sin 22 + (0.2) \cos 22) = 22.86$$

$$W = \frac{22.86}{\sin 22 + 0.2 \cos 22} = \frac{22.86}{0.375 + 0.185} = \boxed{40.82 \text{ N}}$$

EXAMPLE 4WHAT MUST μ BE?