

1. Mandy Lifeboats and Ty Dalwaive are walking on a beach when they see a treasure chest. They push the 67.2-kg chest up the beach (which makes an angle of 25.0° with the horizontal). The coefficient of kinetic friction between the beach sand and the chest is .920. If they push the treasure chest at a constant velocity for 8.33 meters,

- What work do Mandy and Ty do on the chest? 6892.3 J
- Why is it important that they push *parallel* to the surface of the beach (the incline)?

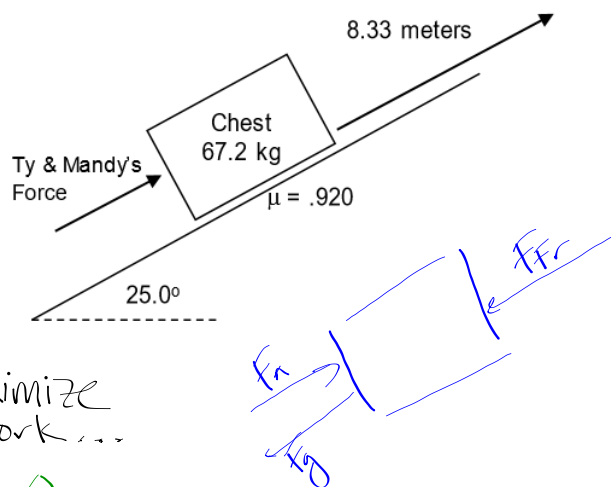
To minimize friction & maximize the force that is doing work...

$$F_A + F_g + F_{Fr} = 0$$

$$F_g = (67.2)(9.8)(\sin 25)$$

$$F_{Fr} = (67.2)(9.8)(\cos 25)(0.920)$$

$$F_A = 827.4 \text{ N} \quad W_A = (827.4)(8.33) \\ = \boxed{6892.3 \text{ J}}$$



2. Suddenly the chest pops open. Inside is a spring ($k = 695 \text{ N/cm}$) that is compressed by 8.60 cm with a 4.70-kg book resting on it. Mandy accidentally triggers the spring's release mechanism.

- a) How high (above the book's original position) will the text go after the spring is released? $v = 0$; $h = 55.8 \text{ m}$
 b) What will the book's maximum upward speed be? $h = 8.6 \text{ cm} = 0.086 \text{ m}$

$\frac{1}{2} k x_0^2 = \frac{1}{2} m v^2 + mgh$
 $\frac{1}{2} (695) (8.6)^2 = (4.7) (9.8) h$
 $2570 \text{ J} = (4.7) (9.8) h$
 $h = 55.8 \text{ m}$

$2570 \text{ J} = \frac{1}{2} (4.7) v^2 + (4.7) (9.8) (0.086)$
 $v = 33.05 \text{ m/s}$

EPE
of
spring

$$695 \text{ N/cm} \cdot \frac{100 \text{ cm}}{\text{m}} = 695000 \text{ N/m}$$

$$8.6 \text{ cm} \cdot \frac{1 \text{ m}}{100 \text{ cm}} = 0.086 \text{ m}$$

$$\frac{1}{2} k x^2 = \frac{1}{2} (695000) (0.086)^2 = 2570 \text{ J}$$

3. You are sitting upon a 27° incline that is 9.472 meters long and you weigh 800 N. Because it is a very slippery surface, the coefficient of kinetic friction is a mere 0.15. There is a flat surface at the bottom of the incline that also has a coefficient of kinetic friction of 0.15. Your friend is pushing you with a constant 100 N force that is parallel to both surfaces the entire way. How far do you travel along the flat surface?

$$mgh + \underbrace{W_F + W_{Fr}}_{\text{on ramp}} = \left[\frac{1}{2}mv^2 \right]$$

Diagram: A block of 800 N is on a 27° incline of length 9.472 m. Forces shown: $F = 100\text{ N}$ (up the incline), F_g (down the incline), and F_{Fr} (up the incline). A calculation shows $-947.2 - 1012.8 = -1480$ with an arrow pointing to 0.

Calculation: $9.472 \cdot \sin 27 = h$

$$\frac{1}{2}mv^2 + \underbrace{W_F + W_{Fr}}_{\text{on flat}} = 0$$

So...

$$mgh + \underbrace{W_F + W_{Fr}}_{\text{on ramp}} + \underbrace{W_F + W_{Fr}}_{\text{on flat}} = 0$$

$$\begin{aligned} & (800)(9.472)(\sin 27) + \text{GPE (initial)} \\ & - (100)(9.472) + \text{Work done by friend} \left\{ \begin{array}{l} \text{on ramp} \\ \text{on flat} \end{array} \right. \\ & - (800)(9.472)(\cos 27)(0.15) + \text{Work done by friction} \\ & - (100)d + \text{Work done by friend} \left\{ \begin{array}{l} \text{on ramp} \\ \text{on flat} \end{array} \right. \\ & - (800)(d)(0.15) + \text{Work done by friction} \end{aligned}$$

$$3440 + -947.2 + -1012.8 + -100d + -120d = 0$$

$$-220d = -1480; \quad d = 6.73\text{ m}$$