

Algebra with Variables:

If you know tables are generated through algebra

with #'s

$$\begin{array}{rcl} \textcircled{1} & 7 \times a + 11 & = 4 \\ & - 11 & - 11 \\ \hline & 7a & = -7 \\ \textcircled{2} & \frac{7a}{7} & = \frac{-7}{7} \\ & a & = -1 \end{array}$$

$$\left\{ \begin{array}{rcl} w \times a + x & = & z \\ & - x & - x \\ \hline wa & = & z - x \\ \frac{wa}{w} & = & \frac{z - x}{w} \\ a & = & \frac{z - x}{w} \\ a & = & \frac{4 - 11}{7} = \frac{-7}{7} \\ a & = & -1 \end{array} \right.$$

Example $a = \frac{v - v_0}{t}$

① $t \cdot a = \frac{v - v_0}{\cancel{t}} \cdot \cancel{t}$

② $\frac{\cancel{a}t}{\cancel{a}} = \frac{v - v_0}{a}$

$$\boxed{t = \frac{v - v_0}{a}}$$

① $at = \frac{v - v_0}{\cancel{a}} \cdot \cancel{a}$

② $at = v - \cancel{v_0}$
 $+v_0 \quad +\cancel{v_0}$

$$\boxed{v = v_0 + \cancel{at}}$$

③ $-at \quad = \cancel{at}$

$$\boxed{v_0 = v - at}$$

Example: Conservation of momentum

momentum before = momentum after

? = $\boxed{\begin{array}{c} m_1 \\ m_2 \\ v_1 \\ v_2 \\ v_1' \\ v_2' \end{array}}$

$$\cancel{m_1 v_1} + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

① $\cancel{-m_1 v_1}$

$-m_1 v_1$

②

$$\frac{\cancel{m_2 v_2}}{\cancel{m_2}} = \frac{m_1 v_1' + m_2 v_2' - m_1 v_1}{m_2}$$

$$v_2 = \frac{m_1 v_1' + m_2 v_2' - m_1 v_1}{m_2}$$

Finding mass...

$$\textcircled{1} \quad m_1 v_1 + m_2 v_2 = \cancel{m_1 v_1'} + m_2 v_2' \\ - m_1 v_1' \quad - \cancel{m_1 v_1'}$$

$$\textcircled{2} \quad m_1 v_1 - \cancel{m_1 v_1'} + \cancel{m_2 v_2} = m_2 v_2' \\ - \cancel{m_2 v_2} \quad - m_2 v_2$$

$$\textcircled{3} \quad \hookrightarrow m_1 v_1 - m_1 v_1' = m_2 v_2' - m_2 v_2$$

$$\textcircled{4} \quad \frac{m_1 (\cancel{v_1} - v_1')}{(\cancel{v_1} - v_1')} = \frac{m_2 v_2' - m_2 v_2}{(v_1 - v_1')} \quad \begin{matrix} a(b+c)= \\ ab+ac \end{matrix}$$

$$m_1 = \frac{m_2 v_2' - m_2 v_2}{v_1 - v_1'}$$