

Previously:

Add polynomials  $(2x^2 - 7) +$   
 $3x^2 - 10x + 4$   $(x^2 - 3x + 4)$

Multiply polynomials  $(2x - 7)(x + 2)$   
 $2x^2 - 3x - 14$

Factor out GCF  $2x^2 + 4x$   
 $2x(x + 2)$

Solve factored polynomials  
 $(x + 2)(2x - 4) = 0$

$x + 2 = 0$      $2x - 4 = 0$

$x = -2$  or  $x = 2$

Factoring  $x^2 + bx + c$ :  $\rightarrow (x+p)(x+q)$

$$\begin{array}{l} (x+7)(x+8) \\ x^2 + 8x + 7x + 56 \\ x^2 + 15x + 56 \end{array}$$

Reverse-multiply polynomials

Find  $p$  and  $q$  so that:

$$p + q = b$$

$$pq = c$$

$$(x+p)(x+q)$$

$$x^2 + \boxed{q \cdot x + p \cdot x} + pq$$

$$x^2 + \underline{(p+q)}x + \underline{pq}$$

How to factor:  $x^2 + bx + c \rightarrow (x+p)(x+q)$

$$x^2 + 7x + 12$$

Find all the factors (p and q) of c

| p   *   q |    | p+q (b) | pq (c) |
|-----------|----|---------|--------|
| 1         | 12 | 13      | 12     |
| 2         | 6  | 8       | 12     |
| 3         | 4  | 7       | 12     |
|           |    |         |        |
|           |    |         |        |

See which factors work:

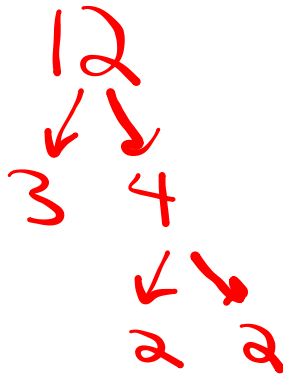
$$p + q = b$$

$$pq = c$$

$$(x+3)(x+4)$$

$$x^2 + 4x + 3x + 12$$

$$x^2 + 7x + 12$$



How to know the signs of  $p$  and  $q$ :

$$x^2 + bx + c \rightarrow (x+p)(x+q)$$

| $b (p+q)$ | $c (pq)$ | $p$      | $q$ |
|-----------|----------|----------|-----|
| +         | +        | +        | +   |
| -         | +        | -        | -   |
| -         | -        | opposite |     |
| +         | -        | opposite |     |

Use the signs of  $b$  and  $c$  to determine the signs of  $p$  and  $q$

$$-x^2 + 2x + 1$$

$$-1(x^2 - 2x - 1)$$

$$x^2 + 2x + 3$$

$$x^2 - 6x + 11$$

$$x^2 - 4x - 7$$

$$x^2 + 3x - 4$$

$$\left. \begin{array}{l} x^2 - 6x + 11 \\ x^2 - 4x - 7 \\ x^2 + 3x - 4 \end{array} \right\} (x + \quad)(x - \quad)$$

Factor the trinomial.

1.  $x^2 + 8x + 7$

$$(x+1)(x+7)$$

|   |   |        |        |
|---|---|--------|--------|
| p | q | b(p+q) | c(p·q) |
| 1 | 7 | 8      | 7      |

4.  $p^2 + 10p + 25$

$$(x+5)^2$$

|   |   |        |        |
|---|---|--------|--------|
| p | q | b(p+q) | c(p·q) |
| 1 | 5 | 10     | 25     |

$$(x+5)(x+5)$$

$x^2 - 7x + 10$

2.  ~~$b^2 - 7b + 10$~~   

$$(x-2)(x-5)$$

|   |    |        |        |
|---|----|--------|--------|
| p | q  | b(p+q) | c(p·q) |
| 1 | -5 | -4     | -5     |

3.  $w^2 - 12w - 13$

$$(w+1)(w-13)$$

|    |     |     |     |
|----|-----|-----|-----|
| 1  | -13 | -12 | -13 |
| -1 | 13  | 12  | -13 |

5.  $m^2 - 10m + 24$

$$(m-4)(m-6)$$

|   |    |    |    |
|---|----|----|----|
| 1 | 24 | 25 | 24 |
| 2 | 12 | 14 | 24 |
| 3 | 8  | 11 | 24 |
| 4 | 6  | 10 | 24 |

6.  $y^2 - 5y - 24$

$$(y+3)(y-8)$$

|    |     |    |     |
|----|-----|----|-----|
| 1  | 24  | 23 |     |
| 1  | -24 | 23 |     |
| 2  | 12  | 10 |     |
| 2  | -12 | 10 |     |
| -3 | 8   | 5  | -24 |
| 3  | -8  | -5 | -24 |
| 4  | 6   | 2  |     |
| 4  | -6  | 2  |     |

Solve a polynomial equation:  $ax^2 + bx + c = 0$

$$x(x + 17) = -60$$

Simplify and rearrange the equation so that it is in the format shown above

Factor the resulting polynomial

Use the zero-products property

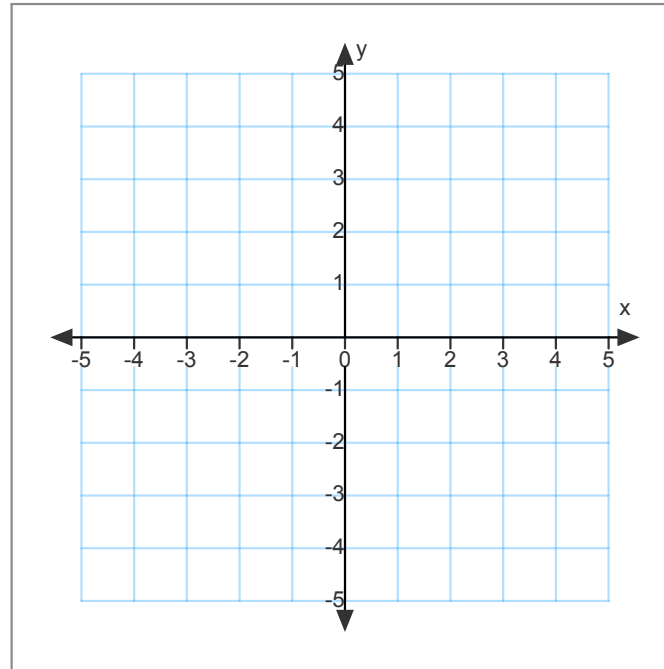
**28.**  $n(n + 6) = 7$

**29.**  $s^2 - 3(s + 2) = 4$

**30.**  $d^2 + 18(d + 4) = -9$

# What does a solution to a polynomial look like?

$$x^2 - 5x + 6$$





## Finding "zeros" of a polynomial function:

$$f(x) = x^2 - 5x - 36$$

"f(x)" means y

To solve a polynomial means to find where  $y = 0$  (in other words, find the x-intercept)

So: set  $f(x) = 0$ , then solve the resulting equation (THIS IS WHAT WE JUST DID!!)

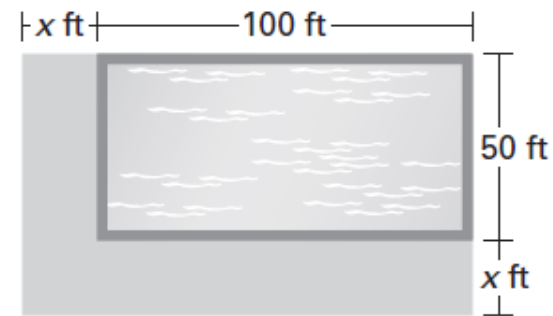
**22.**  $f(x) = x^2 + 11x + 28$

**23.**  $g(x) = x^2 + 11x - 12$

**24.**  $h(x) = x^2 + 3x - 18$

**Patio Area** A community center is building a patio area along two sides of its pool. The pool is rectangular with a width of 50 feet and a length of 100 feet. The patio area will have the same width on each side of the pool.

- Write a polynomial that represents the combined area of the pool and the patio area.
- The combined area of the pool and patio area should be 8400 square feet. How wide should the patio area be?



# Homework:

p. 586, 20-28 all; ~~31-41 odd; 59, 60~~

