TRANSLATION	ROTATION
X (METERS)	O (RADIANS)
v ( M/s)	w (rad/s)
a (m/s2)	$\propto (^{rad}/_{5^2})$
v=v. + at	$w = w_0 + \alpha t$
$X = X_0 + v_0 t + \frac{1}{2} a t^2$	0=00+wot+2~t2
$v^2 = v_0^2 + 2a(x - x_0)$	$\omega^2 = \omega_0^2 + 2 \propto (\Theta - \Theta_0)$
m (kg)	I (kg·m²)
EF = ma	Σ <sub>0</sub> = Ι∝
KE=2mv2	KEROT = ZIWZ
P = mv	my Lac = I w
- ΣF = ΔP/Δt	~20 = <sup>Δ</sup> [/ <sub>4</sub> t
WHEN EF=O, THEN	WHEN ET = O, THEN
P IS CONSERVED	L IS CONSERVED
THE TWO SYSTEMS ARE CONNECTED BY:	
O= % W= % X = dy New FOR TODAY	

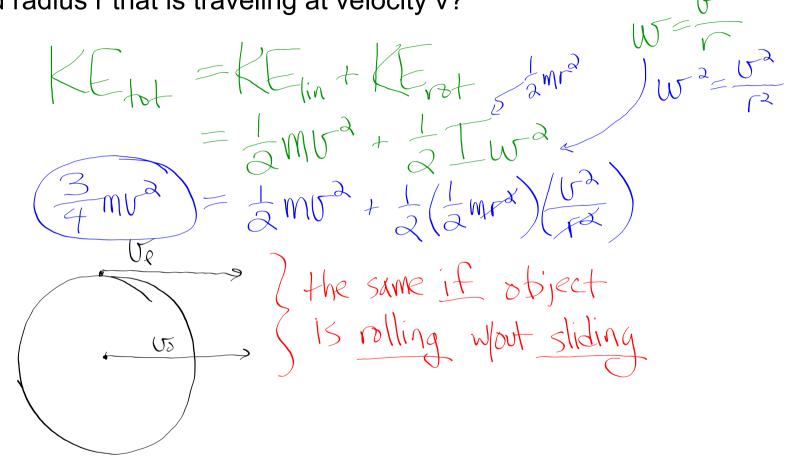
Let's consider rotational KE first:

Big Picture? We modify CLEE -- KE now has two terms, one for translation and one for rotation.

Except for the new term, CLEE is used exactly as before.

Rolling objects are great examples of objects both translating and rotating.

EXAMPLE: What is the total KE of a rolling disk ( $I = \frac{1}{2}mr^2$ ) of mass m and radius r that is traveling at velocity v?



EXAMPLE 2: If a ball ( $I = 2/5 \text{mr}^2$ ) moving at 5 m/sec heads up an incline, how high above the bottom of the incline will it get? Assume the ball's radius is 0.3 meters, and the ball's mass is 1.6 kg.

$$\frac{1}{2}mv_{0}^{2} + \frac{1}{2}Iw_{0}^{2} + myh_{0} + \frac{1}{2}kx_{0}^{2} + W_{0}c = \frac{1}{2}mv^{2} + myh + \frac{1}{2}kx^{2}$$

$$\frac{1}{2}mv_{0}^{2} + \frac{1}{2}Iw_{0}^{2} = mgh$$

$$\frac{1}{2}mv_{0}^{2} + \frac{1}{2}Iw_{0}^{2} = mgh$$

$$\frac{1}{2}(5)^{2} + \frac{1}{2}(5)^{2} = (9.8)h$$

$$h = 1.79m$$

Angular momentum is a conserved quantity when there are no outside torques acting on the system in question.

We can "cheat" and can conserve angular momentum as we did when assuming linear momentum is conserved during collisions if we minimize the time that passes.

When angular momentum is conserved:

IF 
$$\Sigma \tau = 0$$
,  $\Delta L = 0$ 

IF  $\Sigma \tau = 0$ ,  $\Delta L = 0$ 

Let Angular Momentum 1s

Conserved

(i.e. - IT STAYS THE SAME)

Iows = If we if  $\Sigma \tau = 0$ 

Looking at this last equation, a system's angular momentum might change because its moment of inertia changes. How?

- The system's mass might change.
- The location of mass might change.

EXAMPLE 3: An ice skater spinning at 5 rad/sec has an I of 16 kg-m<sup>2</sup>. After pulling her arms in, her I is 10 kg-m<sup>2</sup>. What is her new angular velocity?

$$T_{o}W_{5} = T_{f}W_{f}$$
 $(16)(5) = (10)W_{f}$ 
 $W_{f} = 8 \text{ rad}$ 

EXAMPLE 4: A metal ring (I = mr²) spinning about its center has a radius of 0.5 meters and rotates at 6.5 rad/sec. If the ring's temperature increases so that its radius is now 0.55 meters, what is its new angular velocity?

$$T_{0}W_{0} = T_{0}W_{0}$$
 $W_{0} = M_{0}^{2}W_{0}$ 
 $(.5)^{3}(6.5) = (0.55)^{3}W_{0}$ 
 $W_{0} = 5.37$