

This week: Cover radicals
(square roots)

Test FRIDAY

Last two weeks of semester:

Cover ch. 13 (statistics)

Test over ch. near end of semester

Square roots \neq radicals:

A square root is the number you multiply by itself to get another number.

$$6 \cdot 6 = 36$$

six is the square root of 36

$$9 \cdot 9 = 81$$

9 is the square root of 81

$$1.72 \times 1.72 = 2.9584$$

1.72 is the square root of 2.9584

Radical sign means "find the positive square root" of the number.

$$\sqrt{25} = \text{find the } \underline{\text{positive}} \text{ square root of } 25$$

$$\boxed{25 = 5 \cdot 5}$$

$$25 = -5 \cdot -5$$

$$\sqrt{x} = \underline{\text{always positive}}$$

$$-\sqrt{x} = \underline{\text{always negative}}$$

$$\pm\sqrt{x} = \text{both positive and negative square roots}$$

Square roots of negative #:

NOT A REAL NUMBERS =

we'll ignore them

$$-\sqrt{25} = -5$$

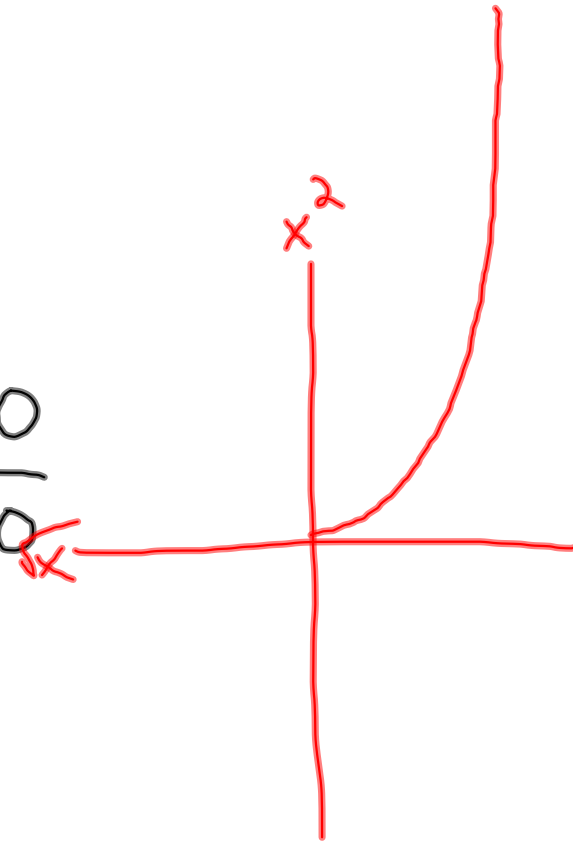
$$\sqrt{-25} = \text{we'll ignore}$$

$$\sqrt{0} = 0 \quad (\text{neither } - \text{ or } +)$$

$$\sqrt{x} = \boxed{\text{integer } (1, 2, 3 \dots)}$$
$$\quad \quad \quad \neq \text{not an integer (decimal)}$$

\sqrt{x}	x
1	1
2	4
3	9
4	16
5	25
6	36

\sqrt{x}	x
10	100
20	400
50	2,500
100	10,000



$\sqrt{x} =$ if the answer is an integer, then x is a "perfect square"

• 81 is a perfect square because

$$\sqrt{81} = 9$$

• 144 is a perfect square because

$$\sqrt{144} = 12$$

• 146 is not a perfect square—

$\sqrt{146}$ is not an integer

For perfect squares

. You can find \sqrt{x} by "progressively estimating":

$$\sqrt{121} = ? \quad \underline{\underline{11}} \quad \sqrt{900} = 30$$

$$9^2 = 81$$

$$12^2 = 144$$

$$10^2 = 100$$

$$20^2 = 400$$

$$25^2 = 625$$

$$40^2 = 1600$$

Evaluate the expression.

1. $\pm\sqrt{81}$

9, -9

2. $\pm\sqrt{25}$

5, -5

$10^2 = 100$
 $100^2 = 10000$
 $50^2 = 2500$
 $30^2 = 900$ 3. $-\sqrt{400}$
 $20^2 = 400$ -20

4. $\sqrt{625}$

25

5. $\sqrt{4900}$

70

6. $\pm\sqrt{169}$

13, -13

~~$\sqrt{490}$~~

Approximate the square root of a number that's not a perfect square:

$$\sqrt{722}$$

$$= \boxed{\text{between } 26 \text{ \& } 27}$$

$$26.87$$

$$10^2 = 100$$

$$20^2 = 400$$

$$30^2 = 900$$

$$25^2 = 625$$

$$28^2 = 784$$

$$27^2 = 729$$

$$26^2 = 676$$

Approximate the square root to the nearest integer.

7. $-\sqrt{29}$

$$5^2 = 25$$

$$6^2 = 36$$

between -5 & -6

8. $\sqrt{108}$

$$10^2 = 100$$

$$11^2 = 121$$

between 10 & 11

9. $-\sqrt{53}$

$$7^2 = 49$$

$$8^2 = 64$$

between -7 & -8

10. $\sqrt{138}$

$$11^2 = 121$$

$$12^2 = 144$$

between 11 & 12

11. $-\sqrt{55}$ ←

12. $\sqrt{640}$

$$25^2 = 625$$

$$26^2 = 676$$

between 25 & 26

irrational #'s cannot be written as fractions of integers.

$$\frac{a}{b} \text{ (where } a \neq b \text{ are integers)} = \text{RATIONAL NUMBER}$$

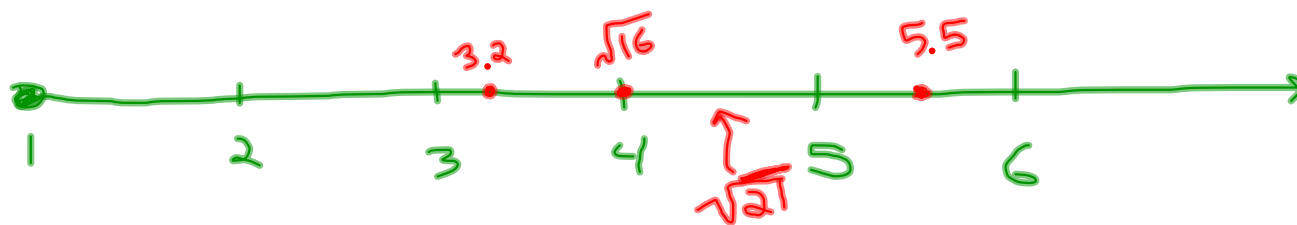
Square roots of whole numbers are either integers ($\sqrt{625} = 25$, $-\sqrt{81} = -9$) OR irrational numbers:

$$\sqrt{626}, \sqrt{82}, -\sqrt{27} = \text{irrational numbers}$$

irrational numbers have a never-ending, never-repeating decimal part:

2.31207561520983.....

$$\begin{array}{c} 3.2 \\ \sqrt{16} = 4 \\ 5.5 \end{array}$$



$$\begin{array}{c} \sqrt{21} \\ 4^2 = 16 \\ 5^2 = 25 \end{array}$$

Homework:

p. 113: 3-14 (all)
15-21 (odd)
24-26 (all)
38-41 (all)