Neural/Cloud Interface to Extend Human-Computer Interaction for WebXR Applications



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Abstract

This is a rough draft of the abstract: There are various types of neural interfaces. There are various types of software for neural interfaces. There are various types of users for neural interfaces. The advantages and disadvantages of using local software versus software running in the cloud. A neural/cloud-based interface is defined as a production-ready and mainstream-ready BCI application in this thesis. Connecting web-based BCIs to the future of software, moving towards 3D and spatial computing, and how the web can play an essential role alongside BCI unobtrusive BCI technologies. Paradigm-shift for BCI software and 3D software running in browsers.

The goal is to provide a comprehensive overview of a neural/cloud interface and the components that comprise it. To lay the groundwork for future developers based on empirical technical experience in developing a real-world neural/cloud interface for IDUN Technologies' in-ear EEG sensor product. As part of this project, a public example code is provided.

We also discuss 3D on the web and the implications for human-computer interaction with a BCI based on a neural/cloud interface. Demonstrating the potential for additional use cases and the future of BCI software, web applications, and 3D software.



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Introduction

This chapter introduces the reader to the primary focus of this thesis and introduces key topics and their explanations. It also displays the research question, aims, objectives, and distinctions of the thesis's primary contents and structure.

1.1 Background

There has been a long-standing interest in developing neural interfaces, systems that sense electrical impulses from the nervous system and use them to intercommunicate with the human brain. Successful research into the development of technologies that enable neural interfaces has been going on for decades, with the first experiments being conducted by Jacques J. Vidal in the late 1970s (Vidal, 1977). Progress has accelerated significantly in the past few years, especially since the advent of modern processing capabilities such as in deep learning with convolutional neural networks (CNN) or generative adversarial networks (GAN) (Gonfalonieri, 2019). In particular, a related discipline called brain-computer interfacing (BCI), a field focused on the direct interaction between brains and computers, has accumulated much momentum since the popularity of companies like Neuralink and Kernel.

One aspect of neural interfaces is hardware tailored to the human body. Whether it is an invasive sensor, such as in electrocorticography (ECoG), a method which uses electrodes placed on the surface of the brain, or a non-invasively placed sensor on the body, such as in electroencephalography (EEG). Both methods measure electrical activities produced by neurons; however, with decreasing spatial precision, the farther the electrode is placed from the brain, the more body structures (e.g. bones) are between firing neurons and the measuring sensor. The other aspect is software that reads and interprets data of these hardware sensors. Both aspects present their own set of challenges and complexities. Nonetheless, complete and applicable neural interfaces work in practice and have been used for many years in patients with neurological disorders (BrainGate, n.d.). There are also consumer and non-clinical neural interfaces available, such as the Neurosity and OpenBCI products, which aim to democratise the use of EEG sensors by offering low-cost hardware and simple-to-use software.



Fig. 1.1: Les Baugh, an amputee, is using a neural interface to control two robotic arms with his thoughts (Campbell, 2014).

1.2 Relevance

The possibilities of connecting the human brain with computers are almost limitless because one has to think that we are the brain, that our own perception of reality, all our feelings, memories and actions are supposed to be contained in the electrical impulses of our brain. The ability to communicate directly with our thoughts and the outside world — whether through digital or physical objects — is a fantastic prospect. There are several use cases: Controlling prosthetic limbs for amputees (Murphy et al., 2017), communication for people with locked-in syndrome (Chaudhary et al., 2022), diagnosing neurological problems and improving the mental capacities of elderly patients (Belkacem et al., 2020) are promising examples, to name a few.

It may appear evident that neural interfaces can significantly impact the field of therapeutics and accessibility for a small subset of the human population. However, one can envision not only alleviating deplorable living conditions but also improving the lives of

healthy people through more natural or efficient ways of interacting with things or by directly altering human brains for certain benefits. Because most current neural interface applications concentrate on the first aspect of therapeutics and accessibility, other use cases, such as stimulating the brain to improve concentration, modifying cognitive load, or even uploading new knowledge directly into the brain, may appear to be science fiction ideas.

Regardless, many capable people — research labs and even entire companies — are developing neural interface hardware and software aimed at the general population without conditions that envision a future for such use cases in the long term. The applicability of a neural interface system to the mainstream will depend on several factors, presumably an important factor of which is the hardware's form factor. Nonetheless, the totality of the ecosystem in which the software resides is a valuable aspect that should not be overlooked.

1.3 Research question

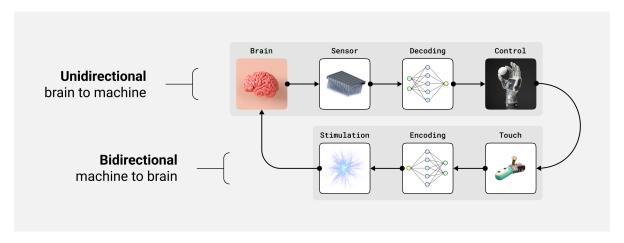


Fig. 1.2: Difference between an unidirectional and bidirectional neural interface and its components (own representation, 2022).

Whether it is a bidirectional and invasive neural interface with the potential to be implanted on a large scale, as e.g. Neuralink is aiming to do, or a unidirectional and non-invasive interface in various form factors that are also aimed at the mass market, such as in a pair of glasses or a pair of headphones, the data collected from the brain would always need to be processed, contextualised, and classified to produce an intelligible output. The research question of the present thesis is on determining what technical components such a software system would require to be production-ready and suitable for a mass-market product. The emphasis is on a holistic view of such a system, which means that the entire technology stack is taken into account in answering the research question.

Furthermore, most current neural interface software systems in production, for example, for an interface implanted in a living patient, are typically run in a local environment, i.e. the software system and its components are typically located on a physically nearby computer, usually connected by a cable, to reduce latency and avoid complexities introduced by a wireless protocol. There is already promising research on wireless mobile brain-computer interfaces (mBCI) by Minguillon et al. (2017) or possible implications of human brain/cloud interfaces (B/CI) by Martins et al. (2019) or by Angelica et al. (2021), which analyse bringing hypothetical future large-scale brain-computer interface software systems into the cloud.

1.4 Hypothesis

Previous research on brain/cloud interfaces has tended to focus on speculations based on hypothetical scenarios in the future, usually based on the premise of other developed technologies such as neural nanorobotics, vital advances in 5G, or the presence of supercomputers in the cloud, e.g. for the augmentation of the human brain, or a communication network for brain-to-brain interfacing (BTBI), and are thus rather distant from today's pertinence. To distinguish the research presented in this thesis, the author coins the term neural/cloud interface (N/CI), which refers to a holistic software interface that connects a neural interface device to the cloud and then to other neural interfaces, software applications, cloud systems, or physical devices.

The primary hypothesis is that a neural/cloud interface is feasible with modern software technologies, requiring only theoretical groundwork based on empirical engineering in a deployable and producible system. This thesis looks at the process and lessons learned from the author's perspective developing a N/CI in the industry for an actual mainstream-capable neural interface device for a BCI end-user application to shed more light on this.

1.5 Goals and aims

The overall goal of this thesis is to give the reader an overview of the definition of a N/CI, its components, and the lessons learned in building a reproducible production-grade, and enduser facing N/CI application with a non-invasive, unidirectional neural interface hardware. In addition to the overall goal, the thesis aims to illustrate a powerful demonstration of the possibilities of neural interfaces on the World Wide Web for virtual reality (VR) or augmented reality (AR) applications running in a browser environment in order to exemplify how to extend the human-computer interaction (HCI) for future 3D applications when combined with a BCI.

1.6 Objectives

The hypothesis of the present thesis states that an N/CI is realisable with contemporary technologies and thus distinguishes itself from previous work with the term brain/cloud interface from Martins et al. and Angelica et al., which, as already mentioned, rather aims at speculative future scenarios. Based on the research question of which components make up an N/CI, the goal is to establish a holistic N/CI and thus identify and evaluate suitable methods for creating such an N/CI. In order to achieve this goal, the author must achieve the following objectives:

- 1. Identify and illustrate the most relevant software components required to realise a production-grade N/CI.
- 2. Identify and deploy the most effective software components in a given and appropriate context to build a production-grade N/CI.
- 3. Develop and publicly release an example N/CI application codebase that is easy to understand and extend.
- 4. Demonstrate the applicability and impact for HCI of a N/CI with web-based VR/AR applications.

Research Context

This chapter describes the context of the research question and the findings from the current literature. The reader is educated specifically on the limitations of current non-invasive and unidirectional BCIs, the paradigm shift in developing cloud-based and production-ready software versus running software in a research environment, and the implications and hypotheses of web-based approaches to BCIs and 3D applications for VR and AR that relate to the future of software in general in the field of spatial computing.

2.1 Limitations of BCIs

The capabilities of BCIs are not without limitations. In addition to the physical limitations, mainly in material science for the hardware aspects of BCIs, the author attempts to address a broader issue related to neuropsychology that directly correlates to the software aspects.

2.1.1 Decoding brain data

As outlined in the previous chapter, a holistic view of BCI must take into account the aspect of decoding measured neural data and making it intelligible to computer software. It is important to emphasise that the task of decoding neural data is different from decoding thoughts, which is a critical factor for software. Moreover, decoding neural data and extracting the thoughts behind it so that the software can understand them are disciplines on their own. For example, getting computers to recognise letters written on a photograph is a very different problem from reading the written words in the sentences (i.e. computer vision and natural language processing).

Another part is understanding the sentences and their meaning, as in natural language understanding (NLU). NLU is considered an AI-hard problem, which means that the difficulty of these computational problems is equivalent to solving the central problem of artificial general intelligence (AGI) (Demasi et al., 2010), assuming that general human-level intelligence is computational. Understanding less structured data, such as EEG data, is more complicated than understanding structured and human-generated syntax such as written language because it contains more hidden features than a paragraph of text. As a result, the author assumes that understanding brain data might be considered an AI-hard problem.

2.1.2 Abstract thoughts

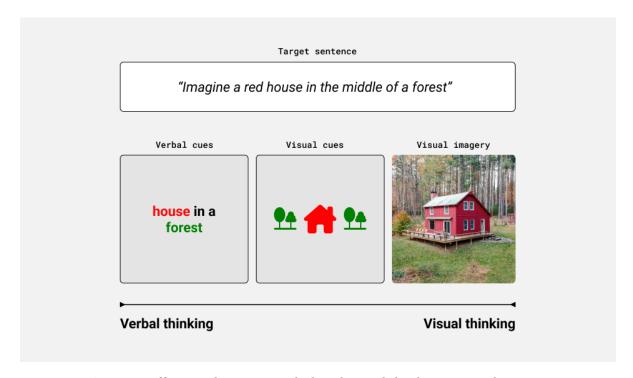


Fig. 2.1: Difference between verbal and visual thinking using the target sentence of a red house in the middle of a forest (own representation, 2022).

Imagine a red house in the middle of a forest. Depending on the individual thought process, one can imagine the house with temporary visual imagery in mind, as in visual thinking, or one can imagine it more verbally, such as conceptually comprehending each word sequentially of what a red house is and that it is located in a forest (Amit et al., 2017). Additionally, it should also be addressed that different types of thoughts exist at different levels of abstraction and complexity. One can assume that the visual image of a red house in the forest is more abstract and far-fetched than, say, the movement of one's own left arm which has a clear physical counterpart. It gets even more complicated when one imagines concepts that are inconceivable to visualise, such as the idea of a company. A company is only an abstract, collectively agreed upon concept without a physical counterpart and is, therefore, even less straightforward and more complex to decode the meaning of measured brain activity than the other mentioned examples of the red house.

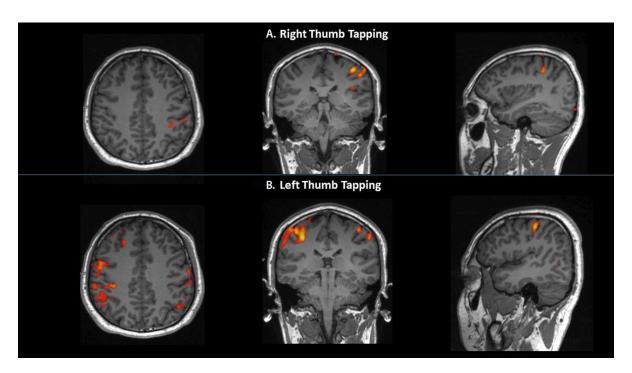


Fig. 2.2: Image of localised activation of neurons during right and left thumb movement using functional magnetic resonance imaging (fMRI) (Rashid et al., 2018).

2.1.3 Technical limitations

Functional tasks of the brain are localised, which means that these signals are generated by local brain areas that can be identified, such as the motor cortex, which has been shown to be responsible for muscle movement as shown on Fig. 2.2. Examining the areas of the brain responsible for activating individual muscle strands can yield a comparable response of muscle stimulation in the brain and thus be measured as output for software to move a prosthesis, for example. However, the more specific, less-functional or abstract the thoughts are, the less the brain areas are spatially visible. To identify, for example, the thought of a red house in a forest in verbal thought, can be classified into three technical problem statements:

- Localisation of each individual neuron and synapse for individual thoughts = current neuroimaging technology and sensors are not sufficient enough to capture each process in a neuron and synapse level of detail.
- Too much data generated not possible to work with it
- Even if we have the technology, it's hard to generate clean brain data that is comparable to previously recorded brain data, because we're all different from each other, we

change over time (neuroplasticity) and we are in different states of mind (different sleep, something bothering someone etc.).

- 2.1.4 Lack of data
- 2.1.5 Low risk and low impact
- 2.2 BCI landscape
- 2.2.1 Real-world BCI applications
- 2.2.2 Unobtrusive hardware and software
- 2.2.3 Active and passive BCIs
- 2.3 Production-grade software
- 2.3.1 Cloud paradigm-shift
- 2.3.2 Web-first BCI architecture
- 2.3.3 3D applications in the browser
- 2.3.4 Web-based AR and VR
- 2.4 N/CI challenges

Methodologies

Skizzieren der akademischen Methodik (kurz und projektbezogen) und der geplanten Vorgehensweise. Begründung der vorgesehenen Workflows, Hard- und Softwaretools. Definition von Phasen (Iterationen) mit Kontrollpunkten für Fortschritt, Feedback und Reflexion respektive die Weiterentwicklung. Möglicher Umfang: ca. 10-20

3.1 Participants

Forty-three patients of the psychiatric clinic with diagnosed major depression (12 male, Mage = 36.35, SDage = 7.92) participated in this study for monetary compensation (10 USD).

3.2 Design

- The study used a between-subject design (treatment group, control group) with the depression score on the XXX depression scale as dependent variable. - The study used a within-subject design (pre-treatment measurement, post-treatment measurement) with the depression score on the XXX depression scale as dependent variable. - The study used a mixed design with the between-subject factor group (treatment, control) and the within-subject factor time (pre-treatment, post-treatment). The depression score on the XXX depression scale served as the dependent variable.

3.3 Materials

- Three types of materials were used. First,... Second,... Third,...

3.4 Procedure

- Before the experiment started, participants were randomly assigned to two groups: the X group and the Y group. - The experiment consistent of two phases. In the first phase,.....

In the second phase,.... - The order of these two phases was counterbalanced - First, participants had to... next... subsequently... finally... - Simultaneously,... - After participants finished X, they...

3.5 Data Analysis

- First, they were randomly assigned to treatment and placebo group - Both groups: 60 minutes intervention - Treatment group: first,... next,... - Placebo group: first,...next,... - Finally, they filled out the depression questionnaire

3.6 Goals

o Did you describe everything that is needed to replicate your research? o Did you cite the sources of your methods or paradigms?

Implementation

4.1 Lorem ipsum

Umfassende und anschauliche (idealerweise Bildmaterial, Screenshots, Zwischenstände. Auch Fehlschläge dokumentieren) Dokumentation, was genau getan / erstellt / programmiert / produziert / etc. wurde. Welche Auffälligkeiten gab es? Welche Entscheidungen wurden getroffen? Welche Änderungen / Einschränkungen / Erweiterungen wurden vorgenommen?

Results

5.1 Ergebnisse: Präsentation des konkreten Endergebnisses. Kompakte Zusammenfassung des Projekts unter Berücksichtigung der anfänglichen Zieldefinition. Wichtig ist dabei, dass man eine kritische Betrachtung der faktischen Resultate vornimmt (Evaluation). Hier ist ein Soll-Ist-Vergleich zur Zielsetzung aus Kapitel 1 mit kritischer Stellungnahme gewünscht. 5.2 Zusammenfassung: Es soll eine Zusammenfassung der Arbeit geschrieben werden und ein Fazit in Bezug auf das Projekt dessen Bedeutung (Relevanz und Nutzen) gezogen werden. Weiterhin soll eine Kritische Betrachtung der eigenen Vorgehensweise erfolgen. Abschließend soll ein Ausblick auf weitere Projektideen, die sich im Rahmen der Arbeit ergeben haben, gegeben werden (Folgeprojekte, Veröffentlichungen, Verwertung). Empfohlener Umfang: ca. 15-20

5.1 Steps Before The Analysis

- Before we analysed the data, we removed all reaction times that were larger than 2000 ms (2% of all observations) based on the assumption that such reaction times are unlikely to reflect spontaneous responses. - The data of two participants were excluded from the analyses because they did not complete the whole study. - Functional images were re-aligned, unwarped, corrected for slice timing, and spatially smoothed using an 8 mm smoothing kernel.

5.2 Main Results

- First, we investigated whether X (research question) - We used an Independent samples t test with groups as independent variable and the depression score as dependent variable - The results showed that the difference between the groups/ conditions was significant - The results showed a significant correlation between... - The results showed a significant interaction between... - Specifically, the average depressions score was lower in the treatment group (M=3.45, SD = 2.18) compared to the placebo group (M=4.83, SD = 2.02).

5.3 Figures And Tables

Add figures to make important results easier to interpret or to provide more information. Use tables to add extensive amounts of information that would be hard to read in text-form.

5.4 Goals

o Did you describe everything that is needed to replicate your results? o Did you describe all pre-processing steps before the main analyses? o Did you mention to which research question each analysis belongs? o Did you avoid interpreting your results? o Did you add figures for making your key results easy to understand (or are they very simple)? o Did you add tables for extensive amounts of (numerical) information?

o Does your discussion go from specific (interpretation) to broad (implications)? o Did you draw conclusions with reservations? ("A possible interpretation is...") o If you expressed a preference for one explanation over another, did provide clear support for this preference? o Did you describe how your research connects to previous research? o Did you make clear what your research adds to existing research? o Did you describe how your research advance our understanding or how they may inspire future applications? o Did you clearly admit limitations before qualifying them? o Did you remind the reader of the value/implications of your research at the end? o Did you include some pointers for future research? (optional)

5.5 Conclusion

- We investigated whether depression can be treated by training a positive focus - Our findings confirm this - Novel perspective on depression - More research needed, more treatments that follow this approach should be developed

Discussion

6.1 Summary

- Research question: Does the REFOCUS treatment work? - Study: treatment group and placebo group with self-reported depression measured afterwards - Findings: Depression was lower after the REFOCUS treatment compared to placebo

6.2 Interpretation

- Explanation 1: REFOCUS treatment reduced depression - Explanation 2: placebo treatment increased depression - However, explanation 2 is unlikely because the same placebo was used in studies A, B, C and there it didn't increase depression

6.3 Integration

- Previous research focused on the question of how unprocessed traumas could cause depression - We are the first who tested the "focus" explanation of depression

6.4 Implications

- It is widely believed that depression is caused by unprocessed traumas - Our findings offer a novel perspective: depression is caused by information processing style - Hence, new approach, new line of research to understand depression, new types of treatment

6.5 Limitations

- We had no measure of depression prior to the treatment - Reason: asking people to score their depression twice can lead to problems (references) - Consequence: we don't know whether depression decreased in treatment group (explanation 1) or increased in placebo group (explanation 2) - However, as mentioned before, it is unlikely that depression increased

- Sample size was relatively low - Reason: it's hard to find enough people with a major depression - However, our results were significant despite the low sample size. This speaks to the effectiveness of the treatment

Bibliography

- Amit, E., Hoeflin, C., Hamzah, N., & Fedorenko, E. (2017). An asymmetrical relationship between verbal and visual thinking: Converging evidence from behavior and fMRI. *NeuroImage*, *152*, 619–627. https://doi.org/10.1016/j.neuroimage.2017.03.029
- Angelica, A., Opris, I., Lebedev, M. A., & Boehm, F. J. (2021). Cognitive Augmentation Via a Brain/Cloud Interface. In I. Opris, M. A. Lebedev, & M. F. Casanova (Eds.), *Modern Approaches to Augmentation of Brain Function* (pp. 357–386). Springer International Publishing. https://doi.org/10.1007/978-3-030-54564-2_17
- Belkacem, A. N., Jamil, N., Palmer, J. A., Ouhbi, S., & Chen, C. (2020). Brain Computer Interfaces for Improving the Quality of Life of Older Adults and Elderly Patients. *Frontiers in Neuroscience*, *14*. Retrieved May 8, 2022, from https://www.frontiersin.org/article/10.3389/fnins.2020.00692
- BrainGate. (n.d.). Publications Timeline. Retrieved May 8, 2022, from https://www.braingate.org/publications-timeline
- Campbell, P. (2014). Amputee becomes first to simultaneously use two APL Modular Prosthetic Limbs. Retrieved May 8, 2022, from https://hub.jhu.edu/2014/12/17/amputeemakes-history/
- Chaudhary, U., Vlachos, I., Zimmermann, J. B., Espinosa, A., Tonin, A., Jaramillo-Gonzalez, A., Khalili-Ardali, M., Topka, H., Lehmberg, J., Friehs, G. M., Woodtli, A., Donoghue, J. P., & Birbaumer, N. (2022). Spelling interface using intracortical signals in a completely locked-in patient enabled via auditory neurofeedback training [Number: 1 Publisher: Nature Publishing Group]. *Nature Communications*, *13*(1), 1236. https://doi.org/10.1038/s41467-022-28859-8
- Demasi, P., Szwarcfiter, J. L., & Cruz, A. J. O. (2010). A Theoretical Framework to Formalize AGI-Hard Problems [ISSN: 1951-6851], 64–65. https://doi.org/10.2991/agi.2010.14
- Gonfalonieri, A. (2019). Deep Learning Algorithms and Brain-Computer Interfaces. Retrieved May 8, 2022, from https://towardsdatascience.com/deep-learning-algorithms-and-brain-computer-interfaces-7608d0a6f01
- Martins, N. R. B., Angelica, A., Chakravarthy, K., Svidinenko, Y., Boehm, F. J., Opris, I., Lebedev, M. A., Swan, M., Garan, S. A., Rosenfeld, J. V., Hogg, T., & Freitas, R. A. (2019). Human Brain/Cloud Interface. *Frontiers in Neuroscience*, *13*, 112. https://doi.org/10.3389/fnins.2019.00112
- Minguillon, J., Lopez-Gordo, M. A., Morillas, C., & Pelayo, F. (2017). A Mobile Brain-Computer Interface for Clinical Applications: From the Lab to the Ubiquity. In J. M. Ferrández Vicente, J. R. Álvarez-Sánchez, F. de la Paz López, J. Toledo Moreo, & H. Adeli (Eds.),

- *Biomedical Applications Based on Natural and Artificial Computing* (pp. 68–76). Springer International Publishing. https://doi.org/10.1007/978-3-319-59773-7_8
- Murphy, D. P., Bai, O., Gorgey, A. S., Fox, J., Lovegreen, W. T., Burkhardt, B. W., Atri, R., Marquez, J. S., Li, Q., & Fei, D.-Y. (2017). Electroencephalogram-Based Brain-Computer Interface and Lower-Limb Prosthesis Control: A Case Study. *Frontiers in Neurology*, 8, 696. https://doi.org/10.3389/fneur.2017.00696
- Rashid, A., Suppiah, S., Hoo, F. K., & Masiran, R. (2018). Bilateral Motor Cortex Control for Left Thumb Movement: An Incidental Finding Through Functional MRI (fMRI) [Publisher: BMJ Publishing Group Section: Unexpected outcome (positive or negative) including adverse drug reactions]. *Case Reports*, 2018, bcr. https://doi.org/10.1136/bcr-2017-221129
- Vidal, J. J. (1977). Real-time detection of brain events in EEG. *Proceedings of the IEEE*. https://doi.org/10.1109/PROC.1977.10542

Appendix A

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Appendix B

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