This is just a text with beamer presentations because I want other theme colors

We want more colors

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Outline

- Single tone case
 - Maximum likelihood estimators of frequency and amplitude
 - Computing probability density functions



Estimating frequency and amplitude of a single tone

Theorem

How you have fallen from heaven, morning star, son of the dawn! You have been cast down to the earth, you who once laid low the nations!

Isaiah 14:12

Estimating frequency and amplitude of a single tone

Given a complex sinusoid defined by:

$$r(t) = A_1 e^{j2\pi f_1 t} + z(t)$$

Where z(t) is a complex Gaussian white noise with zero mean and variance σ^2 .

Givens a set of samples from r(t), how could we estimate the values of A_1 and f_1 ?

Note on Maximum Likelihood Estimation #1

- It's a method to estimate parameters of a statistical model.
- The value of the Maximum Likelihood Estimator of a parameter must make the observed data more likely.

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An example of maximum likelihood estimator: The sample mean of a set of n observations from a random variable X.

$$M_n = \frac{1}{n} \sum_{i=1}^n X_i$$

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$$\lim_{n\to\infty} M_n = \mathrm{E}\{X\}$$

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Defining the PDF of the frequency

Being N the number of samples and T_s the sampling period $1/f_s$, we have.

$$\mathbf{r} = [r(0) \quad r(T_s) \quad r(2T_s) \quad \dots \quad r((N-1)T_s)]^T$$

$$\mathbf{e_1} = [e^{j2\pi f_1 0} \quad e^{j2\pi f_1 T_s} \quad \dots \quad e^{j2\pi f_1(N-1)T_s}]^T$$

$$\mathbf{r} = A_1 \mathbf{e_1} + \mathbf{n}$$

$$p(\mathbf{r}|f_1, A_1) = \frac{1}{\pi^N \sigma^{2N}} \exp\left[-\frac{(\mathbf{r} - A_1 \mathbf{e_1})'(\mathbf{r} - A_1 \mathbf{e_1})}{\sigma^2}\right]$$

$$p(\mathbf{r}|A_1) = \int p(\mathbf{r}|f_1, A_1)p(f_1)df_1$$

$$p(f_1|\mathbf{r}, A_1) = \frac{p(\mathbf{r}|f_1, A_1)p(f_1)}{p(\mathbf{r}|A_1)}$$

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Defining the PDF of the frequency

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