



COMPUTATIONAL FINANCE & RISK MANAGEMENT

UNIVERSITY *of* WASHINGTON

Department of Applied Mathematics

Options in R

CFRM 425 (019b)

R Programming for Quantitative Finance

- Peter James
 - Option Theory (Wiley, 2003)
 - General background
 - Excellent reference book to have in your arsenal
- The fOptions R package
 - <https://www.rmetrics.org/>

- Based in Zurich
- RMetrics package – Contains fOptions and other financial R packages



- Based in Zurich
- Founded in 2007
- Financially supports
 - Summer Schools and Workshops
 - Student Internships
 - Open Source Software Development
 - Publications of eBooks
 - R Programming, R Studio, and R Shiny trainings and seminars

- fOptions: Rmetrics - Pricing and Evaluating Basic Options
- Pricing models

fOptions-package	Basic Option Valuation
BasicAmericanOptions	Valuation of Basic American Options
BinomialTreeOptions	Binomial Tree Option Model
HestonNandiGarchFit	Heston-Nandi Garch(1,1) Modelling
HestonNandiOptions	Option Price for the Heston-Nandi Garch Option Model
LowDiscrepancy	Low Discrepancy Sequences
MonteCarloOptions	Monte Carlo Valuation of Options
PlainVanillaOptions	Valuation of Plain Vanilla Options

Plain Vanilla Option

- Pricing models

<code>GBS*</code>	the generalized Black-Scholes option
<code>BlackScholesOption</code>	a synonyme for the <code>GBSOption</code>
<code>Black76Option</code>	options on Futures
<code>MiltersenSchwartzOption</code>	options on commodity futures

- View Results

<code>print</code>	<code>print</code> method for Options
<code>summary</code>	<code>summary</code> method for Options

Plain Vanilla Option

- First Example: European Call Option:

`GBSOption(TypeFlag, S, X, Time, r, b, sigma)`

`TypeFlag = "c", "p" (call/put)`

`S = Market share price`

`X = Strike price`

`Time = time to expiration, as a year fraction`

`r = risk-free interest rate`

`b = annual dividend rate`

`sigma = return volatility`

- First Example: European Call Option:

```
TypeFlag<-"c"  
S<-530.32  
X<-550  
Time<-283/365  
r<-0.02  
b<-0.05  
sigma<-0.24
```

```
res.GBS <- GBSOption(TypeFlag, S, X, Time, r, b, sigma)  
(summ <- summary(res.GBS))
```

Call:

```
GBSOption(TypeFlag = TypeFlag, S = S, X = X, Time = Time, r = r,  
          b = b, sigma = sigma)
```

Parameters:

	Value:
TypeFlag	c
S	530.32
X	550
Time	0.775342465753425
r	0.000703
b	0
sigma	0.2442

Option Price:

37.04709

Description:

Sat Feb 29 17:55:58 2020

Plain Vanilla Option

- First Example: European Call Option – We can also get results from *slots* on the return object

```
summ@price  
summ@parameters  
summ@parameters$X
```

```
> summ@price  
[1] 37.04709
```

```
> summ@parameters  
$TypeFlag  
[1] "c"
```

```
$s  
[1] 530.32
```

```
$X  
[1] 550
```

```
> summ@parameters$X  
[1] 550
```

```
$Time  
[1] 0.7753425
```

```
$r  
[1] 0.000703
```

```
$b  
[1] 0
```

```
$sigma  
[1] 0.2442
```

Plain Vanilla Option

- In addition, we can calculate the option price along with the associated “Greeks”, by calling the function **GBSCharacteristics(.)**
- Same input data as before:

```
TypeFlag<-"c"  
S<-530.32  
X<-550  
Time<-283/365  
r<-0.02  
b<-0.05  
sigma<-0.24
```
- Now:

```
chars.GBS <- GBSCharacteristics(TypeFlag, S, X, Time, r, b, sigma)  
class(chars.GBS) # list  
names(chars.GBS) # "premium" "delta" "theta" "vega" "rho" "lambda" "gamma"  
# Note: lambda is the same thing as vega
```

```
(resultset <- c(chars.GBS$premium, chars.GBS$delta, chars.GBS$theta,  
               chars.GBS$vega, chars.GBS$rho, chars.GBS$lambda, chars.GBS$gamma))  
# 46.258450018 0.559305500 -43.216176904 189.382574311 194.108880452 6.412036998 0.003618755
```

Black-Scholes Closed Form: European Options

- Let's look at a series of put options
 - Just before expiration
 - Three months to expiration
 - Series of underlying prices

```
TypeFlag<-"p"
SVec <- seq(from = 45, to = 55, by = 1)
X<-50
Time <- 0.001/365 # very close to the bell
r<-0.01
b<-0.0 # No dividend
sigma<-0.25

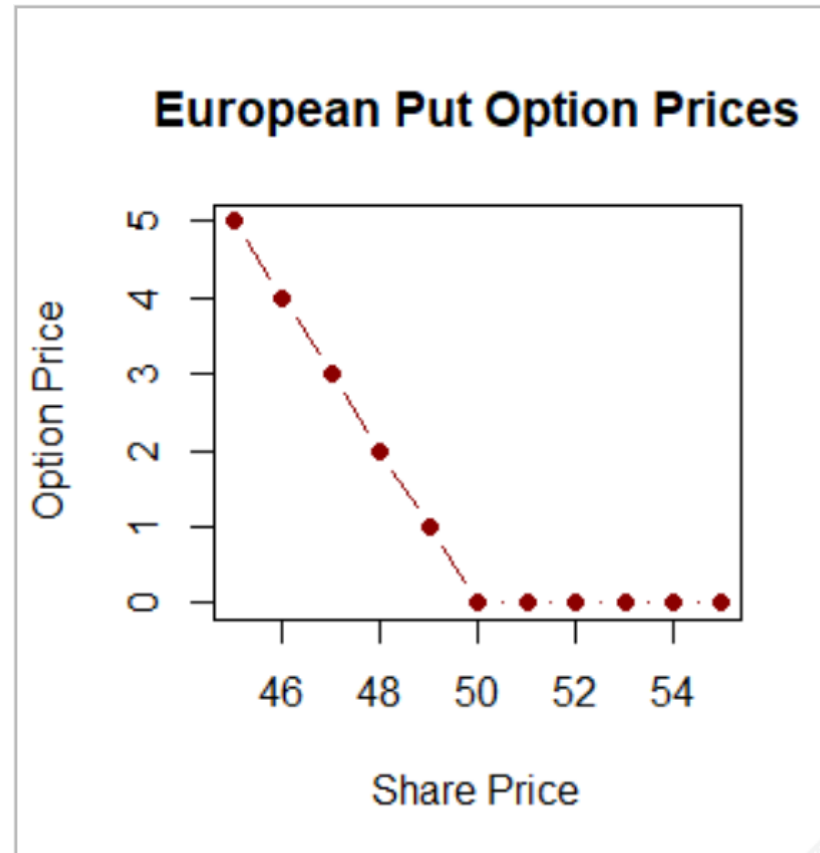
puts.GBS.Maturity <- GBSOption(TypeFlag, SVec, X, Time, r, b, sigma)
summPuts.Mat <- summary(puts.GBS.Maturity)
matPrices <- summPuts.Mat@price

> matPrices
[1] 4.999999986 3.999999989 2.999999992 1.999999995
[5] 0.999999997 0.00825428 0.000000000 0.000000000
[9] 0.000000000 0.000000000 0.000000000
```

Black-Scholes Closed Form: European Options

- Now, let's look at a plot

```
plot(x = SVec, y = matPrices, type = "b", col = 'darkred',  
     main = 'European Put Option Prices Close to Mty',  
     xlab = 'Strike Price', ylab = 'Option Price', lwd = 1.5, pch = 16)
```



- Note that the option prices are equal to the intrinsic values
- Time value is essentially zero

Black-Scholes Closed Form: European Options

- Next, let's look at option prices at three months to expiration

- All other parameters remain the same

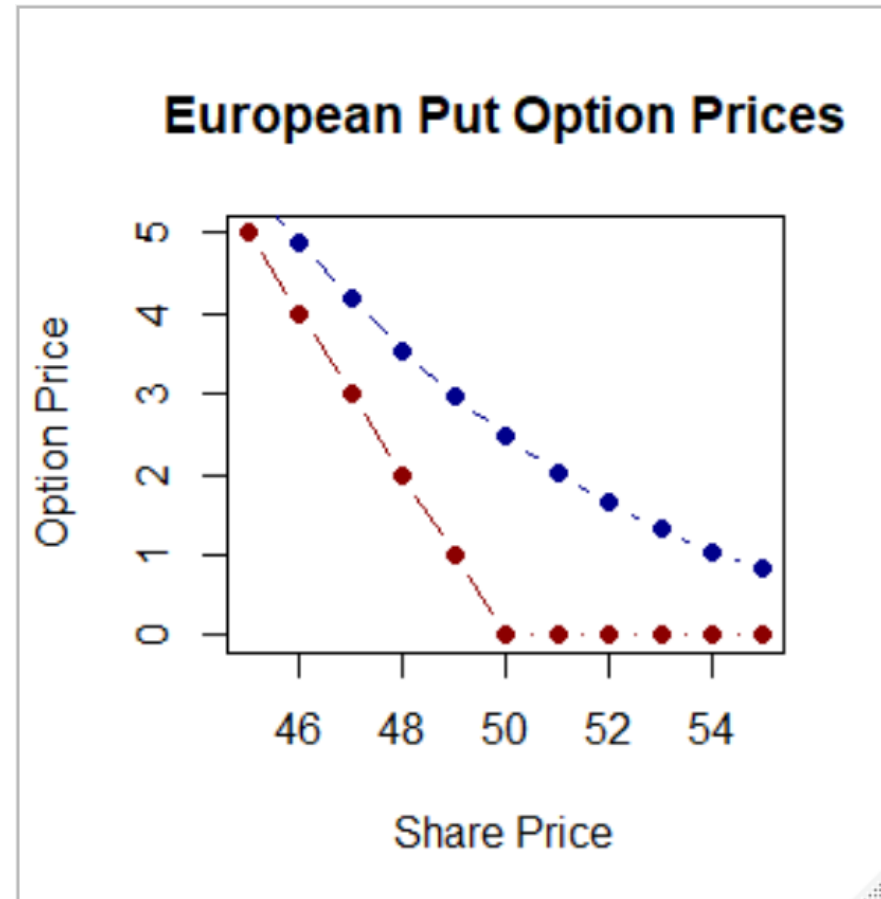
```
Time <- 90/365
```

```
puts.GBS.3M <- GBSOption(TypeFlag, SVec, X, Time, r, b, sigma)
```

```
summPuts.3M <- summary(puts.GBS.3M)
```

```
threeMthPrices <- summPuts.3M@price
```

- Now, overlay these results on the previous plot
- Time value is now positive
- Adds to intrinsic value
- Higher option prices



- Recall: American options may be exercised anytime up to and including the contract expiration date
- In fOptions, we will use the following:
 - Barone-Adesi & Whaley (1987): Closed form approximation
 - https://deriscope.com/docs/Barone_Adesi_Whaley_1987.pdf
 - Bjerk Sund and Stensland (2002): Closed form approximation
 - <https://core.ac.uk/download/pdf/30824897.pdf>
 - Jarrow-Rudd Binomial Tree: Numerical approximation
 - See the James book
- Time-permitting, we will look at Monte Carlo pricing outside of fOptions – maybe roll your own

American Options

- Example 1: Price a single American option (Barone-Adesi & Whaley):

```
# Quick single option contract example:
```

```
TypeFlag<-"p"
```

```
X<-50
```

```
r<-0.01
```

```
b<-0.0      # No dividend
```

```
sigma<-0.25
```

```
put.BAW <- BAWAmericanApproxOption(TypeFlag, S = 55,  
                                     X, Time = 90/365, r, b, sigma)
```

```
put.BAW@price
```

```
# Option price = 0.8253149
```

```
class(put.BAW) # foptions
```


- Example 2: Same input data with same vector (as before) of underlying equity prices `sVec` (Barone-Adesi & Whaley):

```
puts.BAW.3M <- BAWAmericanApproxOption(TypeFlag, S = sVec,  
                                         X, Time = 90/365, r, b, sigma)  
  
summBAW <- summary(puts.BAW.3M)  
(BAW.Prices <- summBAW@price)
```

- Result:

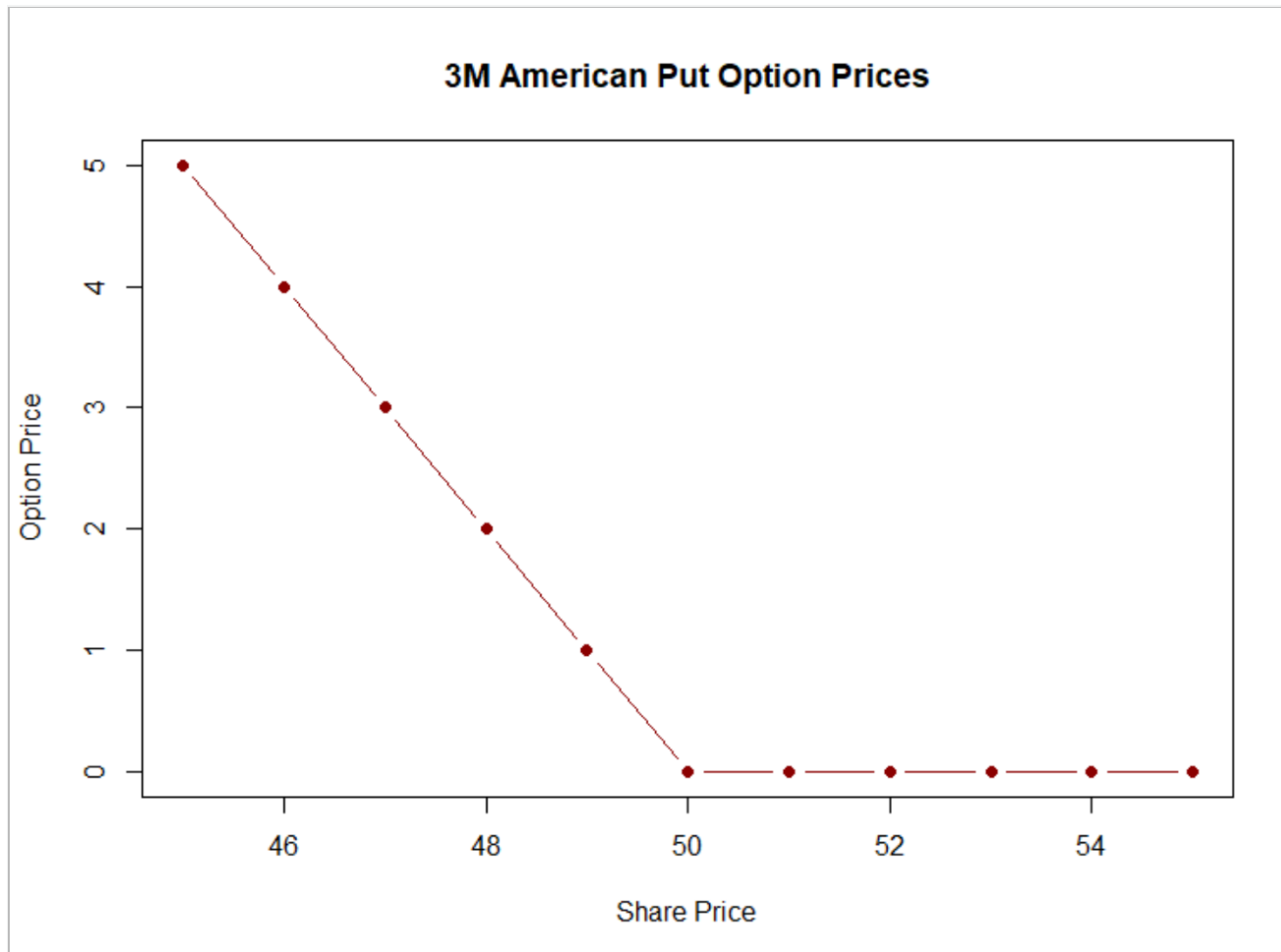
```
[1] 5.6368572 4.8811371 4.1832868 3.5473923 2.9758651 2.4693538 2.0267202  
[8] 1.6453608 1.3213433 1.0498102 0.8253149
```

- Next, let's plot this against the intrinsic values only at expiration

American Options

- Intrinsic values (from the European case):

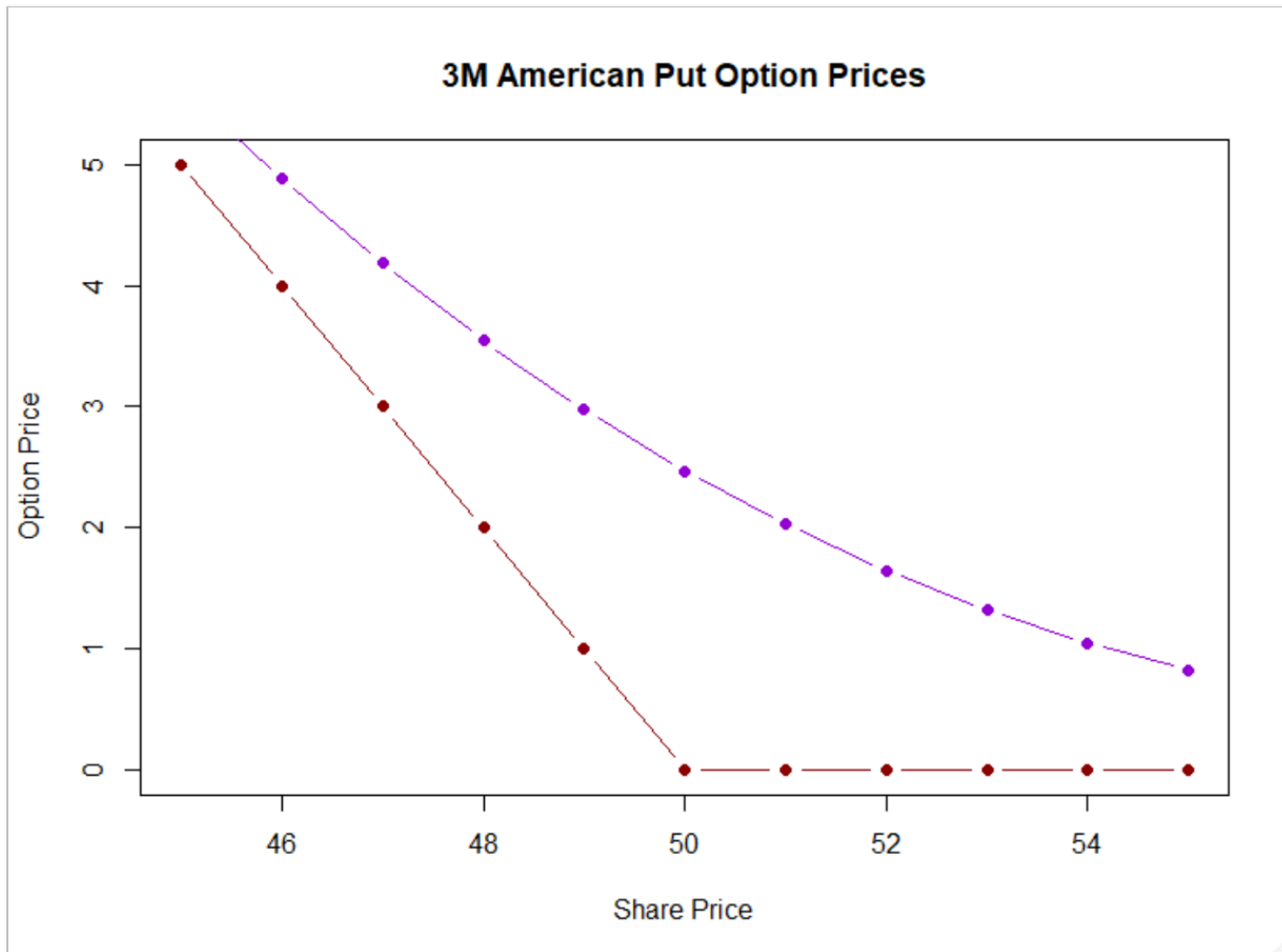
```
# Put intrinsic value plot again first:  
plot(x = SVec, y = matPrices, type = "b", col = 'darkred',  
     main = '3M American Put Option Prices',  
     xlab = 'Share Price', ylab = 'Option Price', lwd = 1.5, pch = 16)
```



American Options

- Overlay the BAW American option prices

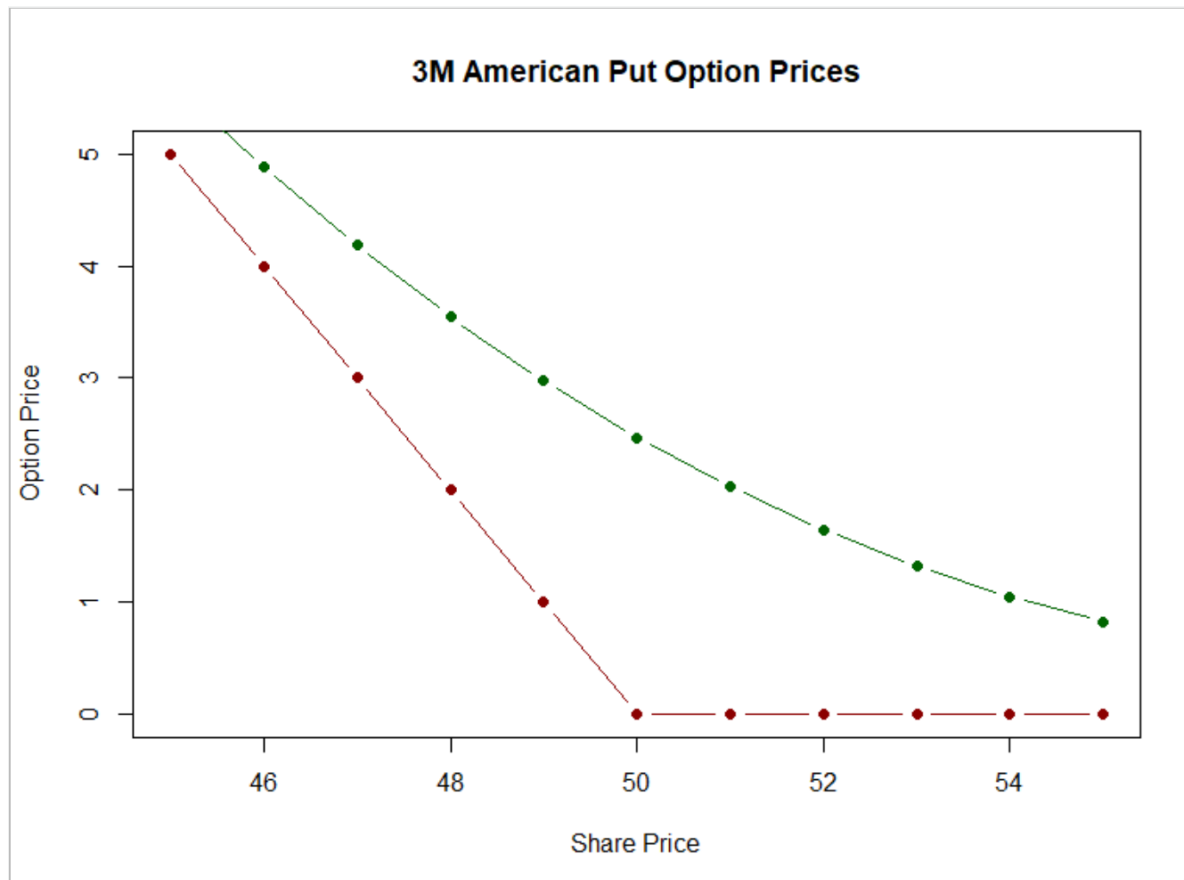
```
lines(x = SVec, y = BAW.Prices, type = "b", col = 'darkviolet',  
      lwd = 1.5, pch = 16)
```



American Options

- Let's do the same with the Bjersund and Stensland Approximation:

```
puts.BjSt.3M <- BSAmericanApproxOption(TypeFlag, S = SVec, X,  
                                         Time, r, b, sigma)  
  
summBjSt <- summary(puts.BjSt.3M)  
BjSt.Prices <- summBjSt@price  
  
lines(x = SVec, y = BjSt.Prices, type = "b", col = 'darkgreen',  
      lwd = 1.5, pch = 16)
```



American Options

- Finally, with the Binomial Tree approximation: Chop the timeline into 100 increments of length Δt
- As we can't vectorize this model with the vector of equity prices, use a loop

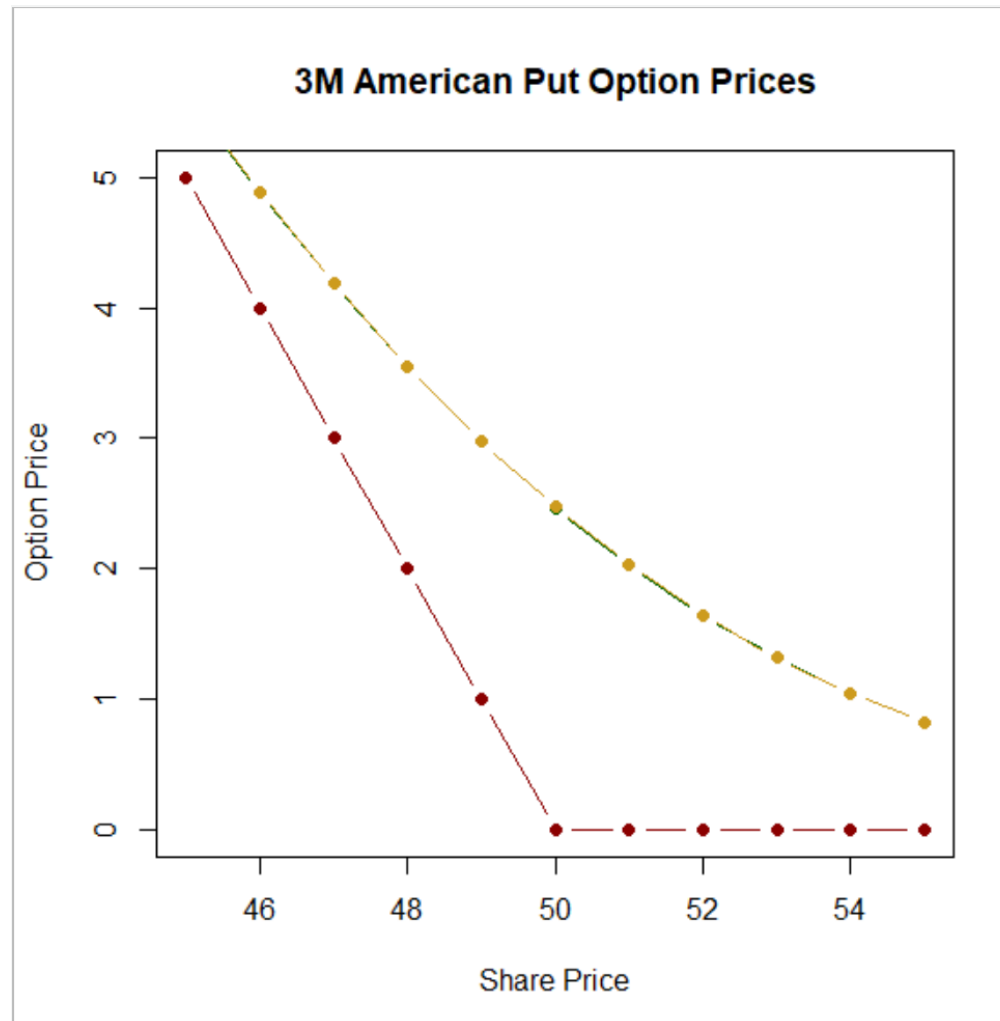
```
v <- vector("double", 0L)
for(s in SVec)
{
  put.JR <- JRBinoomialTreeOption(TypeFlag = "pa", S = s, X,
                                   Time, r, b, sigma, n = 100, title = "American 3M Puts",
                                   description = "Varying Equity Prices")

  v <- c(v, put.JR@price)
}
```

American Options

- Binomial Tree approximation (continued): Overlay the vector of option prices at each underlying share price

```
lines(x = sVec, y = v, type = "b", col = 'goldenrod3',  
      lwd = 1.5, pch = 16)
```



- [END]