

Programming parallel computers: Exercise 2

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1 CP1

Finding the colleration matrix using naive algorithm.

| | ny | nx | time(sec) |
|----|------|------|-----------|
| cp | 1 | 1 | 0.000 |
| cp | 1 | 10 | 0.000 |
| cp | 1 | 100 | 0.000 |
| cp | 1 | 1000 | 0.000 |
| cp | 1 | 2000 | 0.000 |
| cp | 1 | 4000 | 0.000 |
| cp | 10 | 1 | 0.000 |
| cp | 10 | 10 | 0.000 |
| cp | 10 | 100 | 0.000 |
| cp | 10 | 1000 | 0.000 |
| cp | 10 | 2000 | 0.000 |
| cp | 10 | 4000 | 0.001 |
| cp | 100 | 1 | 0.000 |
| cp | 100 | 10 | 0.000 |
| cp | 100 | 100 | 0.001 |
| cp | 100 | 1000 | 0.010 |
| cp | 100 | 2000 | 0.017 |
| cp | 100 | 4000 | 0.018 |
| cp | 1000 | 1 | 0.001 |
| cp | 1000 | 10 | 0.004 |
| cp | 1000 | 100 | 0.037 |
| cp | 1000 | 1000 | 0.406 |
| cp | 1000 | 2000 | 0.820 |
| cp | 1000 | 4000 | 1.659 |
| cp | 2000 | 1 | 0.002 |
| cp | 2000 | 10 | 0.016 |
| cp | 2000 | 100 | 0.147 |
| cp | 2000 | 1000 | 1.622 |
| cp | 2000 | 2000 | 3.304 |
| cp | 2000 | 4000 | 6.641 |
| cp | 4000 | 1 | 0.009 |
| cp | 4000 | 10 | 0.065 |
| cp | 4000 | 100 | 0.588 |
| cp | 4000 | 1000 | 6.545 |
| cp | 4000 | 2000 | 13.269 |
| cp | 4000 | 4000 | 26.612 |

2 CP2

cp2 is parallelised version of cp1.

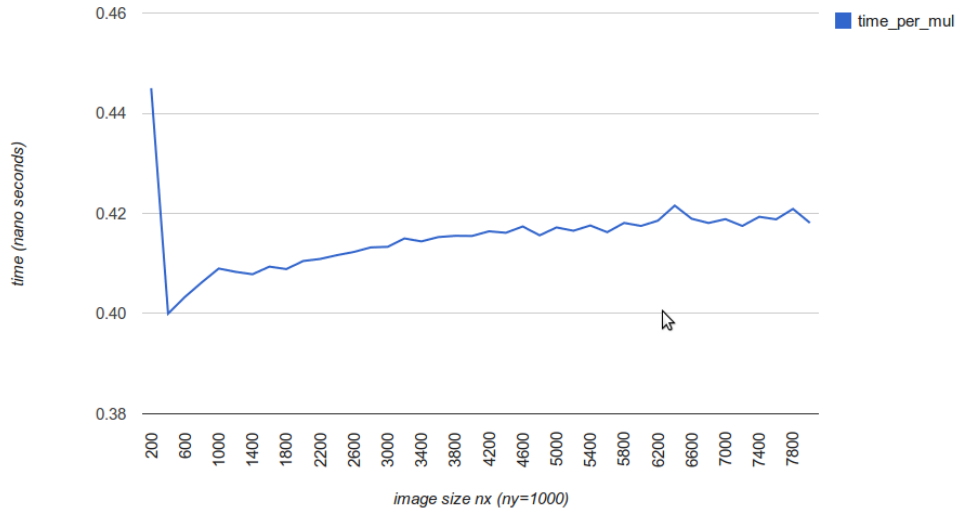


Figure 1: Time taken per multiplication cp1 with ny=1000

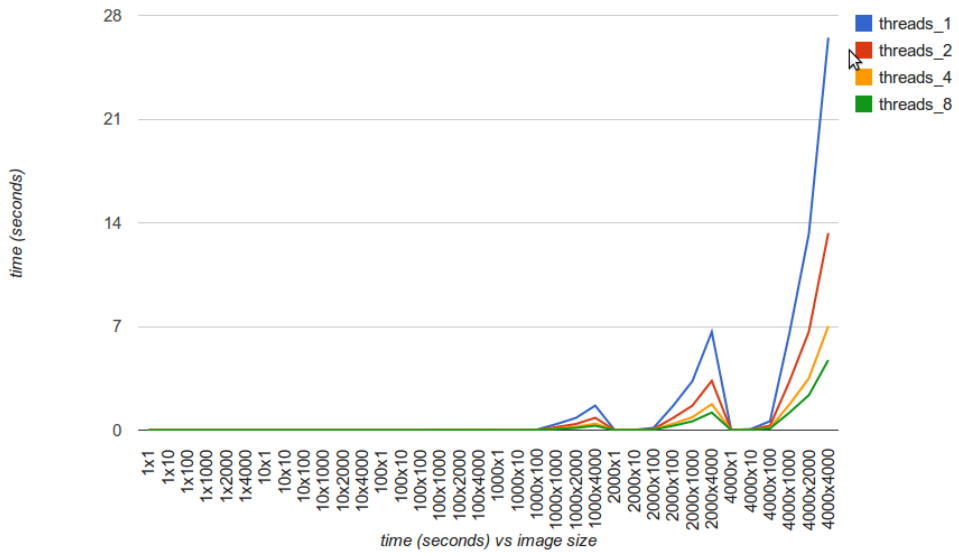


Figure 2: Performance statistics of cp2

| | ny | nx | 1-thread | 2 -threads | 4-threads | 8-threads |
|----|------|------|----------|------------|-----------|-----------|
| cp | 1 | 1 | 0 | 0 | 0 | 0 |
| cp | 1 | 10 | 0 | 0 | 0 | 0 |
| cp | 1 | 100 | 0 | 0 | 0 | 0 |
| cp | 1 | 1000 | 0 | 0 | 0 | 0 |
| cp | 1 | 2000 | 0 | 0 | 0 | 0 |
| cp | 1 | 4000 | 0 | 0 | 0 | 0 |
| cp | 10 | 1 | 0 | 0 | 0 | 0 |
| cp | 10 | 10 | 0 | 0 | 0 | 0 |
| cp | 10 | 100 | 0 | 0 | 0 | 0 |
| cp | 10 | 1000 | 0 | 0 | 0 | 0 |
| cp | 10 | 2000 | 0 | 0 | 0 | 0 |
| cp | 10 | 4000 | 0.001 | 0 | 0 | 0 |
| cp | 100 | 1 | 0 | 0 | 0 | 0 |
| cp | 100 | 10 | 0 | 0 | 0 | 0 |
| cp | 100 | 100 | 0.001 | 0.001 | 0 | 0 |
| cp | 100 | 1000 | 0.01 | 0.005 | 0.003 | 0.002 |
| cp | 100 | 2000 | 0.017 | 0.01 | 0.005 | 0.004 |
| cp | 100 | 4000 | 0.018 | 0.012 | 0.011 | 0.007 |
| cp | 1000 | 1 | 0.001 | 0 | 0 | 0 |
| cp | 1000 | 10 | 0.004 | 0.002 | 0.001 | 0.001 |
| cp | 1000 | 100 | 0.04 | 0.019 | 0.011 | 0.009 |
| cp | 1000 | 1000 | 0.408 | 0.205 | 0.108 | 0.074 |
| cp | 1000 | 2000 | 0.821 | 0.412 | 0.218 | 0.148 |
| cp | 1000 | 4000 | 1.656 | 0.832 | 0.439 | 0.296 |
| cp | 2000 | 1 | 0.003 | 0.002 | 0.001 | 0.001 |
| cp | 2000 | 10 | 0.017 | 0.009 | 0.005 | 0.003 |
| cp | 2000 | 100 | 0.152 | 0.076 | 0.041 | 0.029 |
| cp | 2000 | 1000 | 1.627 | 0.818 | 0.431 | 0.292 |
| cp | 2000 | 2000 | 3.303 | 1.652 | 0.873 | 0.596 |
| cp | 2000 | 4000 | 6.627 | 3.329 | 1.752 | 1.185 |
| cp | 4000 | 1 | 0.011 | 0.006 | 0.004 | 0.004 |
| cp | 4000 | 10 | 0.068 | 0.034 | 0.018 | 0.012 |
| cp | 4000 | 100 | 0.604 | 0.304 | 0.161 | 0.116 |
| cp | 4000 | 1000 | 6.553 | 3.293 | 1.732 | 1.187 |
| cp | 4000 | 2000 | 13.265 | 6.65 | 3.5 | 2.363 |
| cp | 4000 | 4000 | 26.498 | 13.307 | 7.017 | 4.731 |

Table 1: CP2 performance statistics

| | ny | nx | 1-thread | 2-threads | 4-threads | 8-threads |
|----|------|------|----------|-----------|-----------|-----------|
| cp | 1 | 1 | 0 | 0 | 0 | 0 |
| cp | 1 | 10 | 0 | 0 | 0 | 0 |
| cp | 1 | 100 | 0 | 0 | 0 | 0 |
| cp | 1 | 1000 | 0 | 0 | 0 | 0 |
| cp | 1 | 2000 | 0 | 0 | 0 | 0 |
| cp | 1 | 4000 | 0 | 0 | 0 | 0 |
| cp | 10 | 1 | 0 | 0 | 0 | 0 |
| cp | 10 | 10 | 0 | 0 | 0 | 0 |
| cp | 10 | 100 | 0 | 0 | 0 | 0 |
| cp | 10 | 1000 | 0 | 0 | 0 | 0 |
| cp | 10 | 2000 | 0 | 0 | 0 | 0 |
| cp | 10 | 4000 | 0 | 0 | 0 | 0 |
| cp | 100 | 1 | 0 | 0 | 0 | 0 |
| cp | 100 | 10 | 0 | 0 | 0 | 0 |
| cp | 100 | 100 | 0 | 0 | 0 | 0 |
| cp | 100 | 1000 | 0.002 | 0.001 | 0.001 | 0.001 |
| cp | 100 | 2000 | 0.005 | 0.003 | 0.002 | 0.002 |
| cp | 100 | 4000 | 0.008 | 0.006 | 0.004 | 0.004 |
| cp | 1000 | 1 | 0.003 | 0.004 | 0.002 | 0.002 |
| cp | 1000 | 10 | 0.004 | 0.004 | 0.002 | 0.002 |
| cp | 1000 | 100 | 0.01 | 0.011 | 0.006 | 0.006 |
| cp | 1000 | 1000 | 0.085 | 0.044 | 0.024 | 0.023 |
| cp | 1000 | 2000 | 0.178 | 0.093 | 0.053 | 0.043 |
| cp | 1000 | 4000 | 0.42 | 0.235 | 0.131 | 0.121 |
| cp | 2000 | 1 | 0.013 | 0.006 | 0.004 | 0.003 |
| cp | 2000 | 10 | 0.014 | 0.007 | 0.004 | 0.004 |
| cp | 2000 | 100 | 0.04 | 0.02 | 0.011 | 0.011 |
| cp | 2000 | 1000 | 0.357 | 0.184 | 0.1 | 0.077 |
| cp | 2000 | 2000 | 0.857 | 0.486 | 0.25 | 0.179 |
| cp | 2000 | 4000 | 1.881 | 0.96 | 0.542 | 0.438 |
| cp | 4000 | 1 | 0.05 | 0.026 | 0.013 | 0.012 |
| cp | 4000 | 10 | 0.056 | 0.028 | 0.015 | 0.014 |
| cp | 4000 | 100 | 0.158 | 0.08 | 0.043 | 0.044 |
| cp | 4000 | 1000 | 1.655 | 0.9 | 0.5 | 0.351 |
| cp | 4000 | 2000 | 3.56 | 2.21 | 1.053 | 0.723 |
| cp | 4000 | 4000 | 7.644 | 4.924 | 2.142 | 1.751 |

Table 2: CP3 performance statistics

3 CP3

cp3 is vectorised version. The data matrix is converted into vector of float8_t and the all the calculations are dont using vectors.

4 CP4

cp4 is vector multiplication with cache block multiplication with instruction level parallelism. Performance of cp4 with 4 threads is better than 8 threads.

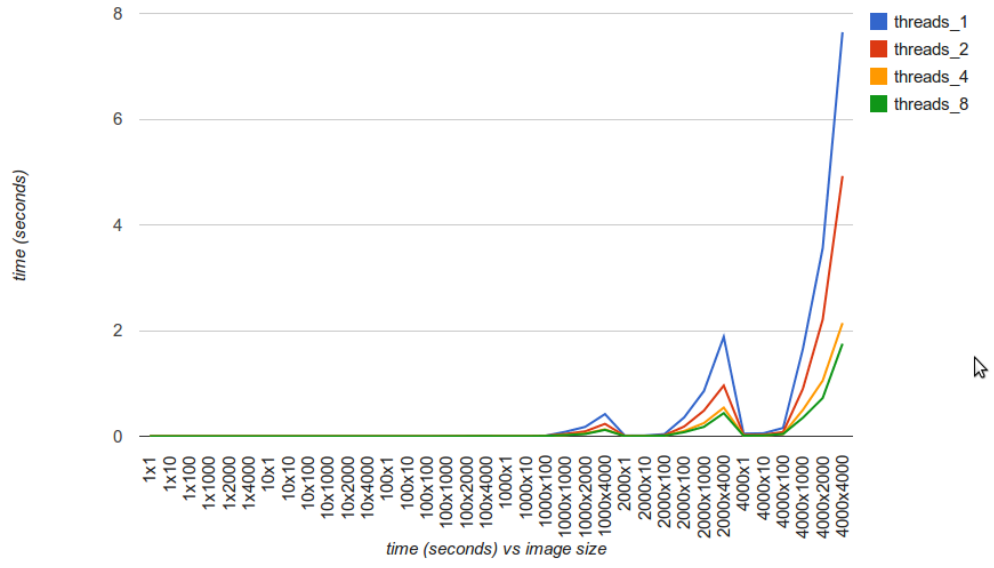


Figure 3: Performance statistics of cp3

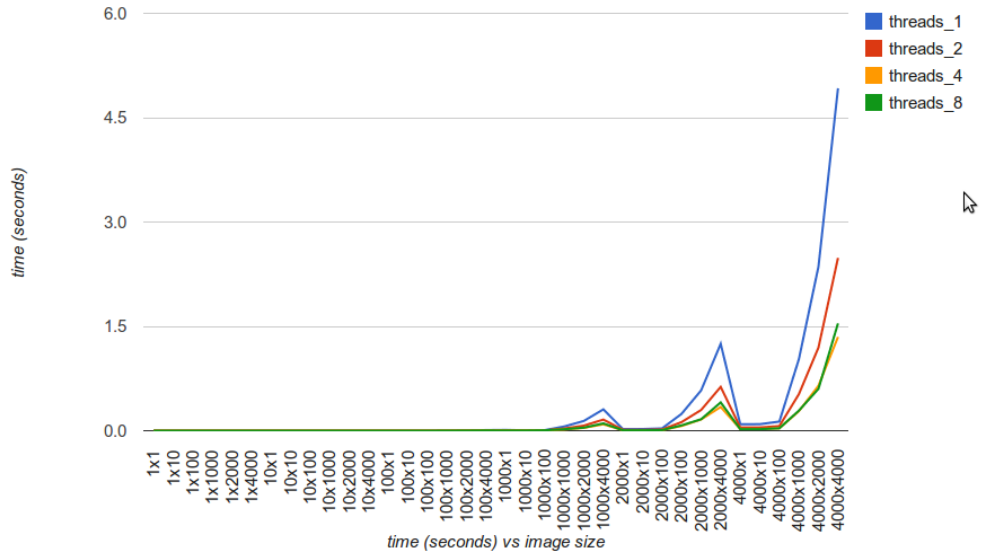


Figure 4: Performance statistics of cp4

| | ny | nx | 1-thread | 2-threads | 4-threads | 8-threads |
|----|------|------|----------|-----------|-----------|-----------|
| cp | 1 | 1 | 0 | 0 | 0 | 0 |
| cp | 1 | 10 | 0 | 0 | 0 | 0 |
| cp | 1 | 100 | 0 | 0 | 0 | 0 |
| cp | 1 | 1000 | 0 | 0 | 0 | 0 |
| cp | 1 | 2000 | 0 | 0 | 0 | 0 |
| cp | 1 | 4000 | 0 | 0 | 0 | 0 |
| cp | 10 | 1 | 0 | 0 | 0 | 0 |
| cp | 10 | 10 | 0 | 0 | 0 | 0 |
| cp | 10 | 100 | 0 | 0 | 0 | 0 |
| cp | 10 | 1000 | 0 | 0 | 0 | 0 |
| cp | 10 | 2000 | 0 | 0 | 0 | 0 |
| cp | 10 | 4000 | 0 | 0 | 0 | 0 |
| cp | 100 | 1 | 0 | 0 | 0 | 0 |
| cp | 100 | 10 | 0 | 0 | 0 | 0 |
| cp | 100 | 100 | 0 | 0 | 0 | 0 |
| cp | 100 | 1000 | 0.002 | 0.001 | 0.001 | 0.001 |
| cp | 100 | 2000 | 0.004 | 0.003 | 0.002 | 0.002 |
| cp | 100 | 4000 | 0.009 | 0.006 | 0.004 | 0.004 |
| cp | 1000 | 1 | 0.011 | 0.007 | 0.004 | 0.003 |
| cp | 1000 | 10 | 0.006 | 0.003 | 0.004 | 0.003 |
| cp | 1000 | 100 | 0.008 | 0.004 | 0.006 | 0.006 |
| cp | 1000 | 1000 | 0.061 | 0.032 | 0.018 | 0.021 |
| cp | 1000 | 2000 | 0.14 | 0.073 | 0.041 | 0.044 |
| cp | 1000 | 4000 | 0.307 | 0.16 | 0.092 | 0.105 |
| cp | 2000 | 1 | 0.023 | 0.013 | 0.007 | 0.006 |
| cp | 2000 | 10 | 0.024 | 0.012 | 0.007 | 0.006 |
| cp | 2000 | 100 | 0.033 | 0.017 | 0.01 | 0.009 |
| cp | 2000 | 1000 | 0.243 | 0.124 | 0.068 | 0.077 |
| cp | 2000 | 2000 | 0.58 | 0.298 | 0.162 | 0.165 |
| cp | 2000 | 4000 | 1.249 | 0.63 | 0.341 | 0.407 |
| cp | 4000 | 1 | 0.093 | 0.047 | 0.025 | 0.022 |
| cp | 4000 | 10 | 0.094 | 0.047 | 0.025 | 0.022 |
| cp | 4000 | 100 | 0.131 | 0.066 | 0.035 | 0.035 |
| cp | 4000 | 1000 | 1.029 | 0.526 | 0.281 | 0.289 |
| cp | 4000 | 2000 | 2.358 | 1.195 | 0.647 | 0.602 |
| cp | 4000 | 4000 | 4.923 | 2.484 | 1.347 | 1.543 |

Table 3: CP4 performance statistics

| ny | nx | time_cp1 | time_cp4.8 | time_cp4.4 | time_cp4.2 | time_cp4.1 |
|------|------|----------|------------|------------|------------|------------|
| 1000 | 200 | 0.089 | 0.009 | 0.009 | 0.013 | 0.014 |
| 1000 | 400 | 0.16 | 0.008 | 0.007 | 0.012 | 0.023 |
| 1000 | 600 | 0.242 | 0.013 | 0.01 | 0.017 | 0.032 |
| 1000 | 800 | 0.325 | 0.017 | 0.015 | 0.026 | 0.049 |
| 1000 | 1000 | 0.409 | 0.021 | 0.018 | 0.032 | 0.061 |
| 1000 | 1200 | 0.49 | 0.025 | 0.024 | 0.042 | 0.081 |
| 1000 | 1400 | 0.571 | 0.031 | 0.028 | 0.05 | 0.095 |
| 1000 | 1600 | 0.655 | 0.034 | 0.032 | 0.057 | 0.109 |
| 1000 | 1800 | 0.736 | 0.04 | 0.038 | 0.068 | 0.129 |
| 1000 | 2000 | 0.821 | 0.043 | 0.041 | 0.073 | 0.141 |
| 1000 | 2200 | 0.904 | 0.053 | 0.046 | 0.084 | 0.161 |
| 1000 | 2400 | 0.988 | 0.06 | 0.05 | 0.091 | 0.174 |
| 1000 | 2600 | 1.072 | 0.07 | 0.055 | 0.099 | 0.191 |
| 1000 | 2800 | 1.157 | 0.072 | 0.059 | 0.108 | 0.207 |
| 1000 | 3000 | 1.24 | 0.077 | 0.063 | 0.116 | 0.222 |
| 1000 | 3200 | 1.328 | 0.082 | 0.068 | 0.124 | 0.242 |
| 1000 | 3400 | 1.409 | 0.089 | 0.074 | 0.136 | 0.259 |
| 1000 | 3600 | 1.495 | 0.094 | 0.079 | 0.145 | 0.284 |
| 1000 | 3800 | 1.579 | 0.099 | 0.083 | 0.153 | 0.292 |
| 1000 | 4000 | 1.662 | 0.104 | 0.088 | 0.163 | 0.321 |
| 1000 | 4200 | 1.749 | 0.112 | 0.097 | 0.18 | 0.347 |
| 1000 | 4400 | 1.831 | 0.115 | 0.108 | 0.201 | 0.392 |
| 1000 | 4600 | 1.92 | 0.121 | 0.116 | 0.217 | 0.416 |
| 1000 | 4800 | 1.995 | 0.126 | 0.126 | 0.239 | 0.45 |
| 1000 | 5000 | 2.086 | 0.133 | 0.135 | 0.256 | 0.498 |
| 1000 | 5200 | 2.166 | 0.139 | 0.14 | 0.268 | 0.501 |
| 1000 | 5400 | 2.255 | 0.144 | 0.145 | 0.278 | 0.53 |
| 1000 | 5600 | 2.331 | 0.149 | 0.151 | 0.291 | 0.542 |
| 1000 | 5800 | 2.425 | 0.155 | 0.156 | 0.3 | 0.582 |
| 1000 | 6000 | 2.505 | 0.161 | 0.161 | 0.309 | 0.58 |
| 1000 | 6200 | 2.595 | 0.165 | 0.167 | 0.319 | 0.601 |
| 1000 | 6400 | 2.698 | 0.171 | 0.172 | 0.33 | 0.624 |
| 1000 | 6600 | 2.765 | 0.177 | 0.18 | 0.346 | 0.649 |
| 1000 | 6800 | 2.843 | 0.184 | 0.185 | 0.356 | 0.669 |
| 1000 | 7000 | 2.932 | 0.189 | 0.191 | 0.364 | 0.686 |
| 1000 | 7200 | 3.006 | 0.193 | 0.196 | 0.378 | 0.71 |
| 1000 | 7400 | 3.103 | 0.2 | 0.202 | 0.387 | 0.726 |
| 1000 | 7600 | 3.183 | 0.204 | 0.207 | 0.396 | 0.748 |
| 1000 | 7800 | 3.283 | 0.21 | 0.213 | 0.407 | 0.765 |
| 1000 | 8000 | 3.345 | 0.215 | 0.219 | 0.421 | 0.789 |

Table 4: Performance measurements of cp1 and cp4 with ny=1000

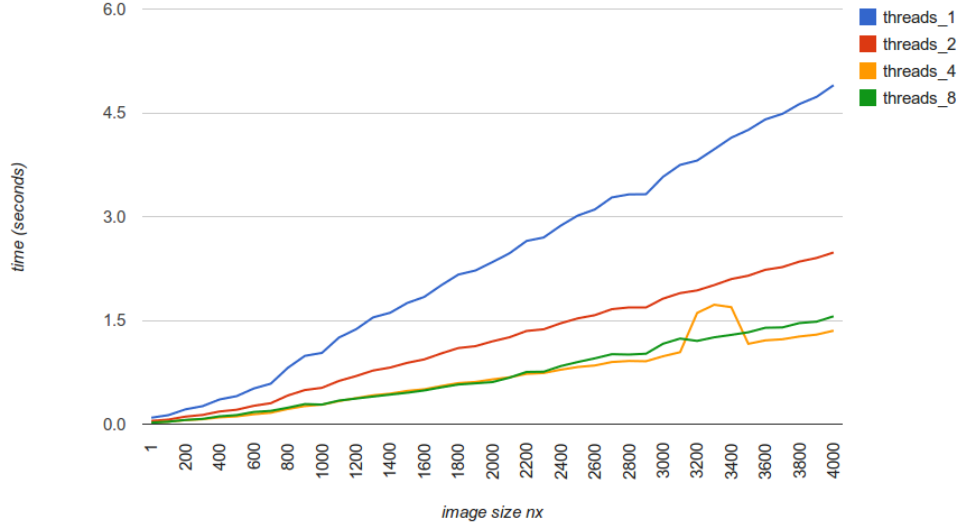


Figure 5: Performance statistics of cp4 with $n_y=4000$

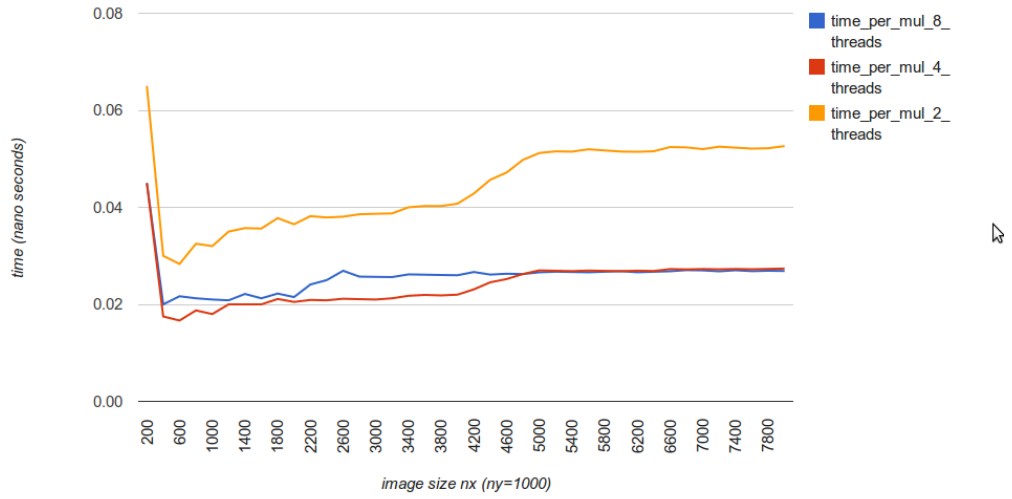


Figure 6: Time per multiplication cp4 with $n_y=1000$