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S631 HW1

1.  $X$  is a random variable.  $S = \{\text{set of all UN members}\}$  and  $X: S \rightarrow \mathbb{R}$  as a function that assigns to each country its corresponding female life expectancy in years (rounded to the nearest integer);  $z$

$s \in S$ , Let  $x$  be a number, the sets  $\{s \in S, X(s) = x\}$  another set  $\{s \in S, X(s) \leq x\}$  (set of all UN members whose female life expectancy in years less than or equal to  $x$ )

The probability for all possible sets exists, therefore,  $X$  is a random variable

2. a)  $\{s \in S, X(s) \leq 80\}$

b)  $\{s \in S, X(s) = 75\}$

c)  $\{s \in S, 65 \leq X(s) \leq 70\}$

3. Let  $F$  be a function,  $F: \Omega \rightarrow [0, 1]$

a)  $F(80) = P(\{s \in S, X(s) \leq 80\})$

b)  $P(x=75) = F(75) - F(74)$

c)  $P(65 \leq x \leq 70) = F(70) - F(64)$

4.

```
> library(alr4)
```

```
> head(UN11)
```

	region	group	fertility	ppgdp	lifeExpF	pctUrban
Afghanistan	Asia	other	5.968	499.0	49.49	23
Albania	Europe	other	1.525	3677.2	80.40	53
Algeria	Africa	africa	2.142	4473.0	75.00	67
Angola	Africa	africa	5.135	4321.9	53.17	59
Anguilla	Caribbean	other	2.000	13750.1	81.10	100
Argentina	Latin Amer	other	2.172	9162.1	79.89	93

```
> lifeexp = UN11$lifeExpF
```

```
> head(lifeexp)
```

```
[1] 49.49 80.40 75.00 53.17 81.10 79.89
```

```
> lifeexp.r = round(lifeexp, 0)
```

```
> all=length(lifeexp.r)
```

```
> all
```

```
[1] 199
```

```
> p1=length(which(lifeexp.r<=80))
```

```
> p1
```

```
[1] 157
```

```
> p2=length(which(lifeexp.r==75))
```

```
> p2
```

```
[1] 12
```

```
> p3.1=length(which(lifeexp.r<=69))
```

```
> p3.1
```

```
[1] 60
```

```
> p3.2=length(which(lifeexp.r<=65))
```

```
> p3.2
```

```
[1] 49
```

```
> p3=p3.1-p3.2
```

```
> p3
```

```
[1] 11
```

```
> P1=p1/all
```

```
> P2=p2/all
```

```
> P3=p3/all
```

```
> P1
```

```
[1] 0.7889447
```

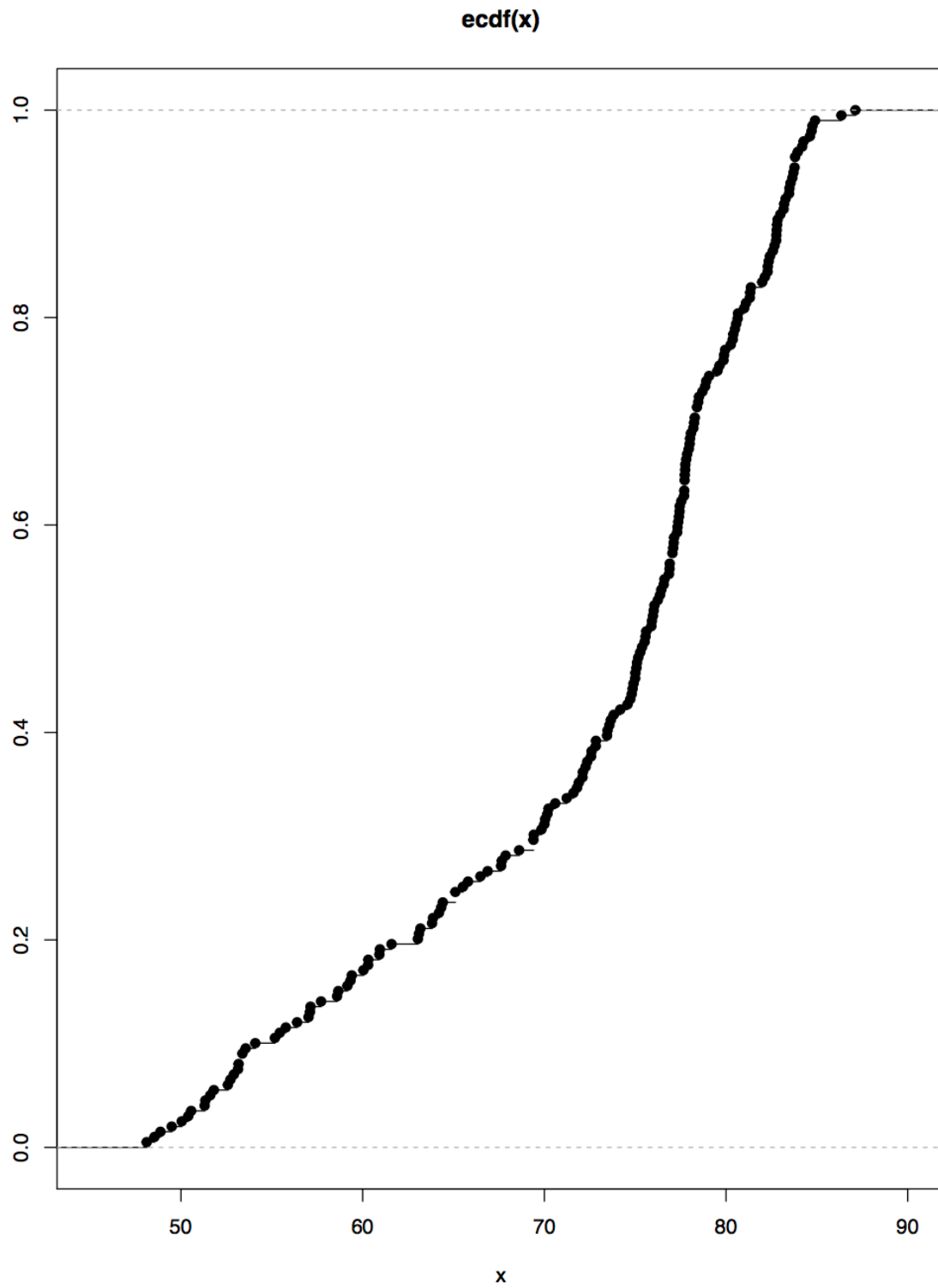
```
> P2
```

```
[1] 0.06030151
```

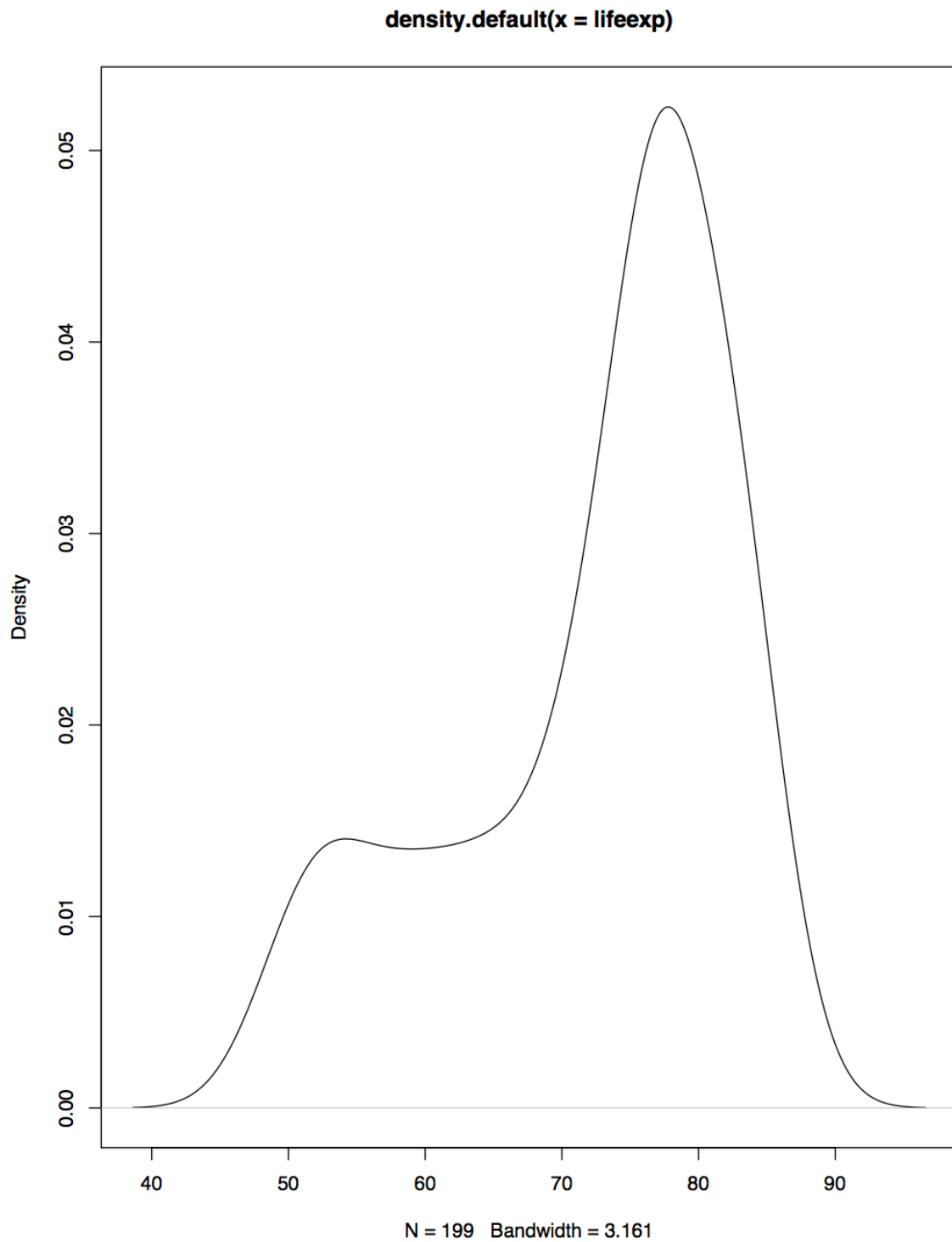
```
> P3
```

```
[1] 0.05527638
```

5. `> plot.ecdf(lifeexp)`



```
> plot(density(lifeexp))
```



Based on the graphs, the variable does not seem to follow a normal distribution since the curve under `density.default(x=lifexp)` does not fall as a bell-shaped curve and it is more like a skewed left shape (left-skewed distribution).